

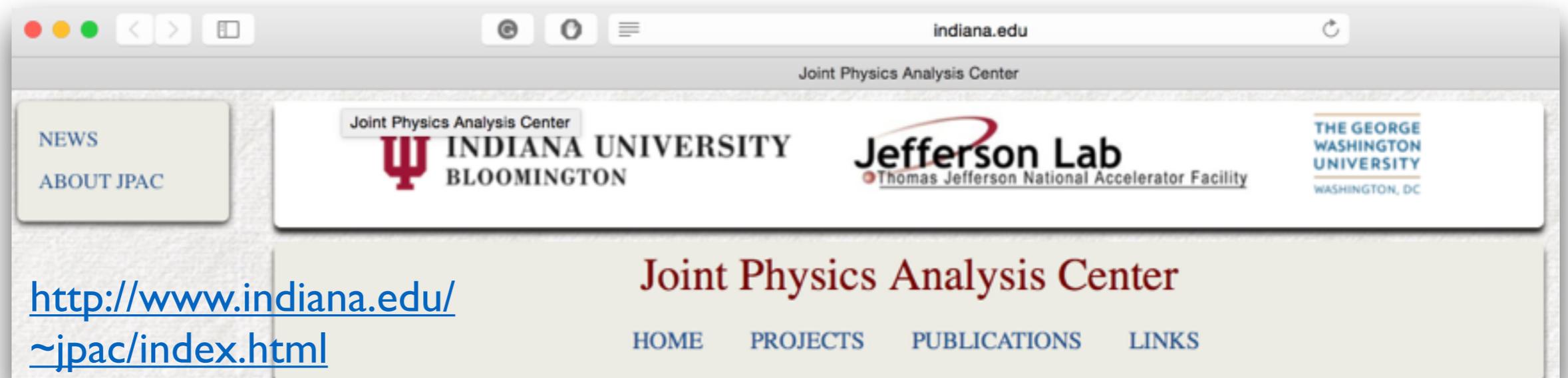
Hyperon Studies at JPAC

Who we are
and what we do

Hyperon Studies

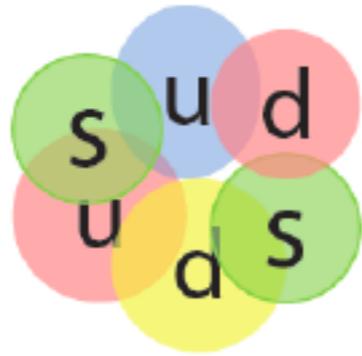
General approach:
Role of reaction
theory

Adam Szczepaniak
Indiana University
Jefferson Lab

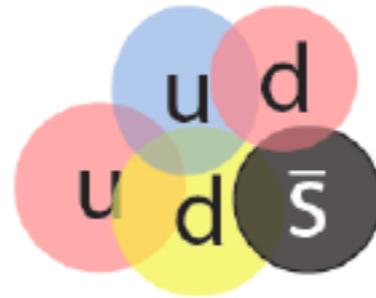


The screenshot shows a web browser window with the URL <http://www.indiana.edu/~jpac/index.html>. The page header includes the text "Joint Physics Analysis Center" and the logos for Indiana University Bloomington, Jefferson Lab (Thomas Jefferson National Accelerator Facility), and The George Washington University. The main content area features the text "Joint Physics Analysis Center" in a large, dark red font, with navigation links for "HOME", "PROJECTS", "PUBLICATIONS", and "LINKS" below it. On the left side, there are buttons for "NEWS" and "ABOUT JPAC".

There may be hadrons that look like ...



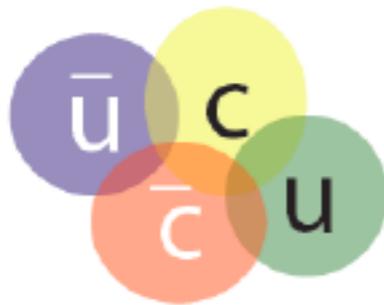
dibaryon



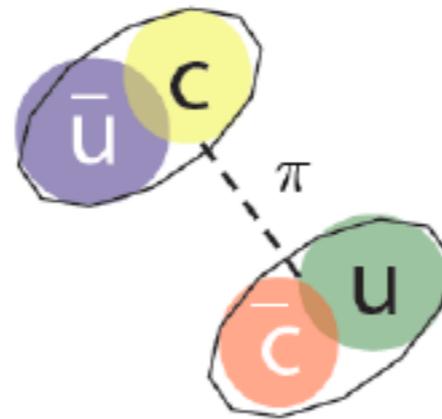
pentaquark



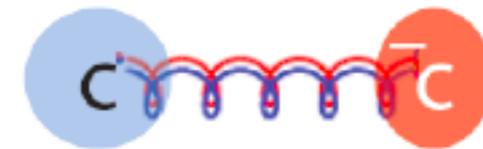
glueball



diquark + di-antiquark



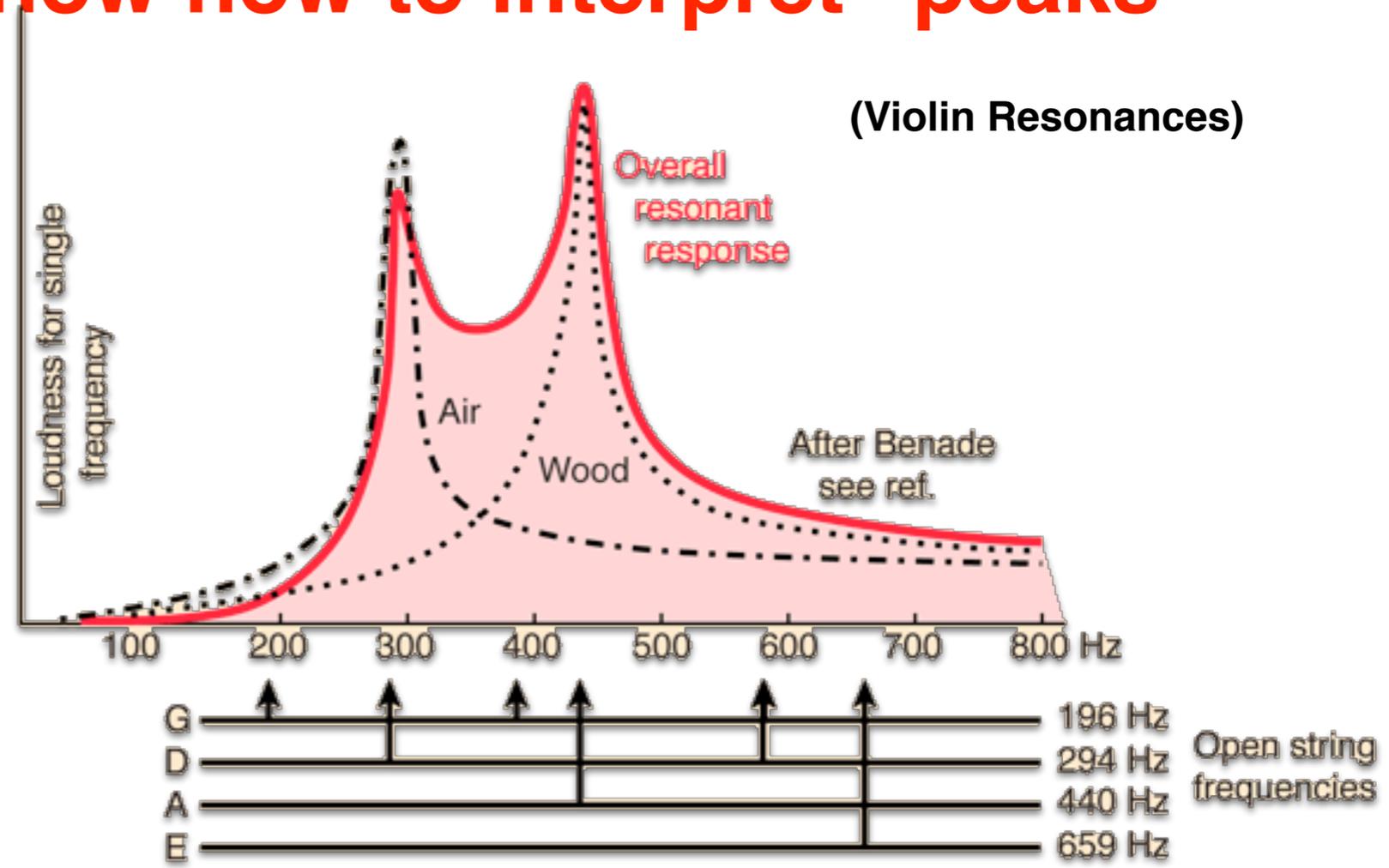
dimeson molecule



$q \bar{q} g$ hybrid

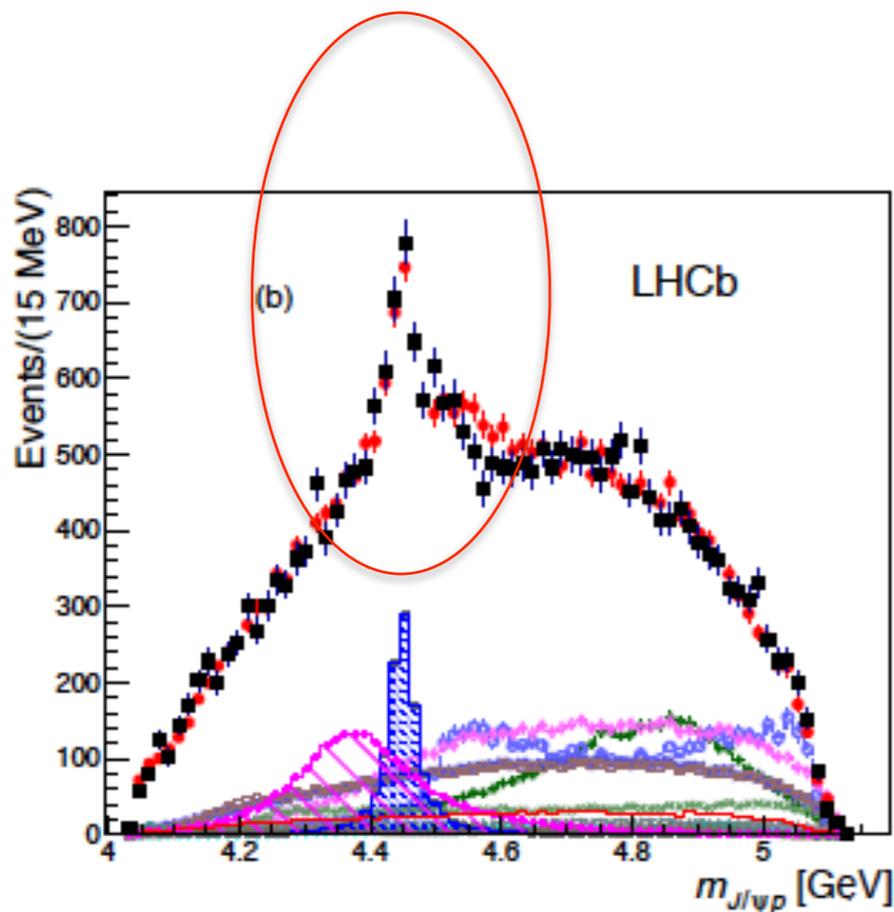
...but before we know this it is necessary to identify resonances

...we need to know how to interpret “peaks”



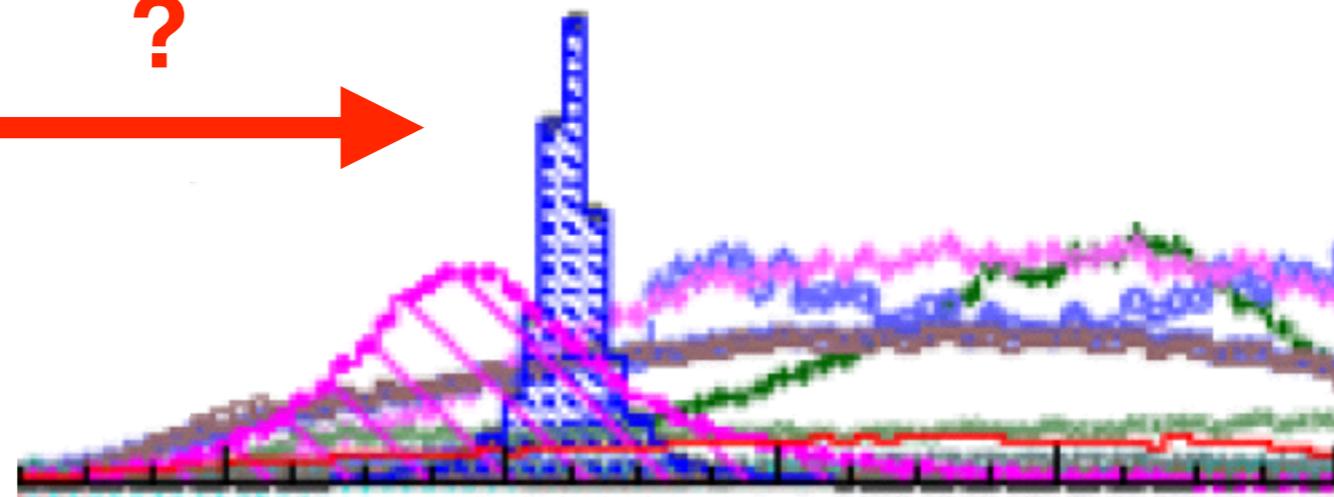
$$\Lambda_b \rightarrow K^- p J/\psi$$

a resonance in pJ/ψ ?

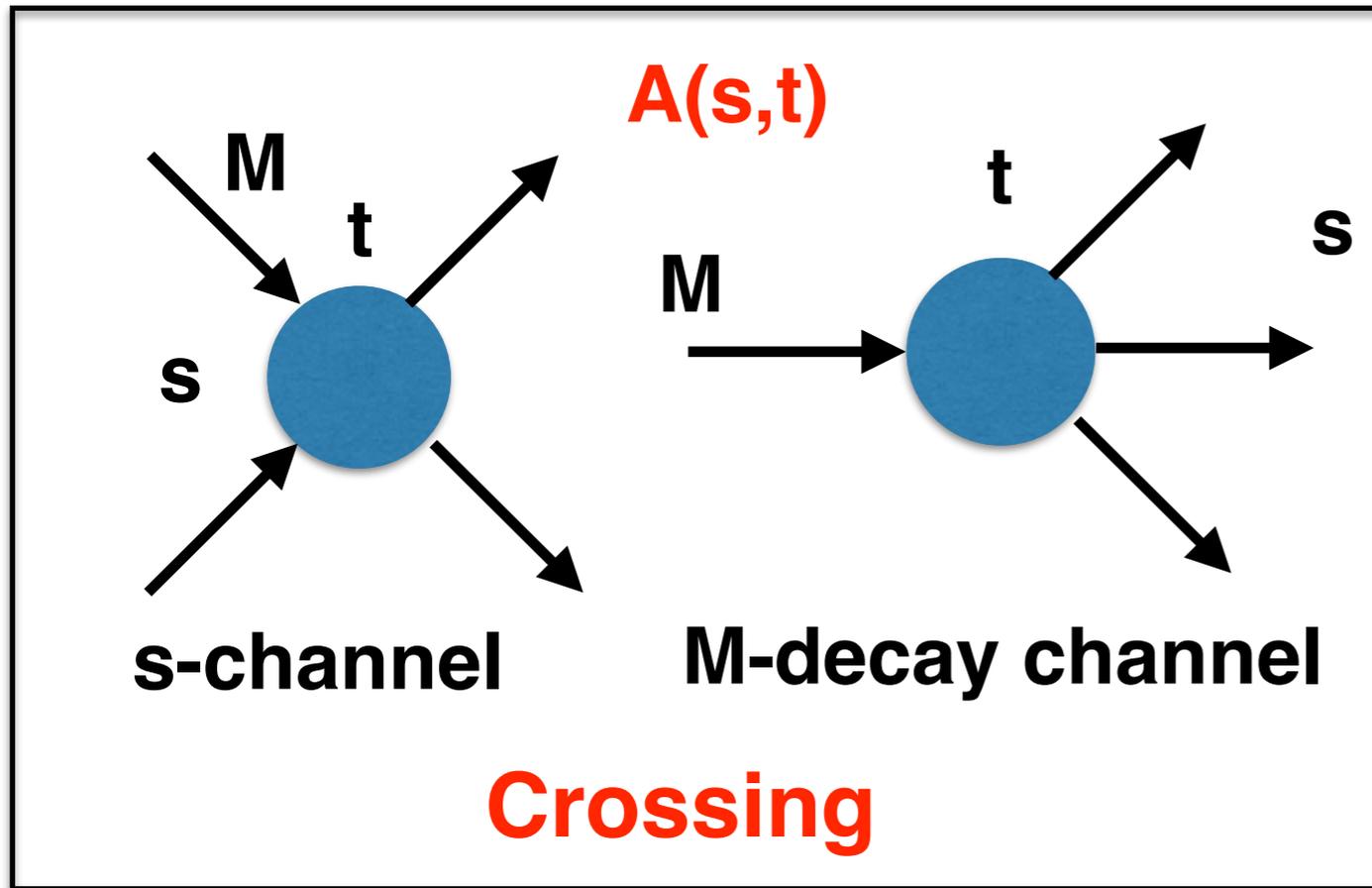


... or a $\bar{K} p$ reflection ?

