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# Time-like Compton Scattering

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**S. Stepanyan (JLAB)**

**Workshop on probing small-size configurations in  
high-t photo/electroproduction**

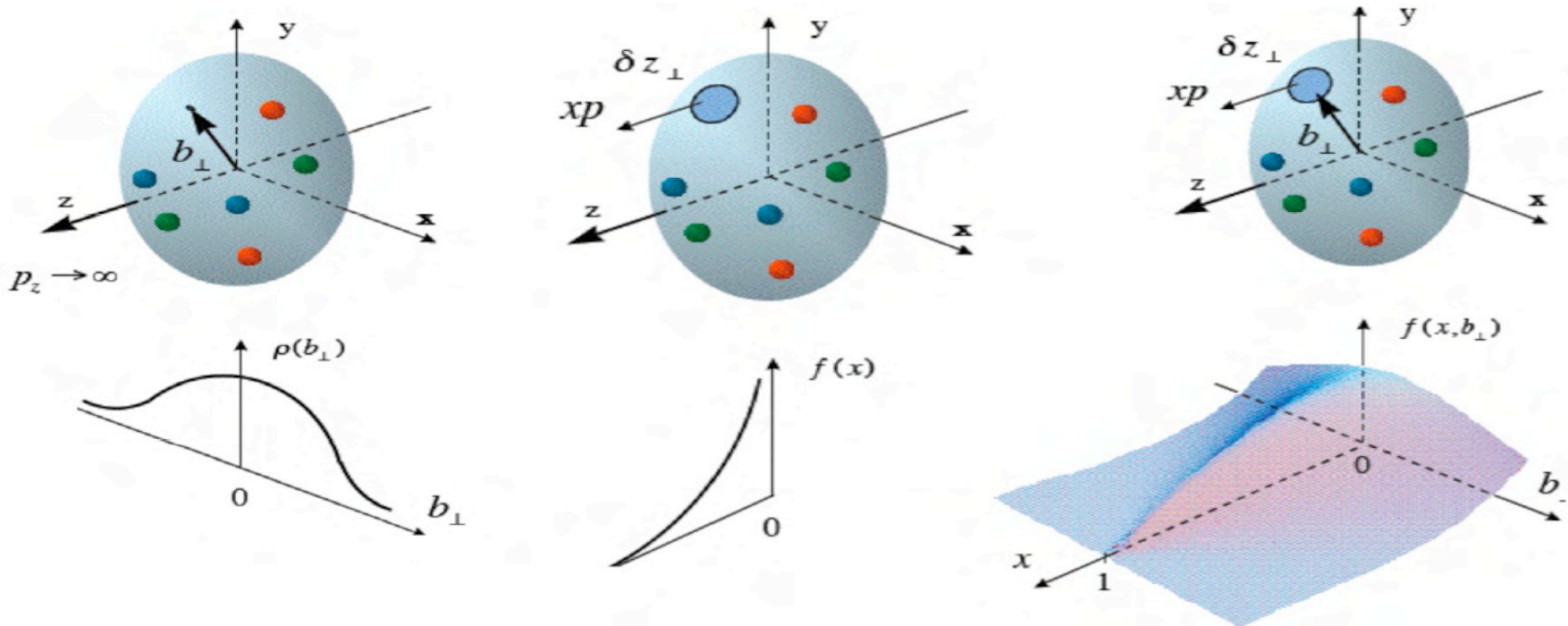
**JLAB, March 25-26, 2011**



- GPDs, DVCS, and nucleon structure
- Extraction of GPDs from Experimental Data
- TCS phenomenology and observables
- Quasi-real Photoproduction of lepton pairs in CLAS
- Perspectives for CLAS12
- Summary



# GPDs and Nucleon Structure



## Elastic Form Factors –

characterize charge and magnetization distributions in the impact parameter space

## DIS Parton Distribution Functions -

discovery of the quark and gluon substructure of the nucleon, with quarks carrying  $\frac{1}{2}$  of the nucleon's momentum and  $\sim 25\%$  of its spin

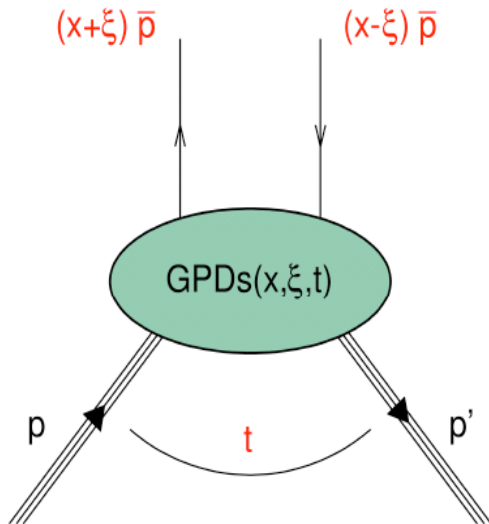
## Generalised Parton

**Distributions –** 3-D imaging of the nucleon, the correlation of quark/antiquark transverse spatial and longitudinal momentum distributions, and on the quark angular momentum distribution



# Determination of GPDs

## Boundary conditions



Four chiral-even GPDs:

$$H^q; E^q; \tilde{H}^q; \tilde{E}^q$$

- **GPDs**  $\rightarrow$  PDFs (in the limite  $t \rightarrow 0$ )

$$H^q(x, 0, 0) = q(x), -\bar{q}(-x)$$

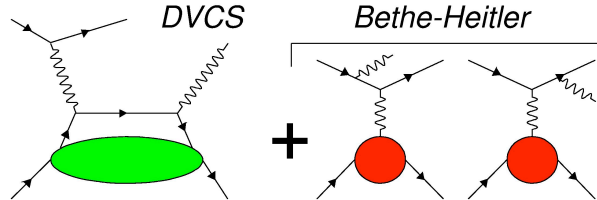
$$\tilde{H}^q(x, 0, 0) = \Delta q(x), \Delta \bar{q}(-x)$$

- **GPDs**  $\rightarrow$  FFs (first moments of GPDs)

$$\int_{-1}^{+1} dx H^q(x, \xi, t) = F_1^q(t) \quad \int_{-1}^{+1} dx \tilde{H}^q(x, \xi, t) = g_A^q(t)$$

$$\int_{-1}^{+1} dx E^q(x, \xi, t) = F_2^q(t) \quad \int_{-1}^{+1} dx \tilde{E}^q(x, \xi, t) = h_A^q(t)$$

# Accessing GPDs experimentally (DVCS)

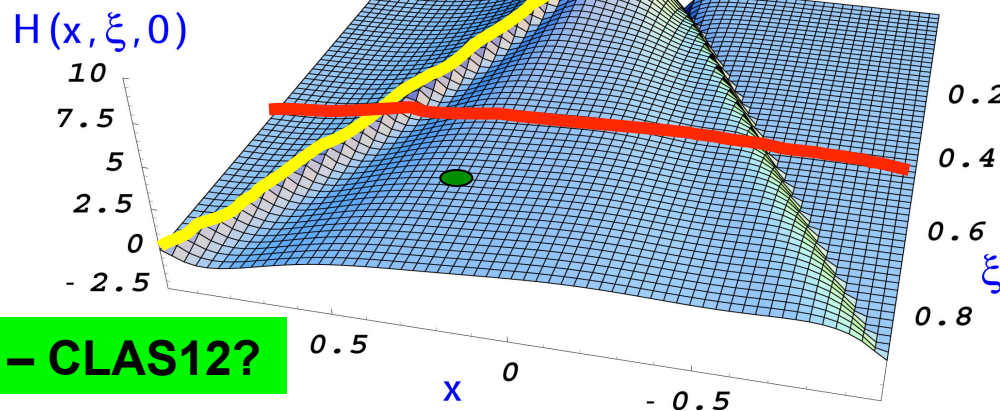
$ep' e\gamma =$ 


$$\mathcal{T} = |\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2 + \mathcal{T}_{DVCS}^* \mathcal{T}_{BH} + \mathcal{T}_{BH}^* \mathcal{T}_{DVCS}$$

$$\mathcal{H}(\xi, t) = \underbrace{i\pi [H(\xi, \xi, t) - H(-\xi, \xi, t)]}_{\text{Im}} + \text{P} \int_{-1}^{+1} dx \left( \frac{1}{\xi - x} \pm \frac{1}{\xi + x} \right) \underbrace{[H(x, \xi, t) \mp H(-x, \xi, t)]}_{\text{Re}}$$

