

**Establishing $S=-1$ hyperon resonances
using kaon-induced meson productions
within dynamical coupled-channels
approach**

**Hiroyuki Kamano
(RCNP, Osaka U.)**

**“Physics with Neutral Kaon Beam at JLab” Workshop (KL2016)
Jefferson Lab, VA, USA, February 1th-3th, 2016**

Outline

- ✓ **Overview of Y^* ($= \Lambda^*, \Sigma^*$) spectroscopy via dynamical coupled-channels (DCC) analysis of $K^- p$ reactions**

[HK, Nakamura, Lee, Sato, PRC90\(2014\)065204; 92\(2015\)025205](#)

- ✓ **Application to $\bar{K} d$ reactions (ongoing)**

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Λ^*			Σ^*		
Particle	J^P	Overall status	Particle	J^P	Overall status
$\Lambda(1116)$	1/2+	****	$\Sigma(1193)$	1/2+	****
$\Lambda(1405)$	1/2-	****	$\Sigma(1385)$	3/2+	****
$\Lambda(1520)$	3/2-	****	$\Sigma(1480)$		*
$\Lambda(1600)$	1/2+	***	$\Sigma(1560)$		**
$\Lambda(1670)$	1/2-	****	$\Sigma(1580)$	3/2-	*
$\Lambda(1690)$	3/2-	****	$\Sigma(1620)$	1/2-	**
$\Lambda(1800)$	1/2-	***	$\Sigma(1660)$	1/2+	***
$\Lambda(1810)$	1/2+	***	$\Sigma(1670)$	3/2-	****
$\Lambda(1820)$	5/2+	****	$\Sigma(1690)$		**
$\Lambda(1830)$	5/2-	****	$\Sigma(1750)$	1/2-	***
$\Lambda(1890)$	3/2+	****	$\Sigma(1770)$	1/2+	*
$\Lambda(2000)$		*	$\Sigma(1775)$	5/2-	****
$\Lambda(2020)$	7/2+	*	$\Sigma(1840)$	3/2+	*
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PDG listing

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✓ Comprehensive partial-wave analyses of $K^- p$ reactions to extract Y^* *defined by poles* have been accomplished *just recently* :

- Kent State University (KSU) group
 (→ 2013, “KSU on-shell parametrization” of S-matrix)
 Zhang et al., PRC88(2013)035204, 035205.
 → Reanalysis of KSU single-energy solution using an on-shell K-matrix model (Fernandez-Ramirez et al., arXiv:1510.07065)
- Our group
 (→ 2014-2015, dynamical coupled-channels approach)
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Dynamical Coupled-Channels (DCC) approach to Λ^* & Σ^* productions

Dynamical Coupled-Channels (DCC) model:

[HK, Nakamura, Lee, Sato, PRC88(2013)035209; PRC90(2014)065204]

$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b; E) + \sum_c \int_0^\infty q^2 dq \underbrace{V_{a,c}^{(LSJ)}(p_a, q; E)}_{\text{CC effect}} \underbrace{G_c(q; E)}_{\text{off-shell effect}} T_{c,b}^{(LSJ)}(q, p_b; E)$$

$$a, b, c = (\bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Sigma, \boxed{\pi\Sigma^*, \bar{K}^*N}, \dots)$$

quasi two-body channels of
three-body $\pi\pi\Lambda$ & $\pi\bar{K}N$

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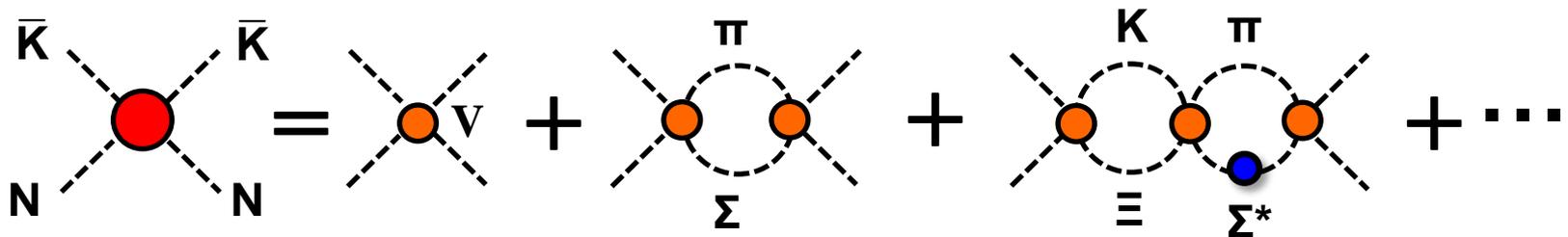
$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b; E) + \sum_c \int_0^\infty q^2 dq \underbrace{V_{a,c}^{(LSJ)}(p_a, q; E)}_{\text{CC effect}} \underbrace{G_c(q; E)}_{\text{off-shell effect}} T_{c,b}^{(LSJ)}(q, p_b; E)$$

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- ✓ Summing up all possible transitions between reaction channels !!
(\rightarrow satisfies **multichannel two-** and **three-body unitarity**)

e.g.) $\bar{K}N$ scattering



- ✓ **Momentum integral** takes into account **off-shell rescattering effects** in the intermediate processes.

What we have done so far

With the DCC approach developed for the **S= -1 sector**, we made:

- ✓ Comprehensive analysis of **ALL** available data (**more than 17,000** data points) of **$K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$** up to **$W = 2.1$ GeV**.

[HK, Nakamura, Lee, Sato, PRC90(2014)065204]

- ✓ Determination of threshold parameters (scattering lengths, effective ranges,...); the **partial-wave amplitudes** of **$\bar{K}N \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$** for **S, P, D, and F waves**.

[HK, Nakamura, Lee, Sato, PRC90(2014)065204]

- ✓ Extraction of **$Y^* = (\Lambda^*, \Sigma^*)$ resonance parameters (mass, width, couplings, ...)** defined by **poles of scattering amplitudes**.

[HK, Nakamura, Lee, Sato, PRC92(2015)025205]

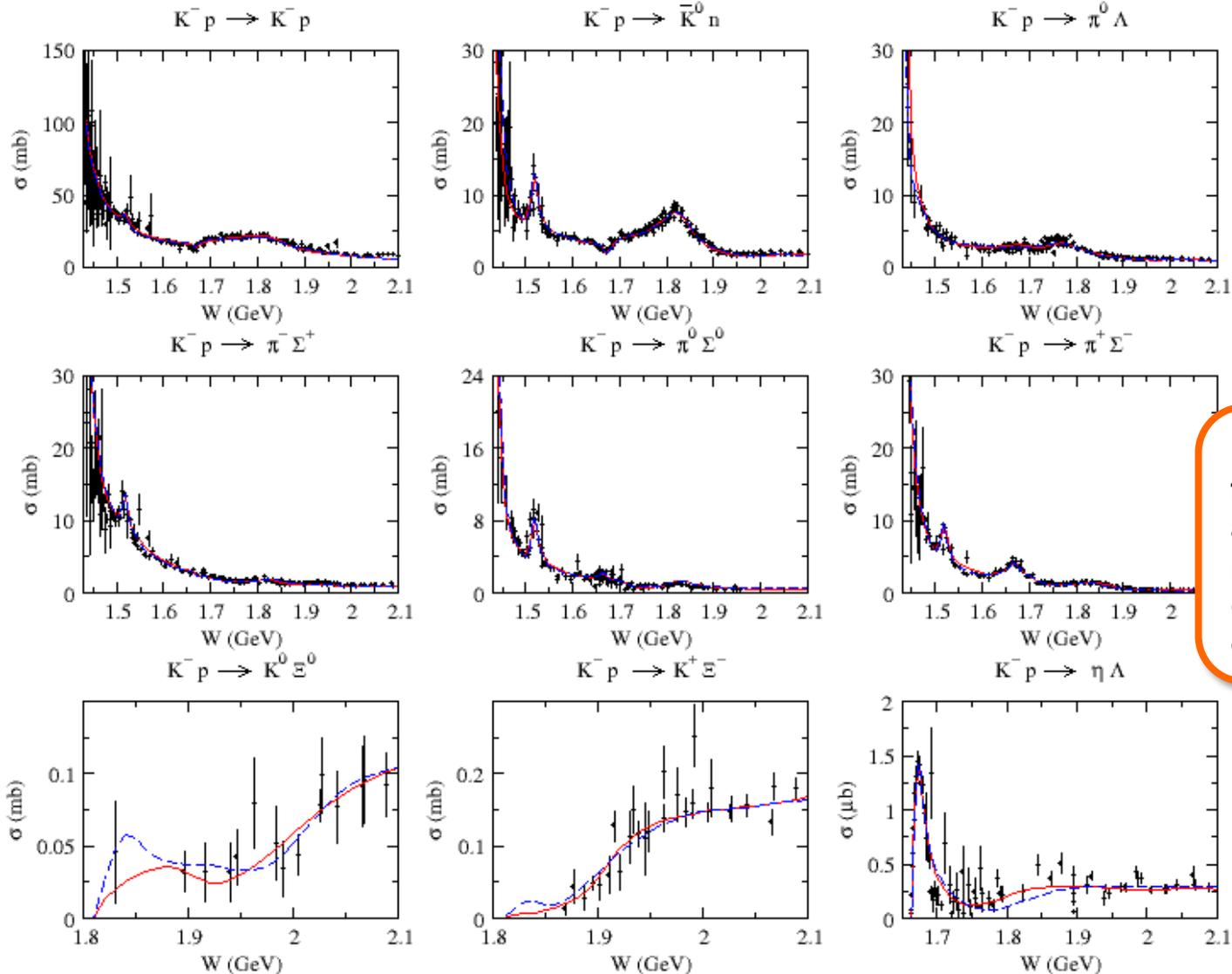
Supercomputers are necessary for the analysis !!



Results of the fits

$K^- p \rightarrow MB$ total cross sections

HK, Nakamura, Lee, Sato, PRC90(2014)065204



Red: Model A

Blue: Model B

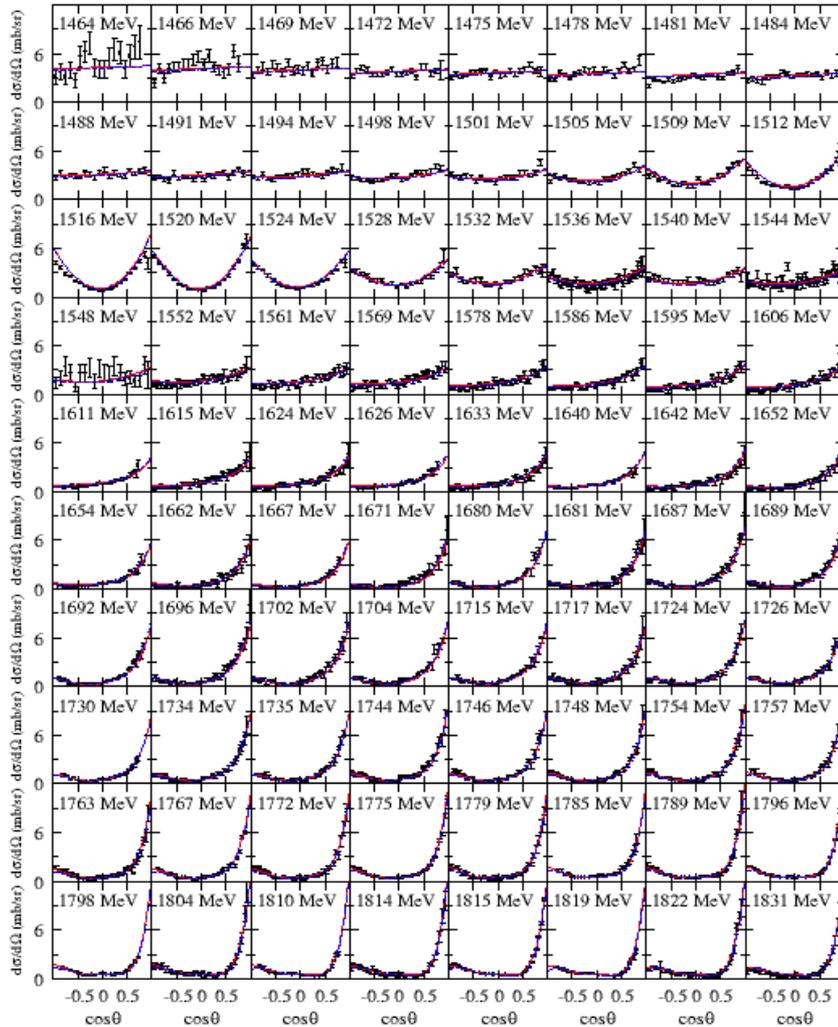
“Incompleteness” of the current database allows us to have two parameter sets that give similar quality of the fit.

Results of the fits

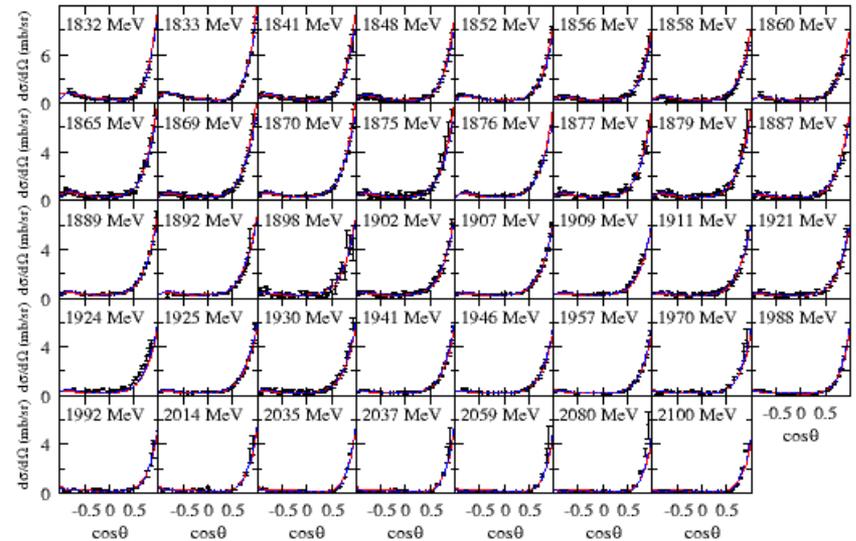
$K^- p \rightarrow K^- p$ scattering

HK, Nakamura, Lee, Sato, PRC90(2014)065204

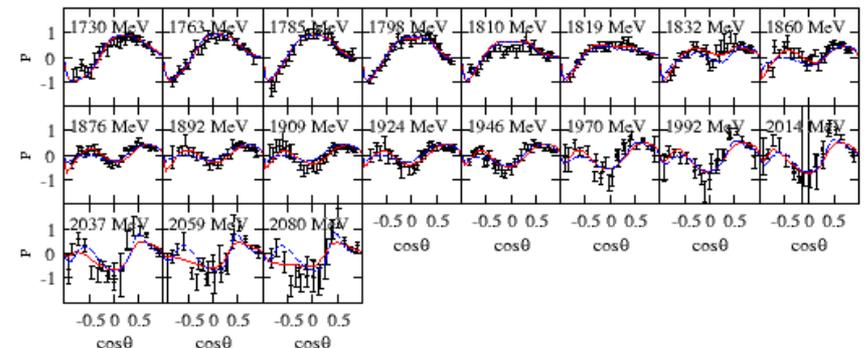
$d\sigma/d\Omega$ (1464 < W < 1831 MeV)



$d\sigma/d\Omega$ (1832 < W < 2100 MeV)

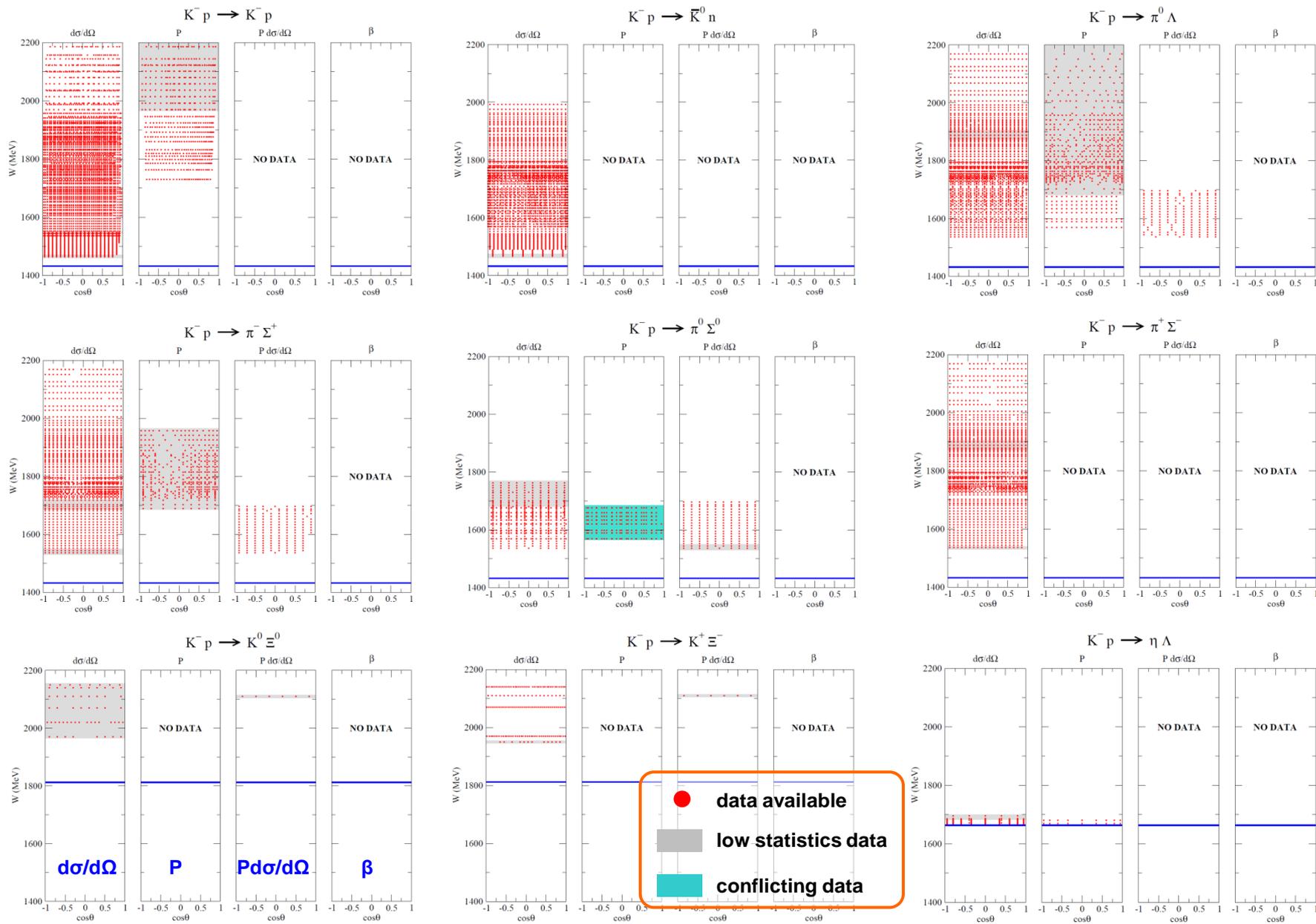


P (1730 < W < 2080 MeV)



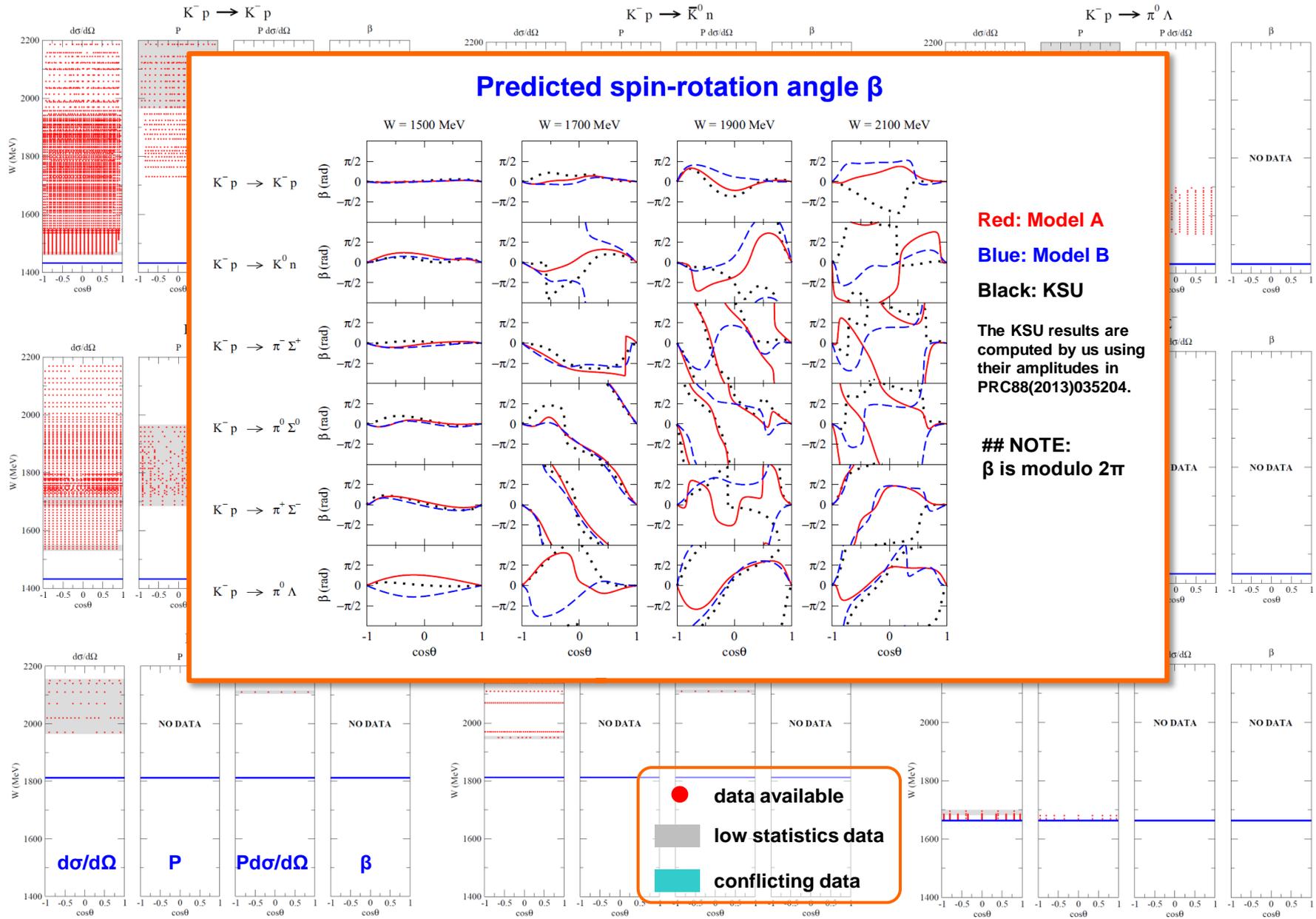
Red: Model A Blue: Model B

Kinematical ($W, \cos\theta$) coverage of available $K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ data



Kinematical ($W, \cos\theta$) coverage of available $K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ data

