PyPWA
A Partial-Wave/Amplitude Analysis Software Framework

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other team members

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Future of Spectroscopy Analysis will be on the study of resonances that are hidden?
★ overlapping
★ wide
★ many-particles final states
★ having small cross-sections
★ with large non-resonant backgrounds
★ ...

Furthermore

• Wave ambiguities
• Leakages
• Baryon contamination (JLab)

• LARGE DATA STATISTICS
• LARGE AMOUNT OF SIMULATION (MC)

In this environment we will need to find
• the poles on the S-Matrix (complex amplitudes) and
• detailed study of interference between states (wave motion) to determine new short-lived states.
PyPWA

Our philosophy

Provide the user with a software framework to analyze resonances from multi-particle final states in photo-production.

- Types of analysis
  - OPTIMIZATION (Parameter Estimation - Fitting)
  - SIMULATION (Monte Carlo)
- Basic TOOLS/MODULAR to be use in the analysis
- Flexible (EASY to CHANGE)
- Very WELL DOCUMENTED
- Interact with multiple programing languages
- Interact with other packages
- Easy integration to ANY amplitude model written in ANY language
- Integrated use of the JLab Scientific Computing Resources
- Parallelization & Vectorization
- Own graphical package and interface with PyROOT (CERN)
Implementation: **PYTHON** basic numpy and scipy libraries

- GUI driven use of JLab resources (i.e., Farms).

- Hybrid programming, where languages are used as they are adequate for the specific task and then interfaced. For example, Python being a high-level programming language makes a better scripting language to “glue” several programming modules, and Fortran and C are more basic languages with much faster number-crunching looping.

- Vectorization works by exploiting the combined add-multiply unit of the Intel Xeon Phi and/or GPUs

- Include full documentation at code level (and also tutorials examples...)

- Many options for optimization (i.e., minimization algorithms) and plotting tools

- Many options for data formats (in and out) - auto-defined txt files/or 4-vectors...
The PyPWA framework and toolkit is divided in

**GENERAL-SHELL**
- Fitting and Simulation
- Can use any model
- Interface is through a user defined Python script taken from a template.
- Integrated batch farm interface
- ISOBAR plotting can be used the ISOBAR file structure is mimicked by the user.
- Simulation produces “masks”.

**ISOBAR**
- Fitting and Simulation
- Exclusively uses the isobar amplitude model and photo-production (linear pol)
- Easy install and mass binning
- Takes advantage of the GAMP\(^1\) event format and the GAMP amplitude generator utilizing “keyfiles” physics descriptions
- Interface is with GUIs
- Interacts directly and exclusively with the Jlab batch farm
- Integrated plotting through Python

\(^1\) Cummings and Weygand (2000) -used by E852-COMPASS-CLAS
<table>
<thead>
<tr>
<th>software structure</th>
<th>General-shell</th>
<th>Isobar (PWA)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>● Parametric fitting of data using any physics model</td>
<td>● Meson Spectroscopy and Partial Wave Analysis using the Isobar model</td>
</tr>
<tr>
<td></td>
<td>● Simulating data from phase space Monte Carlo using Rejection Sampling MC</td>
<td>● Simulating data from phase space Monte Carlo using Rejection Sampling</td>
</tr>
<tr>
<td></td>
<td>● Python is a high level language which eases the writing of intensities.</td>
<td>● Analysis of data using mass plotting tools</td>
</tr>
<tr>
<td></td>
<td>● Access to all Python and PYROOT libraries (and own)</td>
<td>● Integrated Isobar model</td>
</tr>
<tr>
<td></td>
<td>● Integration with lower level languages is easy(F2PY, CYTHON)</td>
<td>● Ease and Speed of use for Jlab users</td>
</tr>
<tr>
<td></td>
<td>● Optional use of “Q factor” for signal quality</td>
<td>● Integration directly to the batch farm</td>
</tr>
<tr>
<td></td>
<td>● GS has a convenient interface with Minuit or other optimization.</td>
<td>● Optional use of “Q factor” for signal quality</td>
</tr>
</tbody>
</table>
The General shell side of PyPWA is focused on **openness and generality**.