**Spin asymmetries (Im,  $x=\xi$ )**  
HERMES, CLAS, Hall A

**Charge asymmetry ( $|\text{Re}|$ )**  
HERMES



**Cross sections ( $|\text{Re}|^2$ )** H1, Hall A

**DDVCS (Im,  $x \neq \xi$ )** – CLAS12?

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# Revealing GPDs

The extraction of GPDs from experimental data will require:

- extensive experimental program [with polarized beam/targets] (CLAS12)

and

- the phenomenological parameterization of GPDs

Commonly used parameterization uses factorized ansatz for the  $t$ -dependence: e.g. the Regge parameterization  $\sim x^{-\alpha t}$



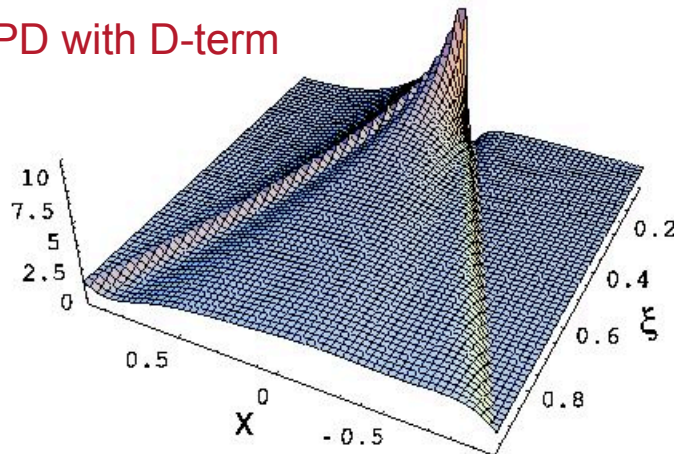
# Parameterization of GPDs

DD-distributions

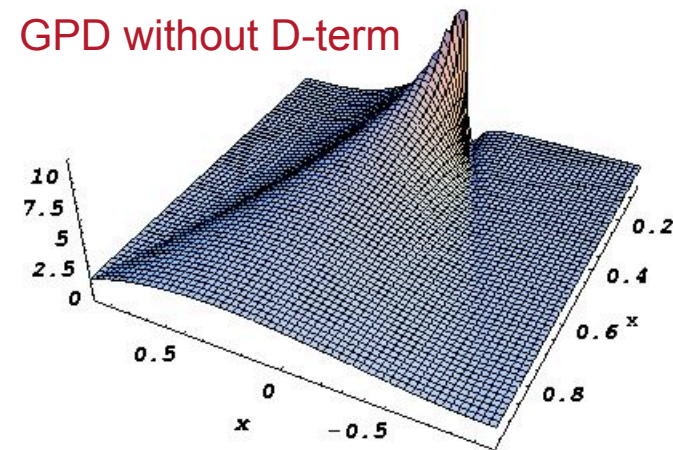
$$H^q(x, \xi) = H_{DD}^q(x, \xi) + \theta(\xi - |x|) \frac{1}{N_f} \mathbf{D}\left(\frac{x}{\xi}\right)$$

**D-term** – to satisfy polynomiality of Mellin moments of GPD

GPD with D-term



GPD without D-term



**Real part of the Compton amplitude is very sensitive to the D-term**

# Extracting the GPDs

Global fit to the DVCS data, using models of GPDs - M. Guidal, Eur.Phys.J. **A37**, p319 (2008)

8 independent quantities to be fit -

$$\text{Im}(\mathbf{H}); \text{Im}(\mathcal{E}); \text{Im}(\tilde{\mathbf{H}}); \text{Im}(\tilde{\mathcal{E}})$$

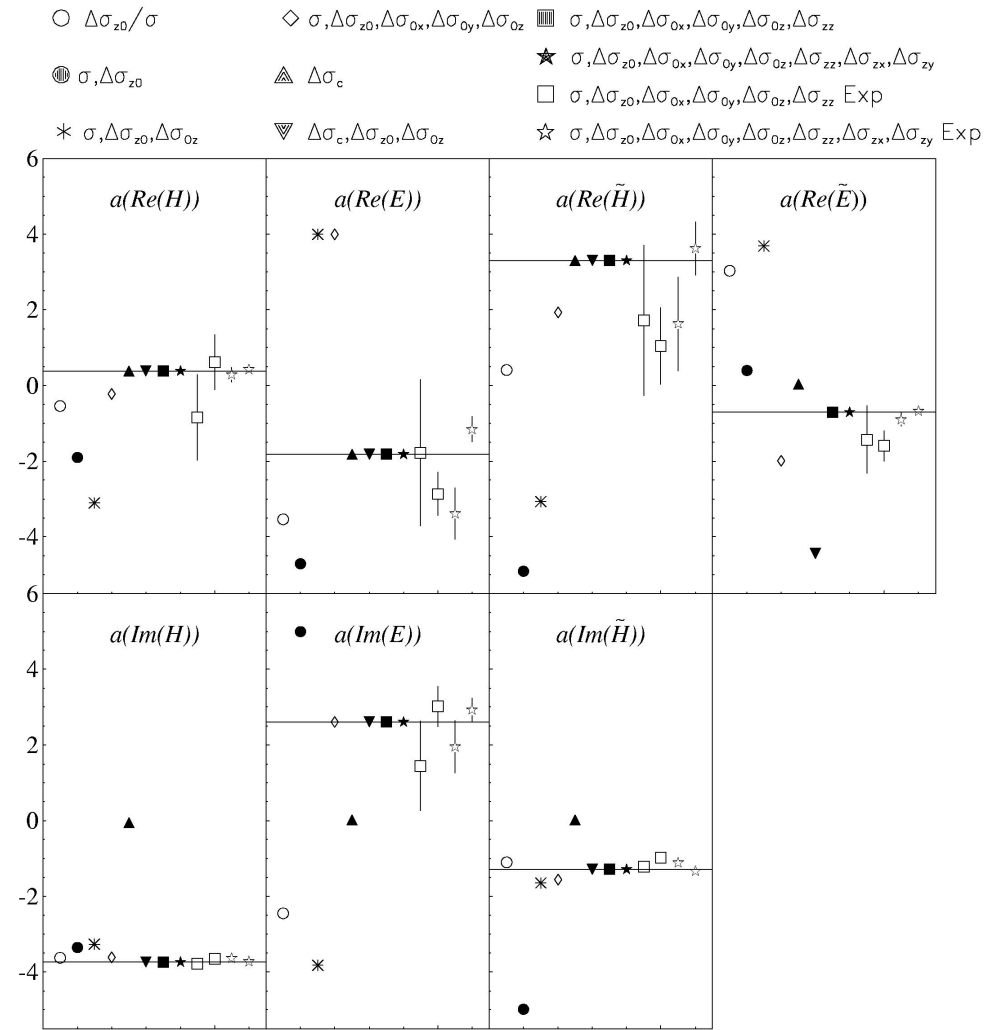
$$\text{Re}(\mathbf{H}); \text{Re}(\mathcal{E}); \text{Re}(\tilde{\mathbf{H}}); \text{Re}(\tilde{\mathcal{E}})$$

