

# Two meson cloud of the baryon antidecuplet

Pentaquark'05,  
Jefferson Laboratory 20/10/2005

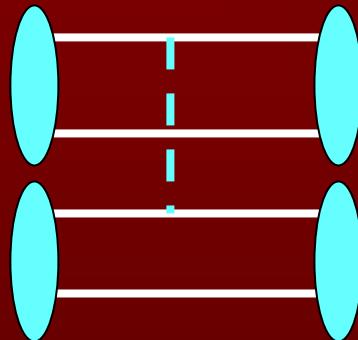
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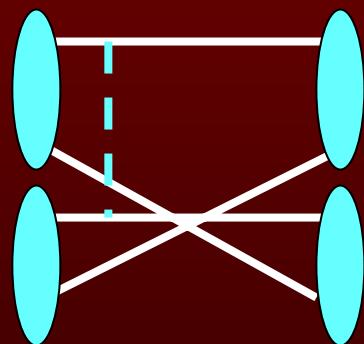
# Outline:

- Resonating Group Method and hadron molecules
- $\Theta^+$  not a molecule
- No  $N\bar{K}\pi$  resonance above threshold ( $Z^*$ ) —
- Two meson cloud of 10

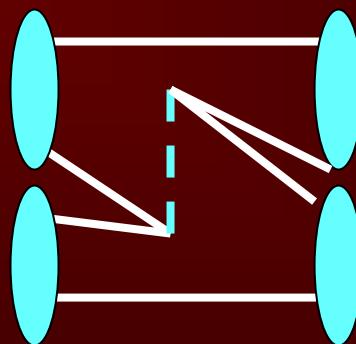
# Exotic SU(3) channels are repulsive (E. Ribeiro 1980)



= 0 (color factor)



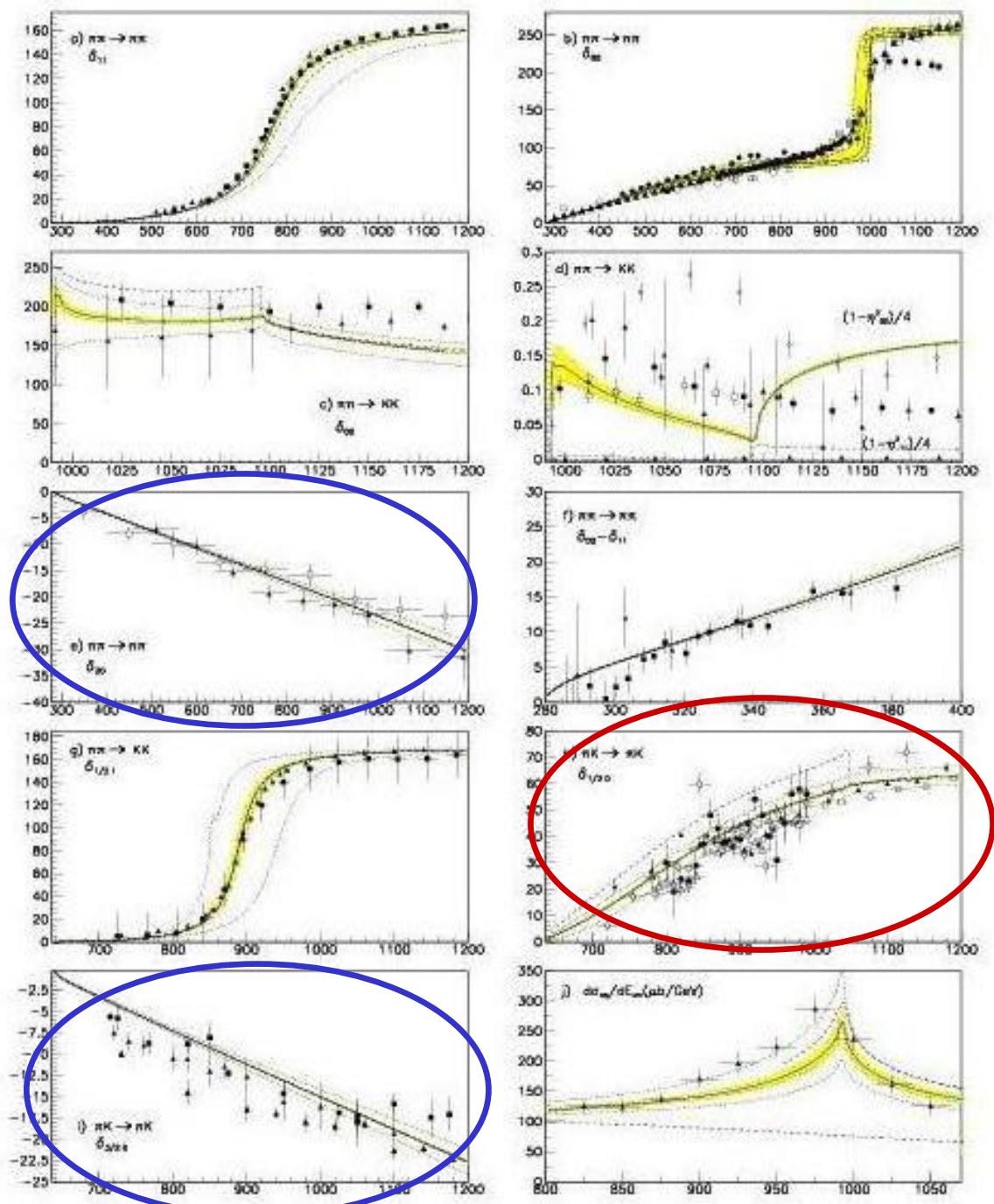
repulsive



attractive

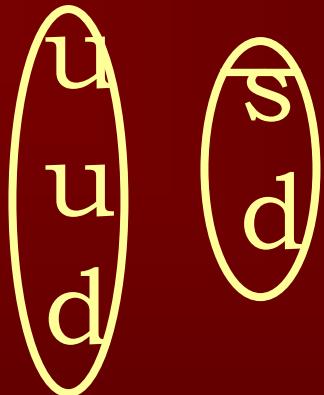
In exotic scattering the second diagram can't contribute  
for example  $\pi^+ \pi^+$  ( $I=2$ )  $u\bar{d} u\bar{d}$  no annihilation

