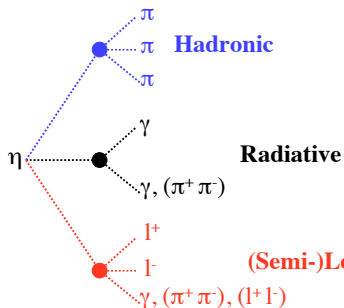


The η -Meson Decay Program at WASA-at-COSY

15.09.2015 | Daniel Lersch for the WASA-at-COSY collaboration

XVI International Conference on Hadron Spectroscopy

The η -Meson

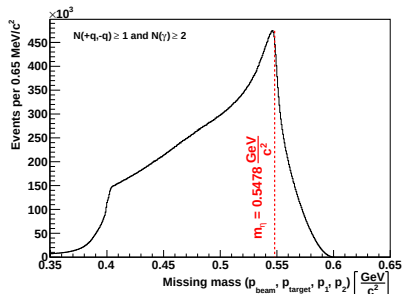
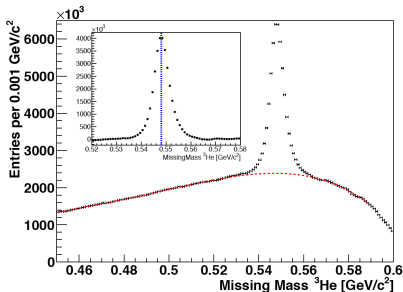


- $m_\eta = 0.5478 \text{ GeV}/c^2$, $\tau \approx 5 \cdot 10^{-19} \text{ s}$
($\Gamma_\eta = (1.31 \pm 0.05) \text{ keV}$)
 - $J^{PC} = 0^{-+} \Rightarrow \eta$ -meson is:
 C -, P -, G - and CP - eigenstate
 - All strong and electromagnetic decays are forbidden to first order
- $\Rightarrow$ **Access to rare decay processes:**
- Explore anomalous sector of QCD
 - Determine electromagnetic transition form factors
 - Study of symmetry-breaking-phenomena

η -Meson production at WASA-at-COSY:

- 1 $pd \rightarrow {}^3\text{He}\eta[\eta \rightarrow \dots] \parallel \sigma(\eta) = (0.412 \pm 0.016) \mu\text{b}$ at $T_{\text{beam}} = 1 \text{ GeV}$
- 2 $pp \rightarrow pp\eta[\eta \rightarrow \dots] \parallel \sigma(\eta) = (9.8 \pm 1) \mu\text{b}$ at $T_{\text{beam}} = 1.4 \text{ GeV}$

The data sets

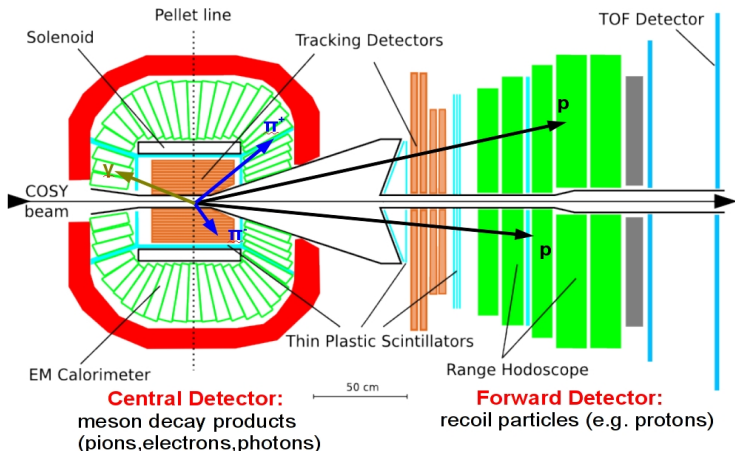


- Reconstruct η -meson via missing mass: $|\mathbf{P}_{\text{in}} - \mathbf{P}_{\text{out}}|$
- Background contributions from direct pion production reactions: $p d \rightarrow ^3\text{He} X$, $pp \rightarrow pp X$
 $X = \pi^+ \pi^-$, $X = \pi^0 \pi^0$ and $X = \pi^+ \pi^- \pi^0$

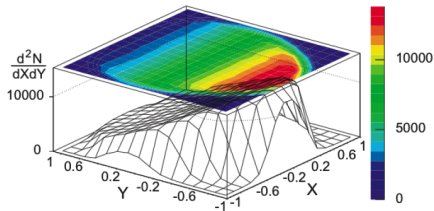
	$p d \rightarrow ^3\text{He} \eta$		$pp \rightarrow pp \eta$		
Data taken in	2008	2009	2008	2010	2012
Duration of beam time	4 weeks	8 weeks	2 weeks	7 weeks	8 weeks
η -mesons detected / produced	$\sim 1 \cdot 10^7$	$\sim 2 \cdot 10^7$	$\sim 1 \cdot 10^8$	$\sim 4 \cdot 10^8$	$\sim 5 \cdot 10^8$

Wide Angle Shower Apparatus - WASA

Example: $pp \rightarrow pp\eta[\eta \rightarrow \pi^+\pi^-\gamma]$



$\eta \rightarrow \pi^+ \pi^- \pi^0$ Dalitz plot analysis



(a) KLOE coll., JHEP, 05, (2008)