?



S-matrix principles: Crossing, Analyticity, Unitarity



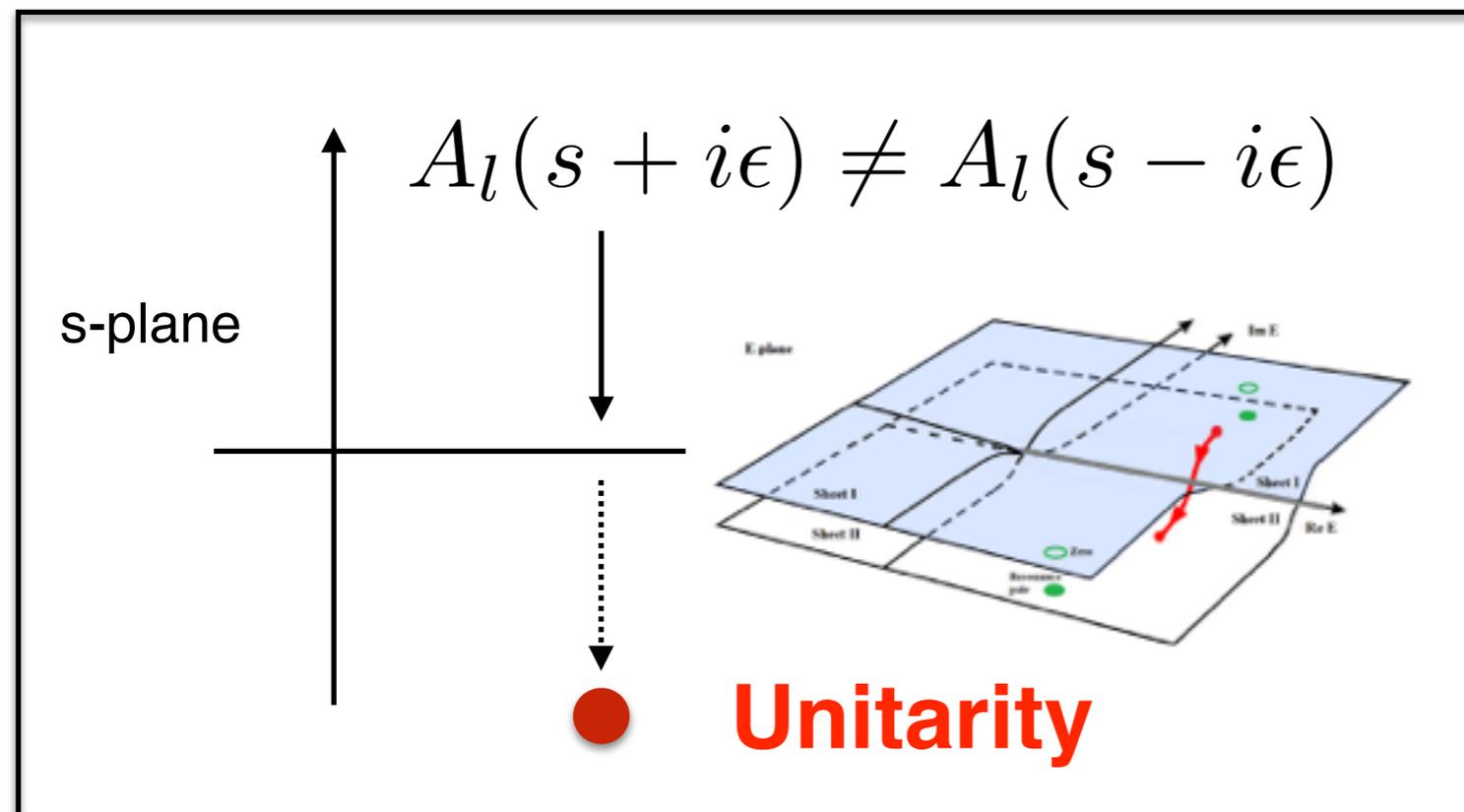
$$A(s, t) = \sum_l A_l(s) P_l(z_s)$$

Analyticity

$$A_l(s) = \lim_{\epsilon \rightarrow 0} A_l(s + i\epsilon)$$

**bumps/peaks on the
real axis (experiment)
come from
singularities in
unphysical sheets**

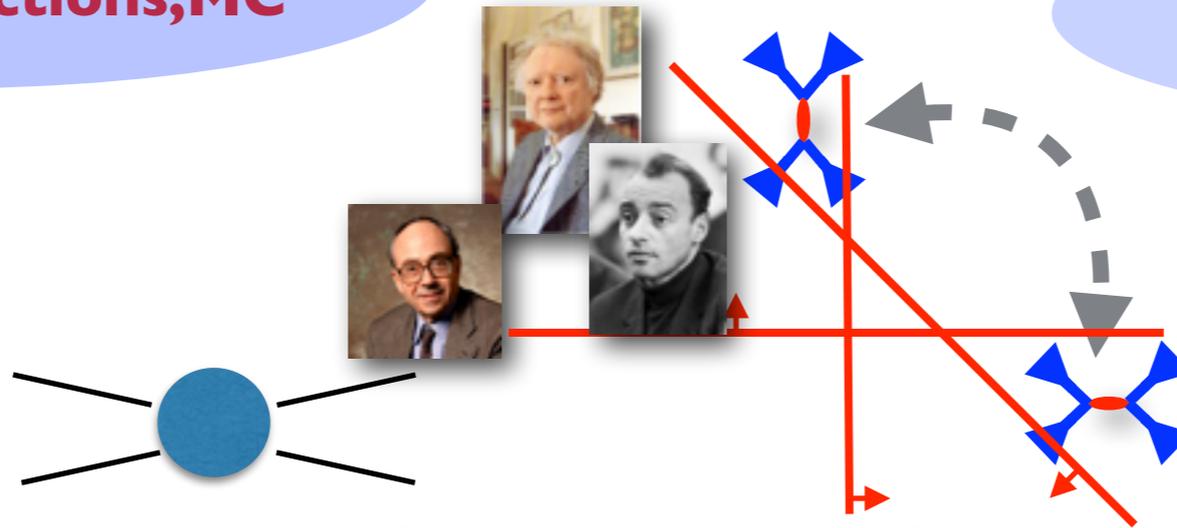
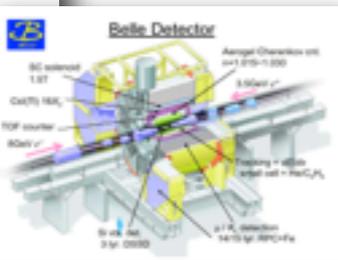
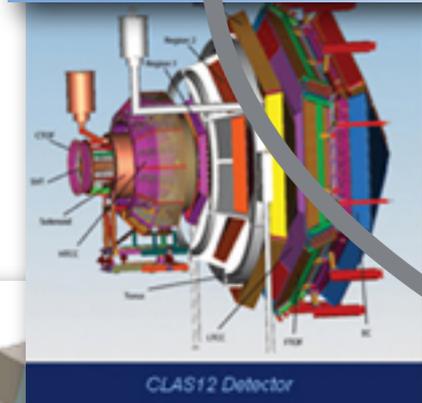
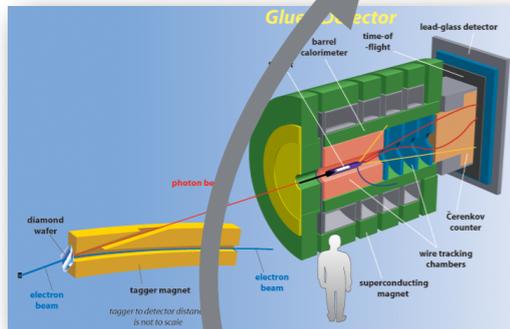
**These singularities
come from QCD**



Amplitude Analysis @ JPAC

Events, X-sections, MC

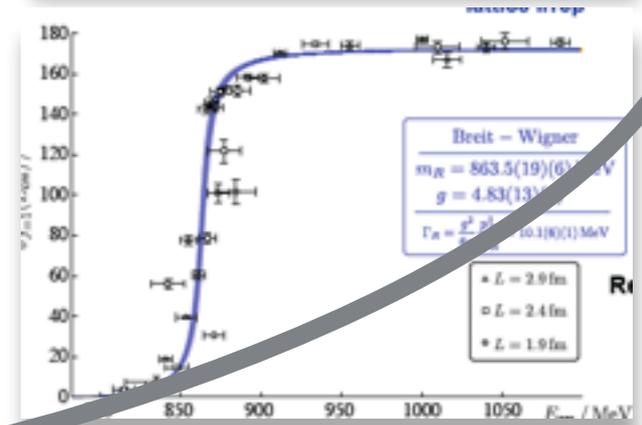
QCD Predictions



$$A(s, t) = \sum_{l=0}^{\infty} f_l(s) P_l(z_s) = \sum_{l=0}^{\infty} g_l(t) P_l(z_t)$$

Amplitude analysis:
based on S-matrix principles:

- analyticity
- unitarity
- crossing

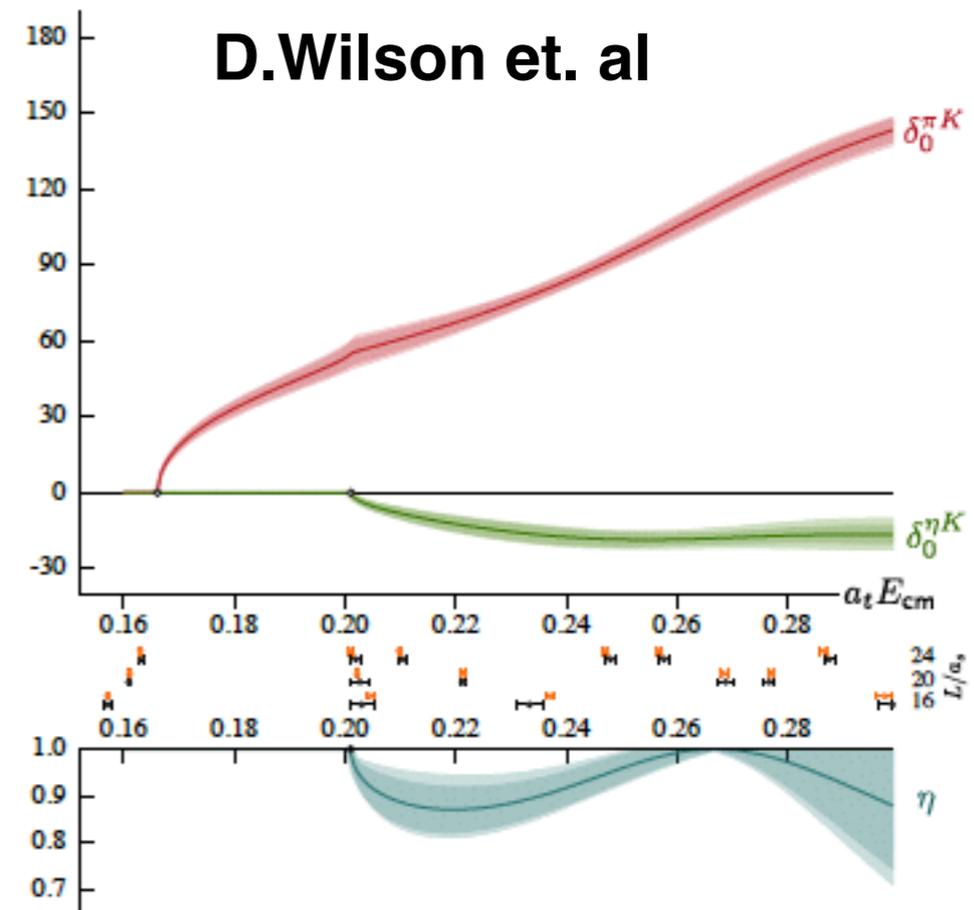
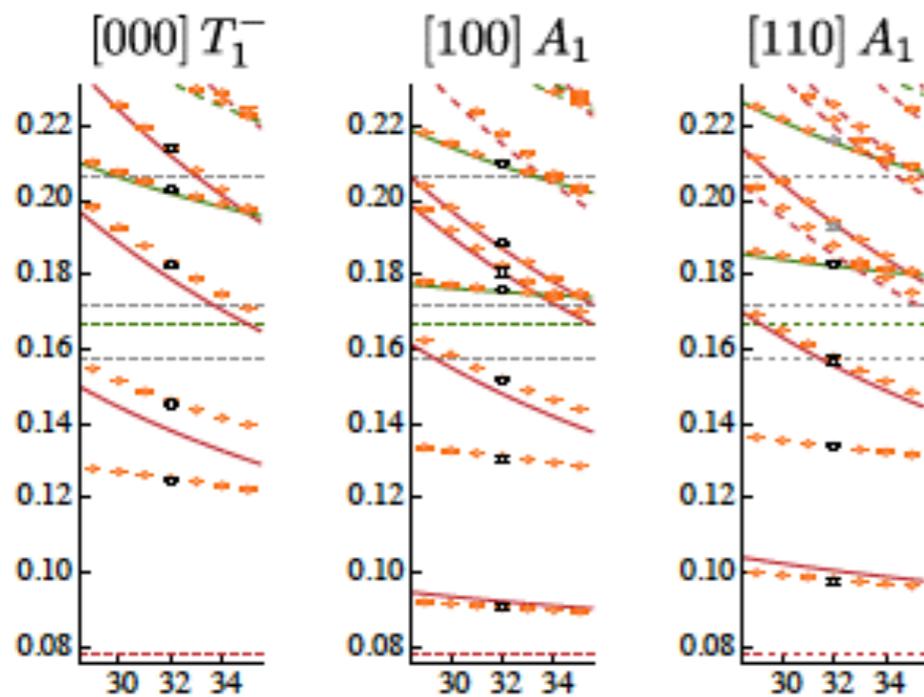


