



JOHANNES GUTENBERG
UNIVERSITÄT MAINZ

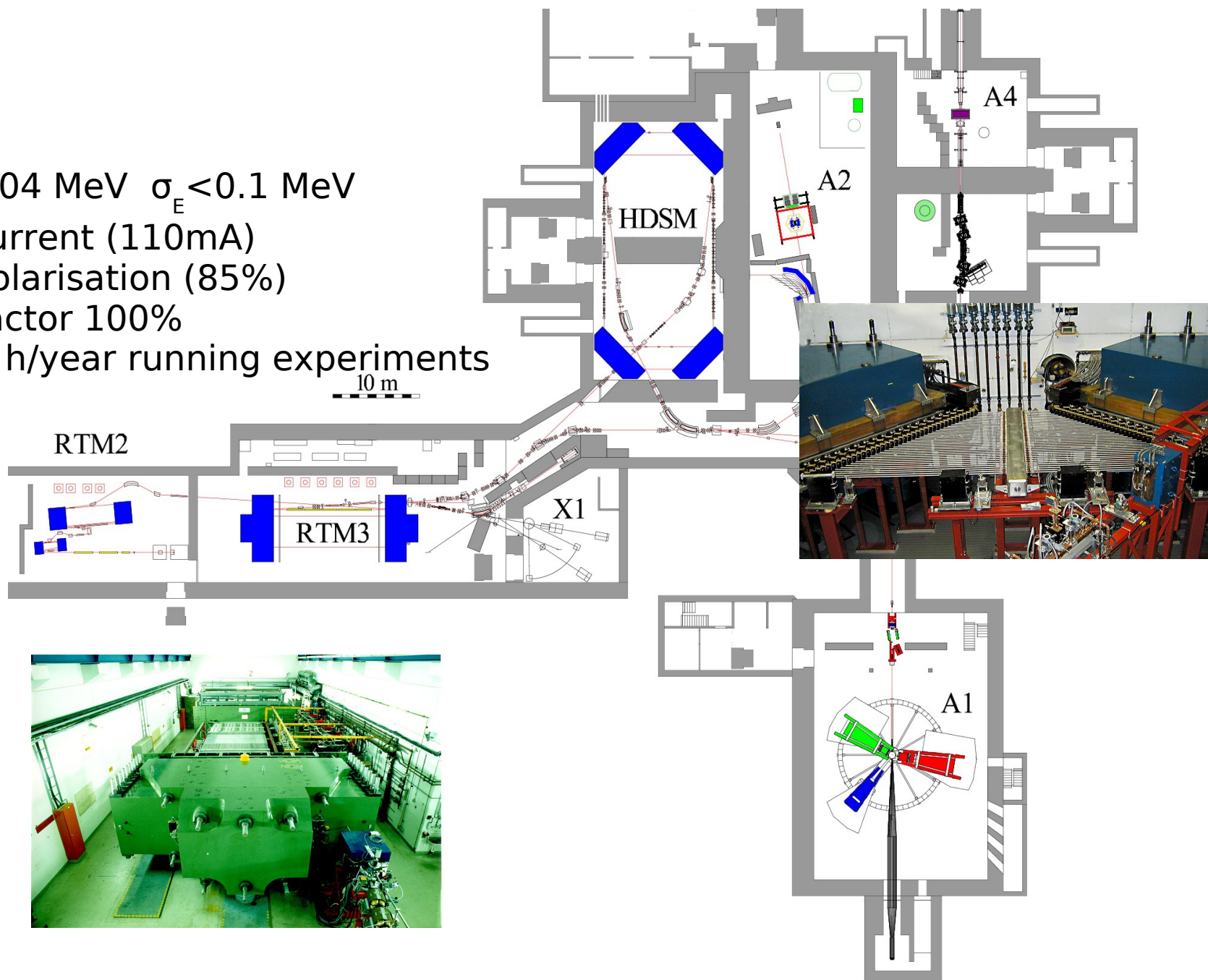
Meson Decays with Crystal Ball at MAMI

Christoph Florian Redmer
Institute for Nuclear Physics
University Mainz
5th August 2012

Institute for Nuclear Physics in Mainz



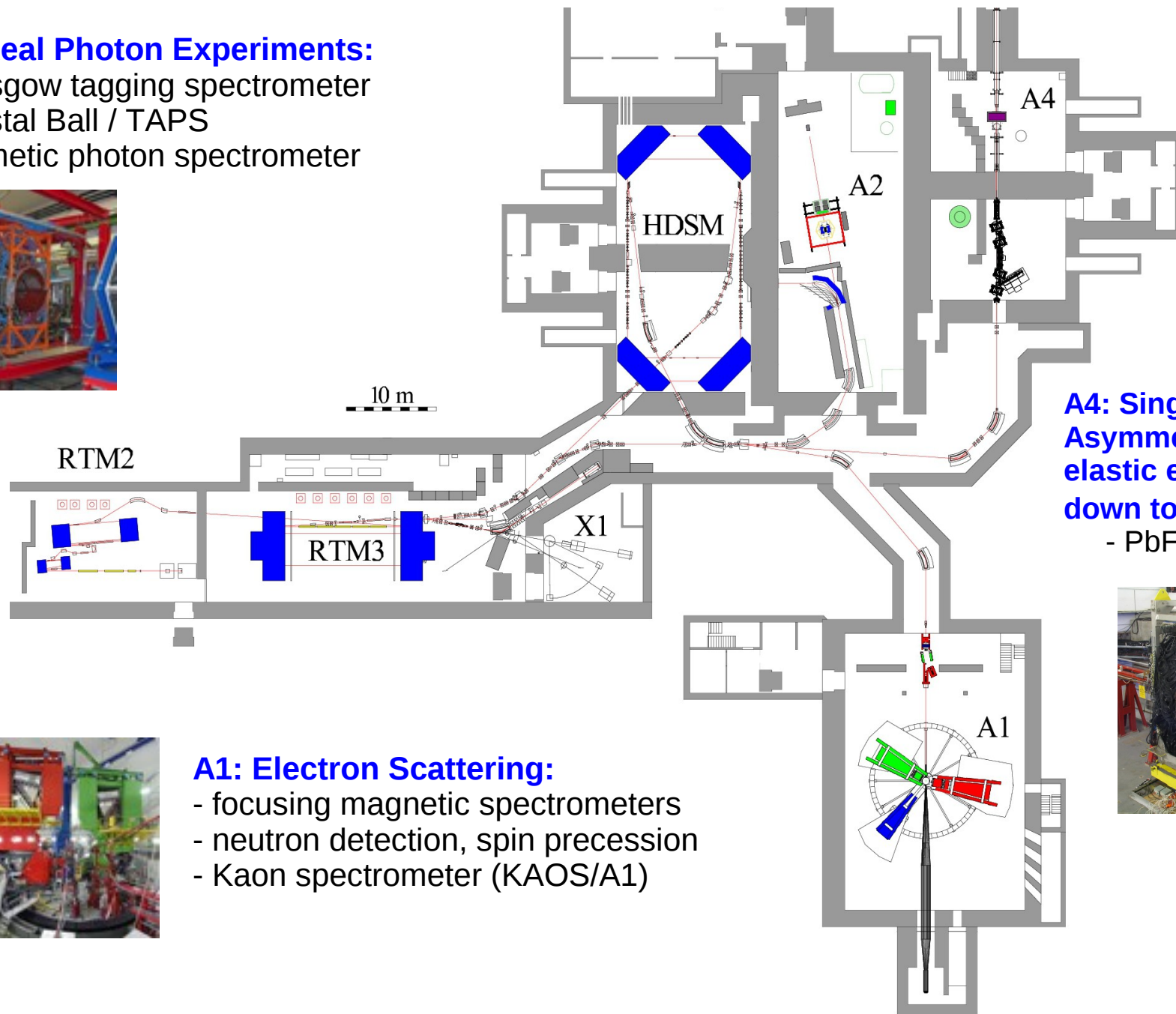
- $E_e < 1604 \text{ MeV}$ $\sigma_E < 0.1 \text{ MeV}$
- High current (110mA)
- High polarisation (85%)
- Duty factor 100%
- ~7000 h/year running experiments



Experiments at MAMI

A2: Real Photon Experiments:

- Glasgow tagging spectrometer
- Crystal Ball / TAPS hermetic photon spectrometer



- ## A4: Single Spin Asymmetries in elastic eN Scattering down to 10^{-6}
- PbF_2 calorimeter



A1: Electron Scattering:

- focusing magnetic spectrometers
- neutron detection, spin precession
- Kaon spectrometer (KAOS/A1)



Crystal Ball at MAMI

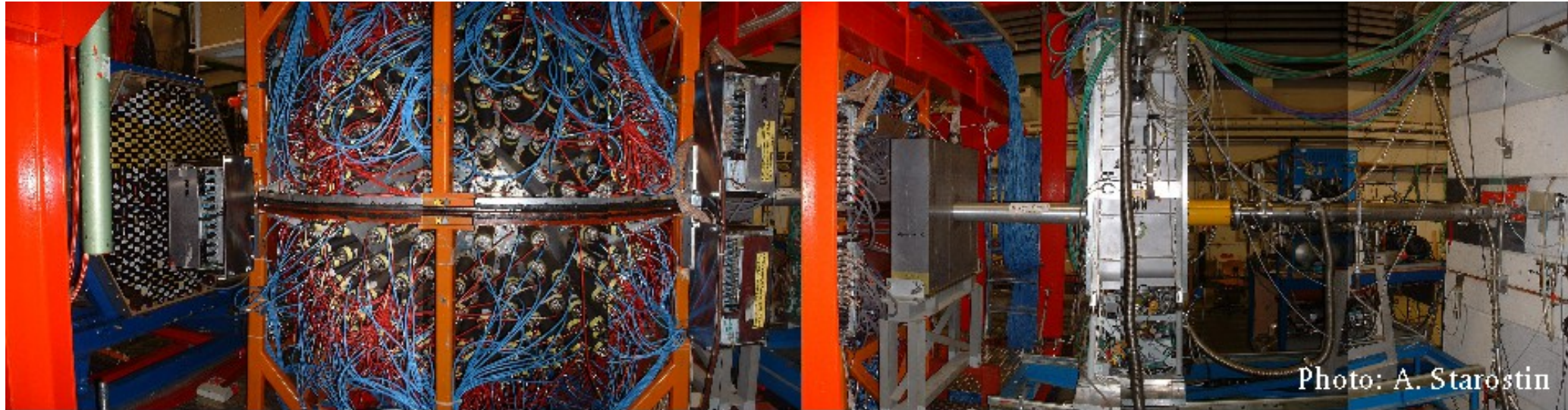
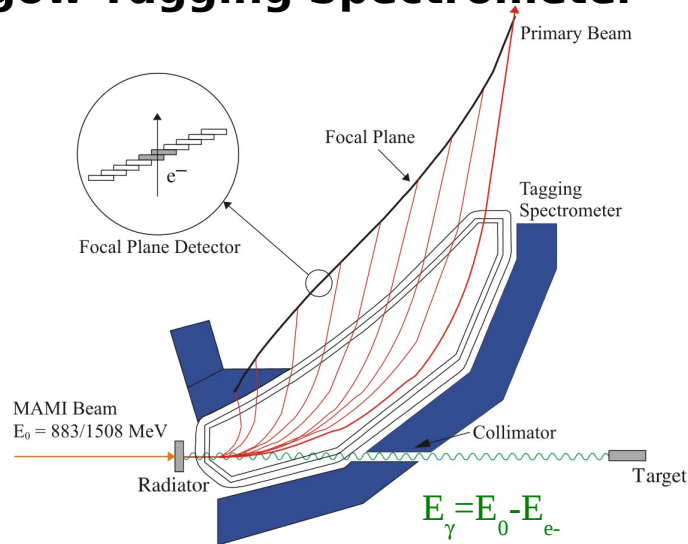


Photo: A. Starostin

Glasgow Tagging Spectrometer

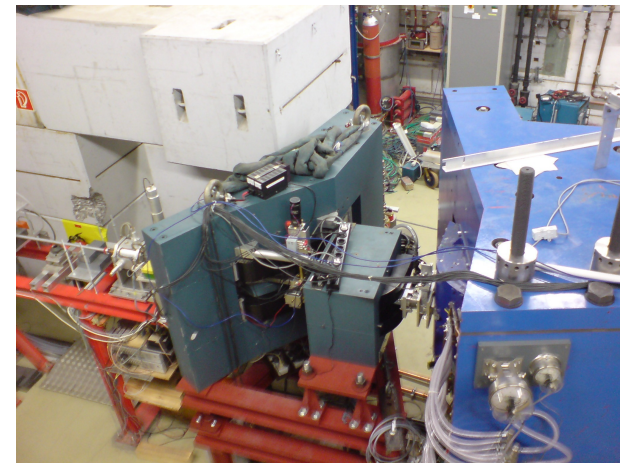


High energy resolution: $\Delta E_\gamma \approx 2 \text{ MeV}$ at $E_{e^-} = 883 \text{ MeV}$

$\Delta E_\gamma \approx 4 \text{ MeV}$ at $E_{e^-} = 1558 \text{ MeV}$

Tagging range: 4.7 to 93% of $E_\gamma \rightarrow E_{\text{max}} = 1491 \text{ MeV}$

End-Point Tagger



- Covers $\sim 1440 < E_\gamma [\text{MeV}] < \sim 1590 \text{ MeV}$
- Essential for tagged η' production
- Successfully commissioned in March 2010