Using 9 independent observables -

$$\sigma; \Delta\sigma_{z0}; \Delta\sigma_{0x}; \Delta\sigma_{0y}; \Delta\sigma_{0z};$$

$$\Delta\sigma_{zx}; \Delta\sigma_{zy}; \Delta\sigma_{zz}; \Delta\sigma_c;$$

Assumption -  $\text{Im}(\tilde{\mathcal{E}}) = 0$





# Conclusions from the fits

- In general, with enough observables fit was able to constrain seven GPDs

*There might be possibilities to reduce the number of independent parameters – dispersion relations or model motivated ansatzes*

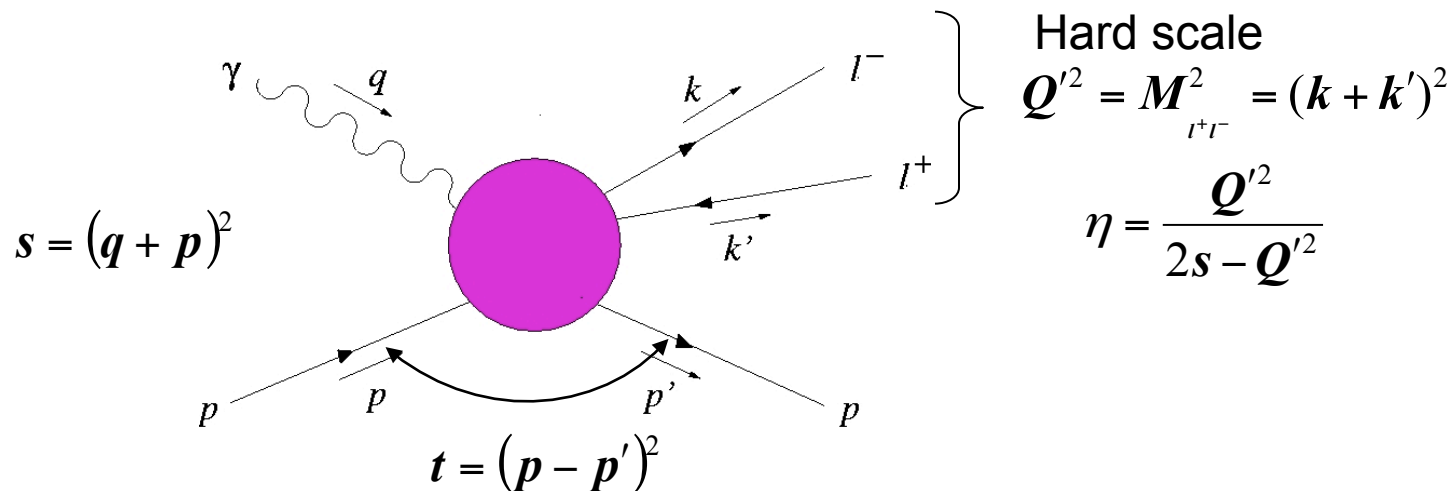
- Imaginary part of CCFs  $\mathcal{H}$  and  $\tilde{\mathcal{H}}$  can be reliably extracted from  $\sigma$ ,  $\Delta\sigma_{z0}$  and  $\Delta\sigma_{0z}$  – planned and ongoing experiments at JLAB
- Real parts of the GPDs can be reliably reconstructed
  - from BCA measurements – **requires lepton beams of both charges**and/or
  - in the combined analysis of several (at least 6) beam and/or target spin asymmetry measurements – **will potentially have large systematic uncertainties and requires huge amount of data**



# Time-like Compton Scattering (TCS)

Information on the real (imaginary) part of the Compton amplitude can be obtained from photoproduction (circularly polarized) of lepton pairs

$$\gamma p \rightarrow p l^+ l^- ; \quad l = e, \mu$$



*TCS is the inverse process to DVCS. Contributions of higher twists are different for DVCS and TCS processes and hence measuring both will help to obtain stronger constraints on GPDs*

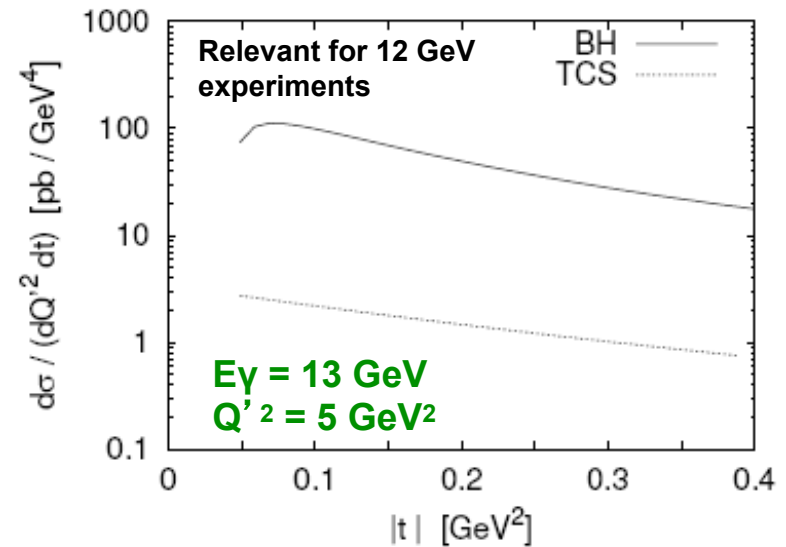
# Lepton pair photo-production

TCS                      Bethe-Heitler (BH)

$$\frac{d^4\sigma}{dx_B dQ^2 dt d\varphi} \propto |T^{BH}|^2 + T^{BH} \cdot \text{Re}(T^{VCS}) + h_{\oplus} T^{BH} \cdot \text{Im}(T^{VCS}) + |T^{VCS}|^2$$

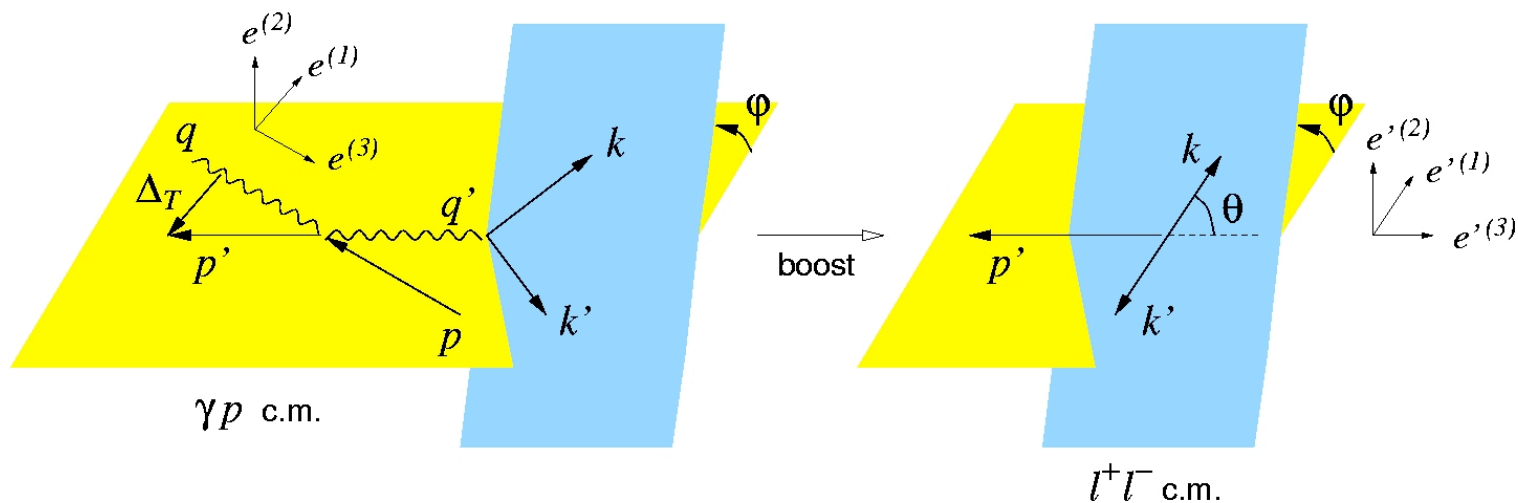
E. Berger et al., hep-ph/0110062

- ❑ BH always dominates in the cross section
- ❑ lepton pair is produced in C-odd state by TCS and in a C-even state by BH, azimuthal angular dependence will project out the interference – analogous to BCA in DVCS