The General Shell uses code inputs from the user, but can fit any model to the data by a user’s choice of:
- Un-binned standard Likelihood method.
- Un-binned Extended Likelihood method.
- Binned Likelihood method.
- Least-squares

\[
-ln \mathcal{L} = -\sum_{i=1}^{N} Q_i ln [I(\vec{x}_i, \vec{d})] + \frac{1}{N_g} \sum_{i=1}^{N_{a}} I(\vec{x}_i, \vec{d})
\]

**Minimization Default:** **Minuit**
many others are easily available from scipy.optimize
PWA - Isobar (Partial Wave Analysis) Formalism


\[ \mathcal{L} = \text{Prob}(N) \prod_{i=1}^{N} p(\vec{x}_i, \vec{d}_i) \]

Extended likelihood

\[ \text{Prob}(N) = \frac{N^N}{N!} e^{-N} \]

Then:

\[ -\ln \mathcal{L} \propto \sum_{i=1}^{N} \ln [\mathbb{P}(\vec{x}_i, \vec{d}_i)] - \int_{\Omega} \mathbb{P}(\vec{x}, \vec{d}) d^n \vec{x} \]

Need a Model to fit:

\[ \frac{d\sigma}{dt \times M^2 \times d\tau} \propto \sum_{\text{ext. spins}} |\mathcal{M}|^2 \equiv I(\tau) \]

\[ I(\tau) = \sum_{\text{ext. spins}} \langle f | \hat{T} \hat{\rho}_i \hat{T}^\dagger | f \rangle \]
**Partial Waves**

\[
P = (-1)^{L+1} \\
C = (-1)^{L+S} \\
G = (-1)^{L+S+I}
\]

The Spin Density Matrix of the incoming Photon is:

\[
\rho_{\epsilon\epsilon'}(P, \alpha) = \frac{1}{2} \begin{pmatrix}
1 + P \cos 2\alpha & iP \sin 2\alpha \\
-iP \sin 2\alpha & 1 - P \cos 2\alpha
\end{pmatrix}
\]

**Unbinned Maximum Likelihood fit**

\[
-ln\mathcal{L} \propto \sum_{i=1}^{N} \ln \left[ \sum_{k\epsilon} \tilde{p}_\gamma \sum_{b, b'} \epsilon V_b^k \epsilon V_b'^k \epsilon A_b(\tau_i) \epsilon A_b^*(\tau_i) \right] - \eta_x \sum_{k\epsilon} \sum_{b, b'} \epsilon V_b^k \epsilon V_b'^k \epsilon \Psi_{b, b'}
\]

**MASS INDEPENDENT FIT (in bins of M and t)**
Problems of destroying “factorization”

# Data events

\[
\mathcal{F}(\vec{p}) = -\ln \mathcal{L} = -\sum_{i=1}^{N} \ln \left[ \sum_{\text{ext. spins}} (\mathcal{M} \mathcal{M}^*) \right] + \eta_x \frac{1}{N_a} \sum_{i} \sum_{\text{ext. spins}} (\mathcal{M} \mathcal{M}^*). \tag{9}
\]

# MC events

\[
I(\tau) = \sum_{k^c} \sum_{b, b'} \epsilon_{A_b(\tau)} \epsilon_{V_{b'}^k} \overline{\rho_{\gamma}} \epsilon_{V_{b'}^{k*} A_{b'}^*(\tau)}
\]

\[
-\ln \mathcal{L} \propto \sum_{i=1}^{N} \ln \left[ \sum_{k^c} \sum_{b, b'} \epsilon_{V_{b}^k \epsilon_{V_{b'}^{k*} A_{b'}^*(\tau_i)}} \right] - \eta_x \sum_{k^c} \sum_{b, b'} \epsilon_{V_{b}^k \epsilon_{V_{b'}^{k*} \Psi_{b, b'}}}
\]

