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Recent Results on Polarized PDFs and Higher Twist

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OUTLINE

- Method of analysis higher twist corrections are taken into account
- Two new sets of very precise data on inclusive polarized DIS
 - low Q² CLAS data
 - COMPASS data mainly at large Q²

Very different kinematic regions

- Impact of the new data on LSS'05 polarized PD and HT
- The sign of the gluon polarization
- Spin of the proton, spin puzzle, flavor decomposition
- Summary



heory In QCD
$$g_1(x,Q^2) = g_1(x,Q^2)_{LT} + g_1(x,Q^2)_{HT}$$

 $g_1(x,Q^2)_{LT} = g_1(x,Q^2)_{pQCD} + \frac{M^2}{Q^2}h^{TMC}(x,Q^2) + O(\frac{M^4}{Q^4})$
 $g_1(x,Q^2)_{HT} = h(x,Q^2)/Q^2 + O(\frac{A^4}{Q^4})$
Hynamical HT power in Λ^2/Q^2 corrections ($\tau = 3,4$)
 $=>$ non-perturbative effects (model dependent) target mass corrections which are calculable

In NLO pQCD

dynamical

 $g_1(x,Q^2)_{pQCD} = \frac{1}{2} \sum_{pQCD} e_q^2 \left[(\Delta q + \Delta q) \otimes (1 + \frac{\alpha_s(Q^2)}{2\pi} \delta C_q) + \frac{\alpha_s(Q^2)}{2\pi} \Delta G \otimes \frac{\delta C_G}{N_s} \right]$

 $\delta C_a, \delta C_G - Wilson$ coefficient functions

A. Piccione, G. Ridolfi

polarized PD evolve in Q^2

 $N_{f}(=3)$ - the number of flavors

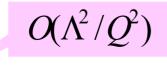
according to NLO DGLAP eqs.

- An important difference between the kinematic regions of the unpolarized and *polarized* data sets
- A lot of the present data are at moderate Q^2 and W^2 :

$$Q^2 \approx 1 - 5 \, GeV^2, \ 4 < W^2 < 10 \, GeV^2$$

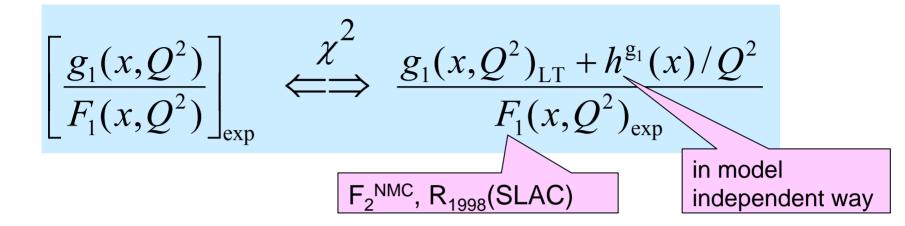
preasymptotic region

While in the determination of the PD in the unpolarized case we can cut the low Q^2 and W^2 data in order to eliminate the less known non-perturbative HT effects, it is **impossible** to perform such a procedure for the present data on the spin-dependent structure functions without loosing too much information.



HT corrections have to be accounted for in polarized DIS !

LSS method of analysis



Input PD
$$\Delta f_i(x,Q_0^2) = A_i x^{\alpha_i} f_i^{MRST}(x,Q_0^2)$$
 $Q_0^2 = 1 \, GeV^2, A_i, \alpha_i - free \, par.$

 $h^{p}(x_{i}), h^{n}(x_{i}) - 10$ parameters (i = 1, 2, ..., 5) to be determined from a fit to the data

8-2(SR) = 6 par. associated with PD; positivity bounds imposed by **MRST'02** unpol. PD

SUM
RULES
$$a_{3} = g_{A} = (\Delta u + \Delta \bar{u})(Q^{2}) - (\Delta d + \Delta \bar{d})(Q^{2}) = F - D = 1.2670 \pm 0.0035$$

$$a_{8} = (\Delta u + \Delta \bar{u})(Q^{2}) + (\Delta d + \Delta \bar{d})(Q^{2}) - 2(\Delta s + \Delta \bar{s})(Q^{2}) = 3F - D = 0.585 \pm 0.025$$

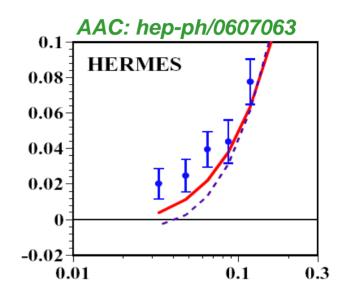
Flavor symmetric sea convention: $\Delta u_{sea} = \Delta \overline{u} = \Delta d_{sea} = \Delta \overline{d} = \Delta s = \Delta \overline{s}$

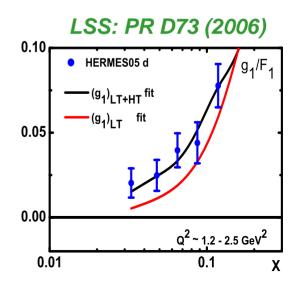
Higher twist effects

(CLAS'06 and COMPASS'06 not included)

$$g_1 = (g_1)_{LT} + h^{g_1}(x)/Q^2$$

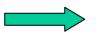
- The low x and low Q² (1.2 ~ 2.5 GeV²) HERMES/d data (*PR D71, 2005*) can not be described by the LT (logarithmic in Q²) term in g₁ => red curves
- Excellent agreement with the data if the HT corrections to g₁ are taken into account in the analysis