# Gomez Nicola Pelaez (2001)

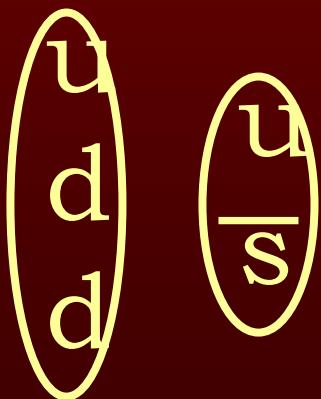


# Exotic Kaon Nucleon molecule?

$pK^0$

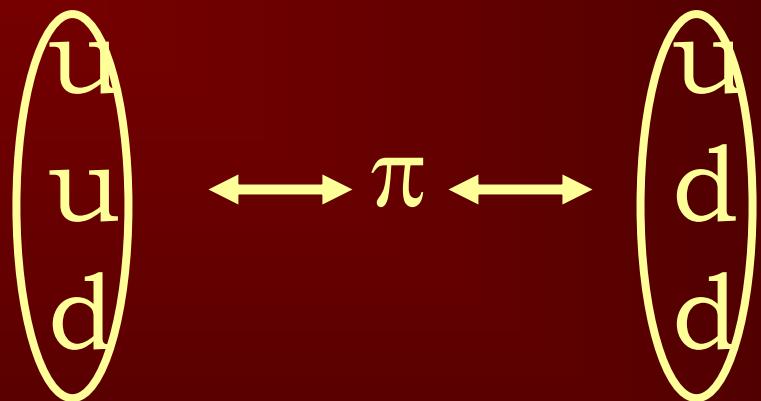


$nK^+$



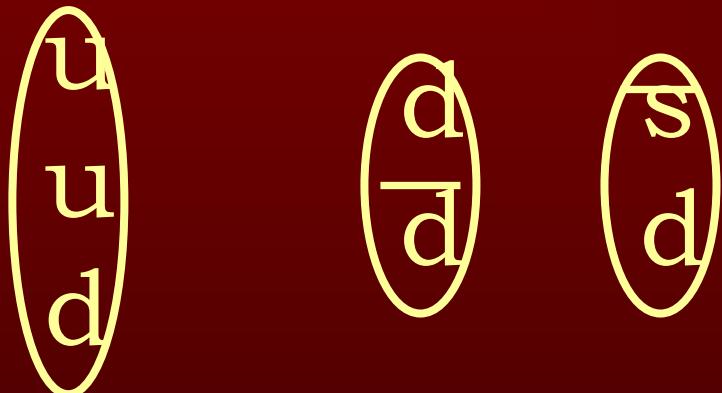
Pauli exclusion principle at work  
No resonance

# A famous exotic molecule



The deuteron

# $\Theta^+$ as heptaquark molecule (Bicudo and Marques, 2003)



P

$\pi$

K M=1573 MeV

Use a pion in the  
valence wavefunction  
for a parity + stat

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Make use of  $K\pi$  correlation:  $\kappa$

Experimental evidence: BES&L

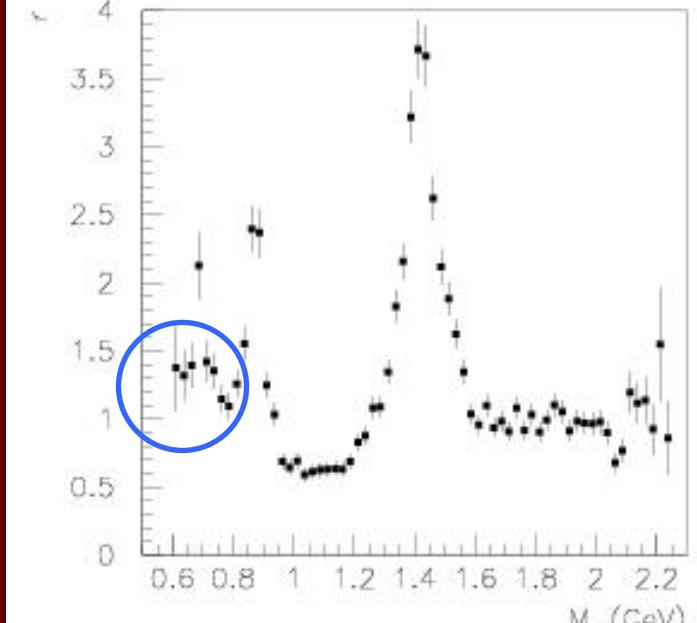
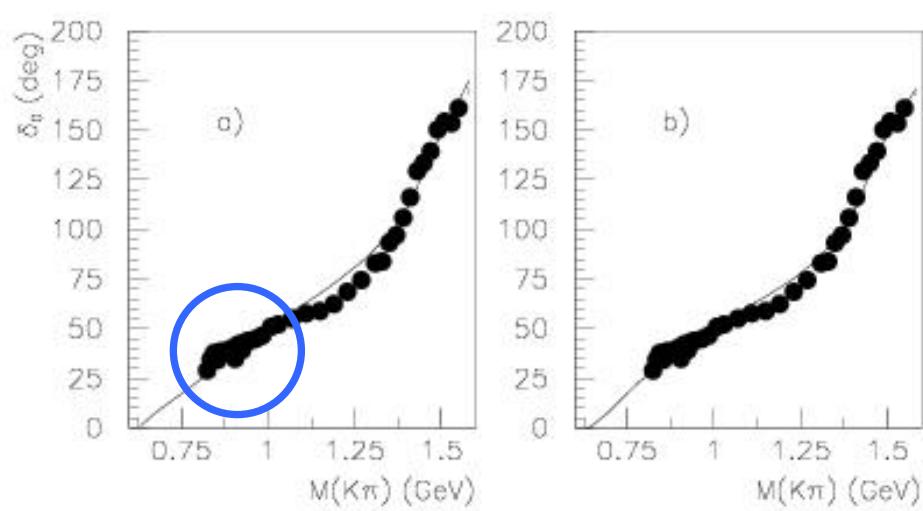
$J/\psi \rightarrow (K\pi)(K\pi)$

Analysis by D. V. Bugg

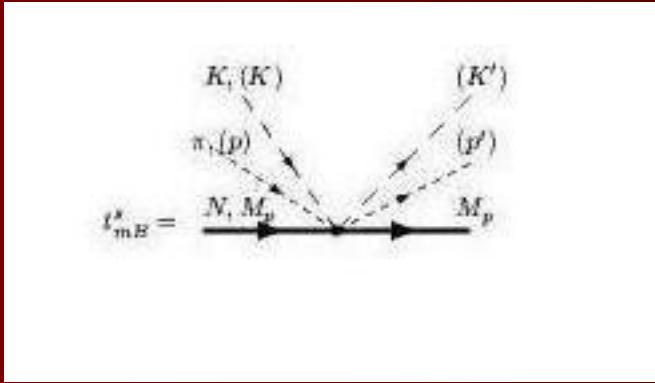
hep-ex/0510026

# Mass spectrum recoiling against a $K^*$

## Phase shift



Mass 700-800 MeV  
Width 400 MeV  
(Gomez Nicola and  
Pelaez, 270 MeV)