Predicted spin-rotation angle β

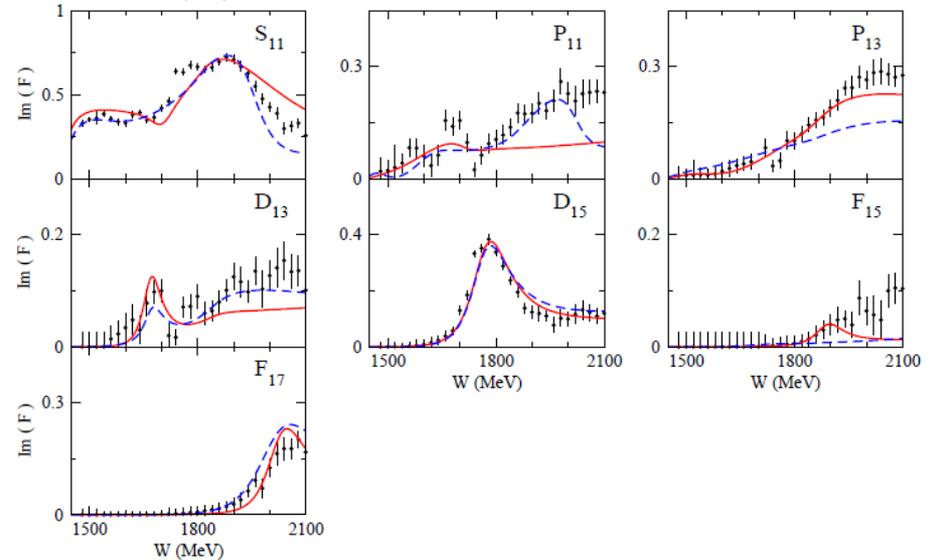
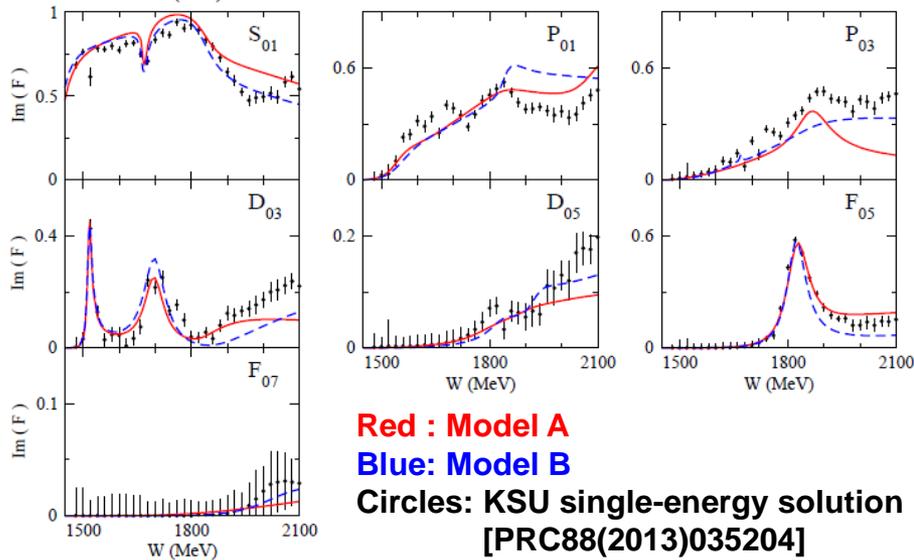
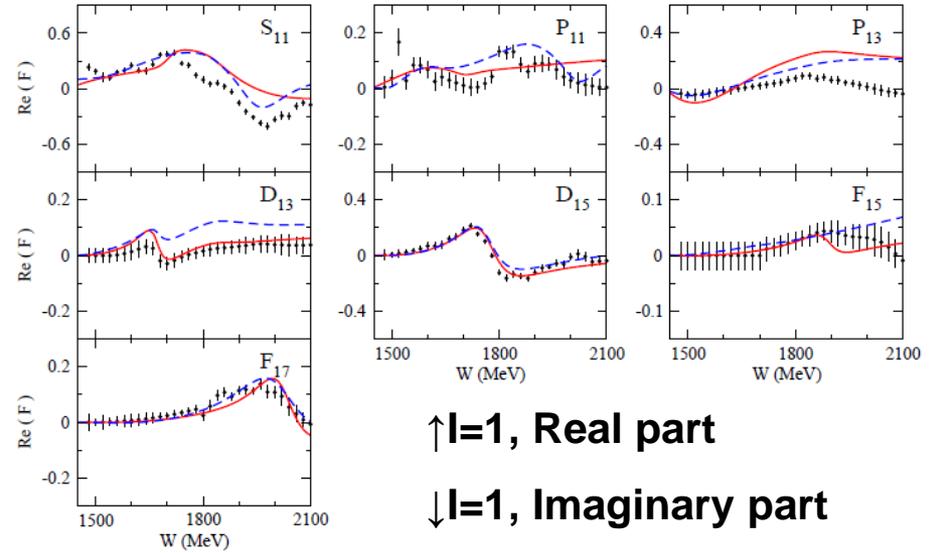
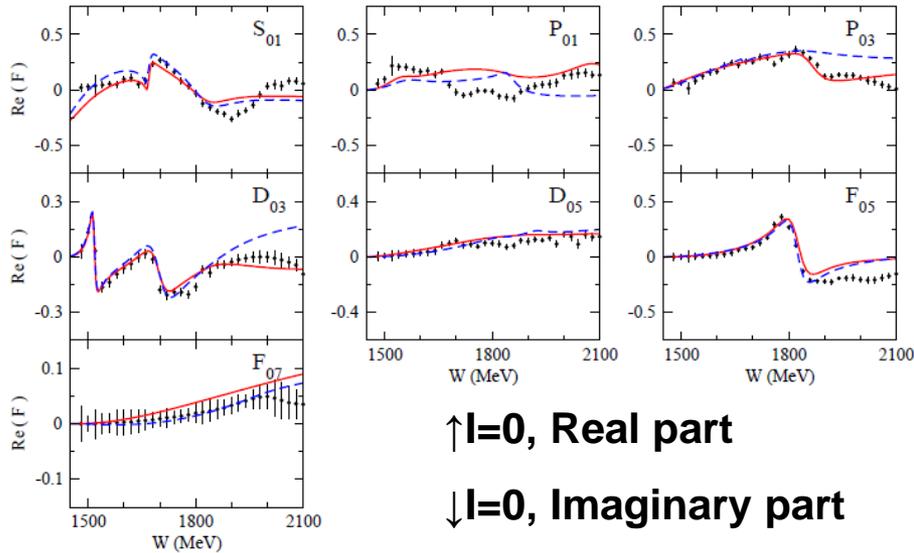


Comparison of extracted partial-wave amplitudes

Extracted $\bar{K}N$ scattering amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

L_{I2J} : $L = S, P, \dots$; $I =$ isospin; $J =$ Total angular mom.

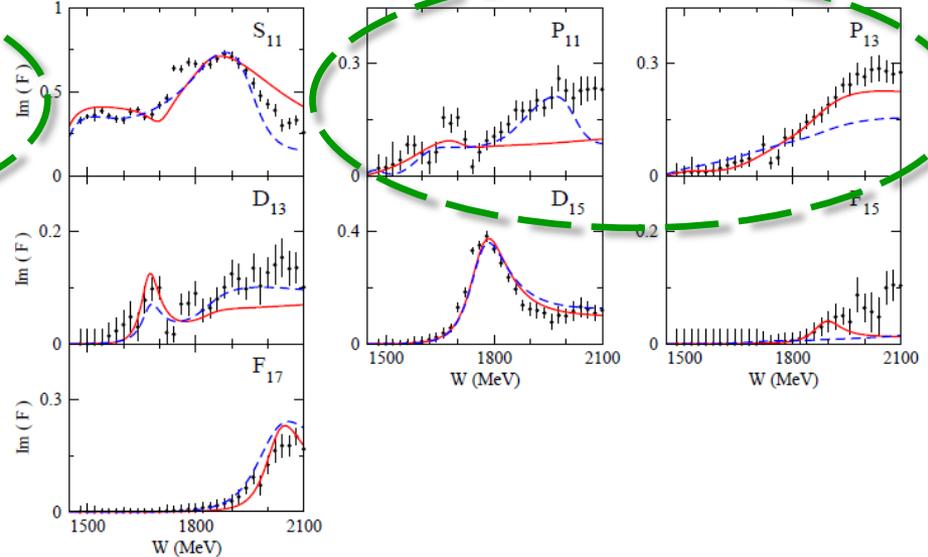
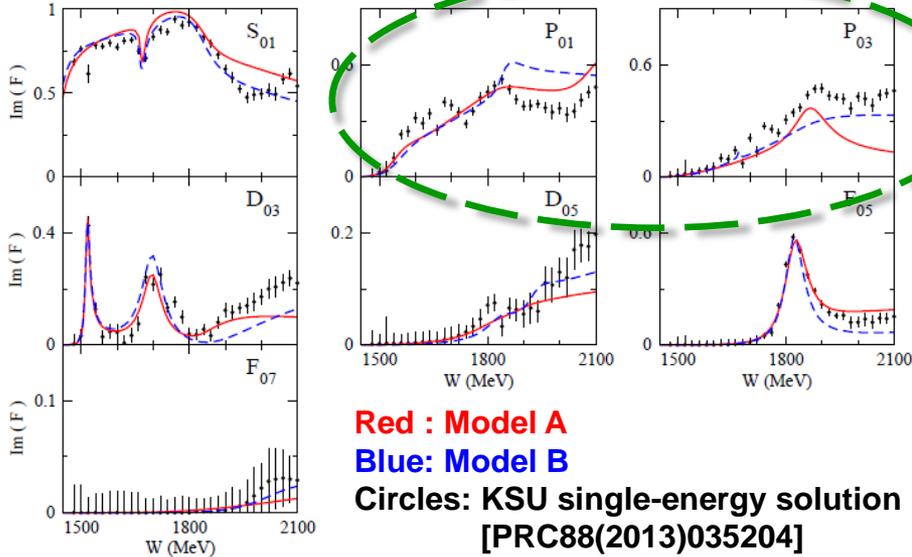
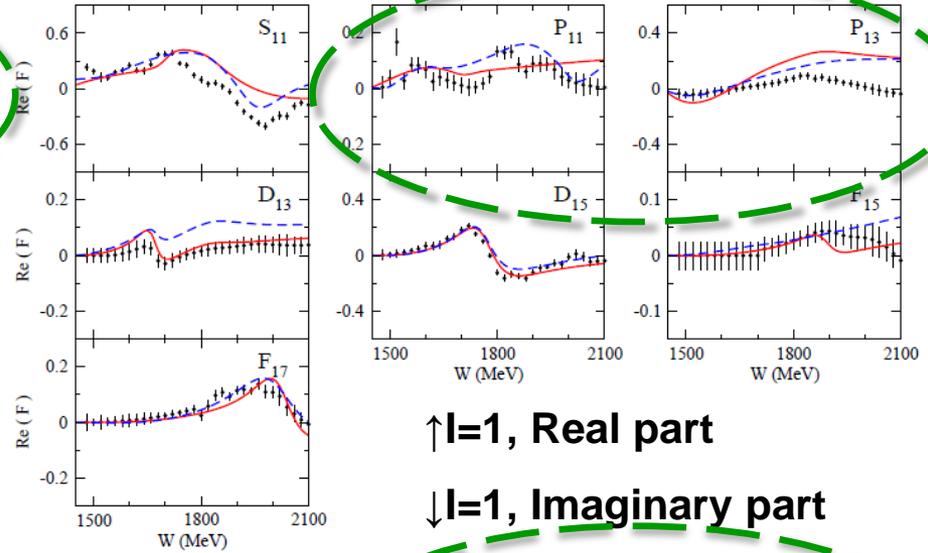
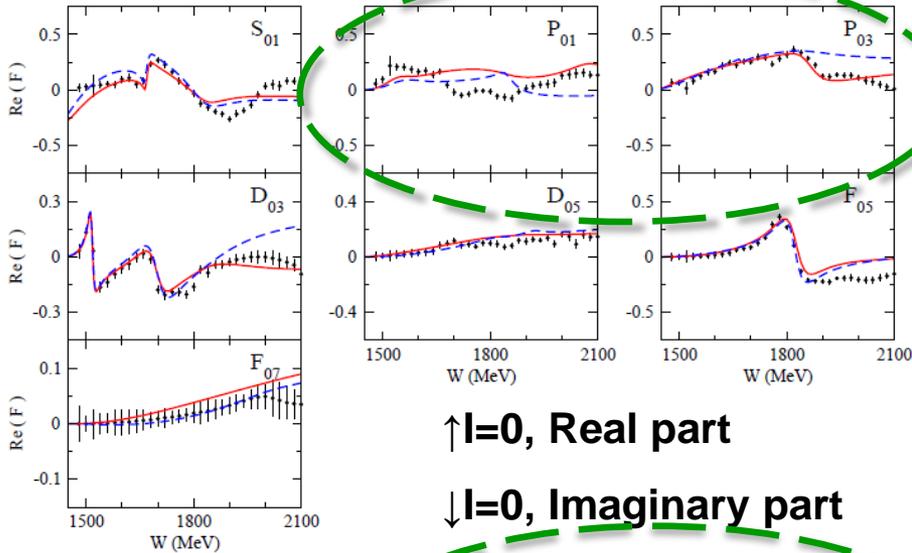


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Extracted Λ^* and Σ^* mass spectrum

HK, Nakamura, Lee, Sato, PRC92(2015)025205

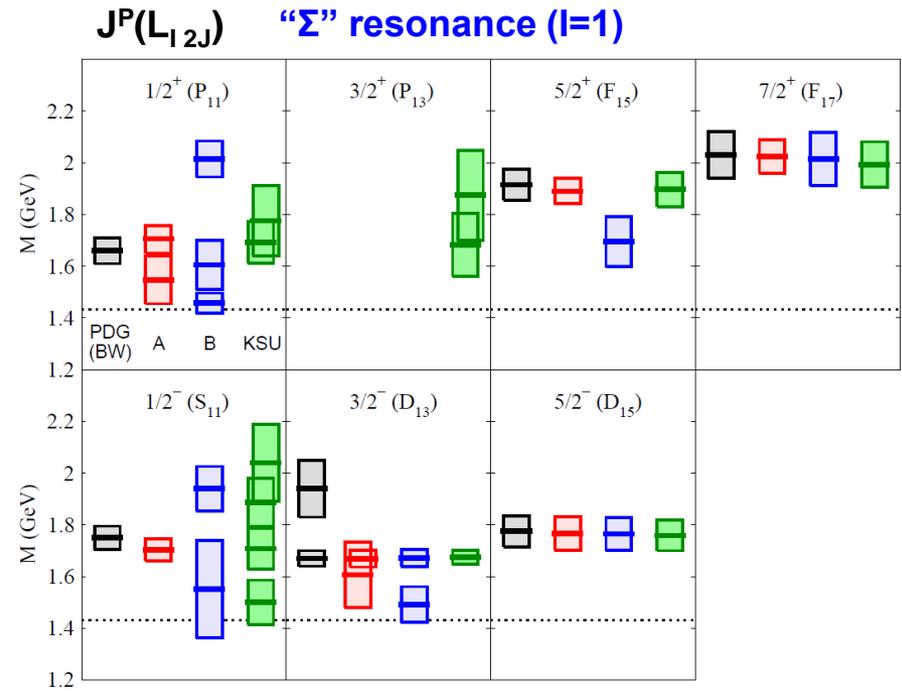
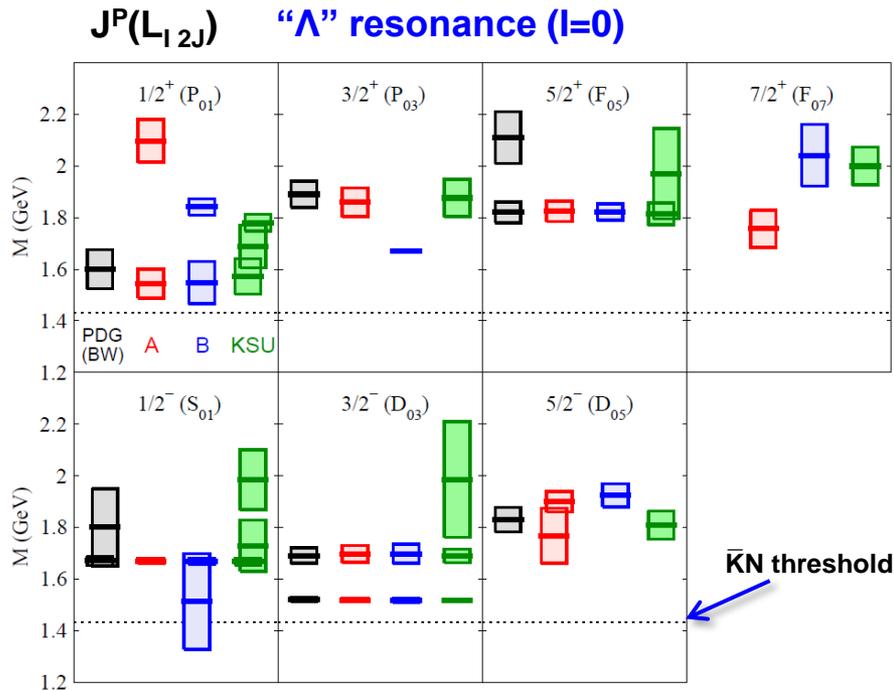
Spectrum for Y^* resonances found above the $\bar{K}N$ threshold

Red: Model A

Blue: Model B

Green: KSU[PRC88(2013)035205]

Black: PDG (only 4- & 3-star Y^* ;
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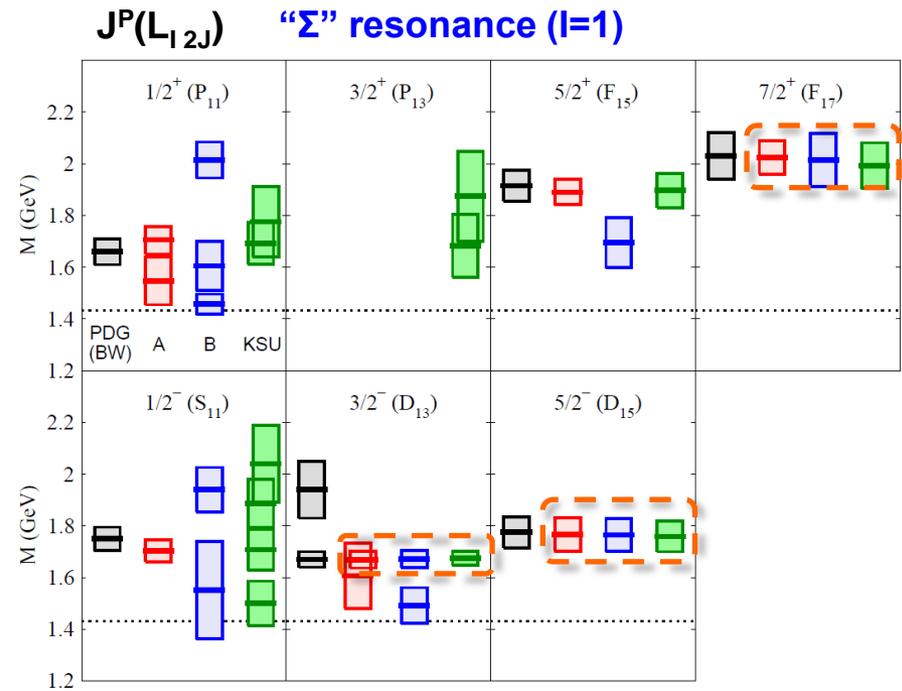
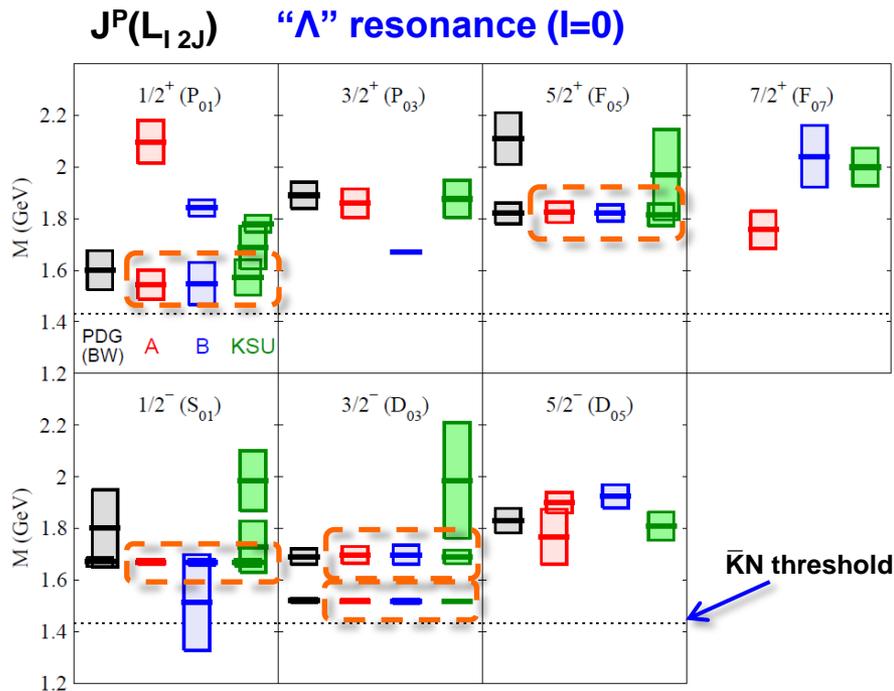
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$-2\text{Im}(M_R)$ ("width")
 $\left\{ \begin{array}{l} \text{Red bar} \\ \text{Red cross} \end{array} \right.$ $\text{Re}(M_R)$ M_R : Resonance pole mass (complex)



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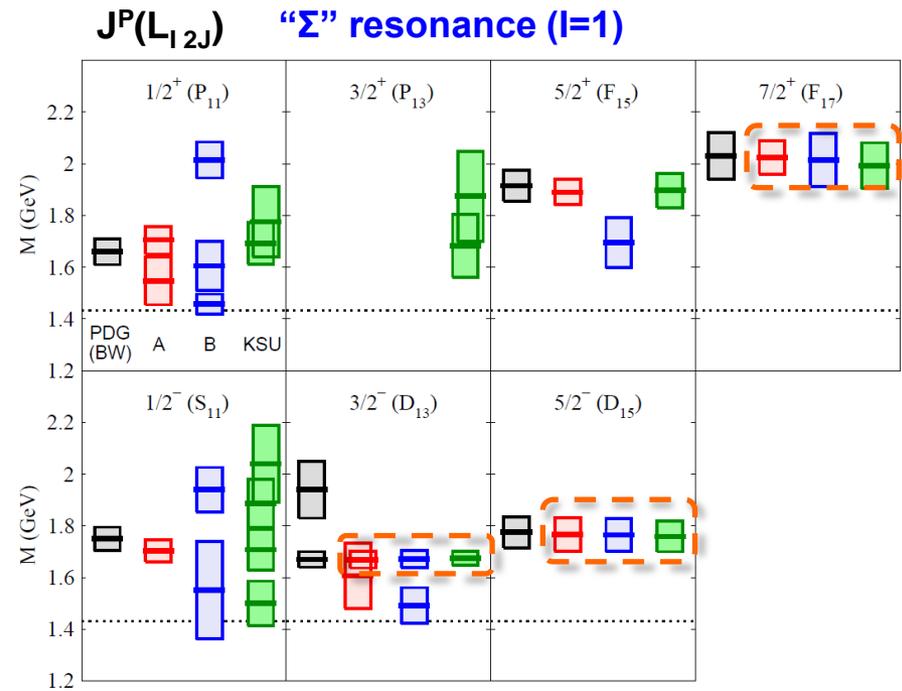
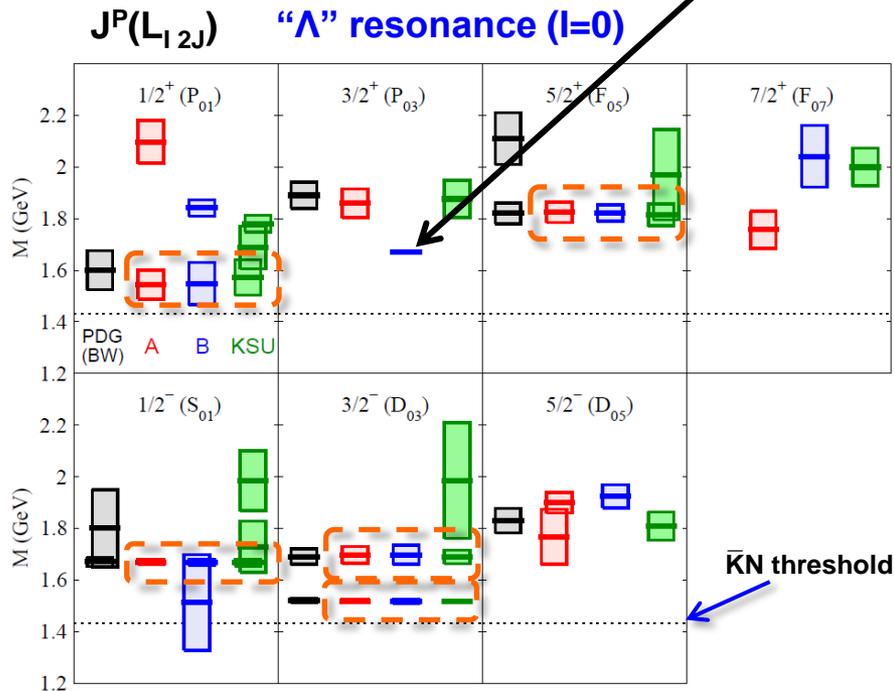
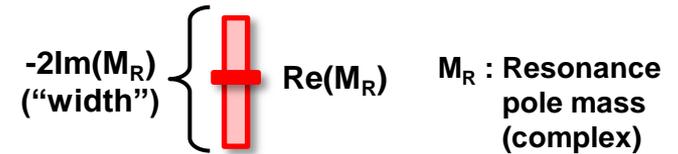
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New narrow $3/2^+$ resonance
 $M = 1671 - 5i$ MeV
near the $\eta\Lambda$ threshold !!