Global effort
JLab/IU/GWU Physics Analysis Center

QCD on the Lattice : simulated scattering experiment

(known kinematical function) $Z(E_i = \text{"data"}) = T(E_i)$ (infinite volume amplitude)

E_i = discrete energy spectrum of states in the lattice



in general "solution" of the Lusher condition requires an analytical model for T

JPAC : Example of Analysis Projects

Light meson decays and light quark resonance

$\omega/\phi \rightarrow 3\pi, \pi\gamma$ (dispersive)

$\omega \rightarrow 3\pi$ (Veneziano, B4)

$\eta \rightarrow 3\pi, \eta'/f_1 \rightarrow \eta\pi\pi$, (Khuri-Treiman, B4)

$J/\psi \rightarrow \gamma\pi^0\pi^0$

Photo-production: (production models, FESR and duality)

$\gamma p \rightarrow \pi^0 p$

$\gamma p \rightarrow pK^+K^-$ (and Kp)

$\gamma p \rightarrow \pi^+\pi^-p, \pi^0\eta p, \omega p$

**Launched in the Fall
of 2013**

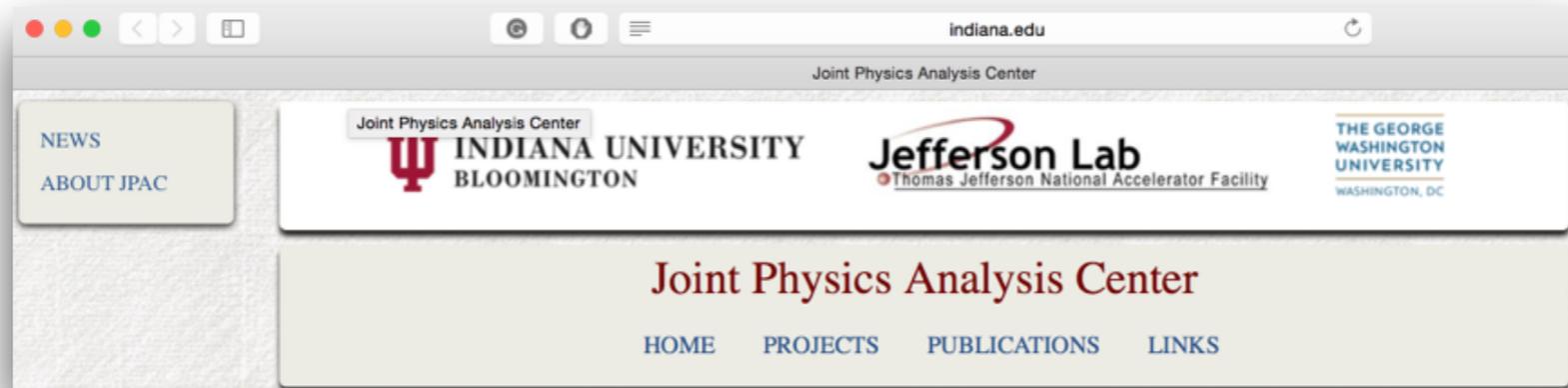
**>20 analysis/papers
published**

Exotica and XYZ's:

$\pi^-p \rightarrow \pi^-\eta p$ & $\pi^-p \rightarrow \pi^-\eta' p$ (FESR)

$B^0 \rightarrow \psi' \pi^- K^+ u, \psi(4260) \rightarrow J/\psi \pi^+\pi^-, \Lambda_b \rightarrow K^- p J/\psi$

$J/\psi \rightarrow 3\pi, KK\pi$ (Veneziano, B4)



<http://www.indiana.edu/~jpac/>

Adam Szczepaniak (IU/JLab)
Mike Pennington (JLab)
Tim Londergan (IU)
Geoffrey Fox (IU)
Emilie Passemar (IU/JLab)
Cesar Fernandez-Ramirez
(JLab → Mexico)
Vincent Mathieu (IU)
Micheal Doering (GWU)
Ron Workman (GWU)

BESIII collaboration

Medina Ablikim (Beijing)
Ryan Mitchell, (IU)
...

LHCb collaboration

T.Skwarnicki (Syracuse)
J.Rademacker, (Bristol)
...

Vladyslav Pauk (Mainz → JLab)
Alessandro Pilloni (Rome → JLab)
Astrid Blin (Valencia)
Andrew Jackura (IU)
Lingyun Dai (IU/JLab → Valencia)
Meng Shi (JLab → Beijing)
Igor Danilkin (JLab → Mainz)
Peng Guo (IU/JLab → CSU)
...

COMPASS collaboration

Mikhail Mikhasenko (Bonn)
Fabian Krinner (TUM)
Boris Grube (TUM)
...

BaBar collaboration

Antimo Palano (Bari)
...

GlueX collaboration

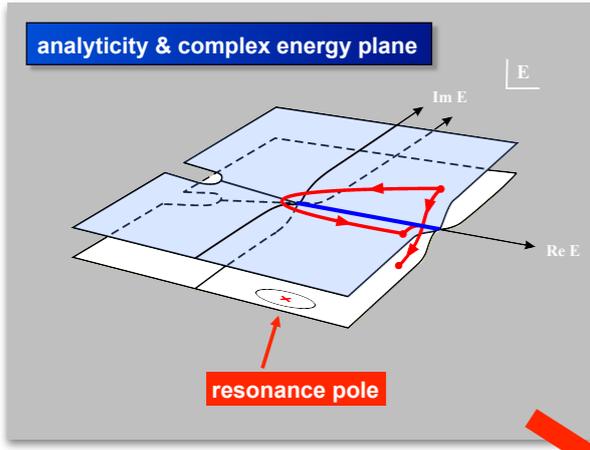
Matthew Shepherd (IU)
Justin Stevens (JLab)
...

CLAS collaboration

Diane Schott (GWU/JLab)
Viktor Mokeev (JLab)

HASPECT

Marco Battaglieri (Genova)
Derek Glazier (Glasgow)
Raffaella De Vita (Genoa)
...



special thanks to Vincent Mathieu



$\gamma p \rightarrow \pi^0 p$

- Formalism
- Model
- Resources
- Run

HOME PROJECTS PUBLICATIONS LINKS

INDIANA UNIVERSITY BLOOMINGTON

Jefferson Lab
Thomas Jefferson National Accelerator Facility

THE GEORGE WASHINGTON UNIVERSITY
WASHINGTON, DC

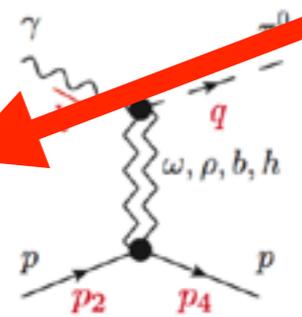
$\gamma p \rightarrow \pi^0 p$

We present the model published in [Mat15a].

The differential cross section for $\gamma p \rightarrow \pi^0 p$ is computed with Regge amplitudes in the domain $E_\gamma \geq 10$ GeV and $0.01 \leq |t| \leq 3$ (in GeV^2). The formalism can be extrapolated outside these intervals.

We use the CGLN invariant amplitudes A_i defined in [Chew57a]. See the section Formalism for the definition of the variables.

The fitting procedure is detailed in [Mat15a]. We report here only the main feature of the model.



Formalism

The differential cross section is a function of 2 variables. The first is the beam energy in the laboratory frame E_γ (in GeV) or the total energy squared s (in GeV^2). The second is the cosine of the scattering angle in the rest frame $\cos \theta$ or the momentum transferred squared t (in GeV^2).

The momenta of the particles are k (photon), q (pion), p_2 (target) and p_4 (recoil). The pion mass is μ and the proton mass is M . The Mandelstam variables, $s = (k + p_2)^2$, $t = (k - q)^2$, $u = (k - p_4)^2$ are related through $s + t + u = 2M^2 + \mu^2$.

The differential cross section is expressed in term of the parity conserving helicity invariant amplitudes in the t -channel F_i

$$\frac{d\sigma}{dt} = \frac{389.4}{64\pi} \frac{k_t^2}{4M^2 E_\gamma^2} \left[2 \sin^2 \theta_t (|F_1|^2 + 4p_t^2 |F_2|^2) + (1 - \cos \theta_t) (|F_3|^2 + 4p_t^2 |F_4|^2) \right]$$

The differential cross section is expressed in $\mu\text{b}/\text{GeV}^2$. We used $(\hbar c)^2$.

The t -channel is the rest frame of the process $\gamma \pi^0 \rightarrow p \bar{p}$.

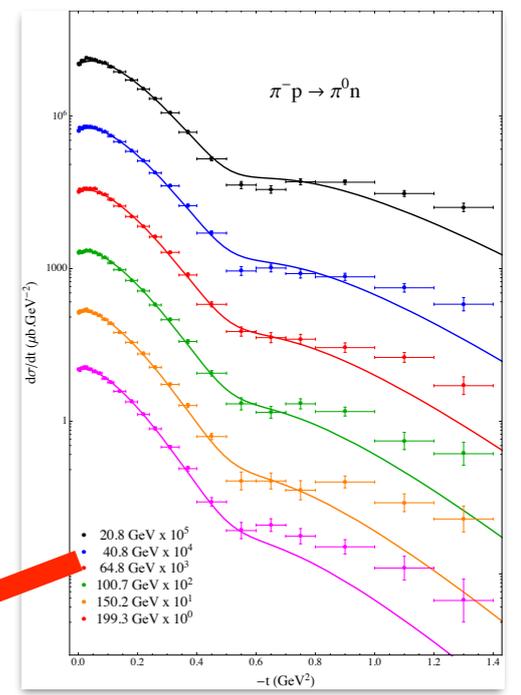
In the t -channel, the momenta of the nucleon p_t and the pion k_t and

$$k_t = \frac{1}{2} \sqrt{t - 4M^2}, \quad q_t = \frac{t - \mu^2}{2}$$

The invariant amplitudes F_i are related through the CGLN A_i amplitude

$$\begin{aligned} F_1 &= -A_1 + 2MA_4, & \eta & \\ F_2 &= A_1 + tA_2, & \eta & \\ F_3 &= 2MA_1 - tA_4, & \eta & \\ F_4 &= A_3 & \eta & \end{aligned}$$

The F_i amplitudes have good quantum numbers of the t -channel, the naturality $\eta = P(-1)^J$ and the product CP .



```
double complex function A(gamma,target,recoil,pip,pim,
,lambda_g,lambda_t,lambda_r,
, params)
implicit double precision (a-h,o-z)
dimension gamma(4)
dimension target(4)
dimension recoil(4)
dimension pip(4),pim(4)
dimension params(100)

double complex Ampl

s = (gamma(4)+target(4))**2 - (gamma(1)+target(1))**2
s = (gamma(2)+target(2))**2 - (gamma(3)+target(3))**2

s1 = (pip(4)+pim(4))**2 - (pip(1)+pim(1))**2
s = (pip(2)+pim(2))**2 - (pip(3)+pim(3))**2

s2 = (pip(4)+recoil(4))**2 - (pip(1)+recoil(1))**2
s = (pip(2)+recoil(2))**2 - (pip(3)+recoil(3))**2

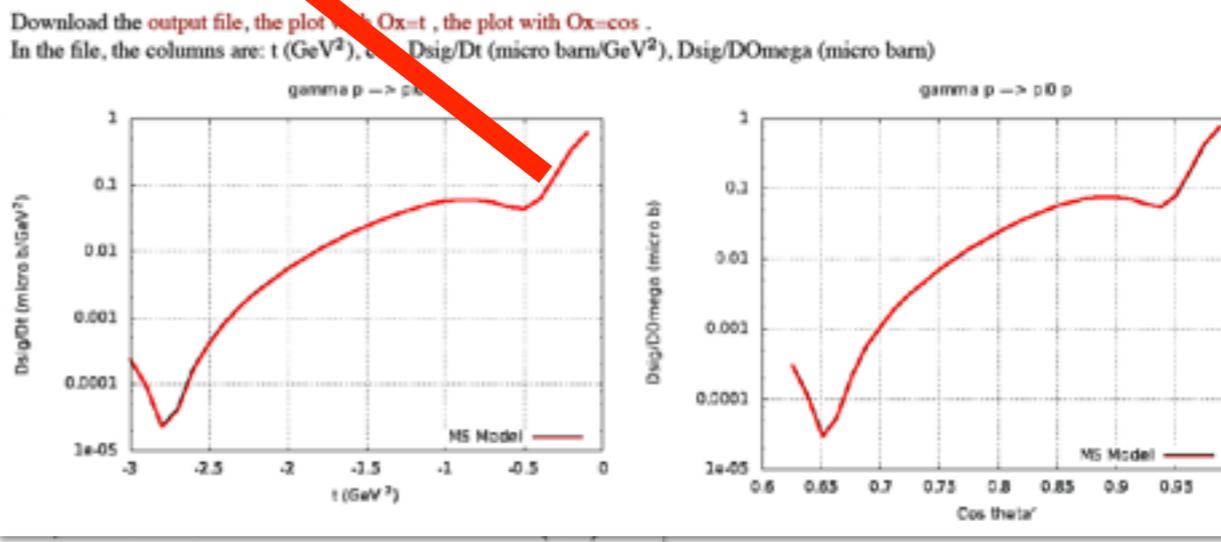
t1 = (gamma(4)-pim(4))**2 - (gamma(1)-pim(1))**2
s = (gamma(2)-pim(2))**2 - (gamma(3)-pim(3))**2

t1 = (target(4)-recoil(4))**2 - (target(1)-recoil(1))**2
s = (target(2)-recoil(2))**2 - (target(3)-recoil(3))**2

call Ath(s,s1,s2,t1,t2,lambda_g,lambda_t,lambda_r,params,Ampl)

A = Ampl

return
end
```



Hyperon Physics

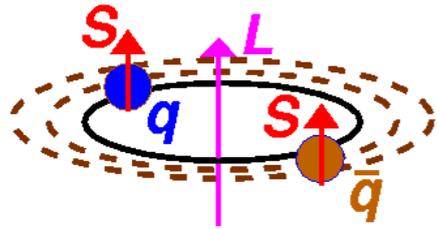
Bridge between light (u,d) and heavy (c,b) quark baryons

Test Quark Model vs QCD (lattice)

