

# Using Beam Normal Asymmetry in QWeak to Access the Elastic Form factors of the Delta(1232)

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# Quantum Chromodynamics (QCD)

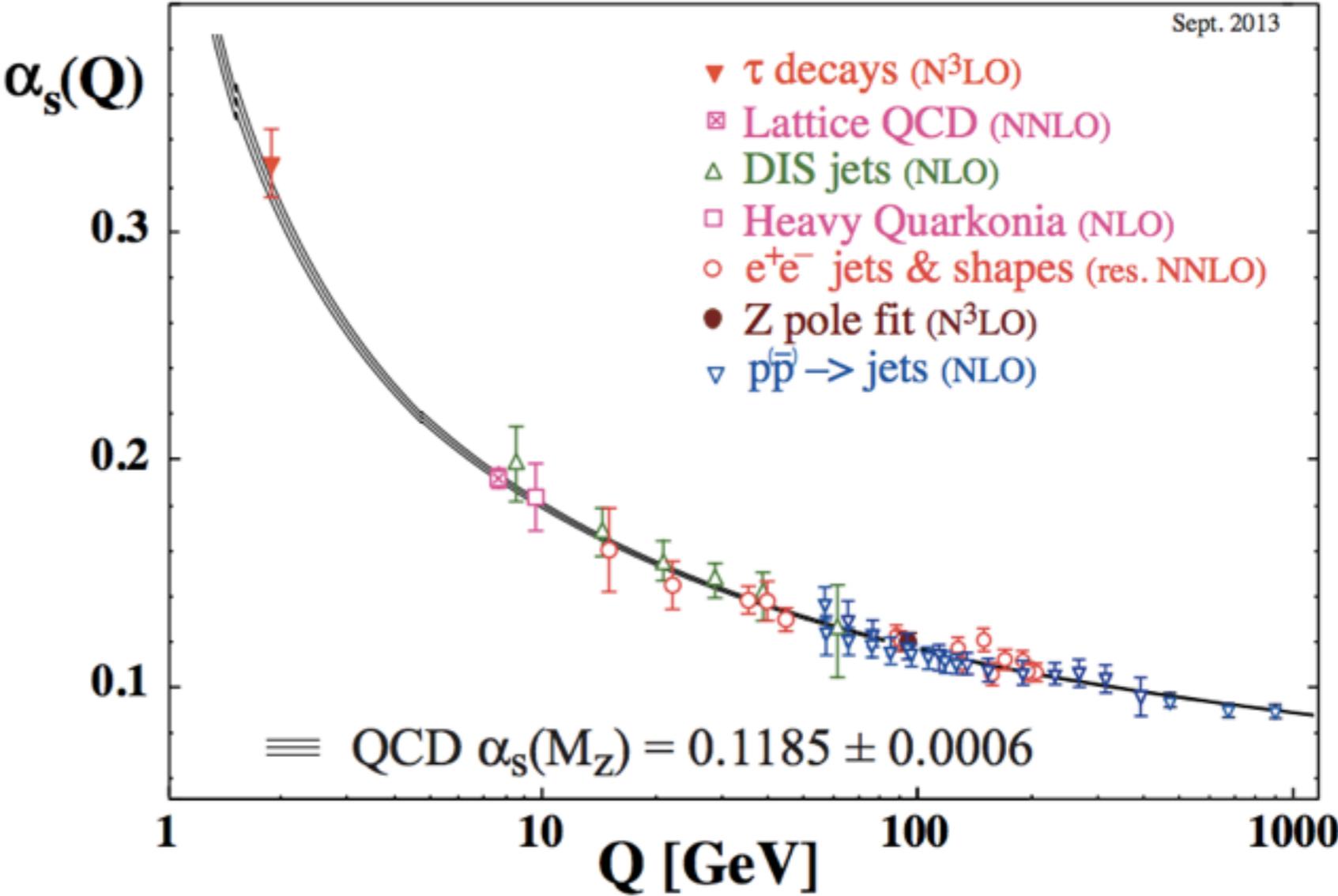
strong interaction is responsible for most of the visible mass

gluon-gluon interactions



weak at high energies but very strong at scales appropriate for life

confinement of quarks



How do we study the strong coupling regime of QCD?

# Motivation

## Spectroscopy

Study of the properties of states of QCD: production mechanisms, mass, width, quantum numbers and decay modes (and form-factors.)

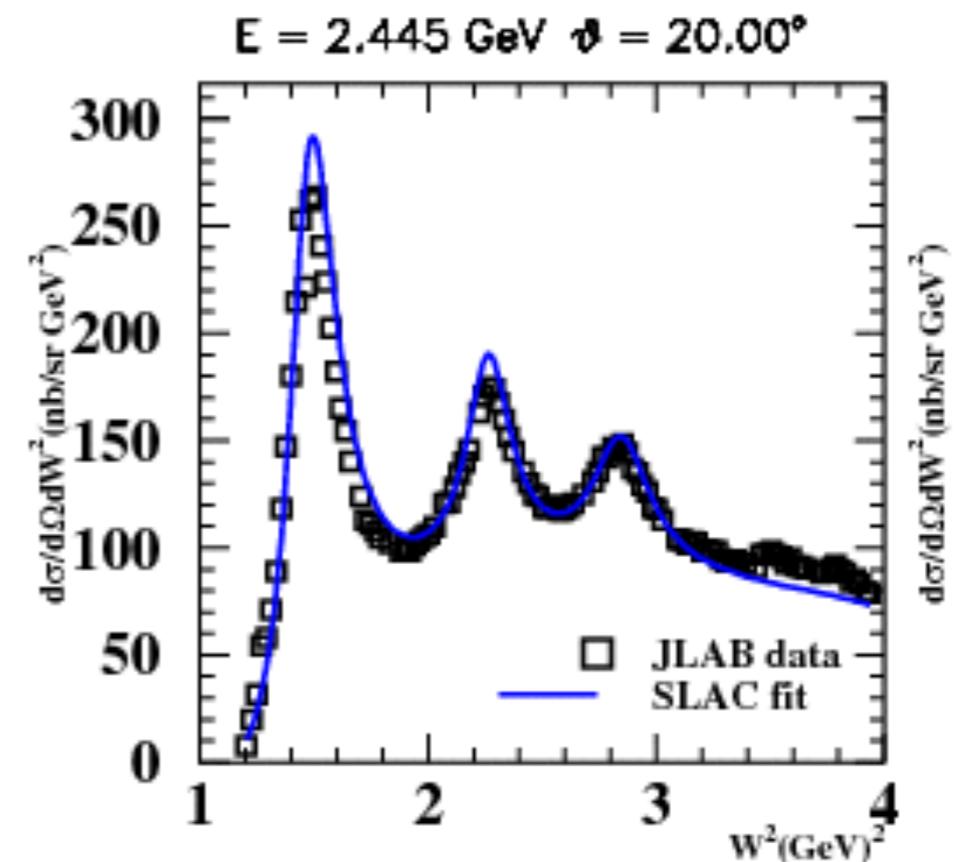
Major success: quark model itself grew out of such studies.

## The $\Delta$ resonance

lowest lying nucleon excitation;  
experimentally well separated;  
very short lived

## Form Factors

Form Factors contain information on the positions of charges within a hadron (infinite momentum frame: form factor is 2D Fourier transform of transverse density.)