$$\begin{array}{l} \textbf{DATA}\\ \textbf{(old set)} \end{array} \qquad \textbf{CERN} \quad \textbf{EMC} - A_1^p \quad \textbf{SMC} - A_1^p, \ A_1^d \quad \textbf{COMPASS'05} - A_1^d \\ \hline \textbf{DESY} \quad \textbf{HERMES} - \quad \frac{g_1^p}{F_1^{p}}, \ \frac{g_1^d}{F_1^{d}} \\ \hline \textbf{SLAC} \quad \textbf{E142}, \ \textbf{E154} - A_1^n \quad \textbf{E143}, \ \textbf{E155} - \frac{g_1^p}{F_1^{p}}, \ \frac{g_1^d}{F_1^{d}} \\ \hline \textbf{JLab} \quad \textbf{Hall A} - \quad \frac{g_1^n}{F_1^n} \\ \hline \textbf{A}_1^N \approx (1 + \gamma^2) \frac{g_1^N}{F_1^N} \qquad \gamma^2 = 4 M^2 x^2 / Q^2 - kinematic factor \end{array}$$

Number of exp. points: 190



LSS'05 polarized PD and HT (PR D73, 2006)

DATA

$$\begin{array}{l} \textbf{CERN} \quad \textbf{EMC} - \ \textbf{A}_{1}^{p} \quad \textbf{SMC} - \quad \textbf{A}_{1}^{p}, \ \textbf{A}_{1}^{d} \quad \textbf{COMPASS'05} - \ \textbf{A}_{1}^{d} \\ \textbf{DESY} \quad \textbf{HERMES} - \quad \frac{g_{1}^{p}}{F_{1}^{p}}, \ \frac{g_{1}^{d}}{F_{1}^{d}} \\ \textbf{SLAC} \quad \textbf{E142}, \ \textbf{E154} - \ \textbf{A}_{1}^{n} \quad \textbf{E143}, \ \textbf{E155} - \frac{g_{1}^{p}}{F_{1}^{p}}, \ \frac{g_{1}^{d}}{F_{1}^{d}} \\ \textbf{JLab} \quad \textbf{Hall A} - \quad \frac{g_{1}^{n}}{F_{1}^{n}} \quad \textbf{CLAS EG1b} - \quad \frac{g_{1}^{p}}{F_{1}^{p}}, \ \frac{g_{1}^{d}}{F_{1}^{d}} \\ \textbf{A}_{1}^{N} \approx (1 + \gamma^{2}) \frac{g_{1}^{N}}{F_{1}^{N}} \end{array} \right.$$

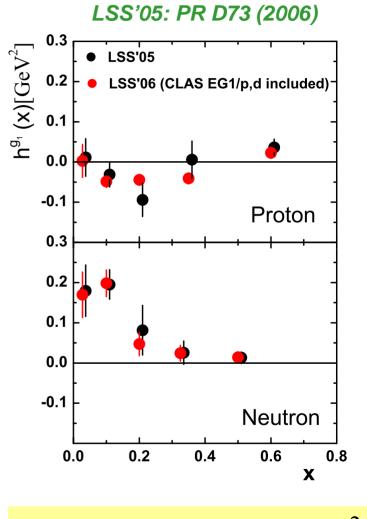
Number of exp. points: $190 \implies 823$

The analysis is performed in a collaboration with E. Leader and A. Sidorov

PR D75 (2007) 0740217

Effect of CLAS'06 p and d data (PL B641, 11, 2006) on polarized PD and HT

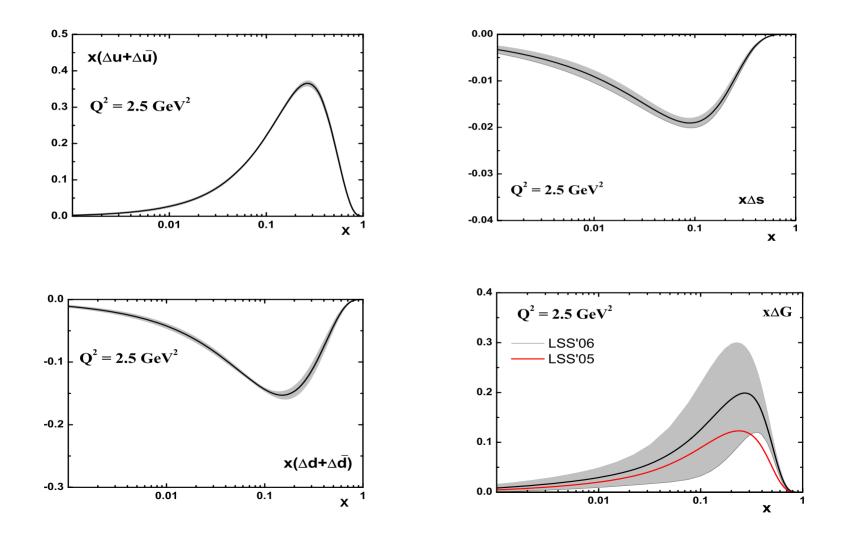
- Very accurate data on g₁^p and g₁^d at low Q²: 1~ 4 GeV² for x ~ 0.1 - 0.6 (W > 2 GeV)
- The determination of HT/p and HT/n is significantly improved in the CLAS x region compared to HT(LSS'05)
- As expected, the central values of PPD are practically not affected by *CLAS* data, BUT the accuracy of its determination is essentially improved (a consequence of much better determination of HT corrections to g₁)



