

# Measurements of hadronic cross sections with the *BABAR* detector



Istituto Nazionale di Fisica Nucleare

On behalf of the *BABAR* Collaboration

**Alessandra Filippi**

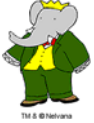
INFN Torino



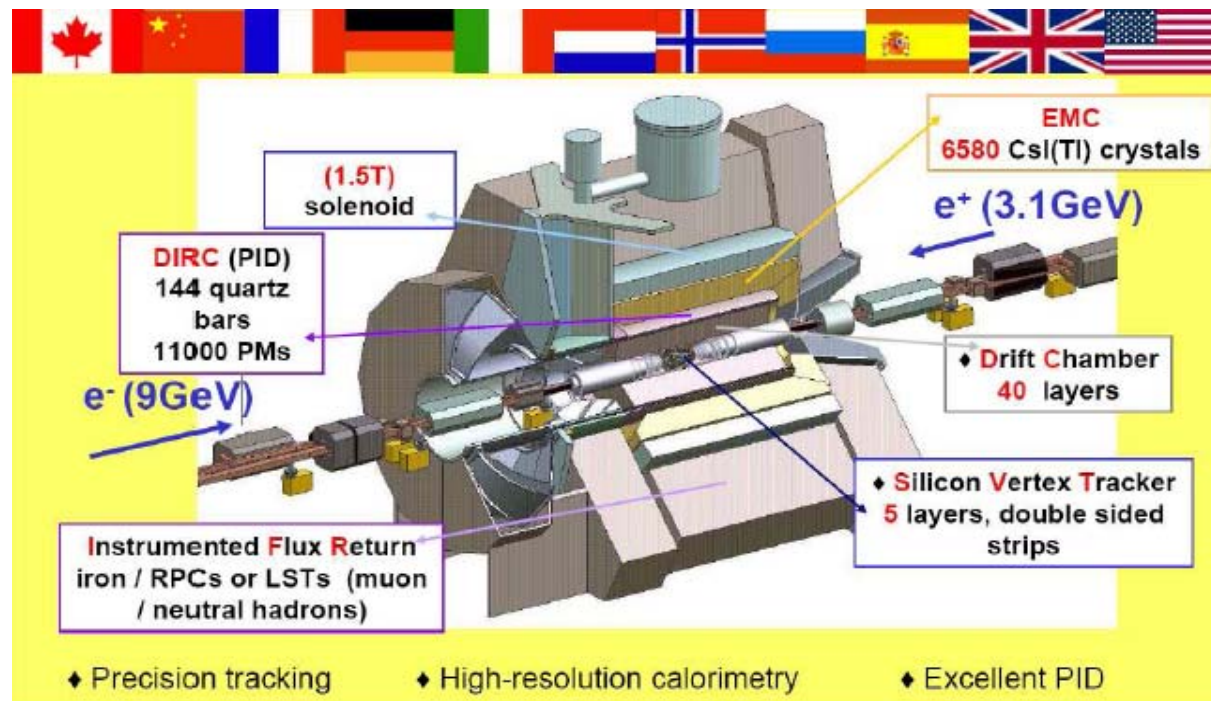
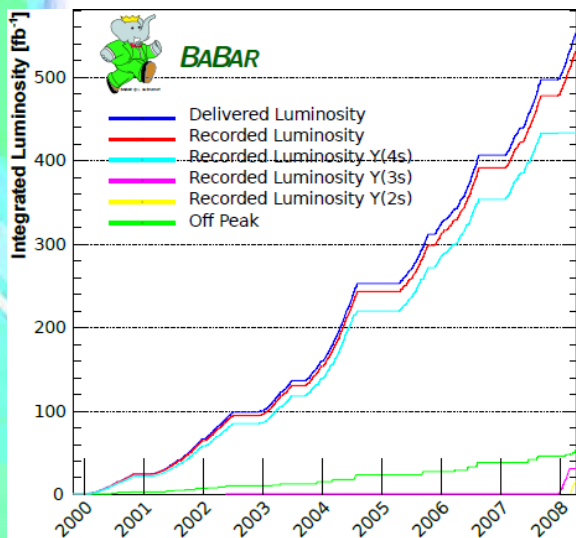


# Outline

- Introduction and motivations
  - Evaluation of  $(g-2)_\mu$  and  $\alpha_{em}(\sqrt{s} = m_Z)$
  - Study of light quark and charm spectroscopy: vector meson excitations,  $K^*$  resonances, charmonium decay modes and branching fractions
- The *BABAR* cross sections database via ISR technique in  $e^+e^-$  collisions
  - Channels with kaons & pions: cross sections and study of resonant substructures
    - $e^+e^- \rightarrow K^+K^-\pi^0$
    - $e^+e^- \rightarrow K_S K^\pm \pi^\mp$
    - $e^+e^- \rightarrow K_S K_L \pi^0$  **NEW (2017)**
    - $e^+e^- \rightarrow K_S K_L \pi^+ \pi^-$
    - $e^+e^- \rightarrow K_S K_S \pi^+ \pi^-$
    - $e^+e^- \rightarrow K^+ K^- \pi^+ \pi^-$
    - $e^+e^- \rightarrow K^+ K^- \pi^0 \pi^0$
    - $e^+e^- \rightarrow K_S K_L \pi^0 \pi^0$  **NEW (2017)**
    - $e^+e^- \rightarrow K_S K^\pm \pi^\mp \pi^0$  **NEW (2017)**
- Conclusions

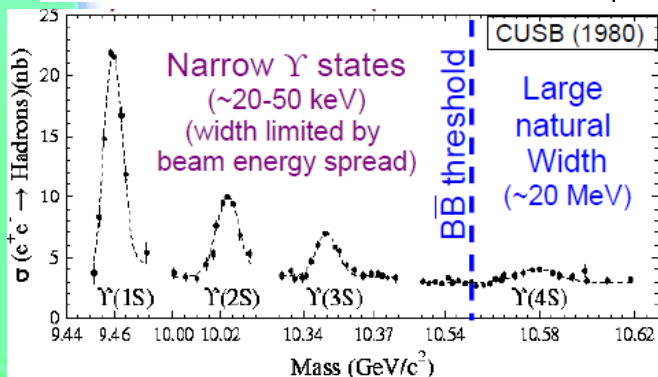


# The *BABAR* experiment at PEP-II, SLAC



NIM A479, 1 (2002); NIM A729, 615 (2013)

PEP-II and *BABAR* operated from Oct 1999 to Apr 2008



$\sim 500 \text{ fb}^{-1}$   
integrated  
luminosity

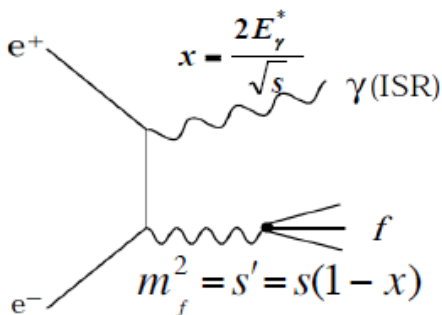
- $\sim 470 \times 10^6 \Upsilon(4S)$
- $\sim 120 \times 10^6 \Upsilon(3S)$  (10x BELLE)
- $\sim 100 \times 10^6 \Upsilon(2S)$  (10x CLEO)
- $\sim 18 \times 10^6 \Upsilon(1S)$  from  $\Upsilon(2S) \rightarrow \pi^+\pi^-\Upsilon(1S)$



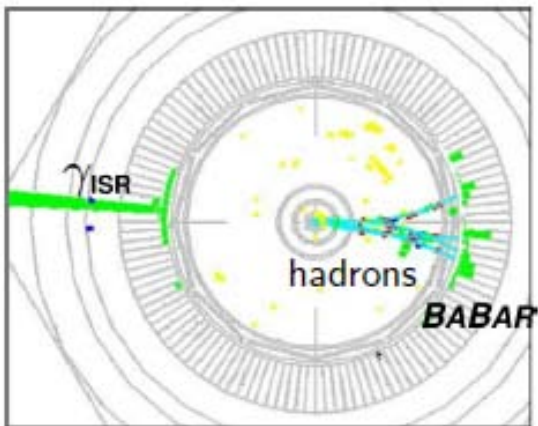
# Initial State Radiation (ISR) at $e^+e^-$ colliders

ISR photon: emitted from the colliding  $e^+$  or  $e^-$

$\sigma(e^+e^- \rightarrow f)$  extracted from  $\sigma(e^+e^- \rightarrow \gamma f)$  through a QED radiation function  $W$  known at  $\sim 1\%$  level



$$\frac{d\sigma_{e^+e^- \rightarrow f\gamma}(s, m_f)}{dm_f d\cos\theta_\gamma^*} = \frac{2m_f}{s} W(s, x, \theta_\gamma^*) \cdot \sigma_{e^+e^- \rightarrow f}(m_f)$$



- $J^{PC} = 1^{--}$  at production vertex
- continuous ISR spectrum: from threshold up to  $\sqrt{s} \sim 8$  GeV
- comparable or better sensitivity compared to energy scans
- larger ISR luminosity
- $\gamma_{ISR}$  selection:  $E_\gamma^* > 3$  GeV
- Reduced acceptance issues
- Kinematic fit for final state: good resolution



# How to solve the $(g-2)_\mu$ discrepancy

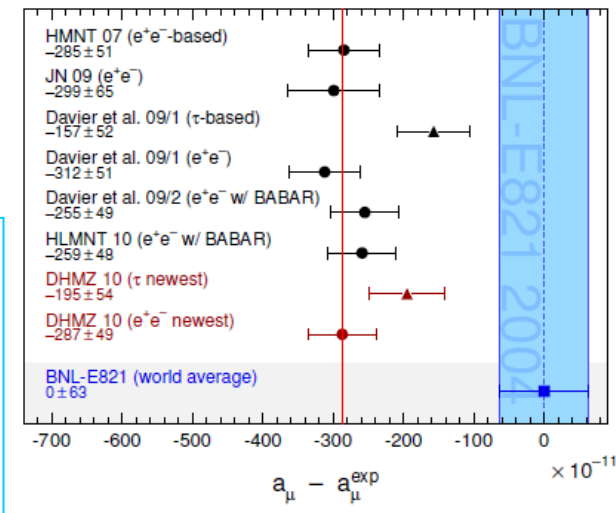
- 3.5 $\sigma$  long-standing discrepancy of theory vs experiment for the muon anomalous magnetic moment:  $a_\mu = (g_\mu - 2)/2$

M. Davier et al, EPJC71, 1515 (2011)

$$a_\mu = a_\mu^{QED} + a_\mu^{EW} + a_\mu^{hadronic, LO} + a_\mu^{hadronic, HO} + a_\mu^{hadronic, LBLs}$$