Crystal Ball at MAMI

TA2PhotoPhysics

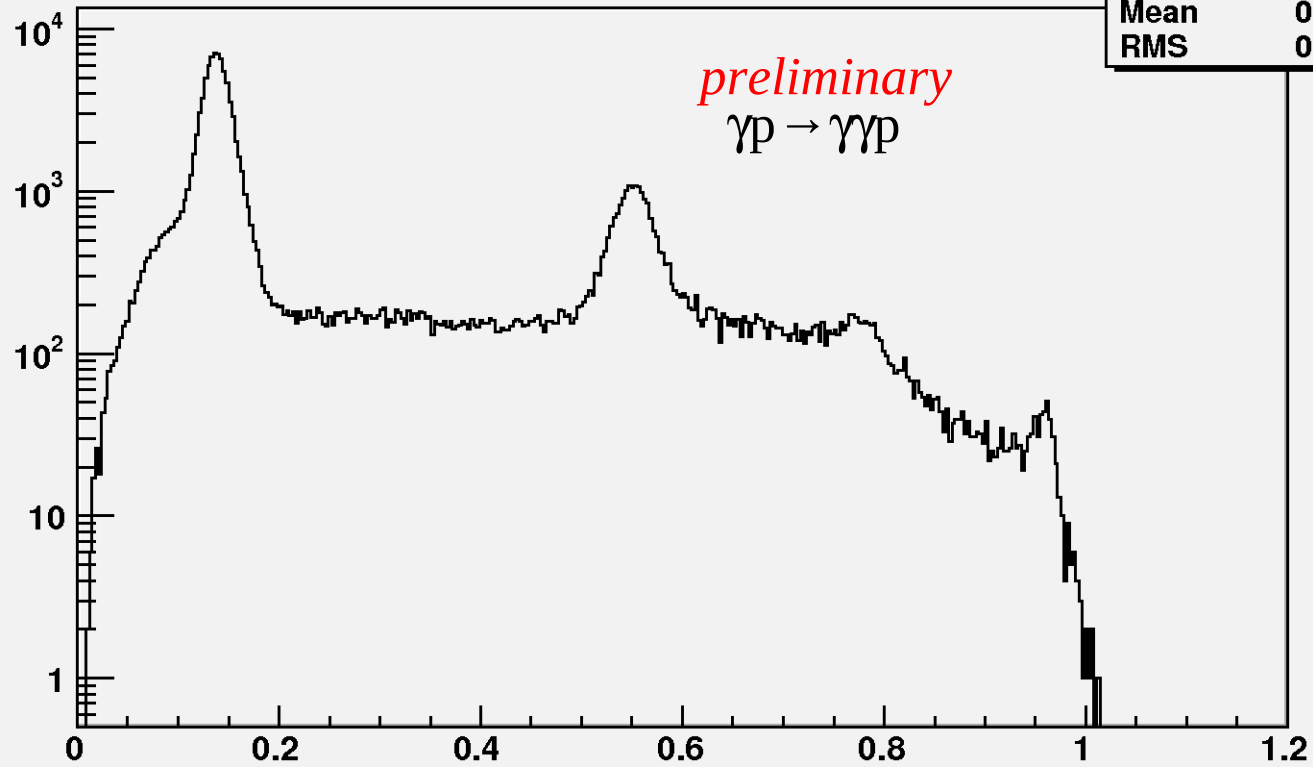
from 27th May 2012

SP_M2gfit.KF2gpm

Entries 135850

Mean 0.2734

RMS 0.2144



Glasgow

: A. Starostin

$$E_{\gamma} = E_0 - E_{e^-}$$

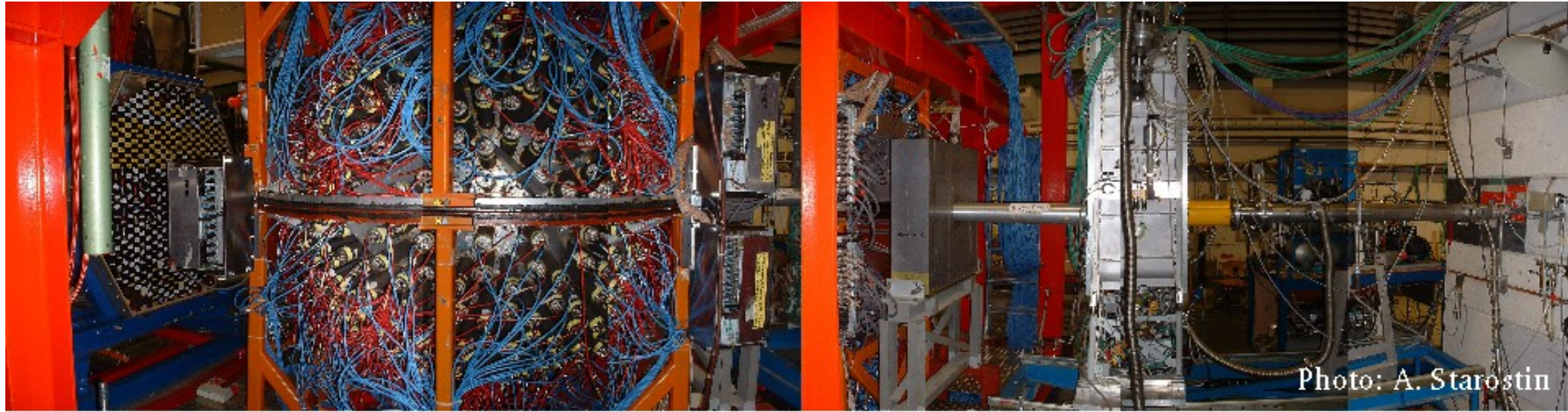
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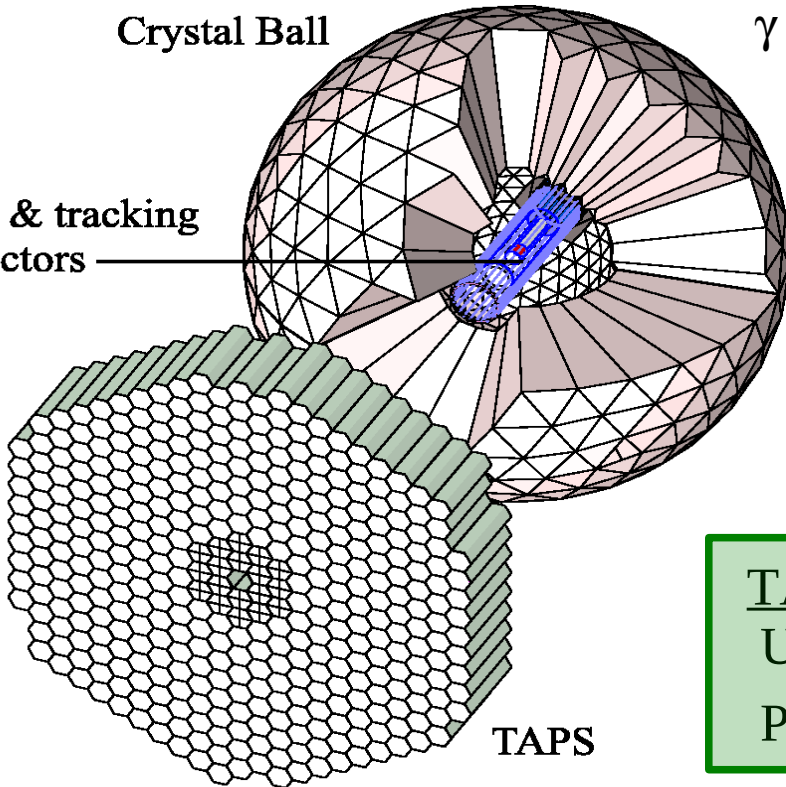
Crystal Ball at MAMI



Crystal Ball

γ

PID & tracking detectors



TAPS

Crystal Ball:

672 NaI(Tl) crystals
93,3% of total solid angle
Each crystal equipped with PMT

$$\frac{\sigma}{E_\gamma} = \frac{2\%}{(E_\gamma/\text{GeV})^{0.25}} \quad \sigma(\theta) = 2^\circ \dots 3^\circ$$

$$\Delta t = 2.5 \text{ ns FWHM} \quad \sigma(\phi) = \frac{2^\circ \dots 3^\circ}{\sin(\theta)}$$

TAPS:

Up to 510 BaF₂ crystals
Polar acceptance: 4-20°

$$\Delta t = 0.5 \text{ ns FWHM}$$

$$\frac{\sigma}{E_\gamma} = \frac{0,79\%}{\sqrt{E_\gamma/\text{GeV}}} + 1,8\%$$

Crystal Ball at MAMI

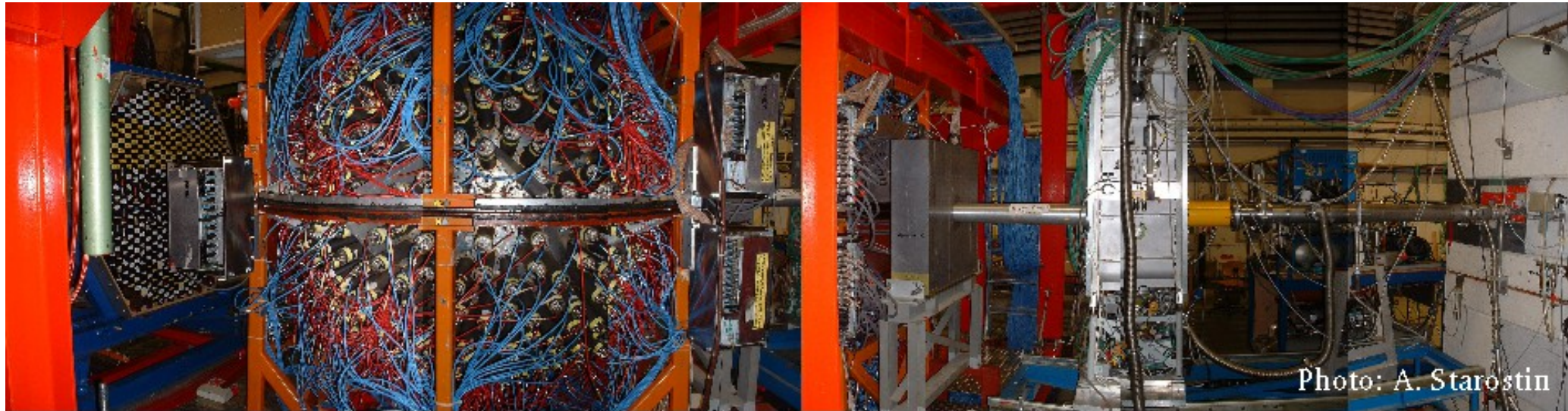
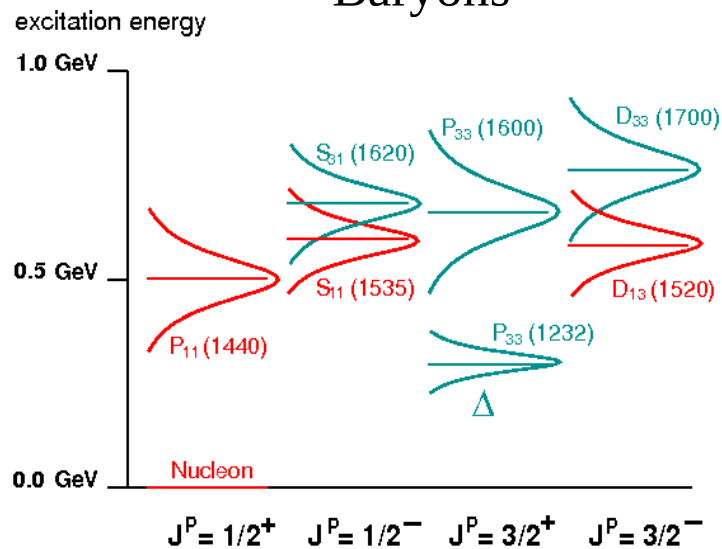
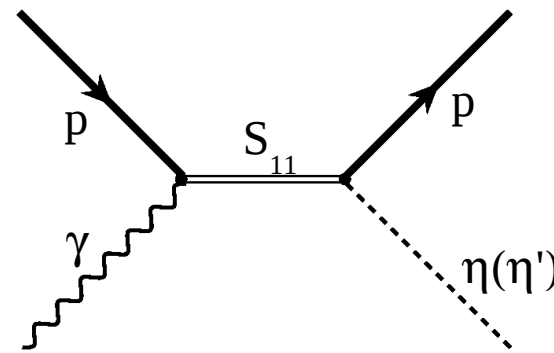


Photo: A. Starostin

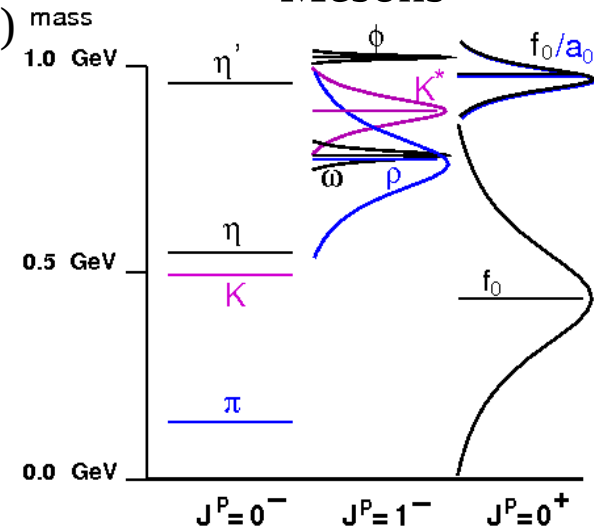
Baryons



Photoproduction ($E_\gamma \leq 1604$ MeV)



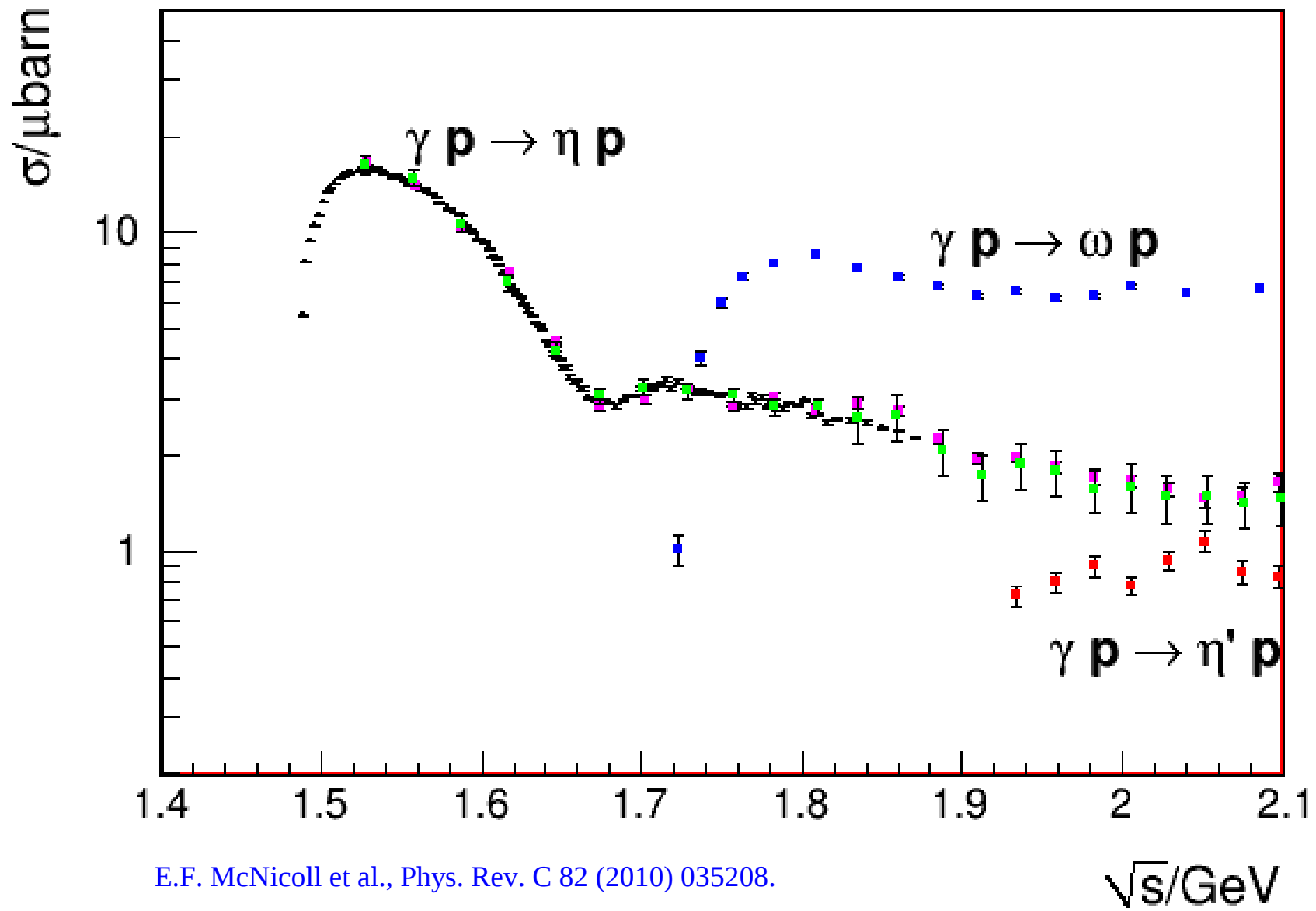
Mesons



- *Meson decays and meson properties*
- *Polarisabilities of nucleons and pions*
- *Properties of the first nucleon excitations*

Experimental Results

Photoproduction Cross Sections



E.F. McNicoll et al., Phys. Rev. C 82 (2010) 035208.