# Two meson-nucleon vertex (approximate on-shell factorizati

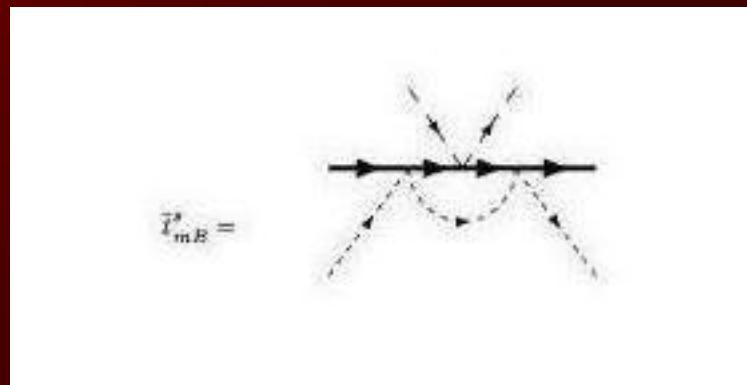
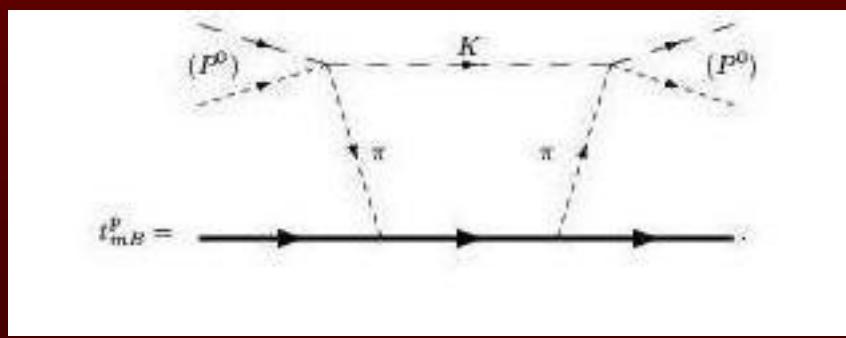
$$\langle \Theta^1 | t_{mB}^s | \Theta^1 \rangle = -\frac{1}{144f^4} (-4(\cancel{K} + \cancel{K}') - 11(\cancel{p} + \cancel{p}'))$$

$$\langle \Theta^0 | t_{mB}^s | \Theta^0 \rangle = -\frac{21}{144f^4} ((\cancel{K} + \cancel{K}') - (\cancel{p} + \cancel{p}'))$$

# $K\pi N$ scattering matrix with Lippman-Schwinger equation



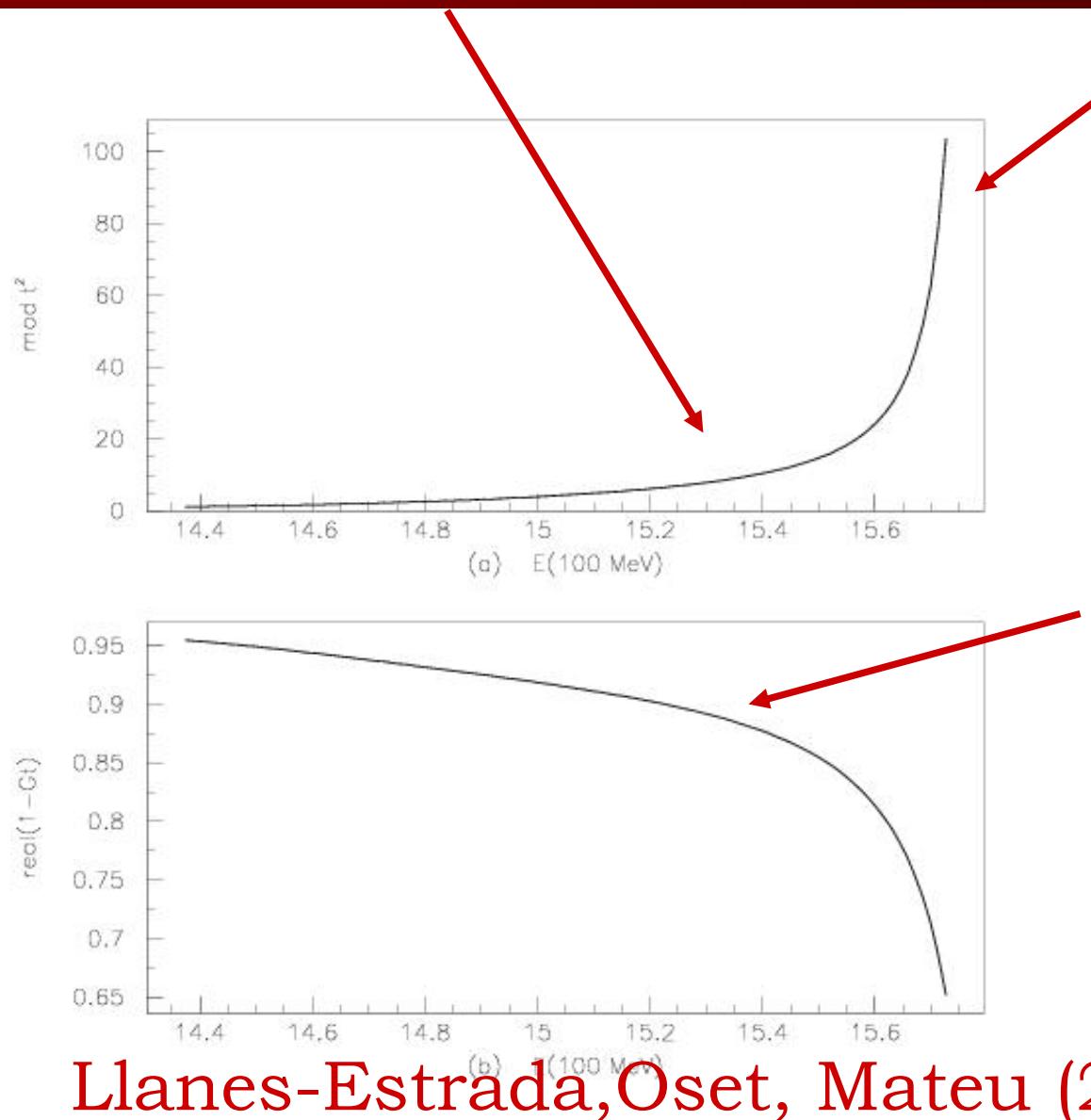
Need to examine other vertices



$$t_{mb}^p$$

$$t_{mb}^{s2}$$

# $|t|^2$ : no resonance



$K\pi N$  threshold effect

1-GV (denominator of Lippman-Schwinger geometric series: no zero.)