# $\Delta$ Elastic Form Factors ( $\gamma^* \Delta \Delta$ )

There are 4 elastic form factors (spin-3/2)

$$G_{E_0}(Q^2), G_{M_1}(Q^2), G_{E_2}(Q^2), \text{ \& } G_{M_3}(Q^2)$$

associated with  
distribution of charge,  
magnetization and non-  
spherical deformations

$$G_{E_0}(0) = e_{\Delta} \quad \text{Charge}$$

$$G_{M_1}(0) \propto \mu_{\Delta} \quad \text{Magnetic moment}$$

$$G_{E_2}(0) \propto D_{\Delta} \quad \text{Dipole moment}$$

$$G_{M_3}(0) \propto O_{\Delta} \quad \text{Octopole moment}$$

$$\text{PDG} \quad \frac{\mu_{\Delta^+}}{\mu_N} = 2.7_{-1.3}^{+1.0} \pm 1.5 \pm 3 \quad (\text{stat, syst, theory})$$

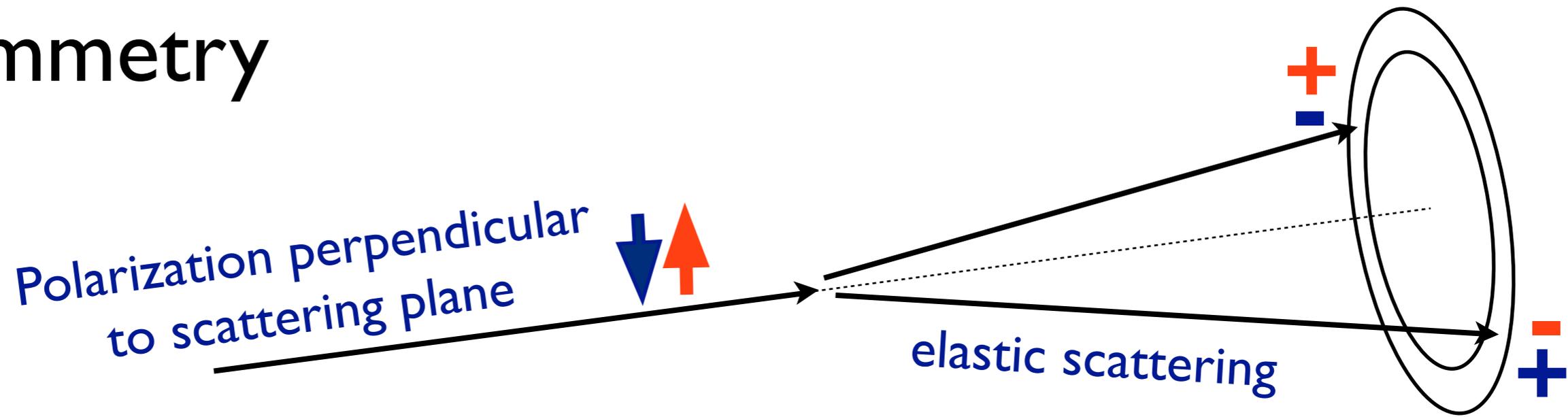
$$\text{Tapps \& Mainz} \\ \gamma p \rightarrow p \pi^0 \gamma'$$

no direct measurements of dipole and octopole moments

$$Q_{p \rightarrow \Delta^+} = -(0.0846 \pm 0.0033) \text{ e fm}^2$$

can potentially extract  
elastic information

# $B_n$ asymmetry



time-reversal invariance forces this SSA to vanish for one-photon exchange

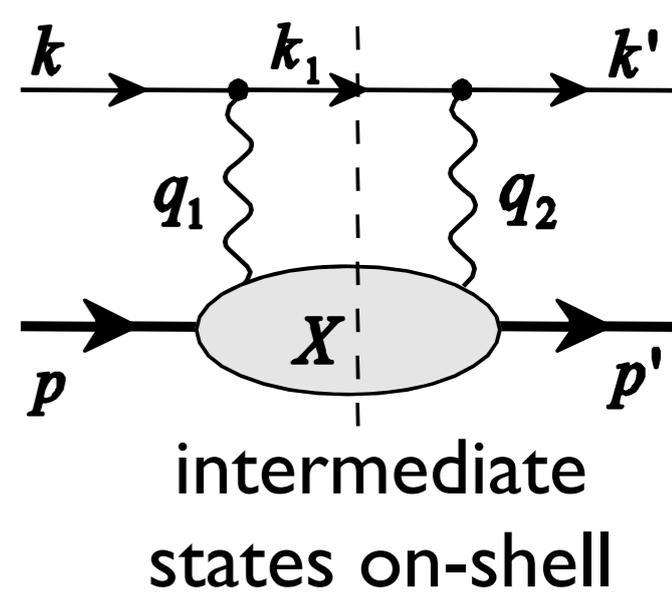
arises from an interference between the one-photon exchange (Born) amplitude and the imaginary part of the two-photon exchange amplitude

$$B_n = \frac{\sigma_{\uparrow} - \sigma_{\downarrow}}{\sigma_{\uparrow} + \sigma_{\downarrow}} = \frac{2\text{Im}(T_{2\gamma} \cdot T_{1\gamma}^*)}{|T_{1\gamma}|}$$