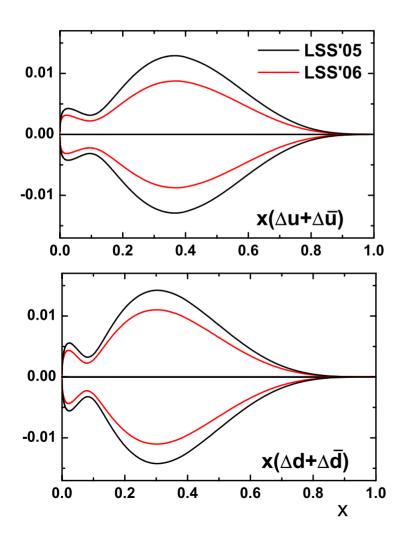
 $g_1 = (g_1)_{LT} + h^{g_1}(x)$

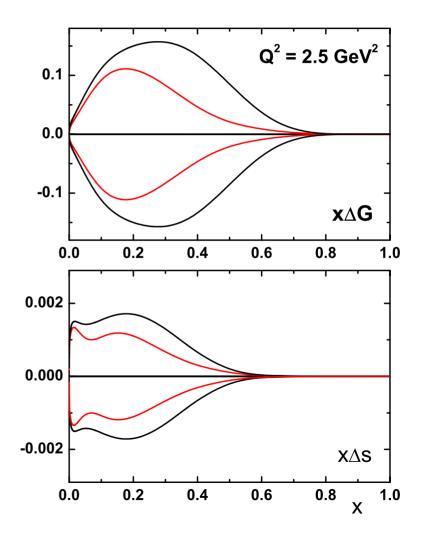
LSS'06 NLO(MS) polarized PDFs

The quark densities (central values) are identical with those of LSS'05.



Impact of CLAS'06 data on the uncertainties for NLO(MS) polarized PD

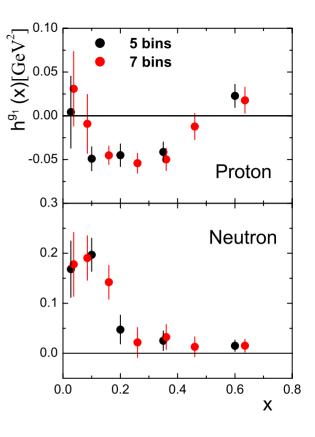


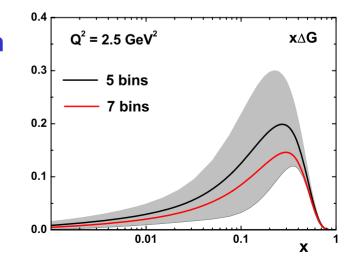


Due to the good accuracy of the CLAS data, one can split the measured x region of the world+CLAS data set into 7 bins instead of 5, and to determine more precisely the x-dependence of HT

The corresponding PPD are practically identical with those of LSS'06 (5 bins)

The only exception is x∆G, but it lies within the error band of x∆G (5 bins) ⇒ small correlation between gluons and HT





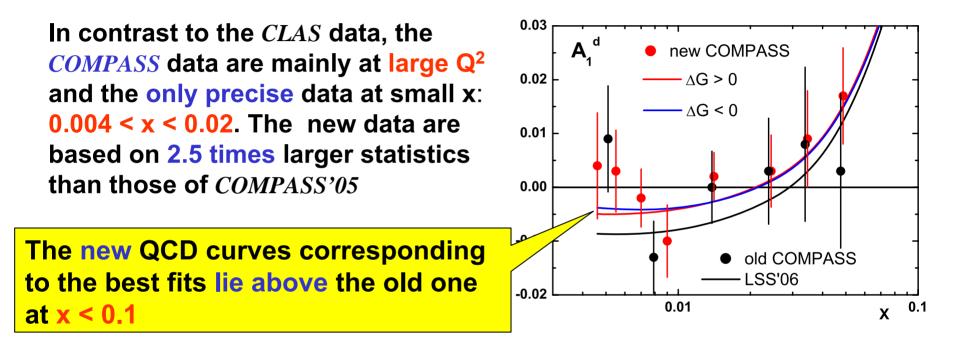
The main message from this analysis It is impossible to describe the very precise CLAS data if the HT corrections are NOT taken into account

NOTE: If the low Q^2 data are not too accurate, it would be possible to describe them using only the leading twist term (logarithmic in Q^2) in g_1 , *i.e.* to mimic the power in Q^2 dependence of g_1 with a logarithmic one (using different forms for the input PDFs and/or more free parameters associated with them) which was done in the analyses of another groups before the CLAS data have appeared. DATA

CERN EMC -
$$A_1^p$$
 SMC - A_1^p , A_1^d COMPASS'06 - A_1^q
DESY HERMES - $\frac{g_1^p}{F_1^{p}}$, $\frac{g_1^d}{F_1^{d}}$
SLAC E142, E154 - A_1^n E143, E155 - $\frac{g_1^p}{F_1^{p}}$, $\frac{g_1^d}{F_1^{d}}$
JLab Hall A - $\frac{g_1^n}{F_1^n}$ CLAS EG1b - $\frac{g_1^p}{F_1^{p}}$, $\frac{g_1^d}{F_1^{d}}$
 $A_1^N \approx (1 + \gamma^2) \frac{g_1^N}{F_1^N}$ $\gamma^2 = 4M^2x^2/Q^2$ - kinematic factor
COMPASS'05 \longrightarrow COMPASS'06

Number of exp. points: $823 \implies 826$

Effect of COMPASS'06 A_1^d data (*hep-ex/0609038*) on polarized PD and HT

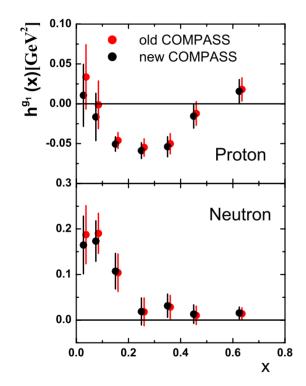


• $(\Delta u + \Delta \overline{u}), (\Delta d + \Delta \overline{d})$ do NOT change

