Significance of studies on Light Hypernuclei

E. Hiyama (RIKEN)

2016/3/15 JLab Hyp. WS

The major goal of hypernuclear physics



Therefore, as a substitute for the 2-body limited YN and non-existent YY scattering data, the systematic investigation of the structure of light hypernuclei is essential.

Hypernuclear *γ***-ray data since 1998** (figure by H.Tamura)



 $V_{\Lambda N} = V_0 + \boldsymbol{\sigma}_{\Lambda} \cdot \boldsymbol{\sigma}_N V_{\sigma \cdot \sigma} + \mathbf{L} \cdot (\mathbf{s}_{\Lambda} + \mathbf{s}_N) V_{\text{SLS}} + \mathbf{L} \cdot (\mathbf{s}_{\Lambda} - \mathbf{s}_N) V_{\text{ALS}} + S_{12} V_{\text{tensor}} + \cdots$

Millener (p-shell model),

Hiyama (few-body)





p



Homework: Please confirm below two states. (1) The ground state of ${}^{4}_{\Lambda}$ He

(2) The excited state of ${}^{4}_{\Lambda}H$ => JLab

In this way, it is important to confirm all of four states in A=4 Λ hypernuclei.

After confirmation, I am planning to calculate following...





Our four-body calculation using NSC97f potential. You see that the results do not reproduce the data. This means that we need more reliable YN interaction. After confirmation experiment, by combining new data and our calculation, we can finally solve CSB important issue.



 E10 "Study on Λ-hypernuclei with the doubleCharge-Exchange reaction" by Sakaguchi, Fukuda and his collaborations

 $^{9}_{\Lambda}\text{He}$ $^{6}_{\Lambda}\text{H}$

Non-strangeness nuclei

Ν

Ν

Nucleon can be converted into Δ . However, since mass difference between nucleon and Δ is large, then probability of Δ in nucleus is not large.

On the other hand, the mass difference between Λ and Σ is much smaller, then Λ can be converted into Σ particle easily.



Interesting Issues for the $\Lambda N-\Sigma N$ particle conversion in hypernuclei

(1)How large is the mixing probability of the Σ particle in the hypernuclei?

(2) How important is the $\Lambda N - \Sigma N$ coupling in the binding energy of the Λ hypernuclei?



These hypernuclei are suited for studying $\Lambda N-\Sigma N$ coupling.

 $^{3}_{\Lambda}$ H (hyper-triton)

Search for evidence of ${}^{3}_{\Lambda}n$ by observing $d + \pi^{-}$ and $t + \pi^{-}$ final states in the reaction of ${}^{6}\text{Li} + {}^{12}\text{C}$ at 2A GeV

C. Rappold,^{1,2,*} E. Kim,^{1,3} T. R. Saito,^{1,4,5,†} O. Bertini,^{1,4} S. Bianchin,¹ V. Bozkurt,^{1,6} M. Kavatsyuk,⁷ Y. Ma,^{1,4} F. Maas,^{1,4,5} S. Minami,¹ D. Nakajima,^{1,8} B. Özel-Tashenov,¹ K. Yoshida,^{1,5,9} P. Achenbach,⁴ S. Ajimura,¹⁰ T. Aumann,^{1,11} C. Ayerbe Gayoso,⁴ H. C. Bhang,³ C. Caesar,^{1,11} S. Erturk,⁶ T. Fukuda,¹² B. Göküzüm,^{1,6} E. Guliev,⁷ J. Hoffmann,¹ G. Ickert,¹ Z. S. Ketenci,⁶ D. Khaneft,^{1,4} M. Kim,³ S. Kim,³ K. Koch,¹ N. Kurz,¹ A. Le Fèvre,^{1,13} Y. Mizoi,¹² L. Nungesser,⁴ W. Ott,¹ J. Pochodzalla,⁴ A. Sakaguchi,⁹ C. J. Schmidt,¹ M. Sekimoto,¹⁴ H. Simon,¹ T. Takahashi,¹⁴ G. J. Tambave,⁷ H. Tamura,¹⁵ W. Trautmann,¹ S. Voltz,¹ and C. J. Yoon³ (HypHI Collaboration)</sup> **nn unbound nn hreakup** threshold **?**They did not report the binding energy.

Observation of nnA system (2013) This is also important to get information on AN- Σ N coupling.

three-body calculation of $\frac{3}{5}n$



E. Hiyama, S. Ohnishi, B.F. Gibson, and T. A. Rijken, PRC89, 061302(R) (2014). What is interesting to study $nn\Lambda$ system?