Asymmetry is very small

$$B_n \sim \alpha_{\text{em}} \frac{m_e}{E_e} \sim 10^{-6} - 10^{-5}$$

2-photon  $\nearrow$   $\alpha_{\text{em}}$   $\nwarrow$  ultra-relativistic

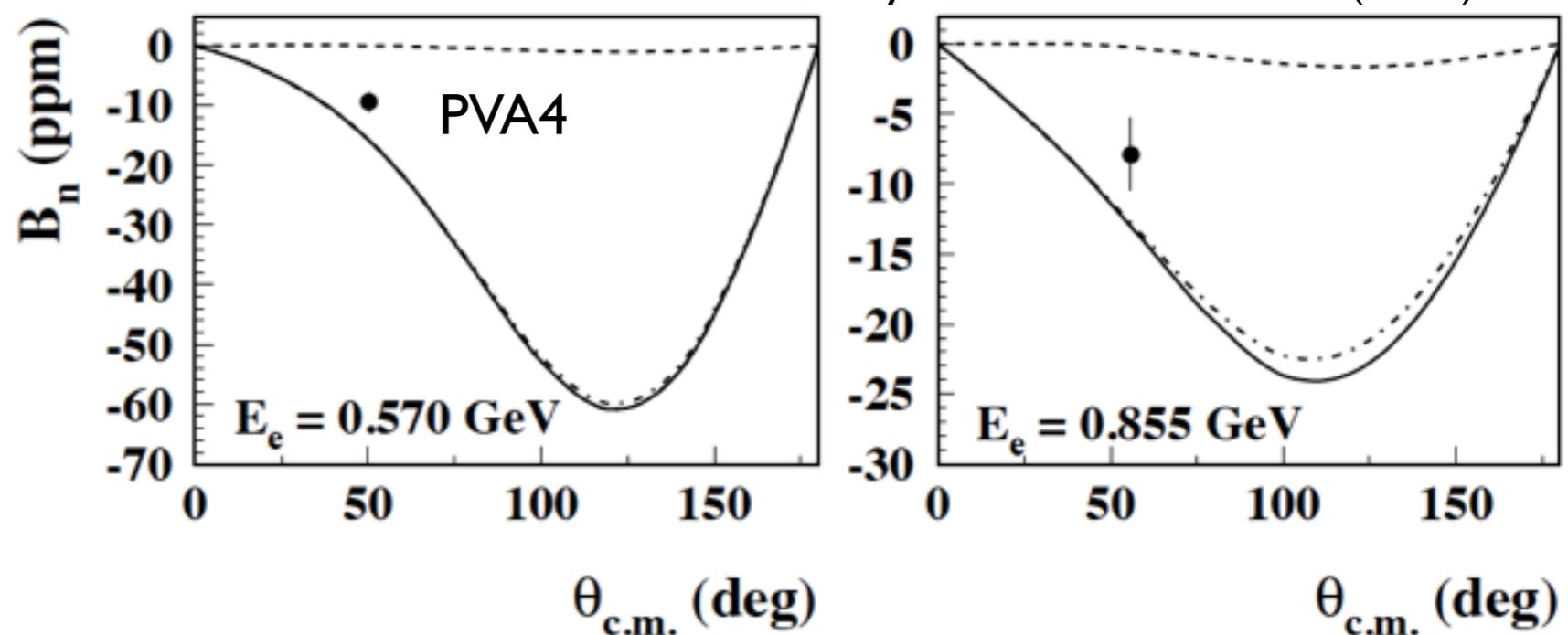


# $B_n$ asymmetry in ep elastic

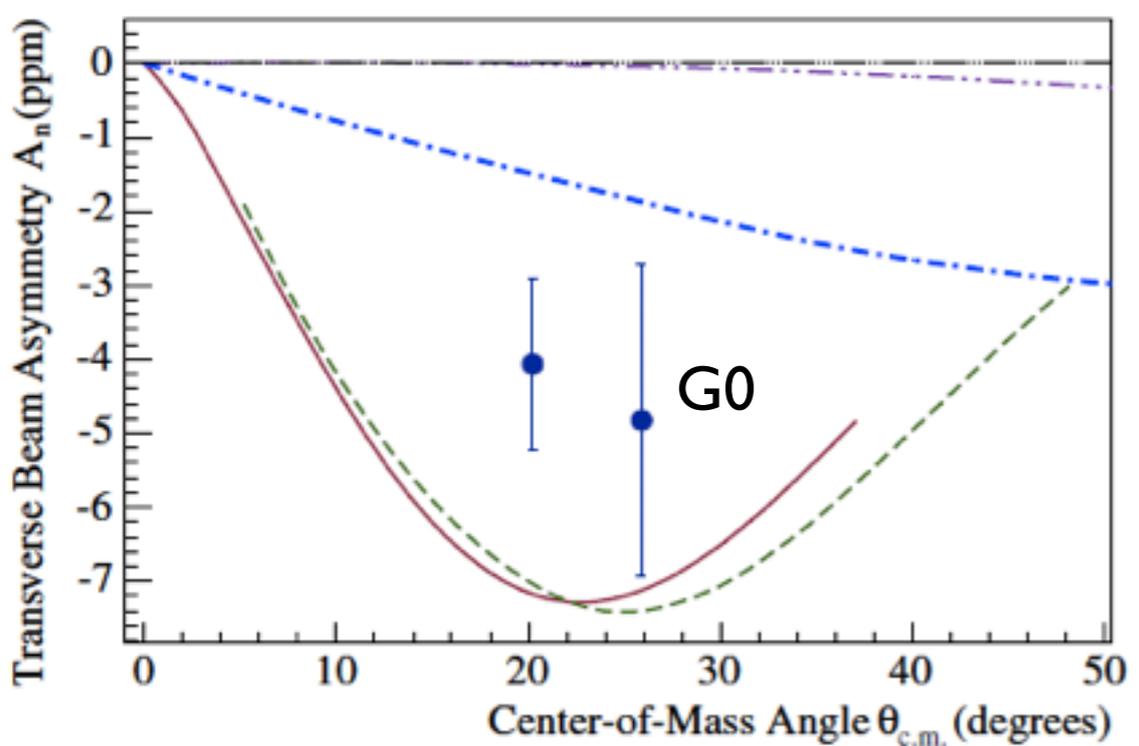
Calculations reasonably well under control - generally reproduce the data to better than a few  $\sigma$

Require excited intermediate states

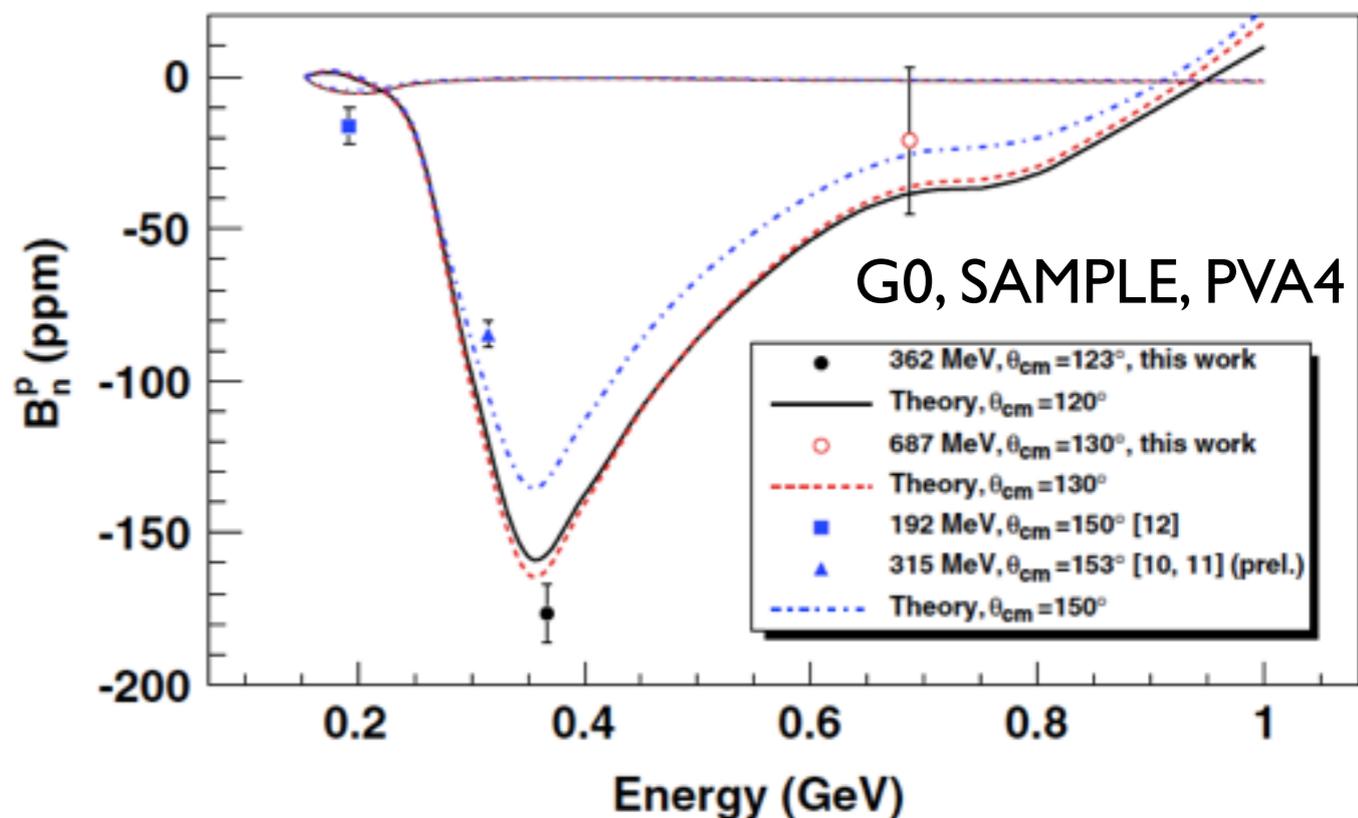
Phys.Rev.Lett. 94, 082001 (2005)