Diagrams from Jegerlehner and Nyffeler, Phys. Rept. 477 (2009) 1

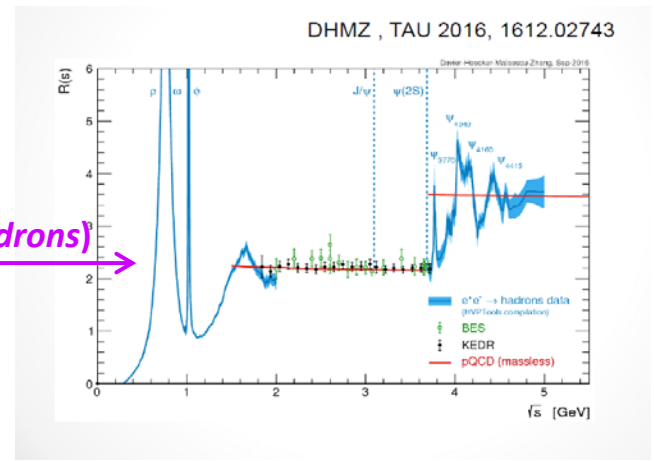
Hadronic light-by-light scattering



- Dominant correction and error from the LO hadronic term
  - Most precise predictions from low-energy  $e^+e^- \rightarrow hadrons$  exclusive cross sections and dispersion relations
  - Wide program of measurements at BABAR

$$a_\mu^{had, LO} = \frac{\alpha^2(0)}{3\pi^2} \int_{m_\pi^2}^{\infty} ds \frac{K(s)}{s} \cdot R(s) \approx \sigma(e^+e^- \rightarrow hadrons)$$

low energy dominance

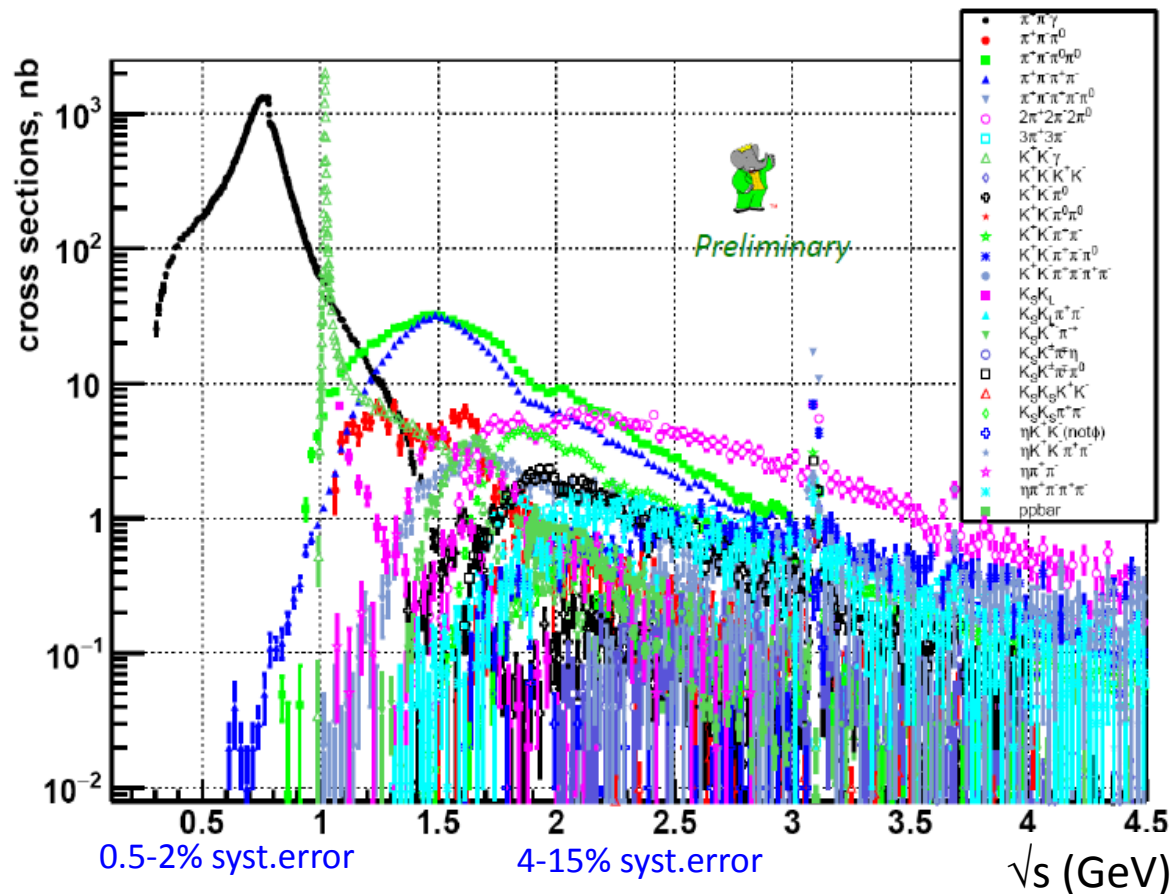






# BABAR exclusive $\sigma_{had}$ measurements

- $2\pi$  dominates for  $\sqrt{s} < 1$  GeV
- $4\pi$  dominates for  $1 < \sqrt{s} < 2$  GeV
- $6\pi$  dominates for  $\sqrt{s} > 2$  GeV



- Extended covered energy range
- Larger precision
- One experiment for all measurements

- Long list of published papers, > 20 studied channels
- Last channels with kaons recently published (2017)

Courtesy Fedor V. Ignatov, via J. Chauveau



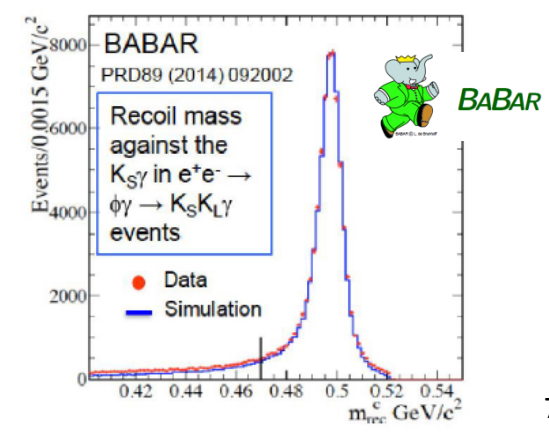
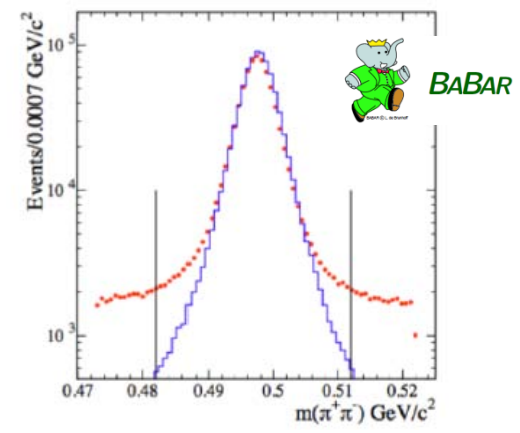
# Kaon identification in *BABAR*

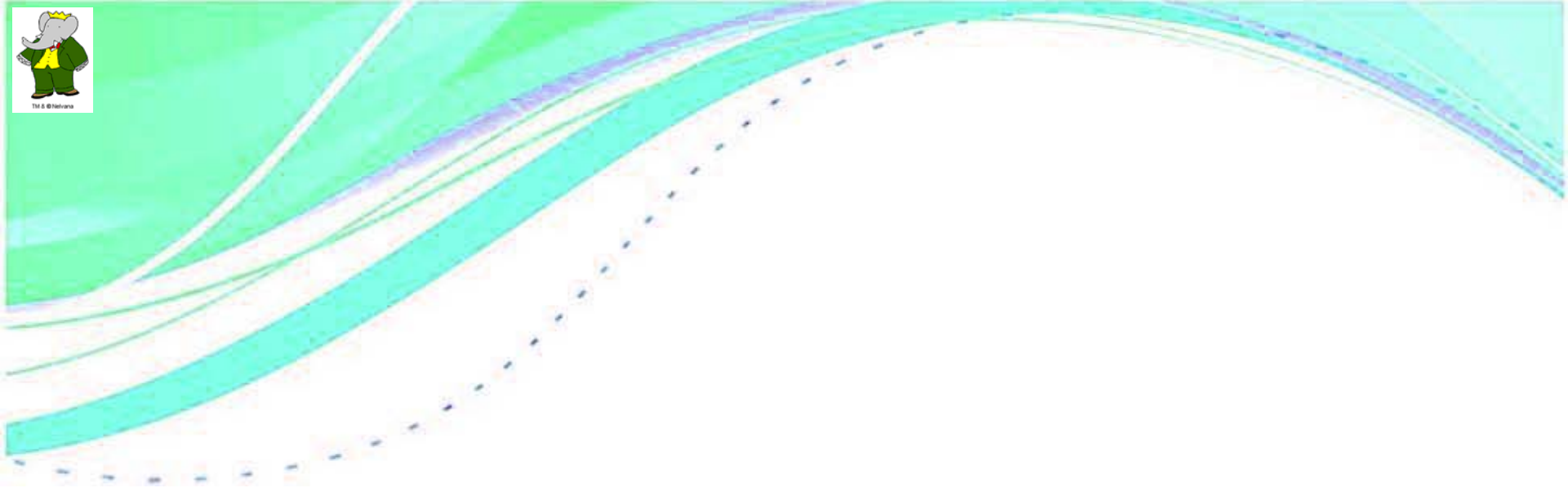
- $K^\pm$ 
  - standard charged particle pid using specific energy loss, time of flight, Cherenkov radiation
  - 80% efficiency, 2% misidentification rate

- $K_S^0$ 
  - reconstructed through pairs of opposite charged tracks with common displaced vertex:  $K_S^0 \rightarrow \pi^+ \pi^-$