Llanes-Estrada, Oset, Mateu (2003)

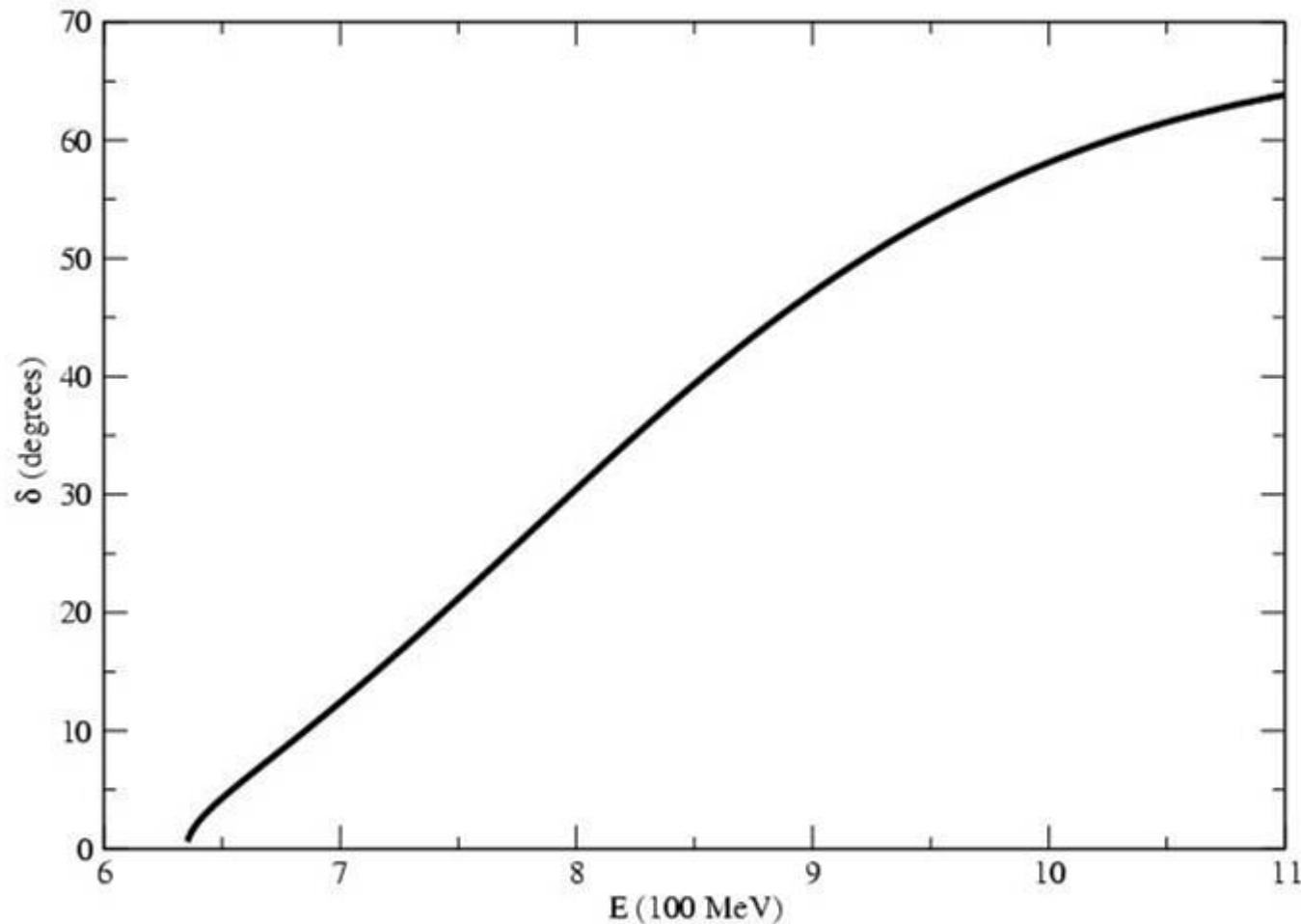
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# Old predictions (compiled by Nowakowski et al. 2003)

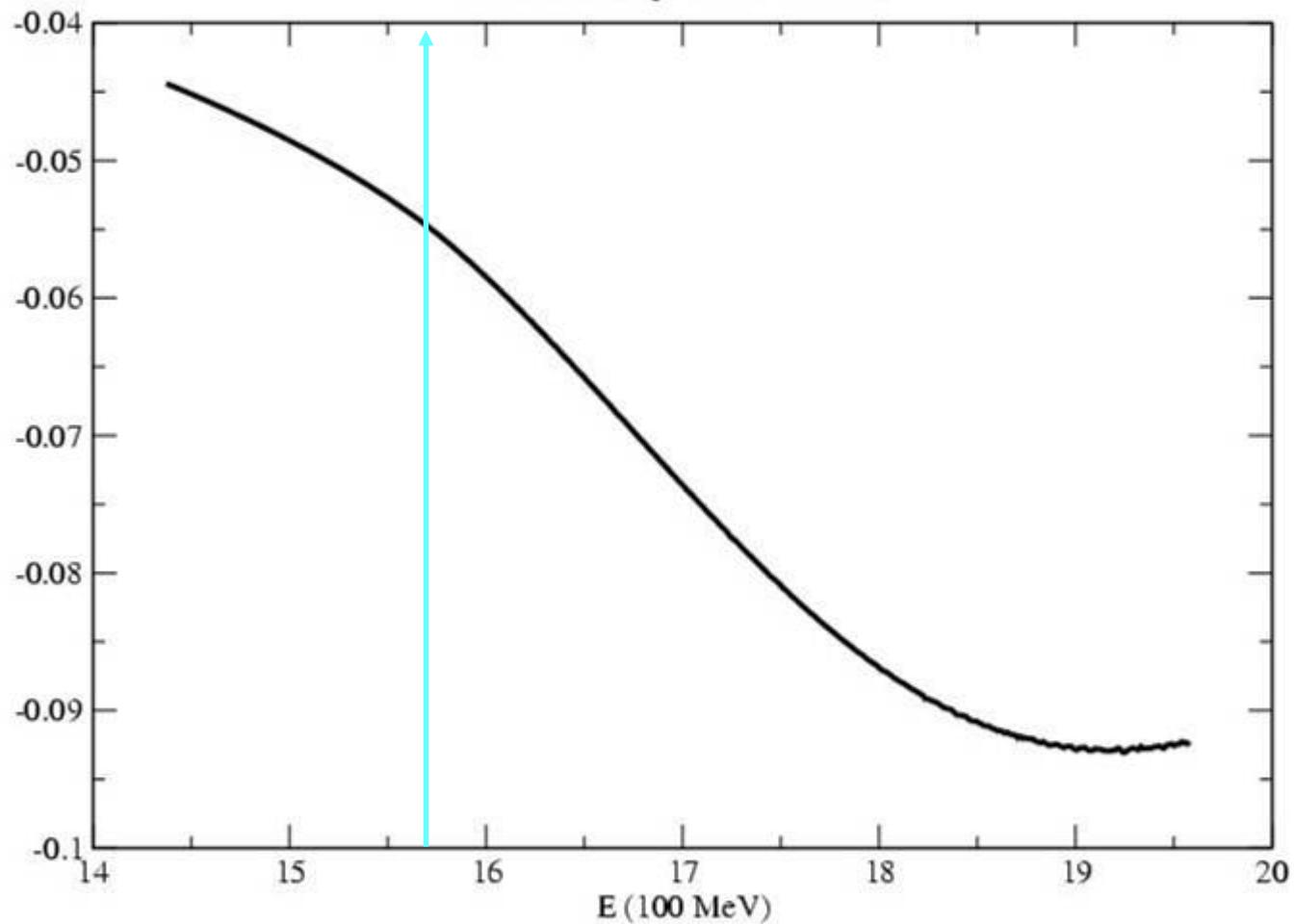
- $P_{01}(1831), P_{13}(1811), D_{03}(1788), D_{15}(2074)$   
(Hyslop et al 1992)
- $K^*N$  resonance around 1830 MeV  
(Aaron et al 1970)
- $S_{01}(1710)$  (Roiesnol 1979)
- 1530, 1570 (notice this second is at the  $K\pi N$  threshold)