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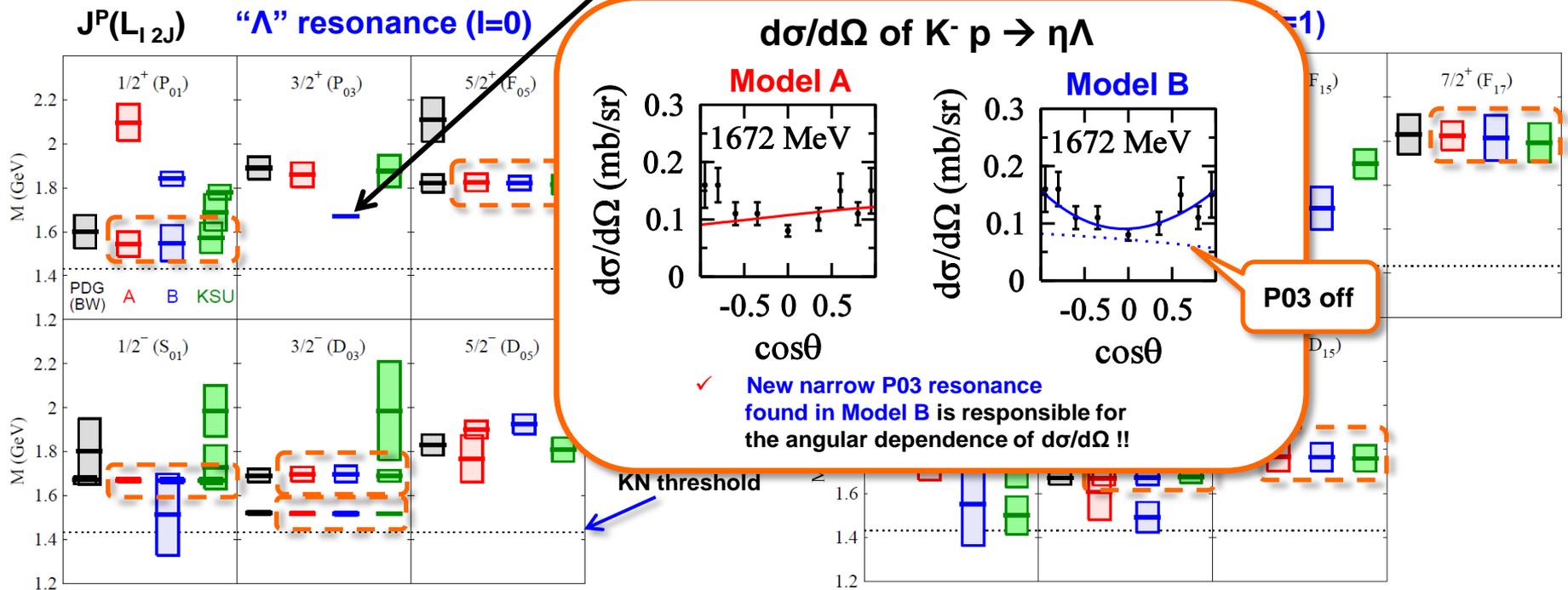
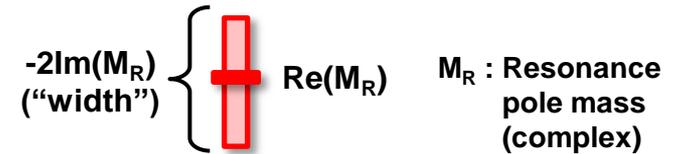
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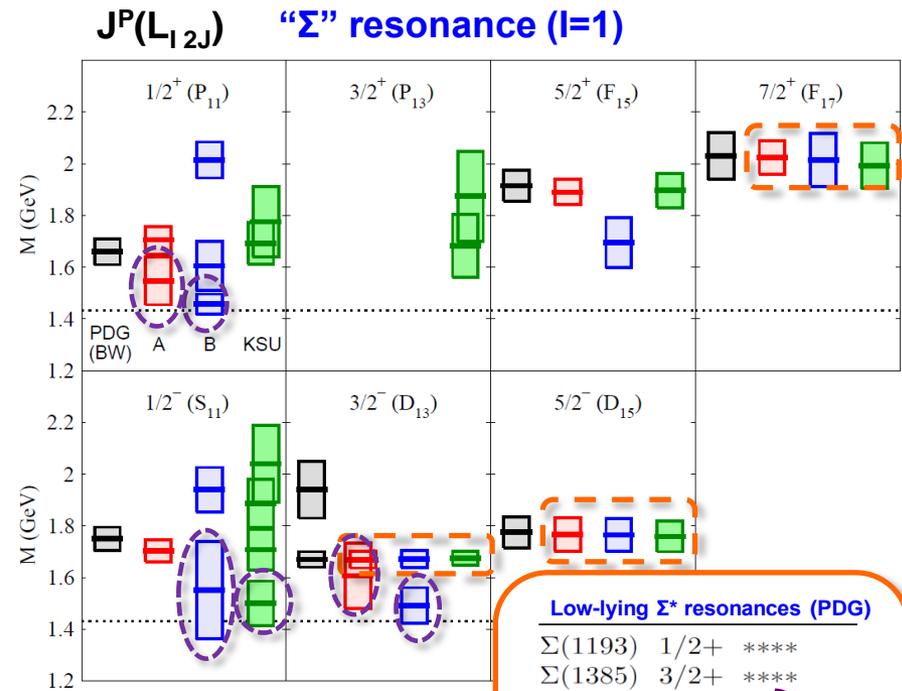
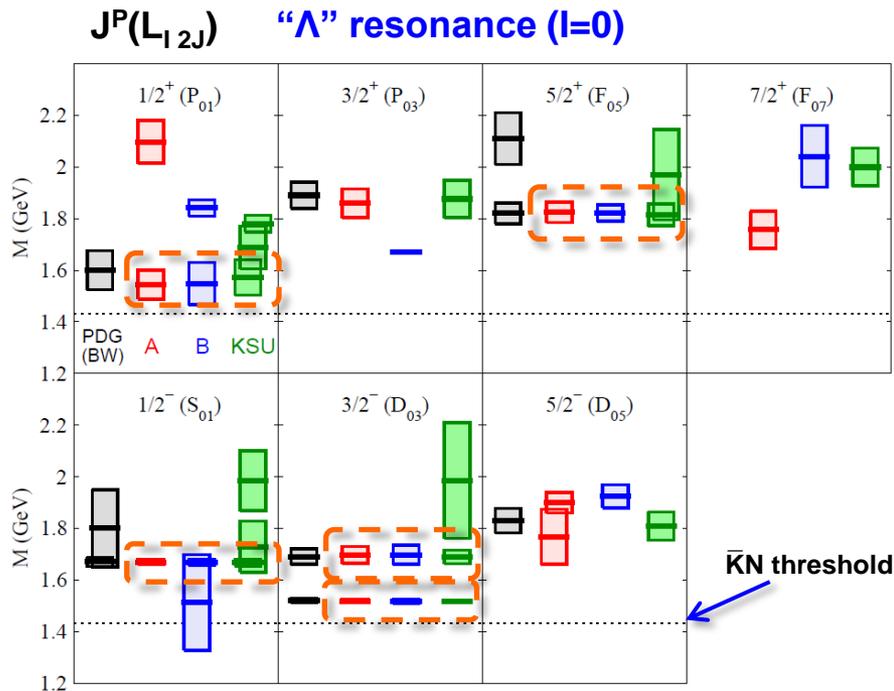
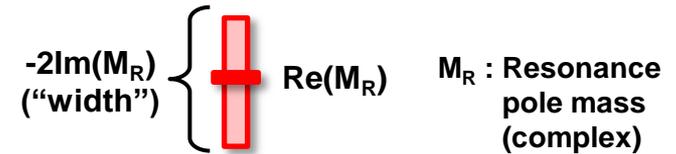
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Low-lying Σ^* resonances (PDG)

$\Sigma(1193)$	$1/2^+$	****
$\Sigma(1385)$	$3/2^+$	****
$\Sigma(1480)$		*
$\Sigma(1560)$		**
$\Sigma(1580)$	$3/2^-$	*
$\Sigma(1620)$	$1/2^-$	**
$\Sigma(1660)$	$1/2^+$	***
$\Sigma(1670)$	$3/2^-$	****

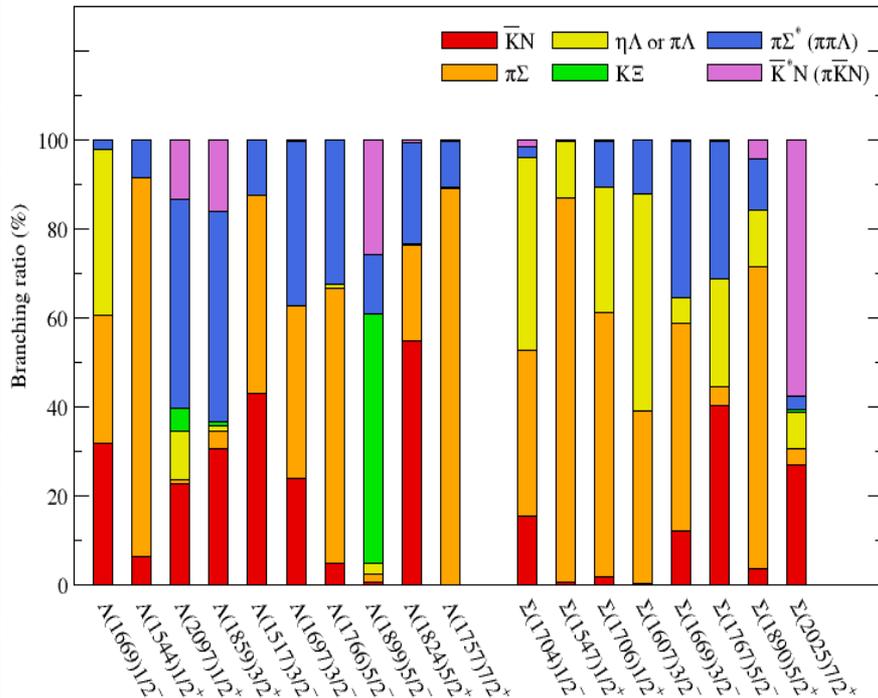
?

Importance of $2 \rightarrow 3$ reactions: Branching ratios of high-mass Y^* resonances

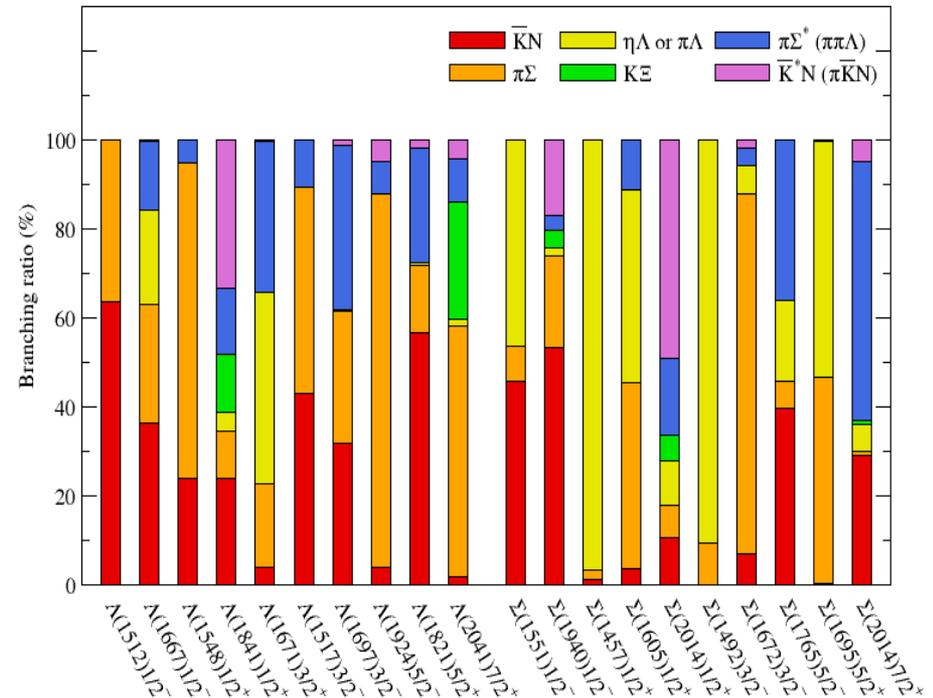
✓ High-mass Y^* have large branching ratio to $\pi\Sigma^*$ ($\pi\pi\Lambda$) & \bar{K}^*N ($\pi\bar{K}N$)

- $K^- p \rightarrow \pi\pi\Lambda, \pi\bar{K}N, \dots$ data would play a crucial role for establishing high-mass Y^* .
 - ➔ Similar to high-mass N^* and Δ^* case, where $\pi\pi N$ channel plays a crucial role. (e.g., measurement of $\pi N \rightarrow \pi\pi N$ reactions at **J-PARC E45**)

Model A



Model B

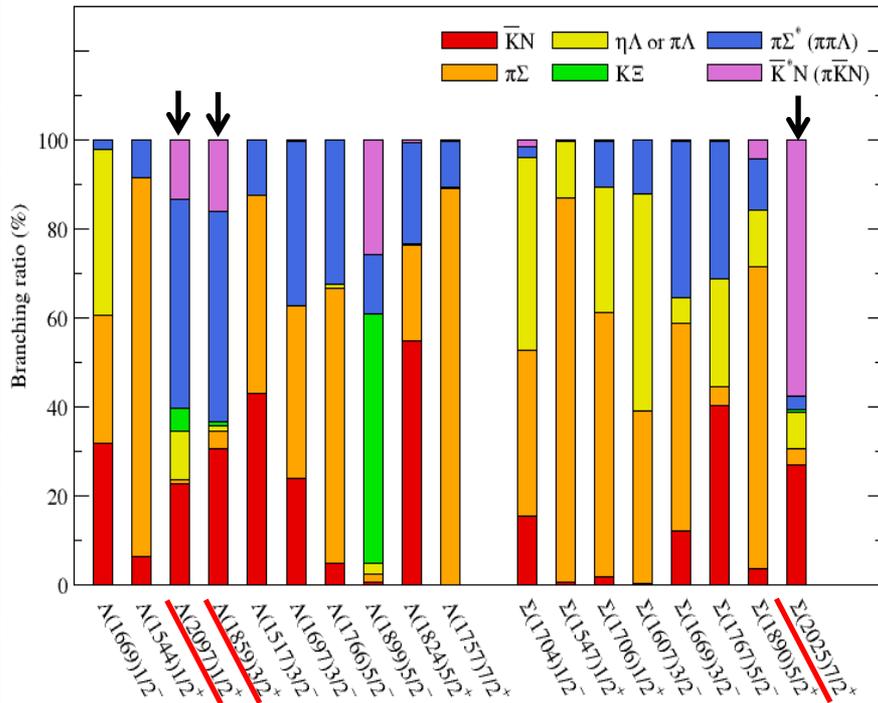


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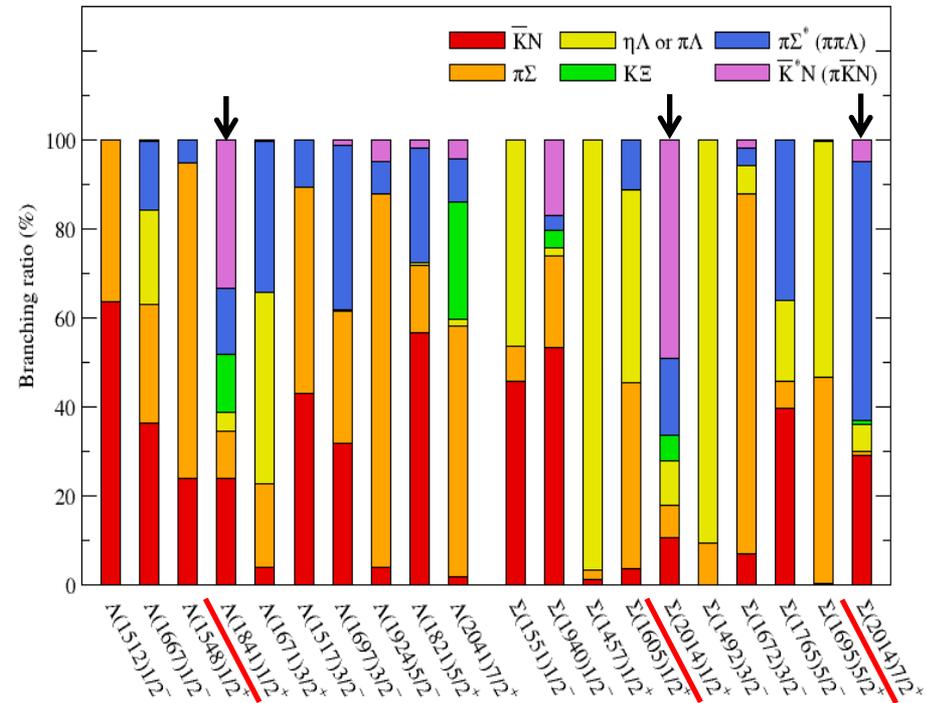
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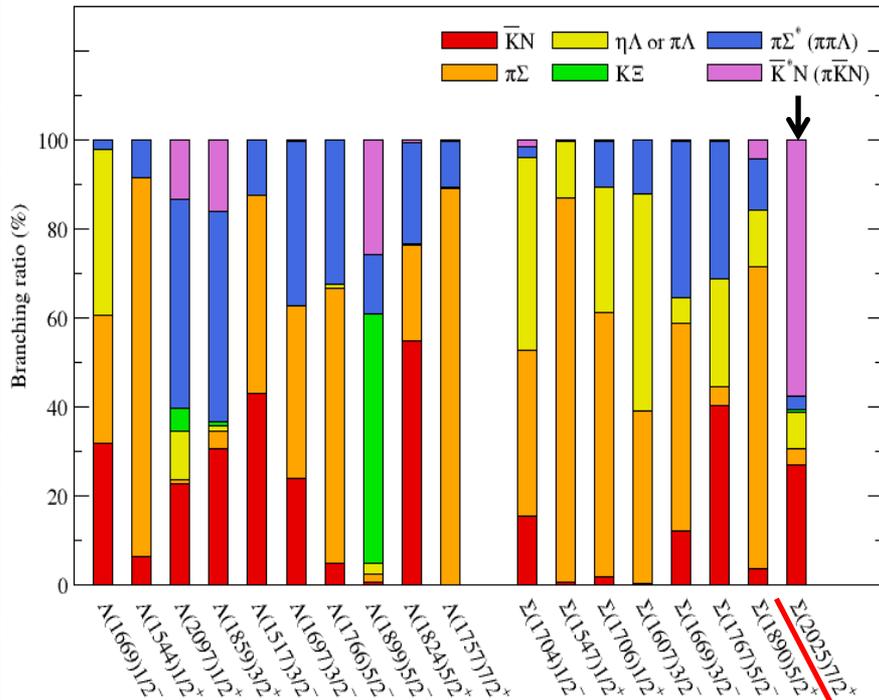
Model B



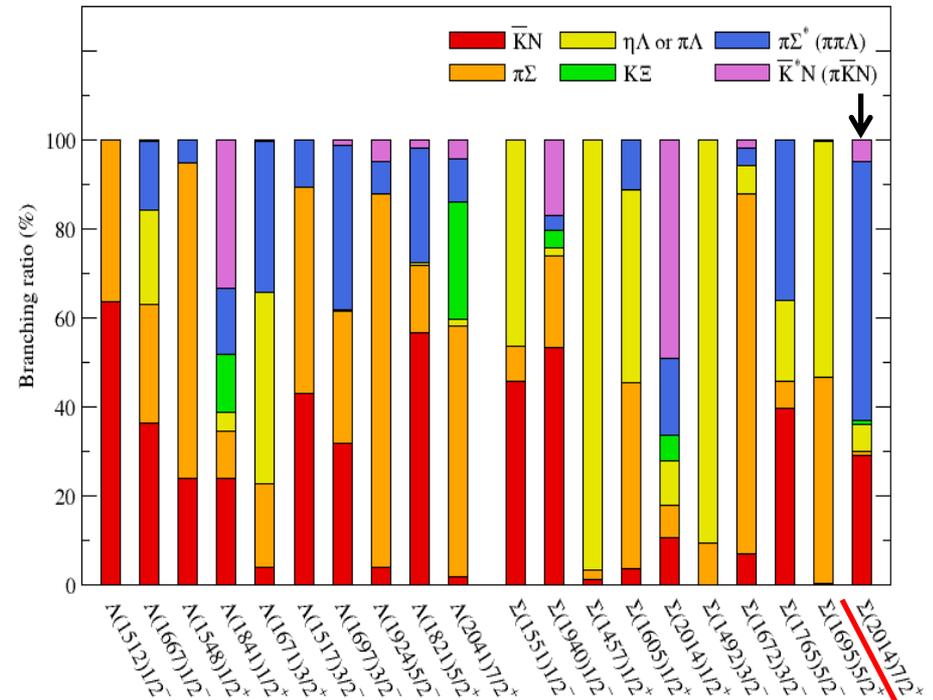
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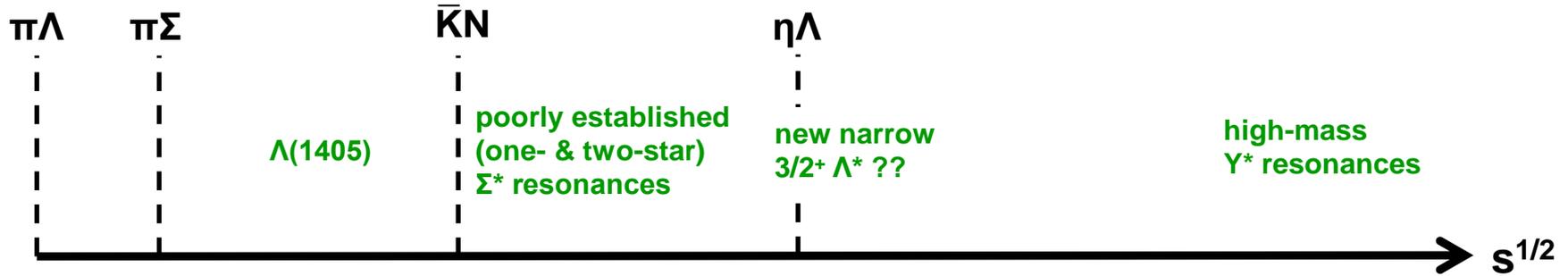
Model A



Model B

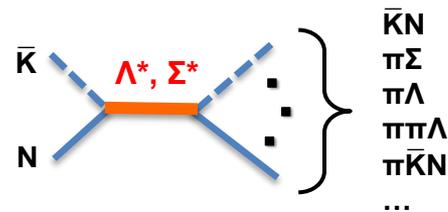


Strategy for establishing Y^* resonances using antikaon-induced reactions





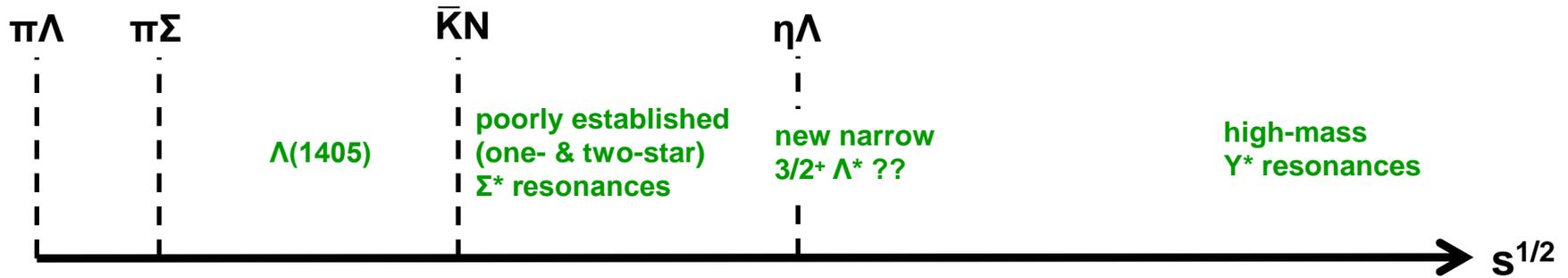
“Complete experiments” for $\bar{K}N \rightarrow \bar{K}N, \pi Y, \eta Y, K\Xi, \omega Y, \eta' Y, \dots$



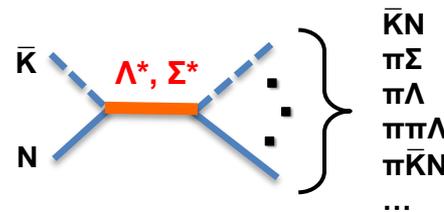


 $2 \rightarrow 3$ reactions: $\bar{K}N \rightarrow \pi\pi\Lambda, \pi\bar{K}N, \dots$

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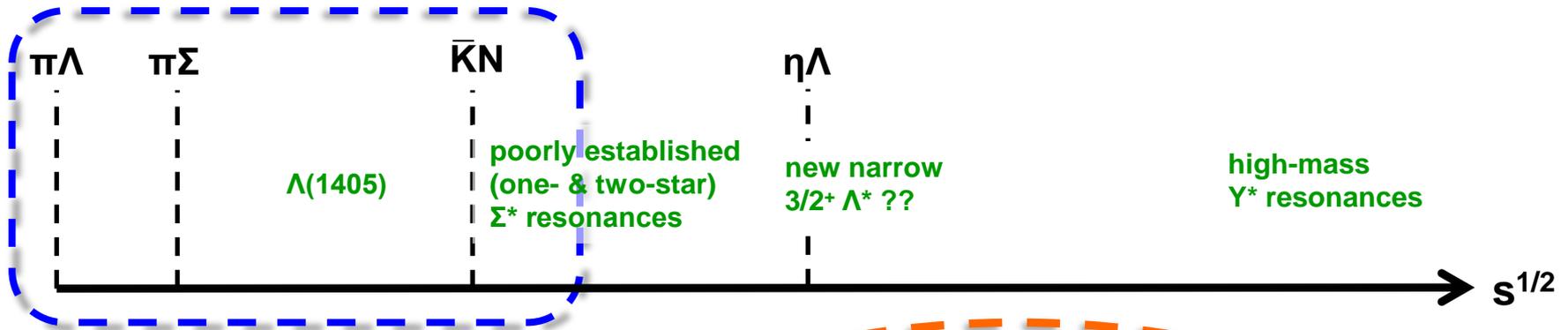
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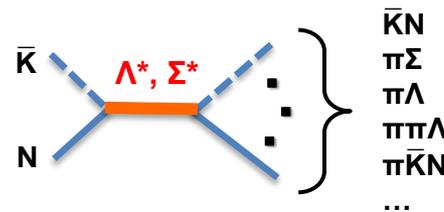
New measurements using HypTPC@J-PARC ??
 [discussions ongoing with J-PARC E45 members (H. Sako, K. Hicks et al.)]

Strategy for establishing Y^* resonances using antikaon-induced reactions



The region where $\bar{K}N$ reactions are not suitable for studying Y^* .

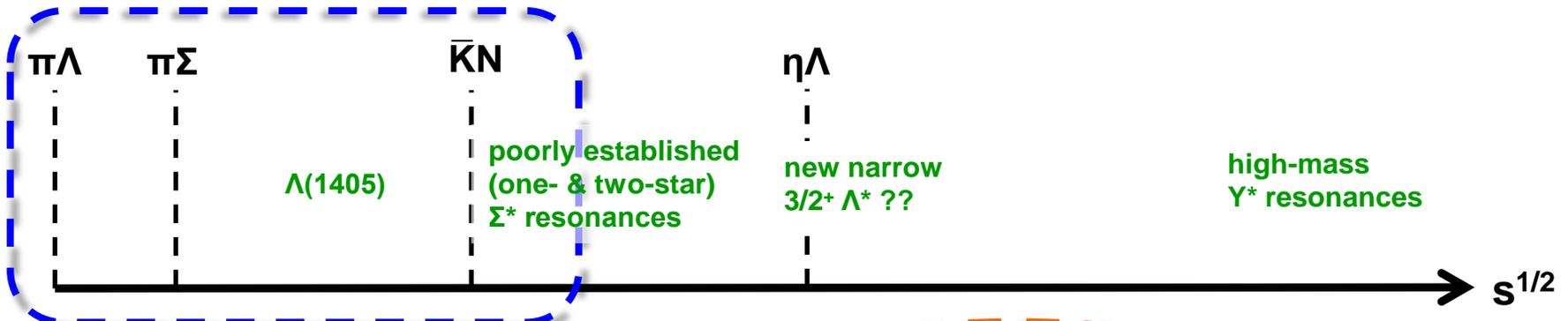
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Strategy for establishing Y^* resonances using antikaon-induced reactions



$\bar{K}d \rightarrow \pi Y N$

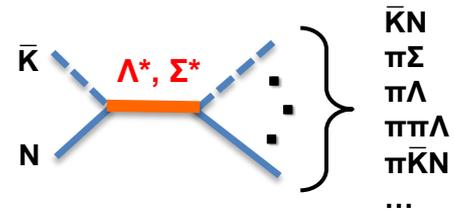


“Complete experiments” for $\bar{K}N \rightarrow \bar{K}N, \pi Y, \eta Y, K\Xi, \omega Y, \eta' Y, \dots$

\bar{K} d N π Y

(e.g, J-PARC E31)

Application of our DCC approach to $\bar{K}d$ reactions is underway, aiming at **COMBINED analysis of $\bar{K}N$ and $\bar{K}d$ reactions** !!!



