Photoproduction of a  $\pi \rho_T$  pair with a large invariant mass and Transversity Generalized Parton Distribution

Lech Szymanowski

Soltan Institute for Nuclear Studies Warsaw, Poland

Workshop on Exclusive Reactions at High Momentum Transfer, JLab, May, 18-21, 2010

Phys. Lett. B 688 (2010) 154 [arXiv:1001.4491]

in collaboration with

M. E. Beiyad (CPhT, Palaiseau and LPT, Orsay), B. Pire (CPhT, Palaiseau),

M. Segond (Leipzig) and S. Wallon (LPT, Orsay)

## Transversity of the nucleon using hard processes

#### What is transversity?

• Transverse spin content of the proton:



• Observable sensible to helicity flip thus give access to transversity  $\Delta_T q(x)$ . Very poorly known



- For massless (anti)particles, chirality = (-)helicity
- Transversity is thus a chiral-odd quantity
- Since QCD and QED are chiral even, the chiral odd quantities which one want to measure should appear in pairs

Jac.

# Transversity of the nucleon using hard processes: using a two body final state process?

#### How to get access to transversity?

- the dominant DA of  $\rho_T$  is of twist 2 and chiral odd ( $[\gamma^{\mu}, \gamma^{\nu}]$  coupling)
- unfortunately  $\gamma^* N^{\uparrow} \rightarrow \rho_T N' = 0$ 
  - this is true at any order, because this would require a transfer of helicity of 2 from photon: impossible!

 $\mathcal{O} \mathcal{Q} \mathcal{O}$ 

Iowest order diagrammatic argument:



# Transversity of the nucleon using hard processes: using a two body final state process?

#### Can one circumvent this vanishing?

- this vanishing is true only a twist 2
- at twist 3 this process does not vanish
- however processes involving twist 3 DAs may face problems with factorization (end-point singularities)
- the problem of classification of twist 3 chiral-odd GPDs is still open (B. Pire, L. S., S. Wallon, in preparation, in the spirit of our Light-Cone Collinear Factorization framework: Anikin, Ivanov, Pire, L. S, S. Wallon

JOG CP



# Master formula based on leading twist 2 factorization



$$\mathcal{A} = \frac{1}{\sqrt{2}} \int_{-1}^{1} dx \int_{0}^{1} dv \int_{0}^{1} dz \; (T^{u}(x, v, z) - T^{d}(x, v, z)) \\ \times \quad (H^{u}_{T}(x, \xi, t) - H^{d}_{T}(x, \xi, t)) \Phi_{\pi}(z) \Phi_{\rho}(v) + \cdots$$

・ロト ・ 日 ・ ミー ・ ヨー ・ シュマ

#### Non pertubative matrix elements

One needs to encode the matrix elements of two kinds of chiral-odd operator:

• transversity GPDs (twist-2 level):

$$\int \frac{dz^{-}}{4\pi} e^{ixP^{+}z^{-}} \langle p_{2}, \lambda_{2} | \bar{\psi}_{q} \left( -\frac{1}{2}z^{-} \right) i\sigma^{+i}\psi \left( \frac{1}{2}z^{-} \right) | p_{1}, \lambda_{1} \rangle$$

$$= \frac{1}{2P^{+}} \bar{u}(p_{2}, \lambda_{2}) \left[ H_{T}^{q}(x,\xi,t)i\sigma^{+i} + \tilde{H}_{T}^{q}(x,\xi,t) \frac{P^{+}\Delta^{i} - \Delta^{+}P^{i}}{M_{N}^{2}} + E_{T}^{q}(x,\xi,t) \frac{\gamma^{+}\Delta^{i} - \Delta^{+}\gamma^{i}}{M_{N}} + \tilde{E}_{T}^{q}(x,\xi,t) \frac{\gamma^{+}P^{i} - P^{+}\gamma^{i}}{M_{N}} \right] u(p_{1},\lambda_{1})$$

- for  $\Delta_{\perp} = 0$  each above factors vanishes except for  $H_T^q$  which thus dominates in the small t domain
- in the forward limit it is the only transversity GPD which survives:  $H_T^q(x, 0, 0) = \Delta_T q(x)$  (quark transversity distribution)
- transversity DAs (twist-2 level):

$$\langle 0|\bar{u}(0)\sigma^{\mu\nu}u(x)|\rho^{0}(p,s)\rangle = \frac{i}{\sqrt{2}}(\sigma^{\mu}_{\rho}p^{\nu} - \sigma^{\nu}_{\rho}p^{\mu})f^{\perp}_{\rho}\int_{0}^{1}du \ e^{-iup\cdot x} \ \phi_{\perp}(u)$$



$$p_{\pi}^{\mu} = \alpha n^{\mu} + \frac{(\vec{p}_{t} - \vec{\Delta}_{t}/2)^{2} + m_{\pi}^{2}}{\alpha s} p^{\mu} + p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2}$$
$$p_{\rho}^{\mu} = \alpha_{\rho} n^{\mu} + \frac{(\vec{p}_{t} + \vec{\Delta}_{t}/2)^{2} + m_{\rho}^{2}}{\alpha_{\rho} s} p^{\mu} - p_{\perp}^{\mu} - \frac{\Delta_{\perp}^{\mu}}{2}$$