Dalitz plot variables:

$$X = \sqrt{3} \frac{T_{\pi^+} - T_{\pi^-}}{T_{\pi^+} + T_{\pi^-} + T_{\pi^0}}$$

$$Y = \frac{3T_{\pi^0}}{T_{\pi^+} + T_{\pi^-} + T_{\pi^0}}$$

- Decay via strong isospin violation: $\Gamma_{meas} = \left(\frac{Q_D}{Q}\right)^4 \bar{\Gamma}$
 - $Q^2 = \frac{m_s^2 - \hat{m}^2}{m_d^2 - m_u^2}$, $\hat{m} = \frac{1}{2}(m_u + m_d)$
 - $\bar{\Gamma}$ calculated with ChPT at Dashen limit, $Q_D = 24.2$
- Dalitz plot analysis: $\frac{d\Gamma}{dXdY} \propto (1 + aY + bY^2 + dX^2 + fY^3 + gX^2Y + \dots)$
 $\rightarrow c, e$ and h would imply C-violation

$$\eta \rightarrow \pi^+ \pi^- \pi^0$$

Results from $pd \rightarrow {}^3\text{He} \eta$

Parameter:		—a	b	d	f
Theo.	ChPT (NNLO) ^(b)	1.271(75)	0.394(102)	0.055(57)	0.025(160)
	NREFT ^(c)	1.213(14)	0.308(23)	0.050(3)	0.083(19)
Exp.	KLOE ^(a)	1.090(5)($^{+8}_{-19}$)	0.124(6)(10)	0.057(6)($^{+7}_{-16}$)	0.14(1)(2)
	WASA ^(d)	1.144(18)	0.219(19)(47)	0.086(18)(15)	0.115(37)

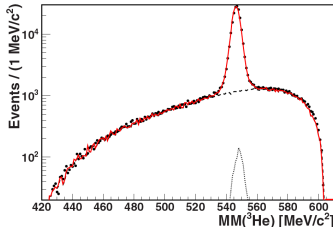
(a) KLOE coll., *JHEP*, 05, (2008)

(b) J. Bijnens and K. Ghorbani., *JHEP*, 11, (2007)

(c) S- P. Schneider et al., *JHEP*, 028, (2011)

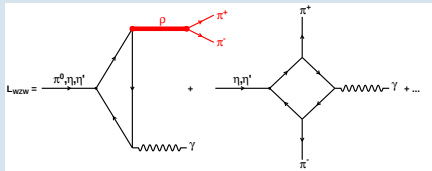
(d) WASA-at-COSY coll., *Phys. Rev.*, C90(045207), 2014

- $\sim 1.2 \cdot 10^5$ $\eta \rightarrow \pi^+ \pi^- \pi^0$ events selected via a kinematic fit for the final event sample
- Dalitz plot analysis for $pp \rightarrow pp\eta[\eta \rightarrow \pi^+ \pi^- \pi^0]$ in progress



$\eta \rightarrow \pi^+ \pi^- \gamma$ The box anomaly and $\pi^+ \pi^-$ FSI

Beyond chiral limit:



- Include $\pi^+ \pi^-$ Final State Interactions
- Modification of decay amplitude:^(a)

(a) F.Stollenwerk et al., *Phys. Lett.*, B707:184-190, 2012

$$A_{\eta \rightarrow \pi^+ \pi^- \gamma} \times [F_{PV}(s_{\pi\pi}) \cdot (1 + \alpha s_{\pi\pi})]$$

$$\Rightarrow \text{Description of FSI: } \begin{cases} \text{by } F_{PV} & \alpha = 0 \\ \text{reaction specific*} & \alpha \neq 0 \end{cases}$$

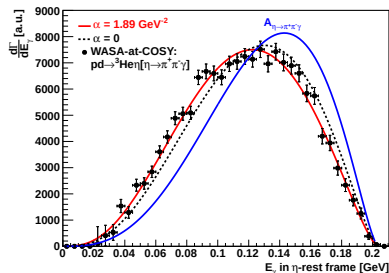
*Input from theory

- $\Gamma^{\text{Theory}}(\eta \rightarrow \pi^+ \pi^- \gamma) = 35.7 \text{ eV}^{(b)}$
- $\Gamma^{\text{Exp.}}(\eta \rightarrow \pi^+ \pi^- \gamma) = (55.3 \pm 2.4) \text{ eV}^{(c)}$

(b) B.R. Holstein, *Phys. Scripta*, T99:55-67, 2002

(c) PDG, *Chin. Phys.*, 090001, 2014

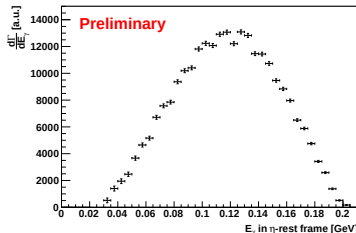
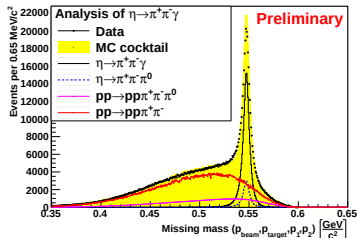
(d) WASA-at-COSY coll. *Phys. Lett.*, B707:243-249, 2012