- $K_L^0$ 
  - Identified via an isolated energy cluster in the calorimeter with cluster shape not consistent with a photon
  - Validated via

$$e^+ e^- \rightarrow \gamma \phi \rightarrow \gamma K_S^0 K_L^0$$





**$K\bar{K}\pi$  final states**

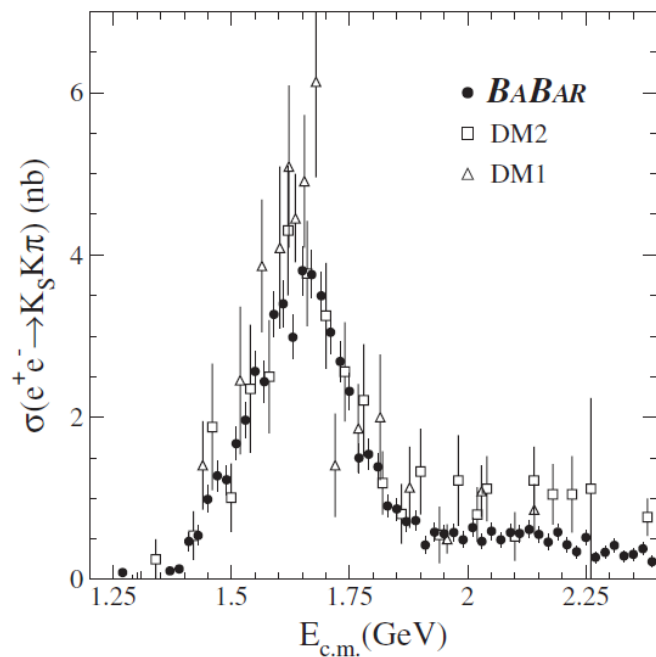


© 2004 University of Illinois at Urbana-Champaign

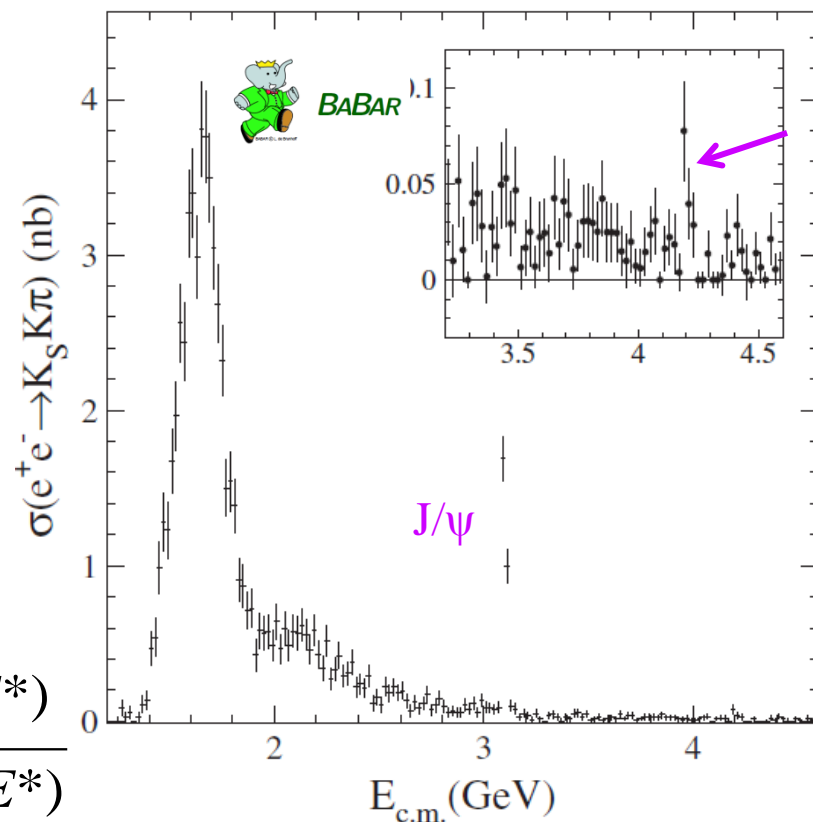


# $e^+e^- \rightarrow K_S K^\pm \pi^\mp$ : cross section

- Event reconstruction:  $\gamma_{ISR}, K_S^0$
- Clear observation of  $J/\psi$
- No evidence for  $Y(4260)$ , upper limit at 90% C.L.  $\Gamma_{ee}^{Y(4260)} \cdot \mathcal{B}_{K_S^0 K^\pm \pi^\mp}^{Y(4260)} = 0.5 \text{ eV}$
- Excess of events observed at  $\sim 4.2 \text{ GeV}$ :  $3.5\sigma$  fluctuation



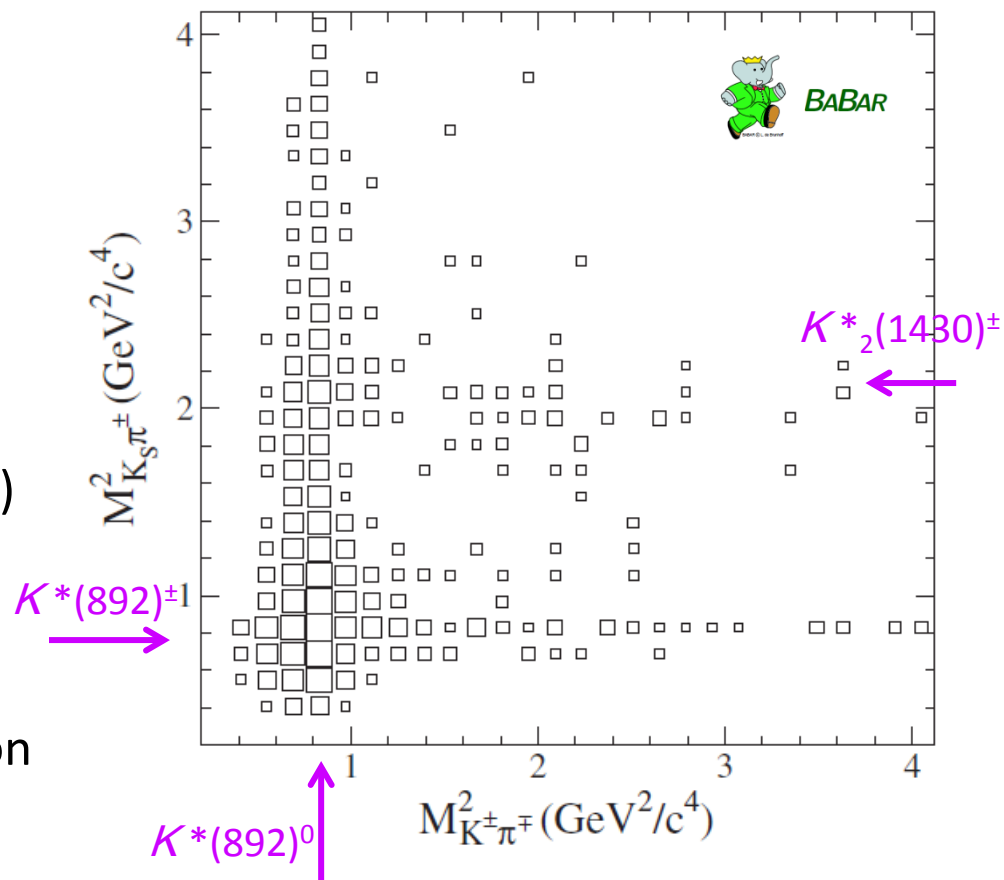
$$\sigma(e^+e^- \rightarrow K_S^0 K^\pm \pi^\mp)(E^*) = \frac{dN_{K_S^0 K^\pm \pi^\mp}(E^*)}{d\mathcal{L}(E^*) \cdot \varepsilon(E^*)}$$





# $e^+e^- \rightarrow K_S K^\pm \pi^\mp$ : Dalitz analysis

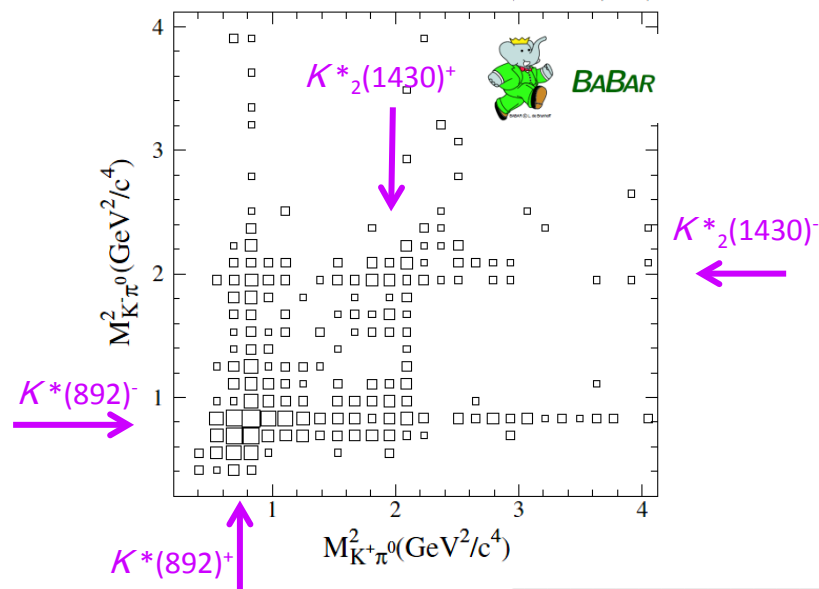
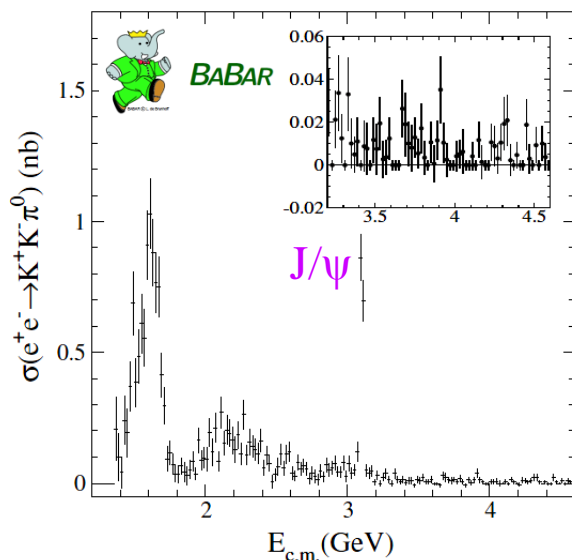
- Main contribution given by  $K^*(892)^\pm K^\mp$  and  $K^*(892)^0 K_S$  or  $K^*_2(1430)^\pm K^\mp$  and  $K^*_2(1430)^0 K_S$ 
  - Both charged and neutral  $K^*$
  - Asymmetric Dalitz plot
- Small contribution from  $KK_1(1410)$  (small width in  $KK\bar{\pi}$ )
- From Dalitz plot analysis the isovector and isoscalar components of the cross section can be extracted
  - Charged/neutral  $K^*$  modeled differently by interference effects
  - Dominant isoscalar component with clear resonant behavior ( $\phi(1680)$ )
  - Isovector component: one broad resonance only ( $\rho(1450)$ )



- Main contribution to  $K_S \pi^\mp$  above 2 GeV given by  $K^*_2(1430)^\pm$

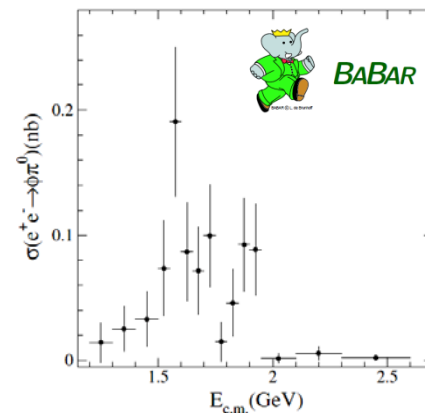
# $e^+e^- \rightarrow K^+K^-\pi^0$

- Clear observation of  $J/\psi$
- No evidence for  $Y(4260)$ , upper limit of decay BR at 90% C.L.: 0.6 eV



