

# Unraveling hadron $P_T$ in SIDIS: Measurements and non-perturbative dynamics

C. Weiss (JLab), Precision Radiative Corrections Workshop, JLab, 16-19 May 2016

- What measurements can help determine the mechanisms producing hadron  $P_T$  in SIDIS?

Charged pion multiplicities: Separating favored–unfavored fragmentation

Lower  $W$ : Choice of kinematic variables

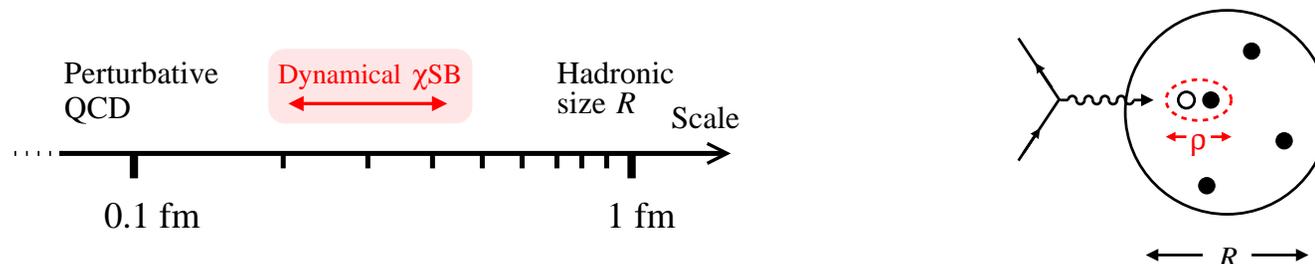
Transition photo/hadroproduction  $\leftrightarrow$  low- $Q^2$  electroproduction

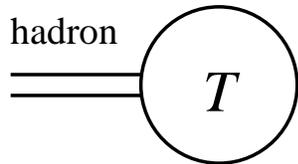
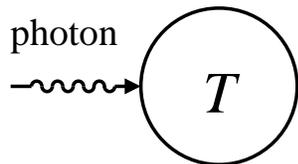
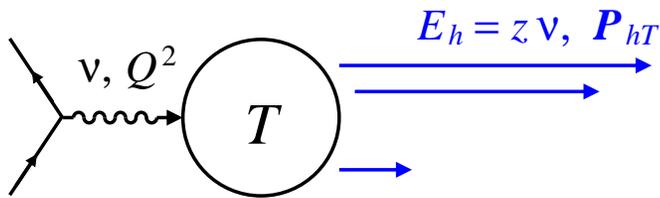
Correlations current  $\leftrightarrow$  target fragmentation regions

- What does non-pert. QCD tell us about TMDs at low scales?

Short-range interactions in dynamical chiral symmetry breaking

Intrinsic  $p_T(\text{sea}) \gg p_T(\text{valence})$ , parton short-range correlations





- High-energy scattering  $\nu \gg \Lambda_h$   
Large number of hadrons  $\sim \log(\nu/\Lambda_h)$

- Longitudinal momentum/energy

$$z = E_h/\nu \quad \text{energy fraction rest frame}$$

$$x_L = P_{hL}/P_{hL}^{\max} \quad \text{momentum fraction CM}$$

$$\eta = \frac{1}{2} \log P_h^+ / P_h^- \quad \text{rapidity}$$

- Transverse momentum  $P_{hT}$

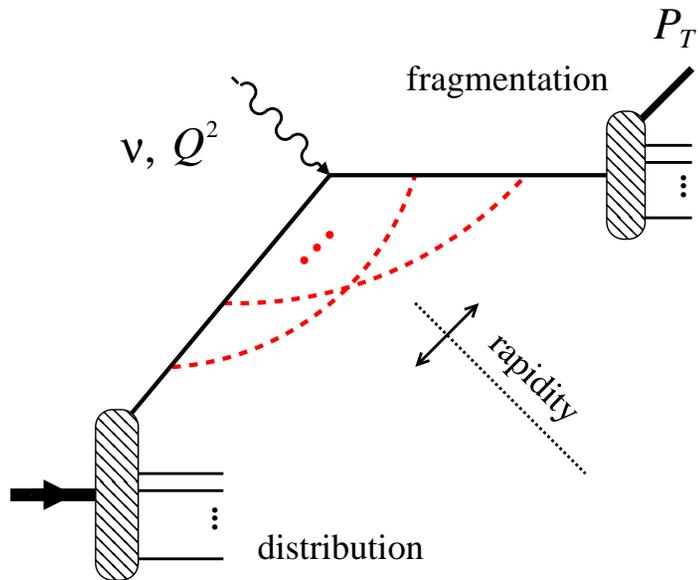
$$P_{hT} \sim \Lambda_h \text{ "soft,"} \quad P_{hT} \gg \Lambda_h \text{ "hard"}$$