$\Rightarrow$ Determine $\frac{\Gamma(\eta \rightarrow \pi^+ \pi^- \gamma)}{\Gamma(\eta \rightarrow \pi^+ \pi^- \pi^0)}$ and α via E_γ -distribution in $pp \rightarrow pp\eta[\eta \rightarrow \pi^+ \pi^- \gamma]$

$$\eta \rightarrow \pi^+ \pi^- \gamma$$

Status in $pp \rightarrow pp\eta$

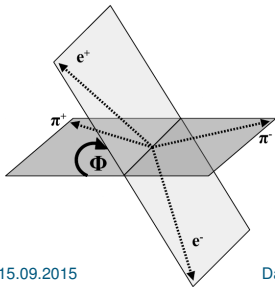


- $\sim 209 \text{ k } \eta \rightarrow \pi^+ \pi^- \gamma$ events reconstructed
 - i) Rejection of wrongly reconstructed photons $\Rightarrow$ Reduce background from $pp \rightarrow pp\pi^+\pi^-$
 - ii) Kinematic fit $\Rightarrow$ Further reduction of multi pion background and improvement of E_γ resolution
- E_γ distribution after background correction from direct pion production
- Next steps (ongoing):
 - 1.) Include efficiency corrections for different assumptions on α
 - 2.) Calculate $\frac{\Gamma(\eta \rightarrow \pi^+ \pi^- \gamma)}{\Gamma(\eta \rightarrow \pi^+ \pi^- \pi^0)}$ and determine α

$\eta \rightarrow \pi^+ \pi^- e^+ e^-$ CP-Violation

$\eta \rightarrow \pi^+ \pi^- \gamma$

- CP-conserving for M_1 and E_2 transitions
- Access to CP-violation:
 - ⇒ Measure E_1 transition
 - ⇒ Need information about polarisation of single photon



$\eta \rightarrow \pi^+ \pi^- \gamma^* [\gamma^* \rightarrow e^+ e^-]$

- Look at asymmetry $A_\Phi^{(a)}$ of angle Φ between decay planes of electrons and pions:

$$A_\Phi = \frac{N(\sin[\Phi] \cos[\Phi] > 0) - N(\sin[\Phi] \cos[\Phi] < 0)}{N(\sin[\Phi] \cos[\Phi] > 0) + N(\sin[\Phi] \cos[\Phi] < 0)}$$

- Upper limit predicted by theory^(a): $\sim 1\%$
- Results found by KLOE:^(b)

$$1.) A_\Phi = (-0.6 \pm 2.5_{\text{stat}} \pm 1.8_{\text{sys}}) \cdot 10^{-2}$$

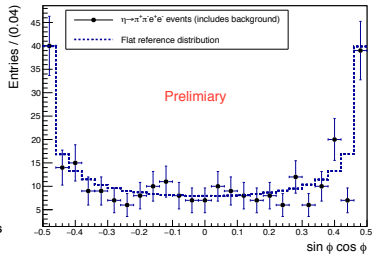
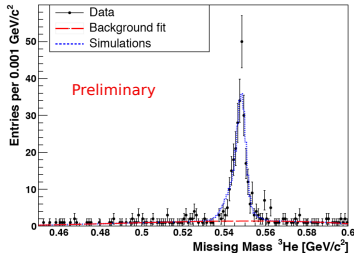
$$2.) \frac{\Gamma(\eta \rightarrow \pi^+ \pi^- e^+ e^-)}{\Gamma_\eta} = (2.68 \pm 0.09_{\text{stat}} \pm 0.07_{\text{sys}}) \cdot 10^{-4}$$

(a) D. Gao. *Mod. Phys. Lett.*, A17:1583-1588, 2002

(b) KLOE coll. *Phys. Lett.*, B675:283-288-914, 2009

$$\eta \rightarrow \pi^+ \pi^- e^+ e^-$$

Results from $pd \rightarrow {}^3\text{He} \eta$



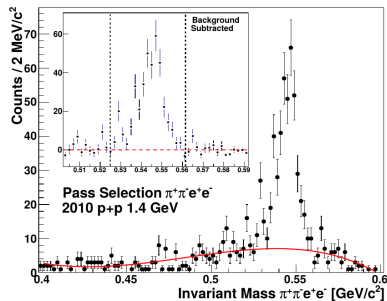
- 251 ± 17 $\eta \rightarrow \pi^+ \pi^- e^+ e^-$ events in the final sample
 - i) Rejection of photon conversion events $\Rightarrow$ Reduce contributions from $\eta \rightarrow \pi^+ \pi^- \gamma / \eta \rightarrow \pi^+ \pi^- \pi^0$
 - ii) Identification of $\pi^\pm$ and $e^\pm$ in the mixed final state $\Rightarrow$ Crucial for the determination of A_Φ
 - iii) Kinematic fit $\Rightarrow$ Reduction of $\eta \rightarrow \pi^+ \pi^- \pi^0 [\pi^0 \rightarrow e^+ e^- \gamma]$
- Preliminary:
 - 1.) $A_\Phi = (-1.1 \pm 6.6_{\text{stat}} \pm 0.2_{\text{sys}}) \cdot 10^{-2}$
 - 2.) $\frac{\Gamma(\eta \rightarrow \pi^+ \pi^- e^+ e^-)}{\Gamma_\eta} = (2.7 \pm 0.2_{\text{stat}} \pm 0.2_{\text{sys}}) \cdot 10^{-4}$
- Need more statistics $\Rightarrow$ **pp η data set**

$$\eta \rightarrow \pi^+ \pi^- e^+ e^-$$

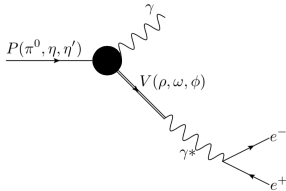
Status in $pp \rightarrow pp\eta$

- Analysis procedure shown above done for a fraction of 2010 $pp \rightarrow pp\eta$ data set:^(c)
 - ~ 220 $\eta \rightarrow \pi^+ \pi^- e^+ e^-$ events reconstructed
 - $\sim 1,000$ events expected for full $pp \rightarrow pp\eta$ data sample
- Analysis in $pp \rightarrow pp\eta$ needs to be continued