Data from Crystal Ball, Crystal Barrel, SAPHIR, CLAS

$\eta \rightarrow \pi^0 \pi^0 \pi^0$

- Isospin violating process

- electromagnetic contributions small
- sensitive to quark mass difference

(Sutherland's Theorem)

$$\Gamma_{\text{exp}} = \left(\frac{Q_D}{Q} \right)^4 \cdot \bar{\Gamma}$$

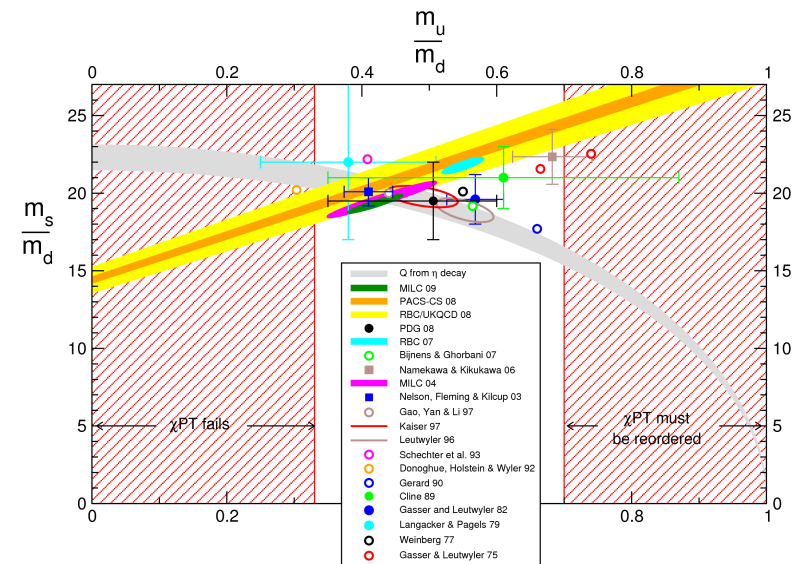
$$Q^2 = \frac{m_d^2 - m_u^2}{m_s^2 - (m_d + m_u)^2 / 4}$$

$$(Q_D)^2 = \frac{(m_K^2 + \frac{1}{2}(m_{\pi^0}^2 - m_{\pi^+}^2))(m_K^2 - m_{\pi^0}^2)}{m_{\pi^0}^2(m_{K^0}^2 - m_{K^+}^2)} = (24.2)^2$$

$\bar{\Gamma}$: Γ calculated at Dashen limit

- Good understanding of decay in ChPT is crucial

- Study Dalitz plot to test ChPT (implementation of $\pi\pi$ scattering)



H. Leutwyler, arXiv:0911.1416, CD2009

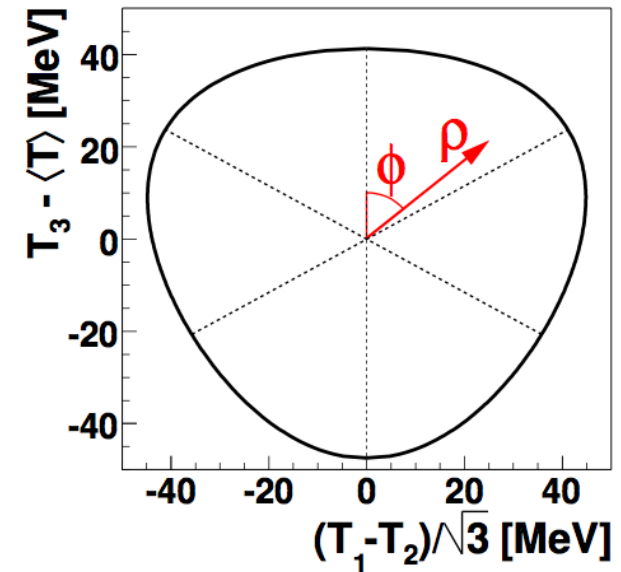
Dalitz-Plot Analysis

- Parametrize Dalitz plot density:

- $\Gamma \propto |A(X,Y)|^2 = N \cdot (1 + aY + bY^2 + dX^2 + fY^3 + \dots)$

$$X = \frac{\sqrt{3}(T_1 - T_2)}{T_1 + T_2 + T_3}$$

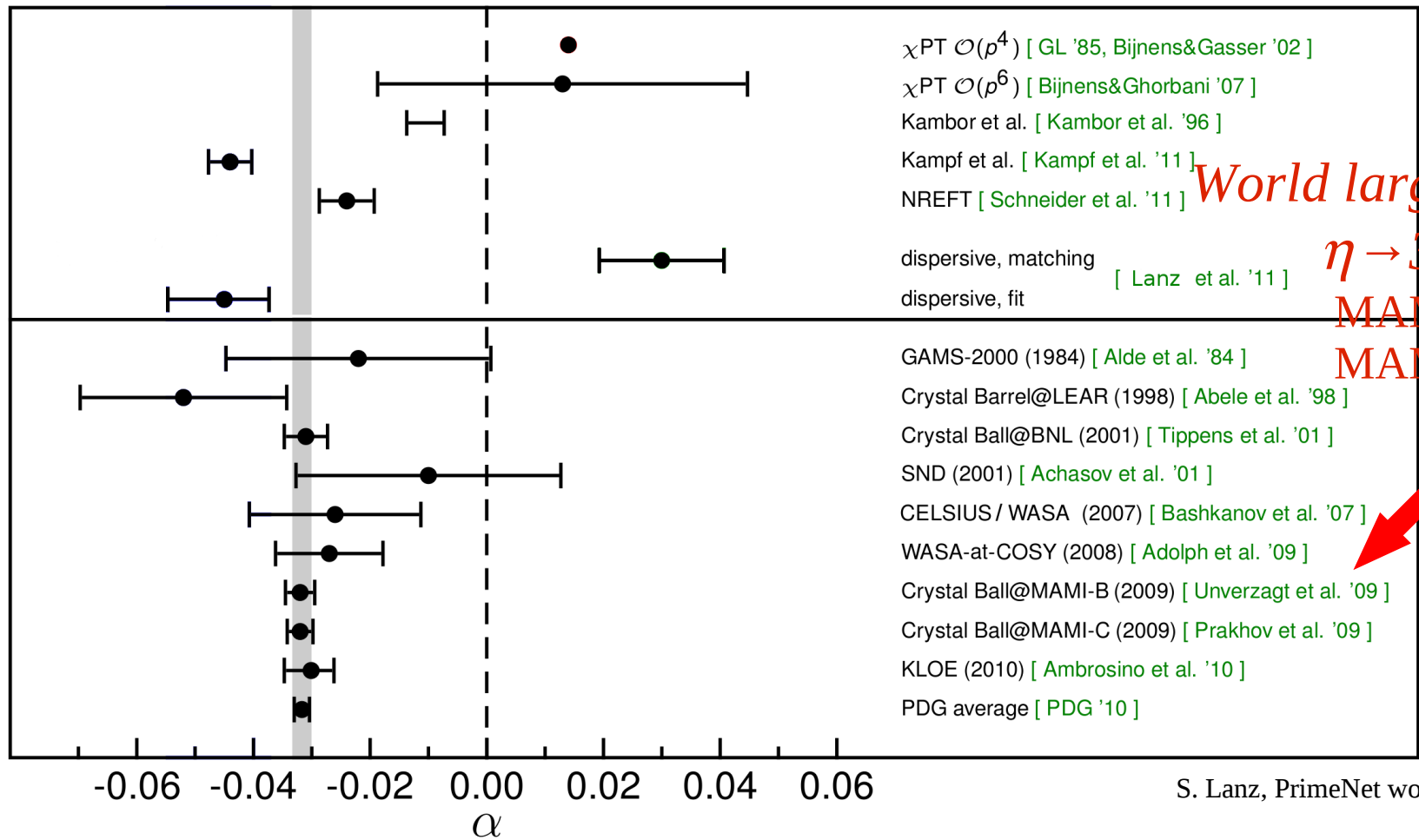
$$Y = \frac{3T_3}{T_1 + T_2 + T_3} - 1$$



- Polar coordinates more convenient for 3 identical particles

- $\Gamma \propto |A(Z, \phi)|^2 = N \cdot (1 + 2\alpha Z + \dots)$

Results for α

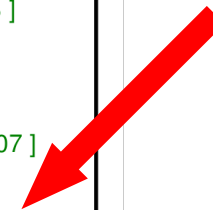


World largest statistics on

$\eta \rightarrow 3\pi^0$ decays!

MAMI-B: 1.8 M

MAMI-C: 3.0 M



S. Lanz, PrimeNet workshop 2011

- Well established experimental database
 - Enough precision to look for higher order effects, e.g. cusp

C/CP-Violating Meson Decays

Citation: K. Nakamura *et al.* (Particle Data Group), JP G **37**, 075021 (2010) and 2011 partial update for the 2012 edition (URL: <http://pdg.lbl.gov>)

TESTS OF DISCRETE SPACE-TIME SYMMETRIES

CHARGE CONJUGATION (C) INVARIANCE

$\Gamma(\pi^0 \rightarrow 3\gamma)/\Gamma_{\text{total}}$	$<3.1 \times 10^{-8}$, CL = 90%
η C-nonconserving decay parameters	
$\pi^+\pi^-\pi^0$ left-right asymmetry	$(0.09^{+0.11}_{-0.12}) \times 10^{-2}$
$\pi^+\pi^-\pi^0$ sextant asymmetry	$(0.12^{+0.10}_{-0.11}) \times 10^{-2}$
$\pi^+\pi^-\pi^0$ quadrant asymmetry	$(-0.09 \pm 0.09) \times 10^{-2}$
$\pi^+\pi^-\gamma$ left-right asymmetry	$(0.9 \pm 0.4) \times 10^{-2}$
$\pi^+\pi^-\gamma$ parameter β (D-wave)	-0.02 ± 0.07 (S = 1.3)
$\Gamma(\eta \rightarrow \pi^0\gamma)/\Gamma_{\text{total}}$	$<9 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow 2\pi^0\gamma)/\Gamma_{\text{total}}$	$<5 \times 10^{-4}$, CL = 90%
$\Gamma(\eta \rightarrow 3\pi^0\gamma)/\Gamma_{\text{total}}$	$<6 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow 3\gamma)/\Gamma_{\text{total}}$	$<1.6 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow \pi^0 e^+ e^-)/\Gamma_{\text{total}}$	[a] $<4 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow \pi^0 \mu^+ \mu^-)/\Gamma_{\text{total}}$	[a] $<5 \times 10^{-6}$, CL = 90%
$\Gamma(\omega(782) \rightarrow \eta\pi^0)/\Gamma_{\text{total}}$	$<2.1 \times 10^{-4}$, CL = 90%
$\Gamma(\omega(782) \rightarrow 2\pi^0)/\Gamma_{\text{total}}$	$<2.1 \times 10^{-4}$, CL = 90%
$\Gamma(\omega(782) \rightarrow 3\pi^0)/\Gamma_{\text{total}}$	$<2.3 \times 10^{-4}$, CL = 90%
asymmetry parameter for $\eta'(958) \rightarrow \pi^+\pi^-\gamma$ decay	-0.03 ± 0.04
$\Gamma(\eta'(958) \rightarrow \pi^0 e^+ e^-)/\Gamma_{\text{total}}$	[a] $<1.4 \times 10^{-3}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \eta e^+ e^-)/\Gamma_{\text{total}}$	[a] $<2.4 \times 10^{-3}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow 3\gamma)/\Gamma_{\text{total}}$	$<1.0 \times 10^{-4}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \mu^+ \mu^- \pi^0)/\Gamma_{\text{total}}$	[a] $<6.0 \times 10^{-5}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \mu^+ \mu^- \eta)/\Gamma_{\text{total}}$	[a] $<1.5 \times 10^{-5}$, CL = 90%
$\Gamma(J/\psi(1S) \rightarrow \gamma\gamma)/\Gamma_{\text{total}}$	$<5 \times 10^{-6}$, CL = 90%

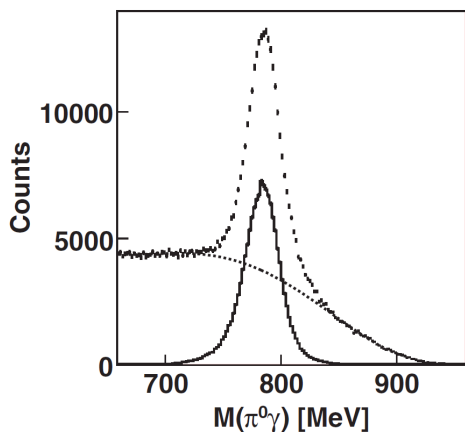
CP INVARIANCE

$\text{Re}(d_\tau^W)$	$<0.50 \times 10^{-17}$ e cm, CL = 95%
$\text{Im}(d_\tau^W)$	$<1.1 \times 10^{-17}$ e cm, CL = 95%
$\eta \rightarrow \pi^+\pi^- e^+ e^-$ decay-plane asymmetry	$(-0.6 \pm 3.1) \times 10^{-2}$
$\Gamma(\eta \rightarrow \pi^+\pi^-)/\Gamma_{\text{total}}$	$<1.3 \times 10^{-5}$, CL = 90%
$\Gamma(\eta \rightarrow 2\pi^0)/\Gamma_{\text{total}}$	$<3.5 \times 10^{-4}$, CL = 90%
$\Gamma(\eta \rightarrow 4\pi^0)/\Gamma_{\text{total}}$	$<6.9 \times 10^{-7}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \pi^+\pi^-)/\Gamma_{\text{total}}$	$<2.9 \times 10^{-3}$, CL = 90%
$\Gamma(\eta'(958) \rightarrow \pi^0\pi^0)/\Gamma_{\text{total}}$	$<1.0 \times 10^{-3}$, CL = 90%
$K^\pm \rightarrow \pi^\pm \pi^+ \pi^-$ rate difference/average	$(0.08 \pm 0.12)\%$
$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0$ rate difference/average	$(0.0 \pm 0.6)\%$
$K^\pm \rightarrow \pi^\pm \pi^0 \gamma$ rate difference/average	$(0.9 \pm 3.3)\%$
$K^\pm \rightarrow \pi^\pm \pi^+ \pi^- (g_+ - g_-) / (g_+ + g_-)$	$(-1.5 \pm 2.2) \times 10^{-4}$
$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0 (g_+ - g_-) / (g_+ + g_-)$	$(1.8 \pm 1.8) \times 10^{-4}$

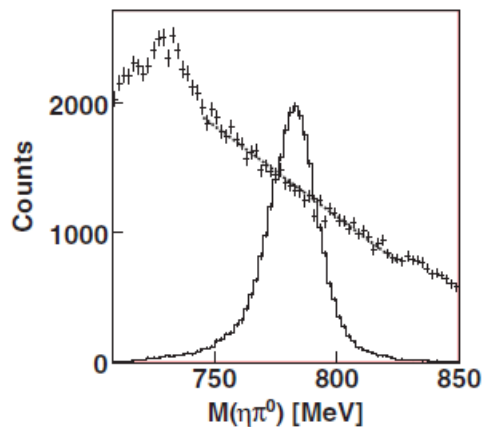
Only weak upper limits
Improve upper limits by factor >10

C-Violation in ω Decays

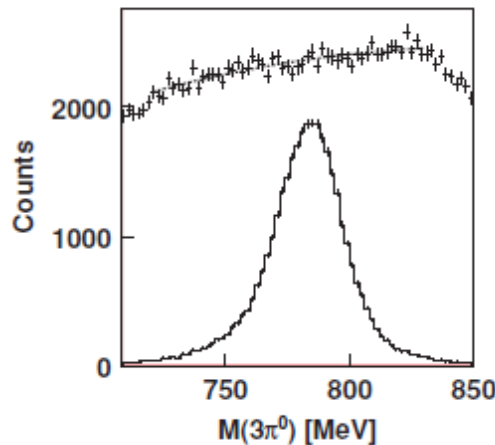
A. Starostin et al., Phys. Rev. C 79, 065201 (2009).