- Theoretical approaches

Soft photo/hadroproduction: Regge expansions based on generalized optical theorem, hadronic structure of photon (VMD)

Hard processes  $P_{hT} \gg \Lambda_h$ : pQCD, collinear factorization

Electroproduction high  $Q^2$ , low  $P_{hT}$ : TMD factorization



$$\frac{d\sigma}{dP_T} \sim \text{FT } f(\mathbf{b}_T, x, \zeta_1, \mu) \times D(\mathbf{b}_T, z, \zeta_2, \mu) + \text{"Y-term"}$$

$(P_T \ll Q, \zeta_1 \zeta_2 = Q^2)$

- QCD radiation, real and virtual  
Effect different from inclusive  $\sigma$ :  
Sudakov suppression due to  $P_T \ll Q$   
*Collins, Soper Sterman 84*
- Separation in rapidity  
distribution  $\leftrightarrow$  fragmentation  
*Collins 11, Collins Rogers. Also SCET-based approaches*  
Arbitrary, but controlled by  $\zeta_1, \zeta_2$
- TMD distribution/fragmentation fns  
QCD operator definition  
Wilson lines describe QCD  
initial/final state interactions  
Universality
- CSS evolution equations govern  
scale and rapidity dependence  
Kernel involves non-perturbative  
structure: VEV of Wilson lines

- Region of applicability?

Effective scale – where do perturbative dependencies become relevant?

Is there a “natural” rapidity separation in SIDIS?

- Structure of TMD distribution and fragmentation functions?

Relation to inclusive PFDs/FFs, hadronic structure?

Valence vs. sea TMD PDFs, favored vs. unfavored TMD FF?

- Transition from low to high  $Q^2$ ?

Matching of TMD factorization with hadronic description?

Dynamical origin of soft  $P_{hT}$ ?

- Characteristics of small and large  $x$ ?

$x \gtrsim 0.1$ : Non-singlet structures: valence quarks, non-perturbative sea

$x \ll 0.1$ : Singlets dominate, large radiative parton densities

↑ **Measurements**

↑ **Knowledge of non-perturbative dynamics**

# Measurements: Hadron multiplicity distributions 5

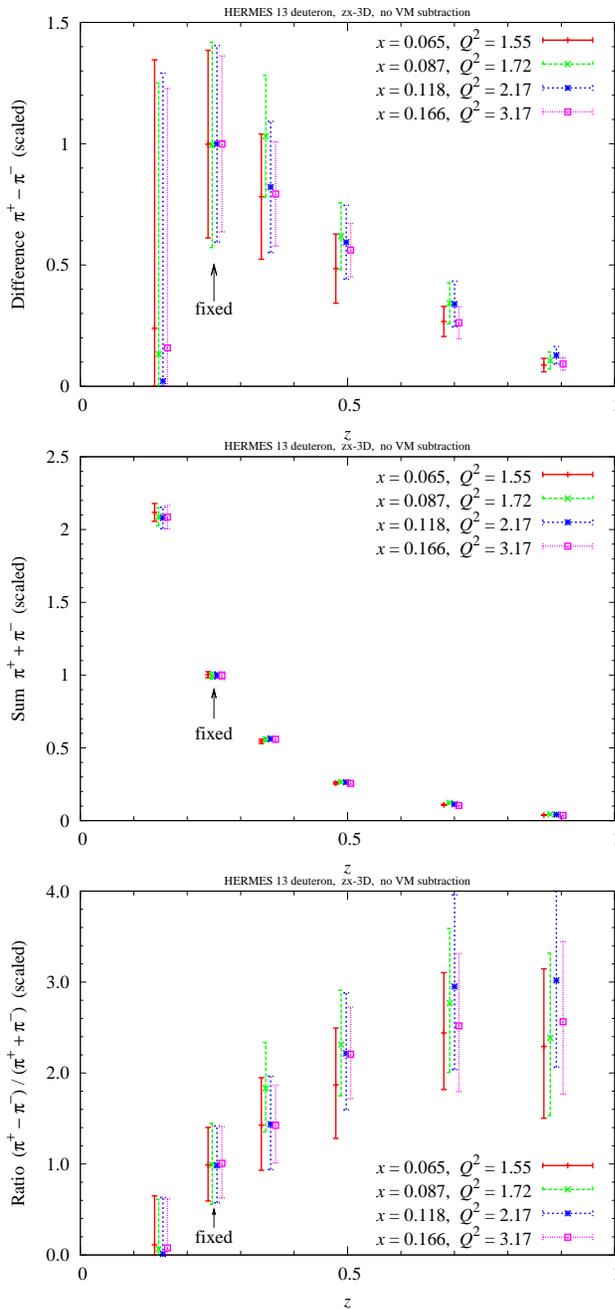
- Unpolarized hadron multiplicity distributions are the basic material for studying the mechanisms of  $P_{Th}$  generation and the applicability of TMD factorization.

