

Summary:  
Impressions and Directions,  
followed by discussion

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Open Questions in Parton Hadron Duality

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UVA



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# Too simple famous theorem

- If we use Nachtmann variable, and
- if we believe duality is perfect,

$$\int_0^1 d\zeta \zeta^n F(\zeta, Q^2) = a_n = \text{const.},$$

- then the structure function is zero,

$$F(\zeta, Q^2) = 0.$$

- (See Gross, Treiman, Wilczek, 1977.)

# Data

- Duality context here  $e+A \rightarrow e+X$
- Relation between scaling function seen at high  $Q^2$  and resonances at lower  $Q^2$ .
- Seen in  $A = p, n, d$ , other nuclei, both  $F_T$  and  $F_L$ , and in polarized cases (Thia, Simona, Eric, Donal, Ionna, Xiaochao, Oscar, Victor, Nilanga)
- $\exists$  violations for  $\Delta$  at various  $Q^2$  in polarized case.

# Definitions

- Local  $W$  ranges
- Moments and truncated moments
- Perturbative expansion (Poggio, Quinn, Weinberg; see Shifman talk, 2003),
  - Exact structure function/cross section, suitably averaged  $\approx$  Perturbative calculation to some order, similarly averaged, at high energy
  - Easier context,  $e^+ e^- \rightarrow \text{hadrons}$

# Theory

- Fewer theory talks than experimental talks!
- Modeling: Veneziano (Tim), Harmonic osc. (Wally)
- Effects on PDF fits (Alberto)
- Utility for finding PDFs as  $x \rightarrow 1$  (Eric, Alberto)
- Utility for  $\alpha_s$  determination (Simonetta)

# Summary of Summary

- Duality has an exciting future
- Especially if we understand what it tells us about QCD
- Not enough teleology understood
  - Workings of definitions
  - Modeling: Venezano, Harmonic Oscillator models
- Useful application: structure functions in limit  $x \rightarrow 1$ .

# Discussion

- What should we do next?
  - Experiment
  - Theory
    - Basic theory
    - Fitting data/extrapolating scaling curves

# Extra slide