(c) D. Coderre, PhD Thesis, 2012



$\eta \rightarrow e^+ e^- \gamma$ and $\eta \rightarrow e^+ e^- e^+ e^-$ Dalitz decays



Single off-shell transition form factor $F(q^2)$

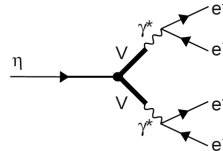
- $\frac{d\Gamma}{dq^2} = \left[\frac{d\Gamma}{dq^2} \right]_{QED} \cdot |F(q^2)|^2$
- Observables to test: $\frac{\Gamma(\eta \rightarrow e^+ e^- \gamma)}{\Gamma_\eta}$ and Dilepton mass
- Recent result: $\frac{\Gamma(\eta \rightarrow e^+ e^- \gamma)}{\Gamma_\eta} = (6.9 \pm 0.4) \cdot 10^{-3(a)}$

(a) K. Olive et al. *Chin. Phys.*, C38, 090001, 2014

Double off-shell transition form factor $F(q_1^2, q_2^2)$

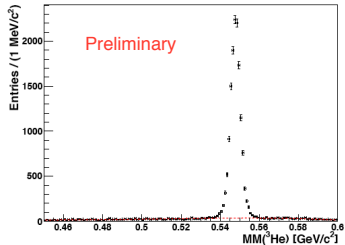
- Different approaches for calculation of $F^{(b)}$
- Observable to test: $\frac{\Gamma(\eta \rightarrow e^+ e^- e^+ e^-)}{\Gamma_\eta}$
- Current result measured by KLOE: $\frac{\Gamma(\eta \rightarrow e^+ e^- e^+ e^-)}{\Gamma_\eta} = (2.4 \pm 0.2_{stat} \pm 0.1_{sys}) \cdot 10^{-5}$

(b) J. Bijnens et al. *arXiv:hep-ph/0106130v1*, 2001 (c) KLOE coll. *Phys. Lett.*, B702:324-328, 2011

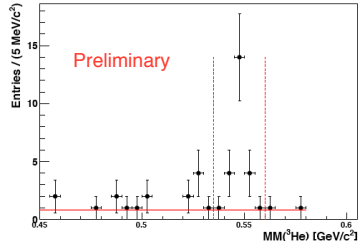


$\eta \rightarrow e^+ e^- \gamma$ and $\eta \rightarrow e^+ e^- e^+ e^-$

Results from $pd \rightarrow {}^3\text{He} \eta$



- $14,040 \pm 120$ events $\eta \rightarrow e^+ e^- \gamma$ events reconstructed
- Preliminary: $\frac{\Gamma(\eta \rightarrow e^+ e^- \gamma)}{\Gamma_\eta} = (6.72 \pm 0.07_{\text{stat}} \pm 0.31_{\text{sys}}) \cdot 10^{-3}$

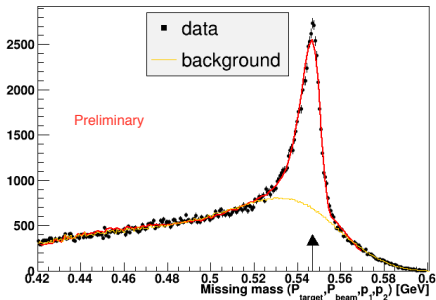


- 18 ± 5 $\eta \rightarrow e^+ e^- e^+ e^-$ events reconstructed
- Preliminary: $\frac{\Gamma(\eta \rightarrow e^+ e^- e^+ e^-)}{\Gamma_\eta} = (3.2 \pm 0.9_{\text{stat}} \pm 0.5_{\text{sys}}) \cdot 10^{-5}$
- Need more statistics $\Rightarrow$ **$pp\eta$ data set**

Challenges in analysis:

- Dilepton pairs from conversion events at the beam pipe
- Handling of large pion background

$\eta \rightarrow e^+ e^- \gamma$ Status in $pp \rightarrow pp\eta$

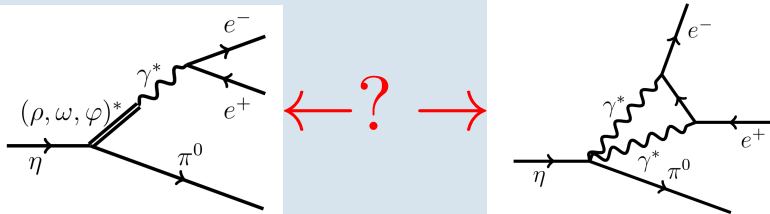


- Reduce uncertainty of $F(q^2)$ at high q^2 :
Increase statistics $\Rightarrow$ $pp\eta$ data set
- ~ 29 k $\eta \rightarrow e^+ e^- \gamma$ events
reconstructed in current
 $pp \rightarrow pp\eta[\eta \rightarrow e^+ e^- \gamma]$ analysis
 - i) PID $\Rightarrow$ Reduction of pions
 - ii) Rejection of conversion events
 $\Rightarrow$ Suppression of $\eta \rightarrow \gamma\gamma$
 - iii) Check for energy and momentum conservation
- In preparation:
 - 1.) Calculation of $\frac{\Gamma(\eta \rightarrow e^+ e^- \gamma)}{\Gamma_\eta}$
 - 2.) Dilepton invariant mass distribution
 $\Rightarrow F(q^2)$

Analysis of $pp \rightarrow pp\eta[\eta \rightarrow e^+ e^- e^+ e^-]$ in preparation