Normalization Integrals
Meson Spectroscopy Strategies at JLab

- Use 8.4–9 GeV linearly polarized photons
  - Identify (naturality) production mechanisms
  - Open phase space to separate meson/baryon production products
  - Sensitivity to masses up to ~ 2.8 GeV/c^2

- Use hermetic detector with large acceptance
  - Decay modes expected to have multiple particles
  - Hermetic coverage for charged and neutral particles
  - Medium resolution: momentum (~ 1-4%), energy (2-20%)
  - High data acquisition rate to enable amplitude analysis

- Perform amplitude analysis
  - Identify wide and rare (small cross sections) resonances
  - Use all available S-Matrix physics constraints on fittings
  - Identify the J^{PC} of resonances -phase motions -interference patterns
  - Check consistency of results in different decay modes
Strong kinematical cuts and a complex PWA are required

Going to higher energies increase phase space: 5.75 to 9 GeV?
Interesting region for strangeonia
Current uses of this software

1) Parametric fit to models
   - omega decay (Dalitz)  
     I. Danilkin, et al.
   - pKK analysis         
     Meng Shi et al.

2) PWA
   CLAS g12 pKK,3pi,...

3) Include “Deck-type” effects into PWA (extended)
   CLAS pKK,3pi,..        
   C. Fernandez et al.
some specifics for general-shell

Beginning the Process

Binning and file structures and anything else to do with the user's specific fit, or simulation is up to them. The only thing they need to start is two files for fitting, or simulation, and an extra variable parser utility for fitting.

For both fitting and simulation there is one file that the user interacts with and one (they can leave alone) used to run the fit (simulation).

Simulation and fitting take text files of variables in a specific format:

\[ X_1=0.25, X_2=1.67, X_3=90.5 \ldots \]

simulation produce two “masks” to be applied to each event
- production mask
- acceptance mask
User’s Main Point of Contact

The main points of contact for the user within the General Shell are the Fn.py and FnSim.py files. They are in the download as FnTemplate.py and FnSimTemplate.py.

They include documentation and examples to help the user write their intensity function, but a basic knowledge of Python is required. They are both a series of functions that each do a specific job for the calculations involved with fitting and simulation. This includes the intensity function, and the initial values and limits for fitting parameters. These files will have to be changed for every different fit, or simulation. Results and Plotting.
This is an example of the sort of function you can fit with PyPWA General. This is the `intFn()` function inside `Fn.py` and it's arguments are the two keyed dictionaries, `kVars` and `params`. `Kvars` are the variables parsed from the text file, while `params` are the parameters fitted by Minuit.

```
def intFn(kVars, params):
    tDist = params['A1']*numpy.exp(params['A2']*(kVars['tM']))
    wConst = (3.0/(4.0*math.pi))
    W = wConst*(0.5*(1-params['A3'])+0.5*(3*params['A3']-1)*math.cos(kVars['theta'])*2
               -math.sqrt(2.0)*params['A6'])*math.sin(2*kVars['theta'])*math.cos(kVars['phi'])
    F=AMP.amp(kVars['s'],kVars['t'],kVars['u'],params['A6'])
    Fsquare=F*numpy.conjugate(F)
    return tDist*W*kVars['P']*Fsquare
```

3 Fitted Function

$$I(sD,tD,uD,\theta,\phi,A1,A2,A3,A4,A5) = A1*W(\theta,\phi,A2,A3,A4)*P(sD,tD,uD)*[F(sD,tD,uD,A5)]^2$$

where $W$ is the Schilling et al. spin dinity matrix (no-polarization):

$$W(\theta,\phi,A2,A3,A4) =$$

\[3/4\pi \left[ 0.5 \left( 1 - A2 \right) + 0.5 \left( 3 \cdot A2 - 1 \right) \cos^2(\theta) - \sqrt{2} \cdot A3 \cdot \sin(\theta) \cos(\phi) - A4 \cdot \sin^2(\theta) \cos(2\phi) \right] \]

and $\theta$, $\phi$ are Adair's angles. $P$ is a kinematic factor given by:

$$P(sD,tD,uD) = sD \cdot tD \cdot uD - m_7^2 \left[ M^2 - m_5^2 \right]$$

where $sD$, $tD$, $uD$ are the Mandelstam variables of the decay such that:

$sD = (p_X - p_{e+}), sD = (p_X - p_{e-})$ and $sD = (p_X - p_{e0})$.

and $p_X = p_{e+} + p_{e-} + p_{e0}$, $M$ is the mass of the three pion system and $m_5$ the mass of the pion (plus).