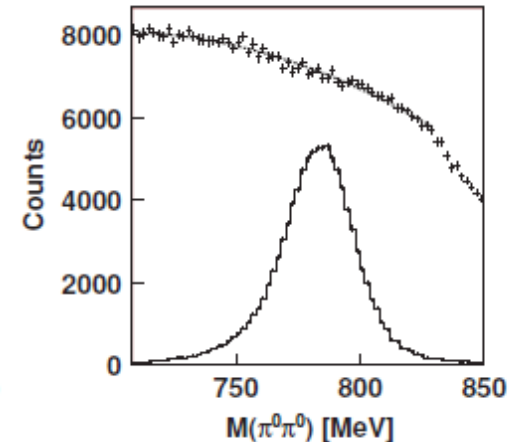
$1.5 \cdot 10^5$ events



<60 events



<219 events



<336 events

Different beam energy interval!



PDG 2010:

$$\Gamma(\omega(782) \rightarrow \eta \pi^0) / \Gamma_{\text{total}}$$

$$\Gamma(\omega(782) \rightarrow 2\pi^0) / \Gamma_{\text{total}}$$

$$\Gamma(\omega(782) \rightarrow 3\pi^0) / \Gamma_{\text{total}}$$

$$<2.1 \times 10^{-4}, \text{ CL} = 90\%$$

$$<2.1 \times 10^{-4}, \text{ CL} = 90\% \quad \text{never done before}$$

$$<2.3 \times 10^{-4}, \text{ CL} = 90\%$$

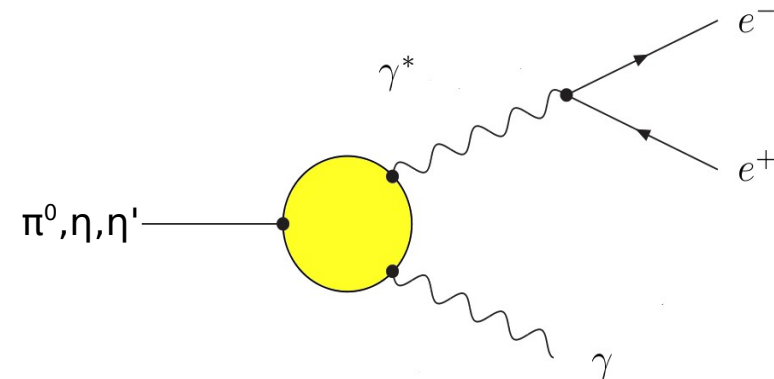
CB at MAMI results are dominating!

Transition Form Factors

- Dalitz decays of light mesons allow to determine the transition form factor in the time-like region
 - study el.-mag. structure of the decaying neutral meson

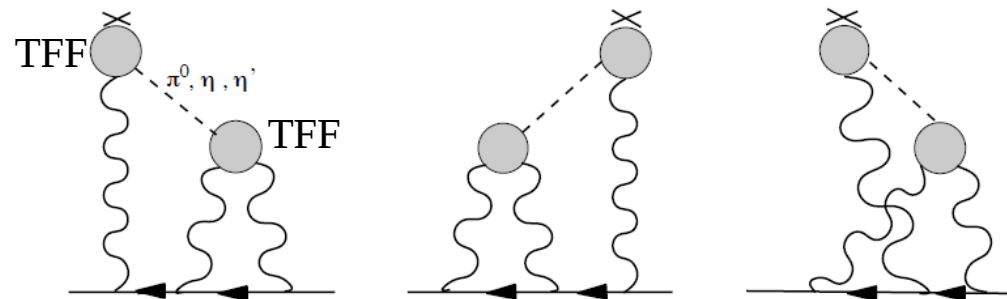
$$\frac{d\Gamma_{e^+e^-\gamma}}{dq^2} = \left[\frac{d\Gamma_{e^+e^-\gamma}}{dq^2} \right]_{QED} \cdot |F(q^2)|^2$$

$$F(q^2) \approx 1 + \frac{q^2}{\Lambda^2} = 1 + bq^2$$



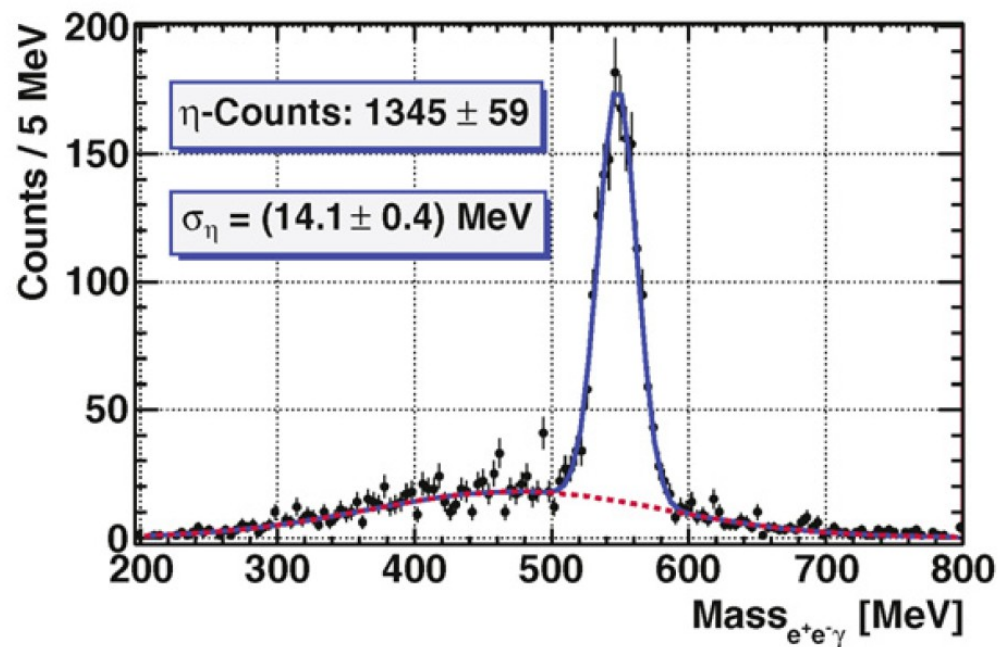
- Important input to calculations of the hadronic light-by-light scattering

- Important contribution to $(g-2)_\mu$
 - One of the largest uncertainties



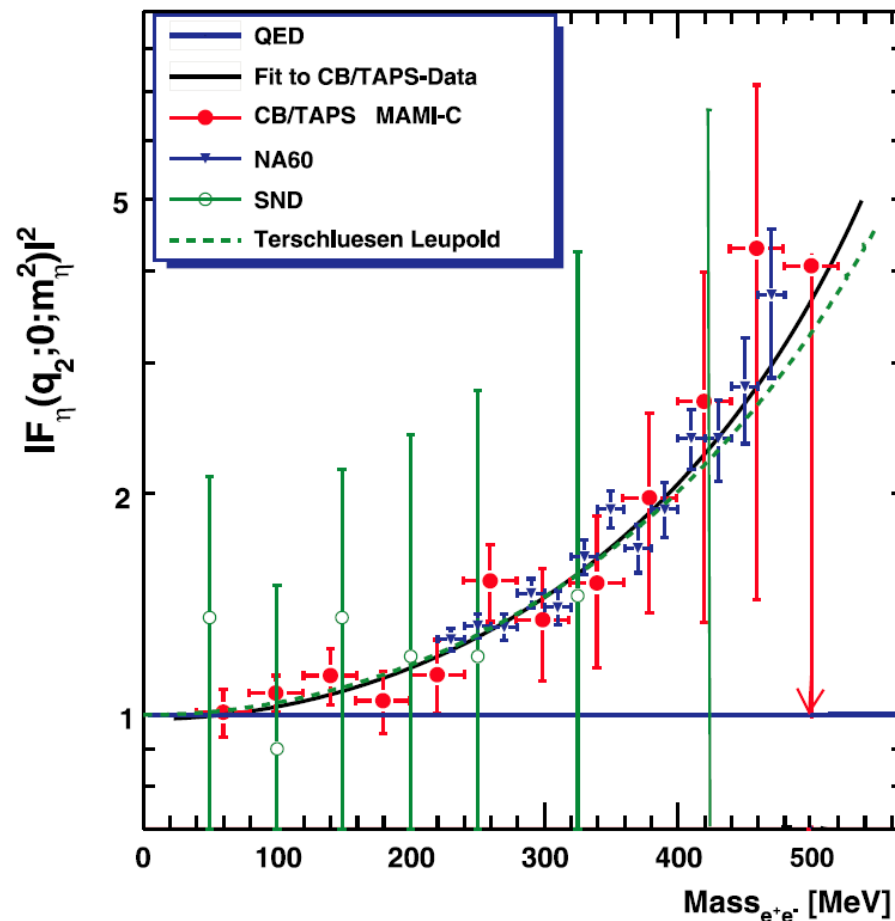
TFF in $\eta \rightarrow e^+e^-\gamma$

H. Berghäuser et al., Phys. Rev. B 701 (2011) 562-567.



Fit to CB/TAPS data:

$$\Lambda = (720 \pm 60_{\text{stat}} \pm 25_{\text{syst}}) \text{ MeV}$$



C. Terschluesen, S. Leupold, private communication
 M.N. Achasov et al. (SND), Phys. Lett. B 504 (2001) 275-281.
 R. Arnaldi et al. (NA60), Phys. Lett. B 677 (2009) 260-266.

New Collaborative Research Center

The Low Energy Frontier of the Standard Model: From Quarks and Gluons To Hadrons and Nuclei



CRC1044

12 years physics program

- The impact of hadron physics for precision tests of the Standard Model
- Timelike and spacelike observables of hadron structure
- Structure and dynamics of light mesons
- Nuclear few-body systems and baryon-baryon interactions

**4 years DFG funding guaranteed
with extension up to 12 years**

Complementary aspects at

MAMI



BES-III/BEPC-II

e^+e^- collider at $\sqrt{s} = 2 \dots 4.5$ GeV:

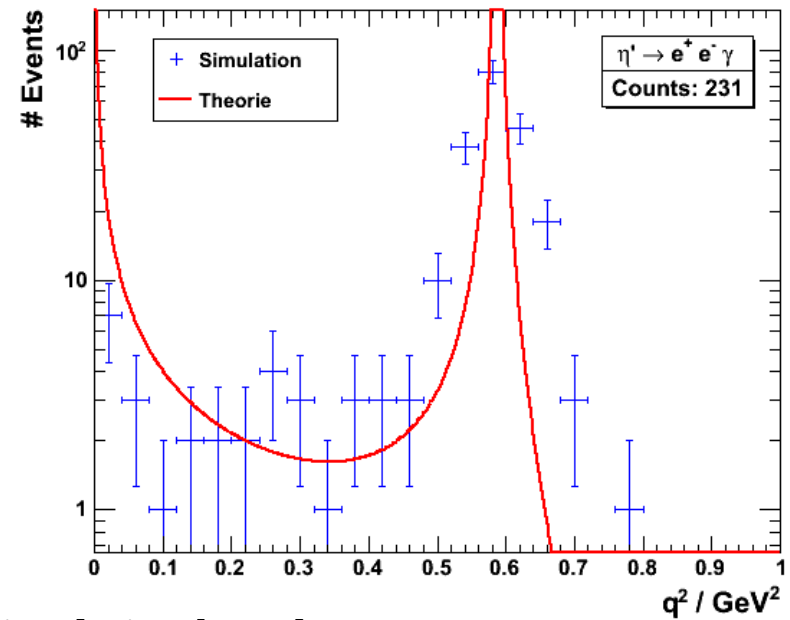


Role of Crystal Ball at MAMI in CRC1044

- Electromagnetic decays of light mesons
 - Production aims for the next 4 years
 - $5 \cdot 10^8 \eta$
 - $2 \cdot 10^8 \omega$
 - $5 \cdot 10^7 \eta'$
- Time-like transition form factors
 - $\eta \rightarrow e^+e^-\gamma$ 30000 events expected
 - $\eta' \rightarrow e^+e^-\gamma$ 200-300 events expected
 - $\omega \rightarrow \pi^0 e^+e^-$ 250-500 events expected
- Goals for 2nd and 3rd funding period
 - TPC for improved tracking and PID
 - Detailed studies of
 - $\eta' \rightarrow e^+e^-\gamma$
 - $\eta' \rightarrow e^+e^-\omega$
 - $\eta' \rightarrow e^+e^-\rho$

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Simulation based on

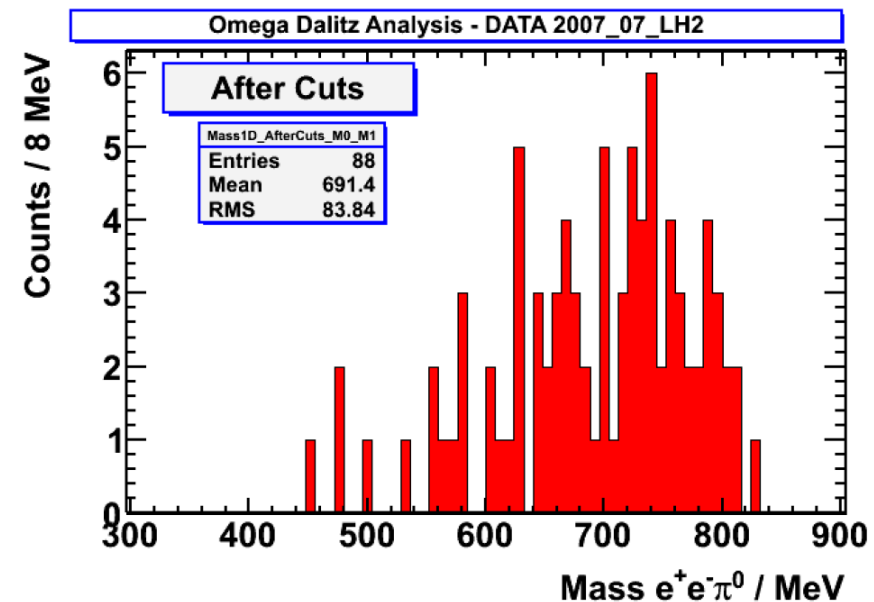
- PDG upper limit for branching ratio
- Estimated η' production rate at MAMI-C (6 weeks, total 18 million η')
- Efficiency from $\eta \rightarrow e^+e^-\gamma$ ($\sim 2\%$)

S. Wagner, Bachelor thesis, University Mainz, 2011
M. Unverzagt, A. Denig

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 - $\eta' \rightarrow e^+e^-\rho$

First study did not yield conclusive result
more statistics from 2009 available



H. Berghäuser, PhD thesis, University Gießen, 2010.
A2-Collaboration

Role of Crystal Ball at MAMI in CRC1044

- Meson decays with unprecedented accuracy
 - Production aims for the next 4 years
 - $5 \cdot 10^8 \eta$
 - $2 \cdot 10^8 \omega$
 - $5 \cdot 10^7 \eta'$
- Branching Ratios
 - $\text{BR}(\omega \rightarrow \eta\gamma / \omega \rightarrow \pi^0\gamma) = 0.0098 \pm 0.0024$
 - $\text{BR}(\eta' \rightarrow \omega\gamma / \eta' \rightarrow \eta\pi^0\pi^0) = 0.147 \pm 0.016$