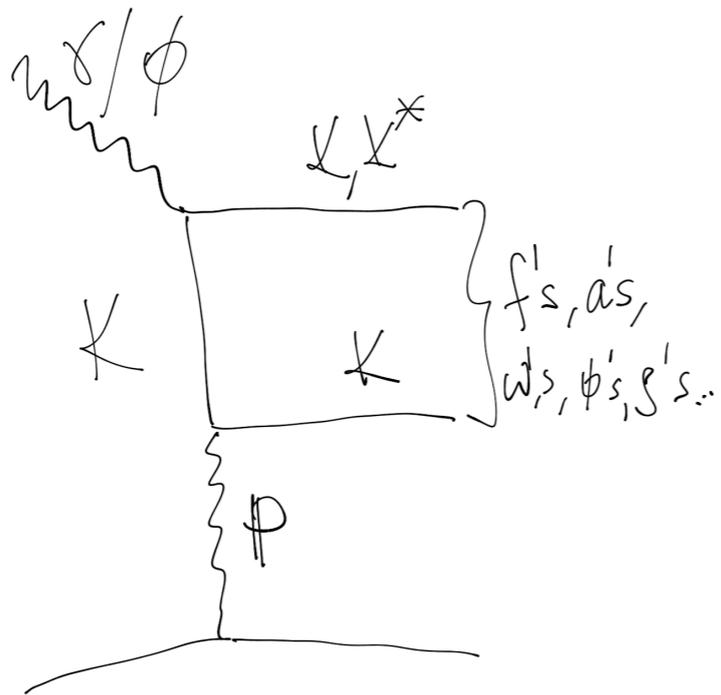
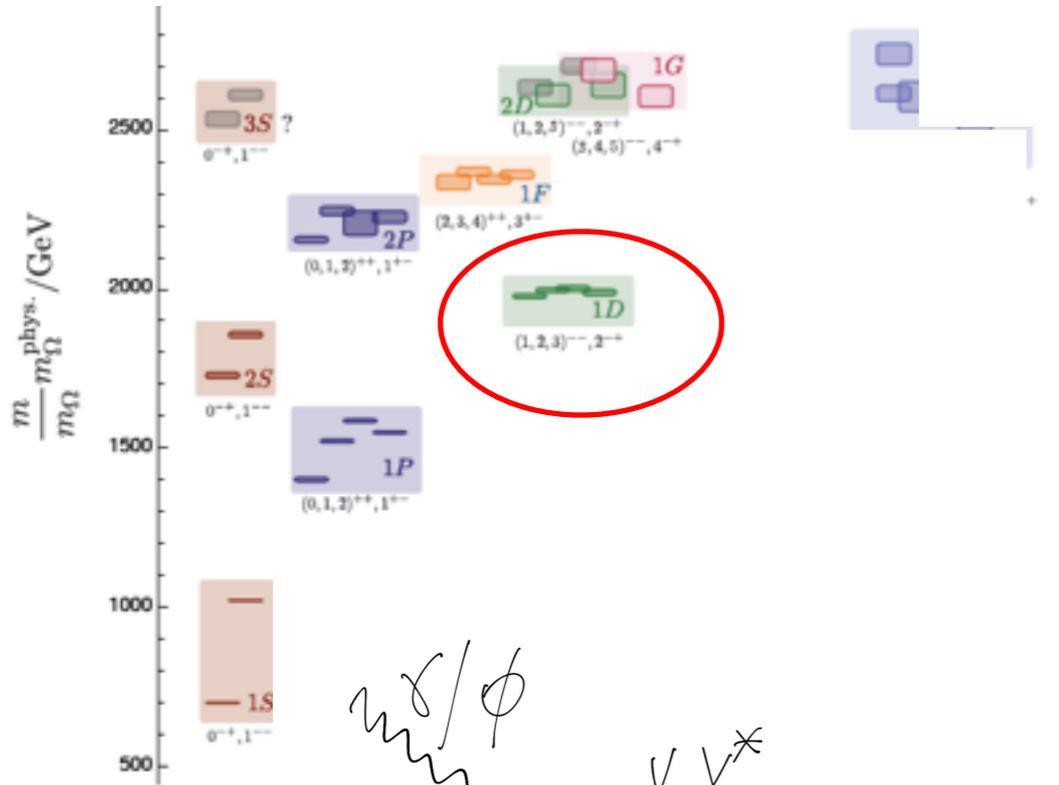
Photon couples to quarks is, glueballs , hybrids or use in associated production of K^* 's and Hyperons

Hyperon spectrum less understood e.g $\Lambda(1405)$ only recently pole positions have started to be reported by the PDG

Some quark model states have not been seen yet



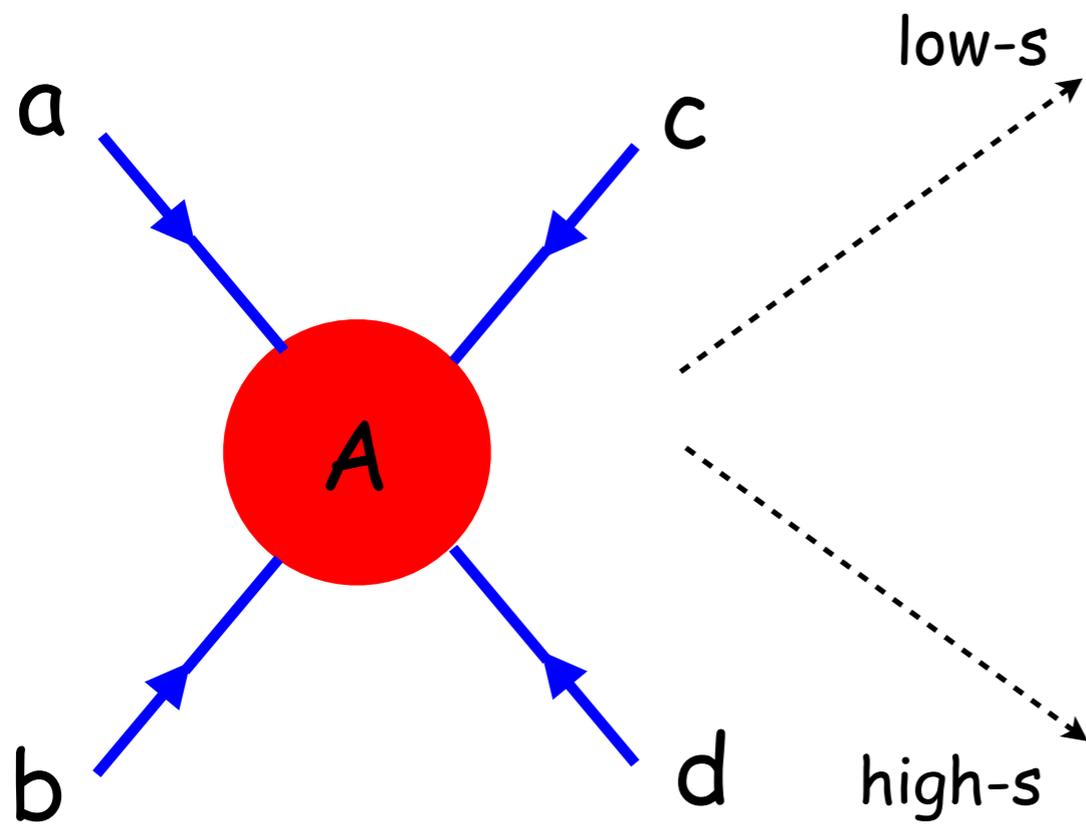
2^- ($L=2, S=1$)



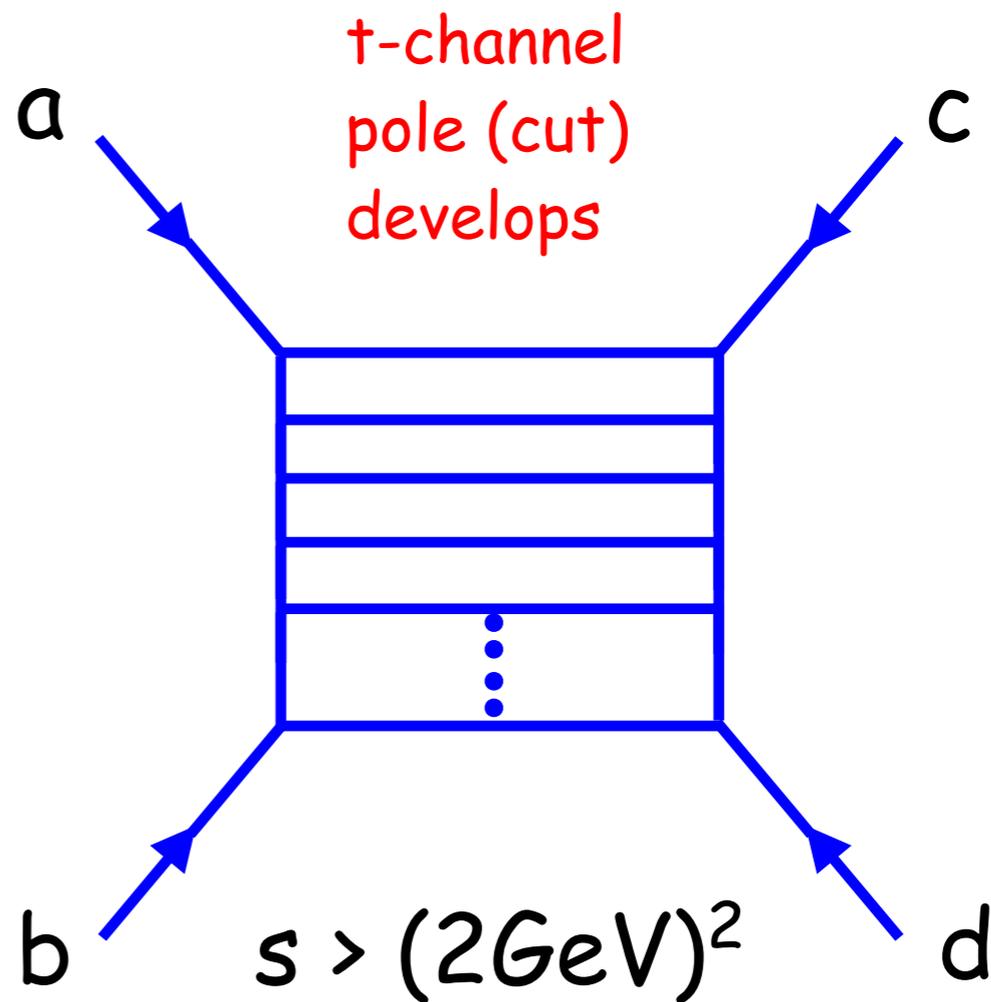
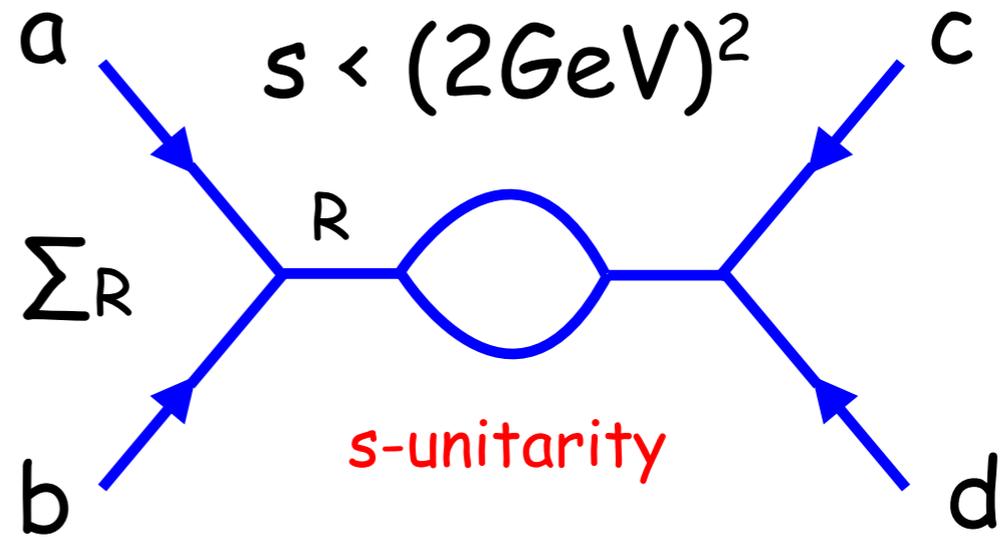
J^G	naturality $=P(-1)^J$	twist $=+1$ if $J=0,2,\dots$ $=-1$ if $J=1,3,\dots$	name
0^+	+1	+1	f_0, f_2, \dots
0^+	+1	-1	$\eta/\eta', \eta/\eta_3, \dots$ ($1^+, 3^+, \dots$)
0^+	-1	+1	$\eta/\eta', \eta/\eta_2, \dots$
0^+	-1	-1	f_1, f_3, \dots
0^-	+1	+1	h_0, h_2, \dots ($0^+, 2^+, \dots$)
0^-	+1	-1	$\omega/\phi_1, \omega/\phi_3, \dots$
0^-	-1	+1	$\omega/\phi_0, \omega/\phi_2, \dots$ ($0^-, 2^-, \dots$: not seen)
0^-	-1	-1	h_1, h_3, \dots
1^+	+1	+1	b_0, b_2, \dots ($0^+, 2^+, \dots$)
1^+	+1	-1	ρ_1, ρ_3, \dots
1^+	-1	+1	ρ_0, ρ_2, \dots ($0^-, 2^-, \dots$: not seen)
1^+	-1	-1	b_1, b_3, \dots
1^-	+1	+1	a_0, a_2, \dots
1^-	+1	-1	π_1, π_3, \dots ($1^+, 3^+, \dots$)
1^-	-1	+1	π, π_2, \dots
1^-	-1	-1	a_1, a_3, \dots

Analyticity is a powerful constraint

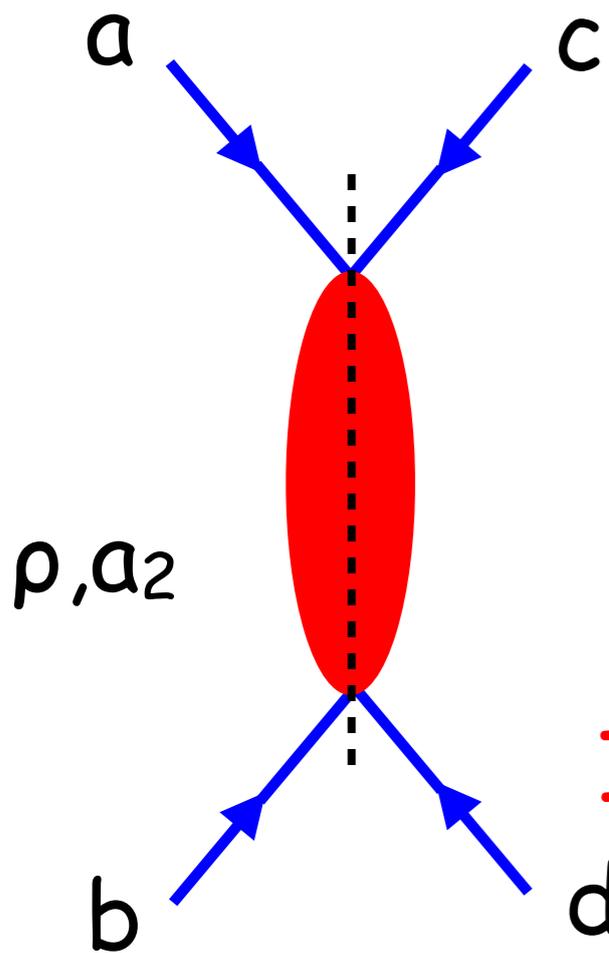
cf. Bonn/Gatchina, EBAC, Julich, Giessen, GWU, Mainz, Zagreb,)