$F(sD, tD, uD, A5)$ is Igor Danilkin et al. amplitude given for a call to his fortran code.
ISOBAR - PWA

The Isobar framework is focused on ease of use and speed. So from the install process until plotting almost everything is automated.

Install is handled by a single program which opens the control GUI, creates the needed directory structure, moves files to their correct location, and does the mass binning, which can take awhile if the user has many events.

The control GUI at right is the first point of contact the user has with PyPWA and the information filled into it will be used throughout the fitting and simulating process.
The Isobar framework's main point of contact for the user is the PWA_GUI at right. The left column is what appears when the program is run and the right is what appears after the FITTING button is pressed.

Each button on the right represents a different step in the fitting process and runs a different program. Each of these buttons will run the program which creates and submits many jsub files directly to Auger.

This GUI also has access to the control, the plotter, and the Waves utility.
Plotting

Plotting in PyPWA Isobar is handled by the above GUI which uses the MatPlotLib Python library for all plotting. This program also consolidates all data for plotting into single file named in the control. This file can be loaded in the future and multiple files can be saved and loaded at different times.
GUI driven
current work...

- Adding more utilities to make General Shell even easier to use.
- Farm and plotting integration for General-Shell
- Increased parallelization with the use of threading (farm - Xeon-Phi)
- Hardware acceleration with Xeon-Phi (Intel) and GPU's (Nvidia)
- Integrating more optimization and Monte Carlo methods
Intel-Xeon-Phi cards using for example OpenMP. Xeon Phi’s contain about 61 of x86 cores that are functionally identical to those of standard laptops and desktops. There are just many more of them running at a lower clock speed to fit into a reasonable thermal design envelope (currently a PCI Express card). The maximum output is at 1TFlop and they have comparable performance with GPGPUs. Writing code for the Xeon Phi is, initially, less complicated than writing code for GPUs since it will behave as any normal CPU.
A Partial-Wave/Amplitude Analysis Software Framework

The PyPWA Project
Thomas Jefferson National Accelerator Facility
Newport News, VA

Home

The PyPWA Project aims to develop a software framework that can be used to perform parametric model fitting to data. In particular, Partial Wave and Amplitude Analysis (PWA) of multiparticle final states. PyPWA is designed for photoproduction experiments using linearly polarized photon beams. The software makes use of the resources at the JLab Scientific Computer Center (Linux farm). PyPWA extract model parameters from data by performing extended likehood fits. Two versions of the software are develop: one where general amplitudes (or any parametric model) can be used in the fit and simulation of data, and a second where the framework starts with a specific realization of the isobar model, including extensions to Deck-type and baryon vertices corrections. Tutorials (Step-by-step instructions) leading to a full fit of data and the use of simulation software are included. Most of the code is in Python, but hybrid code (in Cython or Fortran) has been used when appropriate. Scripting to make use of vectorization and parallel coprocessors (Xeon-Phi and/or GPUs) are expected in the near future. The goal of this software framework is to create a user friendly environment for the spectroscopic analysis of linear polarized photoproduction experiments. The PyPWA Project software expects to be in a continue flow (of improvements!), therefore, please check on the more recent software download version.

Release Version 1.1 (June 22, 2015)

Version 1.1 includes several improvements, including the ability to reload the text files parsed in the General Shell, as well as a more general gampTranslator which allows for non-uniform white space in gamp files.