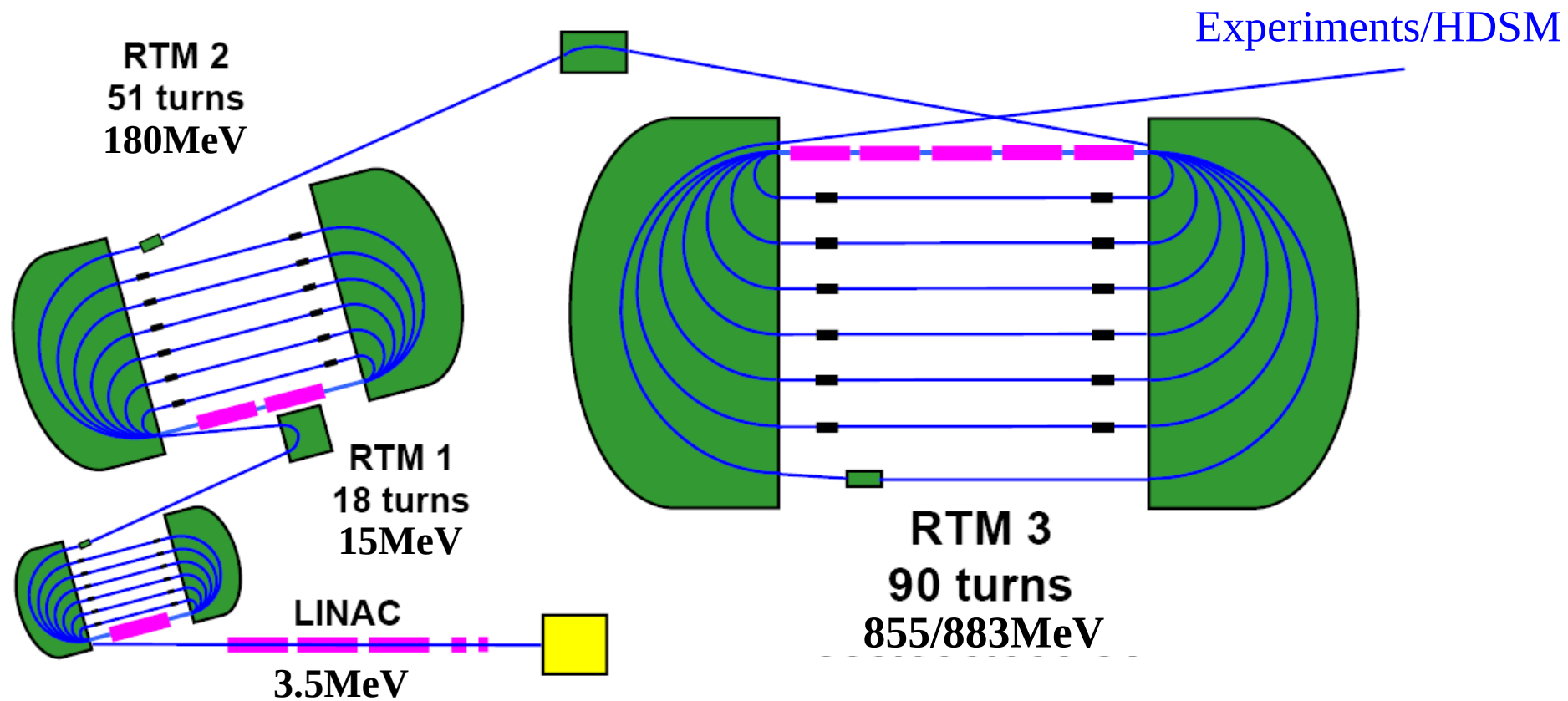
Improve by factor 2 - 5
- Decay dynamics / Tests of ChPT
 - $\eta/\eta' \rightarrow \pi^0\pi^0\pi^0$
 - $\eta' \rightarrow \eta\pi^0\pi^0$ 400000 events expected
- Goals for 2nd and 3rd funding period
 - TPC, new trigger concepts and forward trigger detector
 - Detailed studies of charged decay modes
 - $\eta/\eta' \rightarrow \pi^+\pi^-\gamma$, $\eta/\eta' \rightarrow \pi^+\pi^-\gamma\gamma$, $\eta' \rightarrow e^+e^-\rho$
 - Measurement of absolute branching ratios

Summary

- Crystal Ball at MAMI is ideal for high rate η , η' and ω experiments
 - leading role in neutral decays of η , η' and ω
 - Decay Dynamics
 - Branching Ratios
 - Transition form factor
- New Collaborative Research Centre established at MAMI
 - 4 years of DFG funding guaranteed
 - extension up to 12 years for the full physics program
- First η' run with Crystal Ball successful in March 2012
 - End-point tagger installed and working
 - Taking data right now
- New detector developments:
 - TPC with high rate capability (prototype under construction)
 - forward trigger and tracking detectors under consideration
 - improved detection of charged decays of η , η' and ω

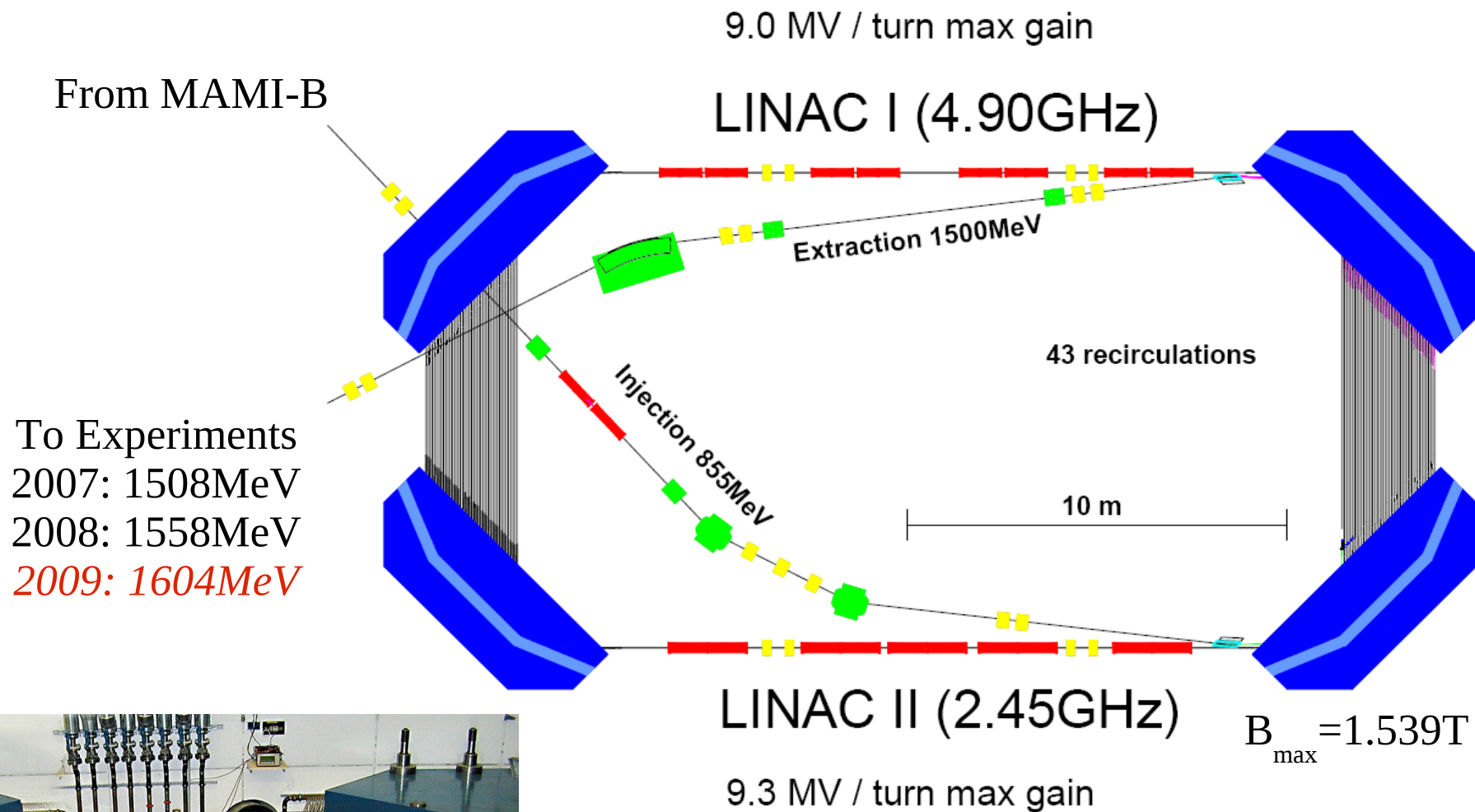
Backup

Mainz Microtron (MAMI-B)



Acceleration via em wave (2.45GHz)
cw: bunch structure ~ 0.4 ns
Injektion LINAC
3 cascaded Race-Track-Microtrons
Magnet of RTM 3 ~ 450 t per Magnet, 1.28T

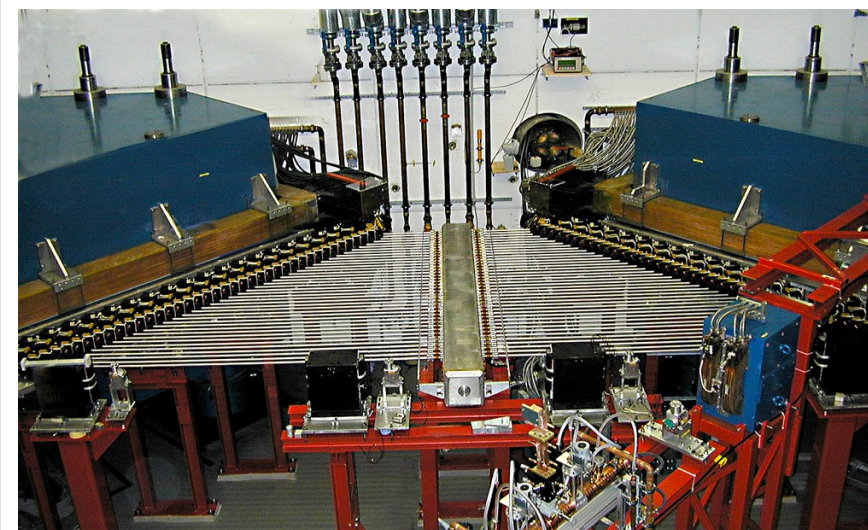
HDSM (MAMI-C)



To Experiments
2007: 1508MeV
2008: 1558MeV
2009: 1604MeV

Harmonic Doubled Sided Microtron (HDSM)

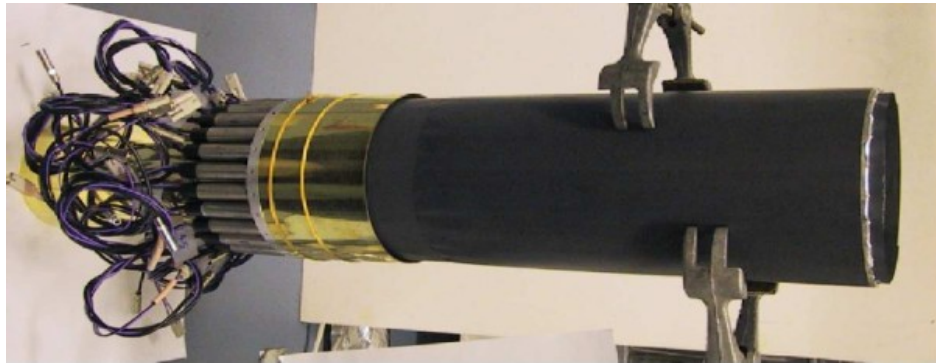
K.-H. Kaiser et al., NIM A 593, 159 (2008).



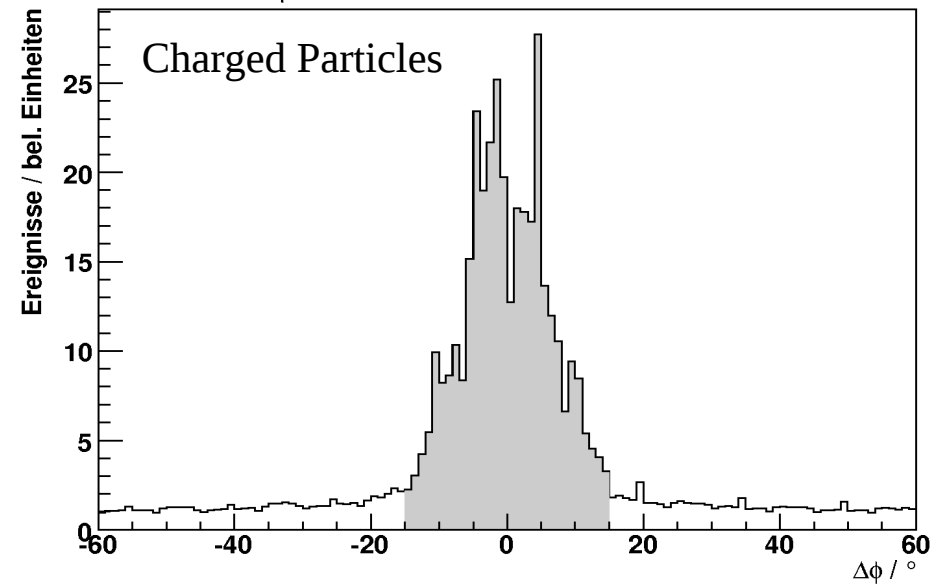
CB PID

Particle Identification Detector (PID):

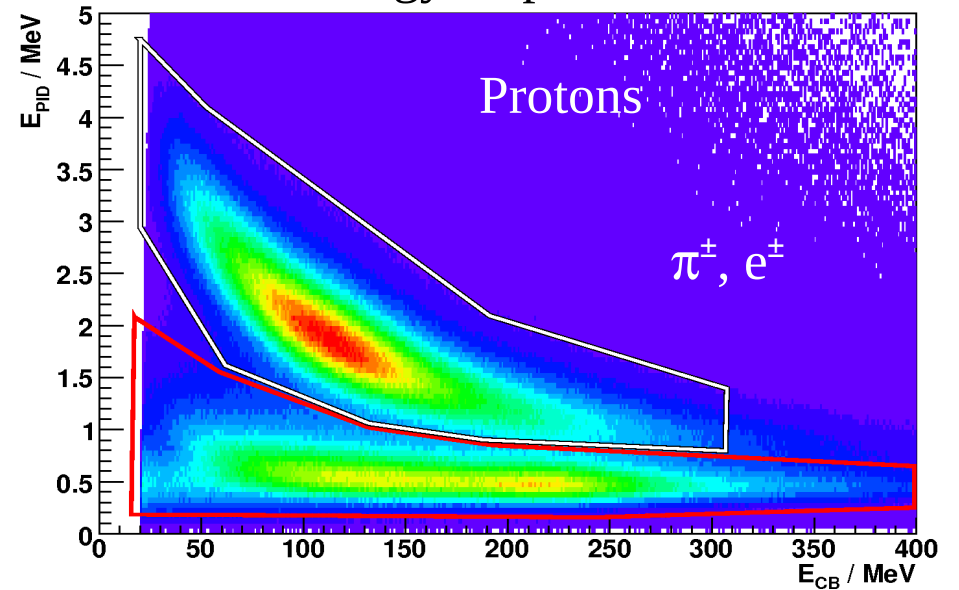
- Cylindrical Detector inside CB
- 24 scintillator strips
- PMT readout