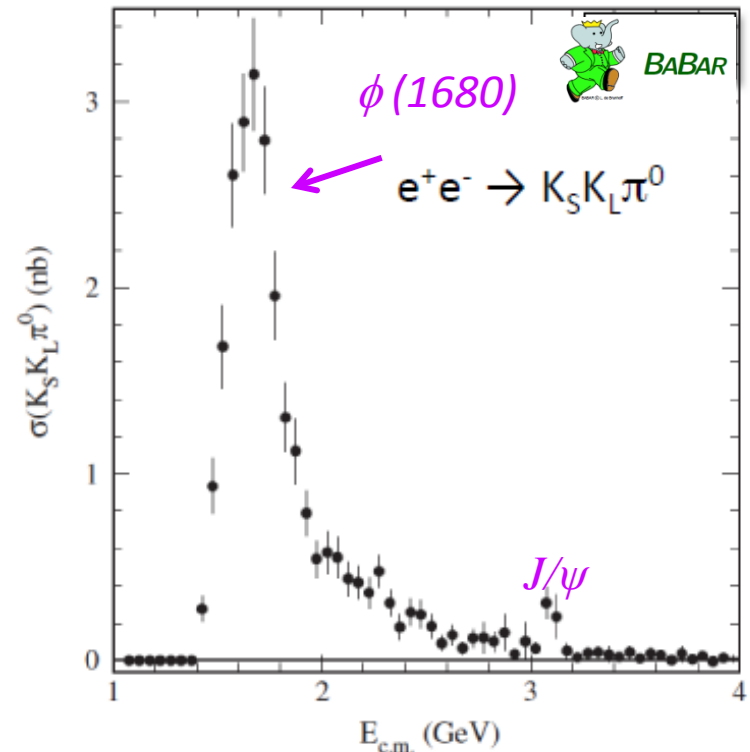
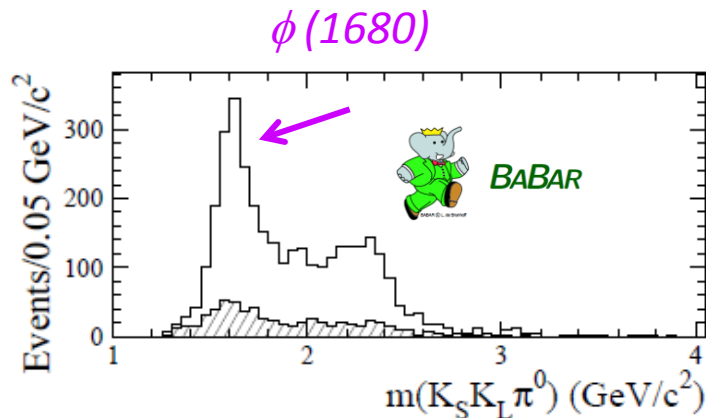
- Resonant substructures:

- Final state produced through  $K^*(892)^\pm K^\mp$  or  $K^*_2(1430)^\pm K^\mp$
- neutral  $K^*$  only, symmetric Dalitz plot
- $\phi\pi^0$  final state: observation of  $C(1480)$ ?  
Of  $\rho(1700)$ ? Of  $\rho(1900)$  as a dip?



# $e^+e^- \rightarrow K_S K_L \pi^0$ : cross section

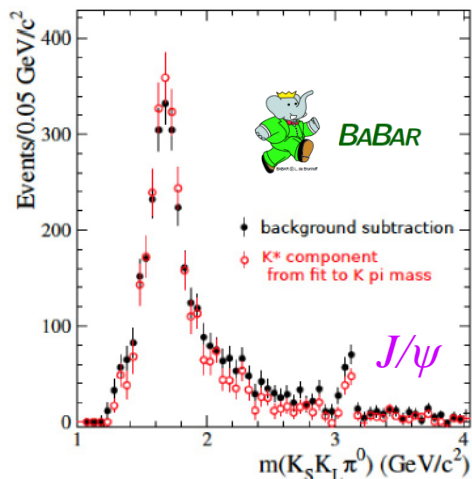
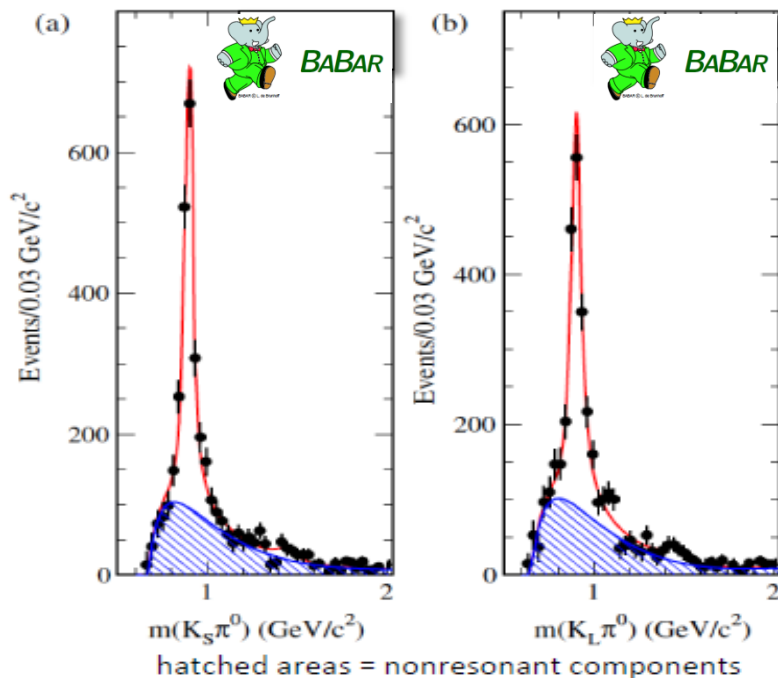
- Event reconstruction:  $\gamma_{ISR}, \pi^0 \rightarrow \gamma\gamma, K_S^0$
- Invariant mass resolution of the final state: 25 MeV
- First measurement of this process: 3700 events
- First observation of  $J/\psi \rightarrow K_S K_L \pi^0$
- Systematic uncertainty:  $\sim 10\%$  at peak,  $\sim 30\%$  at 3 GeV



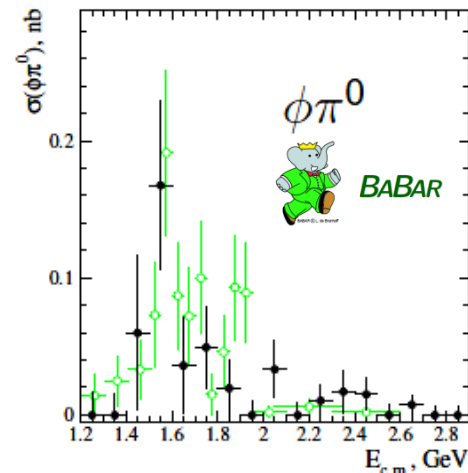


# $e^+e^- \rightarrow K_S K_L \pi^0$ : resonant substructures

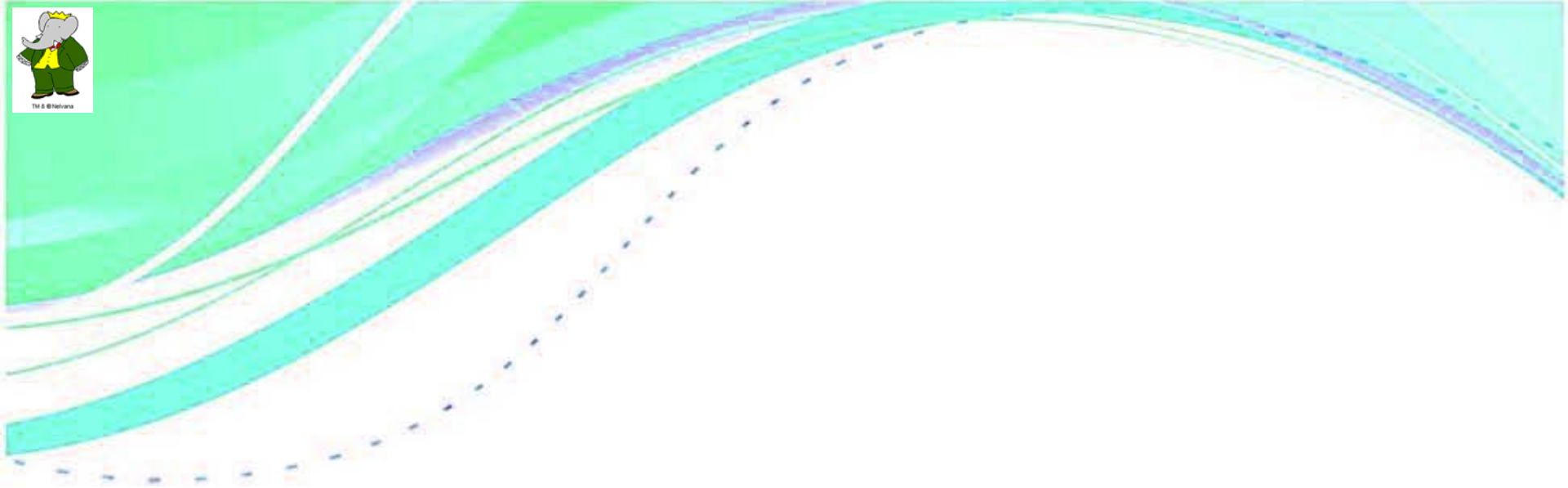
- Fit of background subtracted ( $K_S \pi^0$ ) and ( $K_L \pi^0$ ) invariant mass spectra with coherent resonant+non-resonant contributions
  - Dominant  $K^{*0} \bar{K}^0 + c.c.$ 
    - mostly  $K^*(892)^0 \bar{K}^0 +$  small  $K^*(1430)^0 \bar{K}^0$



- Cross section saturated by  $K^*(892)^0 \bar{K}^0 + c.c.$
- Small contribution from  $\phi \pi^0$ 
  - Possible resonant structure  $I=1$  @ 1.6 GeV?