### $\kappa$ phase shift



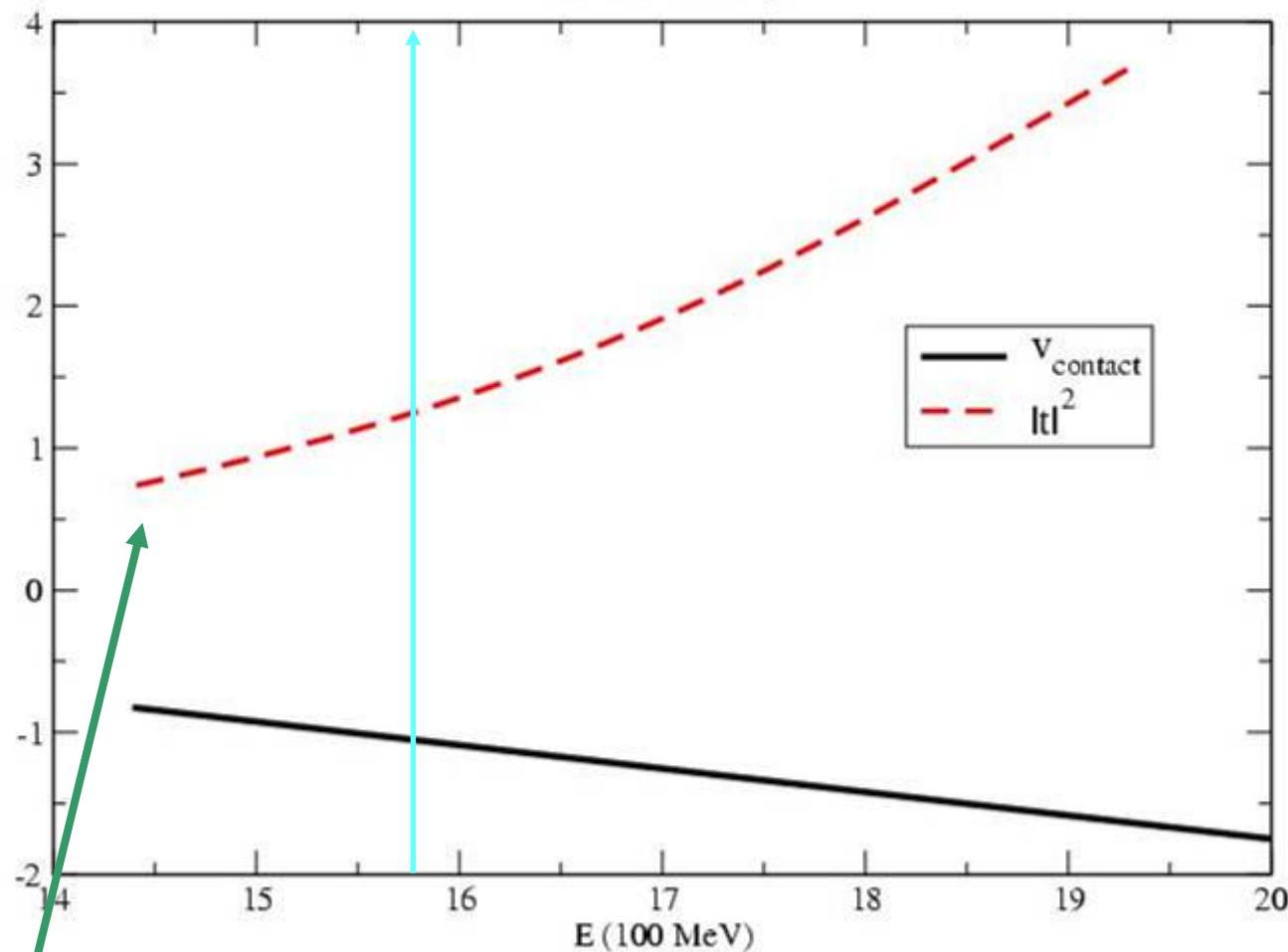
$\text{Re}(G_{\text{mb}})$

$K\pi N$  scattering cutoff  $\Lambda=1 \text{ GeV}$



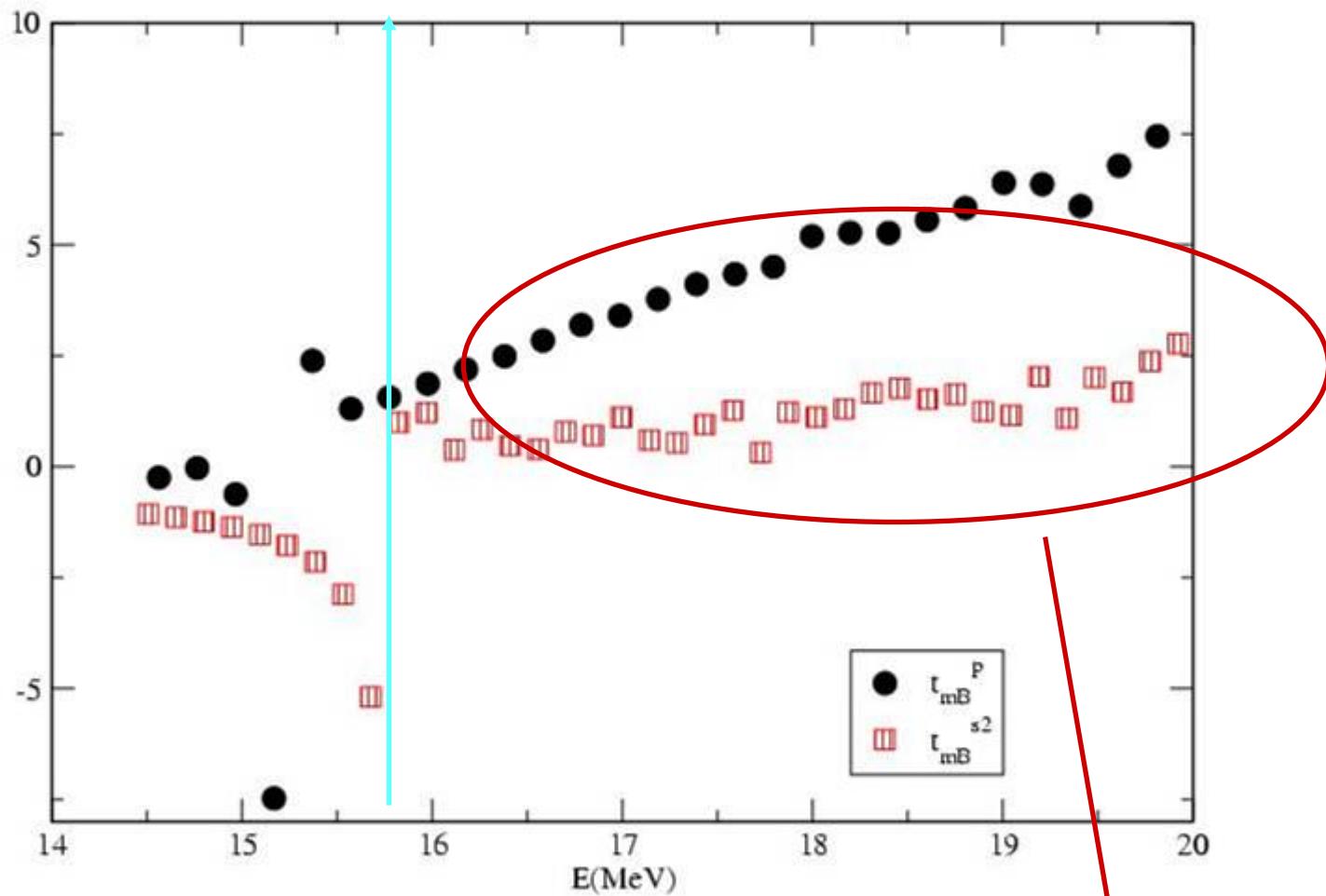
# $K\pi N$ scattering

Contact term only



Contact term only: no resonance

## s and p non-contact potentials



Non-contact terms clearly positive  
Above threshold: no resonance expected

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—
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# Antidecuplet members (inspired by Diakonov, Petrov, Polyakov)

$\Theta(1540)$

Solutions two-meson cluster

$N(1710)$

Mass splitting of baryon states

$\Sigma(1890)$

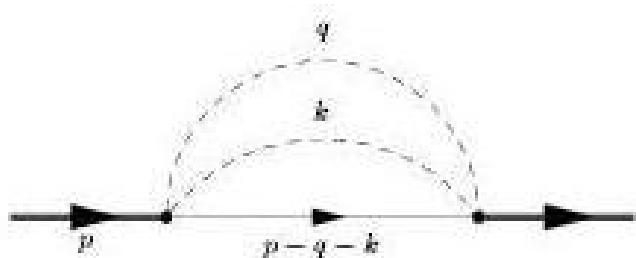
New seen in recent  $N\pi$

$\Xi(2060)$

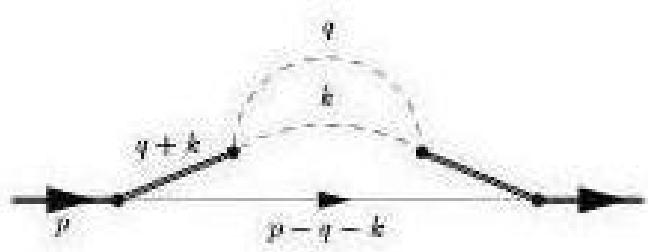
$\Theta(1540) > \Theta$  Karisow

(St. Hoksakay et al., Nucl. Phys. O)

# Decays of $N^*(1710)$



Scalar vertices  
 $N\pi\pi$  s-wave  
 $\Gamma=25$  MeV from PD



Vector: intermediate  
 $\rho$  or  $K^*$  resonance  
 $N\pi\pi$  p-wave  
 $\Gamma=15$  MeV

$$\phi = \begin{pmatrix} \frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & \pi^+ & K^+ \\ \pi^- & -\frac{1}{\sqrt{2}}\pi^0 + \frac{1}{\sqrt{6}}\eta & K^0 \\ K^- & \bar{K}^0 & -\frac{2}{\sqrt{6}}\eta \end{pmatrix}$$