Publication of HERMES and COMPASS multiplicities was major advance!

- Need distributions differential in  $W, Q^2, z, P_{Th}$  ← QED rad corr
- Need actual  $P_{Th}$  distributions, not just Gaussian slopes at low  $P_{Th}$ . Tail at  $P_{Th} \sim \text{few GeV}$  carries important pert & non-pert information
- Need flexible binning, cf. HERMES multiplicity downloader

Experiment	$W$ [GeV]	$Q^2$ [GeV <sup>2</sup> ]	$x$
HERA H1 Alexa13		5 – 100	$10^{-4} - 10^{-2}$
HERA ZEUS Derrick95	75 – 175	10 – 160	$10^{-4} - 10^{-2}$
E665 Adams97	7.5 – 30	0.15 – 20	$1.5 \times 10^{-4} - 0.6$
EMC Ashman91	6 – 20	2 – 250	0.01 – 1
COMPASS Adolph13	6 – 15	1 – 10	0.004 – 0.12
HERMES Airapetian12		1 – 15	0.023 – 0.6
JLab6 Hall C Mkrtchyan07		2 – 4	0.2 – 0.5
JLab6 CLAS Osipenko08		2 – 7	0.1 – 0.8

Summary of  $eN/\mu N$  DIS experiments reporting hadron multiplicity distributions



- Combined multiplicities  $\pi^+ \mp \pi^-$

$$N(\pi^+ - \pi^-) \propto [\sum \text{PDFs}](x) \times [D_{\text{fav}} - D_{\text{unf}}](z)$$

$$N(\pi^+ + \pi^-) \propto [\sum' \text{PDFs}](x) \times [D_{\text{fav}} + D_{\text{unf}}](z)$$

$$D_{\text{fav}} \equiv D_{u \rightarrow \pi^+}, \quad D_{\text{unf}} \equiv D_{u \rightarrow \pi^-} \quad \text{etc.}$$

Separate unfavored and favored FFs.  
Model-independent!

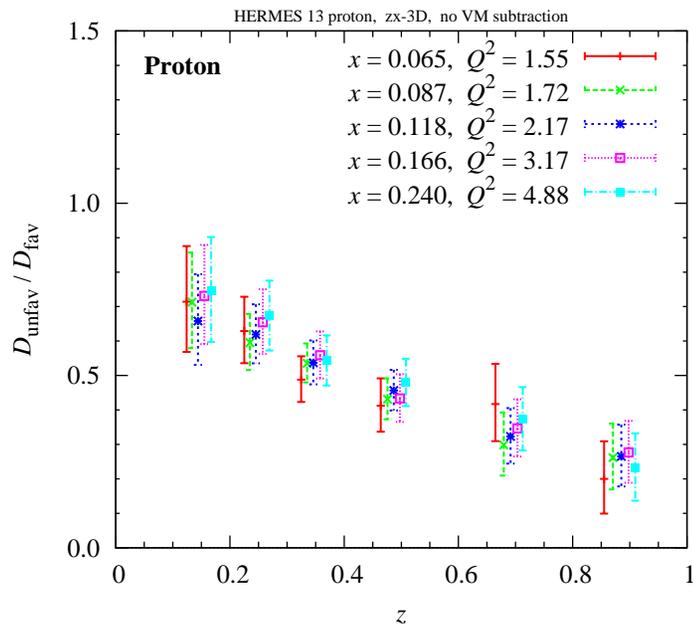
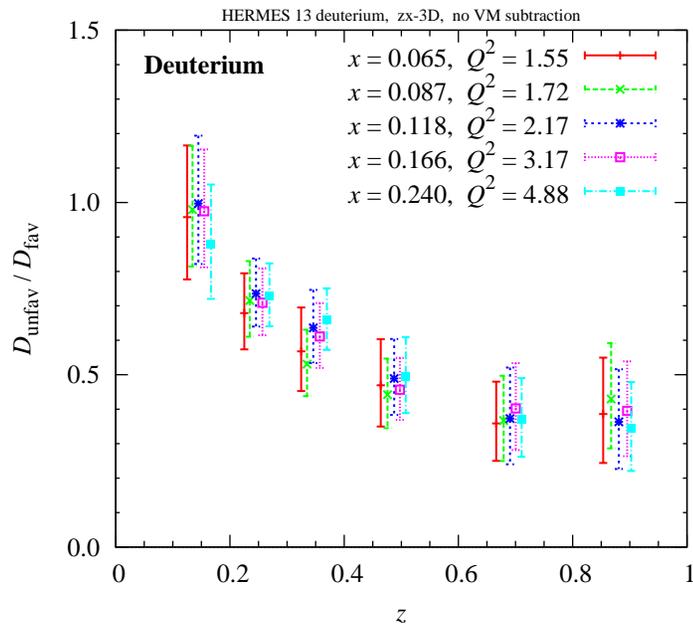
Use deuteron and proton data  
Strangeness can be included