< ロ > < 母 > < 三 > < 三 > 、 三 ・ の < ()



## Computation of the hard part





・ロ > ・ 一日 > ・ 三 > ・ 三 > ・ 今 へ ()・

#### Tensorial structure of the amplitude

$$\begin{aligned} \mathcal{A}_{H_T^q} &= (N_{\lambda_1\lambda_2}^{\perp} \cdot \epsilon_{\rho\pm})(p_{\perp} \cdot \epsilon_{\gamma\perp})A + (N_{\lambda_1\lambda_2}^{\perp} \cdot \epsilon_{\gamma\perp})(p_{\perp} \cdot \epsilon_{\rho\pm})B \\ &+ (N_{\lambda_1\lambda_2}^{\perp} \cdot p_{\perp})(\epsilon_{\gamma\perp} \cdot \epsilon_{\rho\pm})C \\ &- (N_{\lambda_1\lambda_2}^{\perp} \cdot p_{\perp})(p_{\perp} \cdot \epsilon_{\gamma\perp})(p_{\perp} \cdot \epsilon_{\rho\pm})D \end{aligned}$$

Jac.

with

- A, B, C, D scalar functions of  $S_{\gamma N}$ , -u' and  $M^2_{\pi \rho}$
- $\epsilon^{\mu}_{\gamma\perp}$  the transverse polarization of the on-shell photon •  $N^{\perp\mu}_{\lambda_1\lambda_2} = \frac{2i}{n\cdot n} g^{\mu\nu}_{\perp} \bar{u}(p_2,\lambda_2) \# \gamma_{\nu} \gamma^5 u(p_1,\lambda_1)$

Rich spin structure of  $\mathcal{A}_{H^q_T}$  : access to the spin density matrix of  $\rho^0_T,$  polarization asymmetries, ...

# A model based on Double Distribution

## Realistic Parametrization of $H_T^q$

• GPDs can be represented in terms of Double Distribution (Radyushkin) based on Schwinger representation of a toy model for GPDs which has the structure of a triangle diagram in scalar  $\phi^3$  theory

$$H_T^q(x,\xi,t=0) = \int_{-1}^1 d\beta \int_{-1+|\beta|}^{1-|\beta|} d\alpha \ \delta(\beta+\xi\alpha-x) \ f_T^q(\beta,\alpha)$$

- ansatz for these Double Distribution (Radyushkin):
  - $f_T^q(\beta, \alpha) = \Pi(\beta, \alpha) \Delta_T q(\beta)$
  - $\Delta_T q(x)$  : chiral-odd PDF (Anselmino *et al.*)

• 
$$\Pi(\beta, \alpha) = \frac{3}{4} \frac{(1-\beta)^2 - \alpha^2}{(1-\beta)^3}$$
 : profile function  $(f_T^q(\beta, 0) = \Delta_T q(\beta))$ 

• ansatz for the *t*-dependence:

$$H^q_T(x,\xi,t) = H^q_T(x,\xi,t=0) \times F_H(t)$$
  
with  $F_H(t) = \frac{C^2}{(t-C)^2}$  a standard dipole form factor ( $C = .71 \text{ GeV}$ )

# Plots of our model for transversity GPD

x and  $\xi$ -dependence of  $H_T^q(x,\xi,t=0)$ 





0.0

x

-0.5

0.5

## Plots of our model for transversity GPD



Same order of magnitude but significant differences with other parametrizations (Pincetti *et al.*) and lattice calculations (Göckeler *et al.*)



### Unpolarized differential cross section

#### Differential Cross Section and Physical Cuts



## Predictions



## Predictions



Total cross sections for photoproduction:

$$\sigma(S_{\gamma N} = 20 \text{ GeV}^2) \simeq 33 \text{ nb} \quad \sigma(S_{\gamma N} = 200 \text{ GeV}^2) \simeq 0.1 \text{ nb}$$