The lightest nucleus to have a bound state is deuteron.



Search for evidence of ${}^{3}_{\Lambda}n$ by observing $d + \pi^{-}$ and $t + \pi^{-}$ final states in the reaction of ${}^{6}\text{Li} + {}^{12}\text{C}$ at 2A GeV

C. Rappold,^{1,2,*} E. Kim,^{1,3} T. R. Saito,^{1,4,5,†} O. Bertini,^{1,4} S. Bianchin,¹ V. Bozkurt,^{1,6} M. Kavatsyuk,⁷ Y. Ma,^{1,4} F. Maas,^{1,4,5} S. Minami,¹ D. Nakajima,^{1,8} B. Özel-Tashenov,¹ K. Yoshida,^{1,5,9} P. Achenbach,⁴ S. Ajimura,¹⁰ T. Aumann,^{1,11} C. Ayerbe Gayoso,⁴ H. C. Bhang,³ C. Caesar,^{1,11} S. Erturk,⁶ T. Fukuda,¹² B. Göküzüm,^{1,6} E. Guliev,⁷ J. Hoffmann,¹ G. Ickert,¹ Z. S. Ketenci,⁶ D. Khaneft,^{1,4} M. Kim,³ S. Kim,³ K. Koch,¹ N. Kurz,¹ A. Le Fèvre,^{1,13} Y. Mizoi,¹² L. Nungesser,⁴ W. Ott,¹ J. Pochodzalla,⁴ A. Sakaguchi,⁹ C. J. Schmidt,¹ M. Sekimoto,¹⁴ H. Simon,¹ T. Takahashi,¹⁴ G. J. Tambave,⁷ H. Tamura,¹⁵ W. Trautmann,¹ S. Voltz,¹ and C. J. Yoon³ (HypHI Collaboration) **nn unbound nn hereakup** threshold **?**They did not report the binding energy.

scattering length:-2.68fm

Observation of nnA system (2013) One of the lightest bound hypernuclei Theoretical important issue: Do we have bound state for nnA system? If we have a bound state for this system, how much is binding energy?



NN interaction : to reproduce the observed binding energies of ³H and ³He

NN: AV8 potential We do not include 3-body force for nuclear sector.

How about YN interaction?

To take into account of Λ particle to be converted into Σ particle, we should perform below calculation using realistic hyperon(Y)-nucleon(N) interaction.



YN interaction: Nijmegen soft core '97f potential (NSC97f) proposed by Nijmegen group

reproduce the observed binding energies of ${}^3_\Lambda\text{H},~{}^4_\Lambda\text{H}$ and ${}^4_\Lambda\text{He}$





What is binding energy of $nn\Lambda$?



We have no bound state in $nn\Lambda$ system. This is inconsistent with the data.

In this way, we have no possibility to have a bound state for nnA system. Then, I hope that confirm experiment of this system will be performed again at GSI or JLab using ³H target.



Also, it is pointed out that $nn\Lambda$ system might be resonant state by Dr. Gibson. He will give a talk about it in this workshop. Now, we have a question. If we add more two neutrons In this system, what happen?