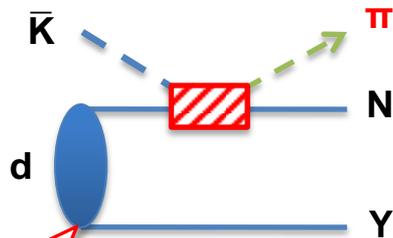
$2 \rightarrow 3$ reactions: $\bar{K}N \rightarrow \pi\pi\Lambda, \pi\bar{K}N, \dots$

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Model for deuteron-target reactions

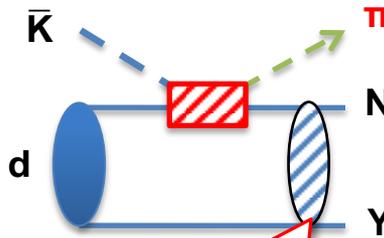
- ✓ Multistep processes are treated “perturbatively”.
- ✓ *Full-off-shell* amplitudes for meson-baryon sub-processes () are taken from **our dynamical coupled-channels model**. HK, Nakamura, Lee, Sato, PRC90(2014)065203

“Impulse” term



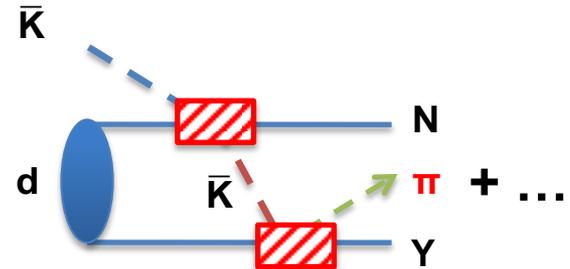
Use, e.g., deuteron w.f. from ANL-V18 potential [PRC51(1995)38]

“YN rescattering” term



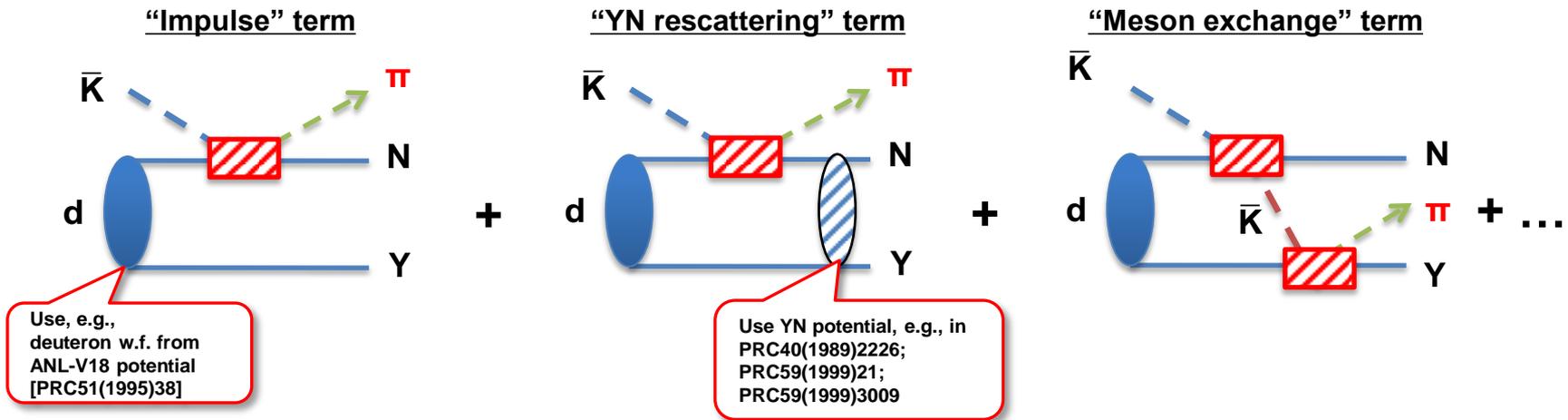
Use YN potential, e.g., in PRC40(1989)2226; PRC59(1999)21; PRC59(1999)3009

“Meson exchange” term



Model for deuteron-target reactions

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- ✓ **Full-off-shell** amplitudes for meson-baryon sub-processes () are taken from **our dynamical coupled-channels model**. HK, Nakamura, Lee, Sato, PRC90(2014)065203



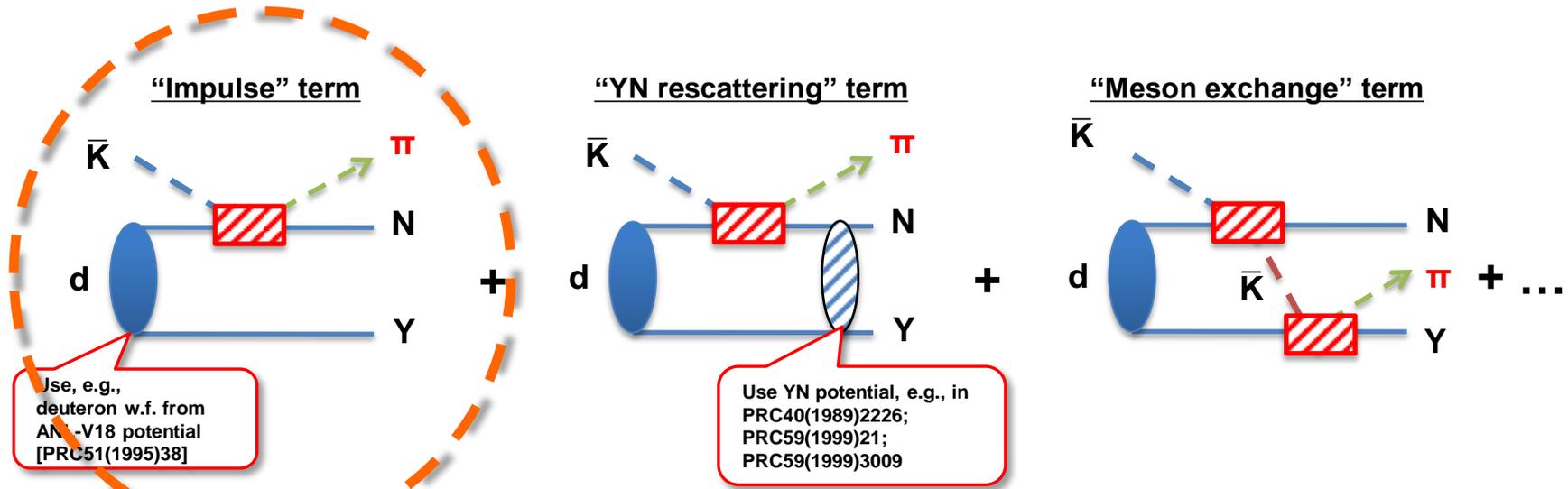
Unique feature of our work:

For meson-baryon sub-processes, we have **full-off-shell** amplitudes

- well-tested by $K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ up to $W = 2.1$ GeV.
- not only for S wave, **but also P, D, F waves.**

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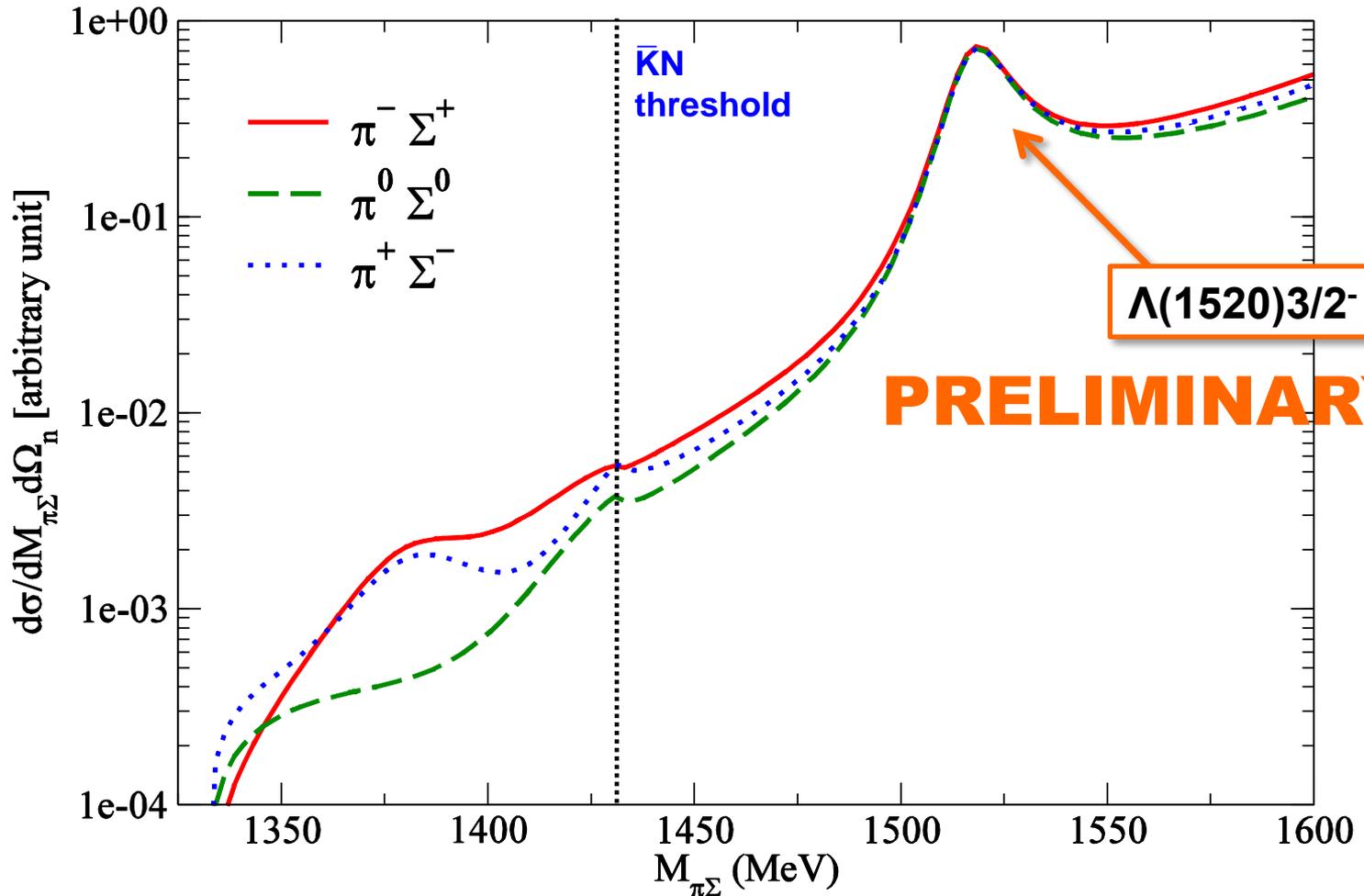
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Results (IMPULSE TERM ONLY !!)

$d\sigma/dM_{\pi\Sigma}d\Omega_n$ for $K^- d \rightarrow (\pi \Sigma)_0 n$
($P_{K^-} = 1 \text{ GeV}$, $\theta_n = 0 \text{ deg.}$)

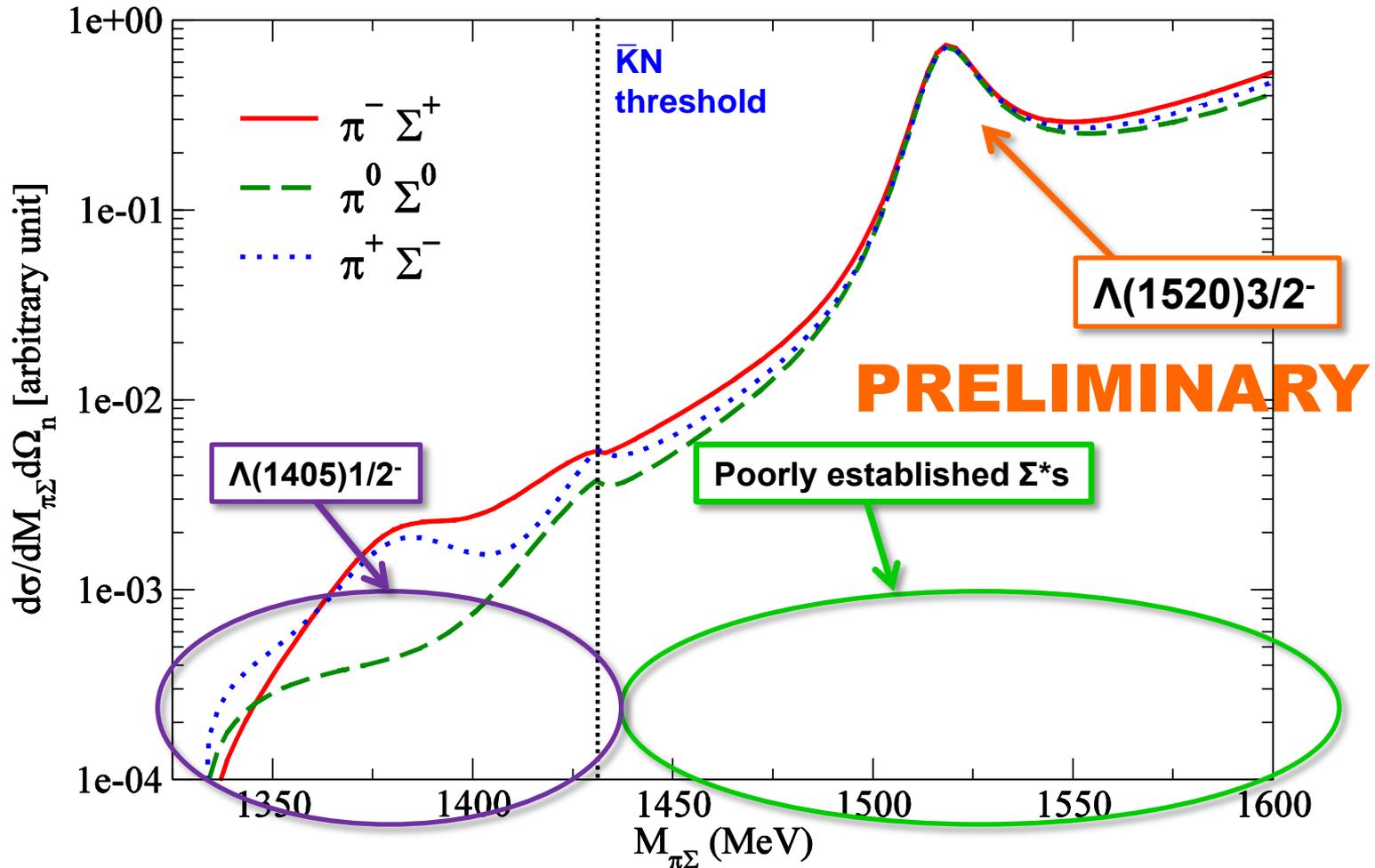
Same kinematics
as J-PARC E31



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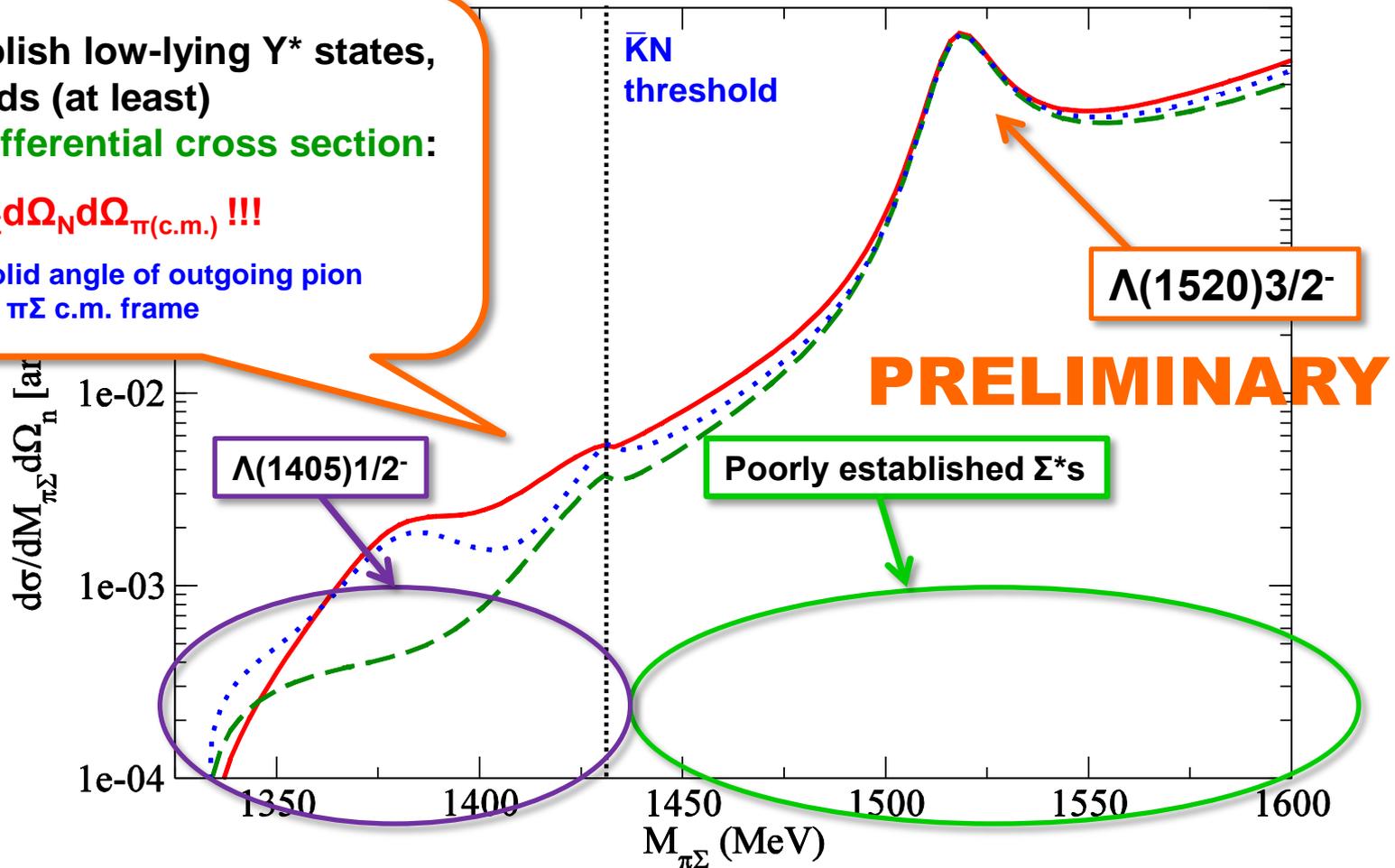
Same kinematics
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To establish low-lying Y^* states,
one needs (at least)

5-fold differential cross section:

$$d\sigma/dM_{\pi\Sigma}d\Omega_Nd\Omega_{\pi(c.m.)} !!!$$

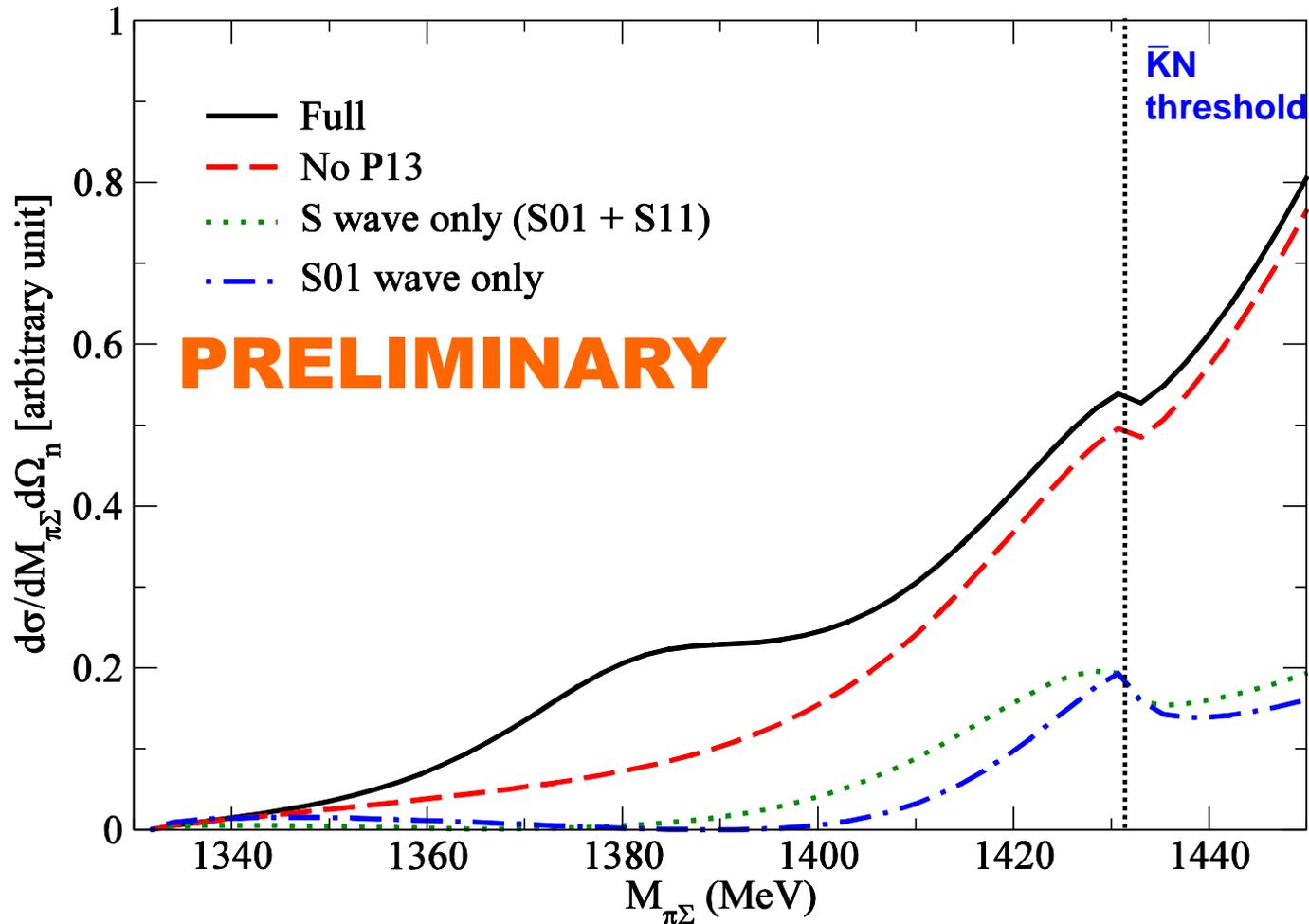
$\Omega_{\pi(c.m.)}$ = solid angle of outgoing pion
in $\pi\Sigma$ c.m. frame



Results (IMPULSE TERM ONLY !!)