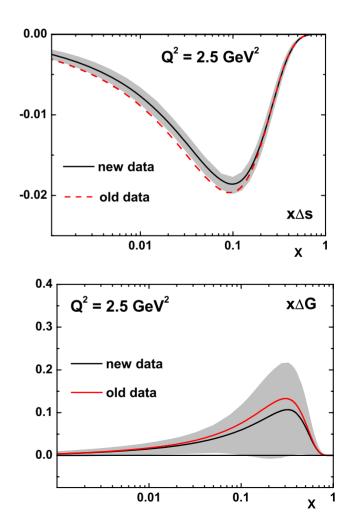
■ x |∆s(x)| and x∆G(x) and their first moments ∆s and ∆G slightly decrease

 $\mathbf{Q}^2 = \mathbf{1} \; \mathbf{GeV}^2$

COMPASS	∆s	∆G	$a_0 = \Delta \Sigma_{MS}$
old	-0.070 ± 0.006	0.173 ± 0.184	0.165 ± 0.044
new	-0.063 ± 0.005	0.129 ± 0.166	0.207 ± 0.040



The values of HT are practically NOT affected by *COMPASS* data excepting the small x where Q^2 are also small

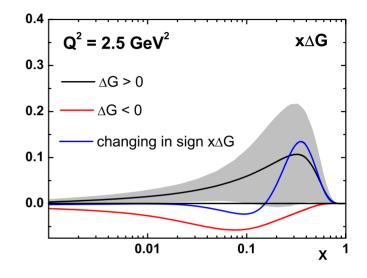


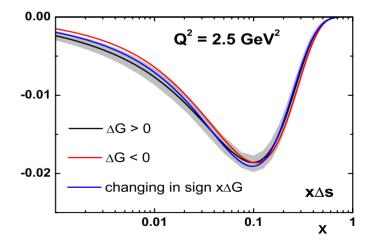
The sign of gluon polarization

The present inclusive DIS data cannot rule out the solutions with negative and changing in sign gluon polarizations

 $\chi^2_{DF}(\Delta G > 0) = 0.895$ $\chi^2_{DF}(\Delta G < 0) = 0.897, \chi^2_{DF}(x \Delta G / chsign) = 0.895$

- The shape of the negative gluon density differs from that of positive one
- In all the cases the magnitude of ∆G is small: |∆G| < 0.25</p>
- The corresponding polarized quark densities are very close to each other





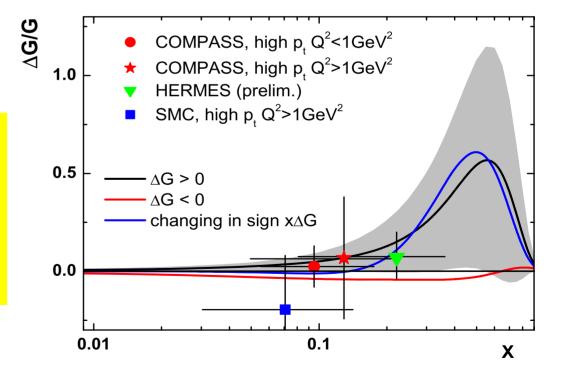
Comparison with directly measured $\Delta G/G$ at $Q^2 = 3 GeV^2$

MRST'02 unpolarized gluon density is used for G(x)

The error band corresponds to statistic and systematic errors of ΔG

The error bars of the experimental points represent the total errors

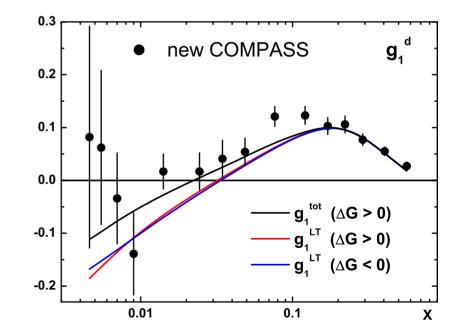
The most precise value of Δ G/G, the COMPASS one, is well consistent with any of the polarized gluon densities determined in our analysis



LSS'06 VS COMPASS'06

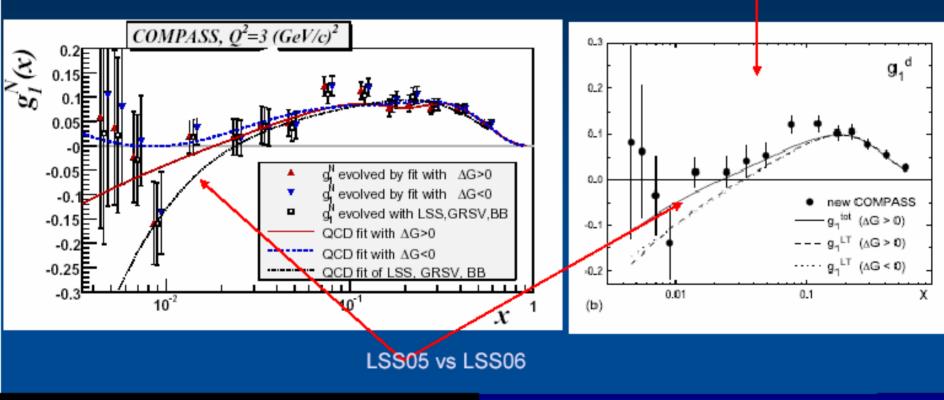
- At small x: 0.004 0.02 (Q² ~ 1-3 GeV²) our results differ from those of COMPASS
- COMPASS → significant difference between (g₁)_{th} corresponding to the best fits for ∆G > 0 and ∆G < 0</p>
- LSS'06 → the theoretical curves for both cases are very close to each other
- The reason → HT effects (40% at small x) which are NOT taken into account by COMPASS