Phys.Rev.Lett. 107 (2011) 022501

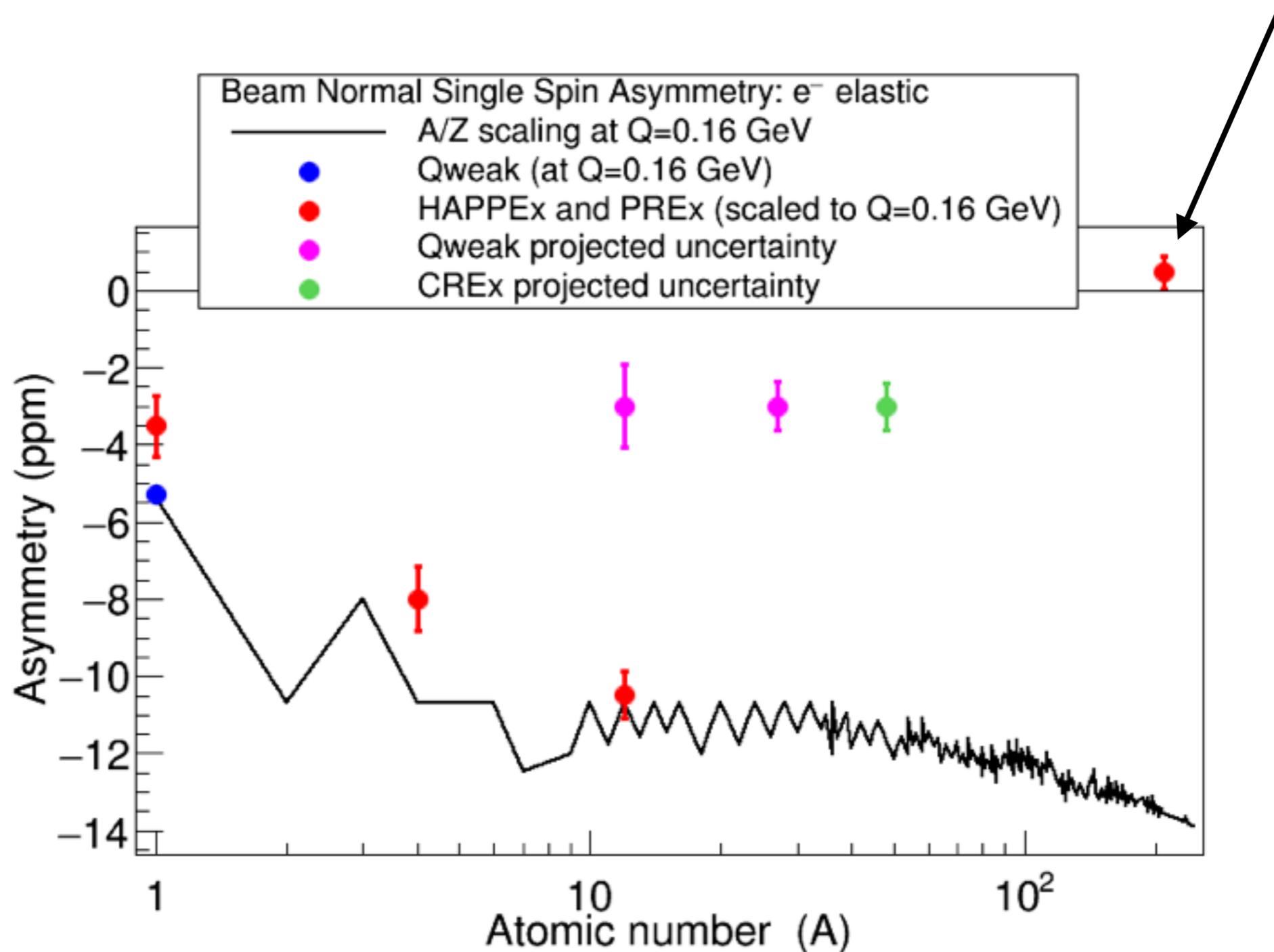


Phys.Rev.Lett. 99 (2007) 092301

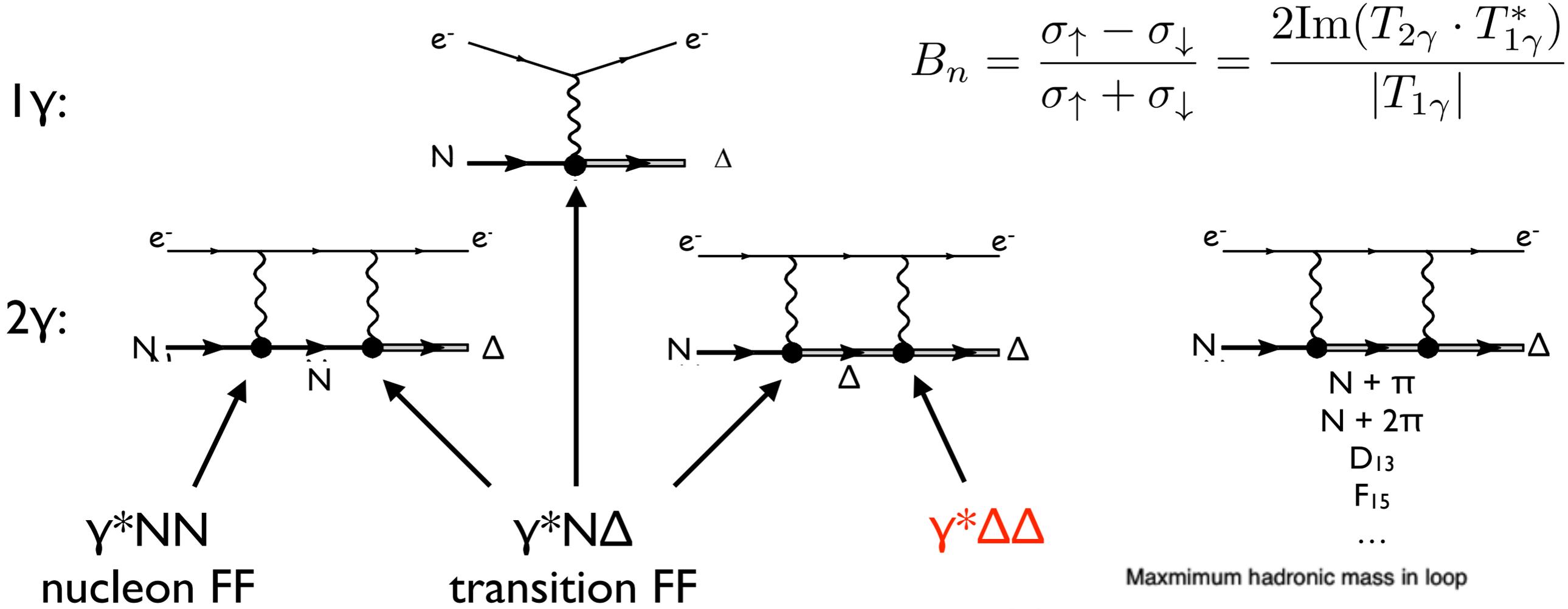


# $B_n$ asymmetry in nuclear elastic

Calculations of  $B_n$  asymmetry in forward-angle elastic scattering match nuclear data except for the heaviest nuclei (assumed due to Coulomb distortion.)