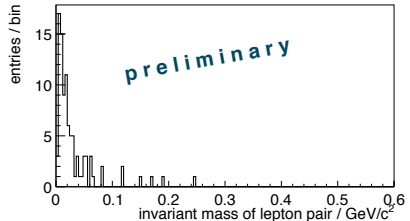
$\eta \rightarrow \pi^0 e^+ e^-$ C-Violation

Different decay models:



- Forbidden by SM:
 $BR(\eta \rightarrow \pi^0 e^+ e^-) < 4 \cdot 10^{-5}$ (a)
- Investigate existing upper limit BR with high statistics $pp \rightarrow pp\eta$ data set

(a) K. Olive et al. *Chin. Phys.*, C38, 090001, 2014



Summary and Outlook

Decay mode	$\Gamma(\eta \rightarrow \dots)/\Gamma_{\eta}^{(a)}$	Issue
$\eta \rightarrow \pi^0 \pi^0 \pi^0$ ^(b)	$(32.68 \pm 0.23)\%$	Dalitz plot analysis
$\eta \rightarrow \pi^+ \pi^- \pi^0$ ^(c)	$(22.92 \pm 0.28)\%$	Dalitz plot analysis
$\eta \rightarrow \pi^+ \pi^- \gamma$ ^(d)	$(4.22 \pm 0.08)\%$	Box anomaly, $\pi^+ \pi^-$ -FSI
$\eta \rightarrow e^+ e^- \gamma$ ^(e)	$(0.69 \pm 0.11)\%$	Single-off-shell transition form factor
$\eta \rightarrow \pi^0 \gamma \gamma$	$(2.7 \pm 0.5) \cdot 10^{-4}$	Test of ChPT
$\eta \rightarrow \pi^+ \pi^- e^+ e^-$ ^(e)	$(2.68 \pm 0.11) \cdot 10^{-4}$	CP-Violation
$\eta \rightarrow e^+ e^- e^+ e^-$ ^(e)	$(2.40 \pm 0.22) \cdot 10^{-5}$	Double-off-shell transition form factor
$\eta \rightarrow \pi^0 e^+ e^-$	$< 4 \cdot 10^{-5}$	C-Violation
$\eta \rightarrow e^+ e^-$	$< 5.6 \cdot 10^{-6}$	Physics beyond the SM

1 $pd \rightarrow {}^3\text{He} \eta [\eta \rightarrow \dots]$

2 $pp \rightarrow pp \eta [\eta \rightarrow \dots] \Rightarrow$ Analysis ongoing

(a): PDG, *Chin. Phys.*, 090001, 2014

(b): WASA-at-COSY coll., *Phys. Lett.*, B677:24-29, 2009

(c): WASA-at-COSY coll., *Phys. Rev.*, C90(045207), 2014

(d): WASA-at-COSY coll., *Phys. Lett.*, B707:243-249, 2012

(e): Publication in preparation

$\Rightarrow$ More fun with η -decays: See talk by M. Kunkel (1F1)

Contents

▸ (2) The η -Meson

▸ (3) The data set

▸ (4) WASA

$\eta \rightarrow \pi^+ \pi^- \pi^0$

▸ (5) Dalitz plot analysis

▸ (6) Results from $pd \rightarrow {}^3\text{He}\eta$

$\eta \rightarrow \pi^+ \pi^- \gamma$

▸ (7) The box anomaly and $\pi^+ \pi^-$ FSI

▸ (8) Status in $pp \rightarrow pp\eta$

$\eta \rightarrow \pi^+ \pi^- e^+ e^-$

▸ (9) CP-Violation

▸ (10) Results from $pd \rightarrow {}^3\text{He}\eta$

▸ (11) Status in $pp \rightarrow pp\eta$

$\eta \rightarrow e^+ e^- \gamma$ and $\eta \rightarrow e^+ e^- e^+ e^-$

▸ (12) Dalitz decays

▸ (13) Results from $pd \rightarrow {}^3\text{He}\eta$

▸ (14) Status in $pp \rightarrow pp\eta$

$\eta \rightarrow \pi^0 e^+ e^-$

▸ (15) C-Violation

▸ (16) Summary and Outlook

Backup

$$\eta \rightarrow \pi^+ \pi^- \gamma$$

- Theoretical Models
- Theoretical Predictions and Recent Measurements
- Analysis (Split-off rejection)
- Analysis (Kinematic fit)
- Determining the E_γ -distribution

$$\eta \rightarrow e^+ e^- \gamma \text{ and } \eta \rightarrow e^+ e^- e^+ e^-$$

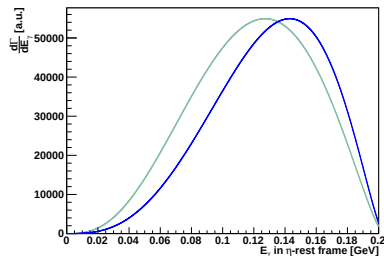
- Form factor $F(q^2)$
- Theoretical predictions for $\Gamma(\eta \rightarrow e^+ e^- e^+ e^-) / \Gamma(\eta)$
- Conversion events
- η Production mechanisms
- Preselection of the $pp \rightarrow pp\eta$ data set
- PID at WASA