 $(g_1)_{exp} \leftrightarrow$ $(g_1)_{LT}(COMPASS) \approx$ $(g_1)_{LT}(LSS) + h^d(x)/Q^2$



QCD analysis of the world data on structure function g₁

Comparison of data and fits - LSS06 (hep-ph/0612360



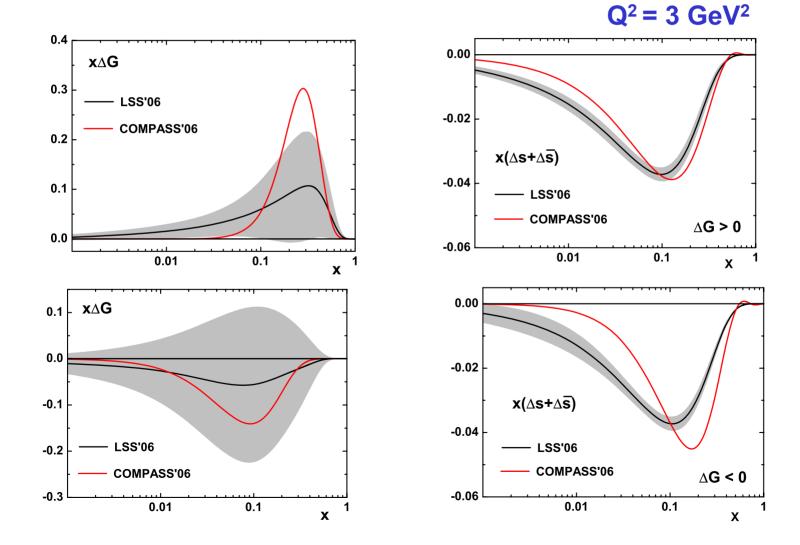
DIS 2007

Krzysztof Kurek The deuteron spin-dependent structure function g1

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• $x \Delta s$ are different, especially in the case of $\Delta G < 0$

• xAG obtaned by COMPASS in both fits are more peaked than ours



Constraint on ΔG from π^0 production at RHIC (*AAC*, *hep-ph/0612037*)

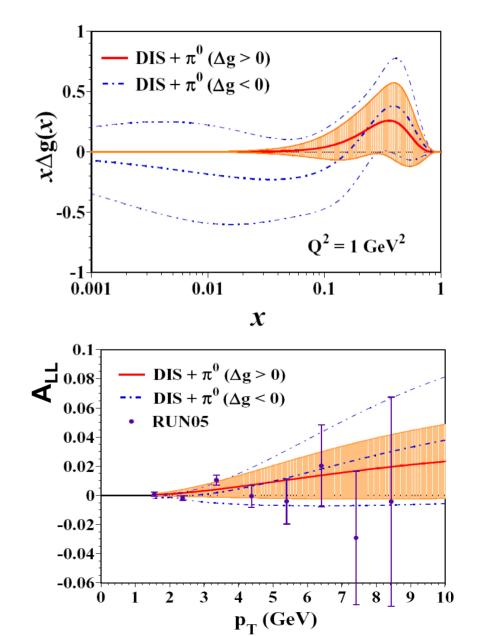
 $\vec{\mathbf{p}} + \vec{\mathbf{p}} \rightarrow \pi^0 + \mathbf{X}$

From DIS + π^0 analysis:

 $\Delta G = 0.31 \pm 0.32$

 $(Q^2 = 1 \text{ GeV}^2)$

Note: In contrast to changing in sign $x\Delta G_{LSS}$, which for $Q^2 > 6 \text{ GeV}^2$ is positive for any x, $x\Delta G_{AAC}$ becomes negative for large x too with increasing of Q^2 .



 $\mathbf{Q}^2 = \mathbf{1} \mathbf{G} \mathbf{e} \mathbf{V}^2$

COMPASS	Δs	ΔG	$a_0 = \Delta \Sigma_{MS}$
old	-0.070 ± 0.006	0.173 ± 0.184	0.165 ± 0.044
new ($\Delta G > 0$)	-0.063 ± 0.005	0.129 ± 0.166	0.207 ± 0.040
new ($\Delta G < 0$)	-0.057 ± 0.010	-0.200 ± 0.414	0.243 ± 0.065

Spin of the proton

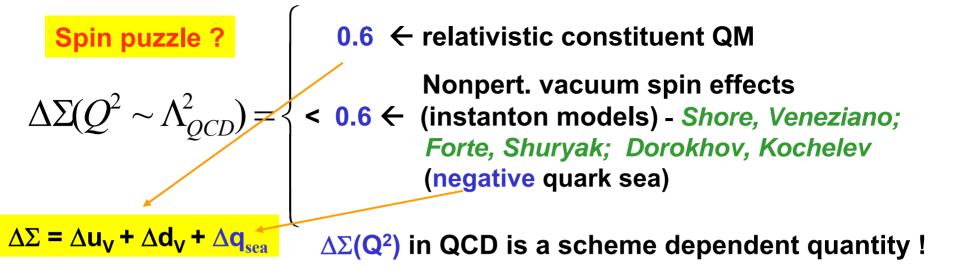
 $S_z = 1/2 = 1/2 \Delta\Sigma(Q^2) + \Delta G(Q^2) + L_q(Q^2) + L_g(Q^2)$

 $= 0.23(-0.08) + -0.17(0.41) + L_{g}(Q^{2}) + L_{g}(Q^{2})$

The big uncertainty is coming from gluons

To be determined from forward extrapolations of generalized PD

 $L_g \approx 0$, Brodsky, Gardner: PL B643 (2006) 22

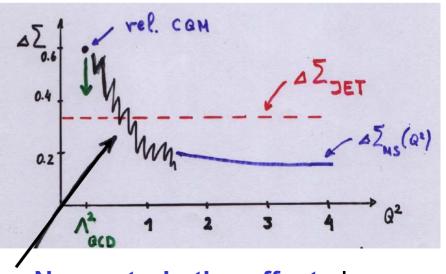


From combined analysis of elastic e^{i} , vp and vp data \rightarrow the strange axial form factor $G^{S}_{A}(Q^{2})$ at $Q^{2} \leq 1$ GeV²

 $G^{S}_{A}(Q^{2} = 0) = \Delta S$

S. Pate, hep-ex/0611053

$$\Delta \Sigma_{\rm JET}({\rm DIS}) \Leftrightarrow \Delta \Sigma(Q^2 \sim \Lambda_{\rm QCD}^2)$$



Nonperturbative effects !