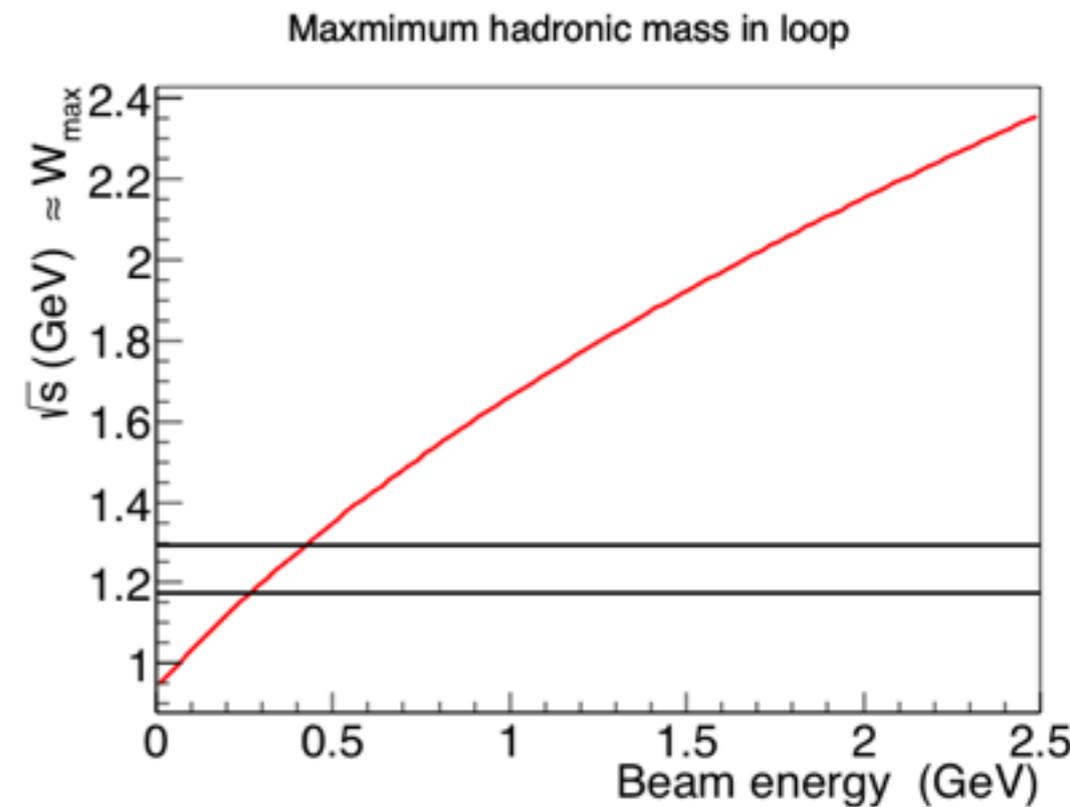


# Asymmetry calculations for $\Delta$ production

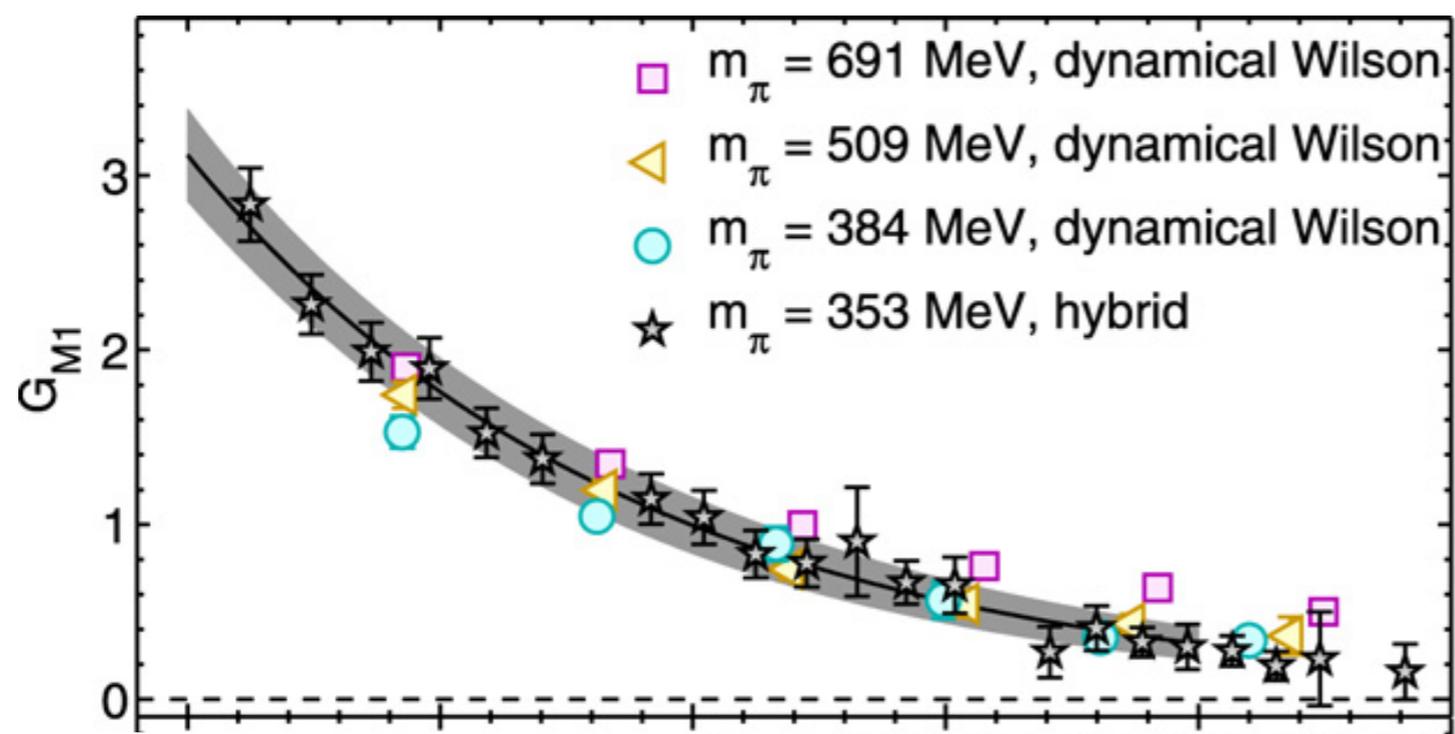


$$B_n = \frac{\sigma_{\uparrow} - \sigma_{\downarrow}}{\sigma_{\uparrow} + \sigma_{\downarrow}} = \frac{2\text{Im}(T_{2\gamma} \cdot T_{1\gamma}^*)}{|T_{1\gamma}|}$$

Some disagreement in the elastic scattering case (suspected missing intermediate states)  
 Treatment of additional intermediate states is difficult (transition to  $\Delta$ )  
 Higher beam energies allow more intermediate states