- Phenomenological analysis

HERMES 2012 data. Strikman, CW 14/16

$x$  and  $z$  dependences factorize ✓

Data reveal different shapes of unfavored and favored FFs ✓



- Unfavored/favored FF ratio extracted from  $\pi^+ \mp \pi^-$  data

Reasonable agreement between deuteron and proton data

Ratio surprisingly large at  $z > 0.5$   
Dynamical explanation?

Simple analysis: Just plotting data

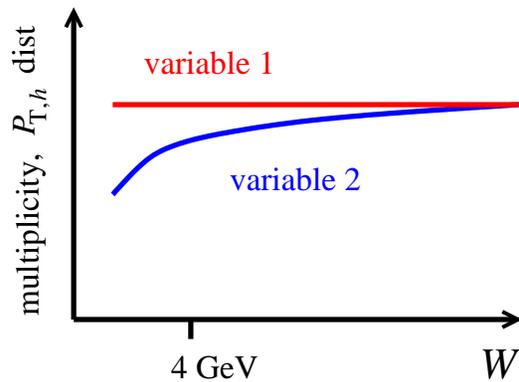
- Could be extended to  $P_T$ -dependent multiplicities

- Alt method: Convolution model fits

Torino group: Prokudin et al.; Bacchetta et al. 13

# Measurements: Kinematic variables for lower $W$ 8

- Rich SIDIS data will become available at  $W \lesssim 4$  GeV with JLab12.  
Kinematics challenging for independent fragmentation or QCD factorization
- Size of apparent “change” of  $P_T$  distributions at low  $W$  depends on choice of longitudinal momentum variable ← QED rad corr



$$z = E_h / \nu$$

energy fraction rest frame

$$x_L = P_{hL} / P_{hL}^{\max}$$

momentum fraction CM

$$\eta = \frac{1}{2} \log P_h^+ / P_h^-$$

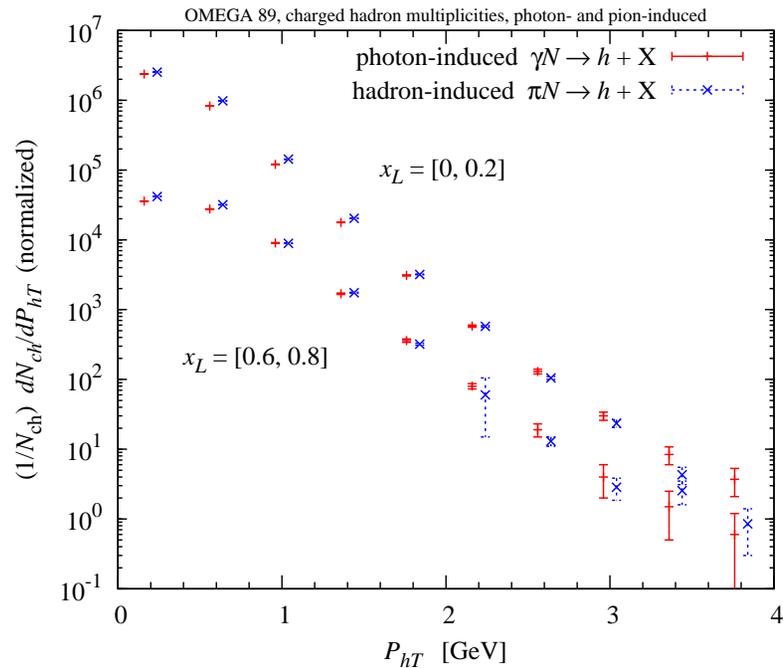
rapidity

$$\zeta = P_h^+ / P_{\text{target}}^+$$

light-cone fraction

- Effect of different choices can be studied using data at higher  $W$  and/or MC simulations (are they accurate enough?)
- Theoretical models of low- $W$  corrections are ambiguous:  
No separation between “kinematic” and “dynamical” effects

# Measurements: Transition low to high $Q^2$ in SIDIS



CERN OMEGEGA 89 data

Similar plots should be made with low- $Q^2$  electroproduction data, comparison at fixed  $W$

- Dynamical origin of low- $P_T$  hadrons in DIS at  $Q^2 \sim \text{few GeV}^2$ ?