$d\sigma/dM_{\pi\Sigma}d\Omega_n$ for $K^- d \rightarrow \pi^- \Sigma^+ n$
($P_{K^-} = 1 \text{ GeV}$, $\theta_n = 0 \text{ deg.}$)

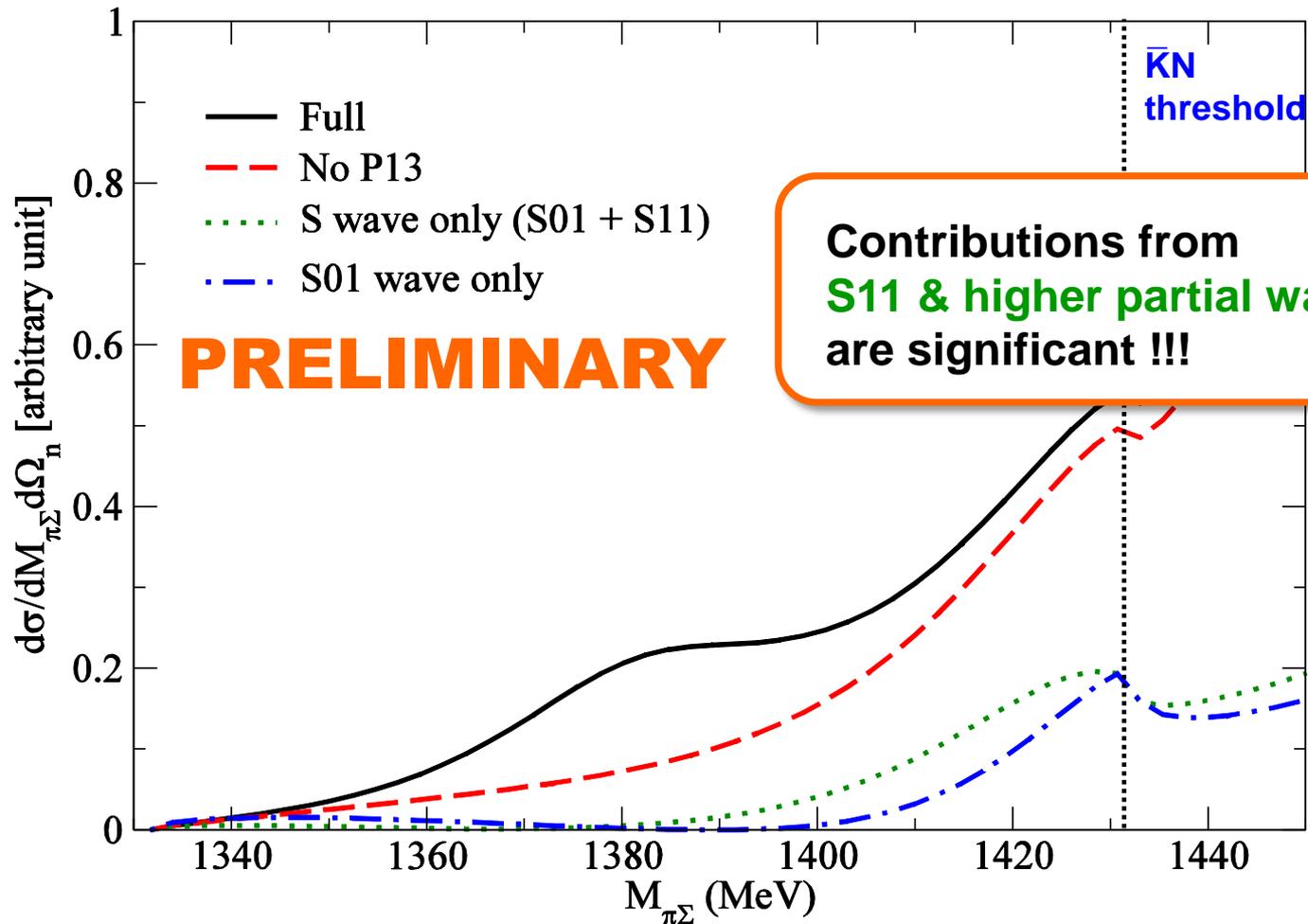
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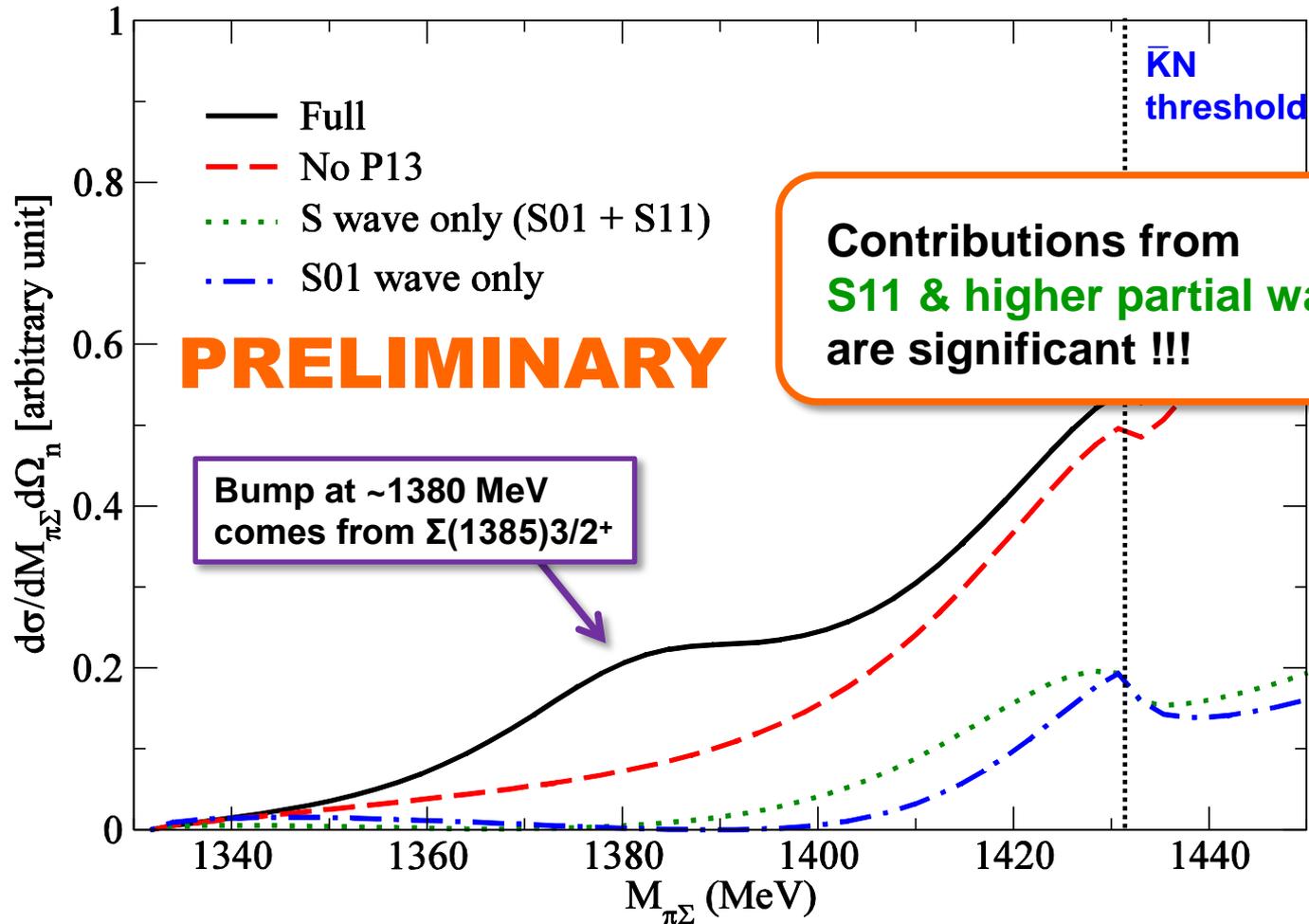
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Summary

- ✓ Accomplished comprehensive analysis of $K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$ up to $W = 2.1 \text{ GeV}$ within a dynamical coupled-channels approach.
- ✓ Successfully extracted **partial-wave amplitudes (up to F wave)** and Y^* resonance parameters defined by poles of amplitudes.
 - **New narrow $J^P = 3/2^+$ Λ^* resonance** ($M_R = 1672 - i5 \text{ MeV}$) located near the $\eta\Lambda$ threshold
 - **Unestablished low-lying Σ^* resonances** just above $\bar{K}N$ threshold

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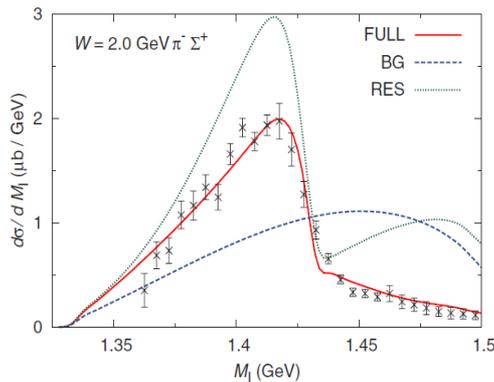
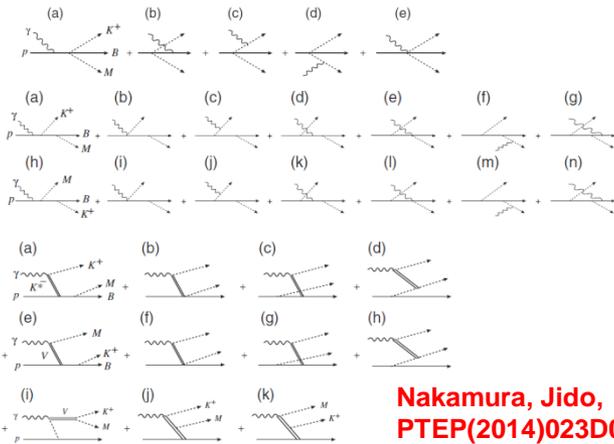
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 - **Unestablished low-lying Σ^* resonances** just above $\bar{K}N$ threshold
 - ✓ Presented preliminary results for **$\bar{K}d$ reaction model**.
 - ✓ New accurate data for **both $\bar{K}N$ and $\bar{K}d$ reactions** are much appreciated !!!
 - **“Complete experiments”** for $2 \rightarrow 2$ reaction ($\bar{K}N \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi, \eta\Sigma, \eta'Y, \omega Y, \Phi Y, \dots$)
 - $2 \rightarrow 3$ reaction ($\bar{K}N \rightarrow \pi\pi Y, \pi\bar{K}N, \dots$) to determine high-mass Y^*
 - Deuteron-target reaction ($\bar{K}d \rightarrow \pi YN, \dots$) to determine low-lying Y^*
- “ $K_L^0 p \rightarrow$ (final states with $S=-1$) ” reactions exclusively produce $l = 1 \Sigma^*$ resonances in direct s-channel processes due to the isospin filter !!**

Back up

How we study the region below the $\bar{K}N$ threshold ?

$\gamma p \rightarrow K^+\pi\Sigma$ @CLAS

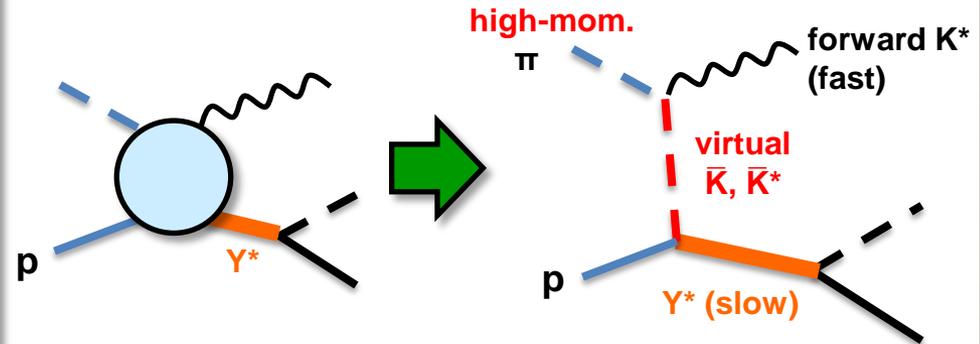
At the CLAS energy, **many** production processes contribute and sizably affect mass distributions as **backgrounds**.



Large model/analysis dependence from complicated production processes.

→ Makes unambiguous determination of $\Lambda(1405)$ difficult.

Forward $p(\pi, K^*)X$ reactions with **high-momentum pion beam** (→ J-PARC E50)



- For forward K^* (small t), the processes are dominated by diffractive t-channel exchange processes.
- We DO have fully unitarized $\bar{K}N \rightarrow MB$ and $\bar{K}^*N \rightarrow MB$ half off-shell amplitudes !!
- 12 GeV JLab can do a similar measurement by replacing incident π by high-energy photon.

➤ Useful also for determining **low-lying Σ^* resonances**

Low-lying Σ^* resonances(PDG)

$\Sigma(1193)$	1/2+	****
$\Sigma(1385)$	3/2+	****
$\Sigma(1480)$		*
$\Sigma(1560)$		**
$\Sigma(1580)$	3/2-	*
$\Sigma(1620)$	1/2-	**
$\Sigma(1660)$	1/2+	***
$\Sigma(1670)$	3/2-	****

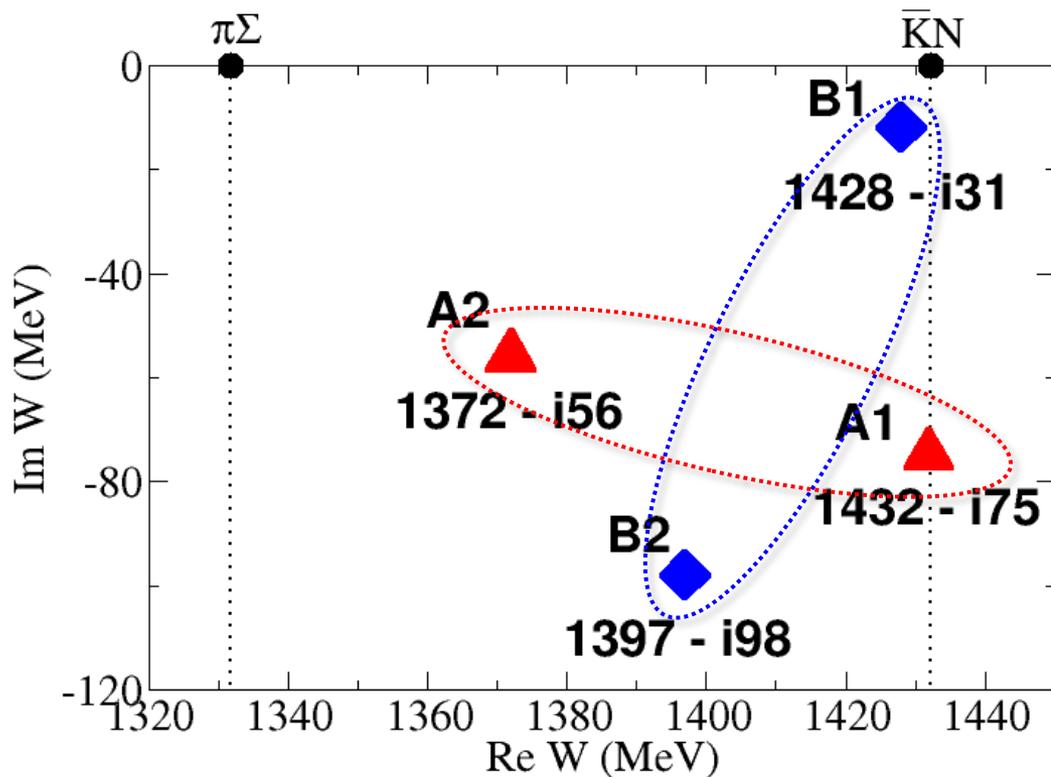
?

S-wave resonances below $\bar{K}N$ threshold from the current analysis

HK, Nakamura, Lee, Sato, PRC92(2015)025205

NOTE: Further extensive analysis including the data below $\bar{K}N$ threshold is necessary to have *conclusive* results for the $\bar{K}N$ subthreshold region.

“Predicted” Λ^* ($J^P = 1/2^-$) resonance poles below $\bar{K}N$ threshold



✓ Two resonance poles are found in both Models A and B.

➤ A1 & B1 seem correspond to $\Lambda(1405)$

➤ Another Λ resonance with mass 30-60 MeV lower than $\Lambda(1405)$ (A2 & B2) is also found to exist.

Red triangles: Model A

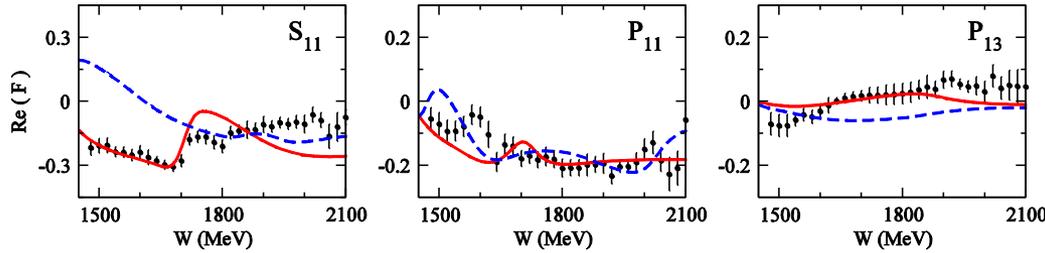
Blue diamonds: Model B

New data can eliminate analysis dependence ??

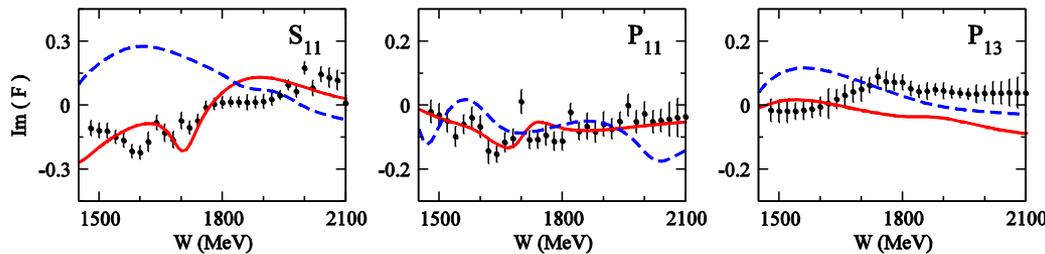
Extracted $\bar{K}N \rightarrow \pi\Lambda$ amplitudes

HK, Nakamura, Lee, Sato,
PRC90(2014)065204;92(2015)025205

Real parts



Imaginary parts

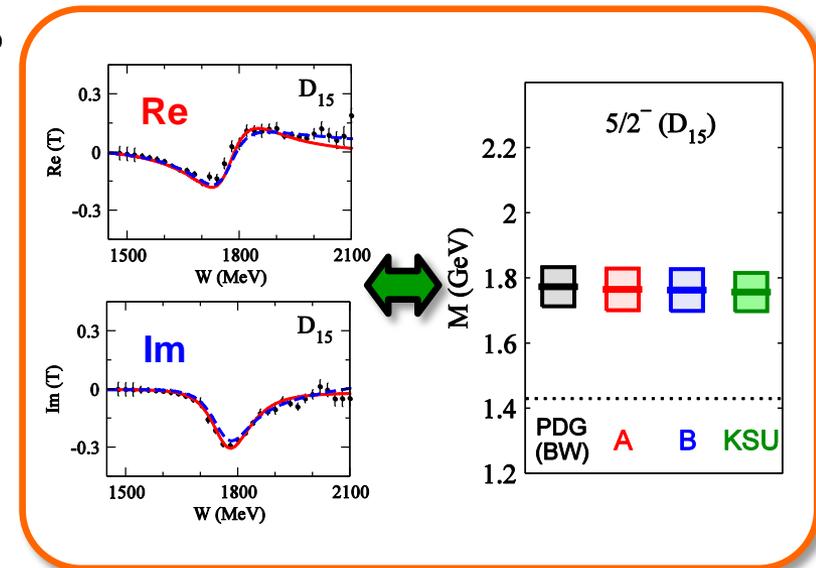
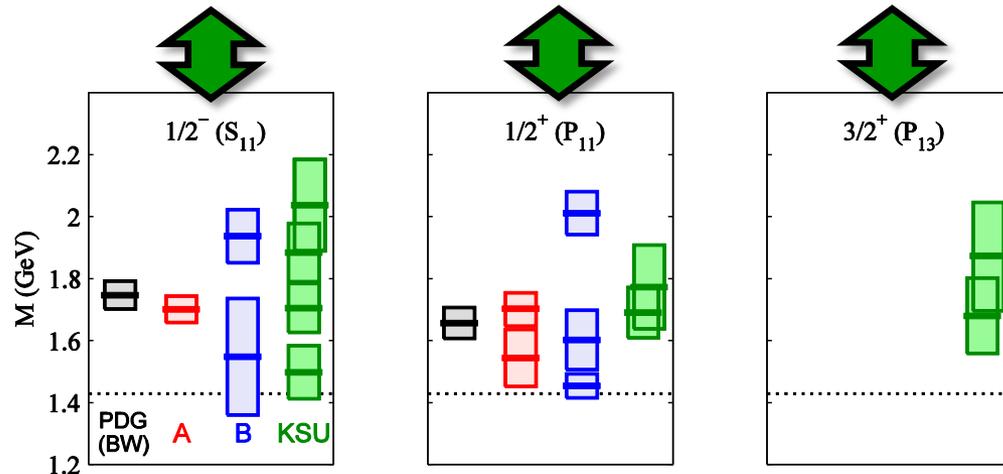


L_{I2J} : $L = S, P, \dots$; $I =$ isospin;
 $J =$ Total angular mom.

Red : Model A

Blue: Model B

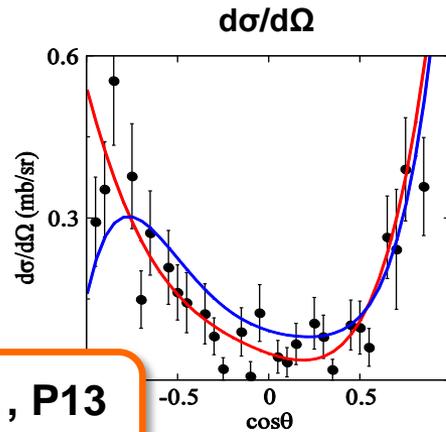
Circles: KSU single-energy solution
[PRC88(2013)035204]



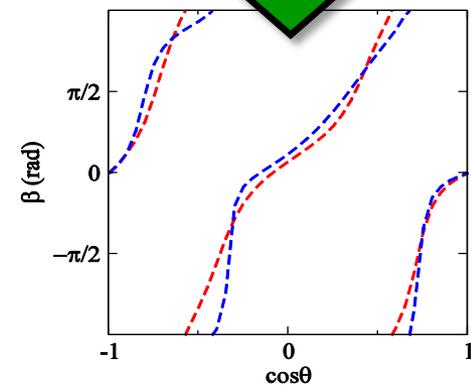
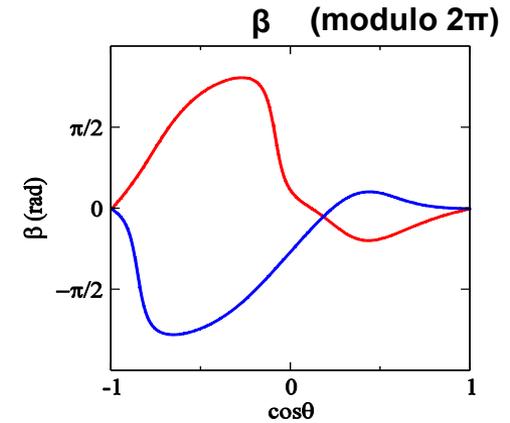
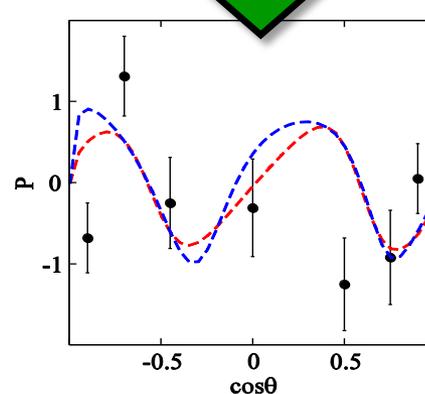
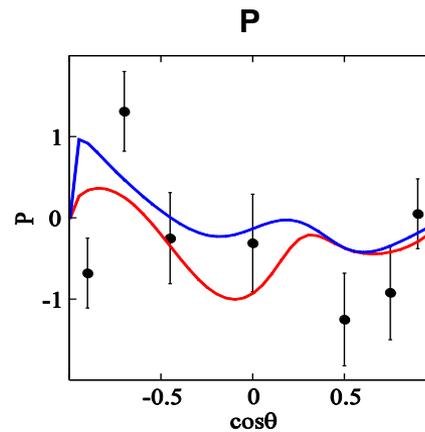
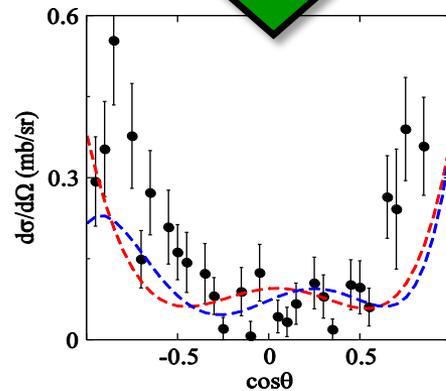
New data can eliminate analysis dependence ??

$K^-p \rightarrow \pi^0\Lambda$ observables @ $W = 1700$ MeV

Red: Model A
Blue: Model B

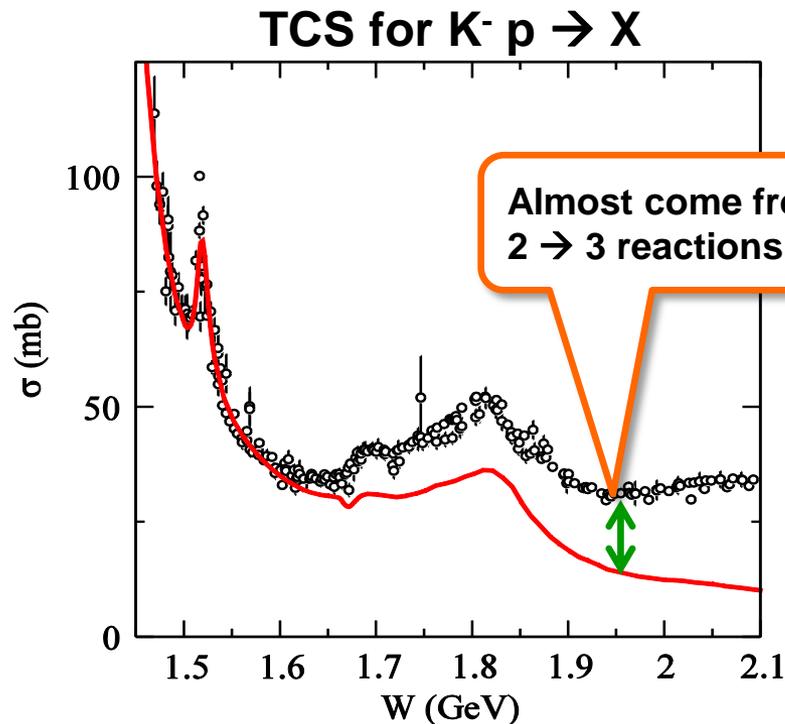


S11, P11, P13 waves off



- At this energy, the difference between Models A & B **mostly comes from S11, P11, P13 waves**.
- High statistics data (of **P and β in particular**) will reduce significantly the analysis dependence !!!

Importance of $2 \rightarrow 3$ reactions: Dominance of cross sections at high W



— Sum of $K^- p \rightarrow \bar{K}N, \pi\Sigma, \pi\Lambda, \eta\Lambda, K\Xi$
(Computed with Model A)

Almost come from
 $2 \rightarrow 3$ reactions !!