# Interference term and angular harmonics

E. Berger et al., hep-ph/0110062



$$\begin{aligned}
 \frac{d\sigma_{INT}}{dQ^2 dt d(\cos \theta) d\varphi} = & -\frac{\alpha_{em}^3}{4\pi s^2} \frac{1}{-t} \frac{M}{Q'} \frac{1}{\tau\sqrt{1-\tau}} \frac{L_0}{L} \left[ \cos \varphi \frac{1 + \cos^2 \theta}{\sin \theta} \text{Re } \tilde{M}^{--} \right. \\
 & \left. - \cos 2\varphi \sqrt{2} \cos \theta \text{Re } \tilde{M}^{0-} + \cos 3\varphi \sin \theta \text{Re } \tilde{M}^{+-} + O\left(\frac{1}{Q'}\right) \right], \\
 & -\nu \frac{\alpha_{em}^3}{4\pi s^2} \frac{1}{-t} \frac{M}{Q'} \frac{1}{\tau\sqrt{1-\tau}} \frac{L_0}{L} \left[ \sin \varphi \frac{1 + \cos^2 \theta}{\sin \theta} \text{Im } \tilde{M}^{--} \right. \\
 & \left. - \sin 2\varphi \sqrt{2} \cos \theta \text{Im } \tilde{M}^{0-} + \sin 3\varphi \sin \theta \text{Im } \tilde{M}^{+-} + O\left(\frac{1}{Q'}\right) \right]
 \end{aligned}$$

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# Angular dependence

E. Berger et al., hep-ph/0110062

$$\frac{dS}{dQ'^2 dt d\varphi} = \int \frac{L(\theta, \varphi)}{L_0(\theta)} \frac{d\sigma}{dQ'^2 dt d\varphi d\theta} d\theta$$

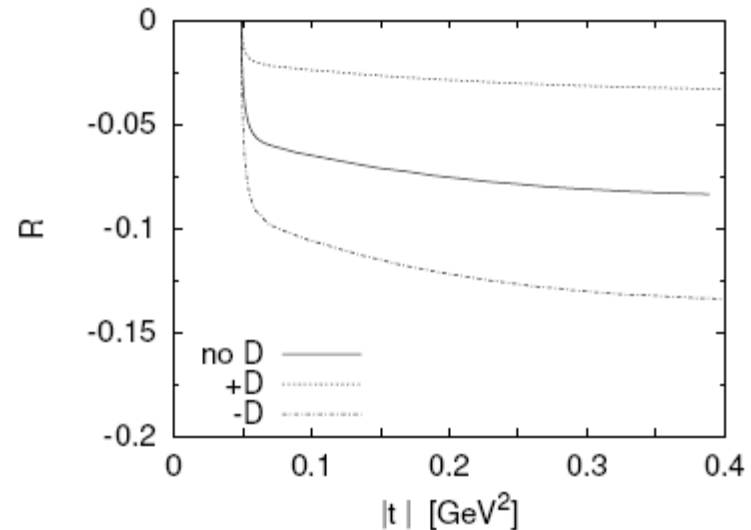
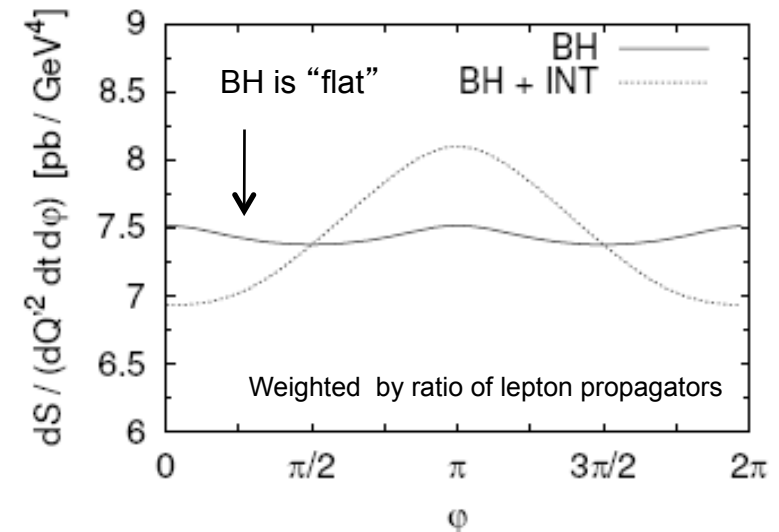
Lepton propagators:

$$L_0 = \frac{Q'^4 \sin^2 \theta}{4};$$

$$L = \frac{(Q'^4 - t)^2 - 4[(k - k')(p - p')]^2}{4}$$

Observable:

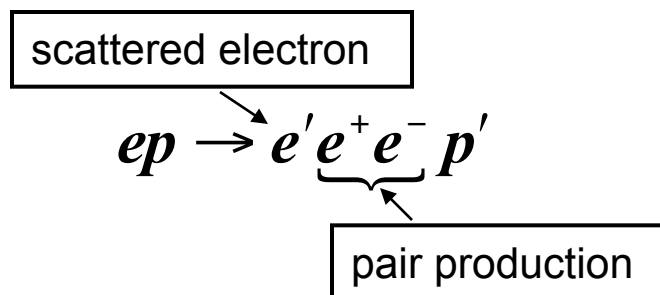
$$R = \frac{2 \int_0^{2\pi} d\varphi \cos \varphi \frac{dS}{dQ'^2 dt d\varphi}}{\int_0^{2\pi} d\varphi \frac{dS}{dQ'^2 dt d\varphi}}$$



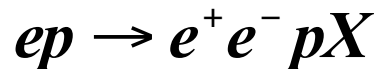
# First TCS analysis from CLAS data

Analysis of electroproduction data to select events in the quasi-real photoproduction region, when incoming electron scatters at  $\sim 0$  degrees