$\Delta\phi$ - between CB and PID

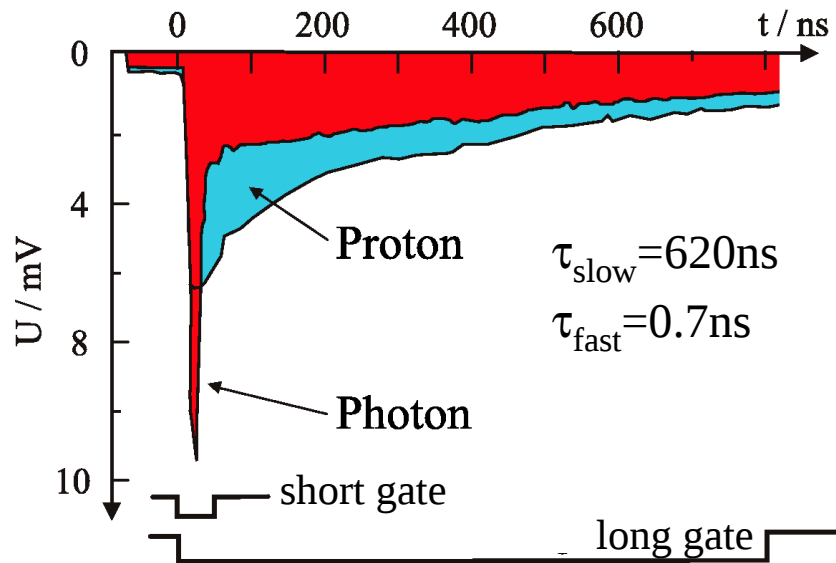
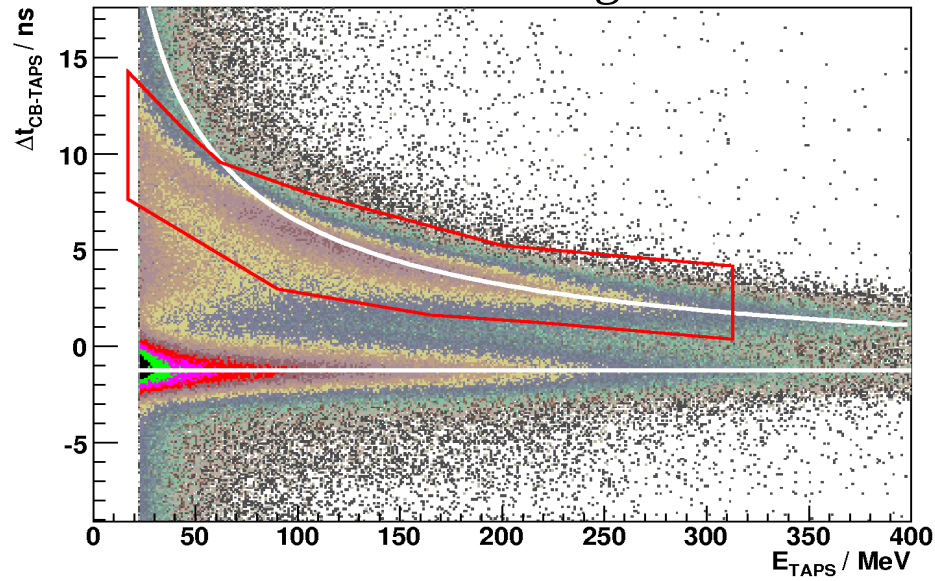


Energy Dependence



TAPS PI

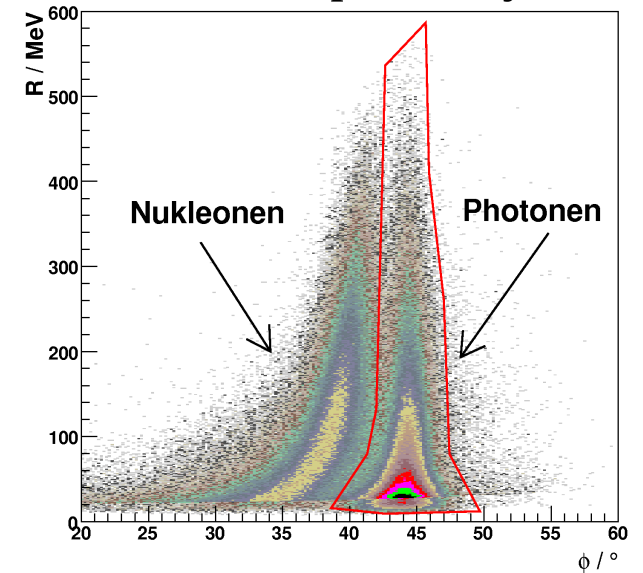
Time-of-Flight



$$R = \sqrt{E_{\text{short}}^2 + E_{\text{long}}^2}$$

$$\phi = \arctan\left(\frac{E_{\text{short}}}{E_{\text{long}}}\right)$$

Pulse-Shape-Analysis

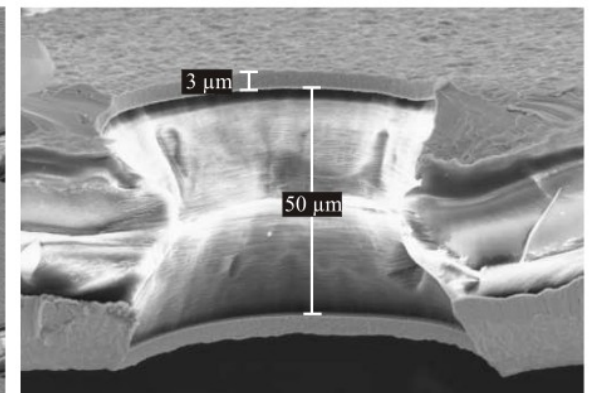
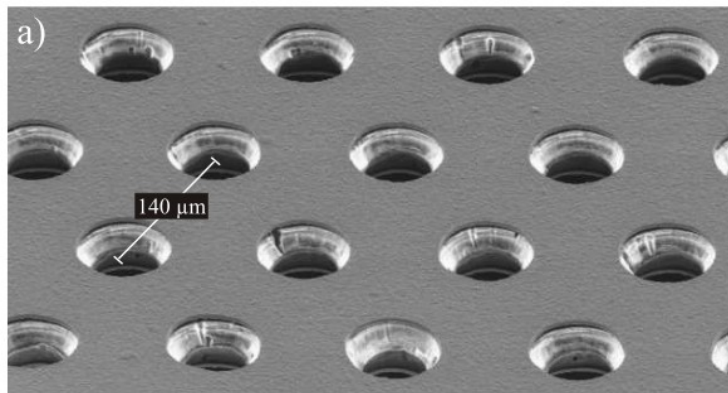
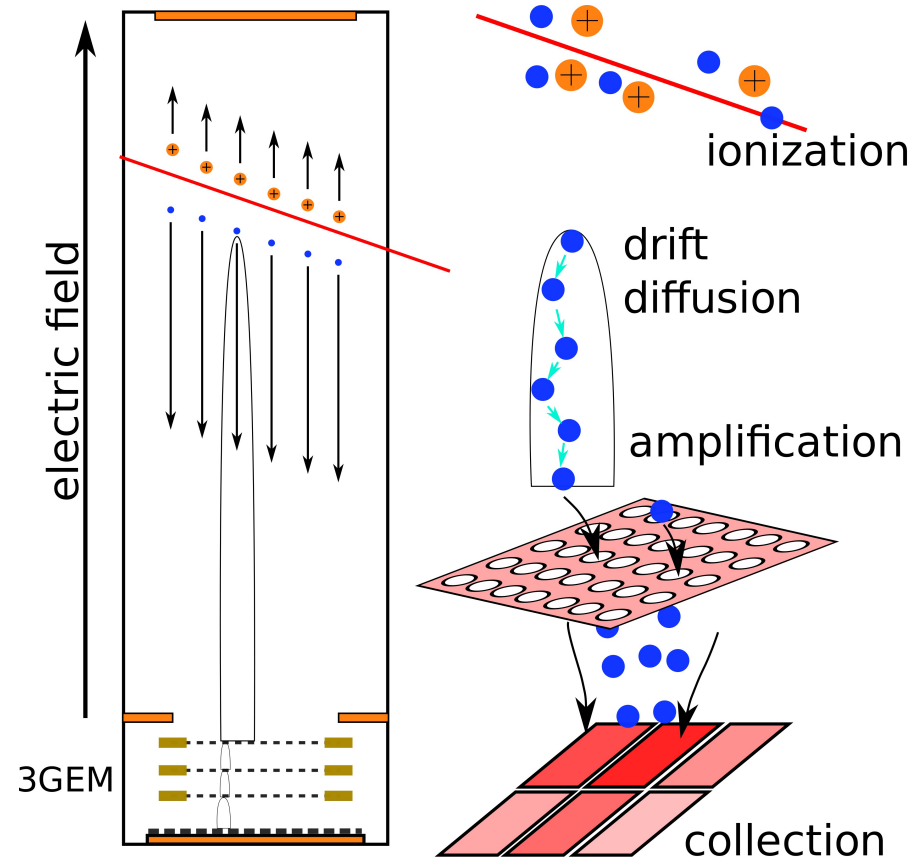
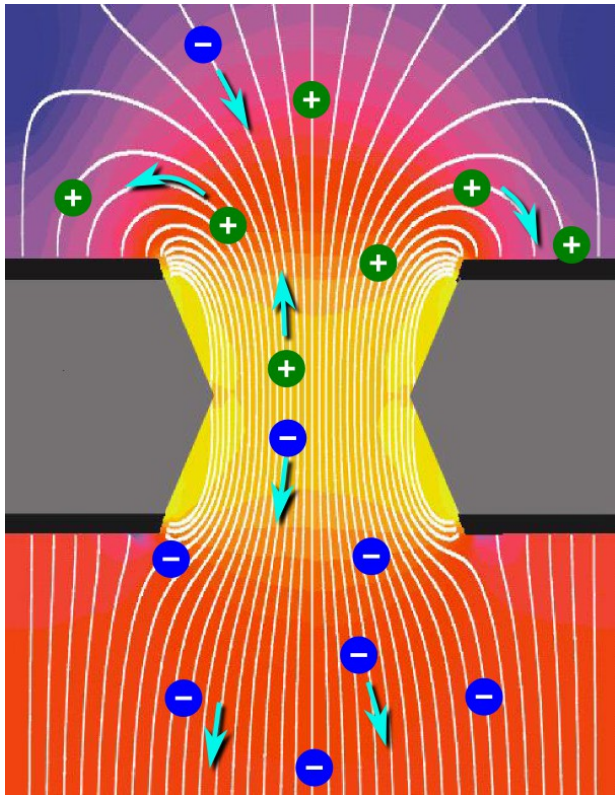


TPC

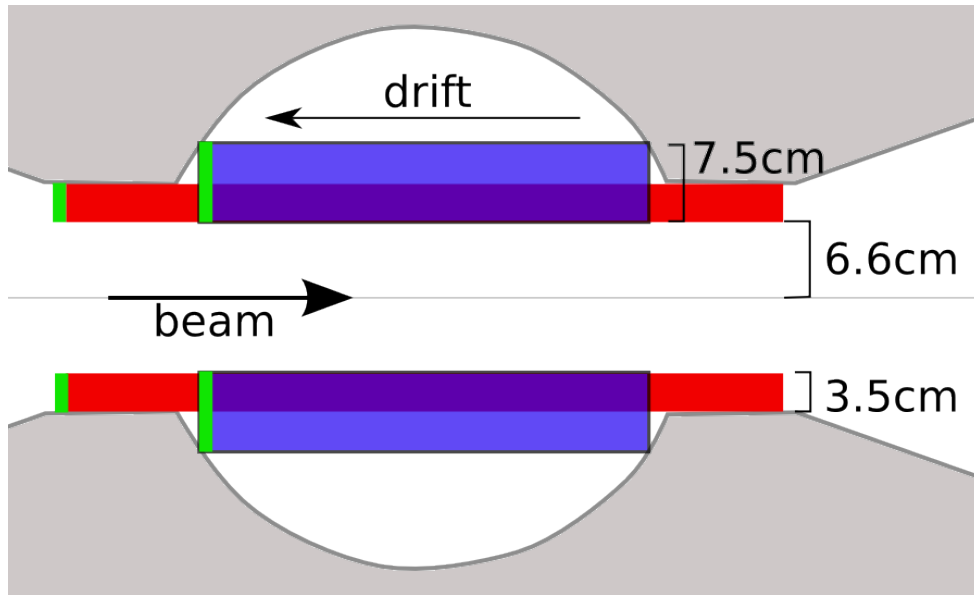
Existing MWPCs are not working for high rate meson decay experiments

TPC advantages:

- Improve resolution
- Higher rate capability
- Contribute to particle ID (dE/dx measurement)
- Track reconstruction



TPC in CB



- Readout on backward end
- Space needed for target and PID
- Pad size: $\approx 2 \text{ mm} \times 5 \text{ mm}$
- \rightarrow 2000 to 5000 channels

Long version:

- $\approx 3.5 \text{ cm}$ effective radius
- Only few pad rows
- Easier installation

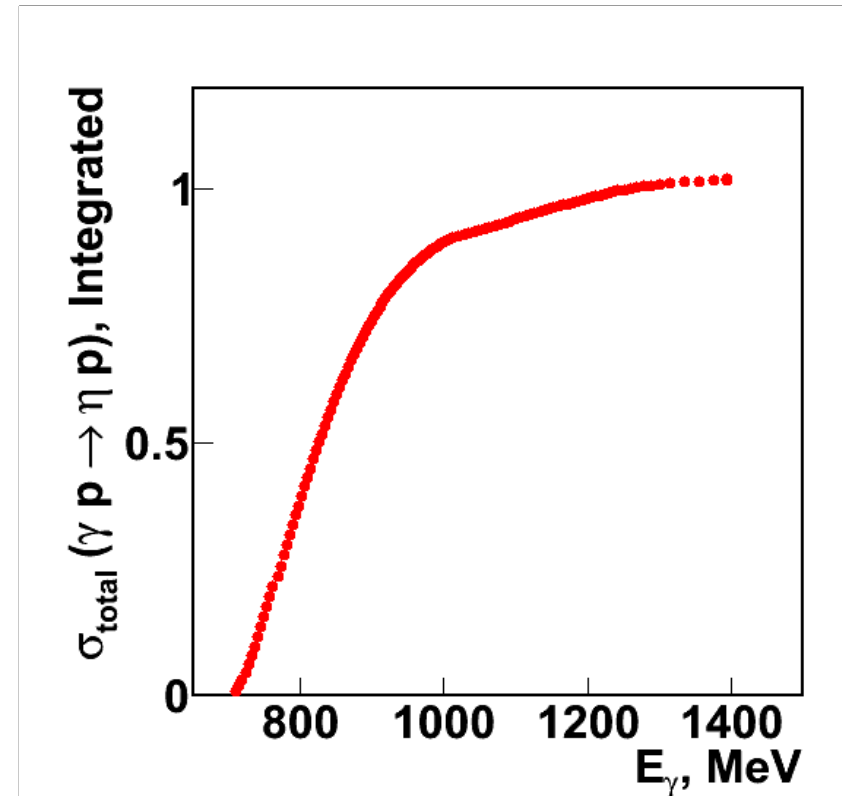
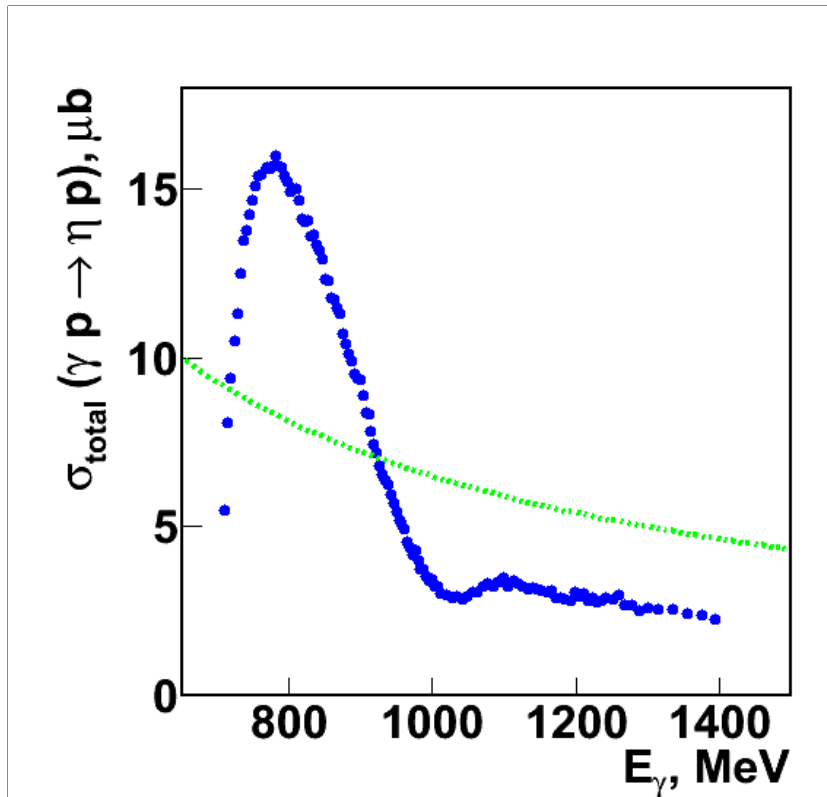
?