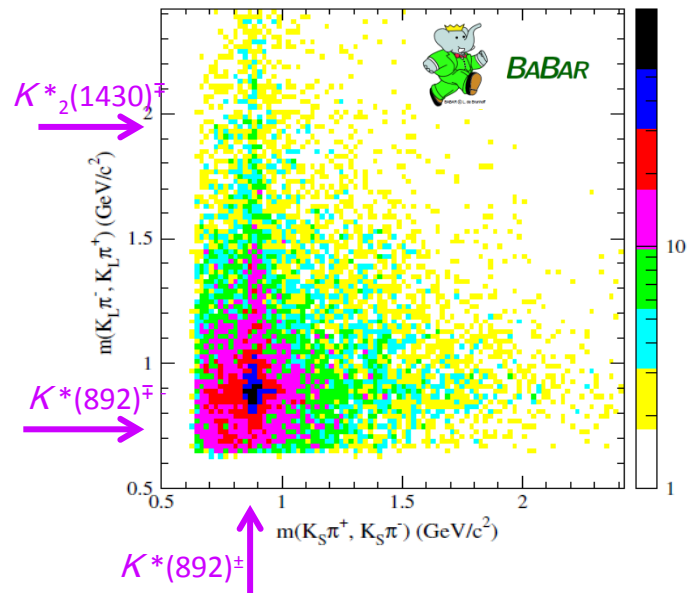
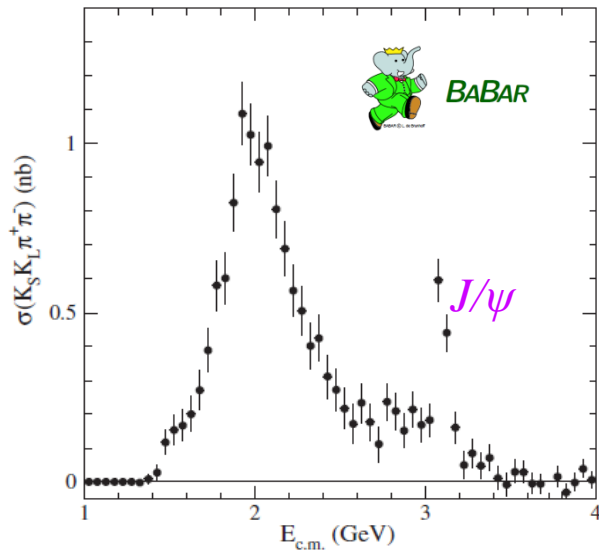


$K\bar{K}\pi\pi$  final states



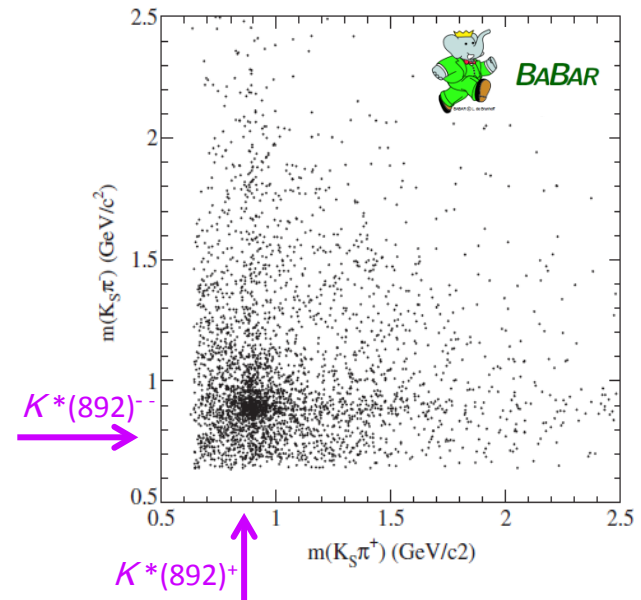
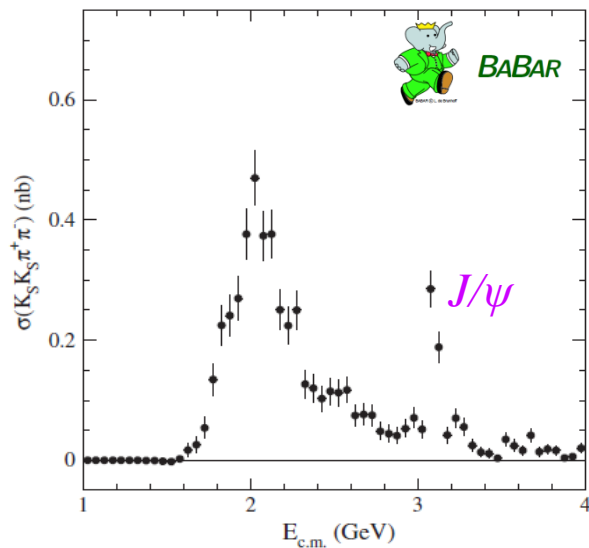
# $e^+e^- \rightarrow K_S K_L \pi^+ \pi^-$

- Events with two tracks (not kaons) not coming from  $K_S$  but consistent with the same decay vertex
- Large background from ISR and non-ISR multihadron events
- Systematic uncertainty:  $\sim 10\%$  for  $E^* < 2$  GeV,  $\sim 30\%$  at 2.5-3 GeV, 100% above 3.4 GeV
- Resonant substructure:
  - Clear bands of  $K^*(892)^\pm$  and indications of  $K^*_2(1430)^\pm$
  - Correlated production of  $K^*(892)^+ K^*(892)^-$  and  $K^*(892)^\pm K^*_2(1430)^\mp$



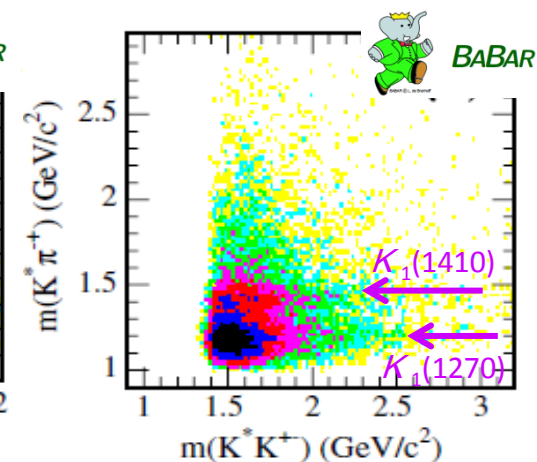
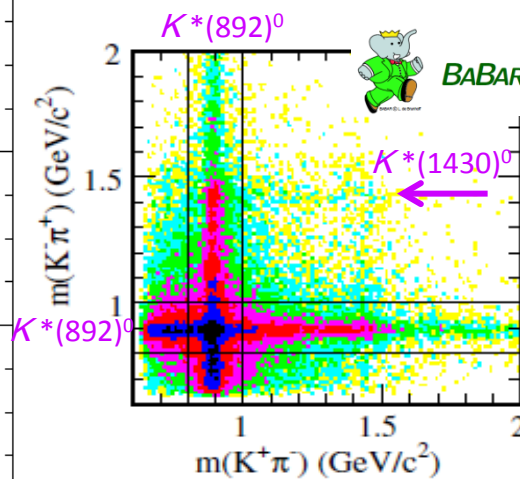
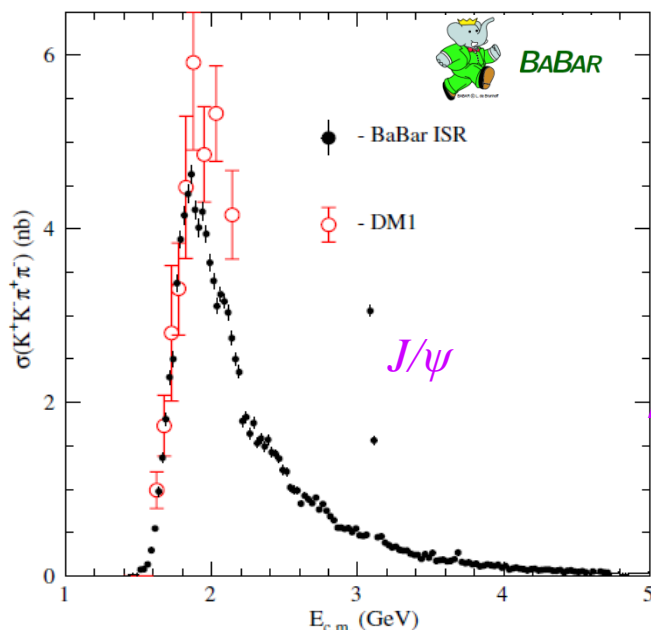
# $e^+e^- \rightarrow K_S K_S \pi^+ \pi^-$

- Only one neutral particle: ISR photon
- Systematic uncertainty dominated by the uncertainty of the background: ~5% at the peak, 50-70% at higher energies
- Resonant substructure:
  - Clear bands of  $K^*(892)^\pm$  and indications of  $K^*_2(1430)^\pm$
  - Correlated production of  $K^*(892)^+K^*(892)^-$ , dominant contribution below 2.5 GeV
  - Number of correlated  $K^*(892)^+K^*(892)^-$  in  $K_S K_S \pi^+ \pi^-$  vs  $K_S K_S \pi^+ \pi^-$  vs  $K^+K^-\pi^0\pi^0$  consistent with 1:2:1
  - no significant signal for  $K^*(892)^\pm K^*_2(1430)^\mp$ , small for  $K^*_2(1430)^\pm K_S \pi^\mp$



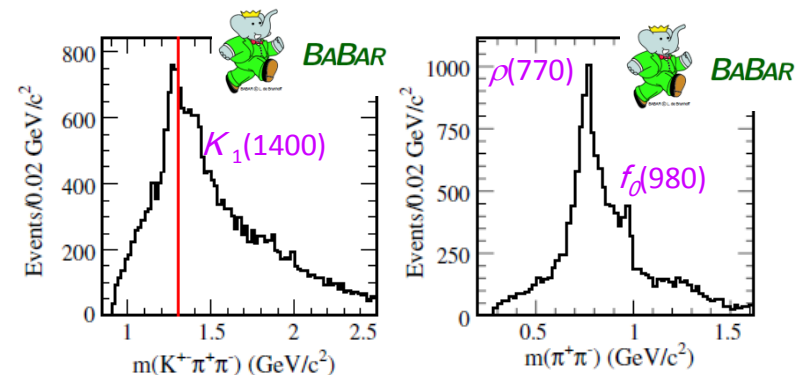
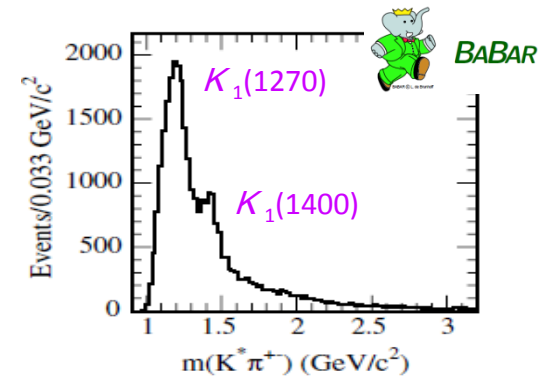
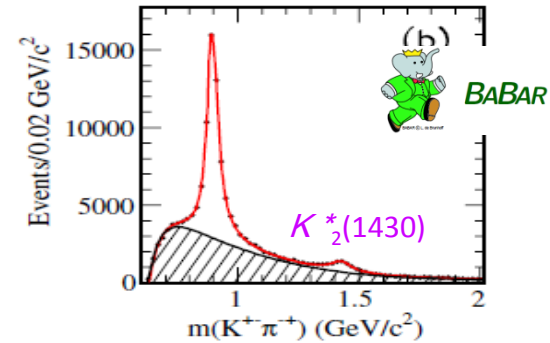
# $e^+e^- \rightarrow K^+K^-\pi^+\pi^-$ : cross section