In the production of  $e^+e^-$  pair, there are two electrons in final state



Final state to analyze



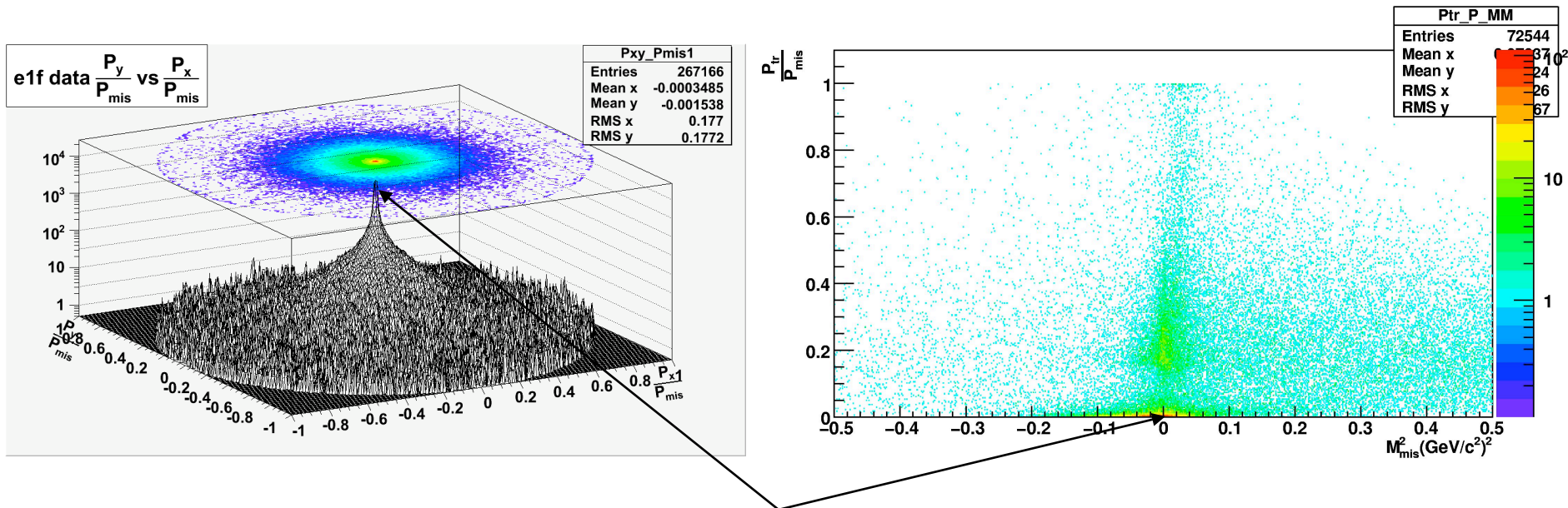
Scattered electron kinematics is deduced from missing momentum analysis



# Quasi-real photoproduction of $e^+e^-$

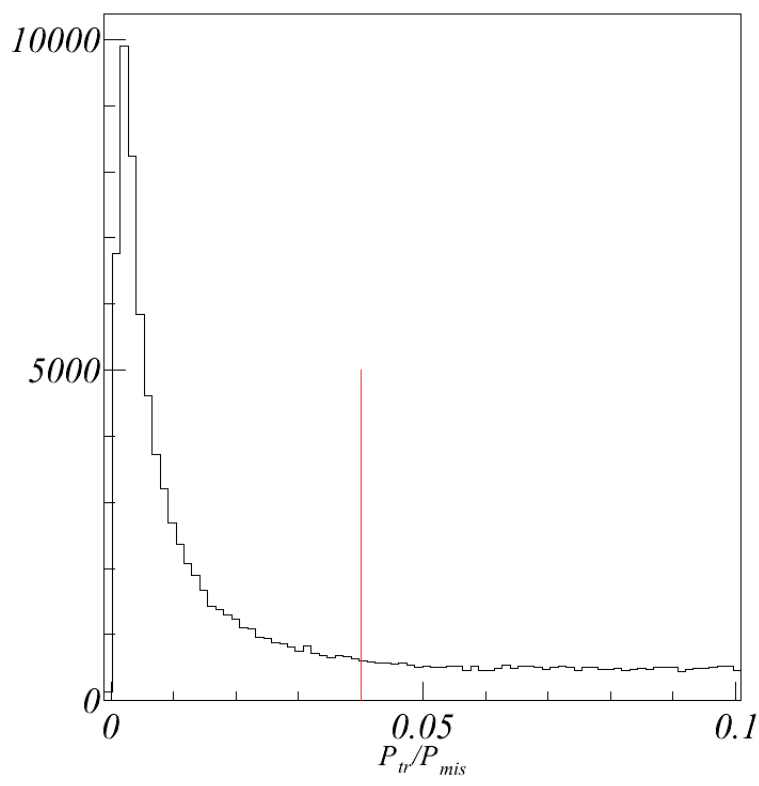
Missing momentum analysis for final state -

$$ep \rightarrow e^+ e^- pX$$



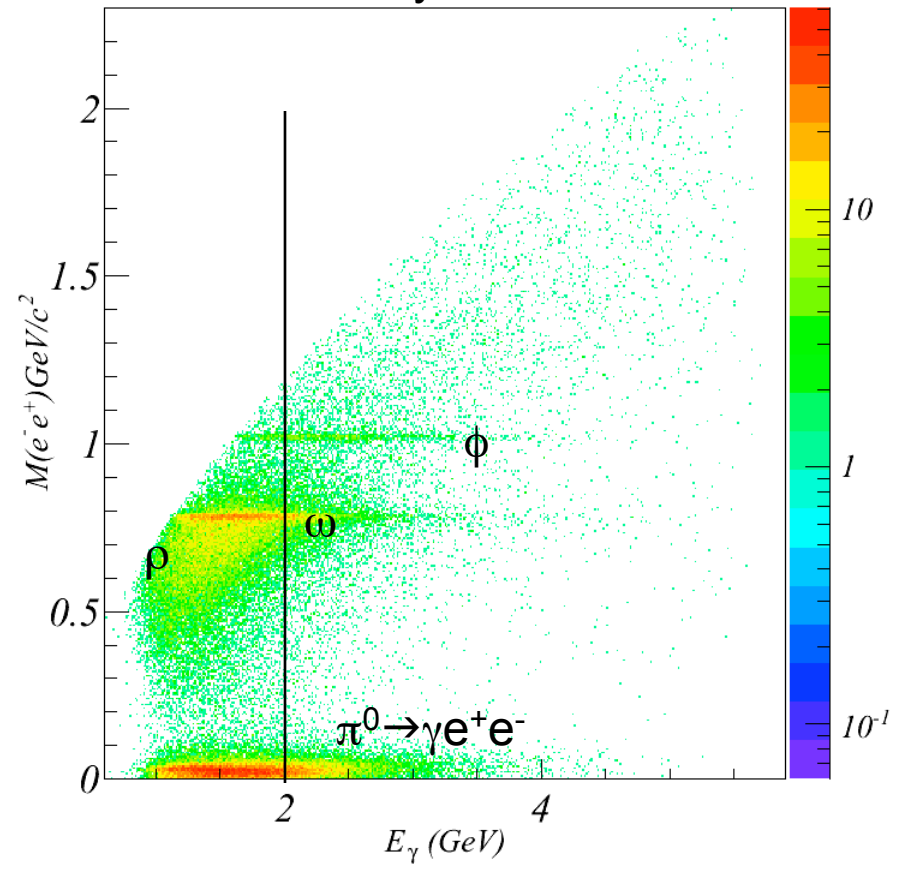
X – is identified as an electron scattered at 0 degrees,  
 $Q^2 < 0.01 \text{ (GeV/c)}^2$  and  $|M_X^2| < 0.1 \text{ (GeV)}^2$

# Selection of events for TCS



Quasi-real photoproduction –  $P_t(Q^2) \sim 0$ , consistent with detector resolution

