

University of
Ljubljana

Search for Θ^+ pentaquark at Belle



hep-ex/0507014
submitted to PLB

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Belle Collaboration

- KEKB and Belle detector
- Inclusive production of Θ^+
- Exclusive production of Θ^+

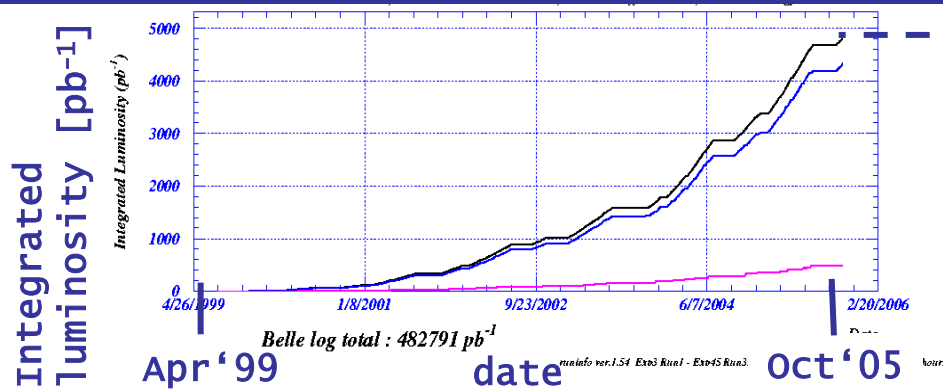
KEKB

KEKB: asymmetric
B factory



$$p(e^+) = 3.5 \text{ GeV}/c$$

$$p(e^-) = 8.0 \text{ GeV}/c$$



$$\int L dt = 480 \text{ fb}^{-1}$$

$$L_{\text{peak}} = 1.58 \times 10^{34} \text{ s}^{-1} \text{ cm}^{-2}$$

Presented analysis:
 $\int L dt = 357 \text{ fb}^{-1}$

Belle detector



3(4) layer
Si det.

e^-
8 GeV

Central Drift
Chamber

e^+
3.5 GeV

Aerogel
Cherenkov
($n=1.015-1.030$)

μ and K_L
Counter
(14/15 layers
RPC+Fe)

EM calorimeter
CsI ($16X_0$)

1.5T SC
solenoid

$$\sigma(p_t)/p_t = 0.3\% \sqrt{p_t^2 + 1}$$

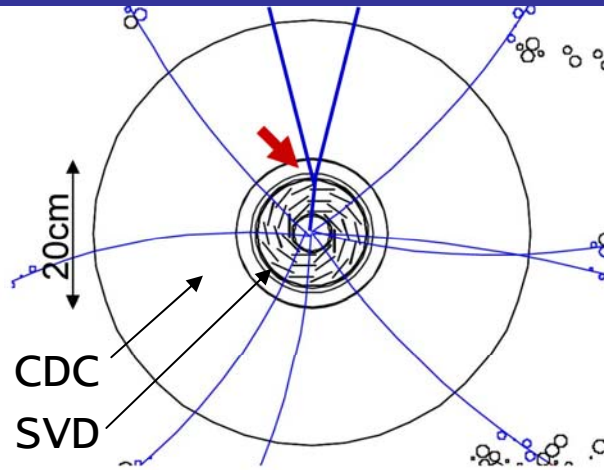
Particle ID

$$\varepsilon(K^\pm) \sim 85\%$$

$$\varepsilon(\pi^\pm \rightarrow K^\pm) < \sim 10\%$$

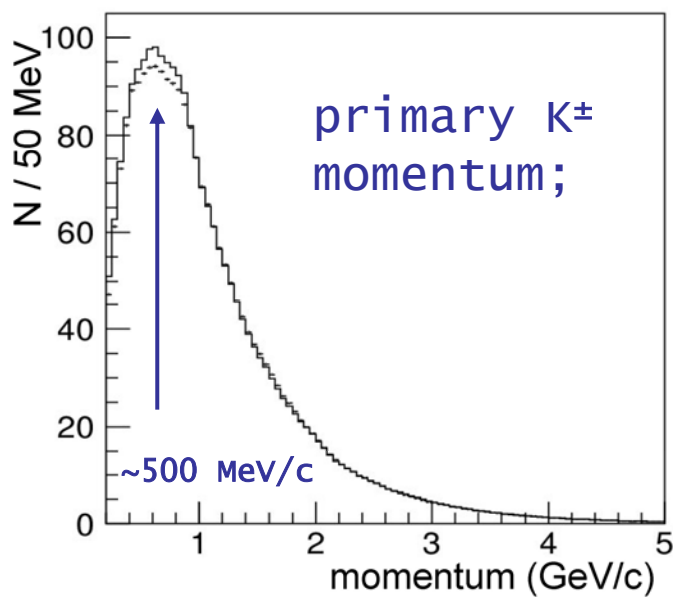
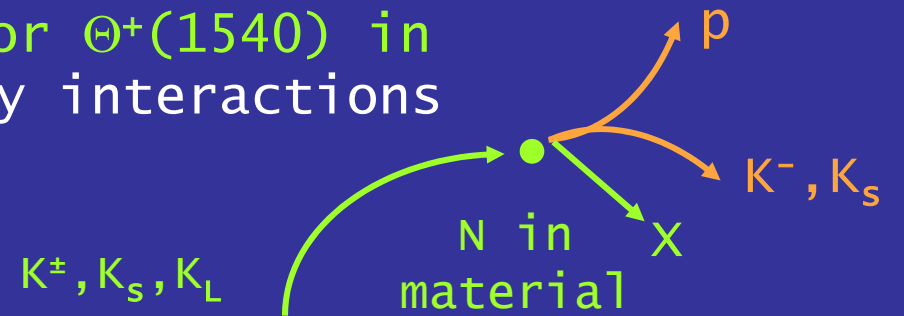
$$@ p < 3.5 \text{ GeV}/c$$

Measurement method



schematic view

- kaons produced in e^+e^- annihilation as projectiles
- search for $\Theta^+(1540)$ in secondary interactions