cf. Regge phenomenology

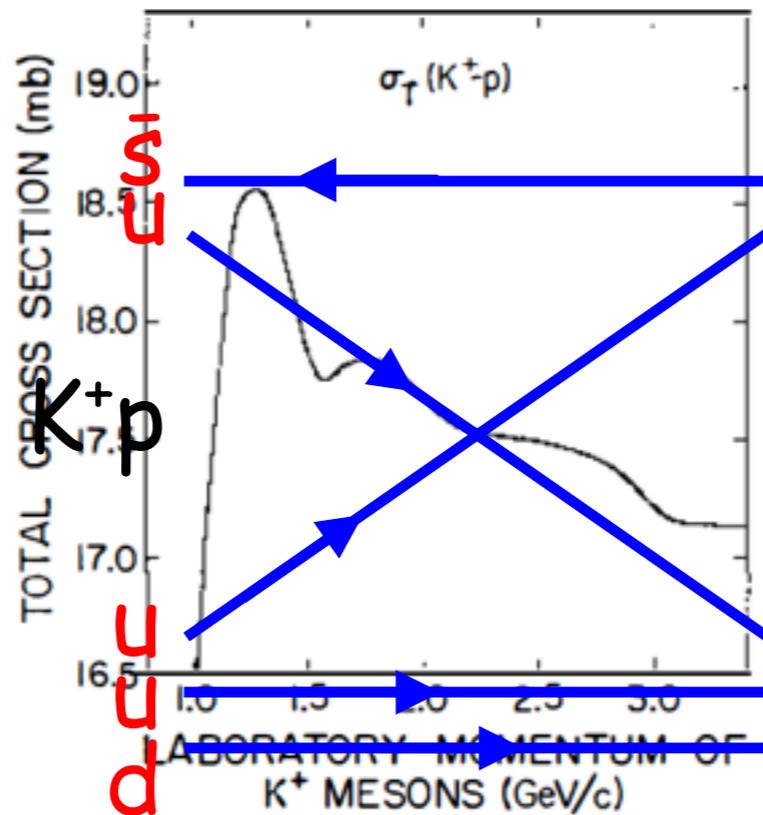


$$\text{Im } A_{\text{Regge}}(N,t)$$

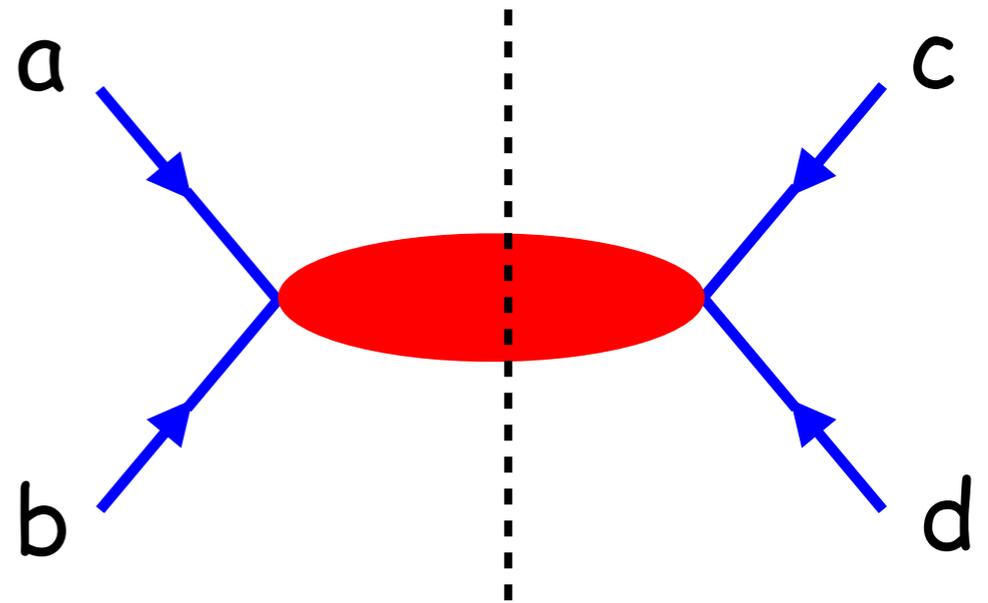


Can use cross-channel reggeons to study direct channel resonances

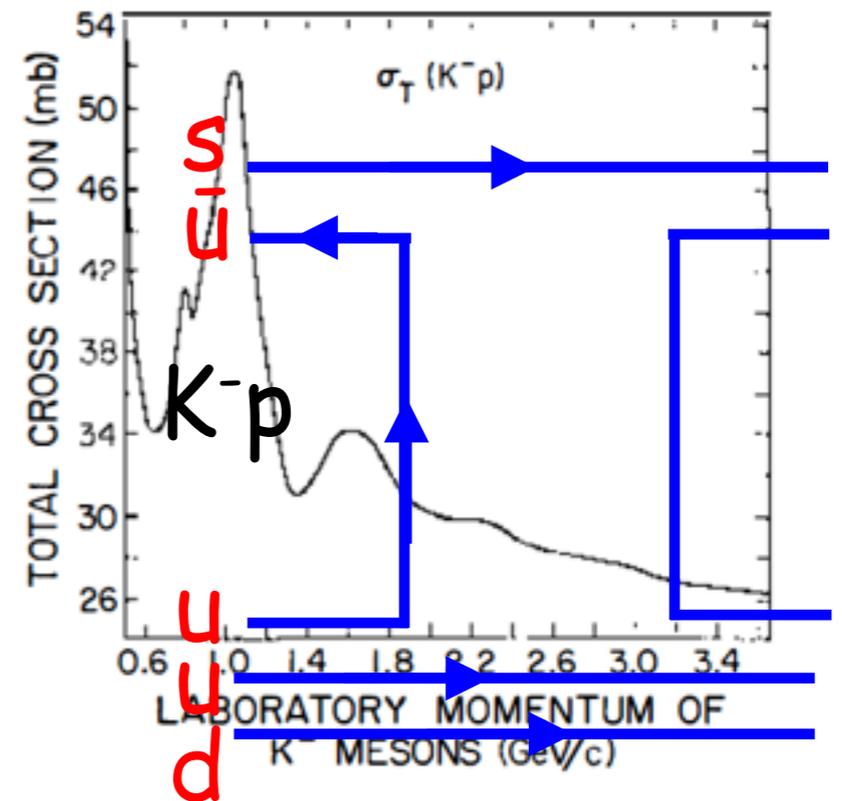
$$\text{Im } A(s,t) = 0$$



$$\int^N ds \text{Im } A(s,t)$$



$$\text{Im } A(s,t) \neq 0$$

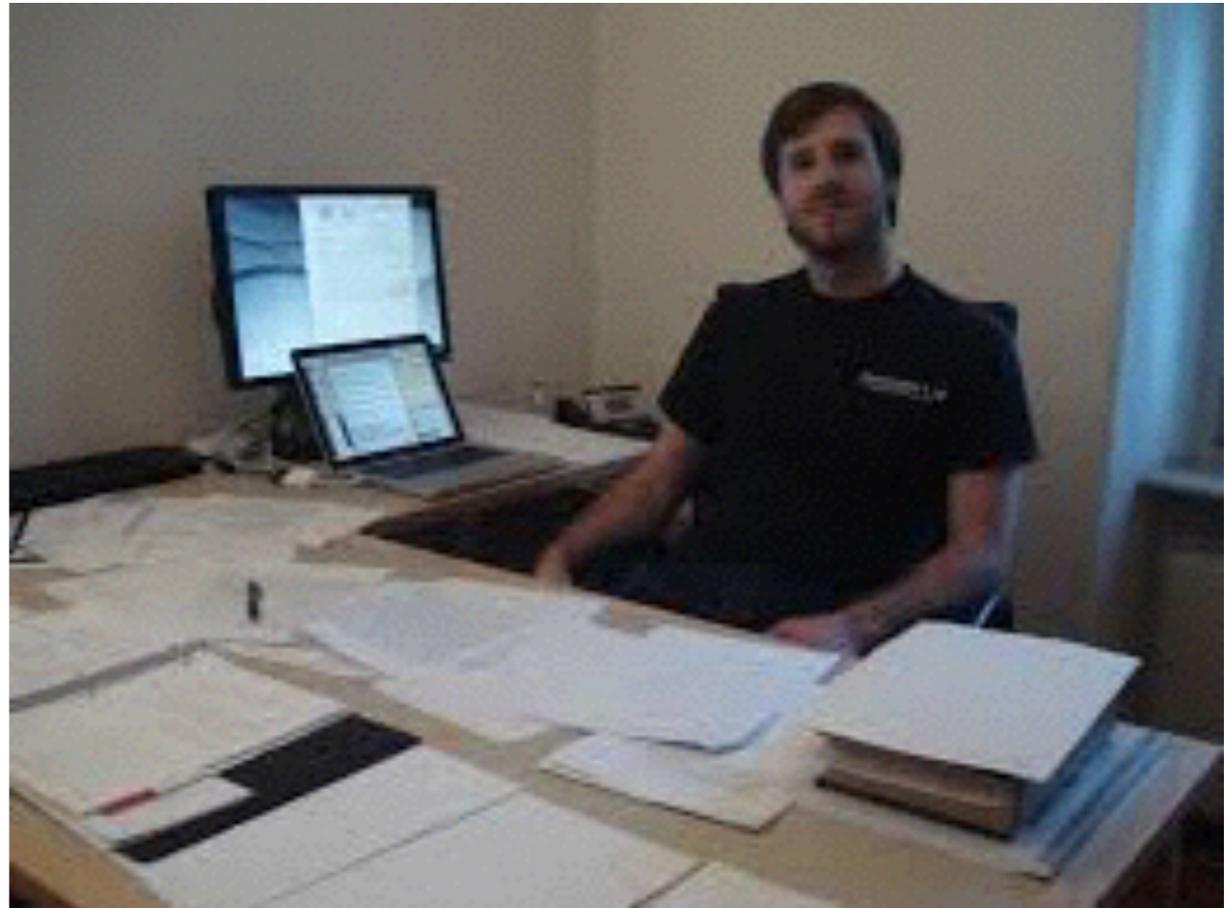


PWA for $\bar{K}N$

Model the amplitude

Fit to data

**Analytically continue to
complex values of
energy to search for
poles**



**Partial-wave analysis ($L_{\max}=5$), Coupled channels, Unitarity
Analyticity: Right threshold behavior (angular momentum
barrier), Resonances and backgrounds are incorporated “by-
hand” through K matrices**

**In the range $2.19 < s < 4.70$ GeV² (8000 data points, 7500 data
points, 5000 data points) We fit the KSU analysis single-
energy partial waves [Zhang et al., PRC 88, 035204 (2015)]
Caveat: we lose correlations among partial waves**

Cesar Fernandez Ramirez et al., arXiv:1510.07065 [hep-ph]

$$S_\ell = I + 2i [C_\ell(s)]^{1/2} T_\ell(s) [C_\ell(s)]^{1/2}$$

$$T_\ell(s) = [K^{-1}(s) - i\rho_\ell(s)]^{-1}$$

$$[i\rho_\ell(s)]_{kk} = \frac{s - s_k}{\pi} \int_{s_k}^{\infty} \frac{[C_\ell(s')]_{kk}}{s' - s} \frac{ds'}{s' - s_k}$$

$k = \pi\Sigma, \bar{K}N, \pi\Lambda, \pi\Sigma(1385), \pi\Lambda(1520), \eta\Sigma, \eta\Lambda, \bar{K}^*N, \pi\Delta(1232), \pi\pi\Sigma, \pi\pi\Lambda$

Resonance

$$[K_a(s)]_{kj} = x_k^a \frac{M_a}{M_a^2 - s} x_j^a$$

Generates pole in the
2nd Riemann sheet

Background

$$[K_b(s)]_{kj} = x_k^b \frac{M_b}{M_b^2 + s} x_j^b$$

Generates pole in the real
axis for $s < 0$ in the 1st Riemann sheet

Phase Space/Analyticity

$$[C_\ell(s)]_{kk} = \frac{q_k(s)}{q_0} \left[\frac{q_k^2(s)r^2}{1 + q_k^2(s)r^2} \right]^\ell$$

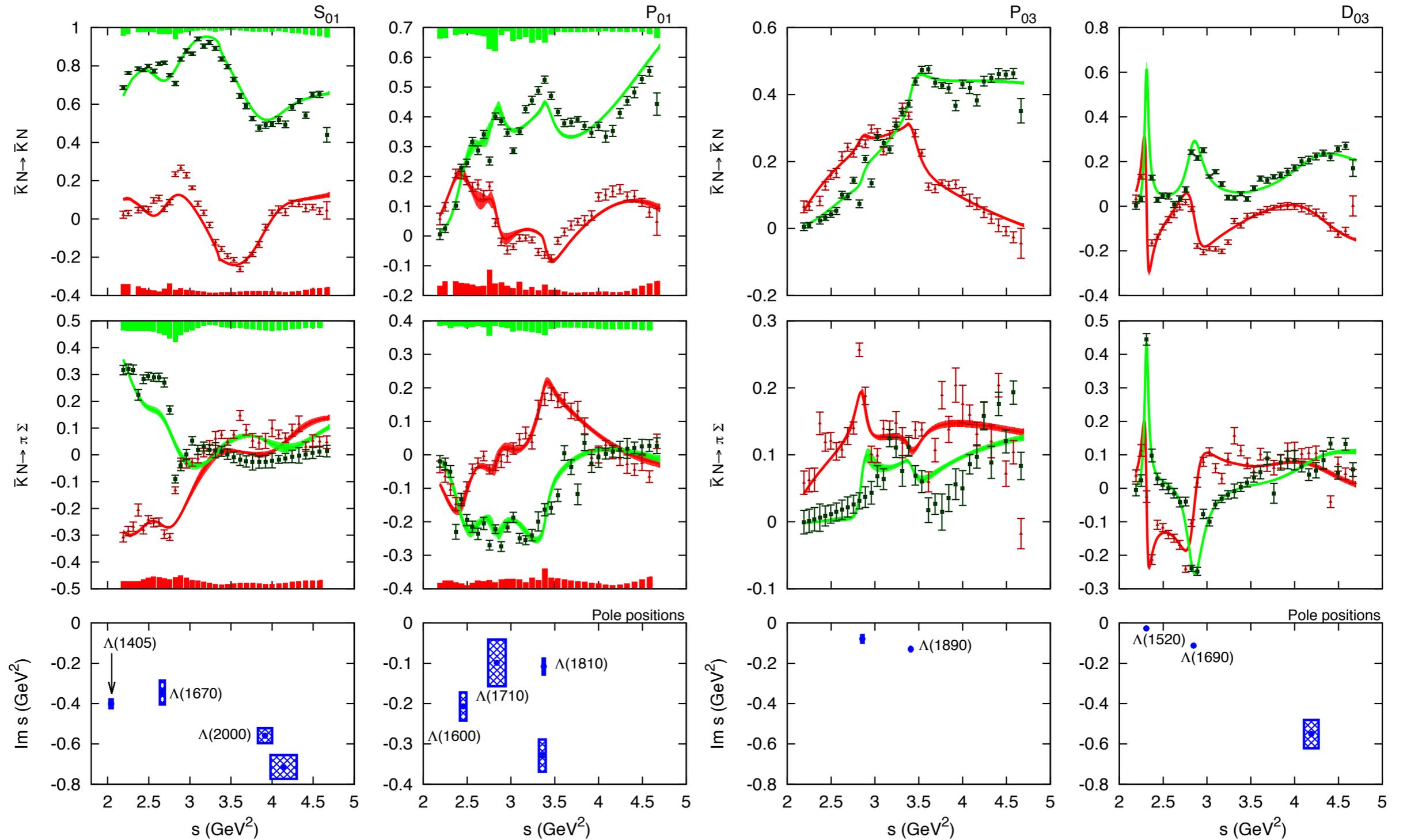
- ❖ Right threshold behavior
 - ❖ Angular momentum barrier
- ❖ Right high-energy behavior
- ❖ $r=1$ fm (interaction radius)