Non-perturbative dynamics?

Soft gluon radiation – CSS evolution?

- Explore transition between  $Q^2 = 0$  and  $Q^2 \sim \text{few GeV}^2$

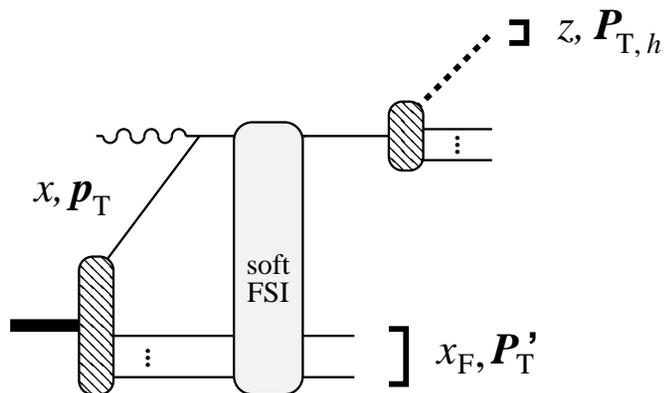
Photo- and hadroproduction have similar  $P_{hT}$  distributions

Expect smooth transition between photo-production and  $Q^2 \sim \text{few GeV}^2$

Successful studies of soft-hard transition at HERA: inclusive, exclusive, diffractive

- Enable hadronic modeling of  $P_T$  distributions at  $Q^2 \sim \text{few GeV}^2$

Initial condition of CSS evolution



- What is source of observed hadron  $P_{T,h}$ ?

Intrinsic  $p_T$  in WF  
 Final-state interaction  
 Parton fragmentation

} obs.  $P_{T,h}$

Cannot separate different sources with single-inclusive measurements alone

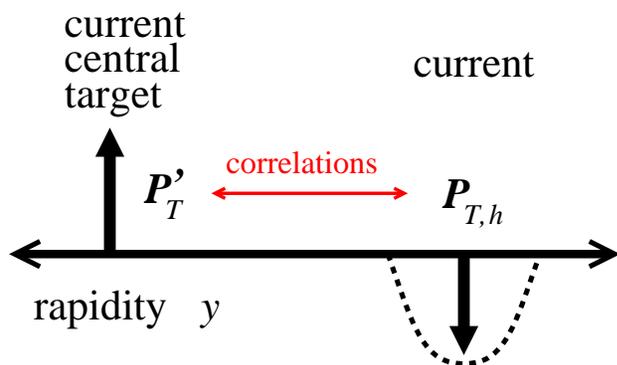
- Correlation measurements

What “balances” observed  $P_{T,h}$ ?

Is  $P_{T,h}$  balanced by broad distribution or single back-to-back hadron?

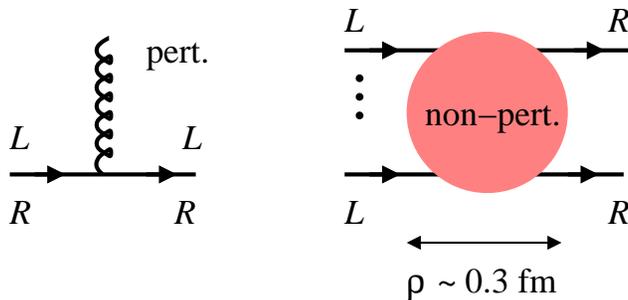
Where in rapidity is it balanced:  
 Current, central, or target region?

Dynamical pictures: String fragmentation, parton short-range correlations



- Next-generation SIDIS measurements

JLab12, EIC



- Chiral symmetry breaking

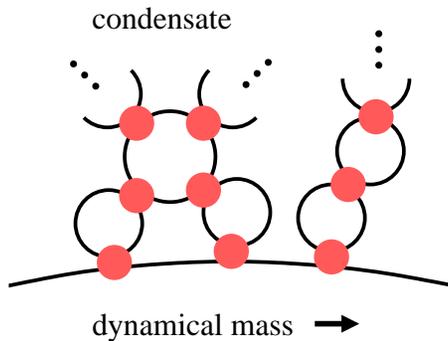
Non-perturb. gluon fields can flip chirality

Condensate of  $q\bar{q}$  pairs  $\langle \bar{\psi}_L \psi_R + \bar{\psi}_R \psi_L \rangle$ , pion as collective excitation – Goldstone boson

Dynamical mass generation:

Constituent quarks, hadron structure

Euclidean correlation functions → Lattice, analytic methods



- Short-range interactions  $\rho \sim 0.3 \text{ fm}$

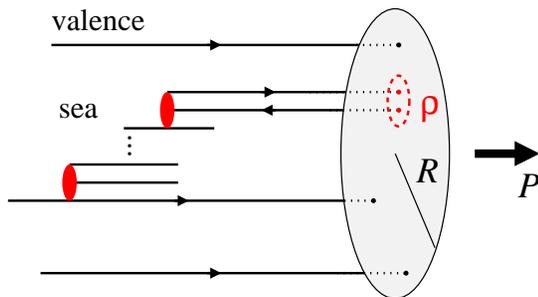
New dynamical scale  $\rho \ll R$

Shuryak; Diakonov, Petrov 80's

Gauge-invariant measure of  $q\bar{q}$  pair size

$\langle \bar{\psi} \nabla^2 \psi \rangle / \langle \bar{\psi} \psi \rangle \sim 1 \text{ GeV}^2$  “average virtuality”

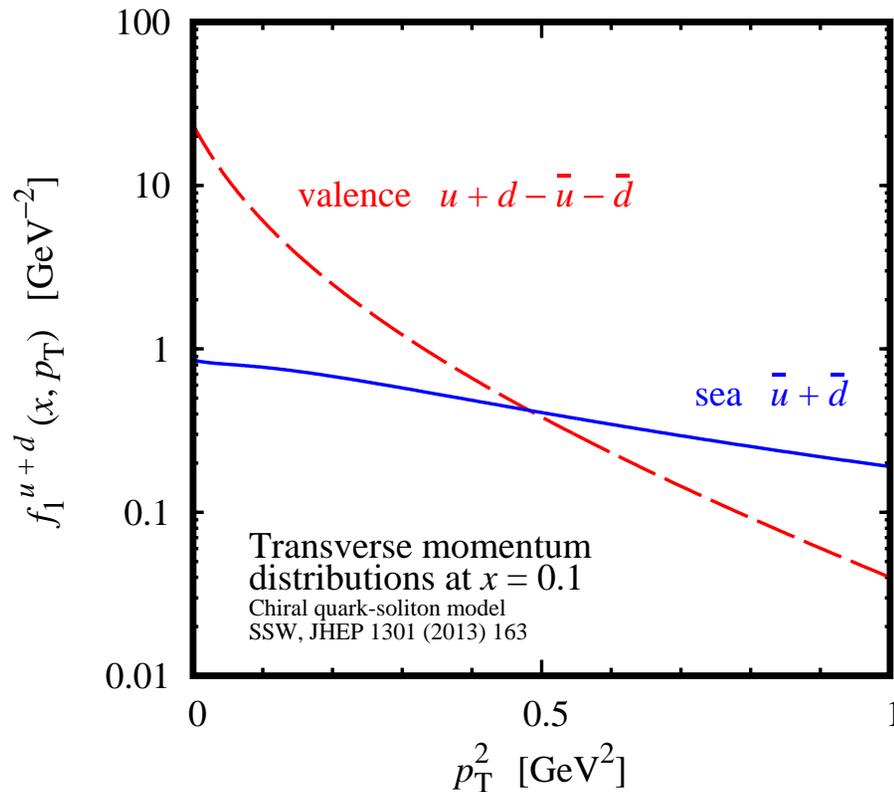
Lattice: Teper 87, Doi 02, Chiu 03. Instantons: Polyakov, CW 96



- How does it affect partonic structure?

Valence quark mostly in configurations of size  $\sim R$

Sea quarks in correlated pairs of size  $\lesssim \rho$



$$f^{\bar{u}+\bar{d}}(x, p_T) \sim \frac{C^{\bar{u}+\bar{d}}(x)}{p_T^2 + M_{\text{const}}^2}$$

Power-like tail of sea quarks

- Dynamical model of  $\chi$ SB

Diakonov, Eides 83; Diakonov, Petrov 86

Effective degrees of freedom:

Constituent quarks, Goldstone bosons

Strongly coupled system, solved

non-perturbatively in  $1/N_c$  expansion

Nucleon as chiral soliton

PDFs at scale  $\mu^2 \sim \rho^{-2} \approx 0.5 \text{ GeV}^2$

- Transverse momentum distributions

Schweitzer, Strikman, Weiss, JHEP 1301 (2013) 163

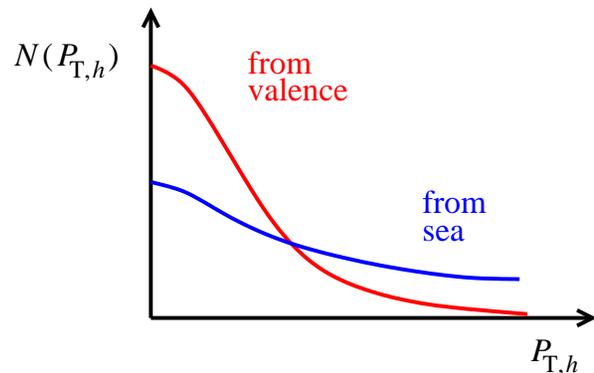
Valence quarks: Drops steeply,  
 $\langle p_T^2 \rangle \approx 0.15 \text{ GeV}^2 = O(R^{-2})$

Sea quarks: Power-like tail extends  
up to cutoff scale  $\rho^{-2}$

Generic feature, rooted in  $\chi$ SB  
and dynamical scales  $\rho \ll R$

Similar tail in  $\Delta\bar{u} - \Delta\bar{d}$

# Dynamics: Non-perturbative $p_T$ consequences



- SIDIS: Different  $P_{T,h}$  distributions of hadrons produced from valence and sea quarks

Schweitzer, Strikman, CW 13

$$\begin{aligned} \pi^+ - \pi^- &\sim u - \bar{u}, \quad d - \bar{d} && \text{valence} \\ \pi^+ + \pi^- &\sim u + \bar{u}, \quad d + \bar{d} && \text{valence} + \text{sea} \end{aligned}$$

$$K^+ \sim u \quad \text{mostly valence}$$

$$K^- \sim \bar{u} \quad \text{sea}$$

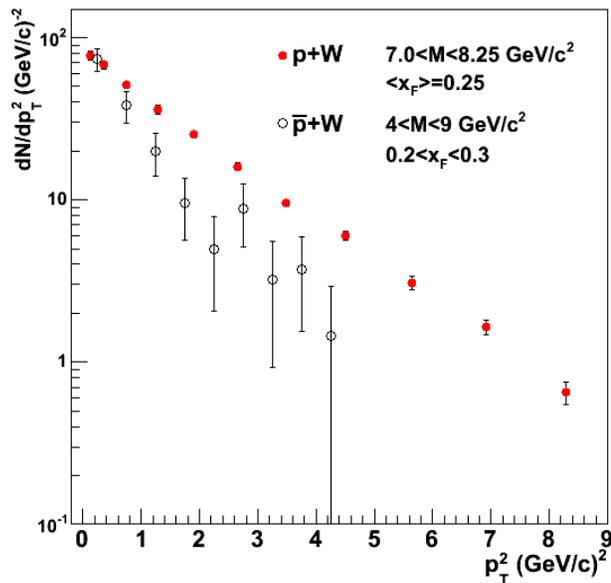
Need better understanding of fav/unfav FF at  $z > 0.5$  to make quantitative predictions

- Dileptons: Different  $P_{T,\text{pair}}$  distns in  $pp/\bar{p}\bar{p}$

$$\begin{aligned} pp & \text{ valence} \times \text{sea} && x_{1,2} \gtrsim 0.1 \\ \bar{p}\bar{p} & \text{ valence} \times \text{valence} \end{aligned}$$

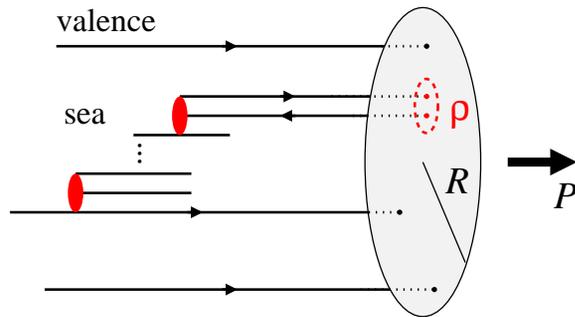
Need  $pp/\bar{p}\bar{p}$  in same kinematics,  $P_{T,\text{pair}} \lesssim 1 \text{ GeV}$

- Large  $p-n$  differences, isovector structures, in longitud. polarized SIDIS at  $P_{T,h} \gtrsim 1 \text{ GeV}$



$P_T(pp) > P_T(\bar{p}p)$  seen in FNAL DY data  
Aidala, Field, Gamberg, Rogers 14