Short version:

- $\approx 7 \text{ cm}$ effective radius
- More data points
- End caps cover lowest crystals
- But end caps very thin

- First test with old TPC from Karlsruhe successful
- 2011: construct prototype

η -Photoproduction



At **MAMI** a beam of tagged photons of **excellent quality** is available:

- **High intensity** photon beam
- **Fine energy resolution**
- **Outstanding stability**

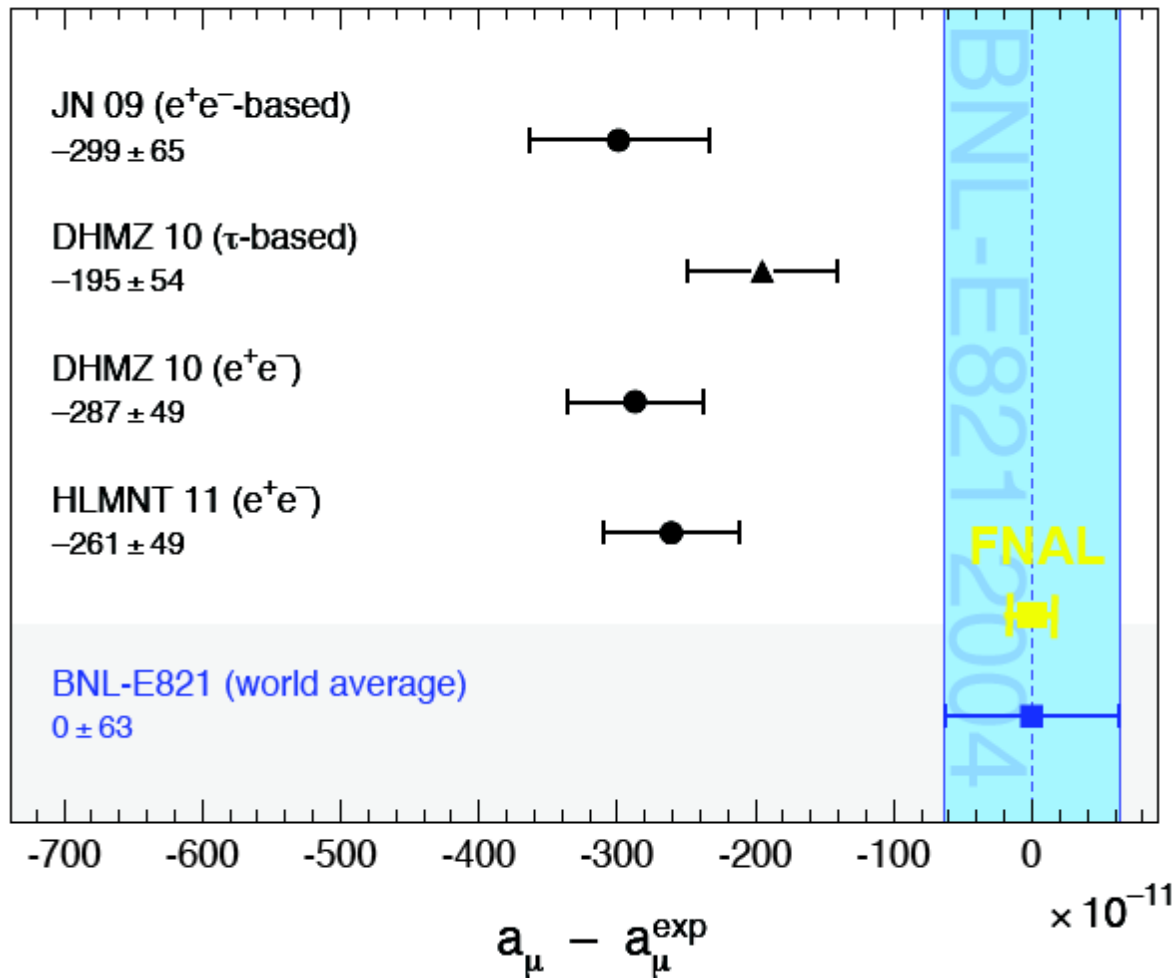
Beam energy nearly perfect for **high statistics** η photoproduction

$(g-2)_\mu$ Theorie vs. Experiment

Standard Model: $(116\,591\,834 \pm 49) \cdot 10^{-10}$

Experiment: $(116\,592\,089 \pm 63) \cdot 10^{-10}$

Status: summer 2011 (published results shown only)



Striking result:

$$a_\mu^{\text{exp}} - a_\mu^{\text{theo (SM)}}$$

> 3 standard deviations

New FNAL $(g-2)_\mu$ measurement E969:



Factor 4 improvement of experimental error

Contributions to $(g-2)_\mu$

- QED contributions:

$$(116584718.09 \pm 0.16) * 10^{-11}$$

- Electro-Weak Contribution:

$$(154 \pm 2) * 10^{-11}$$

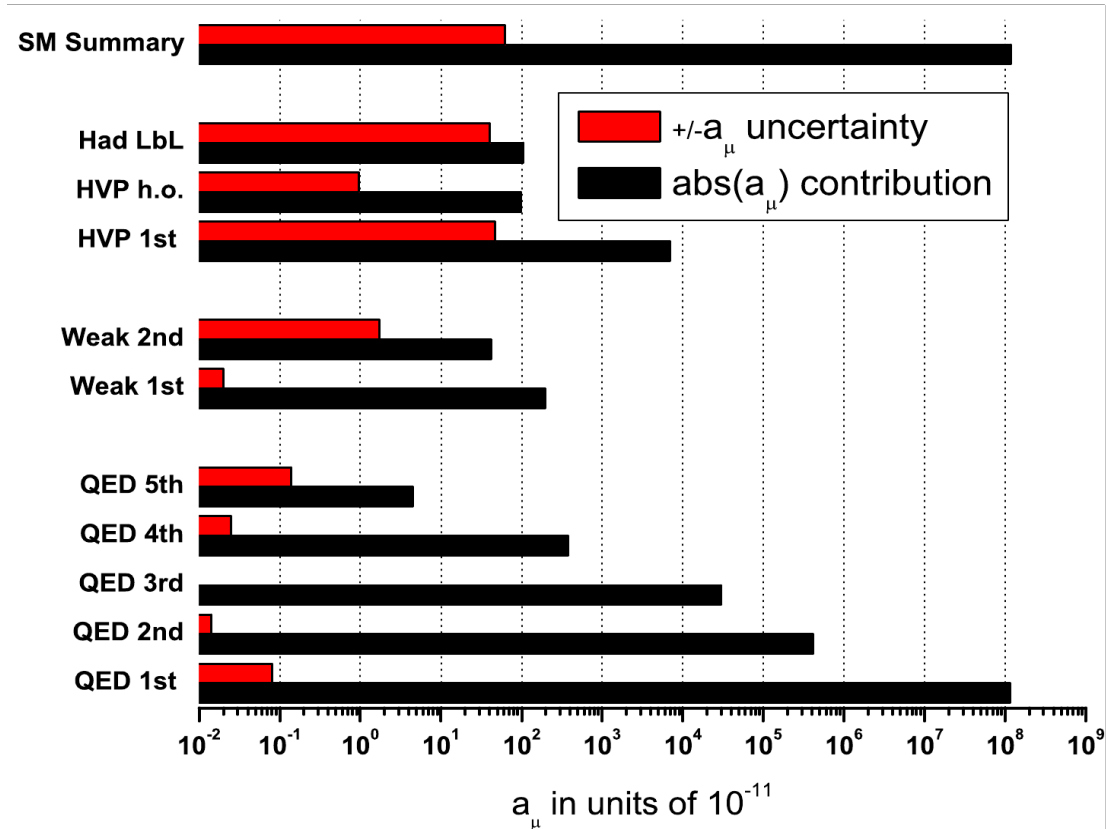
- Hadronic vacuum polarization:

$$(6955 \pm 41) * 10^{-11}$$

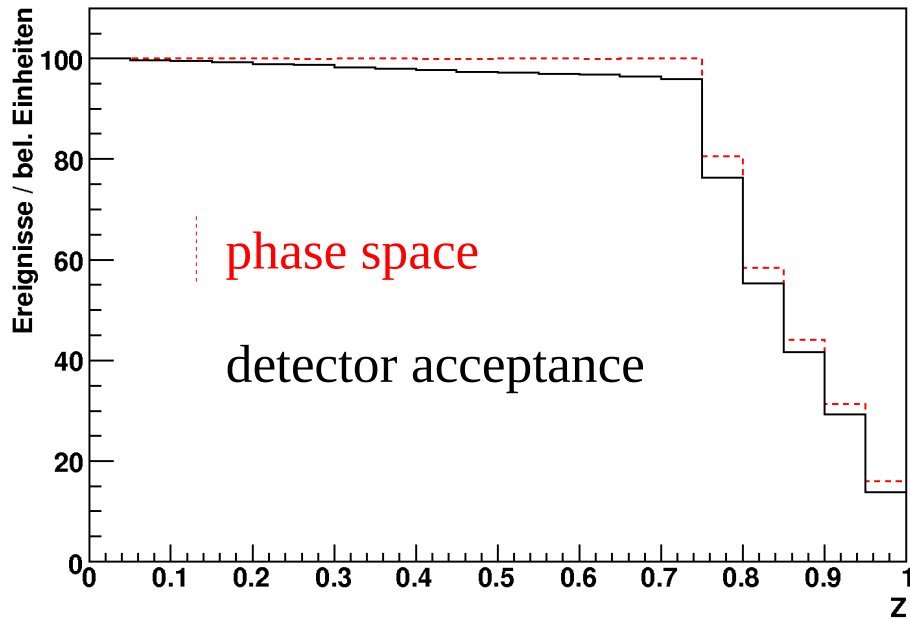
- Hadronic light-by-light:

$$(105 \pm 26) * 10^{-11}$$

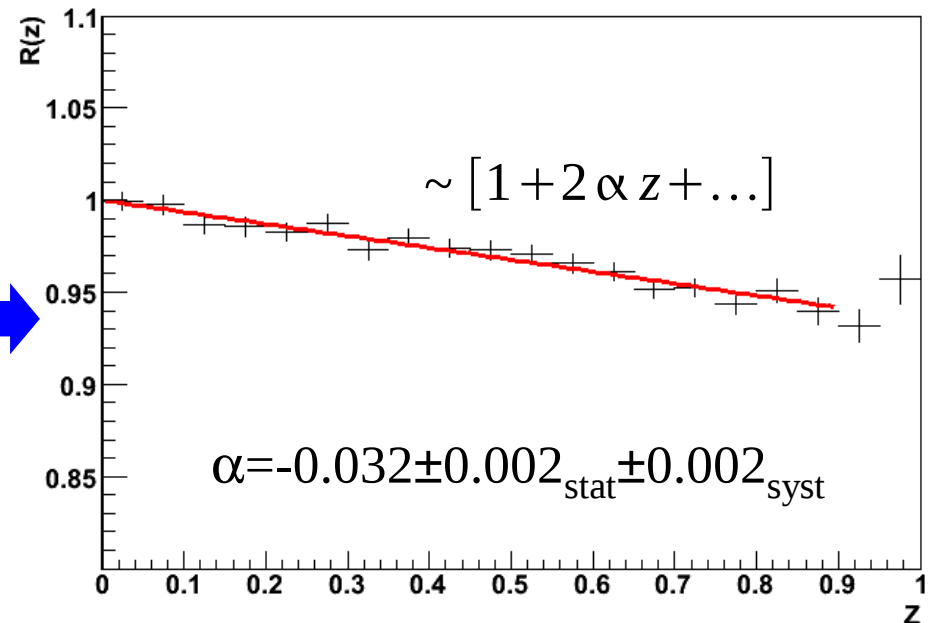
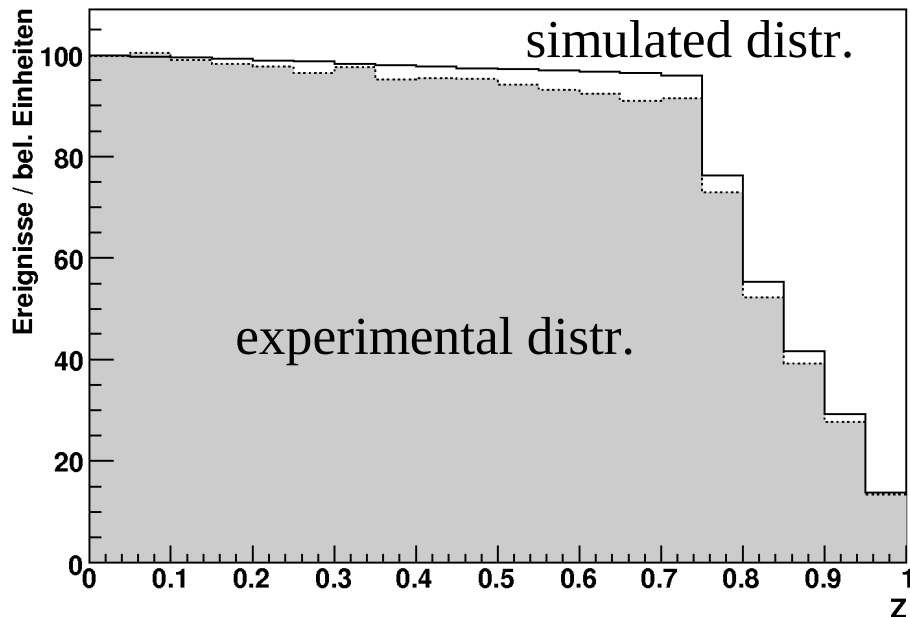
Uncertainty of the light-by-light hadronic contribution is expected to be dominant for the next generation of the $g-2$ measurements