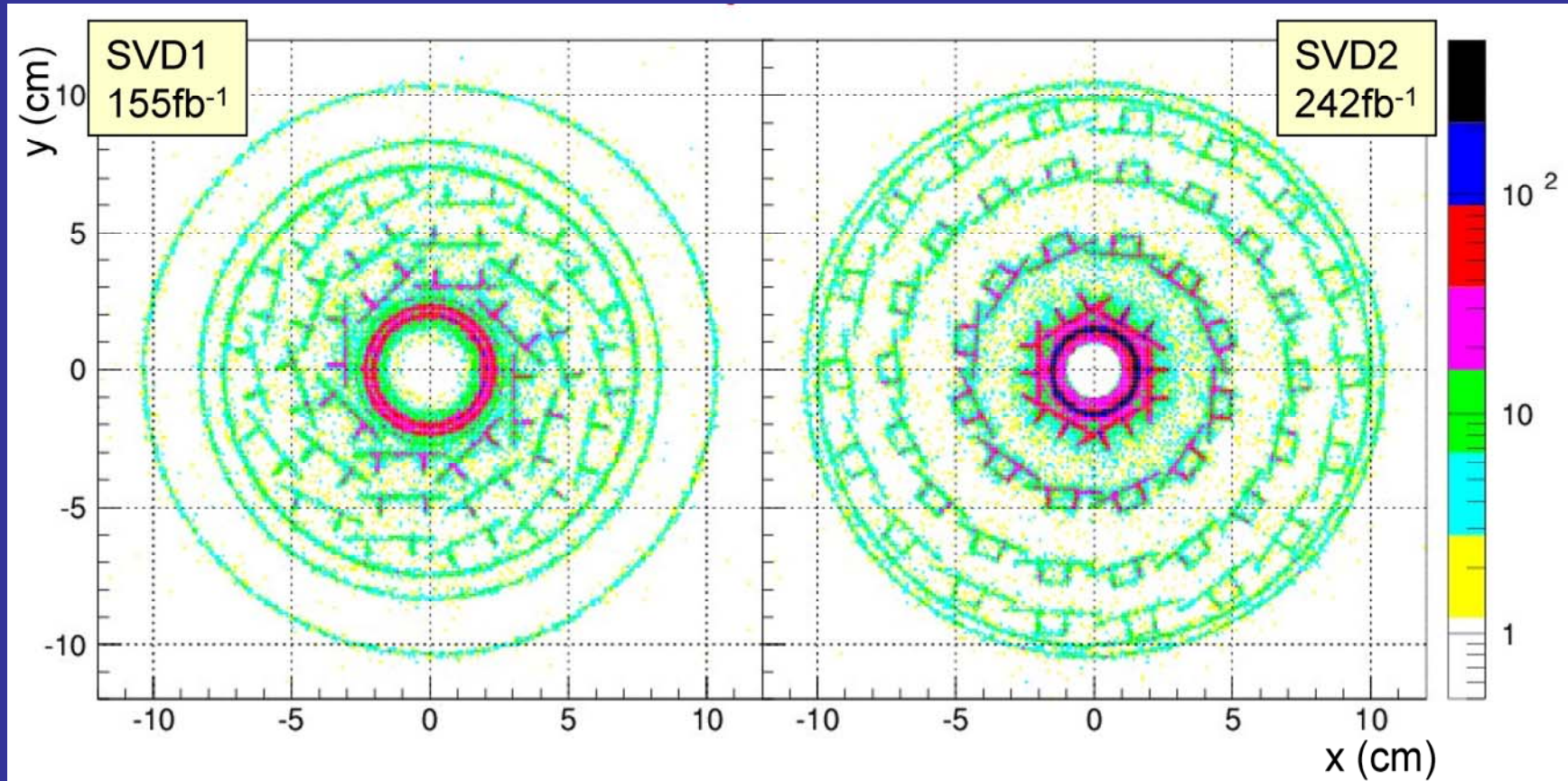
$\begin{pmatrix} - \\ K^0 \end{pmatrix}$	K^\pm	p	n	K^-	K_S
$d\bar{s}$	$u\bar{s}$	uud	udd	$u\bar{s}$	$d\bar{s}$
$\bar{d}s$	$\bar{u}s$				

selection:

- identified p, K^\pm ; not from IP ($\delta r > 0.1$ cm);
- $K_S \rightarrow \pi^+\pi^-$; detached vtx, not from IP ($\delta r > 0.1$ cm), 3σ within $m(K_S)$
- pK detached vtx ($1 \text{ cm} < r < 11 \text{ cm}$);

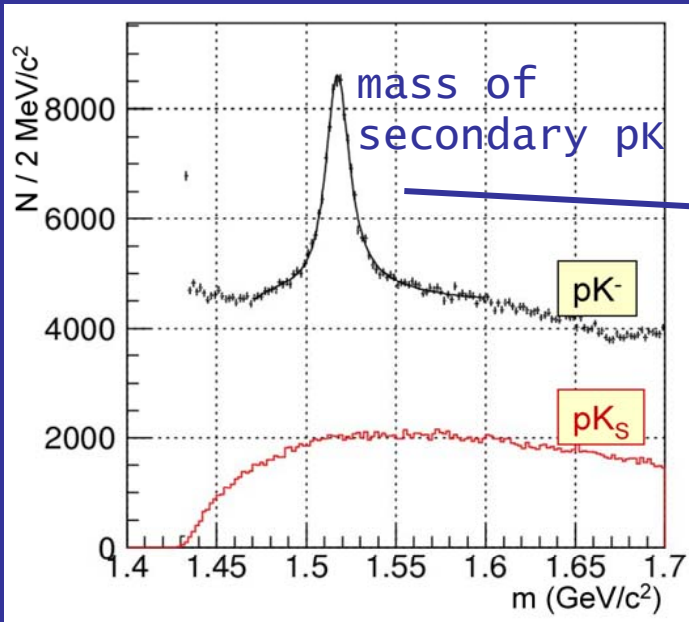
Measurement method

(x, y) coord. of pK_s secondary vertices =>
detector “tomography”



pK pairs arising from interactions with nucleons
in detector material

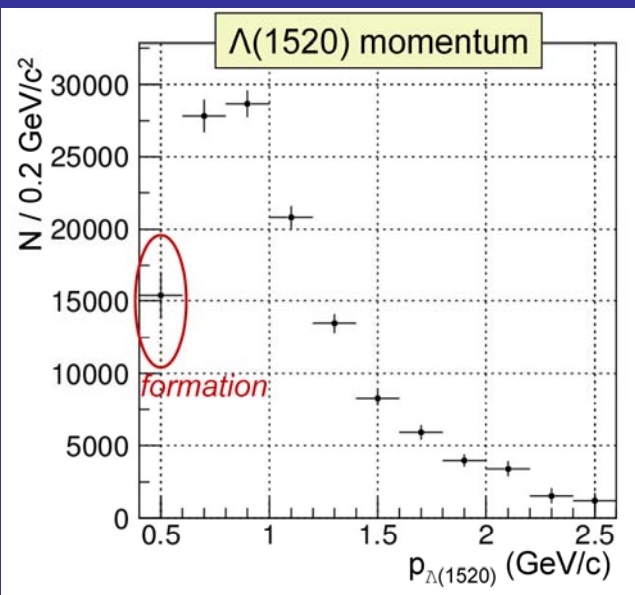
Inclusive production of Θ^+



inclusive \equiv analysis of $m(pK^-)$ and $m(pK_s)$;
 no suppression of inelastic reactions,
 no estimate of charge exchange $K^+n \rightarrow pK_s$

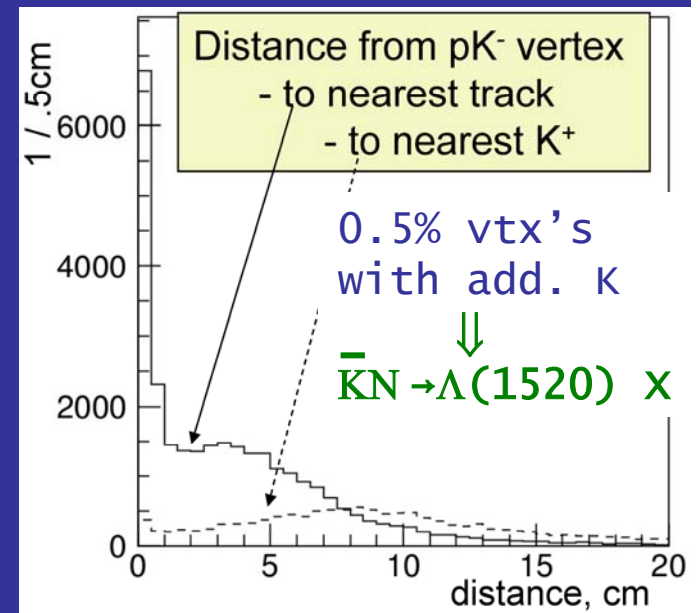
fit to threshold func.+
 D-wave BW \oplus resolution func.