$$B = \begin{pmatrix} \frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & \Sigma^+ & p \\ \Sigma^- & -\frac{1}{\sqrt{2}}\Sigma^0 + \frac{1}{\sqrt{6}}\Lambda & n \\ \Xi^- & \Xi^0 & -\frac{2}{\sqrt{6}}\Lambda \end{pmatrix}$$

SU(3)  
field defns.  
8x8x10

$$P^{333} = \sqrt{6}\Theta_{\frac{1}{10}}^+, P^{133} = \sqrt{2}N_{\frac{1}{10}}^0,$$

$$P^{233} = -\sqrt{2}N_{\frac{1}{10}}^+, P^{113} = \sqrt{2}\Sigma_{\frac{1}{10}}^-,$$

$$P^{123} = -\Sigma_{\frac{1}{10}}^0, P^{223} = -\sqrt{2}\Sigma_{\frac{1}{10}}^+, \quad (1)$$

$$P^{111} = \sqrt{6}\Xi_{\frac{1}{10}}^{--}, P^{112} = -\sqrt{2}\Xi_{\frac{1}{10}}^-,$$

$$P^{122} = \sqrt{2}\Xi_{\frac{1}{10}}^0, P^{222} = -\sqrt{6}\Xi_{\frac{1}{10}}^+,$$

# Construction of effective lagrangian derivative expansion and respecting

$$\mathcal{L}^{8s} = \frac{g^{8s}}{2f} \bar{P}_{ijk} \epsilon^{lmk} \phi_l^a \phi_a^i B_m^j + \text{h.c.}$$

$$\begin{aligned} \mathcal{L}^{8a} = i \frac{g^{8a}}{4f^2} \bar{P}_{ijk} \epsilon^{lmk} \gamma^\mu (\partial_\mu \phi_l^a \phi_a^i - \phi_l^a \partial_\mu \phi_a^i) B_m^j \\ + \text{h.c.} \end{aligned}$$

$$\begin{aligned} \mathcal{L}^{27} = & \frac{g^{27}}{2f} [4 \bar{P}_{ijk} \epsilon^{lbk} \phi_l^i \phi_a^j B_b^a \\ & - \frac{4}{5} \bar{P}_{ijk} \epsilon^{lbk} \phi_l^a \phi_a^j B_b^i] + \text{h.c.} \end{aligned}$$