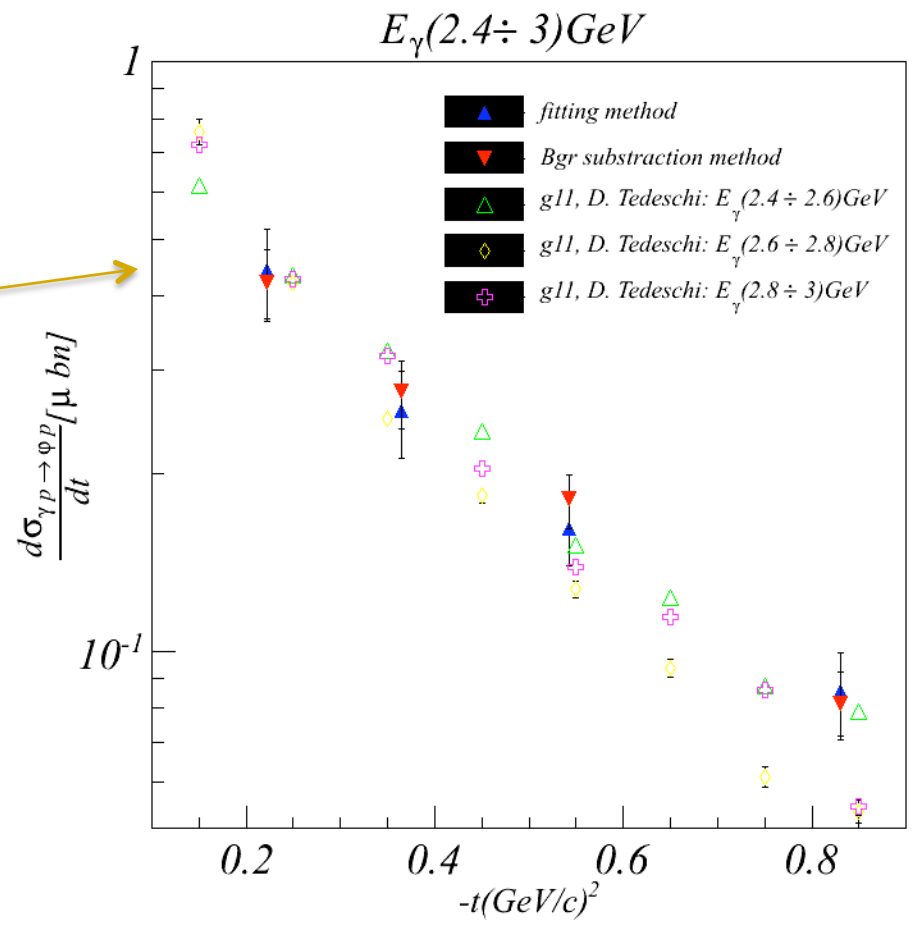
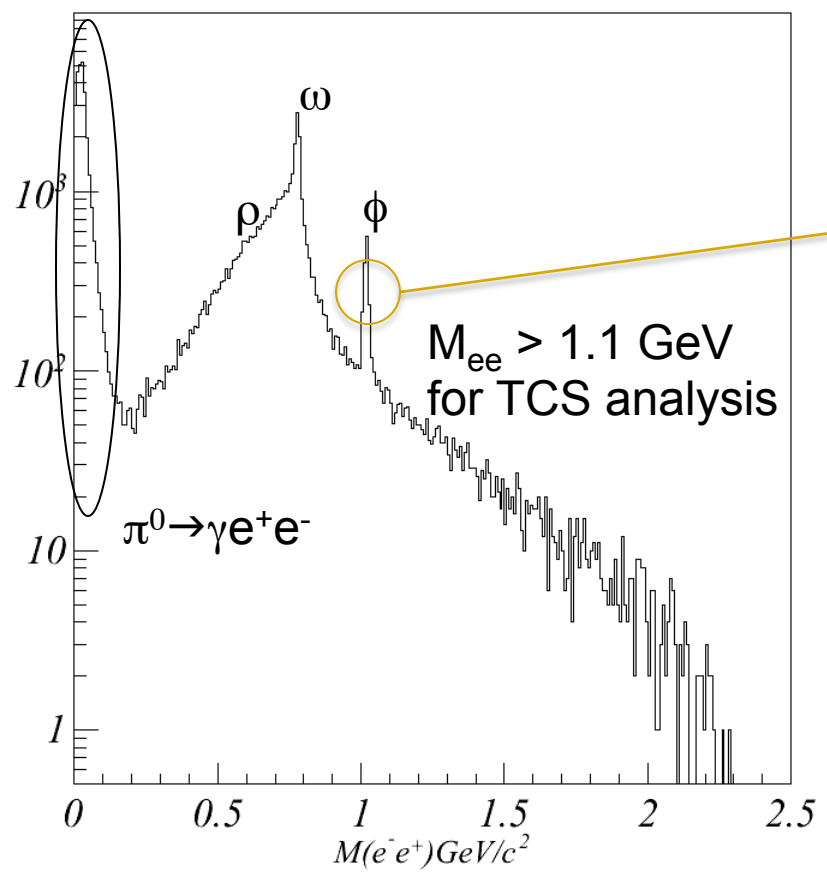
For TCS analysis,  $\sqrt{s} > 2. GeV$





# Photoproduction of lepton pairs

## CLAS/E1-6



Analysis of CLAS e1-6 and e1f data are underway, R. Paremuzyan

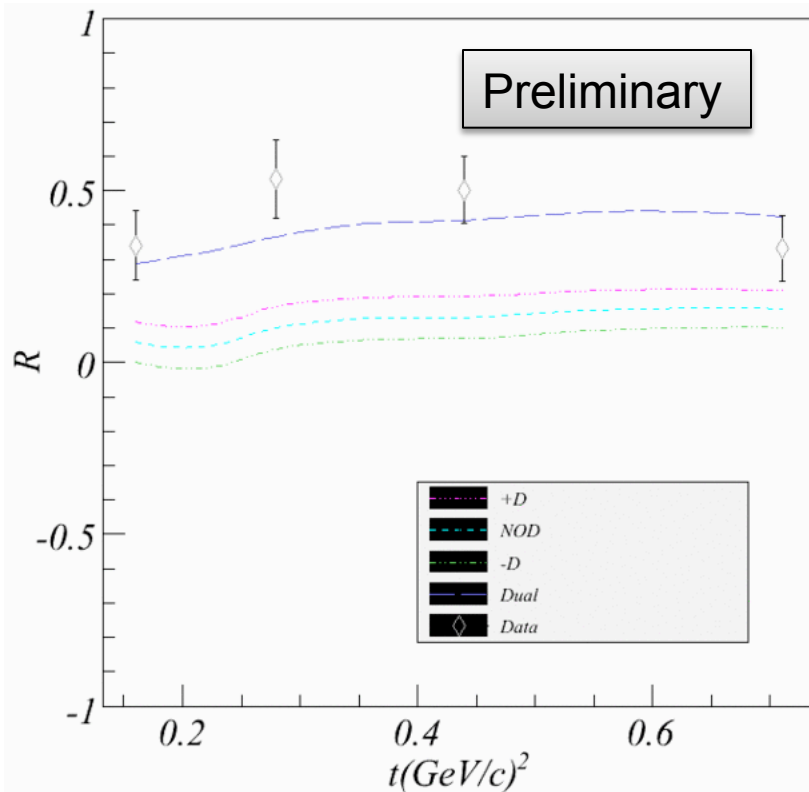


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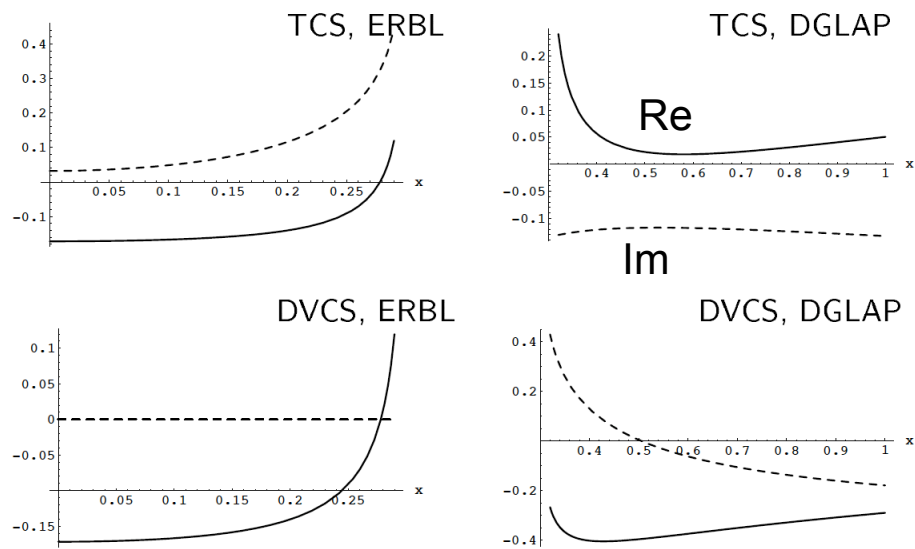


# Angular momentum from CLAS-6 data

LO calculations (Vadim Guzay  
per Berger et al.)