$$[q_k(s)]^2 = \frac{m_1 m_2}{s_k} [s - s_k]$$

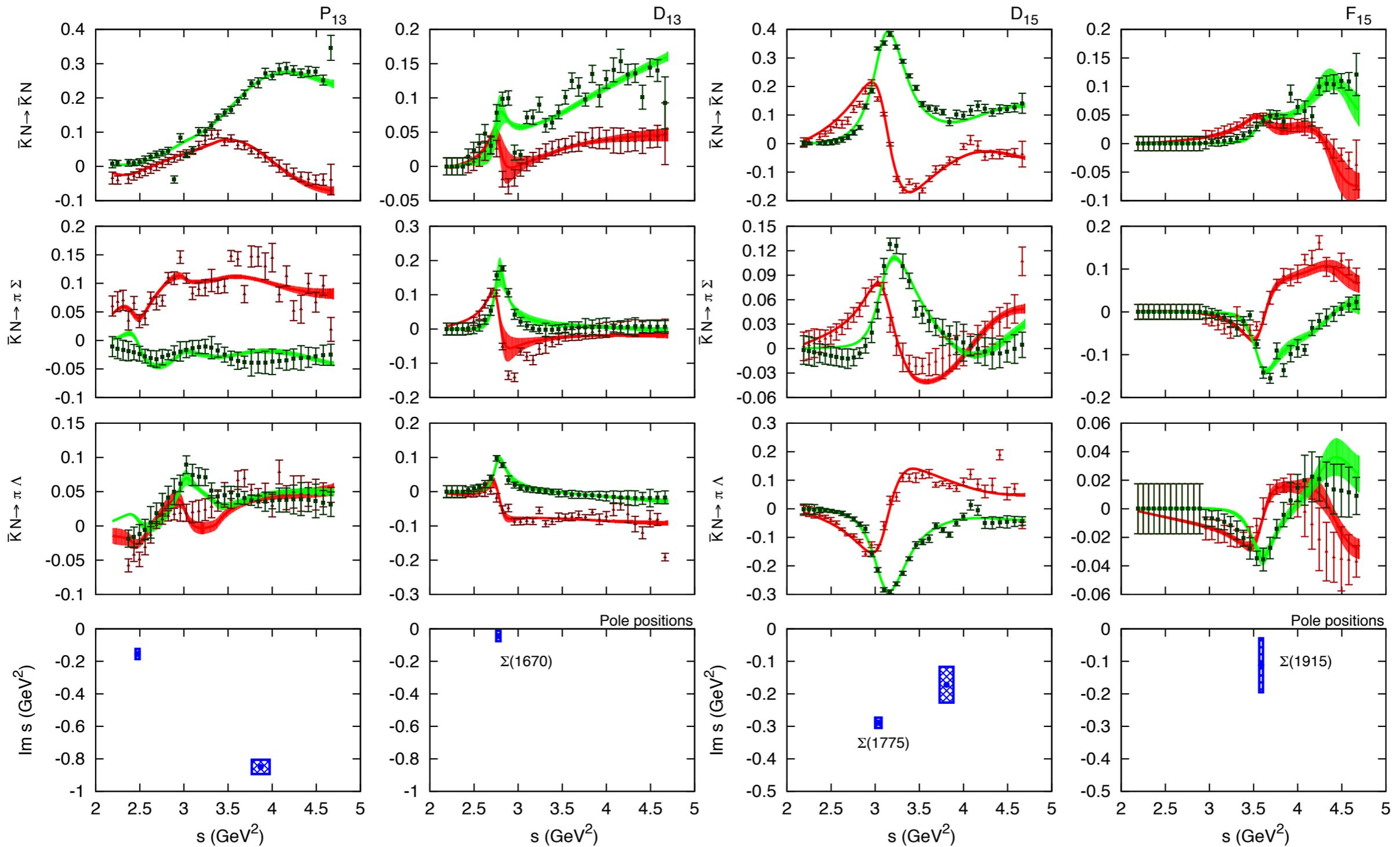
$$[i\rho_\ell(s)]_{kk} = \frac{s - s_k}{\pi} \int_{s_k}^{\infty} \frac{[C_\ell(s')]_{kk}}{s' - s} \frac{ds'}{s' - s_k} = -a_0 \frac{a^\ell}{\pi\Gamma(\ell)} \left[\frac{\pi\Gamma(\ell)(s - s_k)\sqrt{s_k - s}}{1 + a(s - s_k)} \right. \\ \left. - \frac{\sqrt{\pi}\Gamma(\ell + \frac{1}{2})}{\ell a^{\ell+1/2}} ([1 + a(s - s_k)] {}_2F_1 [1, \ell + 1/2, -1/2, 1/a(s_k - s)] \right. \\ \left. - [3 + 2\ell + a(s - s_k)] {}_2F_1 [1, \ell + 1/2, 1/2, 1/a(s_k - s)] \right]$$

Valid for ℓ real and bigger than -1/2

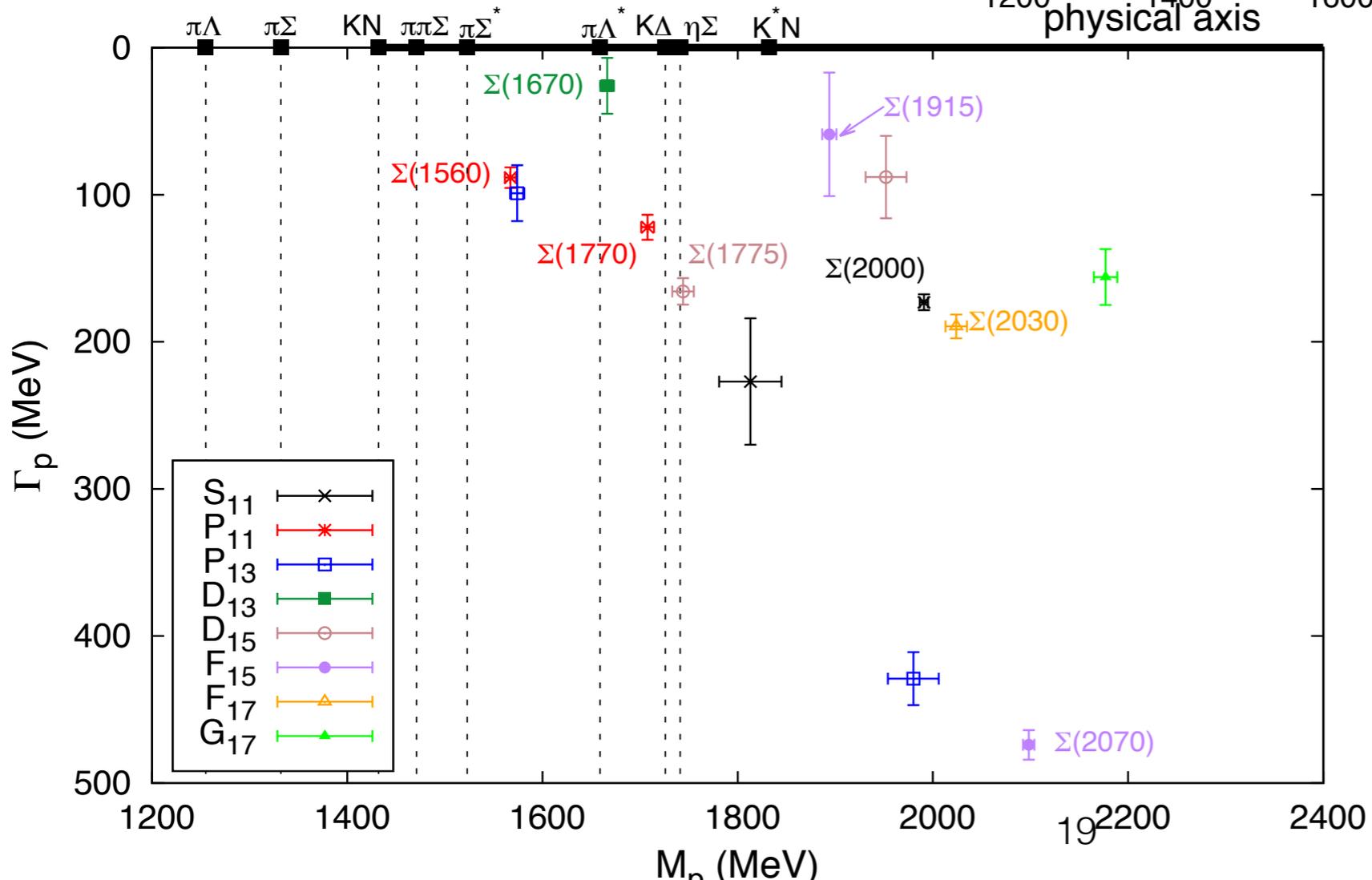
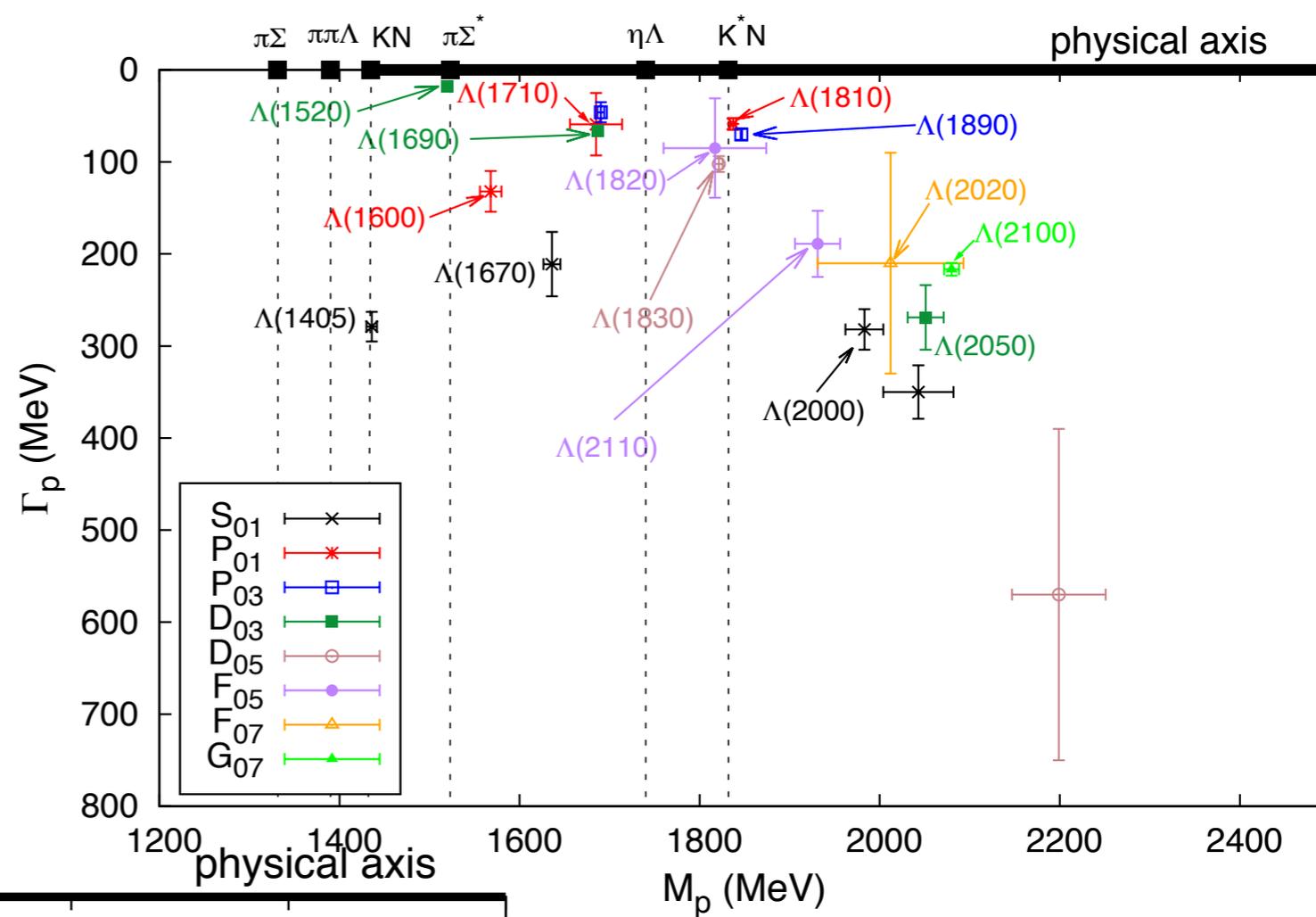
Partial Waves



Partial Waves



Pole Positions



Resonances as Regge Poles

near the resonance pole

$$\alpha' \sim 1 \text{ GeV}^{-2}$$

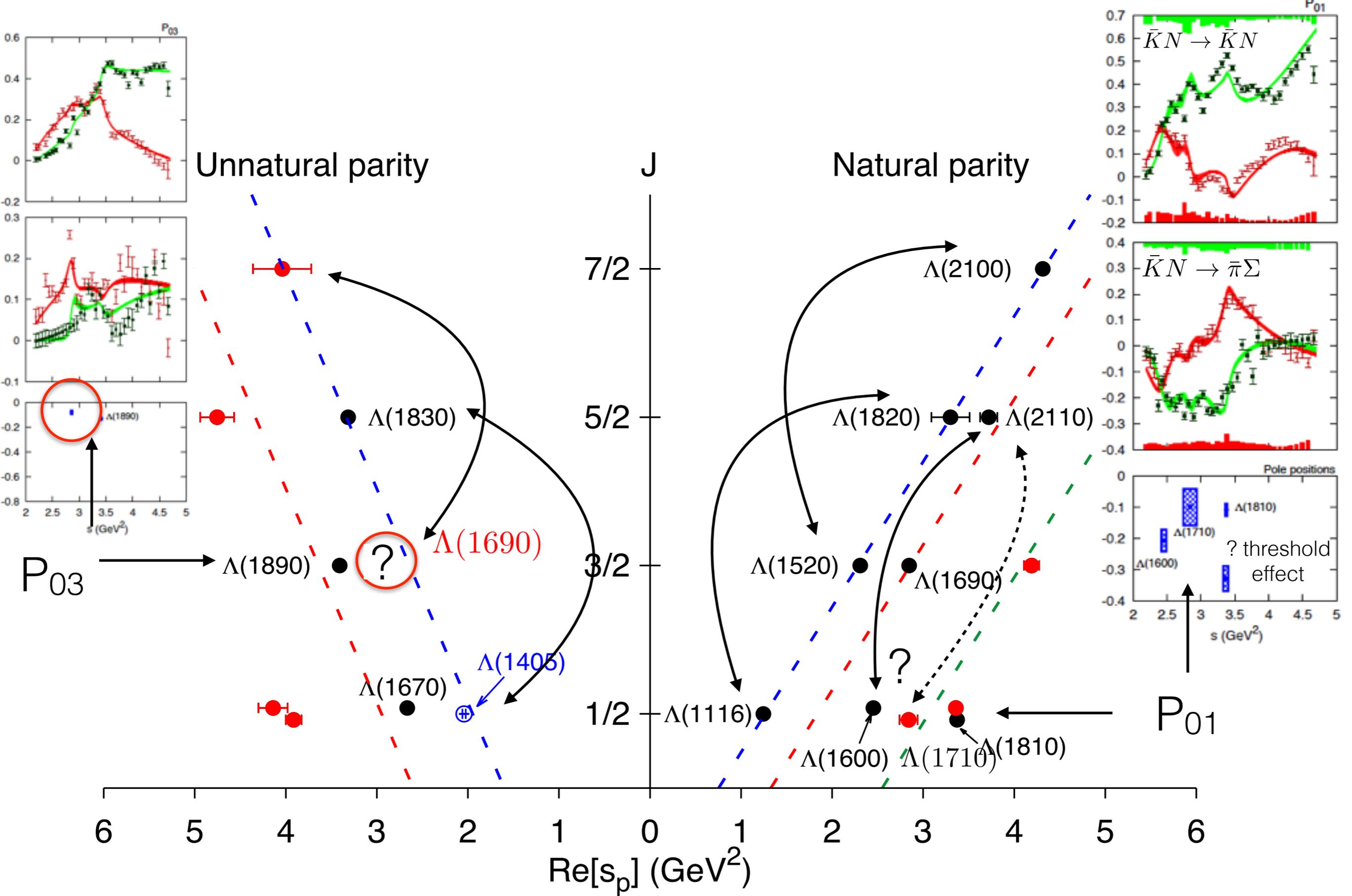
$$T_l \sim \frac{1}{\alpha'(m_l^2 - s)} = \frac{1}{l - (l - \alpha'm_l^2 + \alpha's)}$$