# What does chiral symmetry have to do with mass?

$$\mathcal{L}^{\chi} = \frac{g^{\chi}}{2f} \bar{P}_{ijk} \epsilon^{lmk} (A_{\mu})_l{}^a (A^{\mu})_a{}^i B_m{}^j + \text{h.c.}$$

Chirally sym.  
two derivatives

$$A_{\mu} = \frac{i}{2} (\xi^{\dagger} \partial_{\mu} \xi - \xi \partial_{\mu} \xi^{\dagger})$$

$$\xi = e^{i\phi/\sqrt{2}f}$$

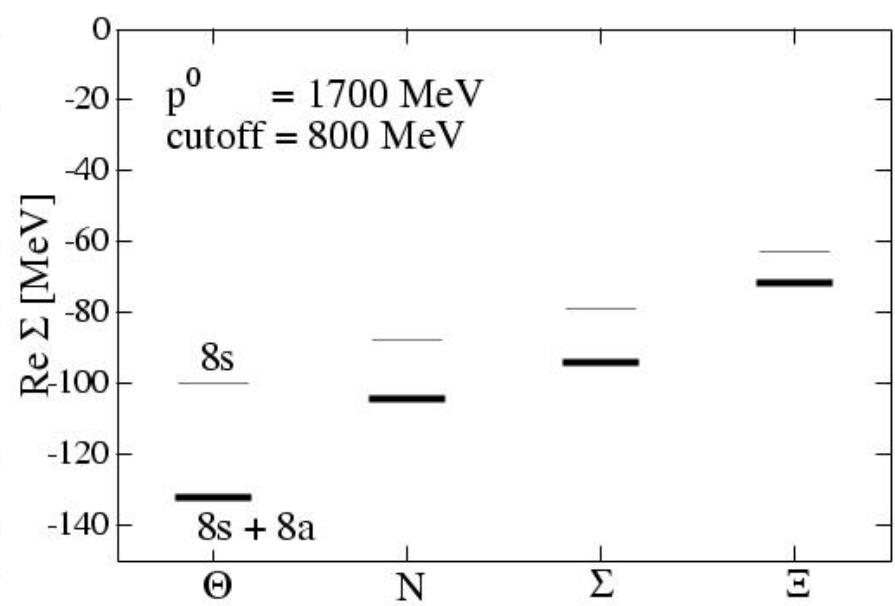
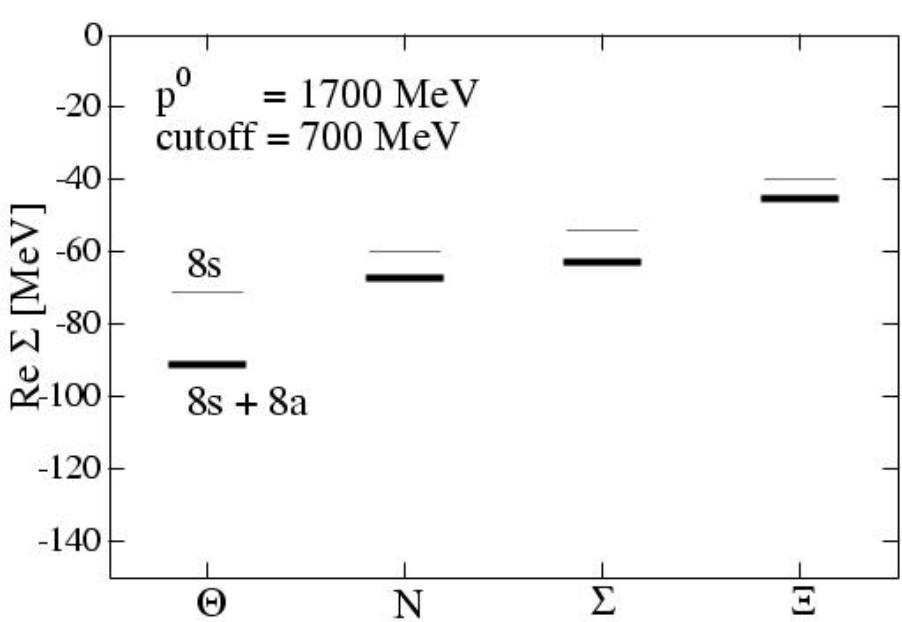
$$S = \xi M \xi + \xi^{\dagger} M \xi^{\dagger}$$

$$M = \begin{pmatrix} m_{\pi}^2 & & \\ & m_{\pi}^2 & \\ & & 2m_K^2 - m_{\pi}^2 \end{pmatrix}$$