TCS for $2 \rightarrow 3$ reactions
($K^- p \rightarrow \pi\pi\Lambda, \pi\bar{K}N, \dots$):

- significant above $W \sim 1.7$ GeV.
- even larger than the $2 \rightarrow 2$ TCS above $W \sim 1.9$ GeV !!

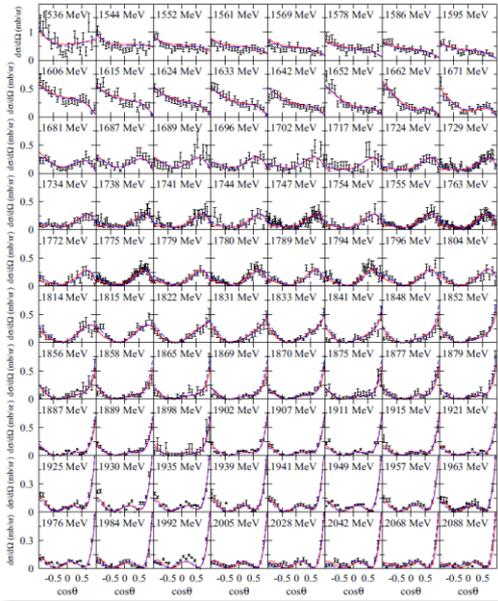
Effects of **3-body channels** on Y^* resonance parameters are expected to be sizable.



However, at present **essentially no differential cross section data** are available for $2 \rightarrow 3$ reactions that can be used for **detailed partial wave analyses** !!

Our strategy for light-quark baryon spectroscopy

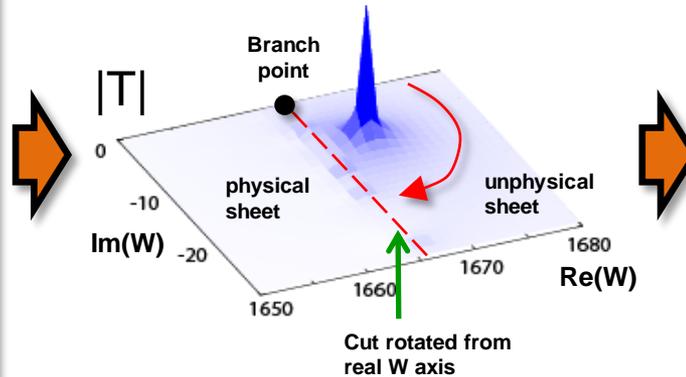
1) Construct a model by making χ^2 -fit of the **world data** of **meson production reactions**:



- ▶ Partial-wave amplitudes, scattering length, ... etc. are extracted.
- ▶ Use **supercomputers** to accomplish coupled-channels analyses:

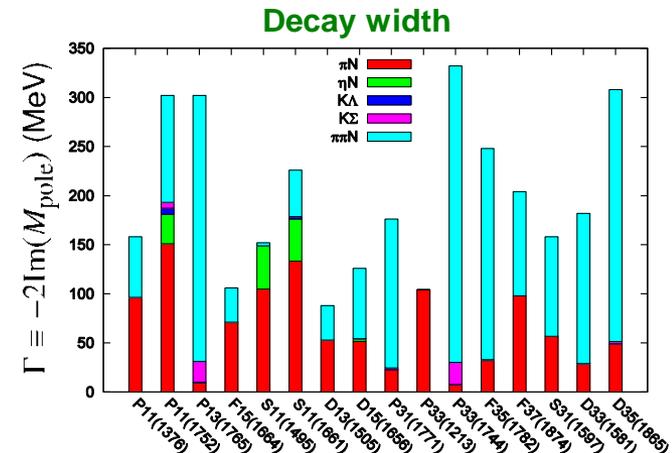
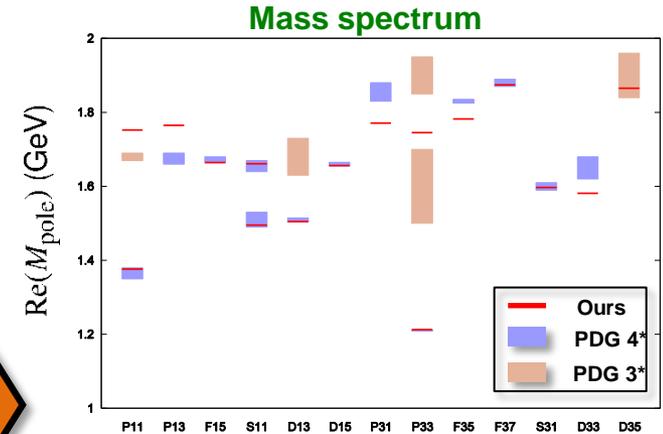


2) Search **poles** of determined scattering amplitudes by making **analytic continuation** to a **complex energy plane**.



- Pole position** → (complex) resonance mass
- Residues** → coupling strengths between Y^* and MB

3) Extract resonance parameters **defined by poles**.



Extracted scattering lengths and effective ranges

HK, Nakamura, Lee, Sato, PRC90(2014)065204

Scattering length and effective range

	Model A		Model B	
	$I = 0$	$I = 1$	$I = 0$	$I = 1$
$a_{\bar{K}N}$ (fm)	$-1.37 + i0.67$	$0.07 + i0.81$	$-1.62 + i1.02$	$0.33 + i0.49$
$a_{\eta\Lambda}$ (fm)	$1.35 + i0.36$	-	$0.97 + i0.51$	-
$a_{K\Xi}$ (fm)	$-0.81 + i0.14$	$-0.68 + i0.09$	$-0.89 + i0.13$	$-0.83 + i0.03$
$r_{\bar{K}N}$ (fm)	$0.67 - i0.25$	$1.01 - i0.20$	$0.74 - i0.25$	$-1.03 + i0.19$
$r_{\eta\Lambda}$ (fm)	$-5.67 - i2.24$	-	$-5.82 - i3.32$	-
$r_{K\Xi}$ (fm)	$-0.01 - i0.33$	$-0.42 - i0.49$	$0.13 - i0.20$	$-0.22 - i0.11$

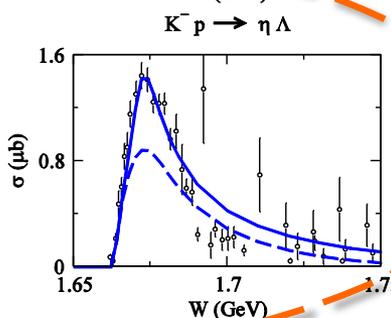
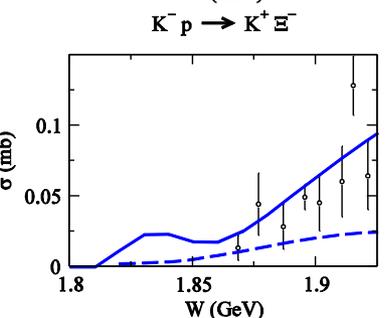
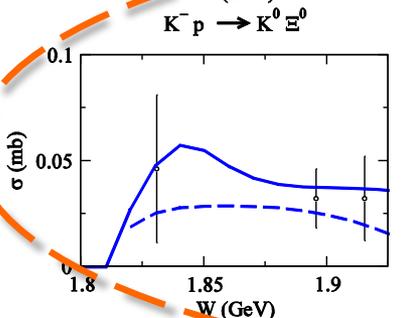
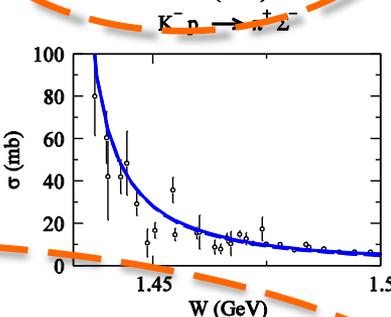
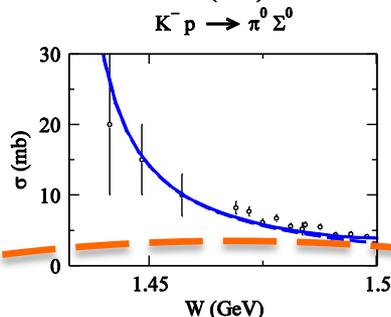
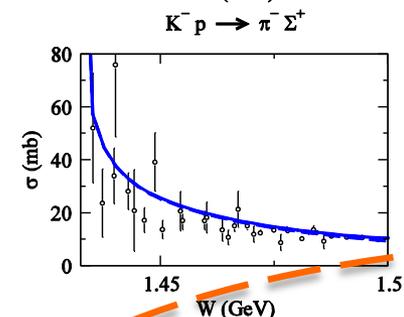
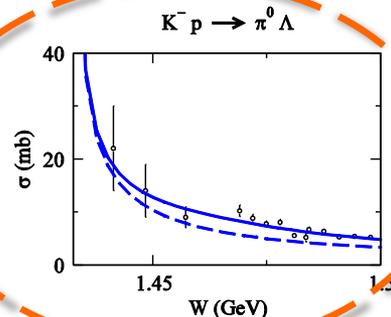
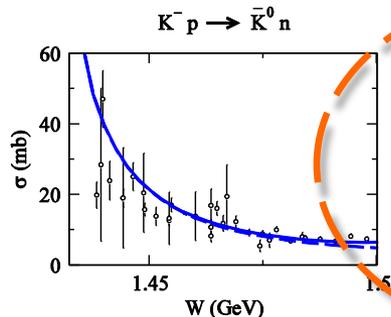
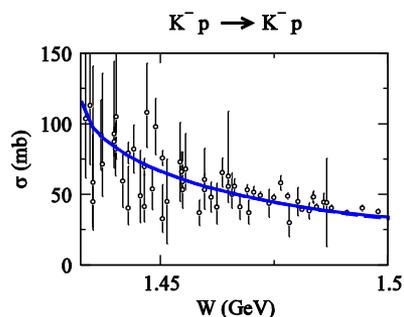
$$a_{K-p} = -0.65 + i0.74 \text{ fm (Model A)}$$

$$a_{K-p} = -0.65 + i0.76 \text{ fm (Model B)}$$

S-wave dominance ??

$K^- p \rightarrow MB$ total cross sections near threshold

Model B



Solid: Full
Dashed: S wave only

**For $K^- p \rightarrow \pi \Lambda, \eta \Lambda, K \Xi$,
higher partial waves
visibly contribute
to the cross sections
even in the threshold
region.**

→ consistent with the observation in
Jackson et al., PRC91(2015)065208



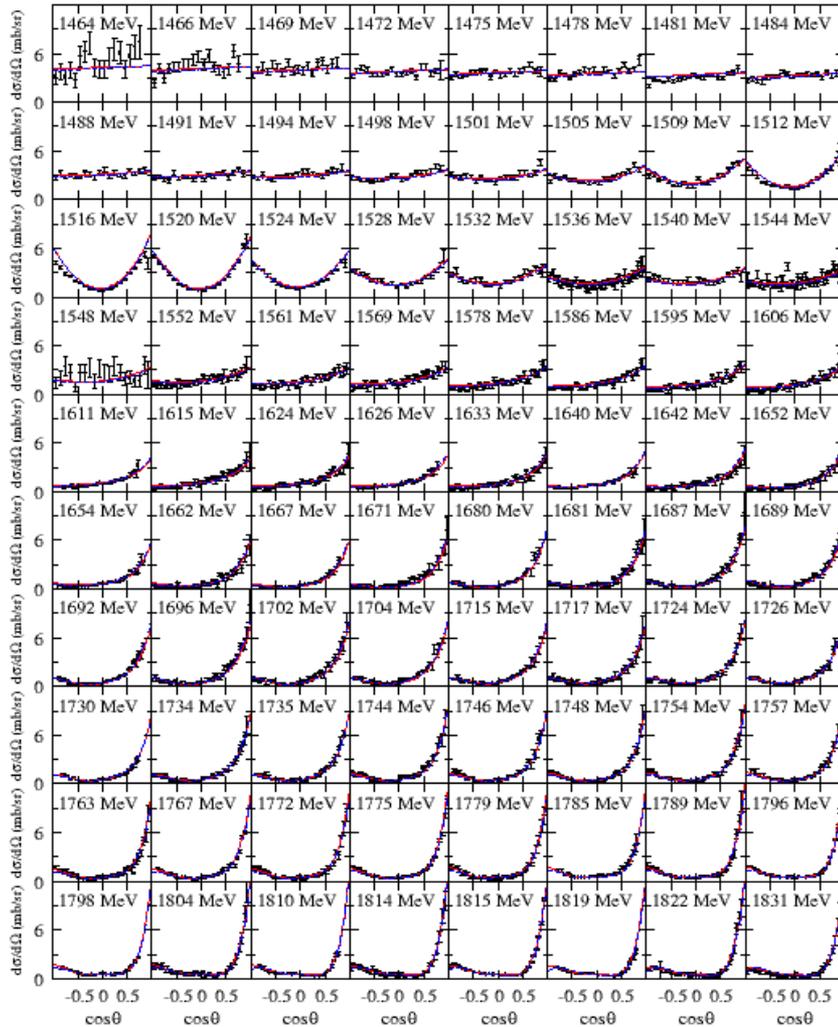
**Naïve expectation for
S-wave dominance
near the threshold
sometimes does not hold !!**

Results of the fits

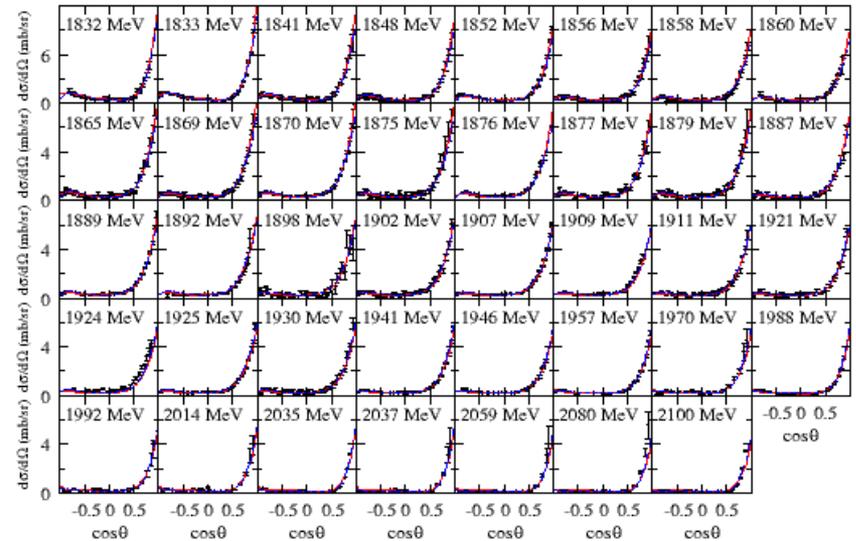
$K^- p \rightarrow K^- p$ scattering

HK, Nakamura, Lee, Sato, PRC90(2014)065204

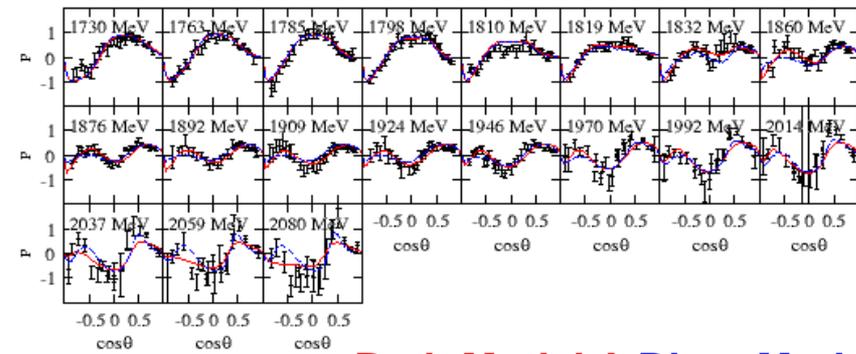
$d\sigma/d\Omega$ (1464 < W < 1831 MeV)



$d\sigma/d\Omega$ (1832 < W < 2100 MeV)



P



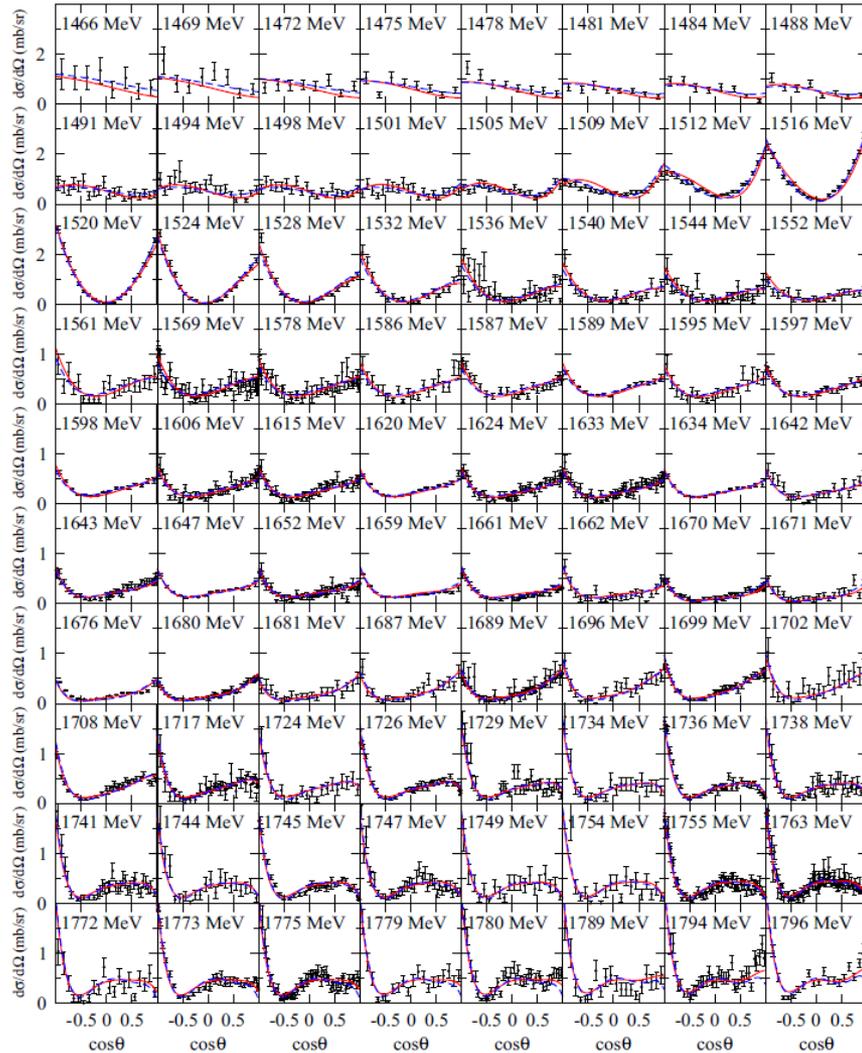
Red: Model A Blue: Model B

Results of the fits

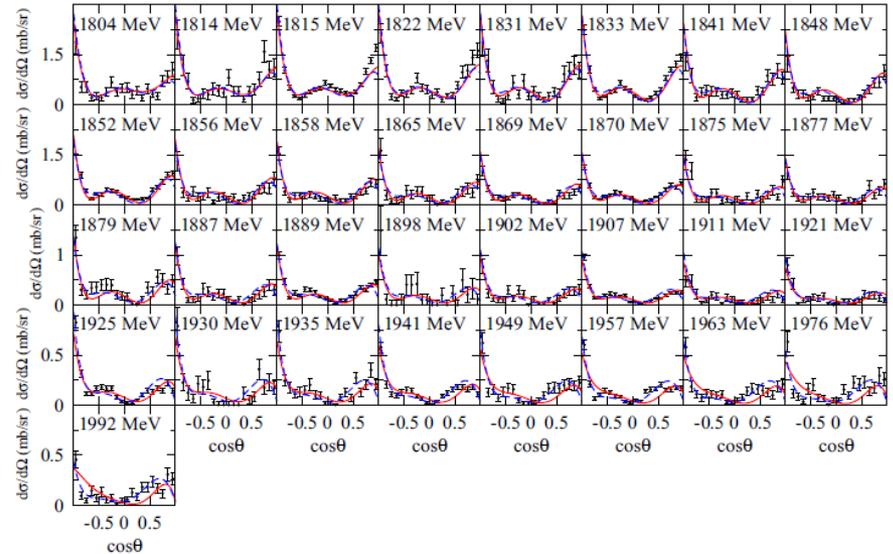
$K^- p \rightarrow K^0 n$ reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$d\sigma/d\Omega$ ($1466 < W < 1796$ MeV)



$d\sigma/d\Omega$ ($1804 < W < 1992$ MeV)



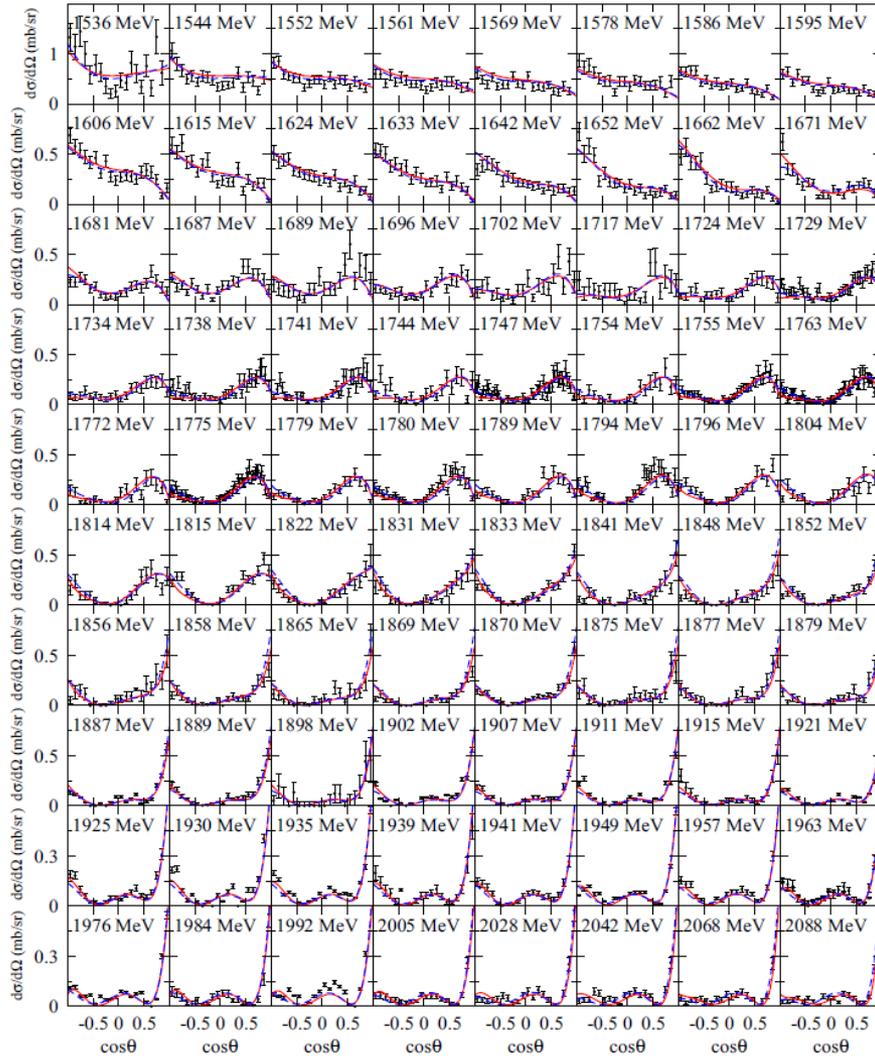
Red: Model A Blue: Model B

Results of the fits

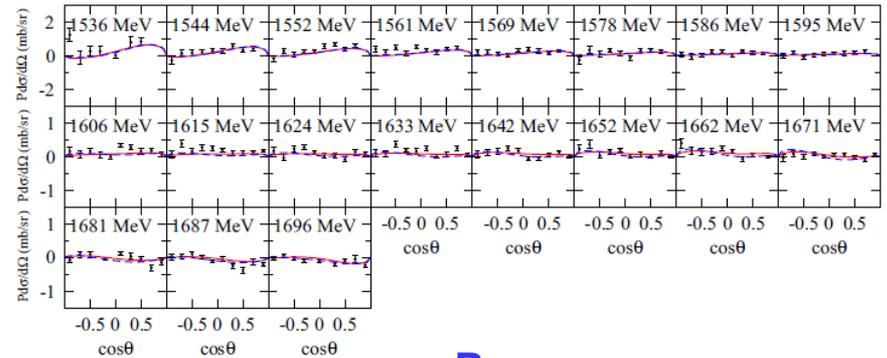
$K^- p \rightarrow \pi^- \Sigma^+$ reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