$\eta \rightarrow \pi^+ \pi^- \gamma$ Theoretical Models

■ N/D-Model:^{a)}

- One-loop chiral corrections and VMD
- Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[\frac{1 + 0.5 m_\rho^2 s_{\pi\pi}}{D_1(s_{\pi\pi})} \right]$

a) B.R. Holstein, *Phys. Scripta*, T99:55-67, 2002

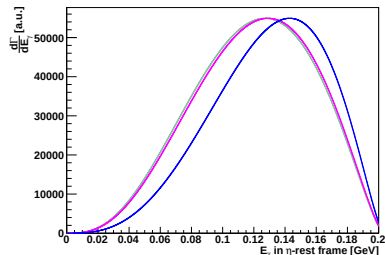


$\eta \rightarrow \pi^+ \pi^- \gamma$ Theoretical Models

- N/D-Model:^{a)}
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- HLS (Hidden Local Symmetries)-Model:^{b)}
 - $\gamma - V$ Transitions
 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[1 + \frac{3 m_\rho^2}{D_\rho(s_{\pi\pi})} \right]$

a) B.R. Holstein, *Phys. Scripta*, T99:55-67, 2002

b) M.Benayoun et al., *Europ. Phys. Journal*, C31:525-547, 2003



$$\eta \rightarrow \pi^+ \pi^- \gamma$$

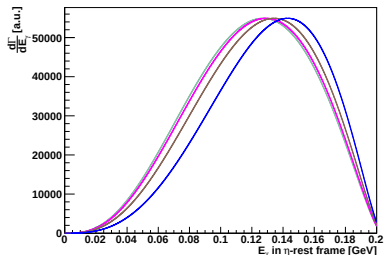
Theoretical Models

- N/D-Model:^{a)}
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 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[\frac{1 + 0.5 m_\rho^2 s_{\pi\pi}}{D_1(s_{\pi\pi})} \right]$
- HLS (Hidden Local Symmetries)-Model:^{b)}
 - $\gamma - V$ Transitions
 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[1 + \frac{3 m_\rho^2}{D_\rho(s_{\pi\pi})} \right]$
- $O(p^6) + 1 - \text{loop-Modell}$:^{c)}
 - Higher momentum orders $O(p^6)$ and one loop chiral corrections
 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[1 + C^{\text{loops}} + \frac{3}{2 m_\rho^2} (p_{\pi^+} + p_{\pi^-})^2 \right]$

a) B.R. Holstein, *Phys. Scripta*, T99:55-67, 2002

b) M.Benayoun et al., *Europ. Phys. Journal*, C31:525-547, 2003

c) J.Bijnens et al., *Phys. Lett.*, B237:488-494, 1990



$\eta \rightarrow \pi^+ \pi^- \gamma$ Theoretical Models

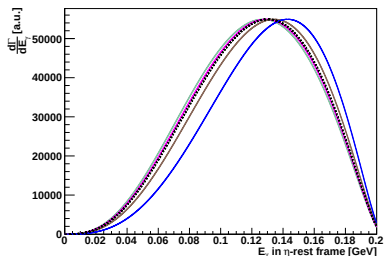
- N/D-Model:^{a)}
 - One-loop chiral corrections and VMD
 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[\frac{1 + 0.5 m_\rho^2 s_{\pi\pi}}{D_1(s_{\pi\pi})} \right]$
- HLS (Hidden Local Symmetries)-Model:^{b)}
 - $\gamma - V$ Transitions
 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[1 + \frac{3m_\rho^2}{D_\rho(s_{\pi\pi})} \right]$
- $O(p^6) + 1 - \text{loop-Modell}$:^{c)}
 - Higher momentum orders $O(p^6)$ and one loop chiral corrections
 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $\left[1 + C^{\text{loops}} + \frac{3}{2m_\rho^2} (p_{\pi^+} + p_{\pi^-})^2 \right]$
- Pion-Vektor-Formfactor:^{d)}
 - $\pi^+ \pi^-$ -interactions (universal)
 - Modify $A_{\eta \rightarrow \pi^+ \pi^- \gamma}$ with: $F_{PV}(s_{\pi\pi}) \approx a \cdot s_{\pi\pi}^3 + b \cdot s_{\pi\pi}^2 + c \cdot s_{\pi\pi} + d$

a) B.R. Holstein, *Phys. Scripta*, T99:55-67, 2002

b) M.Benayoun et al., *Europ. Phys. Journal*, C31:525-547, 2003

c) J.Bijnens et al., *Phys. Lett.*, B237:488-494, 1990

d) F.Stollenwerk et al., *Phys. Lett.*, B707:184-190, 2012



$\eta \rightarrow \pi^+ \pi^- \gamma$ Theoretical Predictions and Recent Measurements

		$\Gamma(\eta \rightarrow \pi^+ \pi^- \gamma) / \Gamma(\eta \rightarrow \pi^+ \pi^- \pi^0)$	$\alpha [\text{GeV}^{-2}]$
Experiment	Gormley et al.	0.202 ± 0.006	1.8 ± 0.4
	Thaler et al.	0.209 ± 0.004	-
	Layter et al.	-	-0.9 ± 0.1
	GAMS-200*	-	2.7 ± 0.1
	CRYSTAL BARREL*	-	1.8 ± 0.53
	CLEO	0.175 ± 0.013	-
	WASA-at-COSY	Preliminary: 0.206 ± 0.011	1.89 ± 0.86
	KLOE	0.1856 ± 0.003	1.32 ± 0.2
	CLAS	Analysis ongoing	-
Theory	N/D	0.2188 ± 0.0088	0.64 ± 0.02
	HLS	0.1875 ± 0.0094	0.23 ± 0.01
	$(O(p^6) + 1 - \text{loop})$	0.1565 ± 0.0063	-0.7 ± 0.1
	Box anomaly	0.119 ± 0.0048	-1.7 ± 0.02