- Systematic uncertainty:  $\sim 20\%$  below 1.6 GeV,  $\sim 2\%$  in the 1.6-3.3 GeV range,  $\sim 10\%$  in the range 3.3-5 GeV
- Cross section systematically lower than DM1 measurements
- Narrow peaks from  $J/\psi$ ,  $\psi(2S)$  + possibly other structures (due to thresholds for intermediate states?)
- Mass resolution: 4.2 MeV below 2.5 GeV, 5.5 MeV above
- Resonant substructure: plenty of intermediate states



# $e^+e^- \rightarrow K^+K^-\pi^+\pi^-$ : resonant substructure

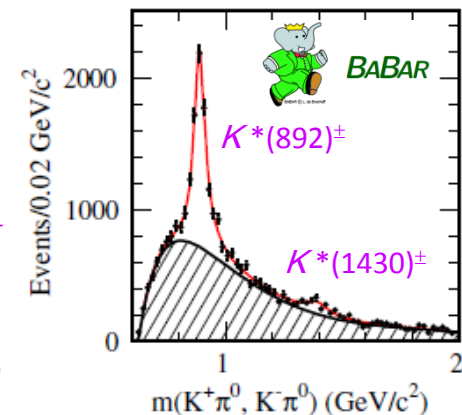
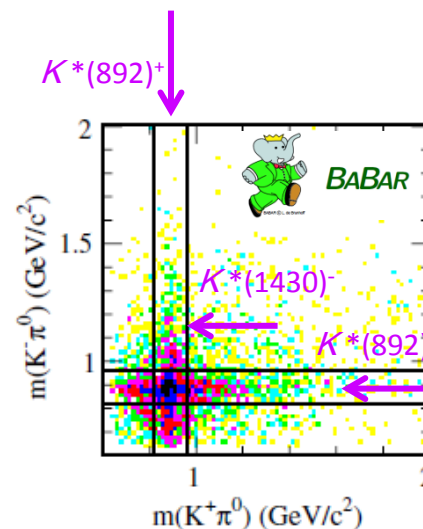
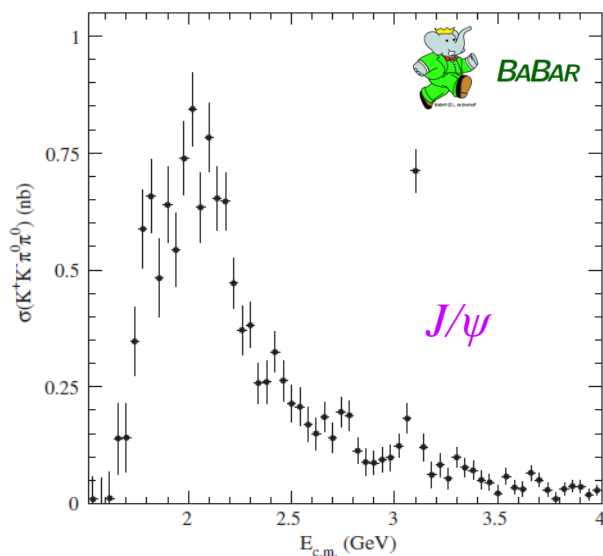
- Clear signal of  $K^*(892)^0$  and  $K^*_2(1430)^0$ 
  - Marginal contributions from  $K^*(1410)^0$  and/or  $K^*_0(1430)^0$  (other  $K^\pm\pi^\mp$  decays)
- $K^*(892)^0\pi^\pm$  invariant mass:
  - Evidence of contributions from  $K_1(1270)$  and  $K_1(1400)$
- Events **without**  $K^*(892)^0K\pi$ :
  - Evidence for  $K_1(1270)$  and  $K_1(1400)$  decaying into  $K\rho(770)$
  - No indications of additional  $\pi^+\pi^-$  structures





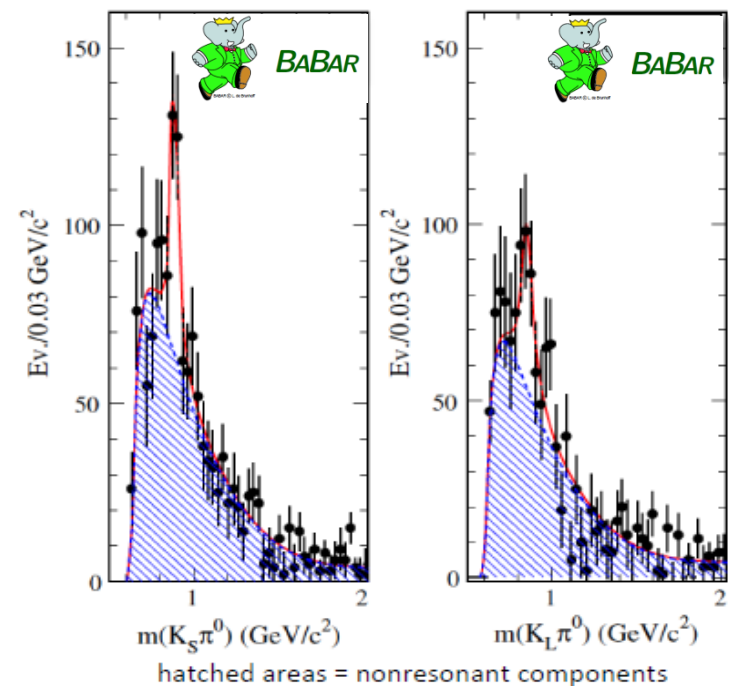
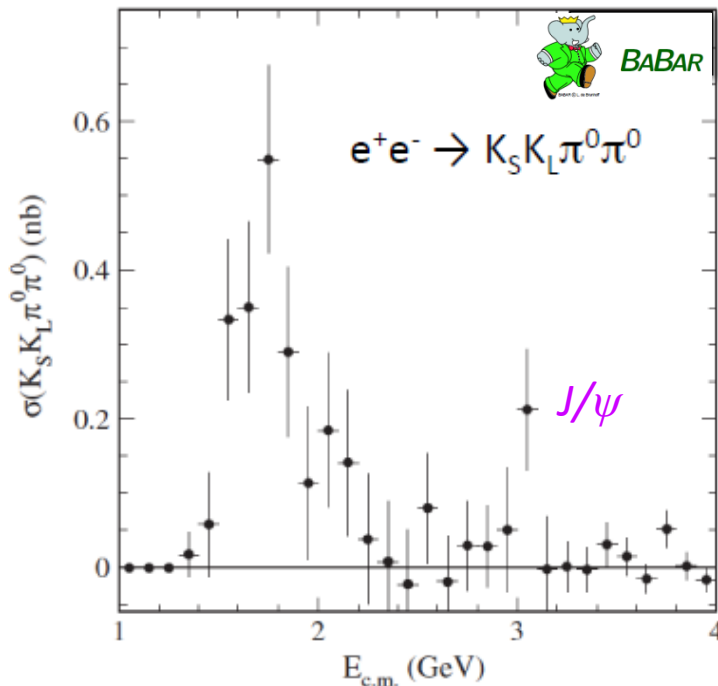
# $e^+e^- \rightarrow K^+K^-\pi^0\pi^0$

- Systematic uncertainty:  $\sim 7\%$  at low mass,  $\sim 16\%$  above 3 GeV
- Mass resolution: 8.8 MeV, increase to 11.2 MeV in the 2.5-3.5 GeV range
- Resonant substructure:
  - Large contributions from  $K^*(892)^\pm$
  - $K^*(1430)^\pm/K^*(892)^\pm$  consistent with the neutral  $K^*$  production in  $K^+K^-\pi^+\pi^-$
  - Clear correlated production observed for  $K^*(892)^+K^*(892)^-$  and  $K^*(892)^+K^*_2(1430)^-$
  - No evidence of resonant production in  $K^+K^-\pi^0$  or  $K^\pm\pi^0\pi^0$



# $e^+e^- \rightarrow K_S K_L \pi^0 \pi^0$

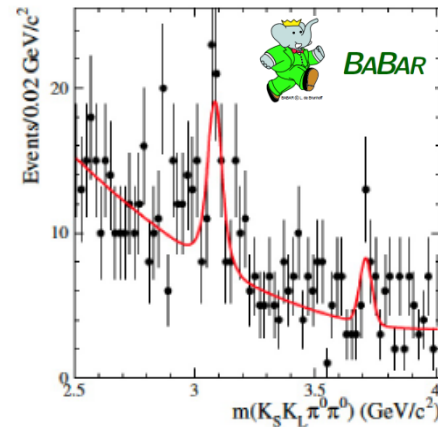
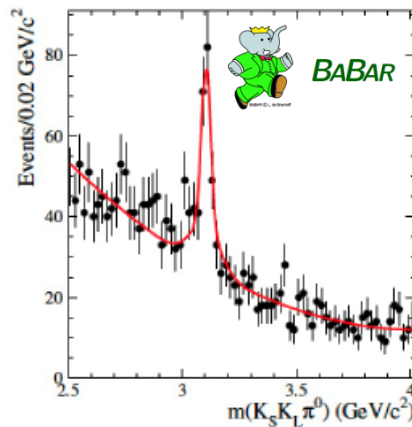
- First cross section measurement
- First observation of  $J/\psi \rightarrow K_S K_L 2\pi^0$  (possibly  $\psi(2S)$ )
- Systematic uncertainty:  $\sim 25\%$  at peak,  $\sim 60\%$  at 2 GeV
- Dominant contribution from  $K^*(892)K \pi$  intermediate state
  - Evident signals from  $K^*(892)^0$  (large background)
  - No significant contribution from  $K^*(892)^0 \bar{K}^*(892)^0$



# Charmonium region: decay branching ratios

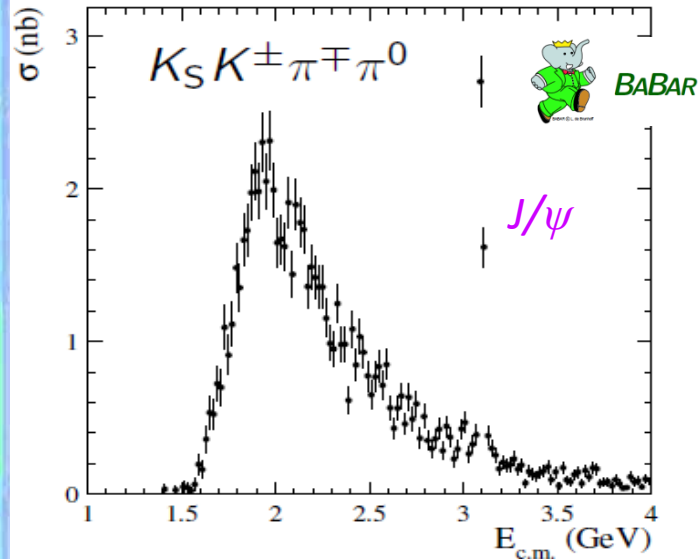
- Many new  $J/\psi$  and  $\psi(2S)$  decay channels observed
- Branching ratio determination based on cross sections:

$$\sigma(e^+e^- \rightarrow c\bar{c} \rightarrow X) \sim \Gamma(c\bar{c} \rightarrow e^+e^-) \cdot \mathcal{B}(c\bar{c} \rightarrow X)$$