Flavor decomposition: polarized sea

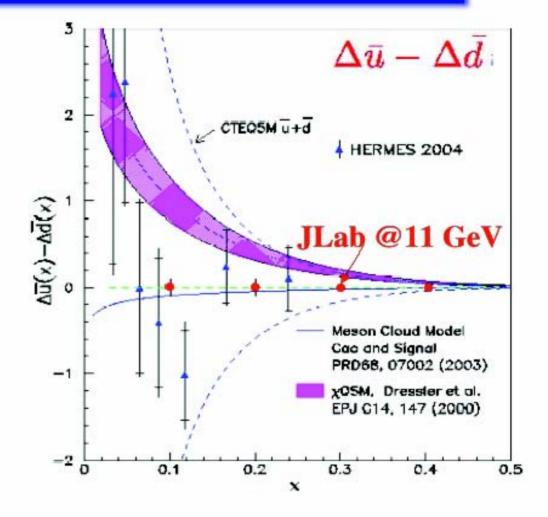
Predictions:

 Instantons (χQSM):

 $\Delta \bar{u} \approx -\Delta \bar{d}$

First data from HERMES

$$\Delta \overline{u} - \Delta \overline{d} \approx 0$$



COMPASS (A. Korzenev at DIS'07)

From SIDIS $\rightarrow \Delta u_{v}(x) + \Delta d_{v}(x) \rightarrow \Gamma_{v} \equiv \int_{0}^{1} (\Delta u_{v}(x) + \Delta d_{v}(x)) dx \text{ at } Q^{2} = 10 \text{ GeV}^{2}$

LO QCD treatment + assumption: $q_{LO} \rightarrow q_{LO}/(1 + R)$ in Eqs. for A_1^h

$$\Delta \overline{u} + \Delta \overline{d} = (\Delta s + \Delta \overline{s}) + 1/2 (a_8 - \Gamma_V)$$

inclusive DIS hyperon β decays $\rightarrow a_8 = 0.585$
$$\Gamma_V = \int_{0.006}^{0.7} (\Delta u_V(x) + \Delta d_V(x)) dx = 0.40 \pm 0.07 (\text{stat}) \implies \Delta \overline{u} + \Delta \overline{d} = 0.0 \pm 0.04 \pm 0.03$$

FNS (NLO analysis of incl. and SIDIS) $\implies -0.10$ (KRE FF), ~ 0.0 (KKP FF)

The flavor decomposition is NOT well determined at present

SUMMARY

- The low Q² CLAS data improve essentially our knowledge of higher twist corrections to g₁ structure function
- The central values of polarized PD are NOT affected, but the accuracy of its determination is essentially improved
- The COMPASS data (mainly at large Q²) influence |As| and AG which slightly decrease, but practically do NOT change HT

Strong support of the QCD framework

- Large (40%) contribution of HT to $(g_1)^d$ at small x (low Q²)
- The present inclusive DIS data cannot rule out the negative and changing in sign gluon densities
- Good agreement with the directly measured $\Delta G/G$

OPEN QUESTIONS

- To constrain better ∆G ⇒ directly from COMPASS, RHIC; more precise experiments on g₁^d (JLab Hall C)
- $\Delta u, \Delta d$ \implies from SIDIS (*COMPASS, JLab*) and A_L(W⁺⁽⁻⁾) at *RHIC*
- L_q (from generalized PD, JLab) and L_q
- $a_8 \neq 3F D = 0.585$? (how much $SU(3)_f$ is broken) $\rightarrow NA48$ at CERN
- HT corrections in SIDIS, O(Λ⁴/Q⁴) term in HT expansion in Bjorken x-space

...etc.



Test of QCD and determination of PDFs and HT

$$(\Delta q_i, \Delta \overline{q_i}, \Delta G)(x, Q_0^2; a_k) \xrightarrow{\text{pQCD}} (\Delta q_i, \Delta \overline{q_i}, \Delta G)(x, Q^2; a_k)$$

DGLAP eqs.

$$a_k - 6 \text{ free par.}$$

$$Q_0^2 = 1 \text{ GeV}^2$$

$$g_1(x, Q^2; a_k)_{\text{LT}}$$

$$\chi^{2} = \sum_{i,j} \frac{\left[g_{1}(x_{i}, Q_{j}^{2})_{\exp} - g_{1}(x_{i}, Q_{j}^{2}; a_{k})_{\text{LT}} - h_{(l)}(x_{(l)})/Q^{2}\right]^{2}}{\Delta g_{1}(x_{i}, Q_{j}^{2})_{\exp}^{2}}$$
10 free parameters

 \Rightarrow $a_k \pm \Delta a_k, h_l \pm \Delta h_l \rightarrow$ 16 free parameters

Flavor symmetric sea convention

- From inclusive DIS only the sum $(\Delta q + \Delta q)$ can be determined $\rightarrow \Delta u$ and Δd , as well as Δu_V and Δd_V depend on the assumption about the sea
- usually a symmetric sea convention is used at Q_0^2 (this is assumption for $\overline{\Delta u}$ and $\overline{\Delta d}$, NOT for $\Delta \overline{s}$)

• $\Delta u = \Delta d = \lambda \Delta s$ \implies we have shown that $(\Delta q + \Delta q)$ as well as Δs do NOT depend on λ

• It was shown from a global inclusive and SIDIS analysis (*D. de Florian at al.*) that while Δu and Δd strongly depend on the fragmentation functions, Δs practically does not change.