NLO contributions (Lech Szymanowski)

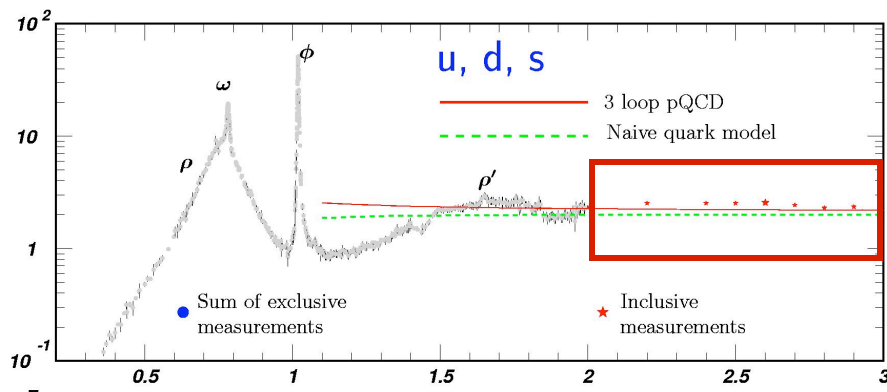


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# TCS with CLAS12

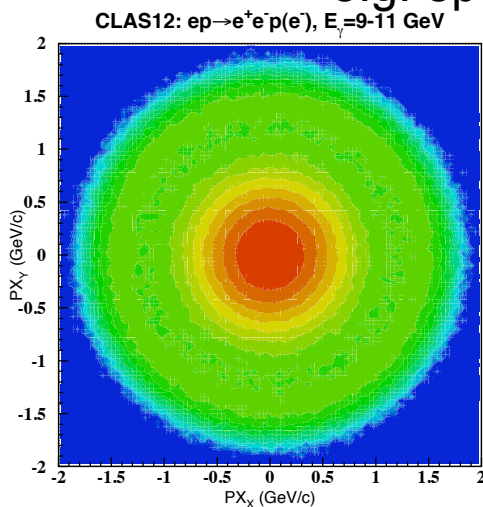


The most suitable region of masses for TCS studies at high energies

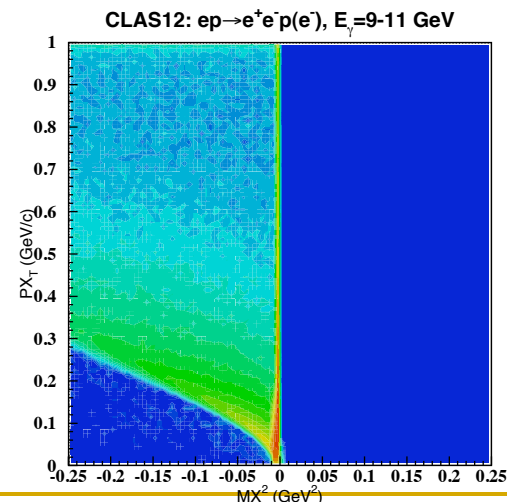
$$\sqrt{s} > 4 \text{ GeV}$$

$$2 \text{ GeV} < M_{ee} < 3 \text{ GeV}$$

Use electroproduction data to extract exclusive photoproduction reactions  
e.g.  $ep \rightarrow e^+e^-p(e^-)$ , ( $e^-$ ) scattered electron at  $\sim 0^\circ$



Simulations of the reaction  $ep \rightarrow BH$ , and  $\rho$ ,  $\omega$ ,  $\phi$  and  $J/\Psi$  with  $\sigma \sim 1/Q^4$  and  $\sigma \sim e^{-3t}$



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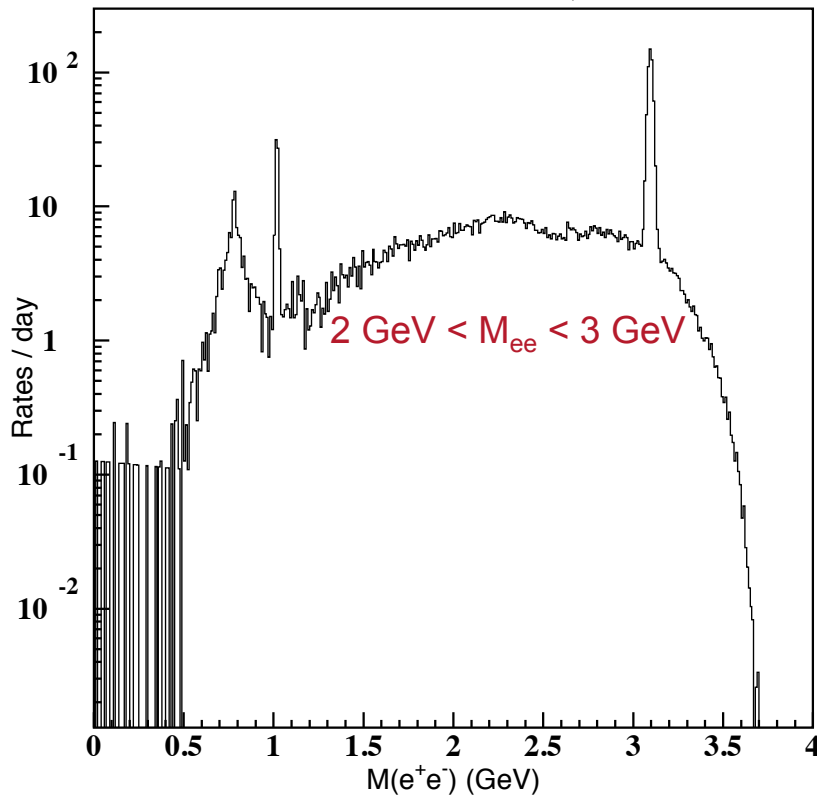


# TCS with CLAS12

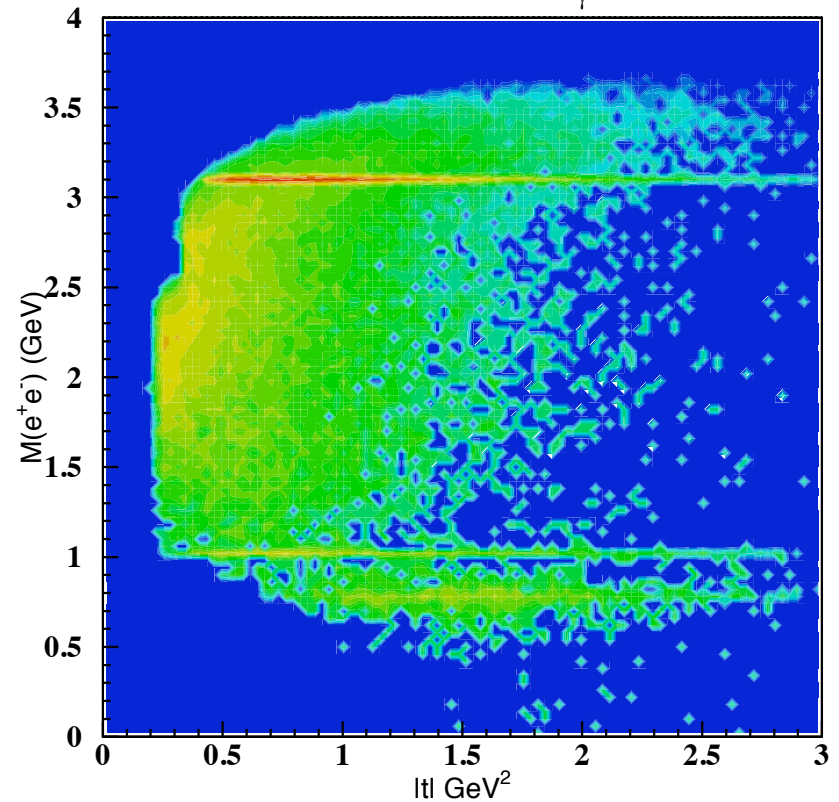
Simulations include V-mesons decay BR to  $e^+e^-$  and photoproduction cross sections