Bug fixes: Directory variable mistake in generalFitting is fixed.

https://pypwa.jlab.org
Jlab web-page - Tutorials and links
wiki - github JeffersonLab/PyPWA
Sphinx generated : docs
Welcome to pythonPWA’s documentation!

Source Listing

- General Shell
  - FnTemplate
  - generalFitting
  - FnSimTemplate
  - generalSim
  - kvParser
- DataTypes
  - gampEvent
  - gampParticle
  - resonance
  - wave
- fileHandlers
  - bampReader
  - gampReader
  - getWavesGen
  - gampTranslator
- Utilities
  - brietWigner
  - FourVec
  - LorentzTransform
  - phaseMotion
  - ThreeVec
  - randM
  - rotation
- Model
  - complexV
  - getPhi
  - intensity
  - magV
  - normInt
  - nTrue
  - prodAmp
  - spinDensity
- BatchFarmServices
  - GUI_alpha_main
  - GUI_gamp_main
  - GUI_subPyNormInt_main
  - PWA_GUI
generalShell

This module contains the general fitting and simulation programs.

FnTemplate

This file is a template the user can utilize to write a new fitting or simulation shell. This template includes examples of all critical functionalities.

generalFitting

class generalShell.fitting.generalFitting
This class is where the work of generalShell is done.

  __init__(dataDir=None, accDir=None, Q=1.0)
  generalFitting class default constructor.

  Kwarg:
  dataDir (string): Filepath of data (x, y) data.
  accDir (string): Filepath of accepted Monte Carlo.
  Q (float): Value of Q factor.

  genLen (int): Integer value for the number of initial (dictionary): Dictionary of initial values.

calcLikelihood(params)
Calculates the log of the Likelihood function.

Args:
  params (dictionary): Dictionary of fitted parameters.

FnSimTemplate

This file is a template the user can utilize to write a new simulation. This template includes examples of all critical functionalities.

dataTypes

This module contains the various data types used within the PWA project.

gampEvent

class pythonPWA.dataTypes.gampEvent, gampEvent(particles=[], accepted=None, raw=None)
This class represents a single gamp event. That is to say that this class contains a set of particles and a flag to specify if this event is accepted into the filtered data set.

gampParticle

class pythonPWA.dataTypes.gampParticle, gampParticle(particleID=None, particleCharge=None, particleXMMomentum=None, particleZMomentum=None, particleE=None)
This class represents a particle described in a single line of a .gamp file.

  toString()
  Returns a string of the particle data members delimited by newlines.

resonance

class pythonPWA.dataTypes.resonance, resonance(cR=1.0, wR=0.0, \[\omega_0=1.0, r_0=0.5, phase=0.0\])
This class represents a resonance.

  toString()
  Returns a string of the resonance data members delimited by newlines.

wave

class pythonPWA.dataTypes.wave, wave(epsilon=0, complexamplitudes=\[0.0=1000.0, \omega_0=100.0, \omega_0=0.0, k=0\])
This class represents a PWA wave.

  toString()
  Returns a string of all the wave properties delimited by newlines.
<table>
<thead>
<tr>
<th>Summary</th>
</tr>
</thead>
<tbody>
<tr>
<td>● PyPWA, both General and Isobar, provides a flexible software framework for Amplitude/Partial-Wave analysis.</td>
</tr>
<tr>
<td>● Python is a high level language which eases the writing of scripts to write amplitudes or to interface with intensities.</td>
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<tr>
<td>● Access to all Python libraries (scipy, numpy,...)</td>
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<td>● Integration directly to the JLab SciComp (batch farm)</td>
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<tr>
<td>● Integration with lower level languages is easy</td>
</tr>
<tr>
<td>● Includes a complete package of PWA (Isobar) in the Isobar model interfaced by GUIs</td>
</tr>
<tr>
<td>● Easy interface of PWA with extensions to the Isobar model.</td>
</tr>
<tr>
<td>● Download PyPWA at pypwa.jlab.org.</td>
</tr>
</tbody>
</table>

... is a work in progress.