four-body calculation of ⁴n



n

Ş

Candidate Resonant Tetraneutron State Populated by the ⁴He(⁸He,⁸Be) Reaction

K. Kisamori,^{1,2} S. Shimoura,¹ H. Miya,^{1,2} S. Michimasa,¹ S. Ota,¹ M. Assie,³ H. Baba,² T. Baba,⁴ D. Beaumel,^{2,3} M. Dozono,² T. Fujii,^{1,2} N. Fukuda,² S. Go,^{1,2} F. Hammache,³ E. Ideguchi,⁵ N. Inabe,² M. Itoh,⁶ D. Kameda,² S. Kawase,¹ T. Kawabata,⁴ M. Kobayashi,¹ Y. Kondo,^{7,2} T. Kubo,² Y. Kubota,^{1,2} M. Kurata-Nishimura,² C. S. Lee,^{1,2} Y. Maeda,⁸ H. Matsubara,¹² K. Miki,⁵ T. Nishi,^{9,2} S. Noji,¹⁰ S. Sakaguchi,^{11,2} H. Sakai,² Y. Sasamoto,¹ M. Sasano,² H. Sato,² Y. Shimizu,² A. Stolz,¹⁰ H. Suzuki,² M. Takaki,¹ H. Takeda,² S. Takeuchi,² A. Tamii,⁵ L. Tang,¹ H. Tokieda,¹ M. Tsumura,⁴ T. Uesaka,² K. Yako,¹ Y. Yanagisawa,² R. Yokoyama,¹ and K. Yoshida² ¹Center for Nuclear Study, The University of Tokyo, 7-3-1 Hongo, Bunkyo, Tokyo 113-0033, Japan ²RIKEN Nishina Center, 2-1 Hirosawa, Wako, Saitama 351-0198, Japan ³IPN Orsay, 15 Rue, Georges, Clemenceau 91400 Orsay, France ⁴Department of Physics, Kyoto University, Yoshida-Honcho, Sakyo, Kyoto 606-8501, Japan ⁵Research Center for Nuclear Physics, Osaka University, 10-1 Mihogaoka, Ibaraki, Osaka 567-0047, Japan ⁶Cvclotron and Radioisotope Center, Tohoku University, 6-3 Aoba, Aramaki, Aoba-ku, Sendai, Miyagi 980-8578, Japan ⁷Department of Physics, Tokyo Institute of Technology, 2-12-1 O-Okayama, Meguro, Tokyo 152-8550, Japan ⁸Faculty of Engineering, University of Miyazaki, 1-1 Gakuen, Kibanadai-nishi, Miyazaki 889-2192, Japan ⁹Department of Physics, The University of Tokyo, 7-3-1 Hongo, Bunkyo, Tokyo 113-0033, Japan ¹⁰National Superconducting Cyclotron Laboratory, Michigan State University, 640 S Shaw Lane, East Lansing, Michigan 4 ¹¹Department of Physics, Kyushu University, 6-10-1 Hakozaki, Higashi, Fukuoka 812-8581, Japan ¹²National Institute of Radiological Sciences, 4-9-1 Anagawa, Inage, Chiba, Japan (Received 30 July 2015; revised manuscript received 11 October 2015; published 3 February 2016)

A candidate resonant tetraneutron state is found in the missing-mass spectrum obtained in the double charge-exchange reaction ${}^{4}\text{He}({}^{8}\text{He}, {}^{8}\text{Be})$ at 186 MeV/u. The energy of the state is $0.83 \pm 0.65(\text{stat}) \pm 1.25(\text{syst})$ MeV above the threshold of four-neutron decay with a significance level of 4.9σ . Utilizing the large positive Q value of the (${}^{8}\text{He}, {}^{8}\text{Be}$) reaction, an almost recoilless condition of the four-neutron system was achieved so as to obtain a weakly interacting four-neutron system efficiently.



Now, we have new data for tetraneutron system.

Theoretical important issue:

 Can we describe observed 4n system using realistic NN interaction and T=3/2 three-body force?

Motivated by experimental data, we started to study tetra neutron system.

On the possibility of generating a 4-neutron resonance with T = 3/2 isospin 3-neutron forces

E. Hiyama

Nishina Center for Accelerator-Based Science, RIKEN, Wako, 351-0198, Japan

R. Lazauskas

IPHC, IN2P3-CNRS/Universite Louis Pasteur BP 28, F-67037 Strasbourg Cedex 2, France

J. Carbonell

Institut de Physique Nucléaire, Université Paris-Sud, IN2P3-CNRS, 91406 Orsay Cedex, France

M. Kamimura

Department of Physics, Kyushu University, Fukuoka 812-8581, Japan and Nishina Center for Accelerator-Based Science, RIKEN, Wako 351-0198, Japan (Dated: March 14, 2016)

> Submitted in PRC. We are waiting for referee comments.

$E_R = 0.83 \pm 0.65 \pm 1.25$ F=2.6 MeV (Upper limit)

For the study of tetraneutron system

We should consider interaction and method:

NN interaction: realistic NN interaction Method: They reported the energy of tetraneutron was bound energy region to resonant energy region. Especially, for the resonant energy region, we should use Complex scaling method.

For this purpose, we use AV8 NN interaction (central, LS, Tensor). The NN potential is applicable for complex scaling method.

Any other missing part in our Hamiltonian? We need T=3/2 three-nucleon force. R. Lazauskas, and J. Carbonell, Phys. Rev. C72, 034003 (2005). S.C. Peiper et al., Phys. Rev. Lett. 90, 252501 (2003). As for 3 nucleon forces, we have Illinois potentials, for example. However, this potential is too complicated to use in order to get resonant state with CSM.