KTeV experiment Fermilab

$$\Xi^0 \rightarrow \Sigma^+ e \overline{\nu}$$

β-decay

 $SU(3)_f$ prediction for the form factor ratio g_1/f_1

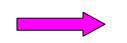
$$\frac{g_1}{f_1} = g_A = 1.2670 \pm .0035$$

Experimental result

$$\frac{g_1}{f_1} = 1.32^{+0.21}_{-0.17} \pm 0.05$$

A good agreement with the *exact* $SU(3)_f$ symmetry !

From exp. uncertainties

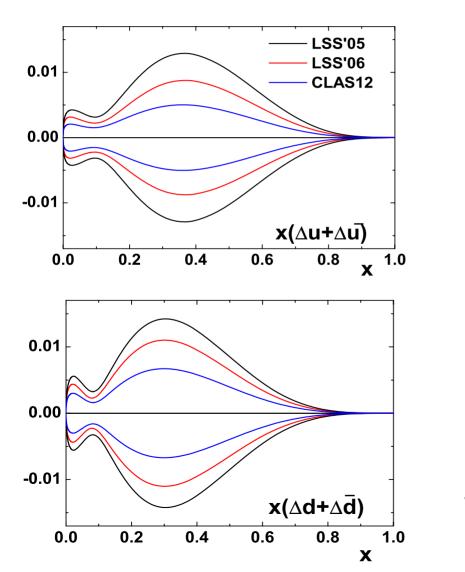


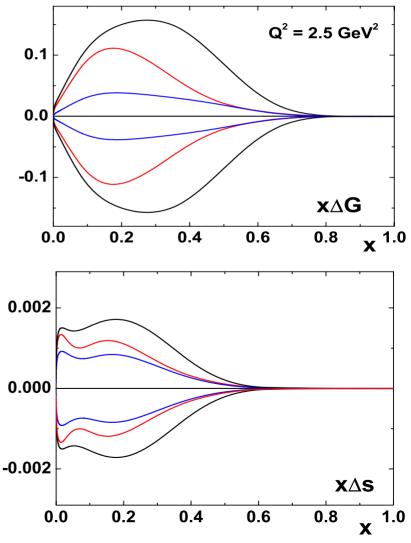
SU(3) breaking is at most of order **20%**

NA48 at CERN \rightarrow 3 times larger statistics \rightarrow the results will be done soon

Indeed, if one calculates the χ^2 - probability for the combined world + CLAS data set using the LSS'05 polarized PDFs and HT, the result for χ^2 is 938.9 for 823 experimental points, which significantly decreases to 718.0 after the fit. This big change of χ^2 is achieved mainly through the changes in the HT values. **Excepting the gluons the parameters for the** input quark densities did NOT change. This strongly supports the theoretical framework in which the leading twist QCD contribution is supplemented by higher twist terms of $O(\Lambda^2/Q^2)$.

The expected uncertainties for NLO(MS) polarized PDFs including the CLAS12 "data" set

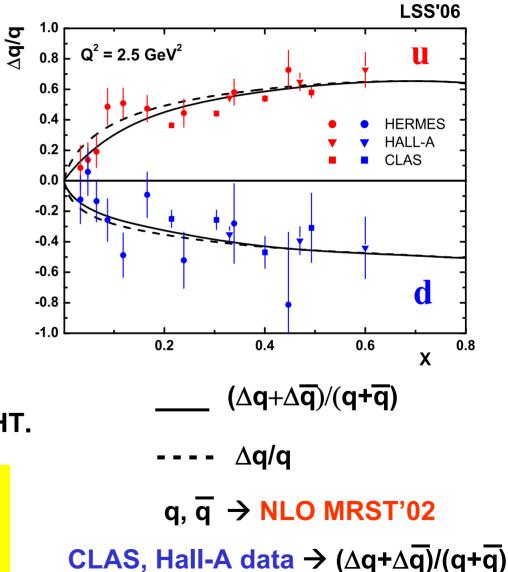




Comparison of $\Delta q/q$ with the data

- CLAS and Hall-A data are extracted in the naive parton model treatment
- HERMES data are extracted in LO QCD approximation
- In the preasymptotic region HT corrections should be taken into account !
- The NLO LSS'06 PDFs are obtained in the presence of HT.

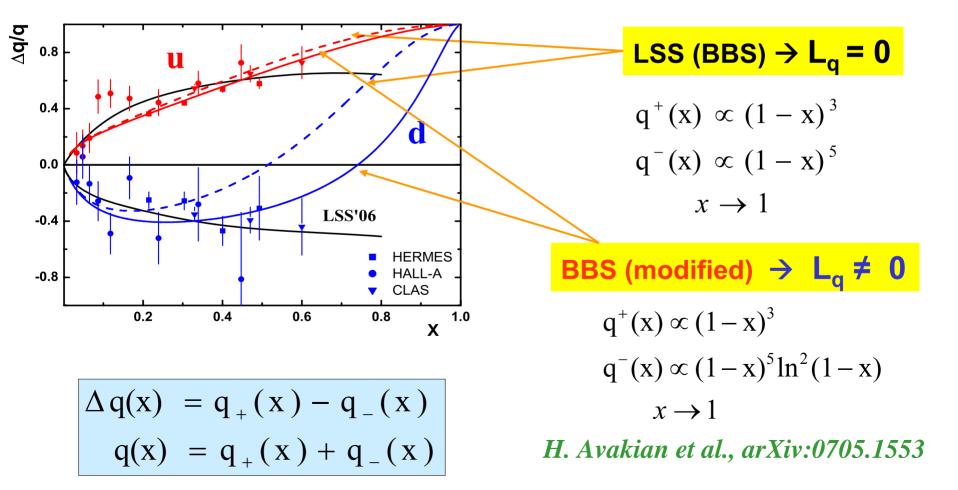
One has to be careful comparing the data on ∆q/q with the QCD curves