* Measured $\eta' \rightarrow \pi^+ \pi^- \gamma$

$\eta \rightarrow \pi^+ \pi^- \gamma$ Theoretical Predictions and Recent Measurements

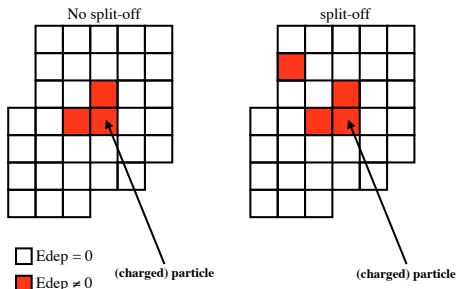
		$\Gamma(\eta \rightarrow \pi^+ \pi^- \gamma) / \Gamma(\eta \rightarrow \pi^+ \pi^- \pi^0)$	$\alpha [\text{GeV}^{-2}]$
Experiment	<i>Phys. Rev.</i> , D2:501-505, 1970	0.202 ± 0.006	1.8 ± 0.4
	<i>Phys. Rev.</i> , D7:2569-2571, 1973	0.209 ± 0.004	-
	<i>Phys. Rev.</i> , D7:2565-2568, 1973	-	-0.9 ± 0.1
	<i>Phys.</i> , C50:451-454, 1991 *	-	2.7 ± 0.1
	<i>Phys. Lett.</i> , B402:195, 1997 *	-	1.8 ± 0.53
	<i>Phys. Rev. Lett.</i> , 99(122001), 2007	0.175 ± 0.013	-
	<i>Phys. Rev. Lett.</i> , B707:243-249, 2013	-	1.89 ± 0.86
	<i>Phys. Lett.</i> , B718:910-914, 2013	0.1856 ± 0.003	1.32 ± 0.2
	<i>Chin. Phys.</i> , 090001, 2014	0.1847 ± 0.003	-
Theory	<i>Phys. Scripta</i> , T99:55-67, 2002	0.2188 ± 0.0088	0.64 ± 0.02
	<i>Europ. Phys. Journal</i> , C31:525-547, 2003	0.1875 ± 0.0094	0.23 ± 0.01
	<i>Phys. Lett.</i> , B237:488-494, 1990	0.1565 ± 0.0063	-0.7 ± 0.1
	<i>Phys. Scripta</i> , T99:55-67, 2002	0.119 ± 0.0048	-1.7 ± 0.02

* Measured $\eta' \rightarrow \pi^+ \pi^- \gamma$

$\eta \rightarrow \pi^+ \pi^- \gamma$ Analysis

i) Rejection of split-offs

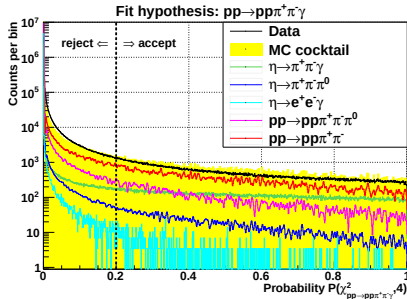
One (charged) particle in the calorimeter



- Hit in calorimeter is assigned to a cluster
- Split-off: Satellite cluster with close distance to primary cluster $\rightarrow$ low energy **fake photon**
- Predominant background: $pp \rightarrow pp\pi^+\pi^-(\gamma)$
- Reject low energy fake photons with close distance to primary cluster

$\eta \rightarrow \pi^+ \pi^- \gamma$ Analysis

ii) Kinematic fit



Use kinematic fit to:

- Improve resolution
- Suppress background

- Least squares fit:

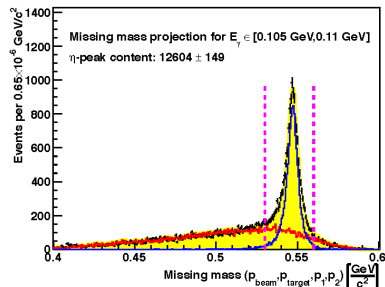
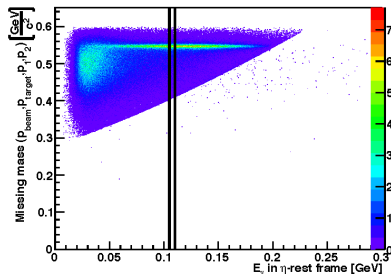
$$\chi^2 = \sum_{i=1}^{N_p} \sum_{j=1}^{N_v} \left(\frac{v_{ij}^{\text{fit}} - v_{ij}^{\text{meas}}}{\sigma_{ij}^{\text{meas}}} \right)^2 + 2 \cdot \sum_{\mu} \lambda_{\mu} F_{\mu}(v_{11}^{\text{fit}}, \dots, v_{N_p N_v}^{\text{fit}})$$

- F_{μ} : energy and momentum conservation
→ 4 constraints

- $P(\chi^2, N) = \frac{1}{\sqrt{2^N \cdot \Gamma(\frac{1}{2}N)}} \int_0^{\chi^2} e^{-\frac{t}{2}} \cdot t^{\frac{1}{2}N-1} dt$