## Predictions





# Muoproduction at Compass (CERN)

#### Very sizable rates

- denote  $\Gamma^{\mu}_{T}(Q^{2}, \nu)$  the quasi real (transverse) photon flux ( $E_{\mu} = 160$  GeV).
- $\bullet$  Total cross section for the muoproduction  $\mu N \to \mu \pi^+ \rho_T^0 N'$

$$\sigma_{\mu} = \int_{0.02}^{1} dQ^2 \int_{16}^{144} d\nu \ \Gamma_T^{\mu}(Q^2,\nu) \ \sigma_{\gamma^*N \to \pi^+ \rho_T^0 N'}(Q^2,\nu) \simeq 0.25 \text{ pb}$$

• Experimental rate: For a muon beam luminosity of 2.5  $10^{32}$  cm<sup>-2</sup>.s<sup>-1</sup>,

$$\mathbf{R}\simeq 6~10^{-2}~\text{Hz}$$

Sac

Very sizable

## Rate estimates at JLab

### Very high rates

• CLAS12 Hall B:

with a photon (7 - 10.5 GeV) flux  $N_{\gamma} \sim 5 \ 10^7$  photons/s

Experimental rate:  $R \sim 0.1 \text{ Hz}$ 

• Hall D (12 GeV)

- photon (8 9 GeV) flux  $N_\gamma \sim 10^8$  photons/s
- number of protons per surface unit  $N_p \sim 1.27 \ {
  m b}^{-1}$  (target : liquid hydrogen (30 cm))

Sac

Experimental rate:  $R = \sigma \times N_{\gamma} \times N_p \sim 5 \text{ Hz}$ 

# Conclusion

- Photoproduction of a  $\pi \rho_T^0$  pair with a large hard scale  $M_{\pi\rho}^2$  sensitive to the transversity GPDs even for unpolarized target and at twist-2 level
- $\bullet$  Parametrization of the dominant chiral-odd GPD  $H^q_T$  based on double distribution
- Promising way to get informations on the generalized chiral-odd quark content of the nucleon: large enough rates to extract transversity GPDs, at COMPASS and JLab@12 GeV
- Possibility to access to :
  - spin density matrix of  $ho_T^0$
  - spin asymmetries
  - chiral-even GPDs H and  $\tilde{H}$  with  $\rho_L^0$

M. El Beiyad, B. Pire, L.S., S. Wallon in preparation

 Such processes with 3 body final state are also promising for non transversity GPD measurement, on top of the now standard DVCS based studies

3

Jac.

# BACKUP

<ロ> < 四> < 回> < 三> < 三> < 三> < 三 > < 三 > へ 0 へ 0

# Transverse polarization of $\rho_T^0$

$$\begin{aligned} \epsilon^{\mu}_{\pm}(p_{\rho}) &= \left(\frac{\vec{p}_{\rho} \cdot \vec{\epsilon}_{\pm}}{m_{\rho}}, \ \vec{\epsilon}_{\pm} + \frac{\vec{p}_{\rho} \cdot \vec{\epsilon}_{\pm}}{m_{\rho}(E_{\rho} + m_{\rho})} \vec{p}_{\rho}\right) \\ \Rightarrow & 2\bar{\alpha} \frac{\vec{p}_{t} \cdot \vec{\epsilon}_{\pm}}{\bar{\alpha}^{2}s + \vec{p}_{t}^{2}} \left(p^{\mu} + n^{\mu}\right) + (0, \vec{\epsilon}_{\pm}) \\ \Rightarrow & 2\bar{\alpha} \frac{\vec{p}_{t} \cdot \vec{\epsilon}_{\pm}}{\bar{\alpha}^{2}s + \vec{p}_{t}^{2}} \left[1 - \frac{\vec{p}_{t}^{2}}{\bar{\alpha}^{2}s}\right] p^{\mu} + 2\frac{\vec{p}_{t} \cdot \vec{\epsilon}_{\pm}}{\bar{\alpha}^{2}s + \vec{p}_{t}^{2}} p_{T}^{\mu} + (0, \vec{\epsilon}_{\pm}) \end{aligned}$$

・ロト ・ 御 ト ・ ヨト ・ ヨト

 $\mathfrak{I}_{\mathcal{A}}$ 

₹

## Transversity PDFs

$$\begin{aligned} \Delta_T u(x) &= 7.5 * 0.5 * (1-x)^5 (x * u(x) + x * \Delta u(x)) \\ \Delta_T \bar{u}(x) &= 7.5 * 0.5 * (1-x)^5 (x * \bar{u}(x) + x * \Delta \bar{u}(x)) \\ \Delta_T d(x) &= 7.5 * (-0.6) * (1-x)^5 (x * d(x) + x * \Delta d(x)) \\ \Delta_T \bar{d}(x) &= 7.5 * (-0.6) * (1-x)^5 (x * \bar{d}(x) + x * \Delta \bar{d}(x)) \end{aligned}$$

# Polarized PDFs

シック 三 《言》《言》《曰》 《曰》