$(4.02 \pm 0.08) \times 10^4 \Lambda(1520) (\pm 2.5 \Gamma)$
 Γ and m consistent with PDG



$pK \rightarrow \Lambda(1520) \rightarrow pK$
 formation,
 $p(\Lambda) \sim 400 \text{ MeV}/c$

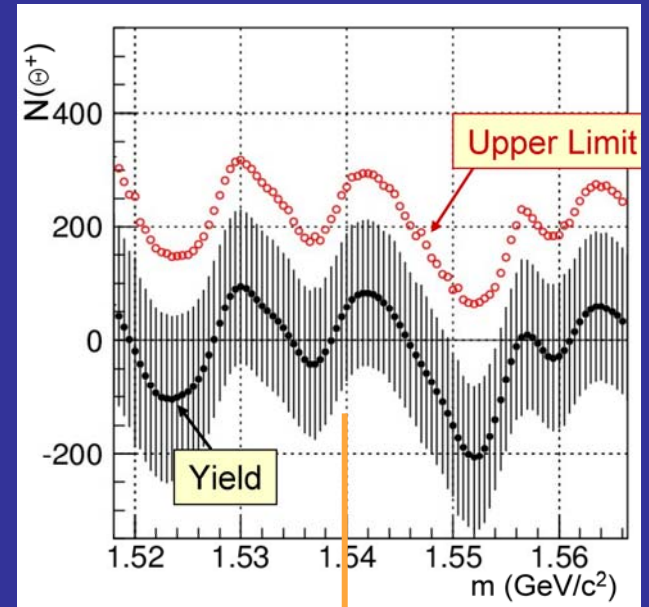
$pK \rightarrow \Lambda(1520) \times$
 $\quad \quad \quad \hookrightarrow pK$
 production



Inclusive production of Θ^+

fit $m(pK_s)$ to Gaussian
+ 3rd order polynomial

$\sigma \sim 2 \text{ MeV}/c^2$ from
MC + small corr.
from $\Omega^- \rightarrow \Lambda K^-$



$$\frac{\sigma(KN \rightarrow \Theta(1540)^+ X)}{\sigma(\bar{K}N \rightarrow \Lambda(1520)X)} = \frac{N_{\Theta^+} \varepsilon_{pK^-} B(\Lambda^* \rightarrow pK^-)}{N_{\Lambda^*} \varepsilon_{pK_s} B(\Theta^+ \rightarrow pK^0) B(K^0 \rightarrow K_s \rightarrow \pi^+ \pi^-)}$$

< 2.5% @ 90% C.L.

assuming $B(\Theta^+ \rightarrow pK_s) = 25\%$;
using $B(\Lambda^* \rightarrow pK^-) =$
 $\frac{1}{2} B(\Lambda^* \rightarrow NK) = \frac{1}{2} (45 \pm 1)\%$;
 ε 's from MC;

Exp.	process	E [GeV]	$\sigma(\Theta^+) / \sigma(\Lambda^*)$
CDF	$pp \rightarrow \Theta^+ X$	1960	<3%
HERA-B	$pA \rightarrow \Theta^+ X$	42	<2%
SPHINX	$pA \rightarrow \Theta^+ X$	12	<2%
Belle	$KA \rightarrow \Theta^+ X$	~ 2	<2.5%
LEPS	$\gamma A \rightarrow \Theta^+ X$	~ 2	$\sim 60\%$
HERMES	$eD \rightarrow \Theta^+ X$	7	$\sim 200\%$

Exclusive production of Θ^+

exclusive \equiv search for $K^+n \rightarrow \Theta^+ \rightarrow pK_s$

motivated by DIANA result
Phys.Atom.Nucl. 66, 1715 (2003)

main steps

- suppression of inelastic reactions
(additional π^0 or unrec. π^+
major bkg.; also contributions from
 $K_{s,L}p \rightarrow pK_s$)

- normalize to charge exchange $K^+n \rightarrow pK_s$ (N^{ch})

- N^{ch} indirectly from elastic $K^+p \rightarrow K^+p$ (N^{el})

- interpretation $N_{\Theta^+}/N^{\text{ch}} \Leftrightarrow \Gamma_{\Theta^+}$
Cahn, Trilling, PRD69, 11501 (2004)

$$N_{\Theta^+}/N^{\text{ch}} = 0.66 \pm 0.19$$

$$\Gamma_{\Theta^+} = 0.9 \pm 0.3 \text{ MeV}$$

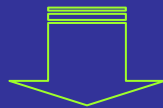
Exclusive production of Θ^+

number of charge exchange events:

$$N^{ch} = \int \underbrace{\Phi^{K^+}(p_{K^+}, \theta)}_{K^+ \text{ flux}} \underbrace{\sigma^{ch}(m_{pK_s})}_{x\text{-sect.}} \underbrace{M(R, \theta)}_{\text{material}} \underbrace{\varepsilon_{pK_s}(m_{pK_s}, p_{pK_s}, R, \mathcal{D})}_{\text{reconstr. efficiency}} dR d\theta$$

$$\underbrace{P(m_{pK_s}, p_{pK_s})}_{\text{no-rescattering prob.}} \underbrace{S(E_N, p_F)}_{\text{nuclear spectral func.}} \delta(\sqrt{s} - m_{pK_s}) dE_N d^3 p_F dp_{K^+} B$$

MC may not reproduce M and ε accurately enough;
 P and S model dependent;



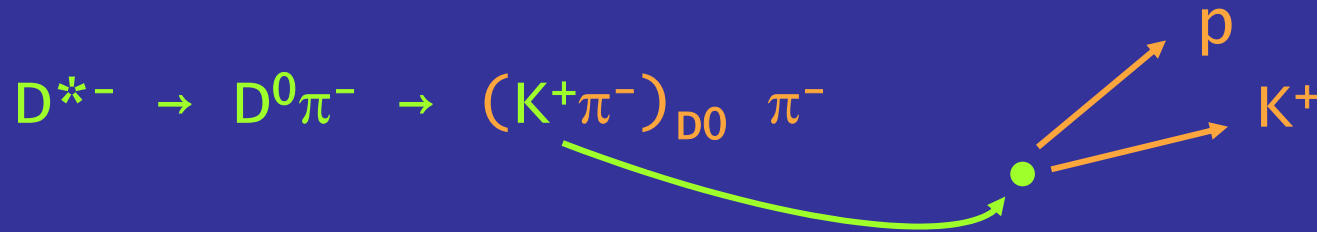
use data and estimate N^{ch} relative to N^{el}