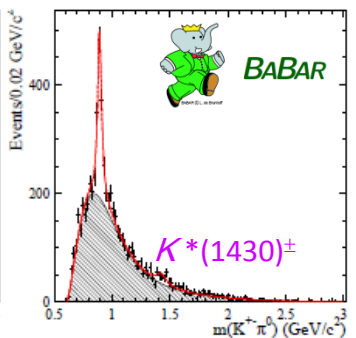
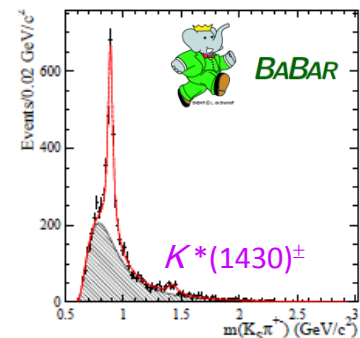
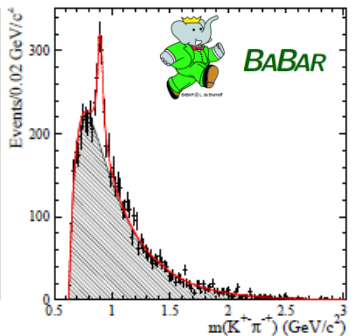
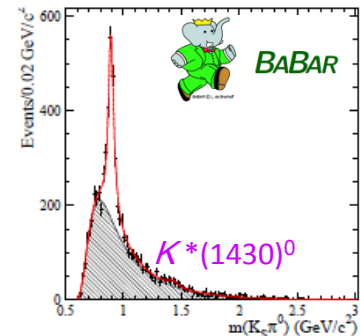
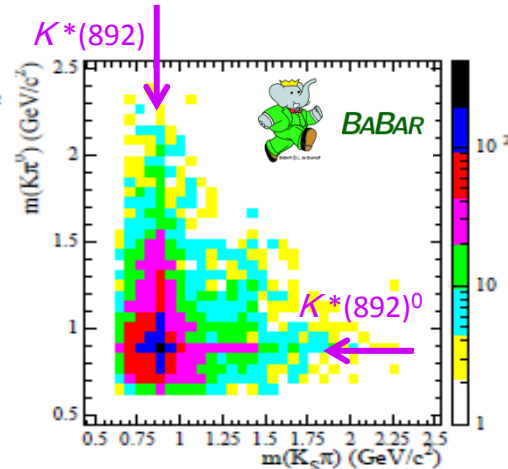
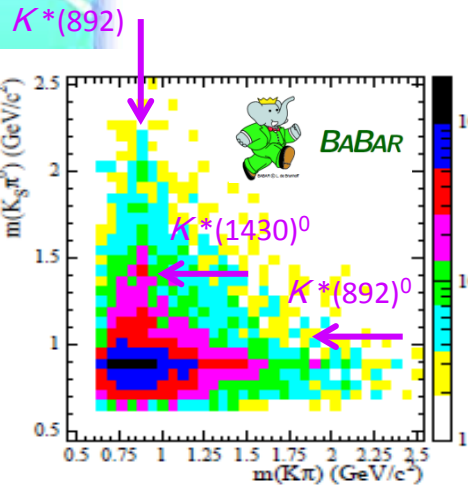


Measured Quantity	Measured Value (eV)	Calculated Branching Fractions ( $10^{-3}$ )	
		This work	Previous
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K_S^0 K_L^0 \pi^0}$	$11.4 \pm 1.3 \pm 0.6$	$2.06 \pm 0.24 \pm 0.10$	–
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K_S^0 K_L^0 \eta}$	$8.0 \pm 1.8 \pm 0.4$	$1.45 \pm 0.32 \pm 0.08$	–
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K_S^0 K_L^0 \pi^0 \pi^0}$	$10.3 \pm 2.3 \pm 0.5$	$1.86 \pm 0.43 \pm 0.10$	–
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K^*(892)^0 \bar{K}^0 + c.c.} \cdot \mathcal{B}_{K^*(892)^0 \rightarrow K^0 \pi^0}$	$6.7 \pm 0.9 \pm 0.4$	$1.20 \pm 0.15 \pm 0.06$	–
$\Gamma_{ee}^{J/\psi} \cdot \mathcal{B}_{J/\psi \rightarrow K_2^*(1430)^0 \bar{K}^0 + c.c.} \cdot \mathcal{B}_{K_2^*(1430)^0 \rightarrow K^0 \pi^0}$	$2.4 \pm 0.7 \pm 0.1$	$0.43 \pm 0.12 \pm 0.02$	$< 4$ [26]
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow K_S^0 K_L^0 \pi^0}$	$< 0.7$	$< 0.3$	–
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow K_S^0 K_L^0 \eta}$	$3.14 \pm 1.08 \pm 0.16$	$1.33 \pm 0.46 \pm 0.07$	–
$\Gamma_{ee}^{\psi(2S)} \cdot \mathcal{B}_{\psi(2S) \rightarrow K_S^0 K_L^0 \pi^0 \pi^0}$	$2.92 \pm 1.27 \pm 0.15$	$1.24 \pm 0.54 \pm 0.06$	–

# $e^+e^- \rightarrow K_S K^\pm \pi^\mp \pi^0$



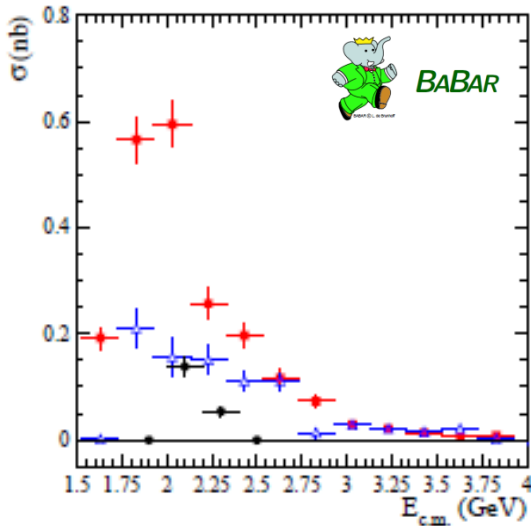
- Systematic uncertainty:  $\sim 6\%$  ( $E^* < 2$  GeV) -  $\sim 12\%$  ( $E^* > 3$  GeV)
- Very rich intermediate state composition
  - Single, double  $K^*(892)^0$  production (charged and neutral)
  - $K^*_2(1430)$ ,  $K^*_0(1430)$
  - $\rho(770)$  resonance





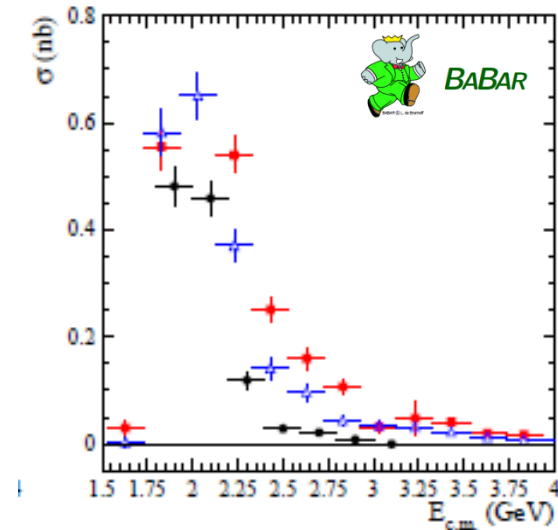
# $e^+e^- \rightarrow K^*(892)K\pi, K_S K\pi$

- Neutral/charged  $K^*(892)$ : dominant contribution



Neutral  $K^0$

- $e^+e^- \rightarrow K^{*0}K^{\pm}\pi^{\mp}$
- $e^+e^- \rightarrow K^{*0}K_S\pi^0$
- $e^+e^- \rightarrow K^{*0}\bar{K}^{*0}$

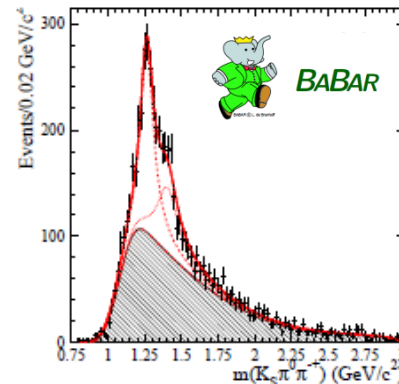
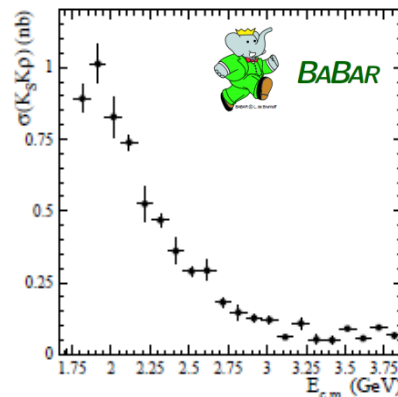
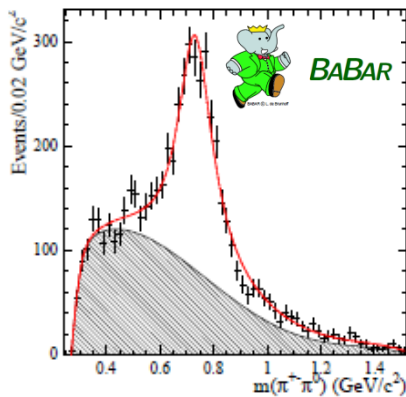


Charged  $K^*$

- $e^+e^- \rightarrow K^{*\pm}K_S\pi^{\mp}$
- $e^+e^- \rightarrow K^{*\pm}K^{\mp}\pi^0$
- $e^+e^- \rightarrow K^{*+}K^{*-}$