At present, we use a simple potential. For this purpose, we use the following shape.

$$V_{ijk}^{3N} = \sum_{T=1/2}^{3/2} \sum_{n=1}^{2} W_n(T) e^{-(r_{ij}^2 + r_{jk}^2 + r_{ki}^2)/b_n^2} \mathcal{P}_{ijk}(T)$$

$$W_1(T = 1/2) = -2.04 \text{ MeV}$$
 $b_1 = 4.0 \text{ fm}$
 $W_2(T = 1/2) = +35.0 \text{ MeV}$ $b_2 = 0.75 \text{ fm}$

Two range Gaussian potentials Four parameters are fixed so as to reproduce the low-energy properties of 3 H, 3 He and 4 He(T=0). To answer these issues, We employ AV8 NN potential + a phenomenological three-body force.

$$V_{ijk}^{3N} = \sum_{T=1/2}^{3/2} \sum_{n=1}^{2} W_n(T) e^{-(r_{ij}^2 + r_{jk}^2 + r_{ki}^2)/b_n^2} \mathcal{P}_{ijk}(T)$$
$$W_1(T = 1/2) = -2.04 \text{ MeV} \quad b_1 = 4.0 \text{ fm}$$
$$W_2(T = 1/2) = +35.0 \text{ MeV} \quad b_2 = 0.75 \text{ fm}$$

These parameters (W_1 , W_2 , b_1 , b_2) are determined so as to reproduce the binding energies of the ground states of ³H, ³He and ⁴He.

For 4n system, we need T=3/2 three-body force. We use the same potential with T=1/2, but, different parameter of W₁.

 $W_1(T=3/2)=$ free $b_1=4.0$ fm $=> W_1$ should be tuned so as to reproduce the observed 4n system $W_2(T=3/2) = +35$ MeV $b_2=0.75$



In order to reproduce the data of 4n system, We need W_1 = -36 MeV~-30MeV.

Attraction is 15 times Stronger.

It should be noted that W1=-2.04 MeV to reproduce the observed binding energy of 4 He, 3 He and 3 H.

Question: W_1 value for T=3/2 is reasonable?

To check the validity of three-body force, we calculate the energies of ${}^{4}\text{H}, {}^{4}\text{He}(\text{T}=1), {}^{4}\text{Li}$.





Table 4.1: Energy levels of $^4{\rm H}$ defined for channel radius $a_{\rm n}=4.9$ fm. All energies and widths are in the cm system.

$E_{\rm x}$ (MeV)	J^{π}	Т	Γ (MeV)	Decay	Reactions
g.s. ^a	2^{-}	1	5.42	n, ³ H	1, 11
0.31	1-	1	6.73 ^b	n, ³ H	11, 12
2.08	0-	1	8.92	n, ³ H	
2.83	1-	1	12.99 °	n, ³ H	11, 12

 $^{\rm a}$ 3.19 MeV above the n + $^{\rm 3}{\rm H}$ mass.

^b Primarily ³P₁.

^c Primarily ¹P₁.



Table 4.24: Energy levels of ⁴Li defined for channel radius $a_{\rm p}=4.9$ fm. All energies and widths are in the c.m. system.

$E_{\rm x}$ (MeV)	J^{π}	Т	Γ (MeV)	Decay	Reactions
g.s. ^a	2^{-}	1	6.03	p, ³ He	3
0.32	1-	1	7.35 ^b	p, ³ He	3
2.08	0-	1	9.35	p, ³ He	3
2.85	1-	1	13.51 °	p, ³ He	3

 $^{\rm a}$ 4.07 MeV above the p + $^{\rm 3}$ He mass.

^b Primarily ³P₁.

^c Primarily ¹P₁.



- Exp. ⁴H (-5.29 MeV)

If we use W_1 =-36MeV~-30 MeV to reproduce the observed data of 4n, We have strong binding energies of ⁴H, ⁴He (T=1) and ⁴Li. This result is inconsistent with the data of A=4 nuclei. The J=2⁻ state of A=4 nuclei should be resonant states. How do we consider this inconsistency?

•The T=3/2 force is just a phenomenological.

$$V_{ijk}^{3N} = \sum_{T=1/2}^{3/2} \sum_{n=1}^{2} W_n(T) e^{-(r_{ij}^2 + r_{jk}^2 + r_{ki}^2)/b_n^2} \mathcal{P}_{ijk}(T)$$

Should we consider spin-dependent term in three-body force? Tensor force, spin-orbit force???

The confirmation experiment for 4n will be performed this year at RIBF. I am waiting for this confirmation.

If the experiment for 4n is confirmed to have a bound state or resonant state, ...