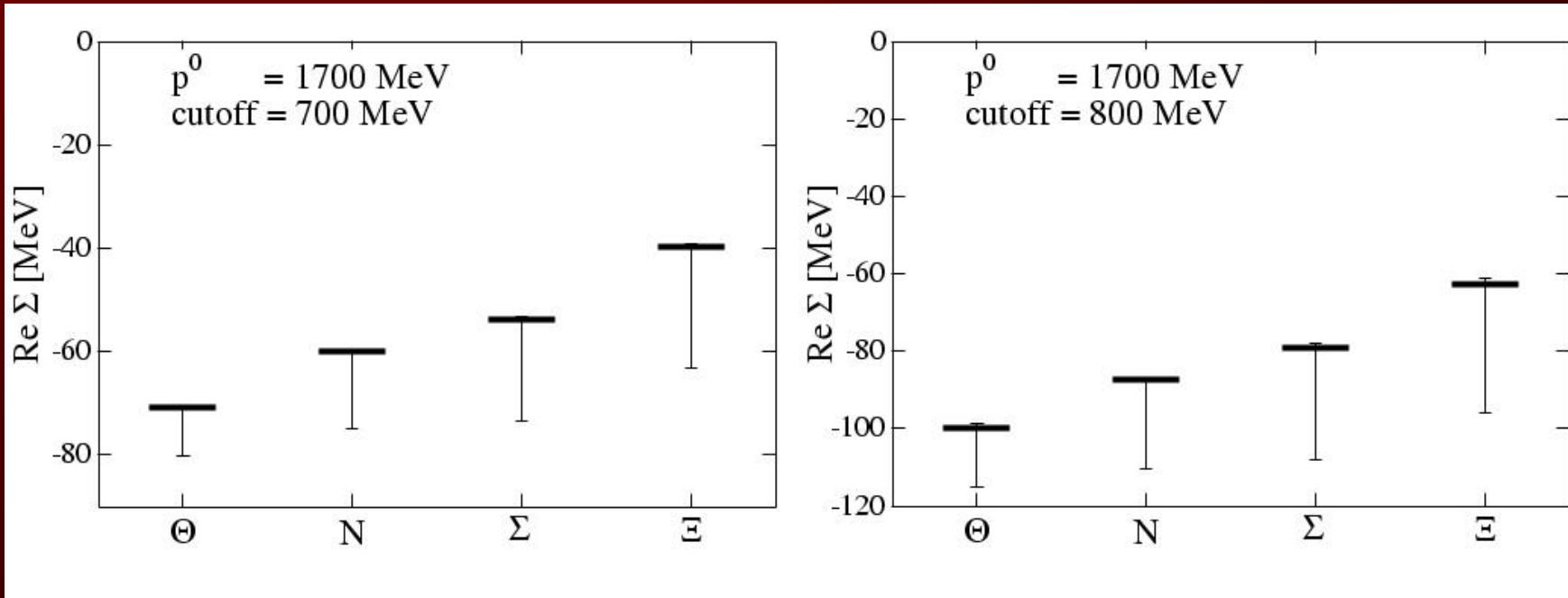
Mass terms  
break SU(3)  
directly

$$\mathcal{L}^M = \frac{g^M}{2f} \bar{P}_{ijk} \epsilon^{lmk} S_l{}^i B_m{}^j + \text{h.c.}$$

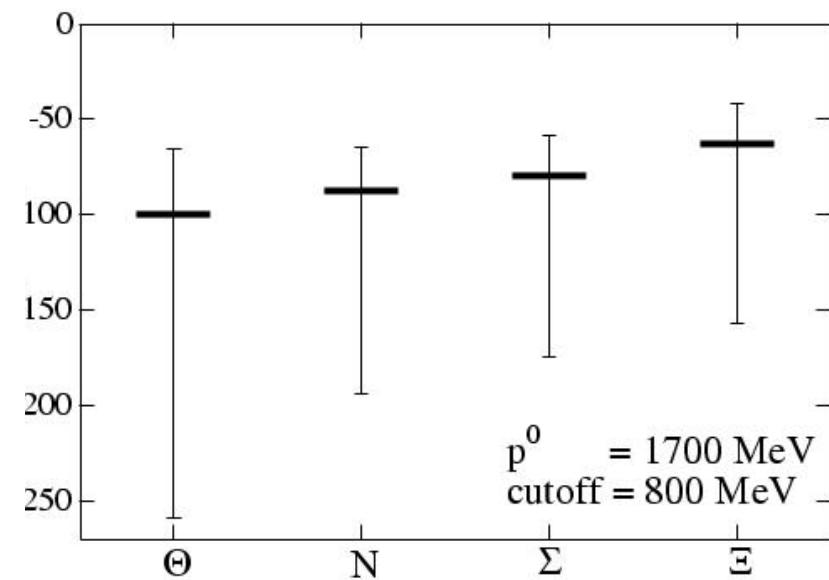
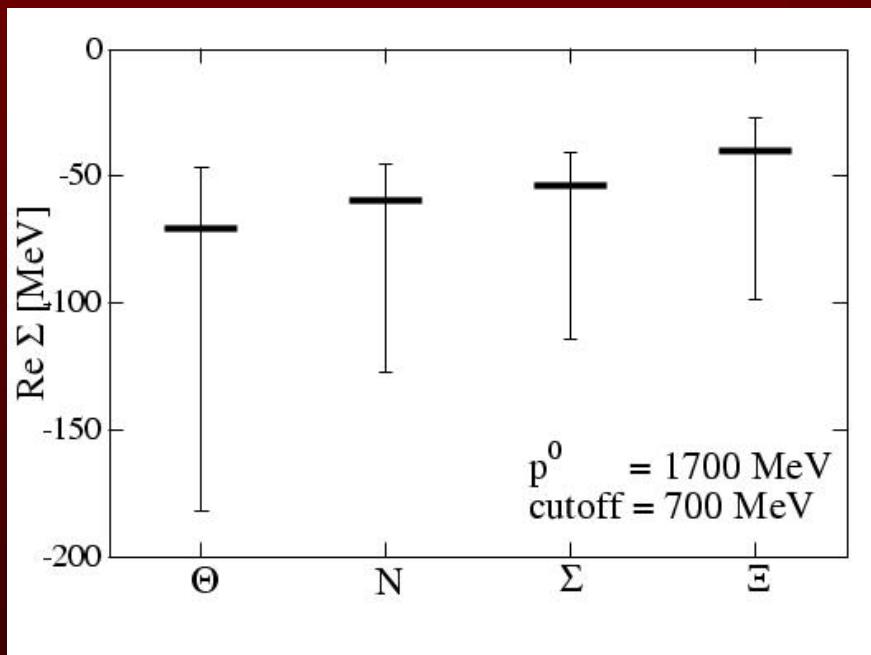
$$\mathcal{L}_s^8 + \mathcal{L}_a^8$$



# $L_s^8 + L^{27}$



$$\mathcal{L}_s^8 + \mathcal{L}^M$$



# Three body decays of pentaquark p

Decay widths [MeV]	$\Gamma^{(8s)}$	$\Gamma(\chi)$
$N(1710) \rightarrow N\pi\pi$ (input)	25	25
$N(1710) \rightarrow N\eta\pi$	0.58	0.32
$\Sigma(1770) \rightarrow N\bar{K}\pi$	4.7	4.5
$\Sigma(1770) \rightarrow \Sigma\pi\pi$	10	3.6
$\Xi(1860) \rightarrow \Sigma\bar{K}\pi$	0.57	0.40

# Three body decays of pentaquark p

Decay	$\Gamma$ (MeV)	$\Gamma^{(8s)}$	$\Gamma^{(8a)}$	$\Gamma_{BMM}^{tot}$
$N(1710) \rightarrow N\pi\pi$	25	15	40	
$N(1710) \rightarrow N\eta\pi$	0.58	-		
$\Sigma(1770) \rightarrow N\bar{K}\pi$	4.7	6.0	24	
$\Sigma(1770) \rightarrow \Sigma\pi\pi$	10		0.62	
$\Sigma(1770) \rightarrow \Lambda\pi\pi$	-		2.9	
$\Xi(1860) \rightarrow \Sigma\bar{K}\pi$	0.57	0.46	2.1	
$\Xi(1860) \rightarrow \Xi\pi\pi$	-		1.1	

# Two meson cloud of the baryon antidecuplet

Thanks to my collaborators A. Hosaka, T.  
. Hyodo, M. Vicente-Vacas, V. Mateu,  
E. Oset, J. Pelaez

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# QNP06

## IVth International Conference on Quarks and Nuclear Physics

Madrid, June 5th-10th 2006

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