- Large  $K_S K^{\pm}\rho^{\mp}(770)$  fraction

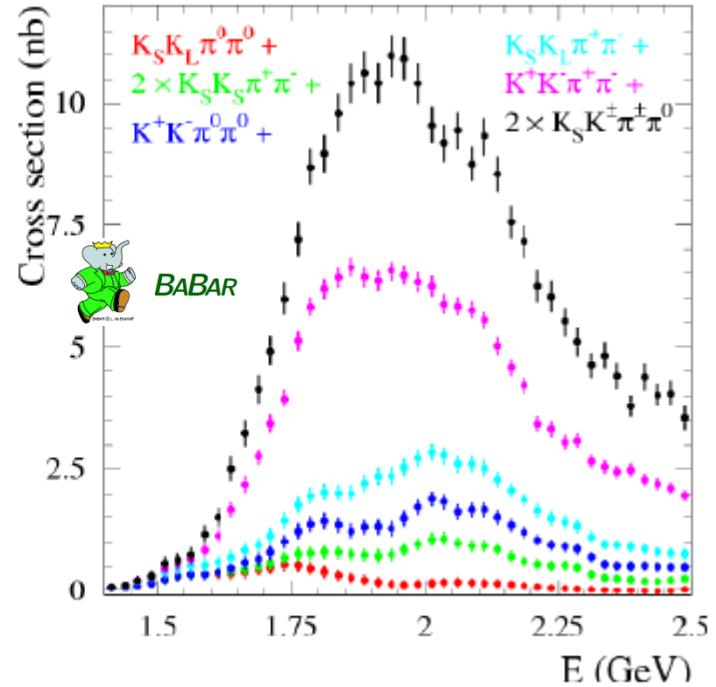
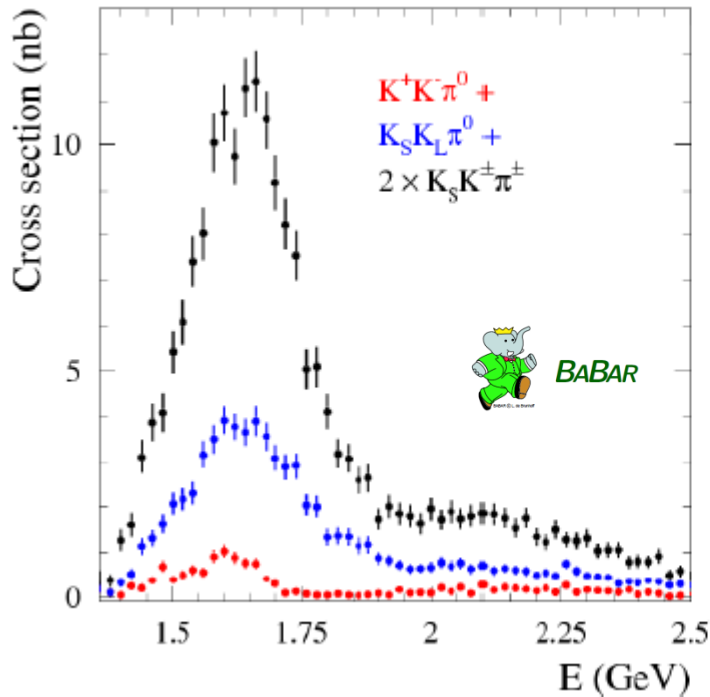
Some events may come from  $K_1 \rightarrow K\rho^{\mp}$   
( $K_1(1270), K_1(1400), K_1(1650)$ )







# Total $e^+e^- \rightarrow K\bar{K}\pi, K\bar{K}\pi\pi$ cross sections

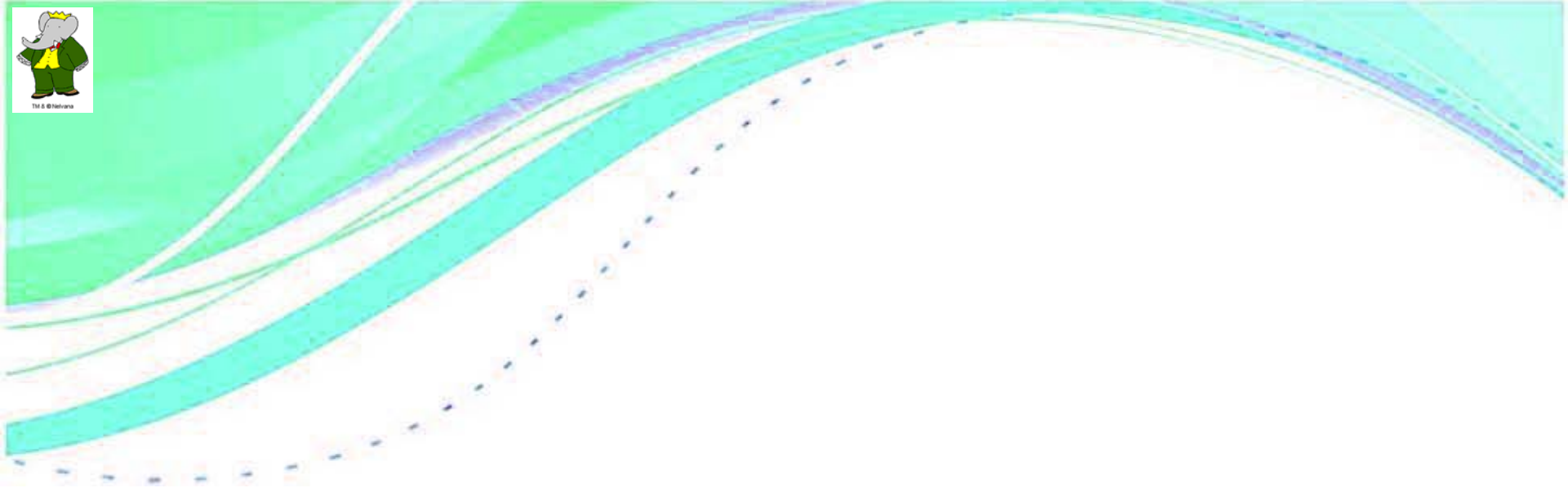


- Cross sections for all channels measured by *BABAR* (except with  $2K_L$ )
  - $K\bar{K}\pi$  :  $\sim 12\%$  of total cross section @  $E^* \sim 1.6$  GeV
  - $K\bar{K}\pi\pi$ :  $\sim 25\%$  of total cross section @  $E^* \sim 2$  GeV
- Symmetry relationships no more necessary
- Significant improvement on  $(g-2)_\mu$  determination :  $30\% \Rightarrow 6\%$  precision



# Conclusions

- The use of ISR technique at  $B$ -factories was pioneered by  $BABAR$  and led to a wealth of precision measurements of many exclusive hadronic cross sections
- $\sigma(e^+e^- \rightarrow \text{hadrons})$ :
  - Most precise determination of the LO hadronic contribution to the muon magnetic momentum anomaly
    - Improvement in precision of  $a_\mu^{\text{had,LO}} \sim 20\%$
  - New information on hadron dynamics and light hadron spectrum
  - First measurements of never observed decay channels
  - First observations of charmonium decay modes and branching fractions
  - Study of new resonances and decay modes
- New experimental inputs awaited from new generation of charm and  $B$ -factories



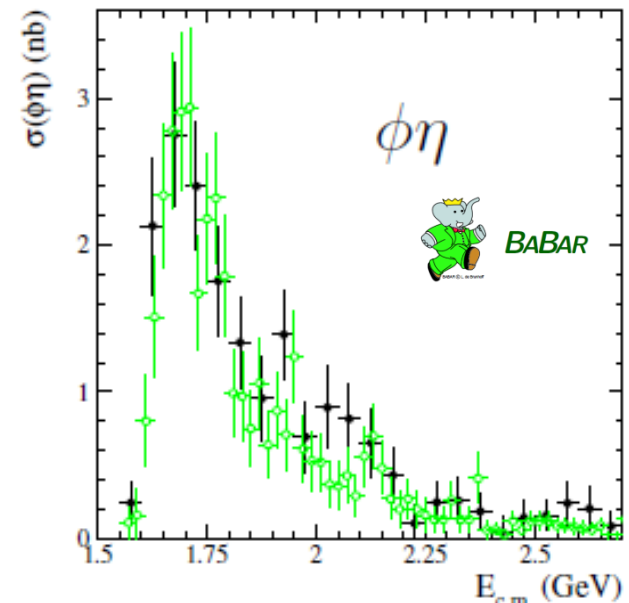
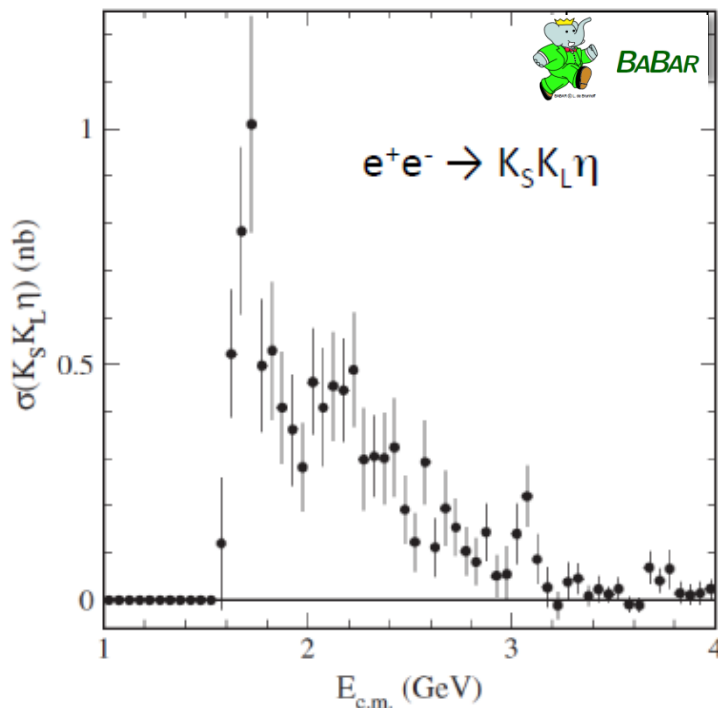
**backup slides**



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# $e^+e^- \rightarrow K_S K_L \eta$ cross section

- Event reconstruction:  $\gamma_{ISR} \eta \rightarrow \gamma\gamma$  in proper mass window,
- First cross section measurement
- First observation of  $J/\psi \rightarrow K_S K_L \eta$
- Systematic uncertainty:  $\sim 25\%$  at peak,  $\sim 60\%$  at 2 GeV
- $\phi\eta$  channel dominating the  $K_S K_L \eta$  channel
  - No significant  $J/\psi$  signal
  - No significant structures in  $K_S \eta$  or  $K_L \eta$



# $e^+e^- \rightarrow K_S K^\pm \pi^\mp \eta$

- First cross section measurement
- First observation of narrow  $J/\psi \rightarrow K_S K^\pm \pi^\mp \eta$
- Systematic uncertainty: 12% below 3 GeV, 19% for  $E^* > 3$  GeV
- No significant structure observed in  $K^\pm K_S$ ,  $K^\pm \eta$ ,  $K_S \eta$
- Dominant  $K^*(892)^\pm + K^*_2(1430)^\pm$
- Suppression of neutral vs charged  $K^*(892)$ , no hint of  $K^*_2(1430)^0$