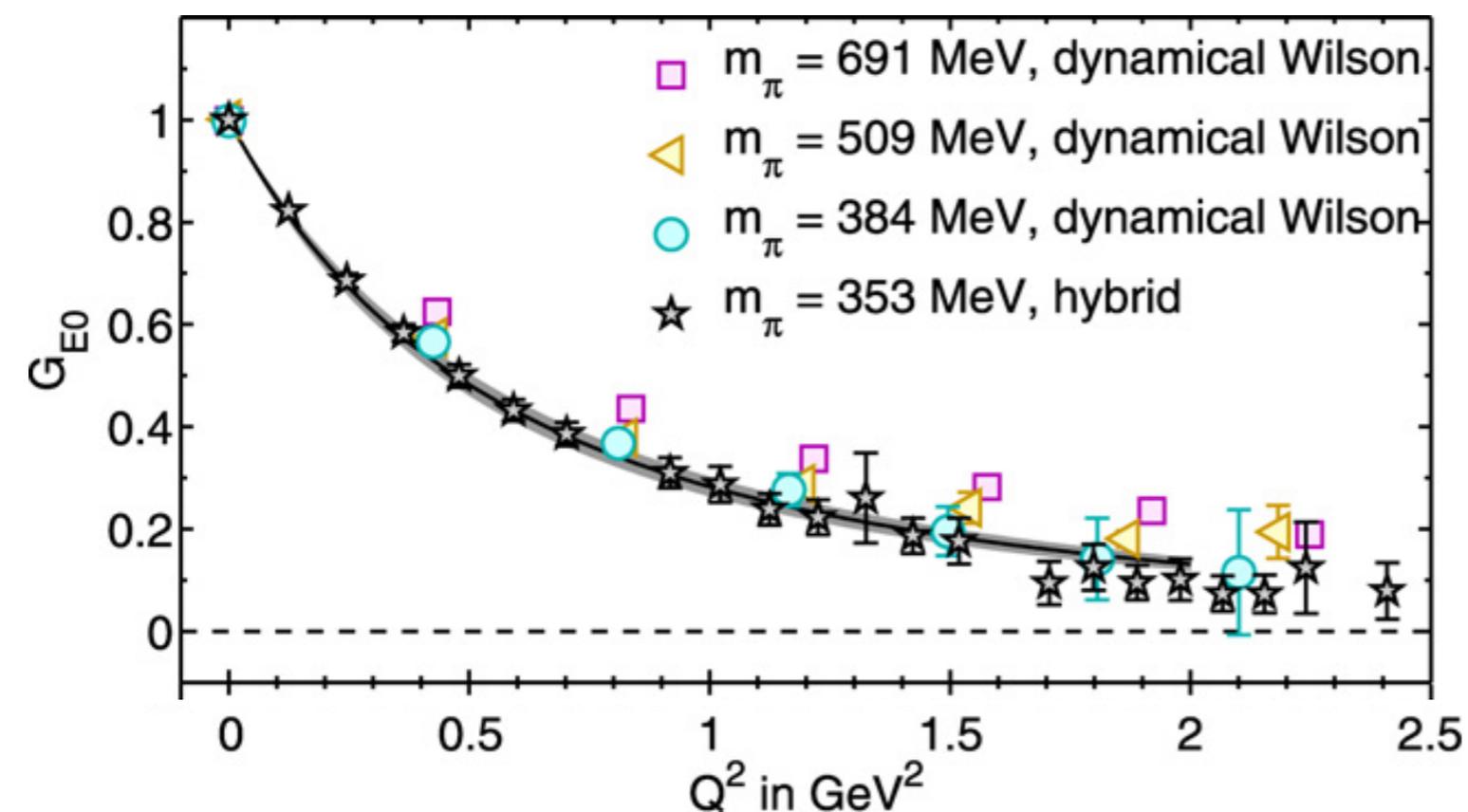


# Lattice Calculation of $\gamma^*\Delta\Delta$



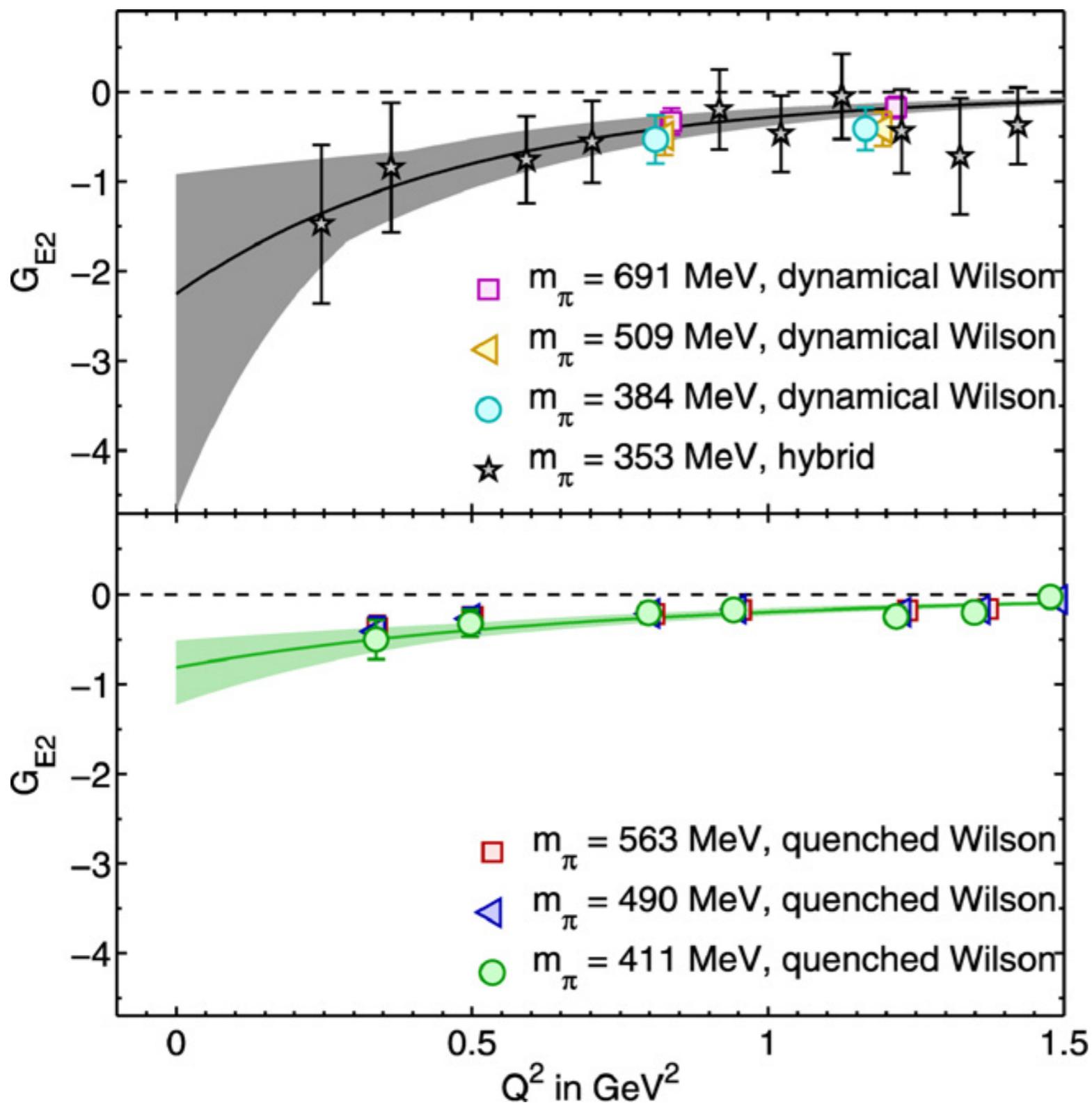
The  $\gamma\Delta\Delta$  form factor is obtained from lattice calculations with a stable  $\Delta$  assuming that the disconnected diagrams are small

$\Delta$  stable at these pion masses



C.Alexandrou et al.  
Nuclear Physics A 825 (2009) 115–144

# Lattice Calculation of $\gamma^* \Delta \Delta$



Factor of 2 difference in lattice results for quadrupole quenched or dynamical.