$K^+n \rightarrow pK_s$

$K^+p \rightarrow K^+p$

Exclusive production of Θ^+

process enabling a “counting” of $K^+p \rightarrow pK^+$:



$$N_{D^*}^{el} = \int \Phi_{D^*}^{K^+}(p_{K^+}, \theta) \sigma^{el}(m_{pK^+}) M(R, \theta) \varepsilon_{pK^+}(m_{pK^+}, p_{pK^+}, R, \mathcal{J}) dR d\theta$$

$$P(m_{pK^+}, p_{pK^+}) S(E_N, p_F) \delta(\sqrt{s} - m_{pK^+}) dE_N d^3 p_F dp_{K^+}$$

ratio N^{ch}/N^{el}

$$N^{ch} = N_{D^*}^{el} \frac{\Phi^{K^+}(m_{pK}) \sigma^{ch}(m_{pK}) \varepsilon_{pKs}(m_{pK}) B}{\Phi_{D^*}^{K^+}(m_{pK}) \sigma^{el}(m_{pK}) \varepsilon_{pK^+}(m_{pK})}$$

Material and nuclear effects mostly cancel out

Exclusive production of Θ^+

reconstruction:



relations:

- $$\underbrace{E_N}_{\text{wavy}} = m_N - 2\varepsilon - \underbrace{p_F^2}_{\text{wavy}} / 2m_N$$

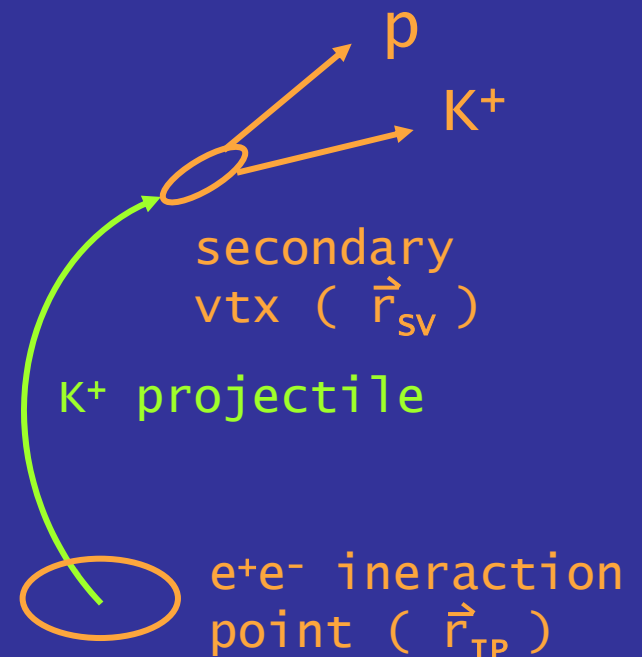
$\varepsilon \sim 7 \text{ MeV}$; Sibirtsev et al., EPJ A23, 491(2005)

- $$\underbrace{E_K}_{\text{wavy}} = E_{pK} - \underbrace{E_N}_{\text{wavy}}$$

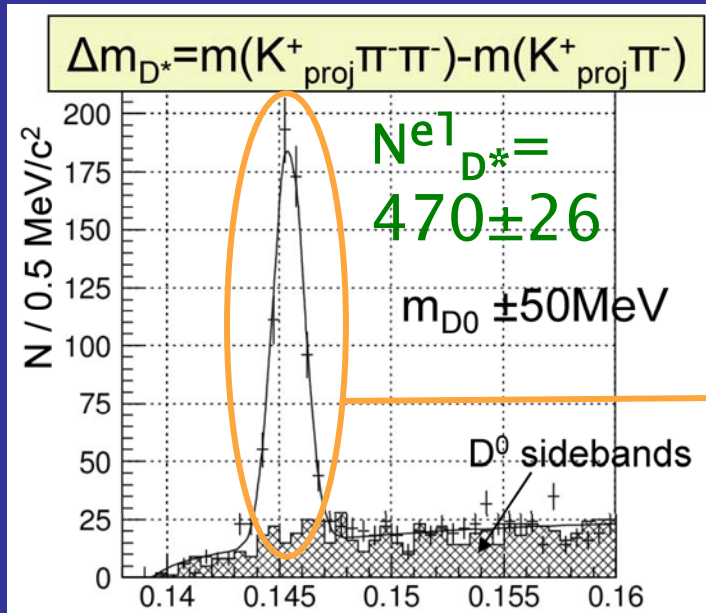
- $$\underbrace{\vec{p}_K}_{\text{wavy}} = \underbrace{f}_{\text{wavy}}(E_K, \vec{r}_{SV}, \vec{r}_{IP})$$

- $$\underbrace{\vec{p}_F}_{\text{wavy}} = \vec{p}_{pK} - \underbrace{\vec{p}_K}_{\text{wavy}}$$

solve iteratively for \vec{p}_K , \vec{p}_F



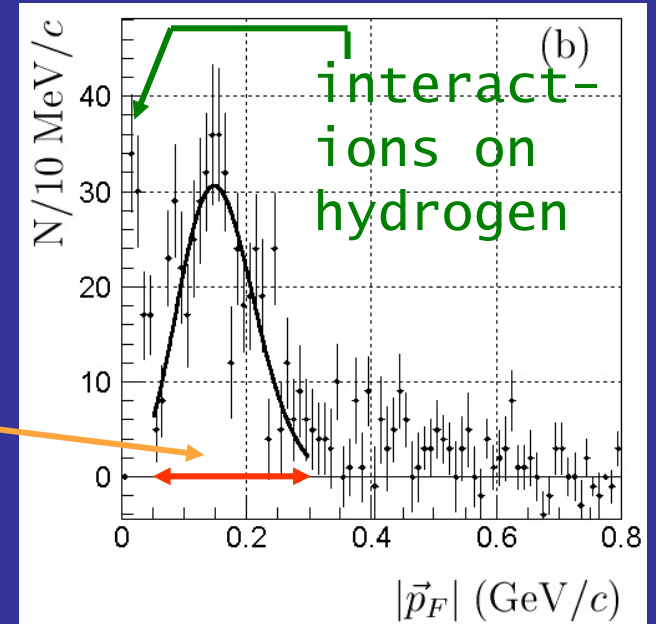
Exclusive production of Θ^+



p_F for elastic events (D^0), bkg. subtracted

selected (enhanced elastic reactions)

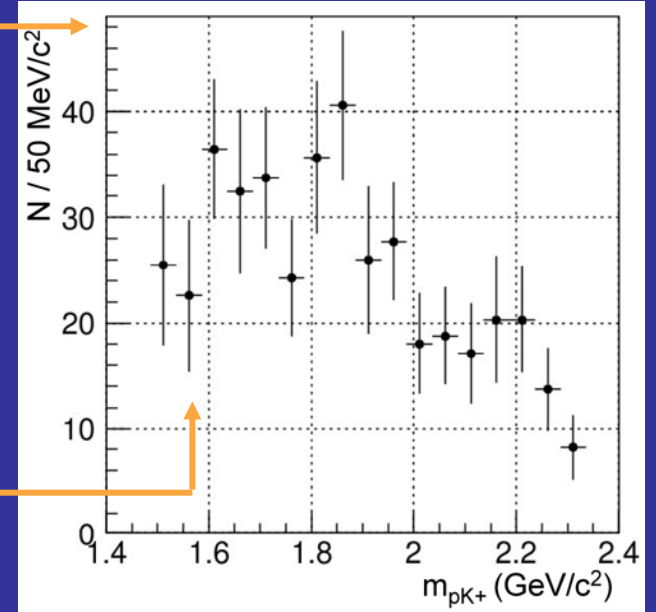
in bins of $m(pK^+)$



Δm_{D^*} from secondary pK^+ pairs combined with additional pions

$$N^{ch} = N^{el}_{D^*} \frac{\Phi^{K^+} \sigma^{ch} \varepsilon_{pKs} B}{\Phi^{K^+}_{D^*} \sigma^{el} \varepsilon_{pK^+}}$$