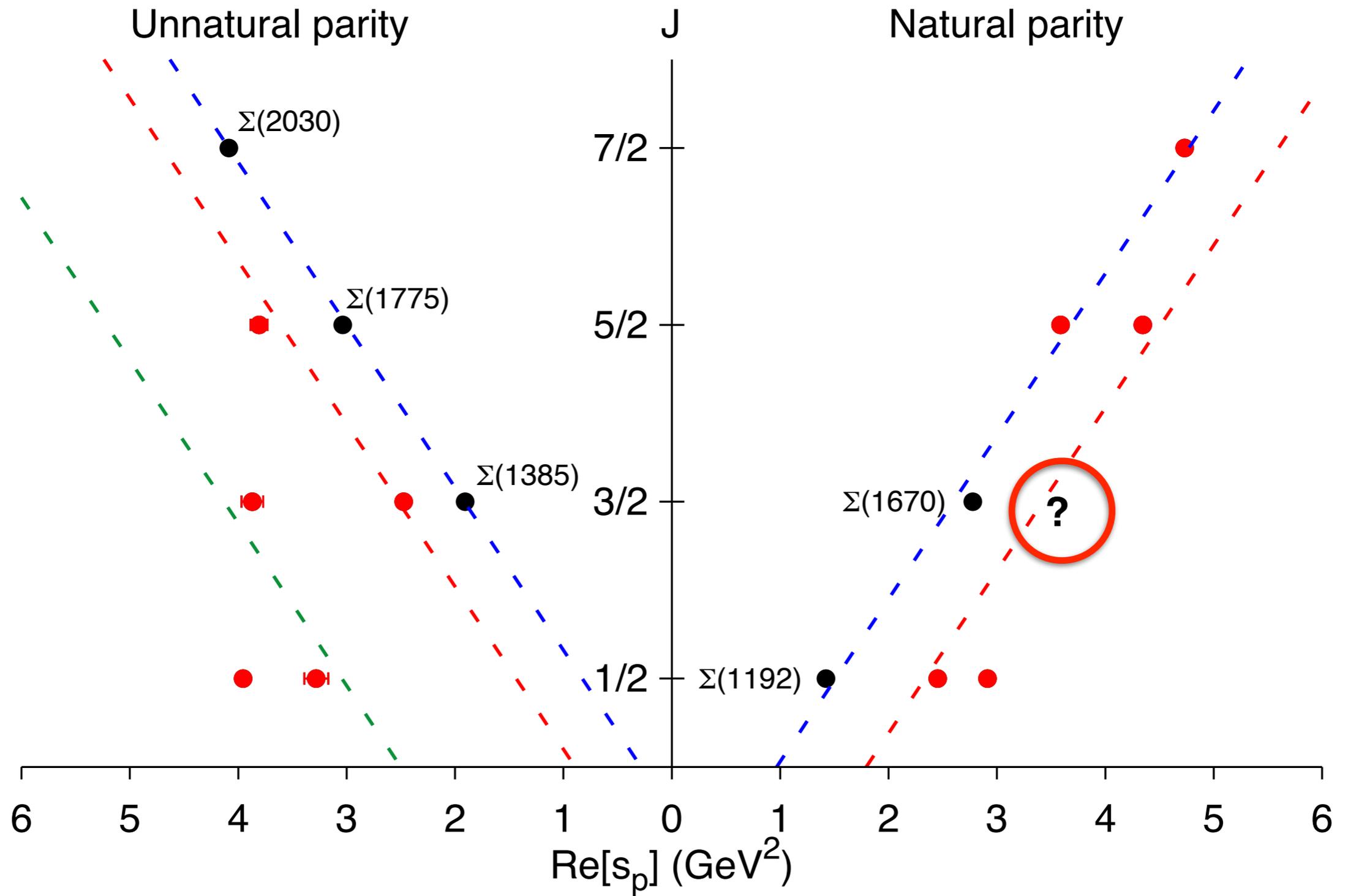
if $l = \alpha_0 + \alpha'm_l^2$ **than** $T_l \sim \frac{1}{l - \alpha(s)}$ **with**

$$\alpha(s) = \alpha_0 + \alpha's$$

In general $T = T(l, s)$ **and a pole corresponds to a trajectory in the l,s space**

A pole in s at a fixed integer l is connected to another pole at a different integer l



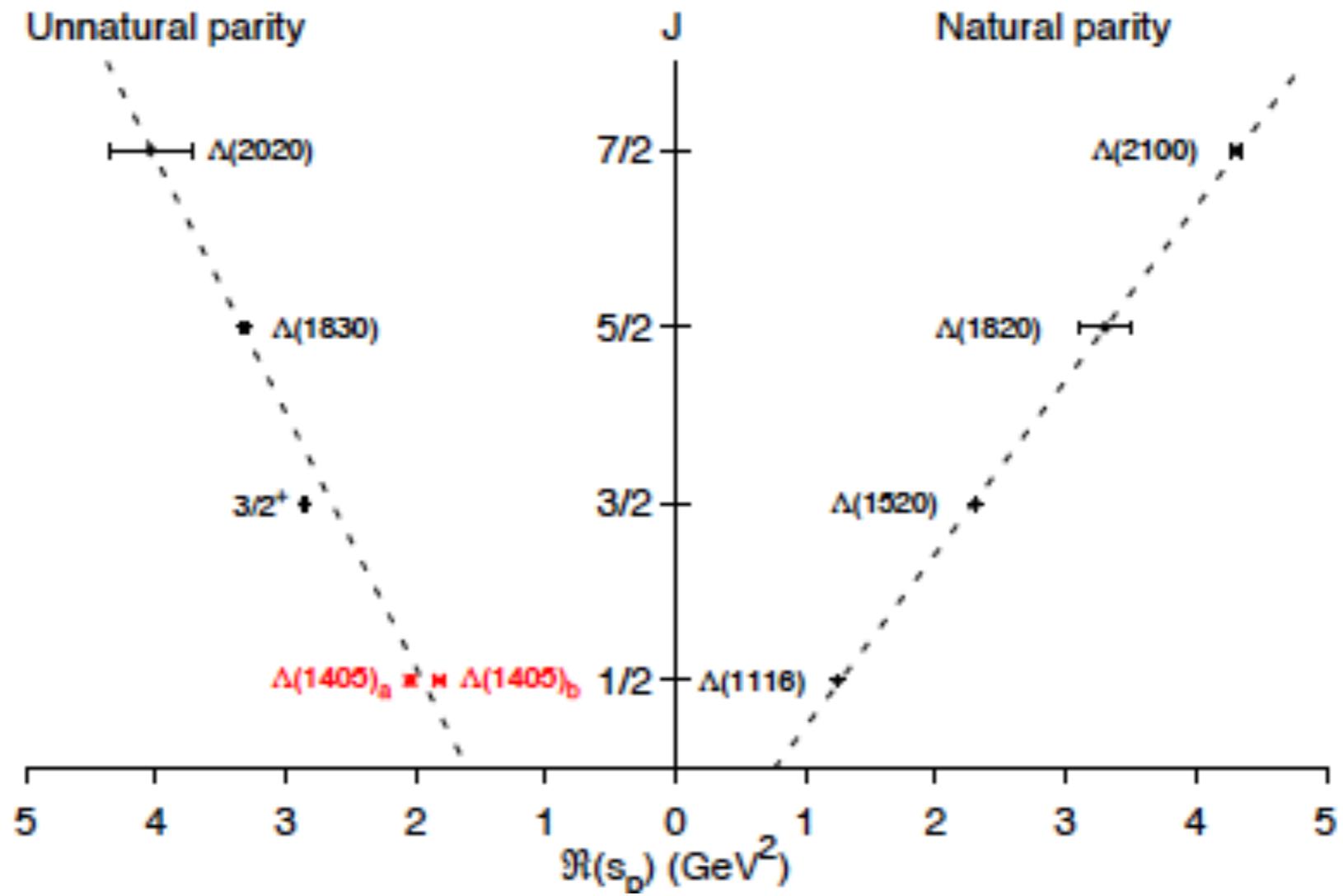


(3 *) $\Sigma(1940)$ nobody gets it, but there is a gap in Rague trajectory

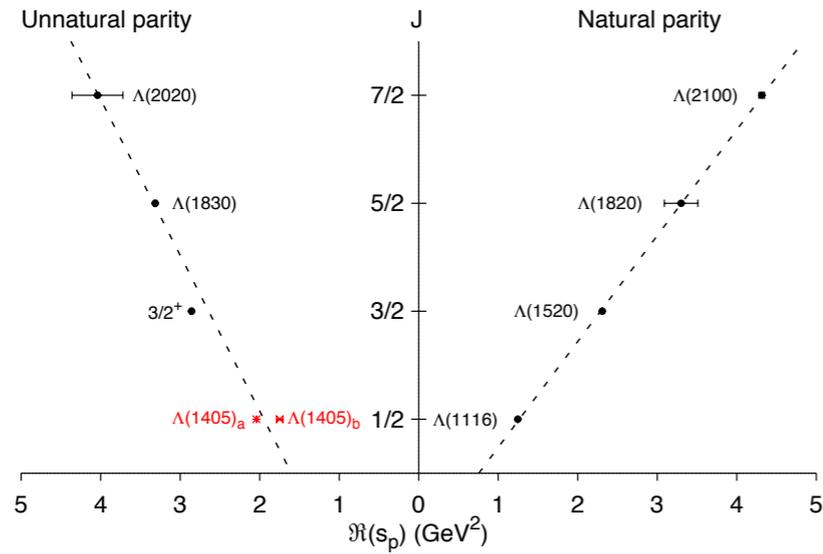
On the nature of $\Lambda(1405)$

- ◆ **Puzzle since the 60's**
- ◆ **Quantum numbers those of a uds state**
- ◆ **Constituent quark models fail to reproduce the mass**
 - ◆ 1550 MeV [Capstick, Isgur, PRD 34, 2809 (1986)]
 - ◆ 1524 MeV [Löring, Metsch, Petry, EPJA 10, 447 (2001)]
- ◆ **Amplitude analysis of KN scattering and $\pi\Sigma K^+$ data finds two poles [Mai, Meißner, EPJA 51, 30 (2015)]**
 - ◆ 1429-12i MeV
 - ◆ 1325-90i MeV
- ◆ **Lattice says: KN molecule [Hall et al., PRL 114, 132002 (2015)]**
- ◆ **Lattice says: three-quark state [Engel et al., PRD 87, 034502 (2013); PRD 87, 074504 (2013)]**
- ◆ **Regge phenomenology [Fernandez-Ramirez et al., arXiv:1512.03136 (2015)]**
- ◆ **Quark-diquark models obtain one $\Lambda(1405)$ with the right energy**
 - ◆ 1430 MeV [Santopinto, Ferretti, PRC 92, 025202 (2015)]
 - ◆ 1406 MeV [Faustov, Galkin, PRD 92, 054005 (2015)]

$\Lambda(1405)$

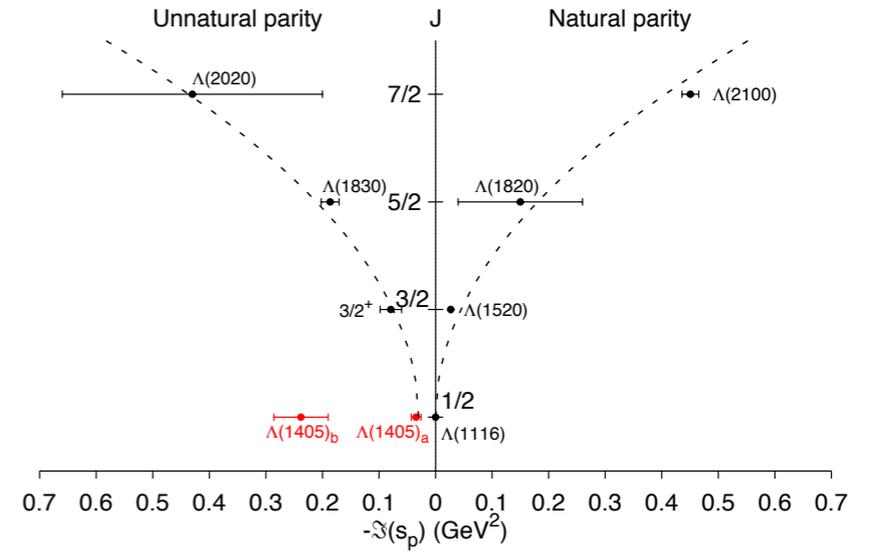


Re

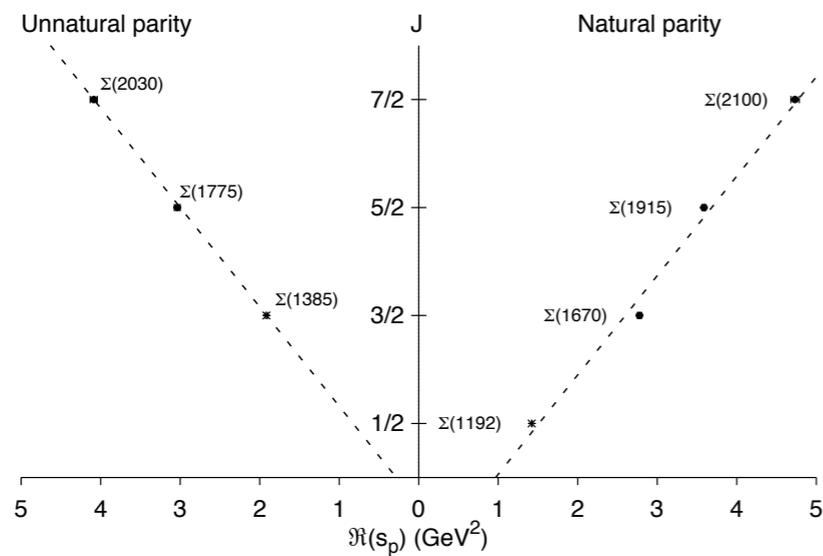


(a) Λ resonances.

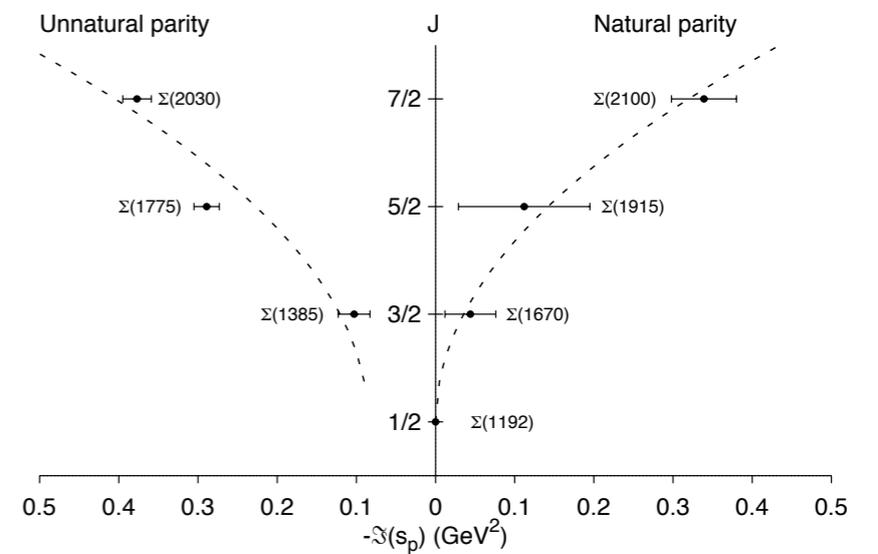
Im



(a) Λ resonances.