Octopole has large uncertainties, consistent with 0

C.Alexandrou et al.  
Nuclear Physics A 825 (2009) 115–144

# Parametrization of $\gamma\Delta\Delta$ form factors

$$G_{E_0}(Q^2) = \frac{1}{(1 + Q^2/\Lambda_{E_0}^2)^2}$$

$$G_{M_1}(Q^2) = G_{M_1}(0)e^{-Q^2/\Lambda_{M_1}^2}$$

$$G_{E_2}(Q^2) = G_{E_2}(0)e^{-Q^2/\Lambda_{E_2}^2}$$

$$G_{M_3}(Q^2) = 0$$

This parametrization fitted to lattice calculations and used in  $B_n$  calculation.

$$G_{E_0}(Q^2) = 1 - \frac{1}{6}R_{\Delta}^2 Q^2 + \dots$$

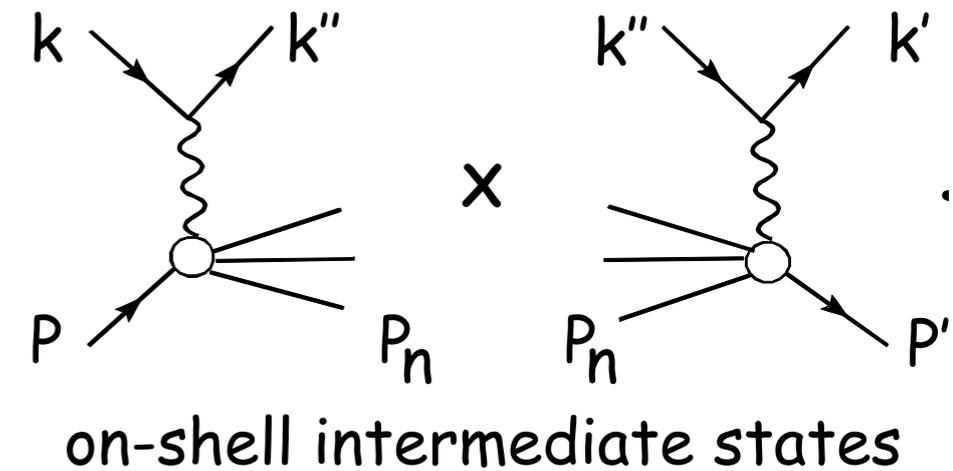
Alternate parametrization

How sensitive are calculations of the beam asymmetry to changes in:

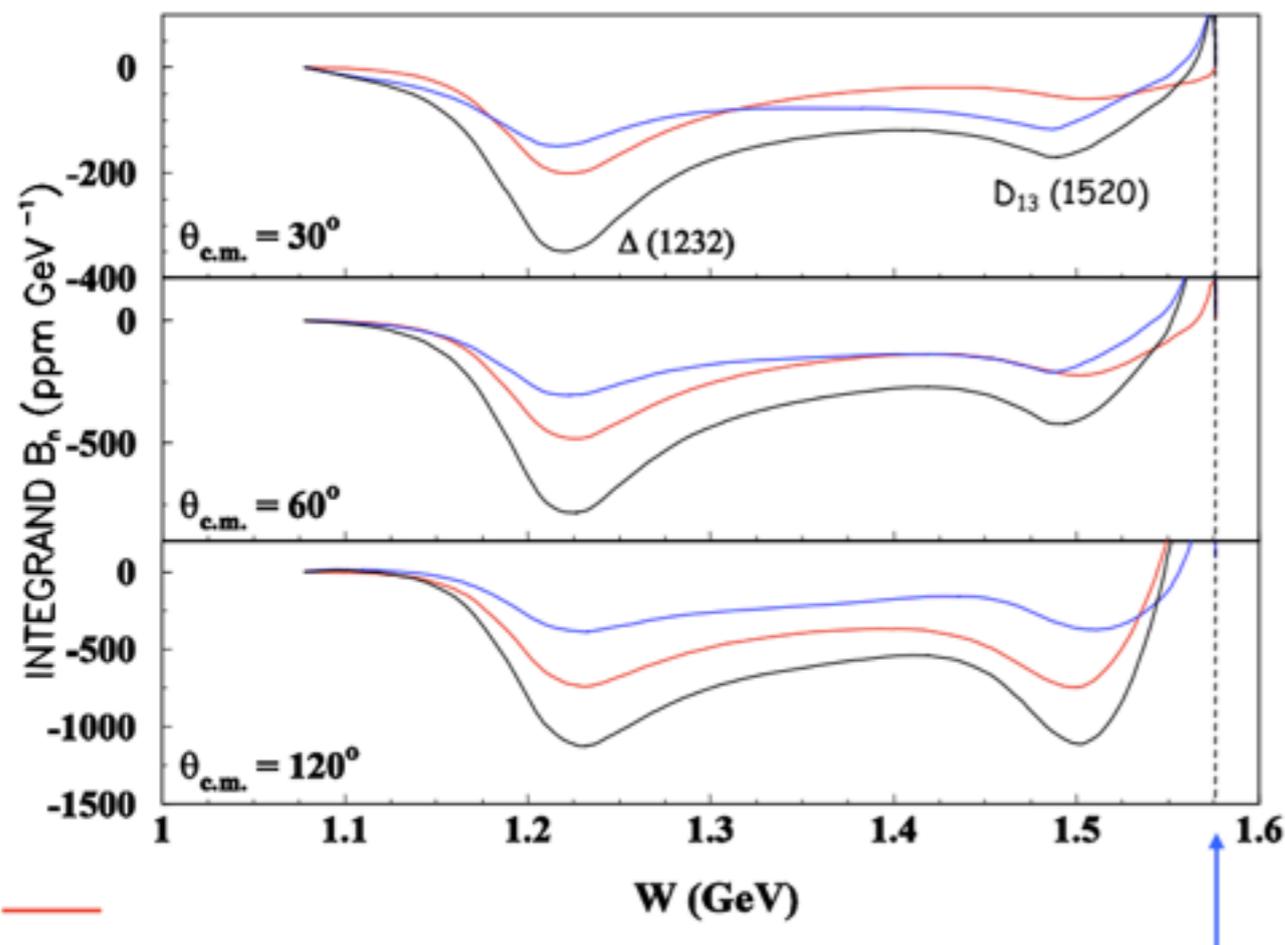
- parametrization of form-factors?
- parameters such as charge radius, magnetic moment, quadrupole moment, ... ?