$$N^{el}_{D^*} = 21 \pm 7 \text{ (}\Theta^+ \text{ mass)}$$

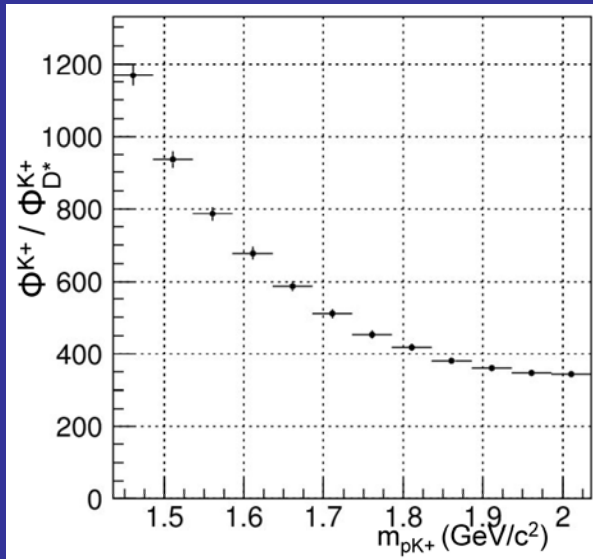


Exclusive production of Θ^+

$$N_{D^*}^{el} \frac{\Phi^{K^+} \sigma^{ch} \varepsilon_{pKs} B}{\Phi_{D^*}^{K^+} \sigma^{el} \varepsilon_{pK^+}}$$

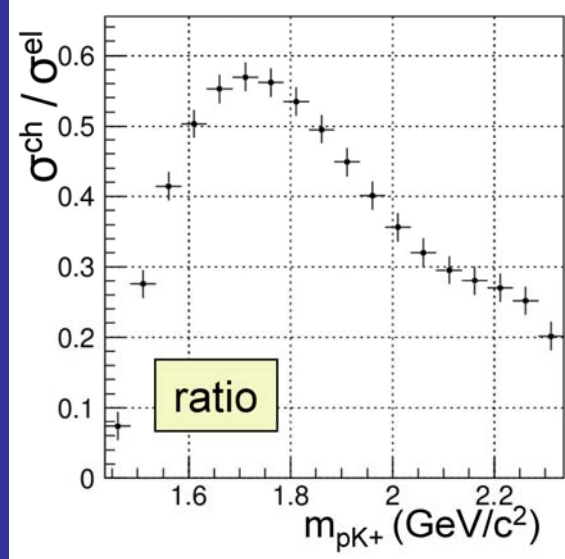
$$N_{D^*}^{el} \frac{\Phi^{K^+} \sigma^{ch} \varepsilon_{pKs} B}{\Phi_{D^*}^{K^+} \sigma^{el} \varepsilon_{pK^+}}$$

$$N_{D^*}^{el} \frac{\Phi^{K^+} \sigma^{ch} \varepsilon_{pKs} B}{\Phi_{D^*}^{K^+} \sigma^{el} \varepsilon_{pK^+}}$$



from ~20% of data
uniform over
running period

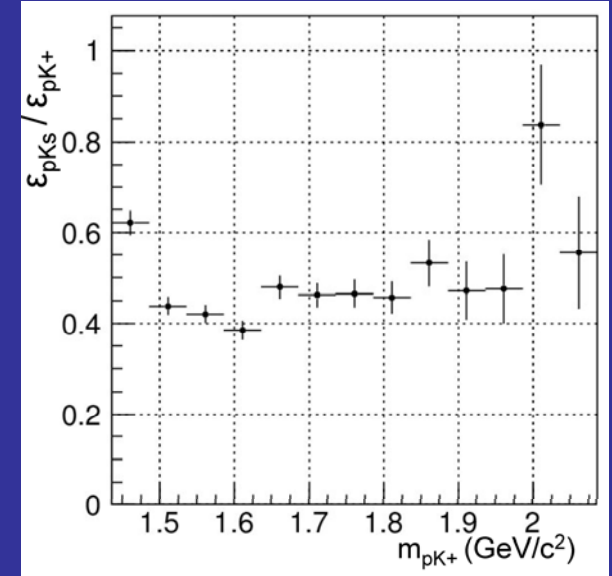
$$\Phi^{K^+} / \Phi_{D^*}^{K^+} = 850 \pm 20$$



from fit to published
data; typical single
experiment uncertainty

$$\sigma^{ch} / \sigma^{el} = 0.35 \pm 0.02$$

(Θ^+ mass)