(b) Σ resonances.



(b) Σ resonances.

FIG. 1. (color online). Chew-Frautschi plot for the the leading Λ and Σ Regge trajectories. Dashed lines are displayed to guide the eye.

FIG. 2. (color online). Projections of the leading Λ and Σ Regge trajectories onto the $(-\Im(s_p), J)$ plane. Dashed lines are displayed to guide the eye.

Compare fits 0^-_a , 0^-_b , 0^-_c

$$\Lambda_a(1405) = 1429 - 12i \text{ MeV}$$

$$\Lambda_b(1405) = 1352 - 90i \text{ MeV}$$

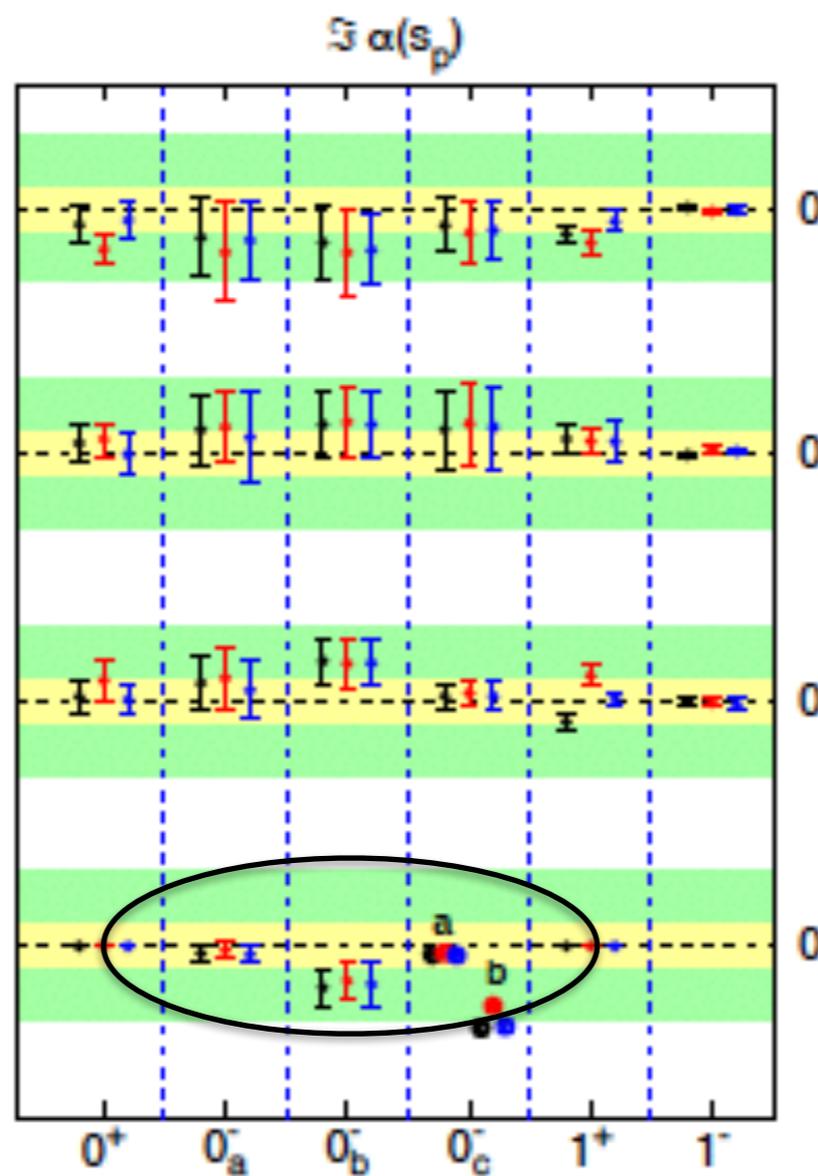
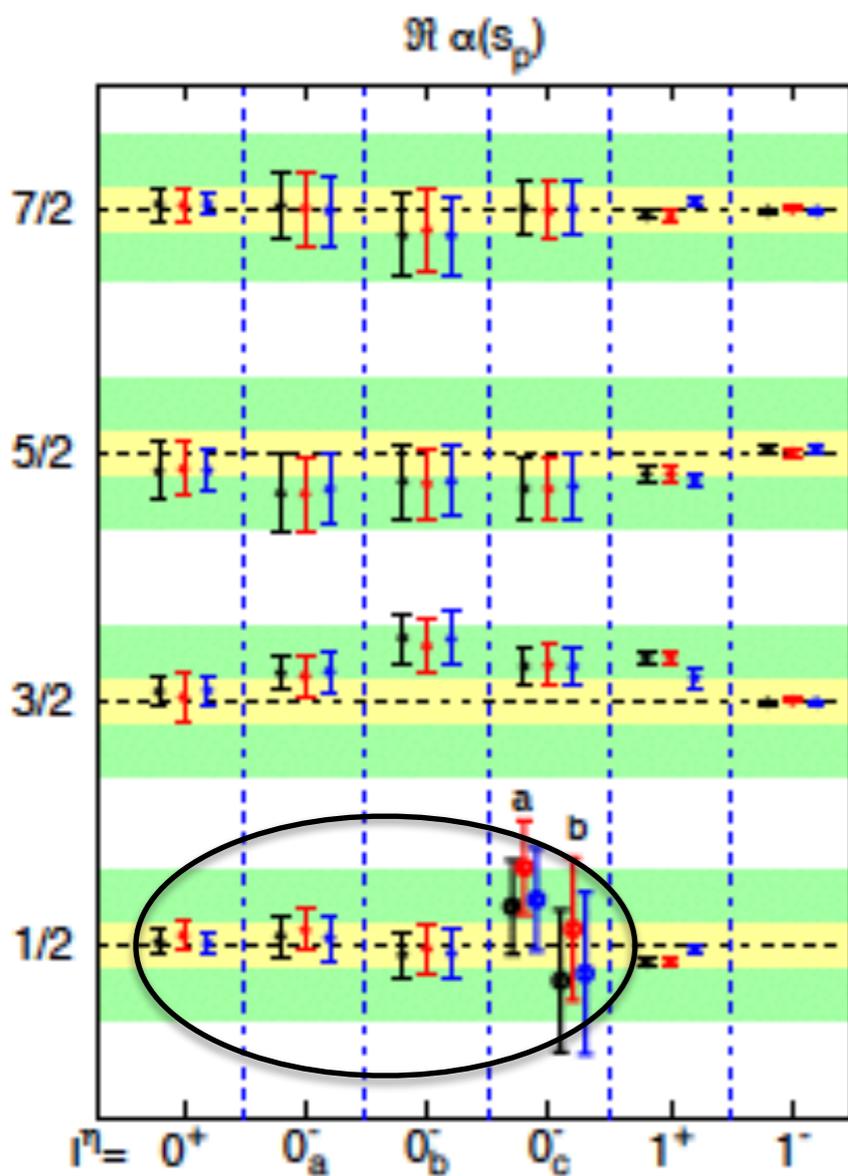
$$\alpha(s) = \alpha_0 + \alpha' s + i \gamma \rho(s, s_t)$$

$$i \rho_A(s, s_t) = i \sqrt{s - s_t},$$

$$i \rho_B(s, s_t) = i \sqrt{1 - s_t/s},$$

$$i \rho_C(s, s_t) = \frac{s - s_t}{\pi} \int_{s_t}^{\infty} \frac{\sqrt{1 - s_t/s'}}{s' - s_t} \frac{ds'}{s' - s}$$

$$= \frac{2}{\pi} \frac{s - s_t}{\sqrt{s(s_t - s)}} \arctan \sqrt{\frac{s}{s_t - s}}$$



$\Lambda_a(1405)$ is closer to the “normal” trajectory

Summary

- **New, analytical model for hyperon spectrum**
- **Need to incorporate Regge constraints**
 - **in direct channel as a constraint on, eg, K-matrix matrix poles**
 - **in cross channels, as constrained on p.w. extraction,**
- **$\Lambda(1405)$: One more piece to the puzzle (more confusion?)**

TABLE II. Summary of Λ^* pole masses ($M_p = \text{Re} \sqrt{s_p}$) and widths ($\Gamma_p = -2 \text{Im} \sqrt{s_p}$) in MeV. Our poles are depicted in Fig. 5 unless they have a very large imaginary part. In [2] the $\Lambda(1520)$ pole was obtained at ($M_p = 1518.8$, $\Gamma_p = 17.2$). Ref. [5] implements two models labeled as KA and KB (see text). I stands for isospin, η for naturality, J for total angular momentum, P for parity, and ℓ for orbital angular momentum. For baryons, $\eta = +$, natural parity, if $P = (-1)^{J-1/2}$ and $\eta = -$, unnatural parity, if $P = -(-1)^{J-1/2}$ where P stands for parity. Resonances marked with \dagger are unreliable themselves due to systematics and lack of good-quality χ^2/dof . Resonances marked with \ddagger are most likely artifacts of the fits.

$I^\eta J^P \ell$	This work		KSU from [3]		KA from [5]		KB from [5]		PDG [1]	
	M_p	Γ_p	M_p	Γ_p	M_p	Γ_p	M_p	Γ_p	Name	Status
$0^- \frac{1}{2}^- S$	$1435.8 \pm 5.9^\dagger$	279 ± 16	1402	49	—	—	—	—	$\Lambda(1405)$	****
	1573^\ddagger	300	—	—	—	—	1512	370	—	—
	$1636.0 \pm 9.4^\dagger$	211 ± 35	1667	26	1669	18	1667	24	$\Lambda(1670)$	****
	—	—	1729	198	—	—	—	—	$\Lambda(1800)$	***
	$1983 \pm 21^\dagger$	282 ± 22	1984	233	—	—	—	—	$\Lambda(2000)$	*
	$2043 \pm 39^\dagger$	350 ± 29	—	—	—	—	—	—	—	—
$0^+ \frac{1}{2}^+ P$	1568 ± 12	132 ± 22	1572	138	1544	112	1548	164	$\Lambda(1600)$	***
	$1685 \pm 29^\dagger$	59 ± 34	1688	166	—	—	—	—	$\Lambda(1710)$	*
	$1835 \pm 10^\ddagger$	180 ± 22	—	—	—	—	—	—	—	—
	$1837.2 \pm 3.4^\dagger$	58.7 ± 6.5	1780	64	—	—	1841	62	$\Lambda(1810)$	—
	—	—	2135	296	2097	166	—	—	—	—
$0^- \frac{3}{2}^+ P$	1690.3 ± 3.8	46.4 ± 11.0	—	—	—	—	1671	10	—	—
	1846.36 ± 0.81	70.0 ± 6.0	1876	145	1859	112	—	—	$\Lambda(1890)$	†
	—	—	2001	994	—	—	—	—	—	—
$0^+ \frac{3}{2}^- D$	1519.33 ± 0.34	17.8 ± 1.1	1518	16	1517	16	1517	16	$\Lambda(1520)$	†
	1687.40 ± 0.79	66.2 ± 2.3	1689	53	1697	66	1697	74	$\Lambda(1690)$	†
	2051 ± 20	269 ± 35	1985	447	—	—	—	—	$\Lambda(2050)$	—
	$2133 \pm 120^\ddagger$	1110 ± 280	—	—	—	—	—	—	$\Lambda(2325)$	—
$0^- \frac{5}{2}^- D$	1821.4 ± 4.3	102.3 ± 8.6	1809	109	1766	212	—	—	$\Lambda(1830)$	†
	—	—	1970	350	1899	80	1924	90	—	—
	2199 ± 52	570 ± 180	—	—	—	—	—	—	—	—
$0^+ \frac{5}{2}^+ F$	1817 ± 57	85 ± 54	1814	85	1824	78	1821	64	$\Lambda(1820)$	†
	1931 ± 25	189 ± 36	1970	350	—	—	—	—	$\Lambda(2110)$	—
$0^- \frac{7}{2}^+ F$	—	—	—	—	1757	146	—	—	—	—
	2012 ± 81	210 ± 120	1999	146	—	—	2041	238	$\Lambda(2020)$	—
$0^+ \frac{7}{2}^- G$	2079.9 ± 8.3	216.7 ± 6.8	2023	239	—	—	—	—	$\Lambda(2100)$	†

Λ^*

TABLE III. Summary of Σ^* pole masses ($M_p = \text{Re} \sqrt{s_p}$) and widths ($\Gamma_p = -2 \text{Im} \sqrt{s_p}$) in MeV. Our poles are depicted in Fig. 5 unless they have a very large imaginary part. Notation is the same as in Table II. Resonances marked with † are unreliable themselves due to systematics and lack of good-quality χ^2/dof .

$I^\eta J^P \ell$	This work		KSU from [3]		KA from [5]		KB from [5]		PDG [1]	
	M_p	Γ_p	M_p	Γ_p	M_p	Γ_p	M_p	Γ_p	Name	Status
Σ^* $1^- \frac{1}{2}^- S$	—	—	1501	171	—	—	1551	376	$\Sigma(1620)$	*
	—	—	1708	158	1704	86	—	—	$\Sigma(1750)$	***
	$1813 \pm 32^\dagger$	227 ± 43	—	—	—	—	—	—	—	—
	—	—	1887	187	—	—	—	—	$\Sigma(1900)$	*
	$1990.8 \pm 4.3^\dagger$	173.1 ± 5.4	—	—	—	—	1940	172	$\Sigma(2000)$	*
	—	—	2040	295	—	—	—	—	—	—
$1^+ \frac{1}{2}^+ P$	1567.3 ± 5.7	88.4 ± 7.0	—	—	1547	184	1457	78	$\Sigma(1560)$	**
	—	—	—	—	—	—	—	—	$\Sigma(1660)$	***
	1707.7 ± 6.6	122.1 ± 8.5	1693	163	1706	102	—	—	$\Sigma(1770)$	*
	—	—	1776	270	—	—	—	—	$\Sigma(1880)$	**
	—	—	—	—	—	—	2014	140	—	—
$1^- \frac{3}{2}^+ P$	1574.1 ± 7.2	99 ± 19	—	—	—	—	—	—	—	—
	—	—	1683	243	—	—	—	—	—	—
	—	—	1874	349	—	—	—	—	—	—
	1980 ± 26	429 ± 18	—	—	—	—	—	—	—	—
$1^+ \frac{3}{2}^- D$	—	—	—	—	1607	252	1492	138	$\Sigma(1580)$	*
	1666.3 ± 7.0	26 ± 19	1674	54	1669	64	1672	66	$\Sigma(1670)$	****
	—	—	—	—	—	—	—	—	$\Sigma(1940)$	***
$1^- \frac{5}{2}^- D$	1744 ± 11	165.7 ± 9.0	1759	118	1767	128	1765	128	$\Sigma(1775)$	****
	1952 ± 21	88 ± 28	2183	296	—	—	—	—	—	—
$1^+ \frac{5}{2}^+ F$	—	—	—	—	—	—	1695	194	—	—
	1893.9 ± 7.2	59 ± 42	1897	133	1890	99	—	—	$\Sigma(1915)$	****
	2098.2 ± 5.8	474 ± 10	2084	319	—	—	—	—	$\Sigma(2070)$	*
$1^- \frac{7}{2}^+ F$	2024 ± 11	189.5 ± 8.1	1993	176	2025	130	2014	206	$\Sigma(2030)$	****
$1^+ \frac{7}{2}^- G$	2177 ± 12	156 ± 19	2252	290	—	—	—	—	$\Sigma(2100)$	*