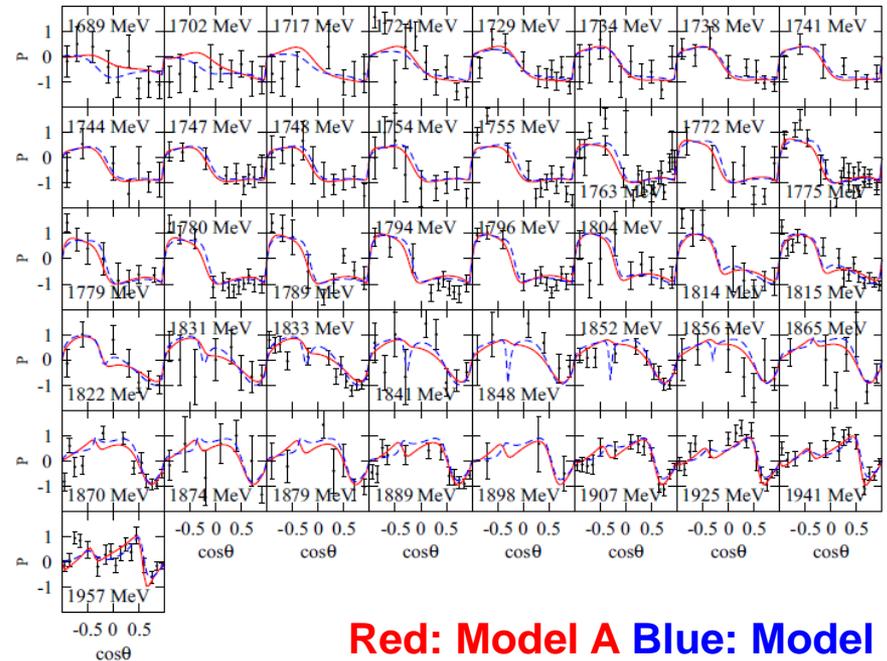
$d\sigma/d\Omega$



$P \times d\sigma/d\Omega$



P



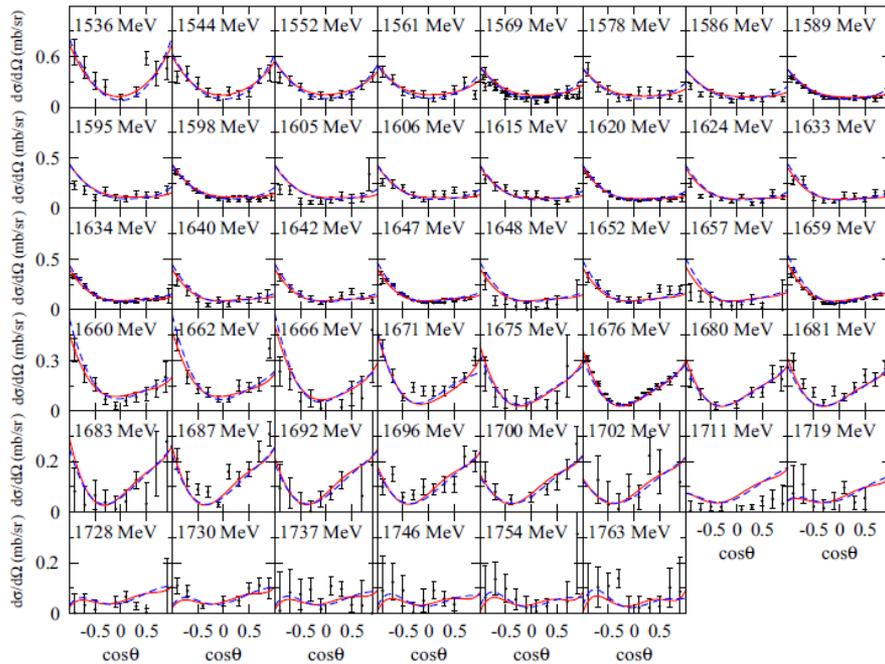
Red: Model A Blue: Model B

Results of the fits

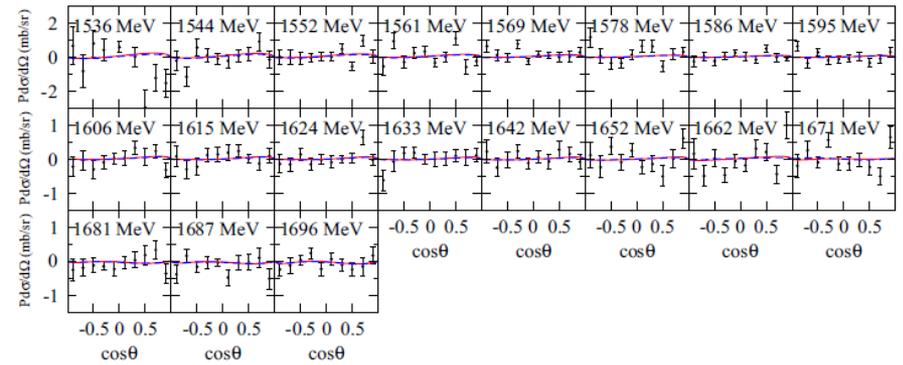
$K^- p \rightarrow \pi^0 \Sigma^0$ reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

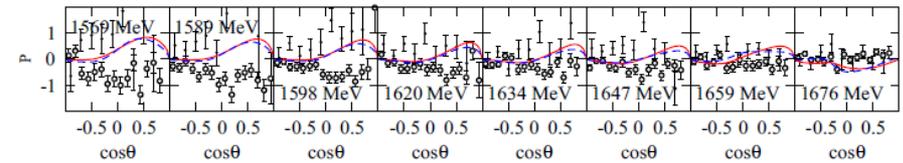
$d\sigma/d\Omega$



$P \times d\sigma/d\Omega$



P



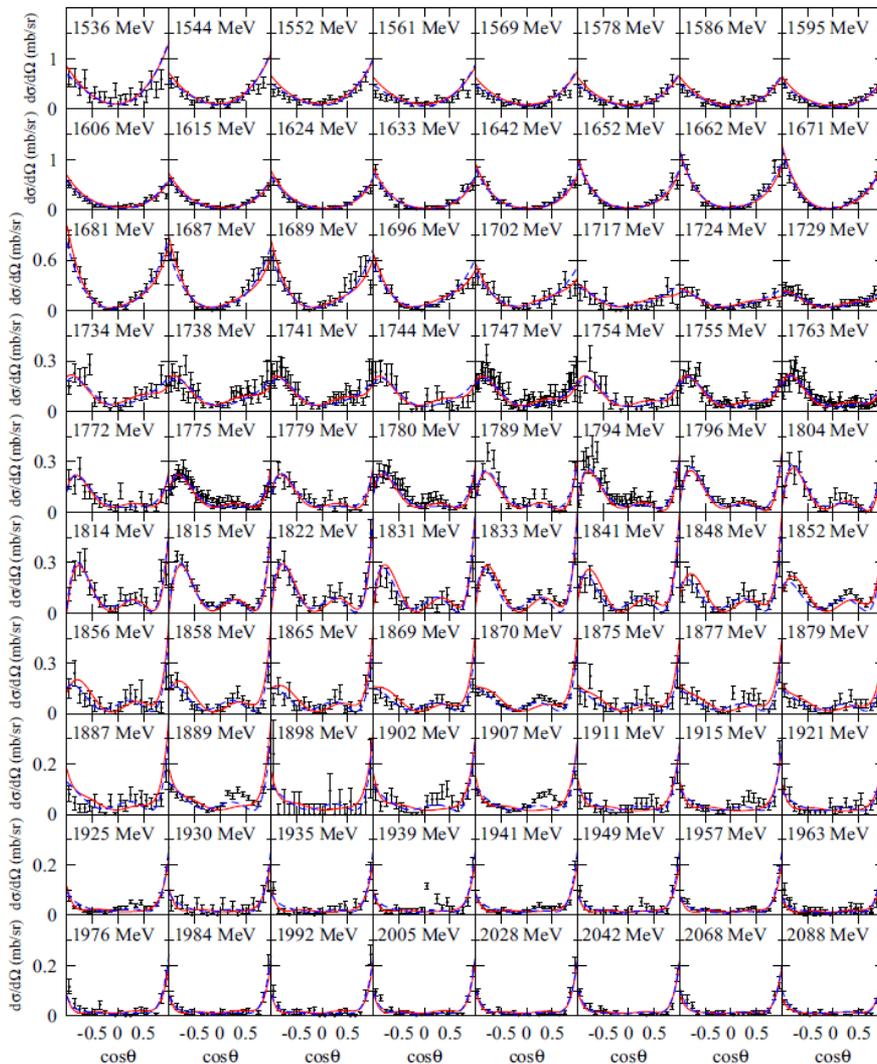
Red: Model A Blue: Model B

Results of the fits

$K^- p \rightarrow \pi^+ \Sigma^-$ reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$d\sigma/d\Omega$



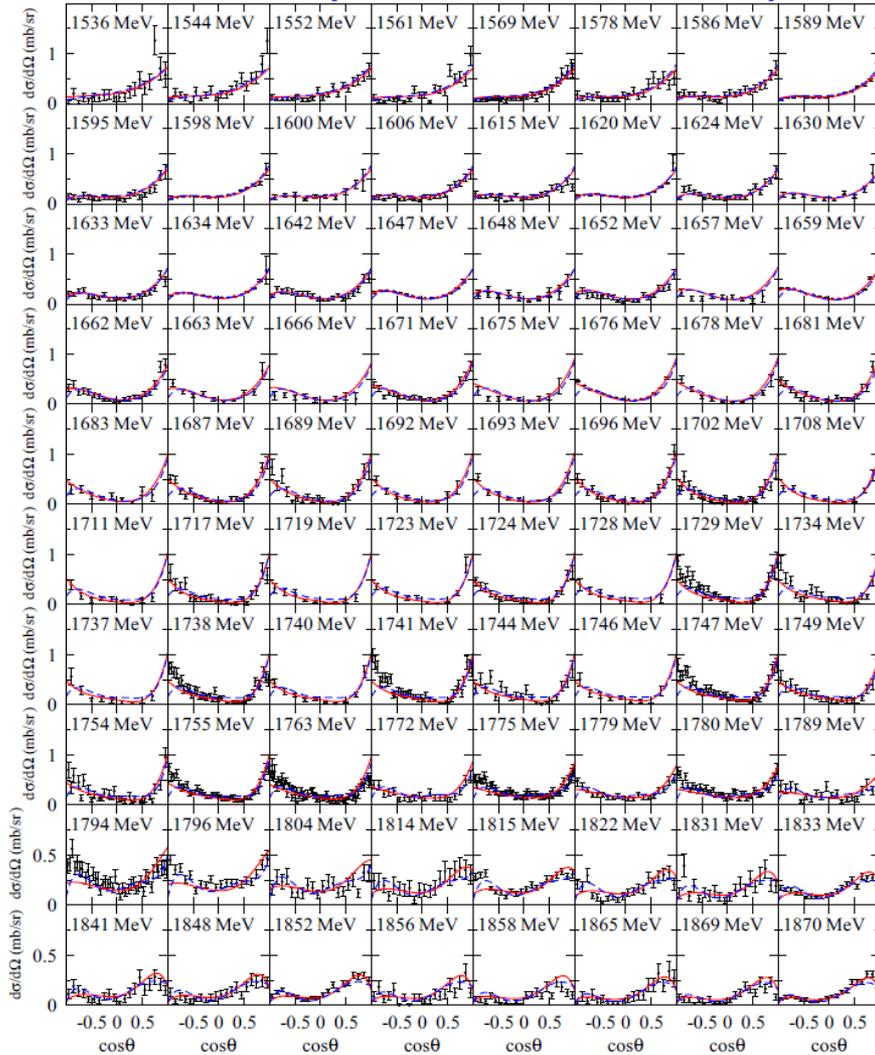
Red: Model A Blue: Model B

Results of the fits

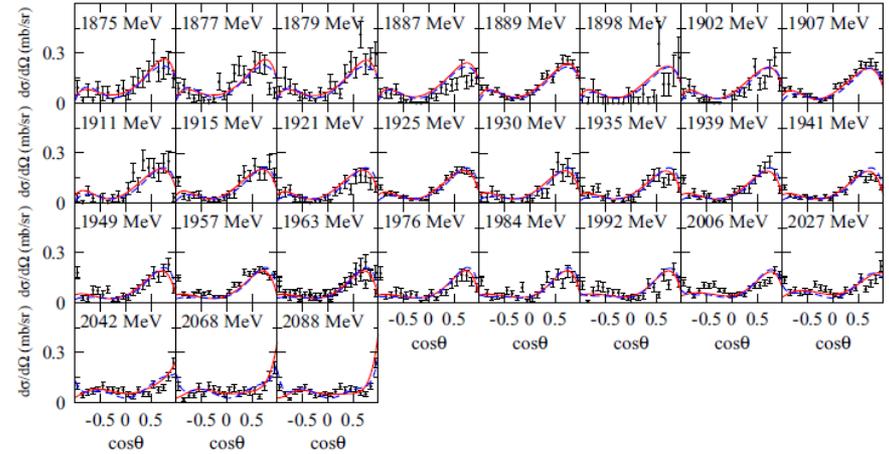
$K^- p \rightarrow \pi^0 \Lambda$ reaction

HK, Nakamura, Lee, Sato, PRC90(2014)065204

$d\sigma/d\Omega$ (1536 < W < 1870 MeV)



$d\sigma/d\Omega$ (1875 < W < 2088 MeV)



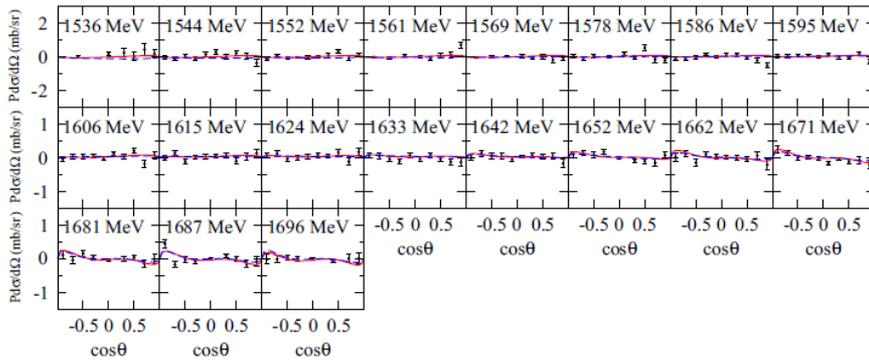
Red: Model A Blue: Model B

Results of the fits

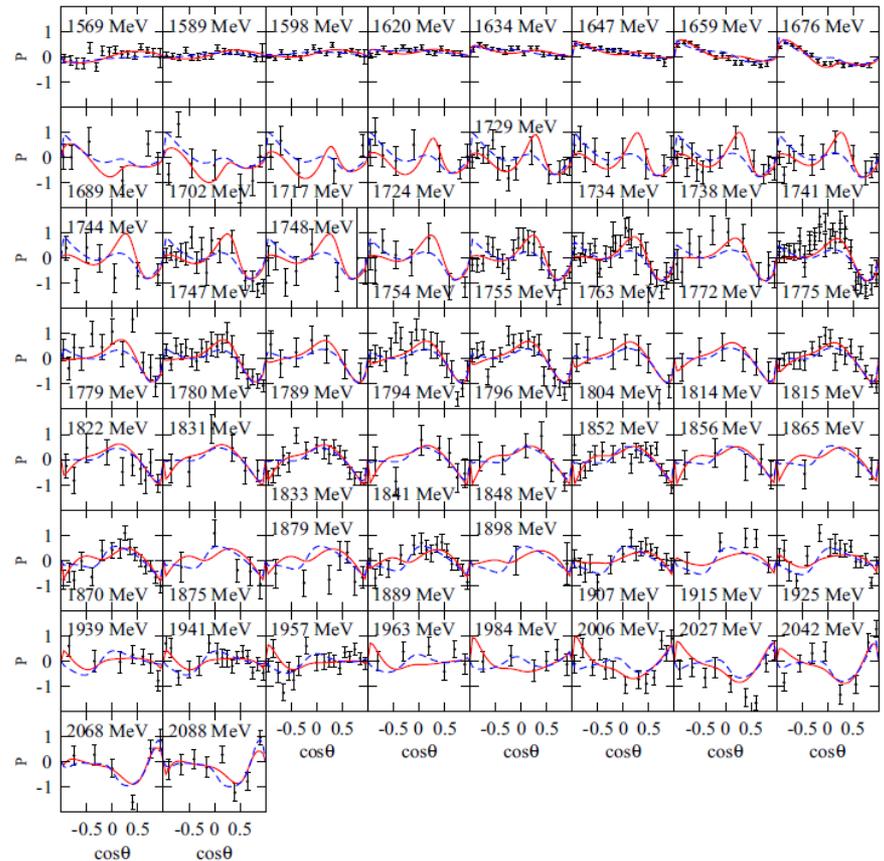
HK, Nakamura, Lee, Sato, PRC90(2014)065204

$K^- p \rightarrow \pi^0 \Lambda$ reaction (cont'd)

$P \times d\sigma/d\Omega$



P



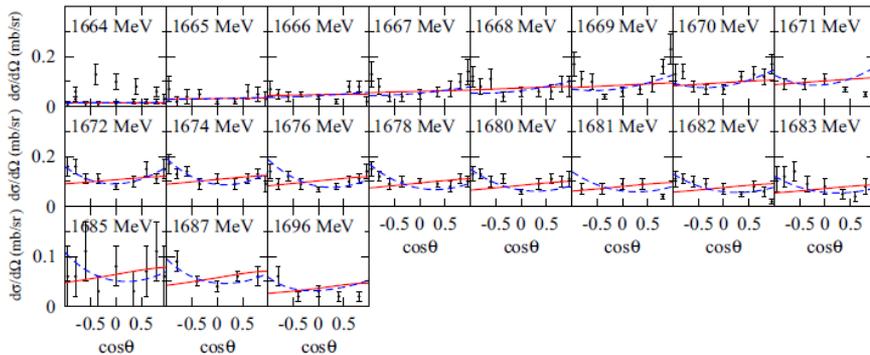
Red: Model A Blue: Model B

Results of the fits

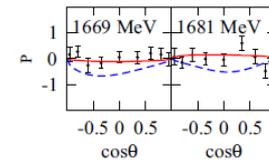
HK, Nakamura, Lee, Sato, PRC90(2014)065204

$K^- p \rightarrow \eta \Lambda$ reaction

$d\sigma/d\Omega$

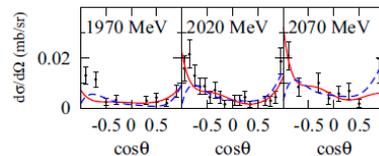


P



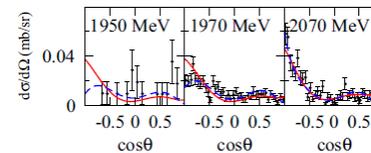
$K^- p \rightarrow K^0 \Xi^0$ reaction

$d\sigma/d\Omega$



$K^- p \rightarrow K^+ \Xi^-$ reaction

$d\sigma/d\Omega$

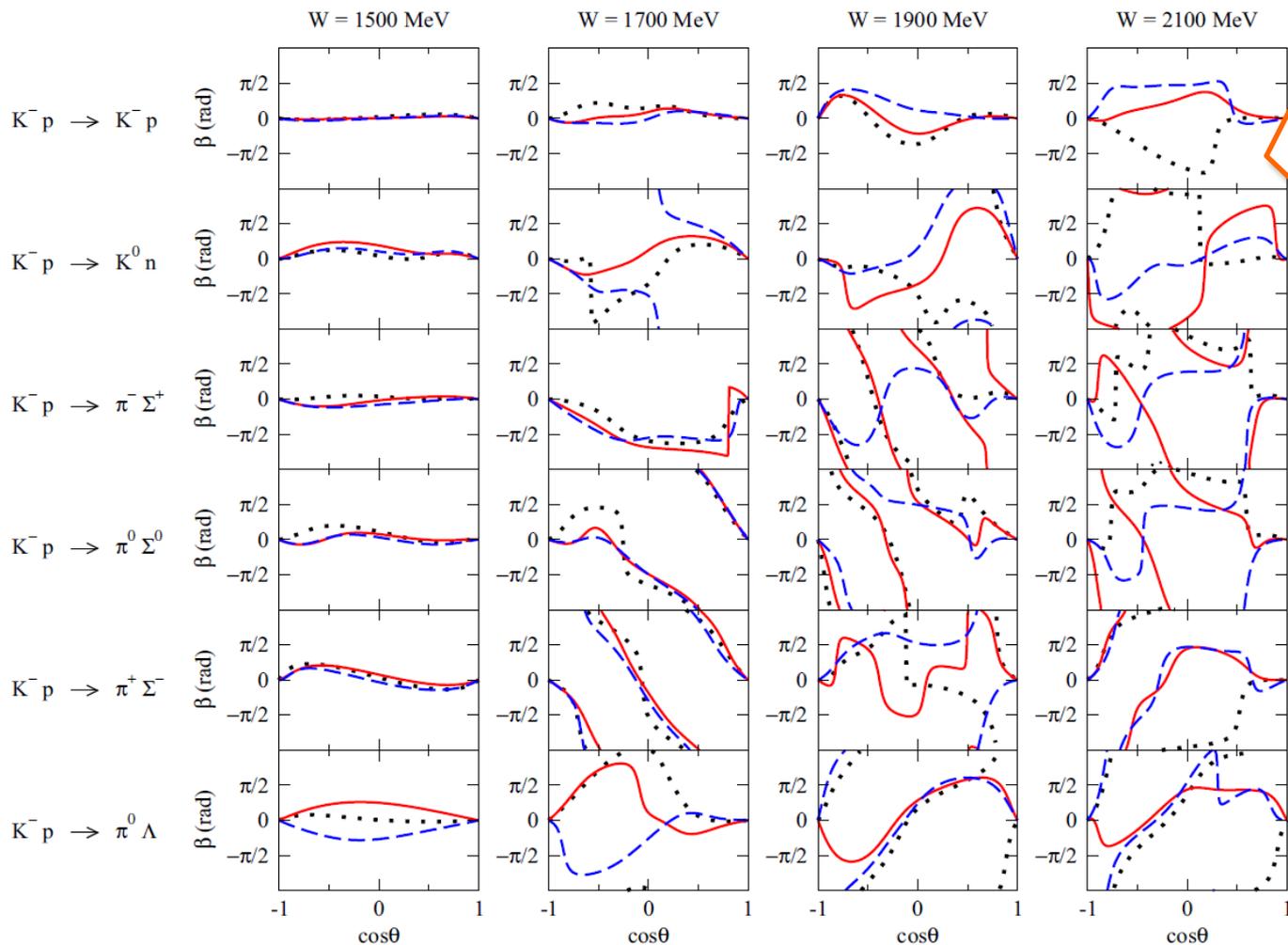


Red: Model A Blue: Model B

Predicted spin-rotation angle β

HK, Nakamura, Lee, Sato, PRC90(2014)065204

Currently no data for spin-rotation angle β



Analysis dependence is clearly seen !!



Measurement of β will give strong constraints on Y^* spectrum !!

Red: Model A

Blue: Model B

Black: KSU

The KSU results are computed by us using their amplitudes in PRC88(2013)035204.

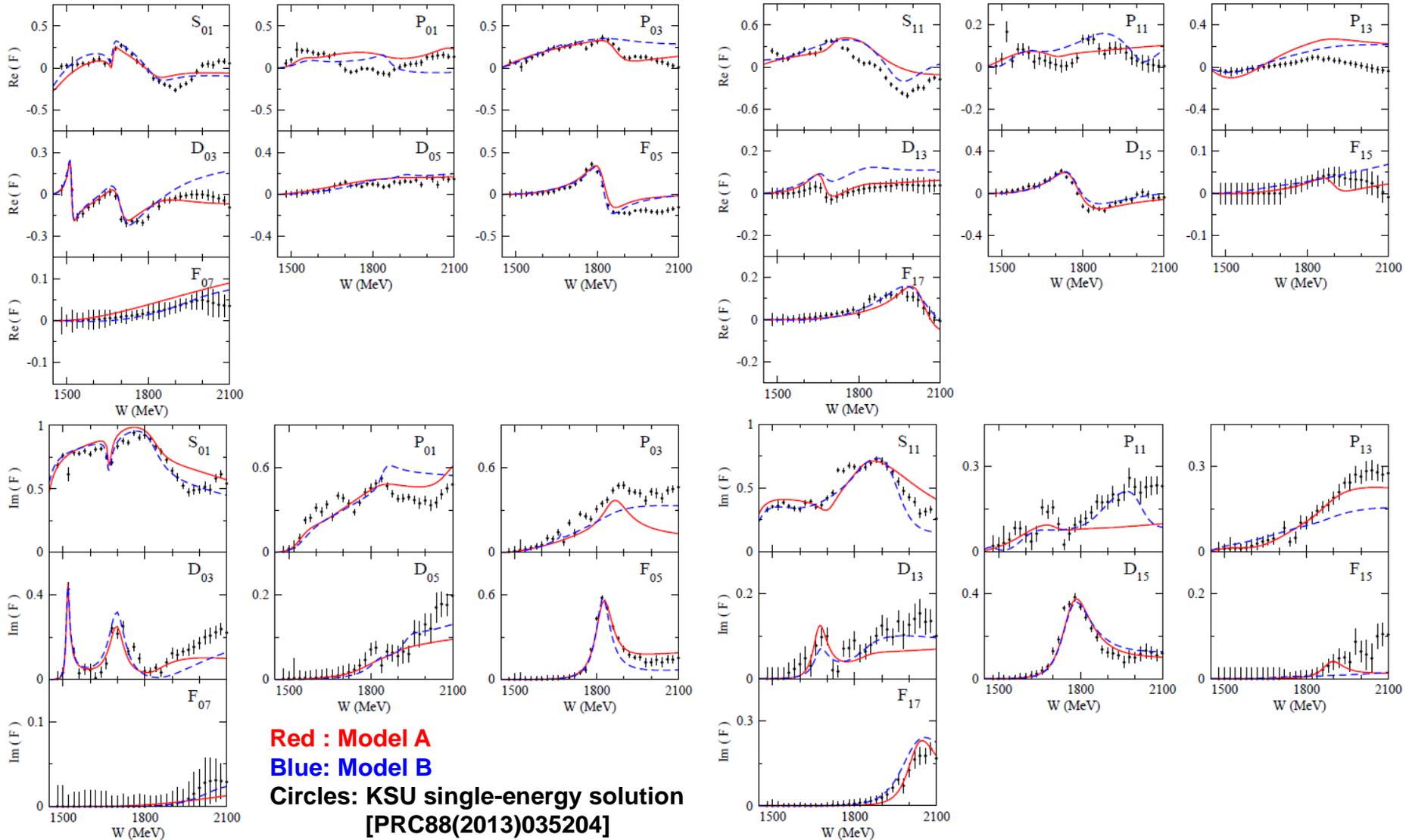
NOTE:
 β is modulo 2π

Comparison of extracted partial-wave amplitudes

Extracted $\bar{K}N$ scattering amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

L_{I2J} : $L = S, P, \dots$; $I =$ isospin; $J =$ Total angular mom.