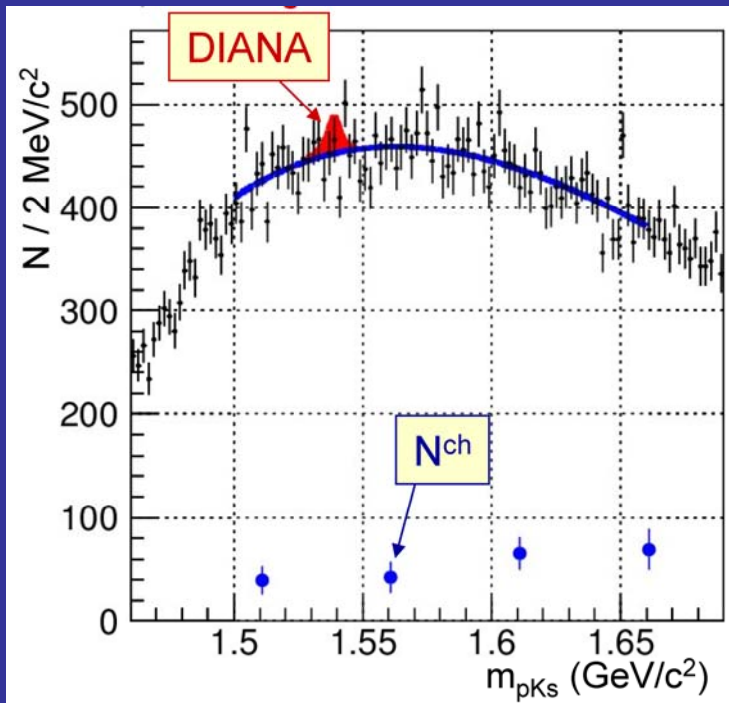


from MC

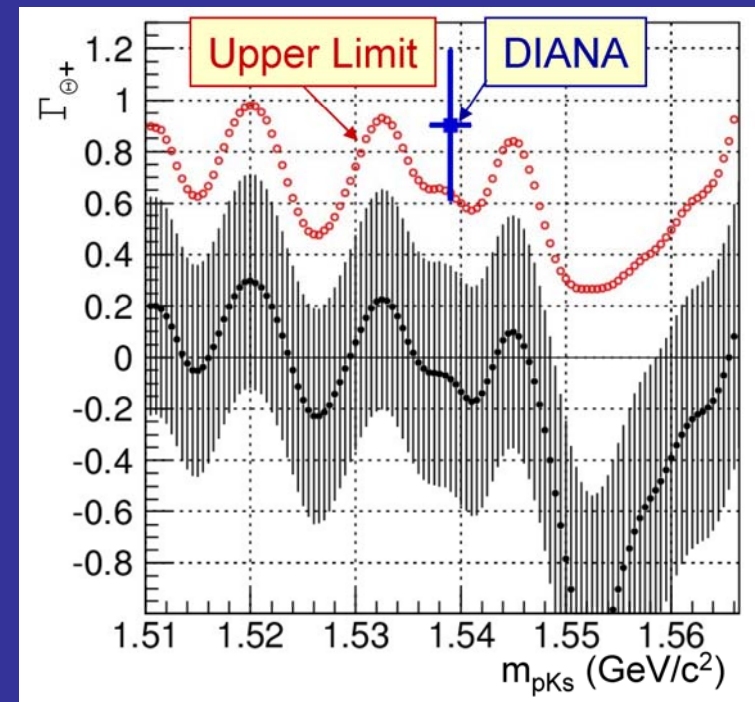
$$\varepsilon_{pKs} / \varepsilon_{pK^+} = 0.43 \pm 0.05$$

Exclusive production of Θ^+

Fit $m(pK_s)$ for possible Θ^+ signal



yield at various $m(pK_s)$ and UL



- no vtx's with additional tracks
- $50 \text{ MeV}/c < p_F < 300 \text{ MeV}/c$
- 3rd order polynom.+signal ($\sigma=2 \text{ MeV}/c^2$)

similar sensitivity as DIANA

DIANA:

$$\Gamma_{\Theta^+} = 0.9 \pm 0.3 \text{ MeV}$$

$$\Gamma_{\Theta^+} < 0.64 \text{ MeV @ 90\% C.L.}$$

Summary

- $\Theta(1540)^+$ signal searched for using kaon secondary interactions
- similar CM energy as in some positive result exp's
- inclusive search
 $\sigma(\text{KN} \rightarrow \Theta(1540)^+X) / \sigma(\bar{\text{K}}\text{N} \rightarrow \Lambda(1520)X) < 2.5\%$ @90% C.L.
- exclusive search
- $\text{K}^+ n \rightarrow \Theta(1540)^+ \rightarrow p \text{K}_s$ yield normalized to total charge exchange $\text{K}^+ n \rightarrow p \text{K}_s$
- similar sensitivity to DIANA exp.
- $\Gamma_{\Theta^+} < 0.64 \text{ MeV}$ @90% C.L. for $m(\Theta^+) = 1540 \text{ MeV}/c^2$
- $\Gamma_{\Theta^+} < 1 \text{ MeV}$ @90% C.L. for $m(\Theta^+) \leq 1570 \text{ MeV}/c^2$

selection details, backup

PID

- p: $L_{p/K} > 0.6$, $L_{p/\pi} > 0.6$
- K^\pm : $L_{K/p} > 0.6$, $L_{K/\pi} > 0.6$
- not identified as e^\pm
- L : likelihood based on CDC, ACC, TOF

K_S

- $\pi^+\pi^- \pm 10$ MeV (3σ) from $m(K_S)$
- z_{dist} at vtx < 1 cm
- δr of daughters > 0.1 cm
- $\theta(p(K_S), r(\text{vtx}, \text{IP})) < 90^\circ$

typical resolution
on sec. vtx
 $\sim 400 \mu\text{m}$ (r)

pK vtx

- $\delta r(p, K^\pm) > 0.1$ cm
- z_{dist} at vtx < 1 cm
- $\theta(p(pK), r(\text{vtx}, \text{IP})) < 90^\circ$

angular cuts (DIANA)
do not improve
S/N or sensitivity
after the p_F selection
applied (suppression
of 1.2, $\epsilon=93\% \Rightarrow$
significance ~ 1.02)

other

- $50 \text{ MeV}/c < p_F < 300 \text{ MeV}/c$
- $d/R > 0.1$ (d – dist. to nearest track,
R – radial coordinate of vtx)

Λ projectiles, backup

Formation:

$$p^2 = \frac{(m_\Lambda^2 - m_p^2 - m_K^2)^2}{4m_p^2} - m_K^2 \Rightarrow p \approx 400 \text{ MeV}/c$$

possible projectiles to produce $\Lambda(1520)$:

K^- , K_S , K_L , Λ (?)

$p(\Lambda) \geq 1.8 \text{ GeV}/c$ ($z \geq 0.35$) to produce $\Lambda(1520)$

@29 GeV fraction $\Lambda(z \geq 0.35) \sim 10\%$

$\sigma(e^+e^- \rightarrow \Lambda X) \sim 80 \text{ pb}$

$\sigma(e^+e^- \rightarrow K^0 X) \sim 470 \text{ pb}$

$\Rightarrow N(\Lambda)/N(K^0) \sim 2\%$

Tasso, PRD45, 3949 (1992)

$\sigma(K^-p \rightarrow \Lambda(1520)) \sim 3 \text{ mb}$, $\sigma(\Lambda p, \text{total}) \sim 30 \text{ mb}$

assuming equal prod. rate of K^0 , K^-

$\Rightarrow \Lambda p \rightarrow \Lambda(1520) X / K p \rightarrow \Lambda(1520) X \sim 10\%$

(if $\sigma(\Lambda p, \text{total})$ saturated by $\Lambda(1520)$)

Λ projectiles
contribute few %
to $\Lambda(1520)$
production

Fitted parameters

of $\Lambda(1520)$:

$m = 1518.5 \pm 0.1 \text{ MeV}/c^2$

$\Gamma = 13.5 \pm 0.4 \text{ MeV}$

PDG:

$m = 1519.5 \pm 1.0 \text{ MeV}/c^2$

$\Gamma = 15.6 \pm 1.0 \text{ MeV}$

Spectral function, backup

Energy of nucleon within a nuclei;

$$E_q = \sqrt{q^2 + m_N^2} - U(q, \rho)$$

$U(q, \rho)$ - nuclear potential

Fermi momentum ~ 300 MeV/c \Rightarrow

$$E_q \approx m_N + q^2/2m_N - U(q, \rho)$$


if $U \propto 1/r$, virial theorem, $U \sim -2 q^2/2m_N$

$$E_q \approx m_N - q^2/2m_N$$

checks:

use of $E_q \approx m_N - 2\varepsilon - q^2/2m_N$, with fixed ε
gives

- correct m_{D0}
- expected p_F distrib.