${}^{5}_{\Lambda}$ n should be bound!

This is important to study $\Lambda N-\Sigma N$ coupling . Then, I hope that production of ${}^{5}_{\Lambda}n$ will be performed at JLab using decay pion spectroscopy in the future. ⁷He ^ PR(20

PRC91, 054316 (2015)



¹E. Hiyama and M. Isaka ¹Nishina Center for Accelerator-Based Science, Institute for Physical and Chemical Research (RIKEN), Wako 351-0198, Japan

> ^{1,2}M. Kamimura ²Department of Physics, Kyushu University, Fukuoka, 812-8581, Japan

T. Myo General Education, Faculty of Engineering, Osaka Institute of Technology, Osaka, 535-8585, Japan

T. Motoba

Laboratory of Physics, Osaka Electro-Communication University, Neyagawa 572-8530, Japan Yukawa Institute for Theoretical Physics, Kyoto University, Kyoto 606-8317, Japan

The structure of neutron-rich Λ hypernucleus, $\frac{1}{\Lambda}$ He is studied within the framework of $\alpha + \Lambda + n + n$ four-body cluster model. We predict second $3/2^+$ and $5/2^+$ states as narrow resonant states to be 0.03 MeV and 0.07 MeV with width $\Gamma \sim 1$ MeV with respect to $\alpha + \Lambda + n + n$ threshold which correspond to the second 2^+ state of ⁶He coupled to $0s \Lambda$. By estimation of differential cross section of ${}^{7}\text{Li}(\gamma, K^+)^{7}_{\Lambda}$ He, there is a possibility to observe these state at JLab in the future. We also calculate second 2^+ state of ⁶He as resonant state within the framework of $\alpha + n + n$ three-body cluster model. Our result is 2.81 MeV with $\Gamma = 4.63 MeV$ with respect to $\alpha + n + n$ threebody, which is inconsistent with the recent SPIRAL data. It is suggested that search experiment at JLab of the second $3/2^+$ and $5/2^+$ states of $^{7}_{\Lambda}$ He would provide an opportunity to confirm the second 2^+ state of the core nucleus ${}^{6}_{1}$ He.



⁷He



⁶He : One of the lightest n-rich nuclei

⁷He: One of the lightest n-rich hypernuclei

Observed at JLAB, Phys. Rev. Lett. 110, 12502 (2013). CAL: E. Hiyama et al., PRC 53, 2075 (1996), PRC 80, 054321 (2009)



$^{7}Li(e,e'K^{+})^{7}_{\Lambda}He$



The calculated energy of the excited state is in good agreement with the data.

Question: In 7 He, do we have any other new states? If so, what is spin and parity?

First, let us discuss about energy spectra of ⁶He core nucleus.





Only GANIL group observed this state. Other experimental groups failed to observe it. How do we confirm this state?

> $\Gamma = 1.6 \pm 0.4 \text{ MeV}$ 2^+_2 1.6 ± 0.3 MeV



 $\Gamma=0.12 \text{ MeV} \\ 2_{1} \\ 0 \text{ MeV} \\ \alpha+n+n \\ -0.98 \\ 0+ \\ 6 \text{He} \\ Exp. \\ \text{bto in 2012} \\ 0 \\ 1 \\ 0.8 \text{ MeV} \\ 0.8 \text{ MeV}$

Data in 2012 X. Mougeot et al., Phys. Lett. B 718 (2012) 441. p(⁸He, t)⁶He

Γ=0.14 MeV ²⁺///////// 0.8 MeV 0 MeV α +n+n -0.98 0+⁶He Cal.

I propose to measure $3/2^+$, $5/2^+$ states in 7 _AHe at JLab.



Cal.



If we observe second 5/2⁺,3/2⁺ states in $^{7}_{\Lambda}$ He at JLab, we can confirm the second 2⁺ state in 6 He.

In this way, hypernuclear physics can contribute to unstable nuclear physics.

Summary

I suggest to measure the following three hypernuclei.

(1) 1⁺ state of ${}^4_{\Lambda}H$

Important to obtain information on CSB effect.

(2) ⁵_^n

Important to obtain information on $\Lambda N\text{-}\Sigma N$ coupling , T=3/2 three-body force and to confirm the existence of 4n

(3) The second 3/2+,5/2+ states in $^{7}_{\Lambda}$ He

Important to confirm the second 2+ state of 6He This is a great contribution to unstable nuclear physics. 'bridge physics of hypernuclei and unstable nuclei'

I hope to have these new data at JLab in the future.

Thank you!