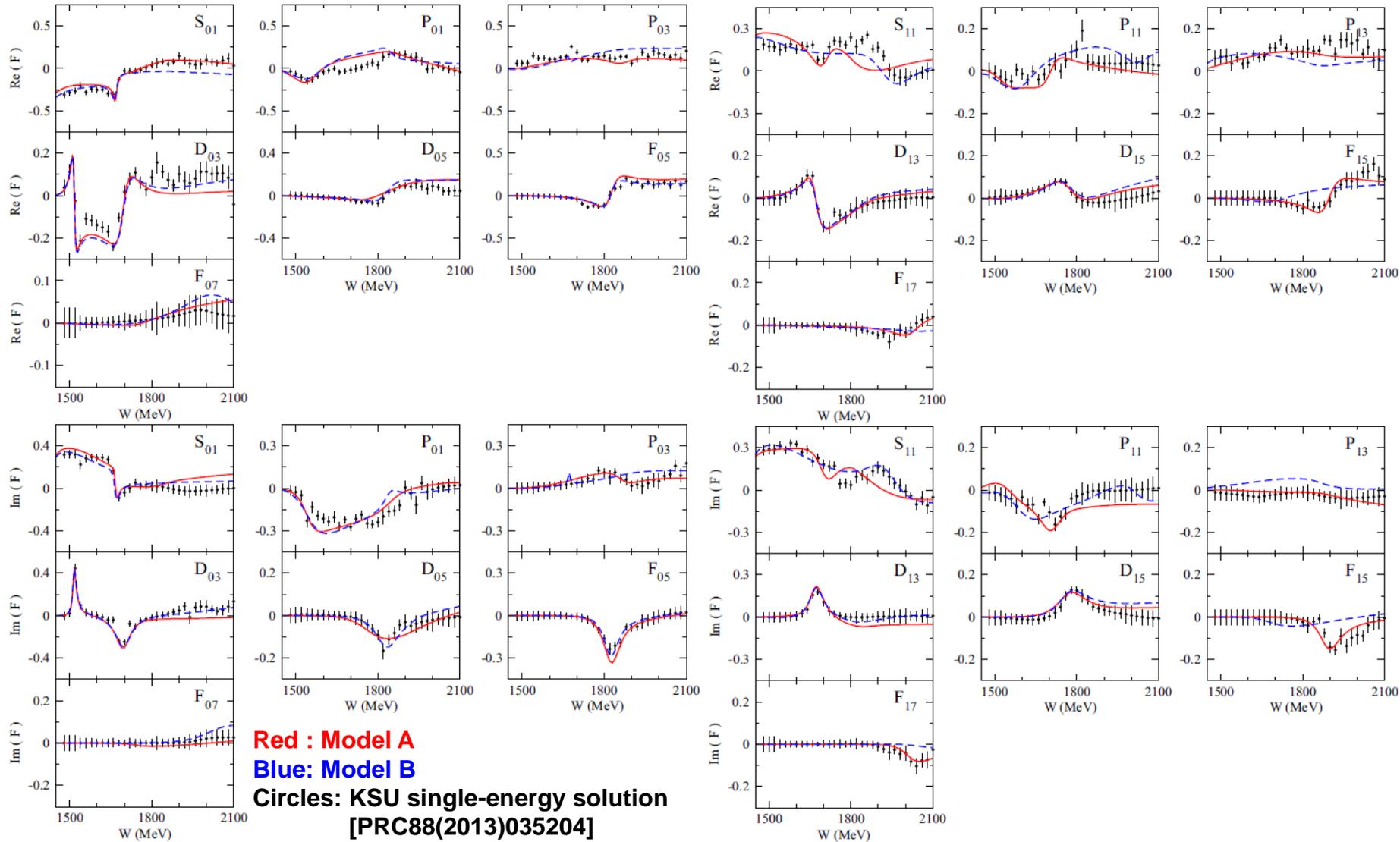


Comparison of extracted partial-wave amplitudes

Extracted $\bar{K}N \rightarrow \pi\Sigma$ amplitudes

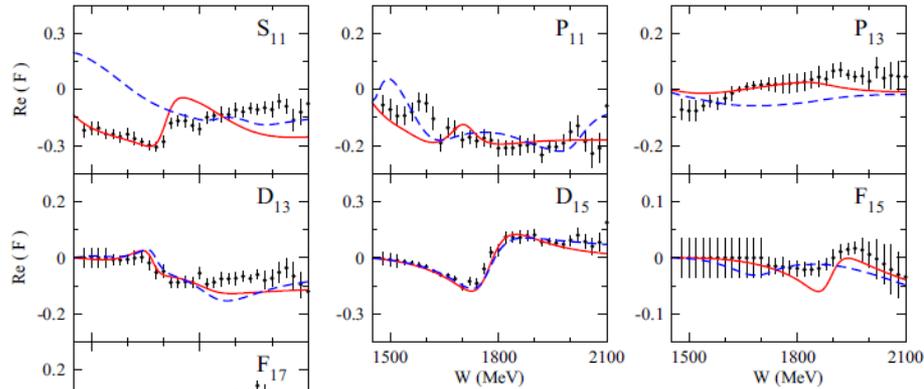
HK, Nakamura, Lee, Sato, PRC90(2014)065204

L_{12J} : $L = S, P, \dots$; $I =$ isospin; $J =$ Total angular mom.

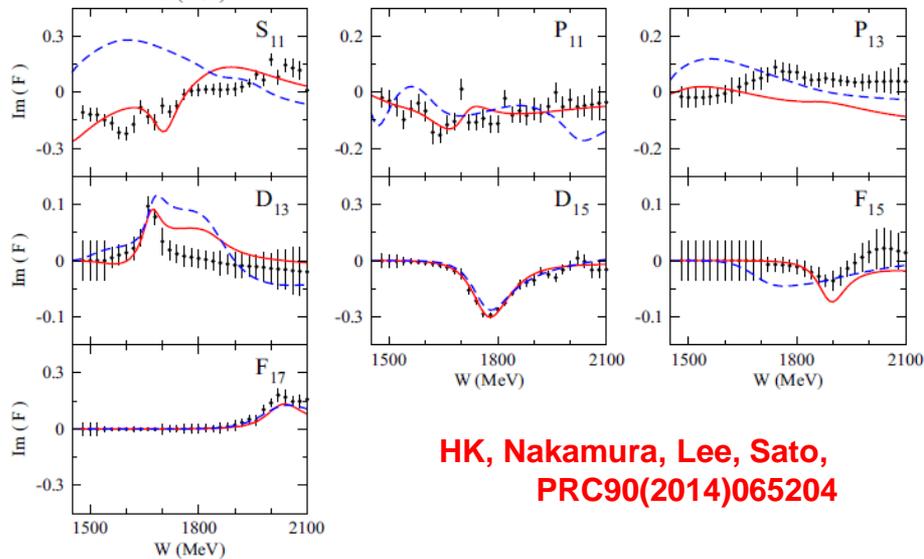


Comparison of extracted partial-wave amplitudes

Extracted $\bar{K}N \rightarrow \pi\Lambda$ amplitudes

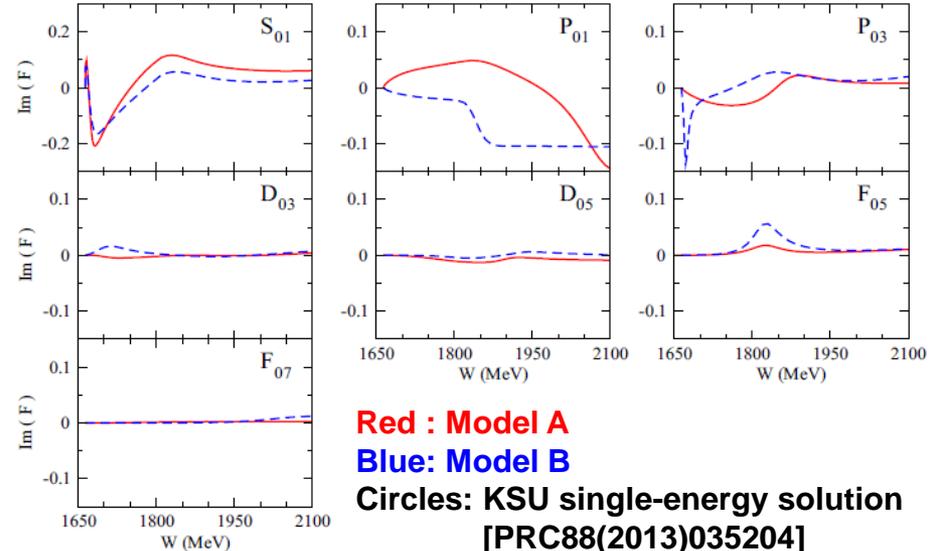
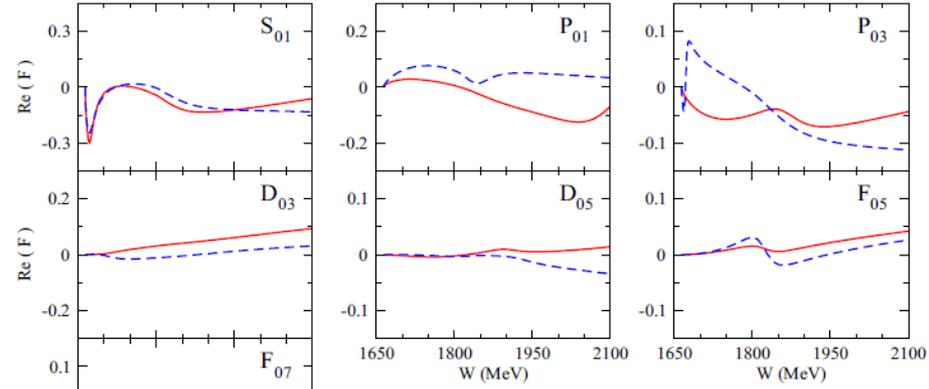


L_{I2J} : $L = S, P, \dots$; $I =$ isospin ;
 $J =$ Total angular mom.



HK, Nakamura, Lee, Sato,
 PRC90(2014)065204

Extracted $\bar{K}N \rightarrow \eta\Lambda$ amplitudes



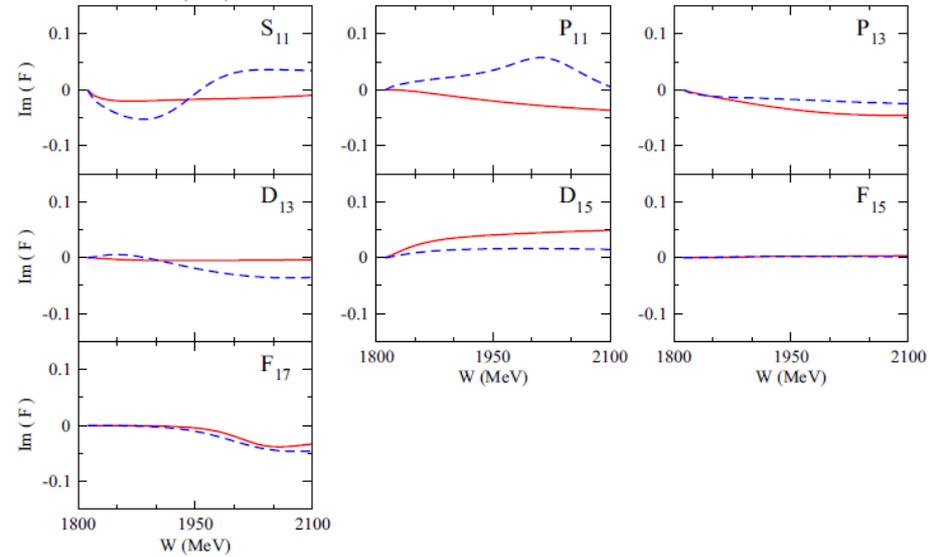
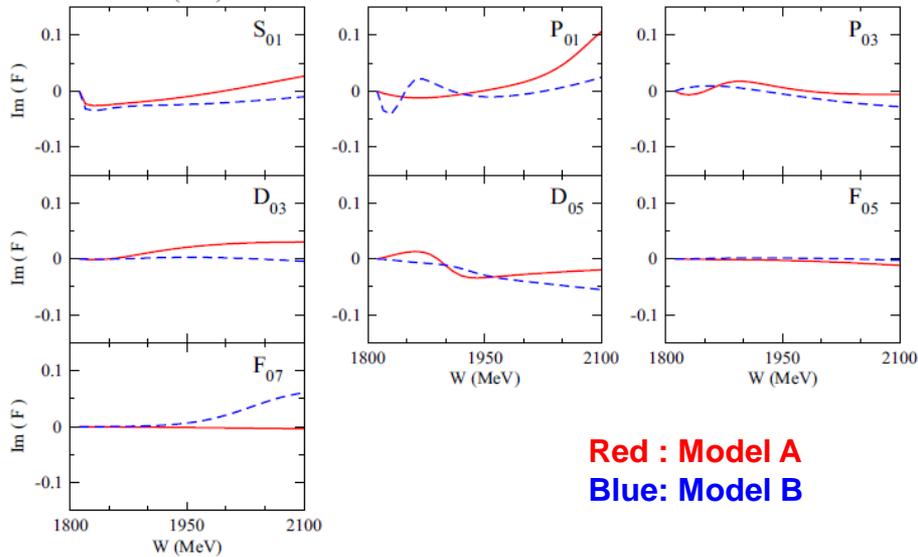
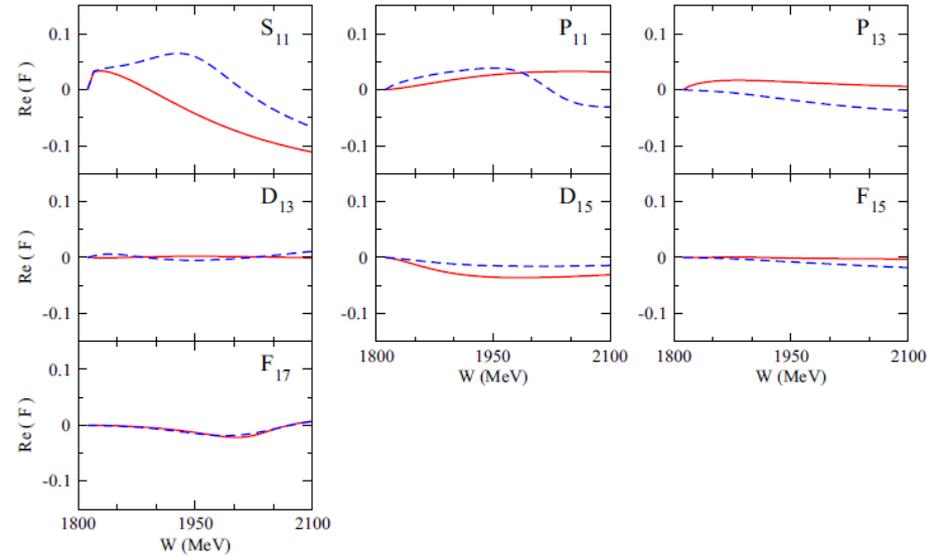
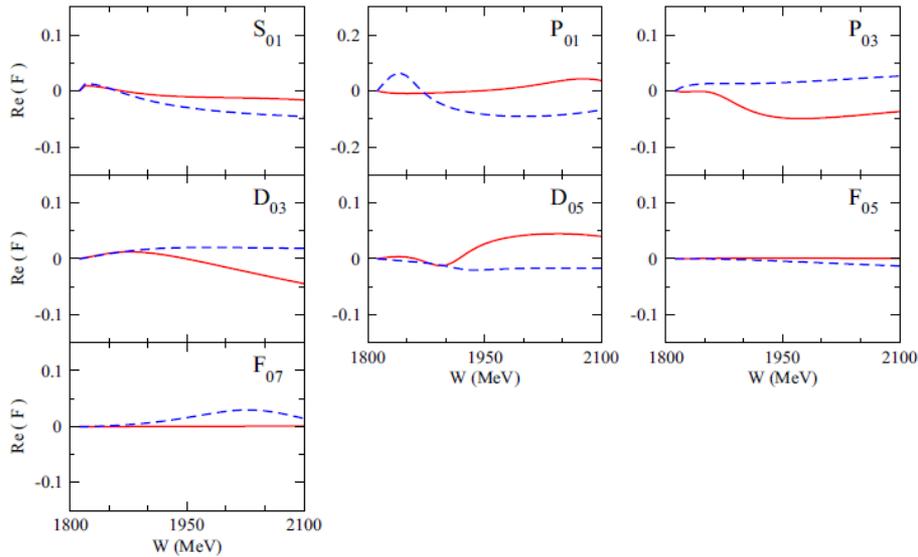
Red : Model A
 Blue: Model B
 Circles: KSU single-energy solution
 [PRC88(2013)035204]

Comparison of extracted partial-wave amplitudes

Extracted $\bar{K}N \rightarrow K\bar{E}$ amplitudes

HK, Nakamura, Lee, Sato, PRC90(2014)065204

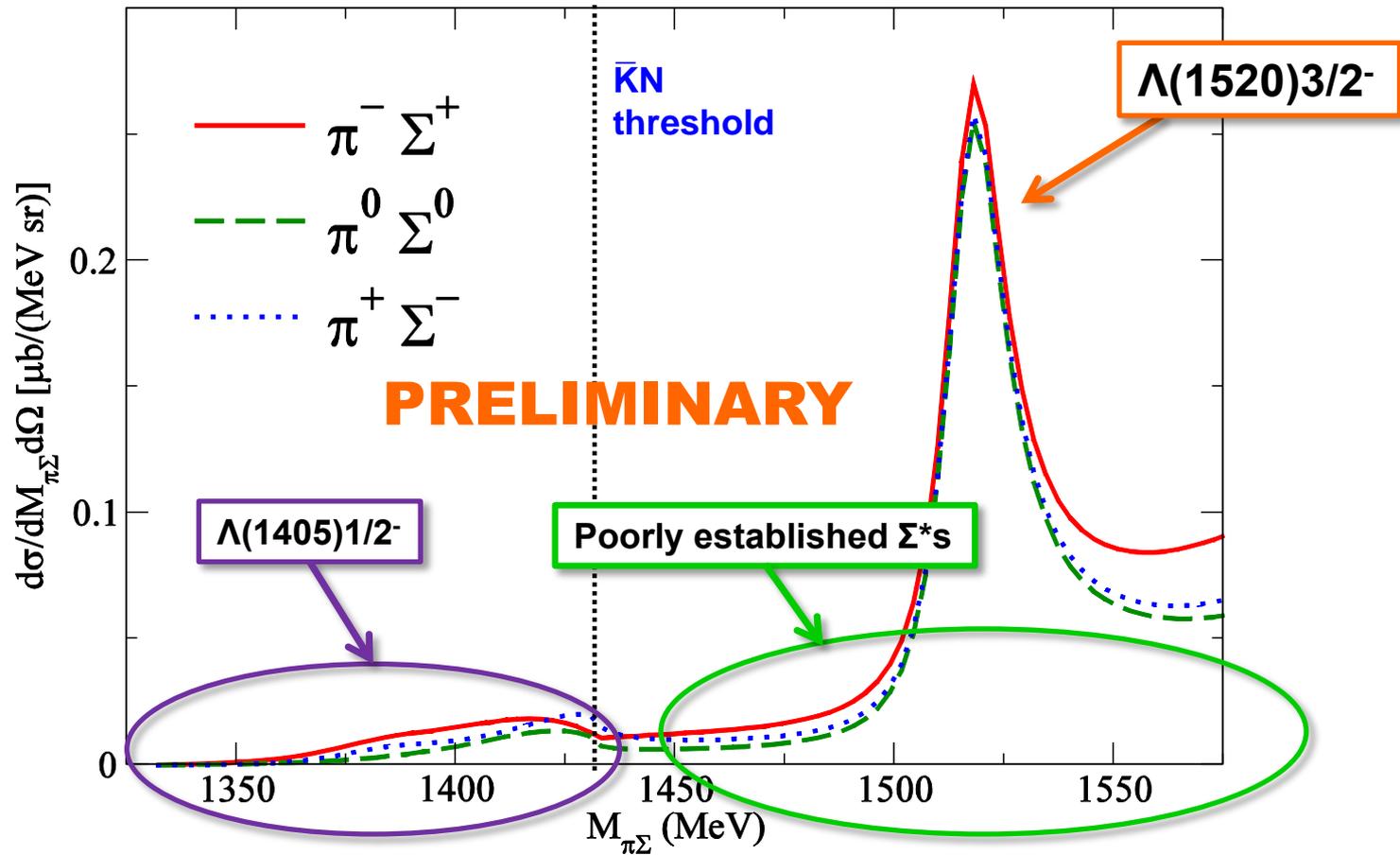
L_{I2J} : $L = S, P, \dots$; $I =$ isospin; $J =$ Total angular mom.



Red : Model A
Blue: Model B

Results (IMPULSE TERM ONLY !!)

$d\sigma/dM_{\pi\Sigma}d\Omega_n$ for $K^- d \rightarrow (\pi \Sigma)_0 n$
($P_{K^-} = 600$ MeV, $\theta_n = 0$ deg.)



Results (IMPULSE TERM ONLY !!)

$$d\sigma/dM_{\pi\Sigma}d\Omega_n \text{ for } K^- d \rightarrow (\pi \Sigma)_0 n$$

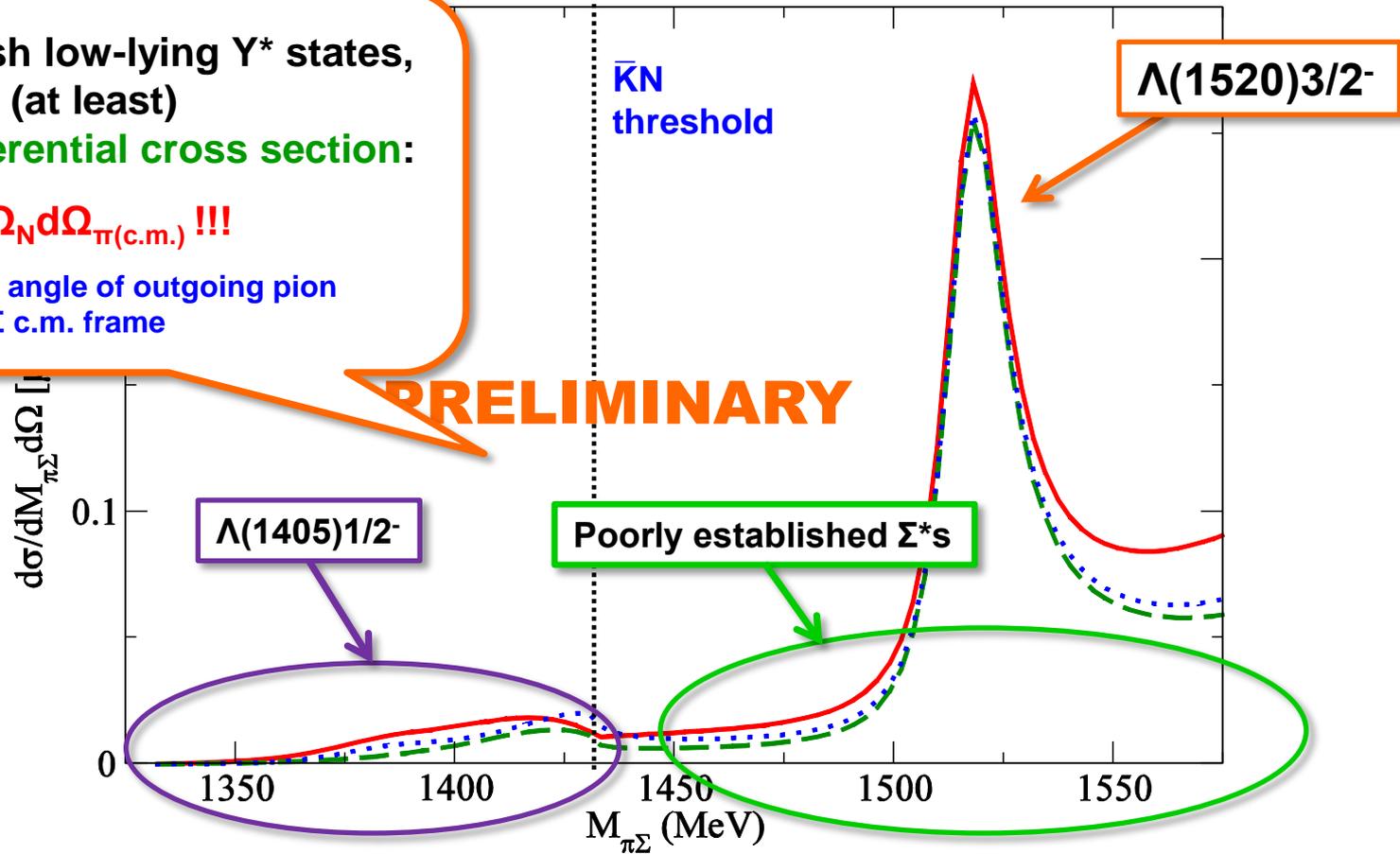
$$(P_{K^-} = 600 \text{ MeV}, \theta_n = 0 \text{ deg.})$$

To establish low-lying Y^* states, one needs (at least)

5-fold differential cross section:

$$d\sigma/dM_{\pi\Sigma}d\Omega_Nd\Omega_{\pi(c.m.)} !!!$$

$\Omega_{\pi(c.m.)}$ = solid angle of outgoing pion in $\pi\Sigma$ c.m. frame



Results (IMPULSE TERM ONLY !!)

$d\sigma/dM_{\pi\Sigma}d\Omega_N$ for $K^- d \rightarrow \pi^- \Sigma^+ n$
($P_{K^-} = 600$ MeV, $\theta_n = 0$ deg.)