A. Sibirtsev et al.
EPJ A23, 491(2005)
Z.Phys. A358, 357(1997)

use of $E_q = m_N - E_R$

E_R (removal energy)

tuned to reproduce $m_{D0} \rightarrow E_R = 26$ MeV

$E_R = 2\varepsilon + q^2/2m_N$, nucleons with higher momenta
are more tightly bound

Θ^+ exclusive - integrals, backup

$$N^{ch} = \int \Phi^{K^+}(p_{K^+}, \theta) \sigma^{ch}(m_{pKs}) M(R, \theta) \varepsilon_{pKs}(m_{pKs}, p_{pKs}, R, \mathcal{D}) dR d\theta \\ P(m_{pKs}, p_{pKs}) S(E_N, p_F) \delta(\sqrt{s} - m_{pKs}) dE_N d^3 p_F dp_{K^+} B$$

all quantities depending only on $m(pK) \rightarrow$ factorize

- products $M\varepsilon$ approx. independent of $\theta \rightarrow$ decoupled from Φ
- fraction of recon. D^* in p_F hydrogen peak w.r.t. all \sim independent of $p(pK)$; since fraction $\propto 1/P \Rightarrow P \sim \neq F(p(pK))$

$$N^{ch} = \sigma^{ch}(m_{pKs}) \varepsilon_{pKs}(m_{pKs}) \overbrace{P(m_{pKs})}^{\text{cancels in the ratio}} \cdot \int \Phi^{K^+}(p_{K^+}) \varepsilon_{pKs}(p_{pKs}) S(E_N, p_F) \delta(\sqrt{s} - m_{pKs}) dE_N d^3 p_F dp_{K^+} B$$

cancels in the ratio

remaining eff. dependence on $p(pK)$ at given $m(pK)$

$S(E_N, p_F) = W(p_F) \delta(E_N - f(p_F));$
 $W(p_F)$ Fermi mom. distrib. (data);
 $f(p_F)$ defined so that
 $E_N = f(p_F) \Leftrightarrow \text{max. of } S(E_N, p_F)$

Θ^+ exclusive - integrals, backup

$$N^{ch} = \sigma^{ch}(m_{pKs}) \varepsilon_{pKs}(m_{pKs}) P(m_{pKs}).$$

$$\cdot \int \Phi^{K^+}(p_{K^+}, \theta) \varepsilon_{pKs}(p_{pKs}) W(p_F) \delta(E_N - f(p_F)) \delta(\sqrt{s} - m_{pKs}) dE_N d^3 p_F dp_{K^+} B$$

ratio N^{ch}/N^{el}

$$N^{ch} = N_{D^*}^{el} \frac{\Phi^{K^+}(m_{pK}) \sigma^{ch}(m_{pK}) \varepsilon_{pKs}(m_{pK}) B}{\Phi_{D^*}^{K^+}(m_{pK}) \sigma^{el}(m_{pK}) \varepsilon_{pK^+}(m_{pK})}$$

$$\frac{\Phi^{K^+}(m_{pK})}{\Phi_{D^*}^{K^+}(m_{pK})} = \frac{\int \Phi^{K^+}(p_{K^+}) \varepsilon_{pKs}(p_{pKs}) W(p_F) \delta(\sqrt{s} - m_{pKs}) d^3 p_F dp_{K^+}}{\int \Phi_{D^*}^{K^+}(p_{K^+}) \varepsilon_{pK^+}(p_{pK^+}) W(p_F) \delta(\sqrt{s} - m_{pKs}) d^3 p_F dp_{K^+}}$$

MC integration; p_F assumed isotropic w.r.t. p_K ;
 $\varepsilon(p(p_K)) \rightarrow 3\%$ corr. to the ratio;
 uncertainty dominated by assumed E_N , p_F relation

p_F distribution, backup

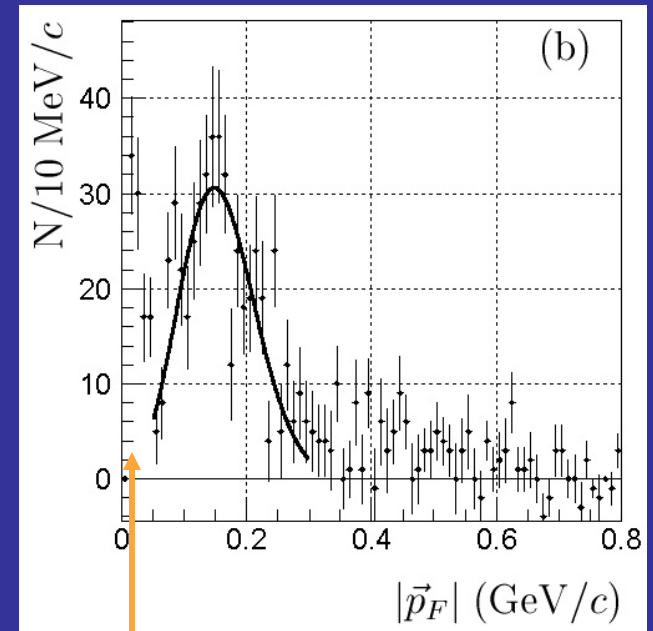
Fit to

$$p_F^2 \left[1 + \frac{4}{3} \left(\frac{p_F}{p_0} \right)^2 \right] \exp(-p_F^2 / p_0^2)$$

(oscillator model)

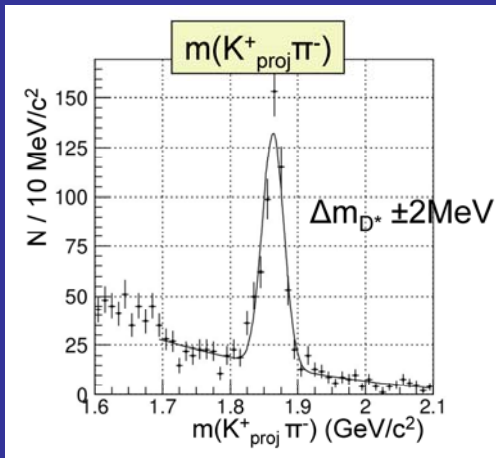
$$p_0 = 115 \pm 4 \text{ MeV}/c$$

comparable to other measurements of p_F ,
e.g. B.M. Abramov et al.,
JETP Lett. 71, 359(2000)



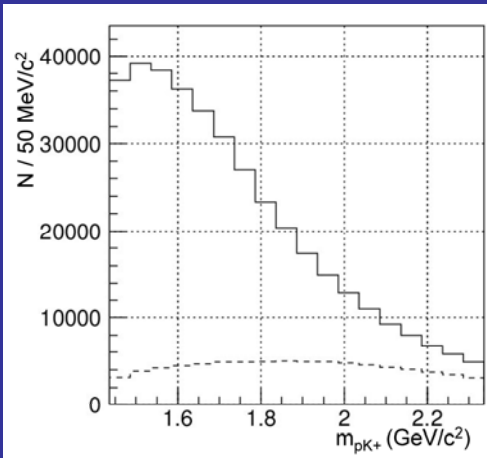
using $E_N = m_N \Rightarrow$
hydrogen peak exactly at 0