Fiducial acceptance, and momentum and angular smearing of CLAS12 are used

CLAS12:  $ep \rightarrow e^+e^-p(e^-)$ ,  $E_\gamma = 9-11$  GeV



CLAS12:  $ep \rightarrow e^+e^-p(e^-)$ ,  $E_\gamma = 9-11$  GeV



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# TCS with CLAS12

- No real photon beams will be available with  $E_\gamma > \sim 6.6$  GeV
- The same technique can be used - electroproduction of lepton pairs in the quasi-real photoproduction region
- Significant amount of beam time for electroproduction at 11 GeV with CLAS12 is already approved

| Proposal         | Contact Person       | Physics   | Energy (GeV) | PAC days | Parallel Running | Target                   |
|------------------|----------------------|---|--------------|----------|------------------|--------------------------|
| <b>PR-09-103</b> | <i>Gothe, Mokeev</i> | <i><math>N^*</math> at high <math>Q^2</math></i>                | 11           | 60       | 119              | LH2<br>TCS &<br>$J/\psi$ |
| E12-06-119a      | <i>Sabatie</i>       | <i>DVCS pol. beam</i>   | 11           | 80       |                  |                          |
| PR-11-005        | <i>Battaglieri</i>   | <i>Meson Spectroscopy</i>                                       | 11           | 119      |                  |                          |
| E12-06-112       | <i>Avakian</i>       | <i><math>ep \rightarrow e\pi^{+/-0} X</math></i>                | 11           | 60       |                  |                          |
| E12-06-108       | <i>Stoler</i>        | <i>DVMP in <math>\pi^0, \eta</math> prod<br/>L/T separation</i> | 11           | 80       | 20<br>20         |                          |
|                  |                      |   | 8.8          | 20       |                  |                          |
|                  |                      |   | 6.6          | 20       |                  |                          |
| E12-06-117       | <i>Brooks</i>        | <i>Quark Hadronization</i>                                      | 11           | 60       | 60?              | NUCLEAR<br>$J/\psi$      |
| E12-06-106       | <i>Hafidi</i>        | <i>Color transparency</i>                                       | 11           | 60       |                  |                          |

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# Summary

- Huge amount of data with polarized beam and targets will be obtained on DVCS with CLAS12 at beam energies up to 11 GeV
- Nevertheless, DVCS data alone will not be sufficient to fully constrain the GPDs
- Extraction of GPDs from these measurements will require combined analysis, using models of GPDs
- In particular, extraction of the real part of the Compton amplitude will suffer in accuracy if only electroproduction data are used
- The real part of the amplitude can be accessed directly in Beam Charge Asymmetry in DVCS – **requires lepton beams of both polarities**
- The same information can be obtained from azimuthal asymmetries in **Time-like Compton Scattering**
- In addition, with enough statistics, TCS will give complementary information on the imaginary part of the Compton amplitude – advantage, e.g., **different contributions for higher twist effects**



## Summary (cont.)

- Preliminary analysis of CLAS 6 GeV electroproduction data showed feasibility of measuring the TCS in electroproduction experiments

Theoretical support will be greatly appreciated!

Thanks for Vadim

- With CLAS12, data will be available for TCS studies “almost for free” from already approved electroproduction experiments at 11 GeV
- Full proposal for TCS (general  $\gamma A \rightarrow e^+e^-$ , including  $J/\Psi$ ) with CLAS12 is in works, may (will) be submitted to PAC 38

TCS can be also an important reaction to be considered for studying GPDs (gluonic) on EIC, experimentally will be simpler than DVCS



# Backups



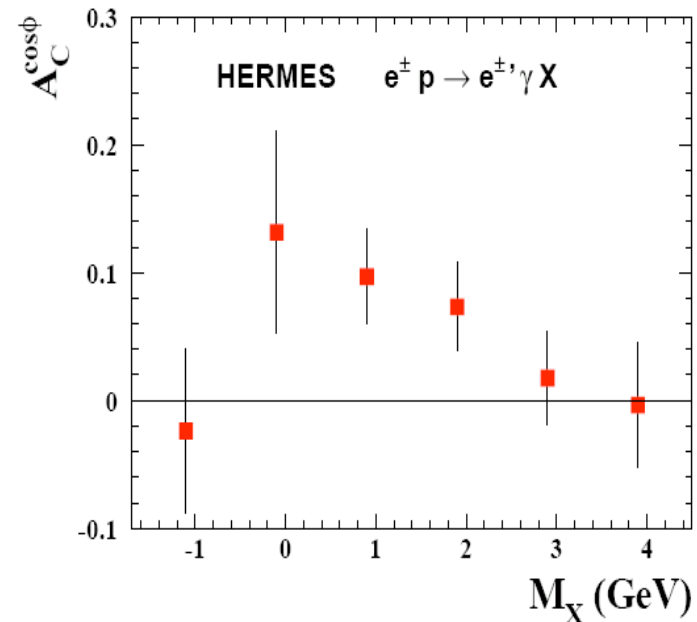
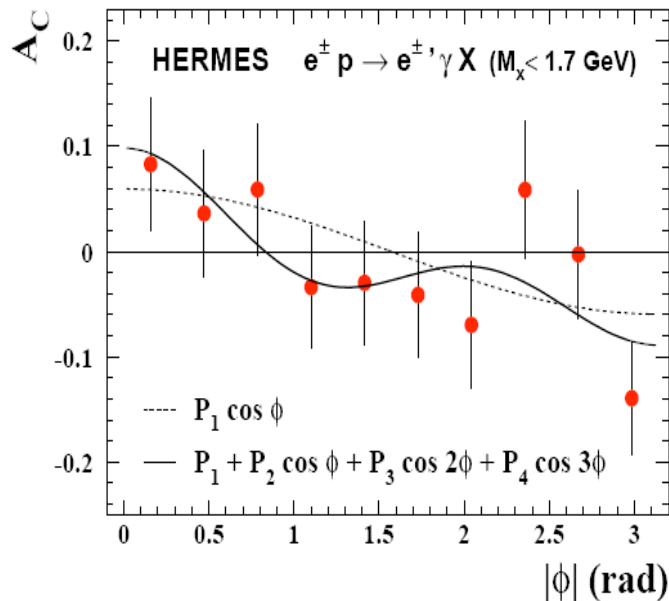
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# Beam charge asymmetry

$$A_C(\phi) = \frac{N^+(\phi) - N^-(\phi)}{N^+(\phi) + N^-(\phi)} \propto \frac{Re\mathcal{H}}{F_1} \cdot \cos\phi$$



A. Airapetian et al., HERMES coll., Phys. Rev. D **75**, 011103(R) (2007)

BCA requires lepton beams of both charges, not available in any of existing facilities