The behavior of $\Delta q/q$ at large x \implies a challenge to the experiment

LSS, as well as GRSV, AAC, BB: $\Delta q/q \rightarrow const \{ + \text{ for } u, - \text{ for } d \}$ $X \rightarrow 1$ BBS model (Brodsky et al):

$$\Delta q/q \rightarrow 1$$
 for $q = u, d$
 $X \rightarrow 1$



The first moments of higher twist

Thanks to the very precise CLAS data the first moments of HT corrections are now much better determined.

$$\overline{h}^N = \int_{0.0045}^{0.75} dx \ h^N(x), \ N = p, n$$

$$\bar{n}^{p} = (-0.014 \pm 0.005) \, GeV^{2}$$

$$\overline{h}^n = (0.037 \pm 0.008) \, GeV^2$$

$$\overline{h}^{p} - \overline{h}^{n} = (-0.051 \pm 0.009) \, GeV^{2}$$

 $\overline{h}^p - \overline{h}^n < 0 \quad \leftarrow$

 $\overline{h}^{p} + \overline{h}^{n} = (0.023 \pm 0.009) \, GeV^{2}$

In agreement with the instanton model predictions and sum rules in QCD

 $\frac{\overline{h}^{p} + \overline{h}^{n} < |\overline{h}^{p} - \overline{h}^{n}|}{\mathsf{QCD}} \leftarrow \begin{array}{c} \text{In agreement with } 1/\mathsf{N}_{\mathsf{C}} \text{ expansion in} \\ \mathsf{QCD} (Balla \ et \ al., NP \ B510, 327, 1998) \end{array}$

In our notations
$$\longrightarrow \int_{0}^{1} dx h^{g_1}(x) = \frac{4}{9} M^2(d_2 + f_2)$$

HT (τ =3) HT (τ =4)

Our numerical results are in a qualitative agreement with those obtained from the analyses of the first moments of g_1 at JLab $[O(\Lambda^4/Q^4)$ terms are also taken into account]: A. Deur et al., PRL 93, 212001 (2004), A. Z.-E. Meziani et al., PL B613, 148 (2005), etc.

Important: To study the next term $O(\Lambda^4/Q^4)$ in

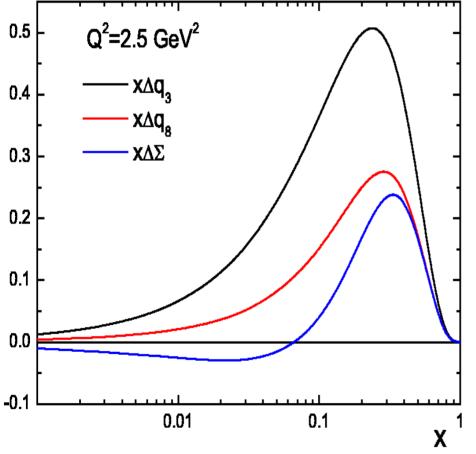
HT expansion in Bjorken x- space



more precise data are needed

JLab Proposal PR-07-011 (Hall C): A High Precision Measurement of the Deuteron Spin-Structure Function g1/F1

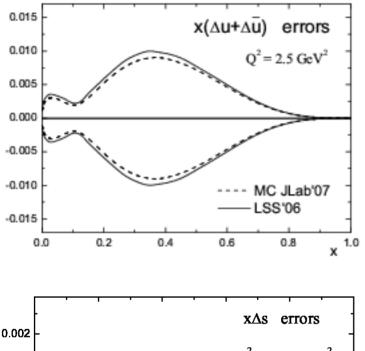
Why deuteron best for $\Delta G(\mathbf{x})$? $g_1^{p(n)}(x,Q^2) = \frac{1}{9} [(\pm \frac{3}{4} \Delta q_3 + \frac{1}{4} \Delta q_8 + \Delta \Sigma) \otimes (1 + \frac{\alpha_s(Q^2)}{2\pi} \delta C_q) + \frac{\alpha_s(Q^2)}{2\pi} \Delta G \otimes \delta C_G]$

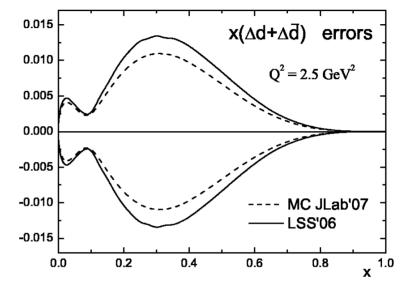


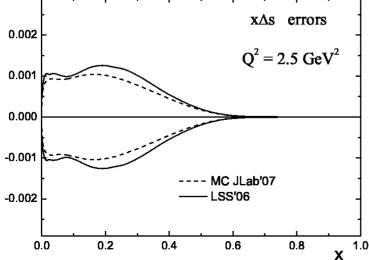
• The Δq_3 terms from p and n about twice size of Δq_8 and $\Delta \Sigma$ terms, cancel in deuteron.

 Relative gluon contributions largest in deuteron: relevant because experimental errors dominated by systematic scale factors.

Physics Impact in LSS framework







Impact on polarized quark distributions relatively small