additional plots , backup



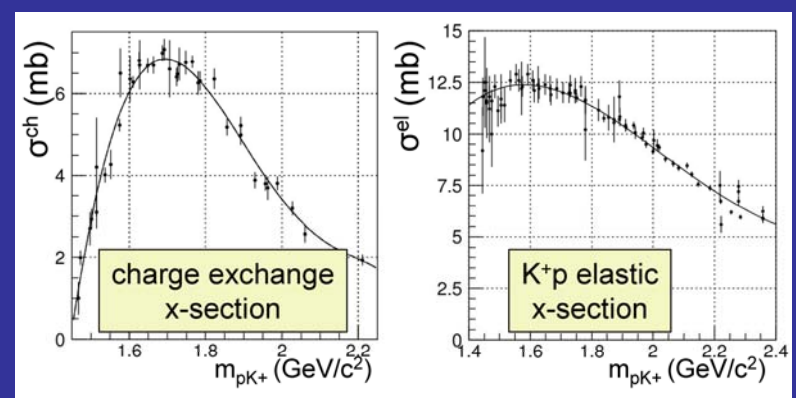
$$N_{D^*}^{el} = 470 \pm 26$$

$$\sigma = 16 \text{ MeV}/c^2$$



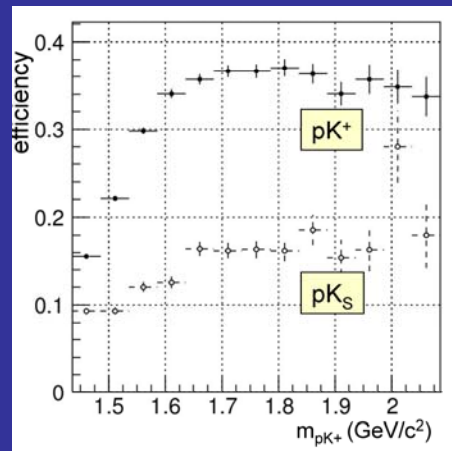
$$\Phi^{K^+} / \Phi^{K^+}_{D^*} = 850 \pm 20$$

major uncertainty from E_N , p_F relation



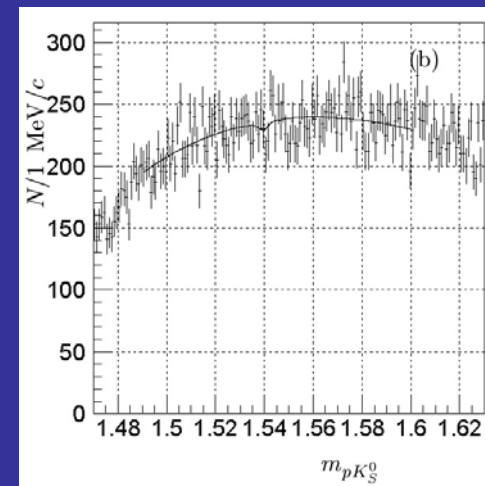
$$\sigma^{ch} / \sigma^{el} = 0.35 \pm 0.02$$

from fit to published data; typical single experiment uncertainty



$$\epsilon^{pK_s} / \epsilon^{pK^+} = 0.43 \pm 0.05$$

from Geant based MC; uncertainties in tracking and K_s eff., second. vtx eff., material desc., reaction kinem., MC stat.



Fit to $m(pK_s)$

sensitivity to Γ_{Θ^+}
 $\pm 0.42 \text{ MeV}$

Γ_{Θ^+} , backup

R.N. Cahn, G.H. Trilling, PRD69, 11501 (2004)

BW form

$$\sigma(m) = B_i B_f \sigma_0 [\Gamma^2/4] / [(m-m_0)^2 + \Gamma^2/4]$$

$$\sigma_0 = 68 \text{ mb} \quad (J=1/2)$$

mass resolution broader than natural width \Rightarrow

$$\text{integral } I = \int \sigma(m) dm = 107 \text{ mb } B_i B_f \Gamma$$

estimate of 26 signal evts in two 5 MeV bins,
bkg. level ~ 22 evts / bin

assumed bkg. from charge exchange, $\sigma^{\text{ch}} = 4.1 \pm 0.3 \text{ mb} \Rightarrow$

$$I = (26/22) \times 5 \text{ MeV} \times 4.1 \text{ mb} = 24 \text{ mb MeV}$$

$$B_i = B_f = 1/2$$

$$\Gamma = 0.9 \pm 0.3 \text{ MeV}$$

$K_S, K_L p \rightarrow \Theta^+ \rightarrow p K_S$, backup

A. Kaidalov, private comm.

apart from charge exchange reactions also
 $K_S p \rightarrow K_S p$ and $K_L p \rightarrow K_S p$ may contribute to signal

$K_L p \rightarrow \Theta^+ \rightarrow p K_S$

interference between amplitudes for same final state
can lead to “hole” in $\sigma(K_L p, \text{total})$ due to Θ^+

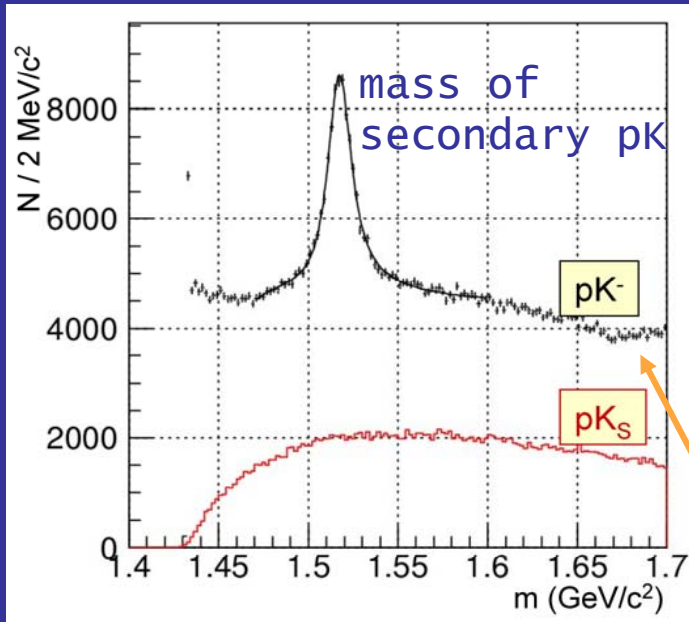
$\sigma(K_L p, \text{total}) \sim 2 \text{ mb} \Rightarrow$ negative interference $< 1 \text{ mb}$
(also depending on decay angles)

$\sigma(K^+ n \rightarrow \Theta^+ \rightarrow p K_S) \sim 17 \text{ mb}$ (DIANA)

“hole” negligible

$K_S p \rightarrow \Theta^+ \rightarrow p K_S$ would also compensate for that

Other Σ states, backup



total $\sigma(pK^-)$ shows
two prominent structures
at 1520 MeV/c² and
at \sim 1800 MeV/c²;
latter due to several
overlapping Λ and Σ states;
clearly seen, hard to interpret

Look for $\Sigma(1670)$ 4* resonance
 $m=1665-1685$ (\approx 1670) MeV/c²
 $\Gamma=40-80$ (\approx 60) MeV

Fit $m(pK_S)$ to sum of
3rd order polyn.+
D-wave BW

$$N(\Sigma(1670)) = (2.4 \pm 1.3) \times 10^3$$

$$\Sigma(1670)/\Lambda(1520) < 2 \text{ @90\% C.L.}$$

assuming $B(\Lambda^* \rightarrow pK^-) =$
 $\frac{1}{2} B(\Lambda^* \rightarrow NK) = \frac{1}{2} (45 \pm 1)\%$;
 $B(\Sigma(1670) \rightarrow p\bar{K}^0) = 10\%$

Some additional statistics, backup

95% C.L. limits:

$$\Gamma_{\Theta^+} < 0.78 \text{ MeV (@ } 1539 \text{ MeV}/c^2)$$
$$< 1.11 \text{ MeV (wide range)}$$

probability of stat. fluctuation
for the signal of the DIANA size
to the level observed by BELLE ~3%