- Parton short-range correlations

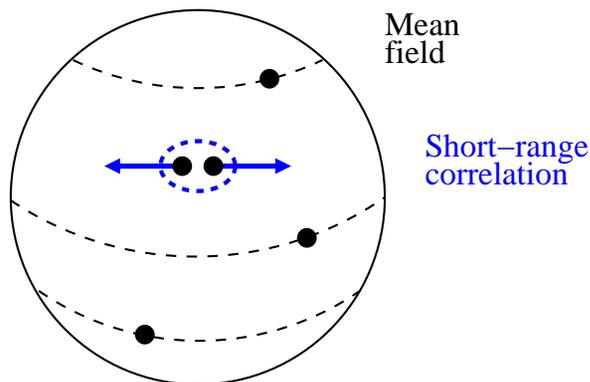


Sea quarks in nucleon LC wave function in correlated pairs of size  $\rho \ll R$   
Explains high-momentum tail of  $p_T$  distribution

Pairs have distinctive spin-isospin structure: Scalar-isoscalar  $\sigma$ , pseudoscalar-isovector  $\pi$

Restoration of chiral symmetry at high  $p_T$ :  
 $|\Psi_\sigma|^2 = |\Psi_\pi|^2$  at  $p_T^2 \sim \rho^{-2}$

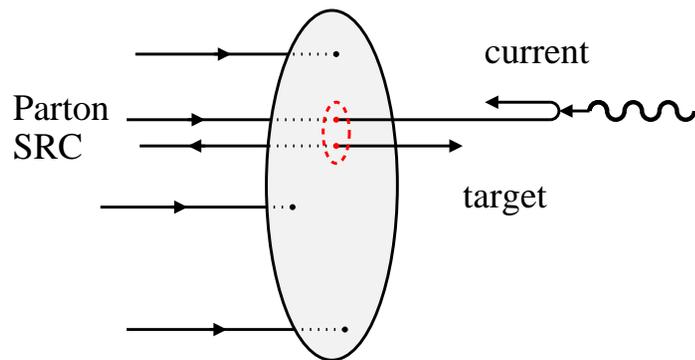
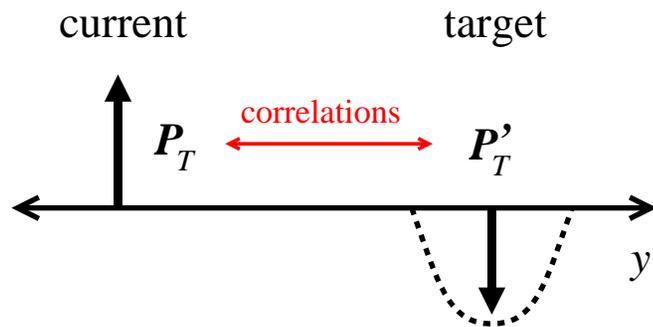
- Cf.  $NN$  short-range correlations in nuclei



Mean field  $\Psi(\mathbf{r}_1, \dots, \mathbf{r}_N) \approx \prod_i^N \Phi(\mathbf{r}_i)$

Rare configs with  $|\mathbf{r}_i - \mathbf{r}_j| \ll$  average experience short-range  $NN$  interaction, generate high momentum components

Indirect probes: Momentum distributions,  $x > 1$   
Direct probes:  $(e, e'NN)$  in special kinematics  
JLab Hall A, CLAS, Hall C at 12 GeV



- Back-to-back  $P_T$  correlations between hadrons in current and target regions

Require special kinematics

Other possible sources of correlations

- Kinematics for nonperturbative correlations

Sufficient separation in rapidity

$$\Delta y \approx \ln[W^2 / (P_{T,h}^2 + m_h^2)] \gtrsim 4$$

Moderate virtuality to avoid pQCD radiation

$$Q^2 \sim \text{few GeV}^2$$

Momentum fractions of nonperturbative sea

$$x \sim 0.05\text{--}0.1$$

→ “Kinematic window” at  $W^2 \approx 30 \text{ GeV}^2$ ,  
 $P_{T,h}^2 \approx 0.5 \text{ GeV}^2$

COMPASS: Detection of target fragments?

EIC: Medium energies ideal

JLab12: Probably marginal, but should be explored

# Summary

- Determining the dynamical origin of soft hadron  $P_T$  in SIDIS remains challenging . . . very interesting problem!
- Unfavored fragmentation looks surprisingly strong at  $z \gtrsim 0.5$  and  $P_T \sim 1 \text{ GeV}$ 
  - Dynamical reason?
  - Impact on TMD extraction?
  - Should be tested with  $e^+e^-$  hadron correlation data
- Qualitative differences predicted between non-perturbative  $p_T$  distributions of valence and sea quarks
- Unpolarized SIDIS multiplicity data with separated dependences and flexible binning are essential for further progress, together with Drell-Yan,  $e^+e^-$ , and photo/hadroproduction data
- Large  $p-n$  difference (isovector) expected in longit. pol. SIDIS at  $P_T \gtrsim 1 \text{ GeV}$