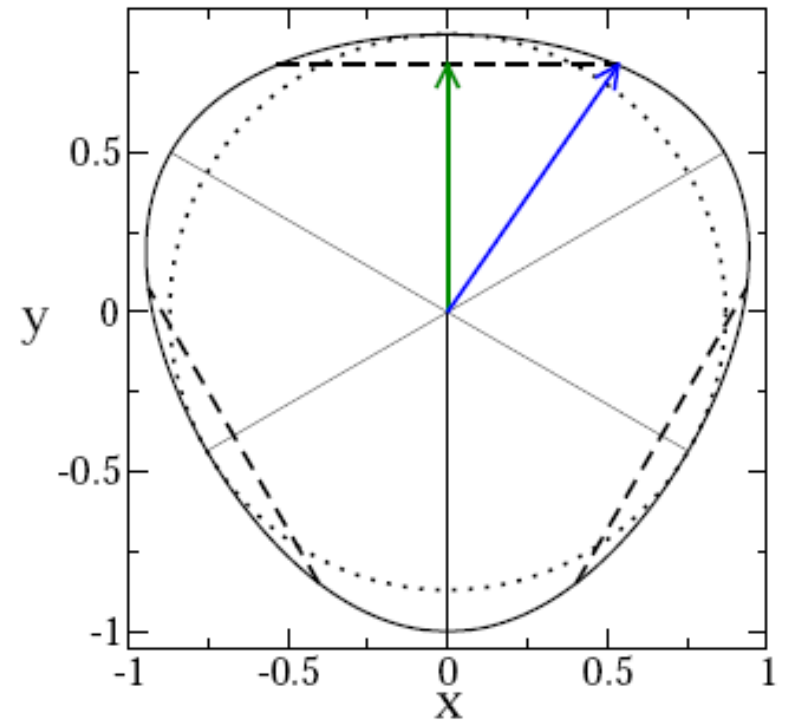
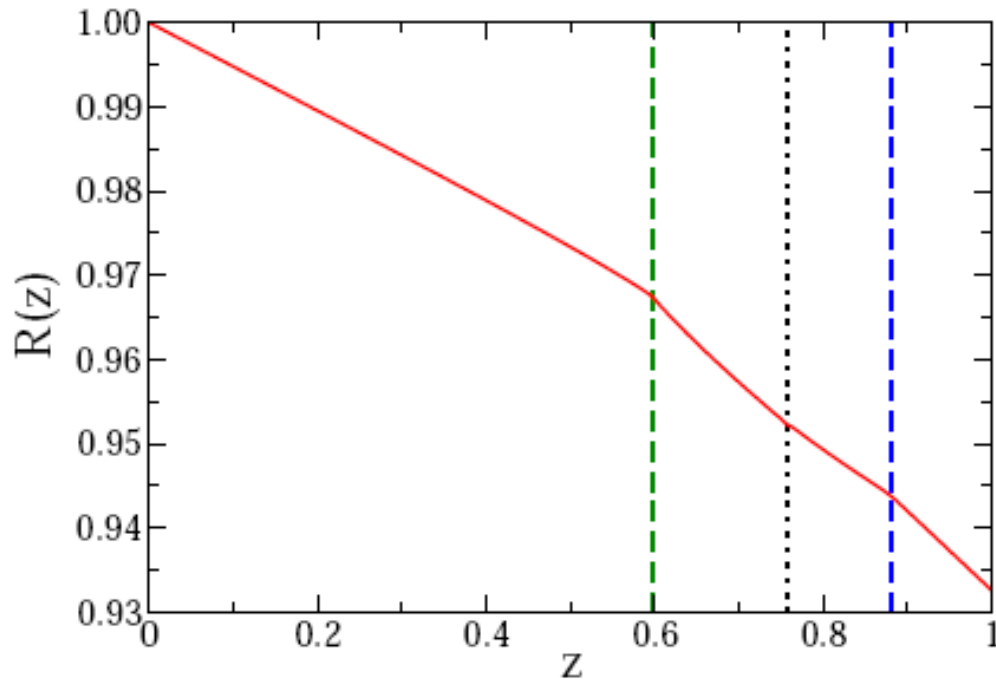
Result for α



- precise simulation required



Effect of Cusp on α



Cusp has 5% effect on Dalitz Plot Parameter

C. Ditsche, B. Kubis, Ulf-G. Meißner, Eur. Phys. J. C 60, 83 (2009).

Further effects:

- Kinematic boundaries
- Second order in amplitude expansion

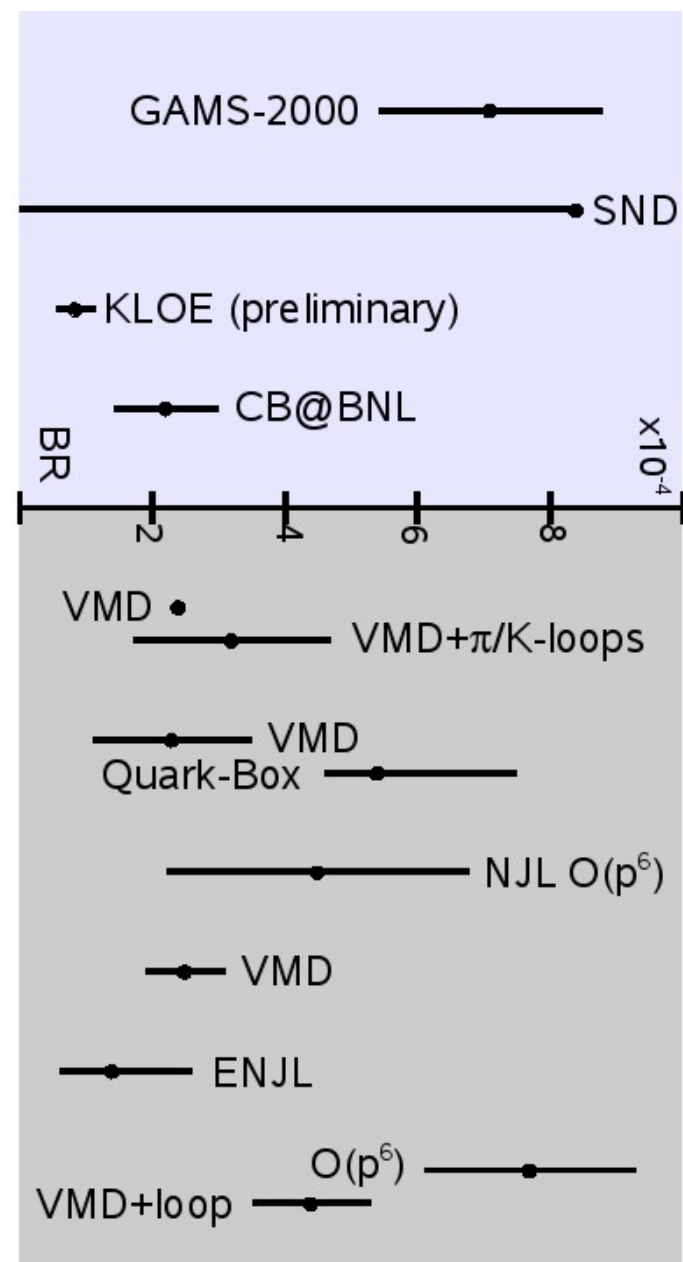
Tests with $\eta \rightarrow \pi^0 \gamma \gamma$

$$L_{eff} = L_2 + L_4 + L_6 + \dots$$

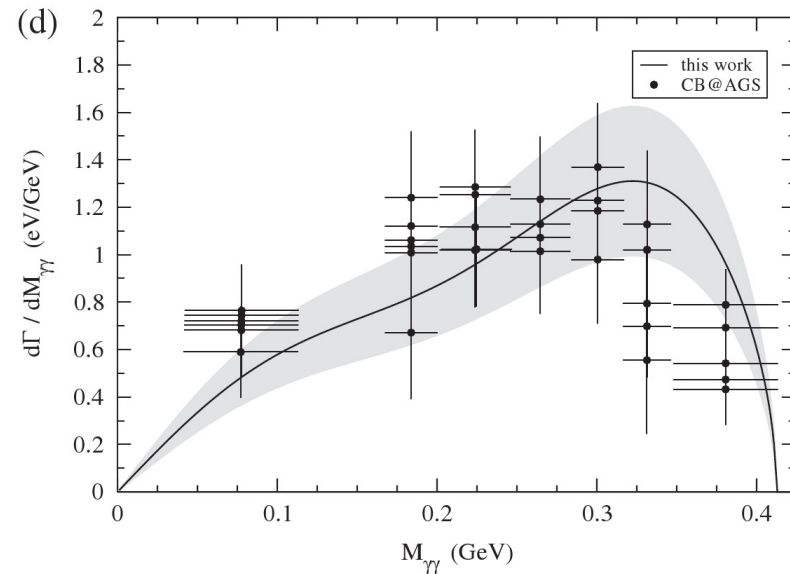
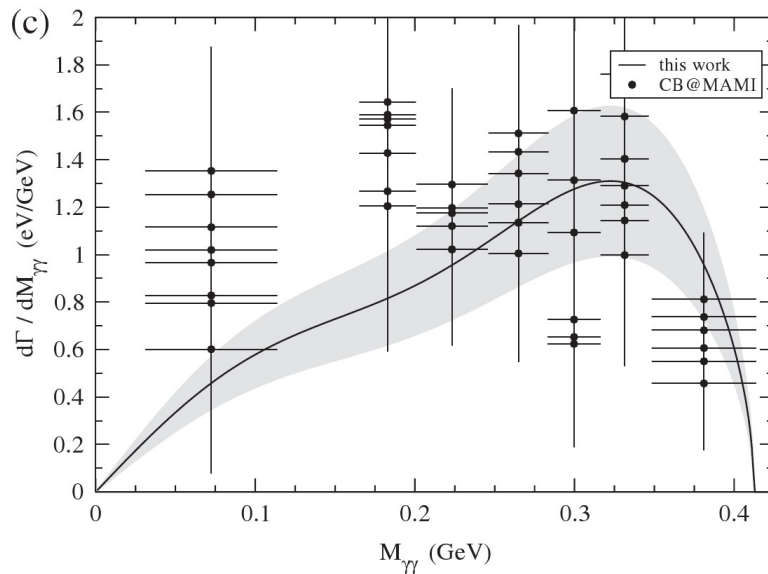
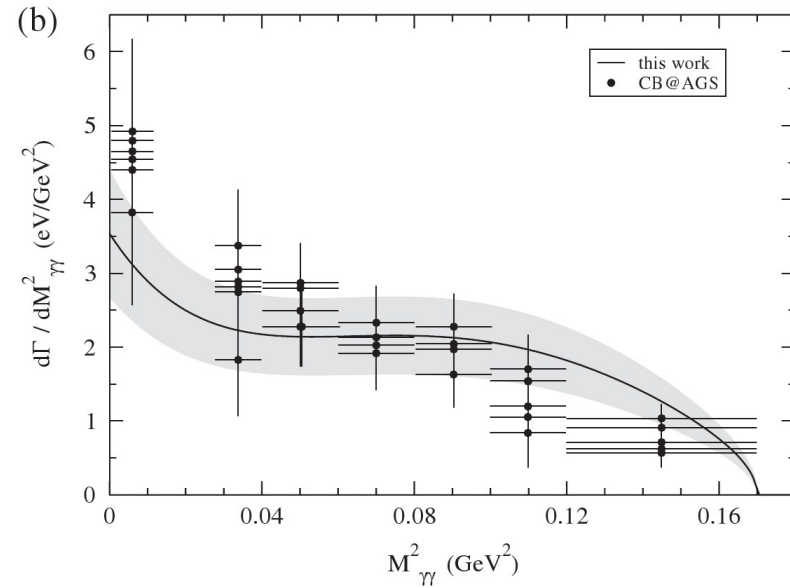
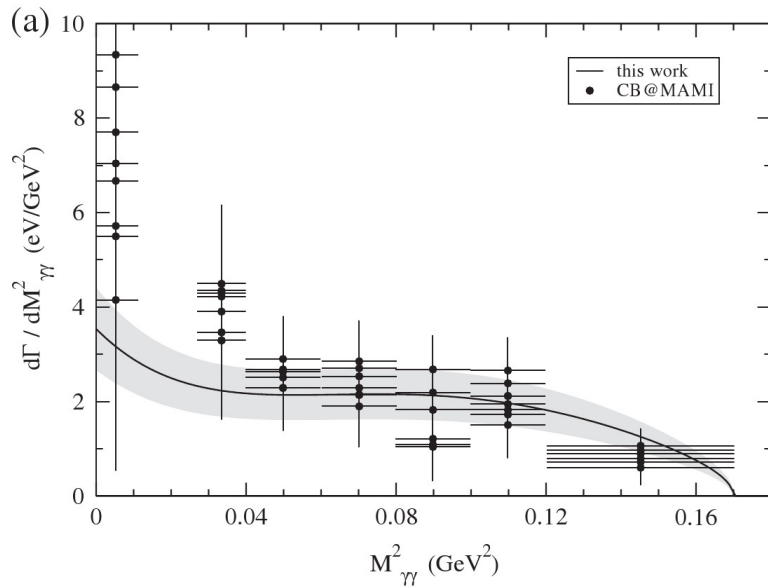
Tree level amplitude at $O(p^2)$ vanishes as neither π^0 nor η can emit a photon

Tree level amplitude at $O(p^4)$ vanishes as neither π^0 nor η can emit a photon, π and K loops largely suppressed by G -parity violation and the large Kaon mass, respectively

First sizable contribution from $O(p^6)$, but coefficients must be determined using models (e.g. VMD)



Branching Ratio of $\eta \rightarrow \pi^0 \gamma \gamma$

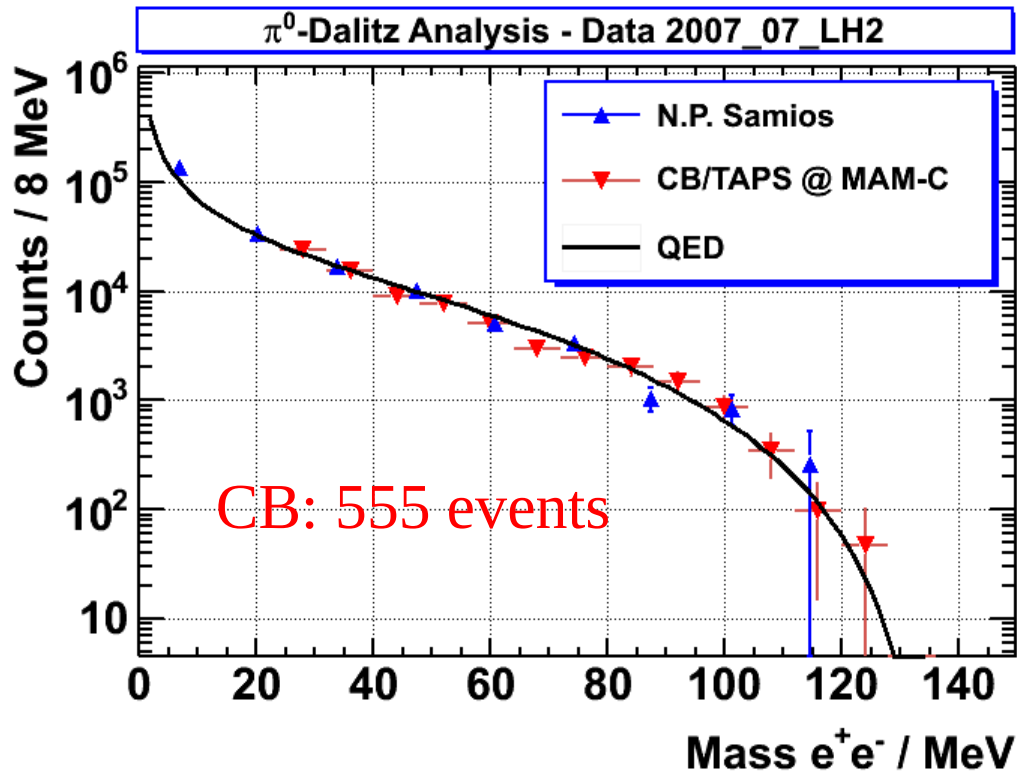


$$BR(\eta \rightarrow \pi^0 \gamma \gamma) = (2.290 \pm 0.059_{stat} \pm 0.022_{syst}) \cdot 10^{-4} \text{ (preliminary)}$$

S. Prakhov (UCLA)

TTF in $\pi^0 \rightarrow e^+e^-\gamma$

H. Berghäuser, PhD thesis, Gießen, 2010.



N.P. Samios et al. (BNL), Phys. Rev. 121 (1961) 275-281.

- Expected behaviour:

$$F(m^2) = \frac{1}{1 - \frac{m^2}{\Lambda^2}} \quad m_\pi \ll \Lambda \quad \Rightarrow \quad F(m^2) \approx 1$$

$\eta' \rightarrow e^+e^-\gamma$