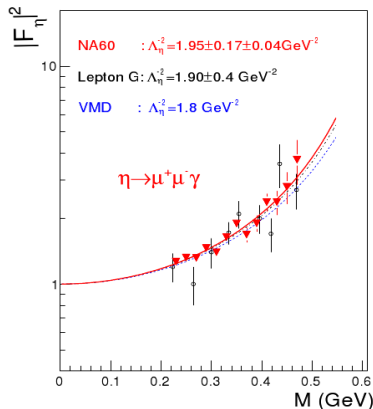
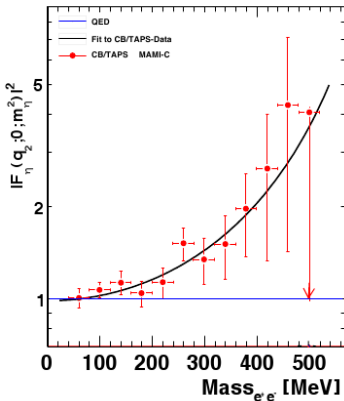
$$\eta \rightarrow \pi^+ \pi^- \gamma$$

Determining the E_γ -distribution



- Scan two proton missing mass distribution in E_γ -intervals
- Subtract background for each E_γ -interval
- Obtain number of $\eta \rightarrow \pi^+ \pi^- \gamma$ events

$\eta \rightarrow e^+ e^- \gamma$ Form factor $F(q^2)$



Single-pole formula: $F_P(q^2) = (1 - b_P^2 q^2)^{-1}$, $b_P \equiv \frac{1}{\Lambda_P}$

$$\eta \rightarrow e^+ e^- e^+ e^-$$

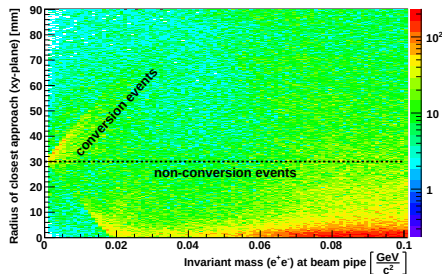
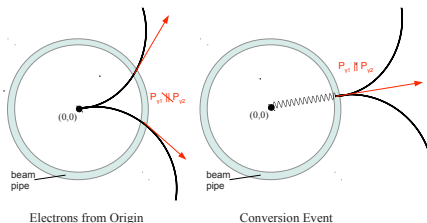
Theoretical predictions for $\Gamma(\eta \rightarrow e^+ e^- e^+ e^-)/\Gamma(\eta)$

- Double transition form factor $F(q_1^2, q_2^2)$
- Different approaches for calculation of $F^{(a)}$:

$F(q_1^2, q_2^2)$	$\Gamma(\eta \rightarrow e^+ e^- e^+ e^-)/\Gamma(\eta) [10^{-5}]$
1	2.52 ± 0.02
$\frac{m_\rho^4}{(m_\rho^2 - q_1^2)(m_\rho^2 - q_2^2)}$	2.65 ± 0.02
$\frac{m_\rho^2}{(m_\rho^2 - q_1^2 - q_2^2)}$	2.64 ± 0.02
$\frac{m_\rho^4 - \frac{4\pi^2 F_\pi^2}{N_C} (q_1^2 + q_2^2)}{(m_\rho^2 - q_1^2)(m_\rho^2 - q_2^2)}$	2.61 ± 0.02

(a) J. Bijnens et al. *arXiv:hep-ph/0106130v1*, 2001

Conversion events



- Conversion events: small opening angle and origin at beam pipe
- Non-Conversion events: large opening angle and origin at reaction vertex

η Production mechanisms

	$pd \rightarrow {}^3\text{He}\eta$	$pp \rightarrow pp\eta$
T_{beam}	1 GeV	1.4 GeV
$\sigma(\eta)^{a),b)}$	$(0.412 \pm 0.016) \mu\text{b}$	$(9.8 \pm 1) \mu\text{b}$
Suited for	study of not-so-rare η decays	study of (not-so-) rare η decays
Background	low multi-pion background	high multi-pion background

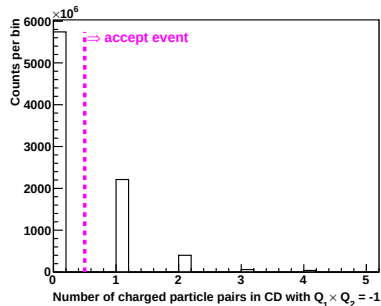
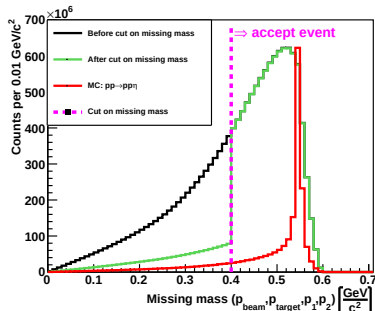
Reaction	$T_{\text{beam}}[\text{GeV}]$	$\sigma[\mu\text{b}]^{b),c)}$
$pd \rightarrow {}^3\text{He}\pi^0\pi^0$	0.893	2.8 ± 0.3
$pd \rightarrow {}^3\text{He}\pi^+\pi^-$	0.893	5.1 ± 0.5
$pp \rightarrow pp\pi^+\pi^-\pi^0$	1.36	4.6 ± 1.5
$pp \rightarrow pp\pi^0\pi^0$	1.36	200 ± 30
$pp \rightarrow pp\pi^+\pi^-$	1.36	660 ± 100

a) R. Bilger et al., *Phys. Rev.*, C65(044608), 2002

b) CELSIUS/WASA coll., *Phys. Lett.*, B649:122-127, 2007

c) M. Bashkanov et al., *Phys. Lett.*, B637:223-228, 2006

Preselection of the $pp \rightarrow pp\eta$ data set



Preselection done in two steps:

- Condition on missing mass $\Rightarrow$ Rejection of multi-pion background
- Condition on charged tracks in the Central Detector $\Rightarrow$ Selection of charged η decay modes

PID at WASA