# Calculation dependence on beam energy

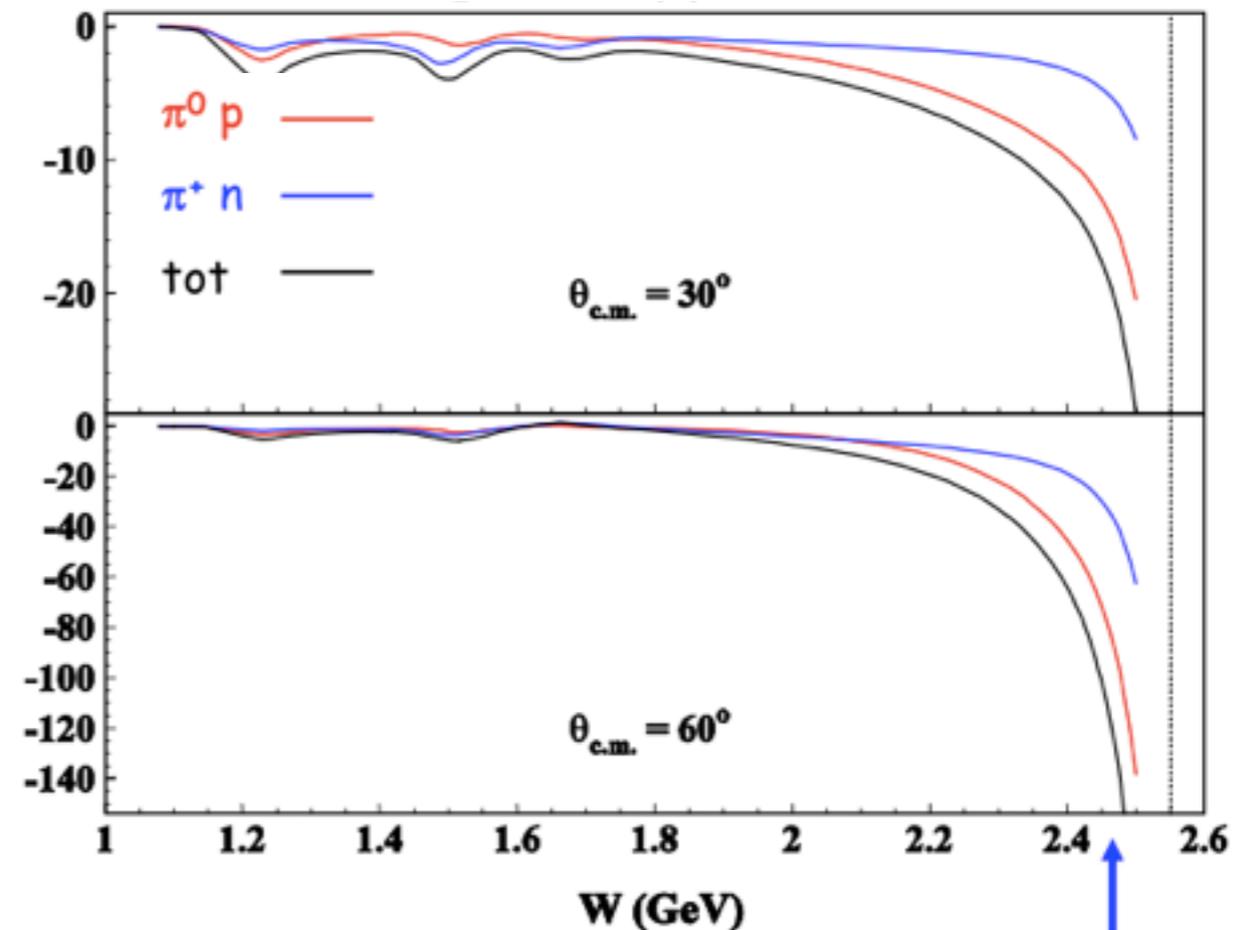
Example from calculation for elastic scattering  
 Higher beam energy increases maximum  
 intermediate hadronic mass



0.855 GeV



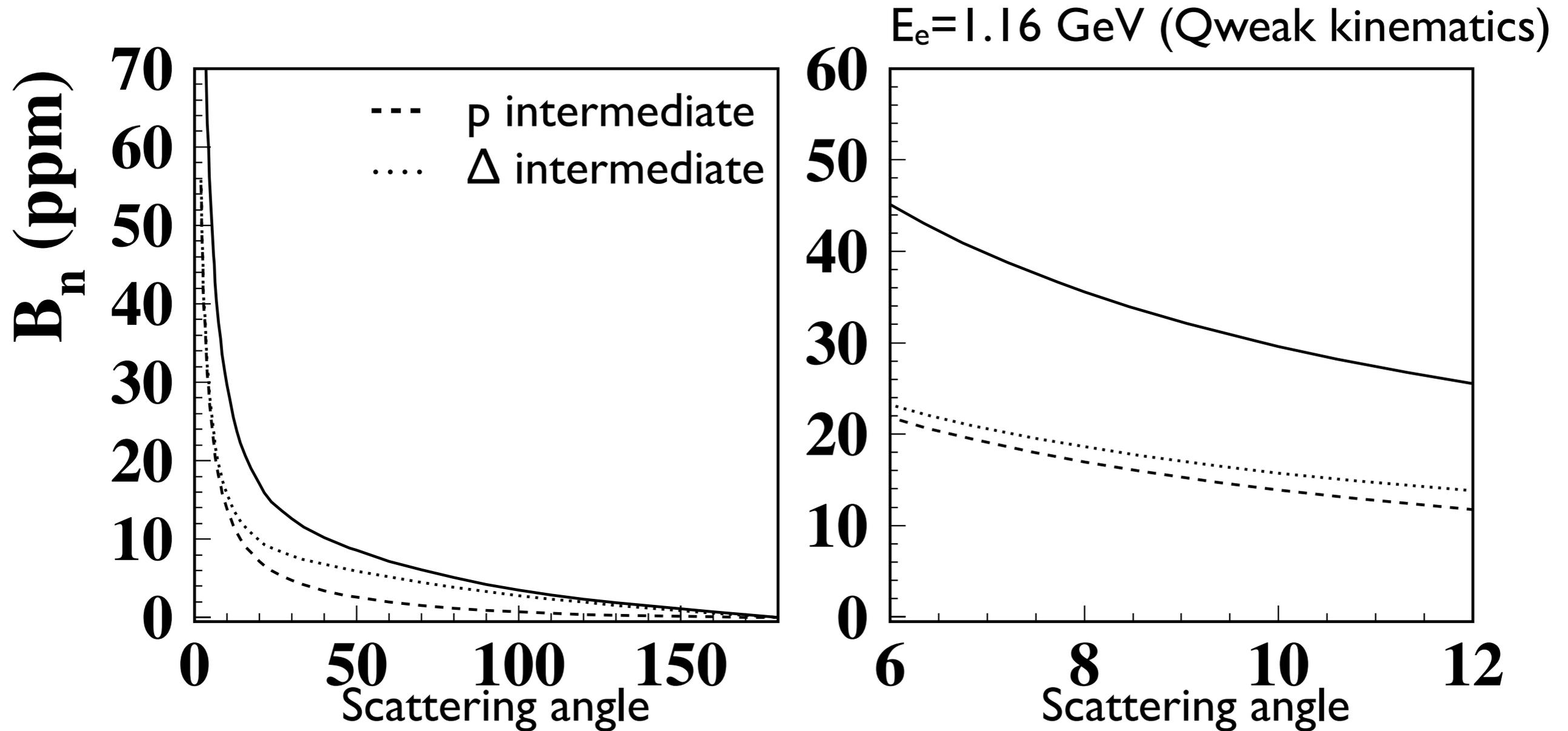
3 GeV



PRC 70, 045206 (2004) Pasquini & Vanderhaeghen

# $B_n$ asymmetry calculation

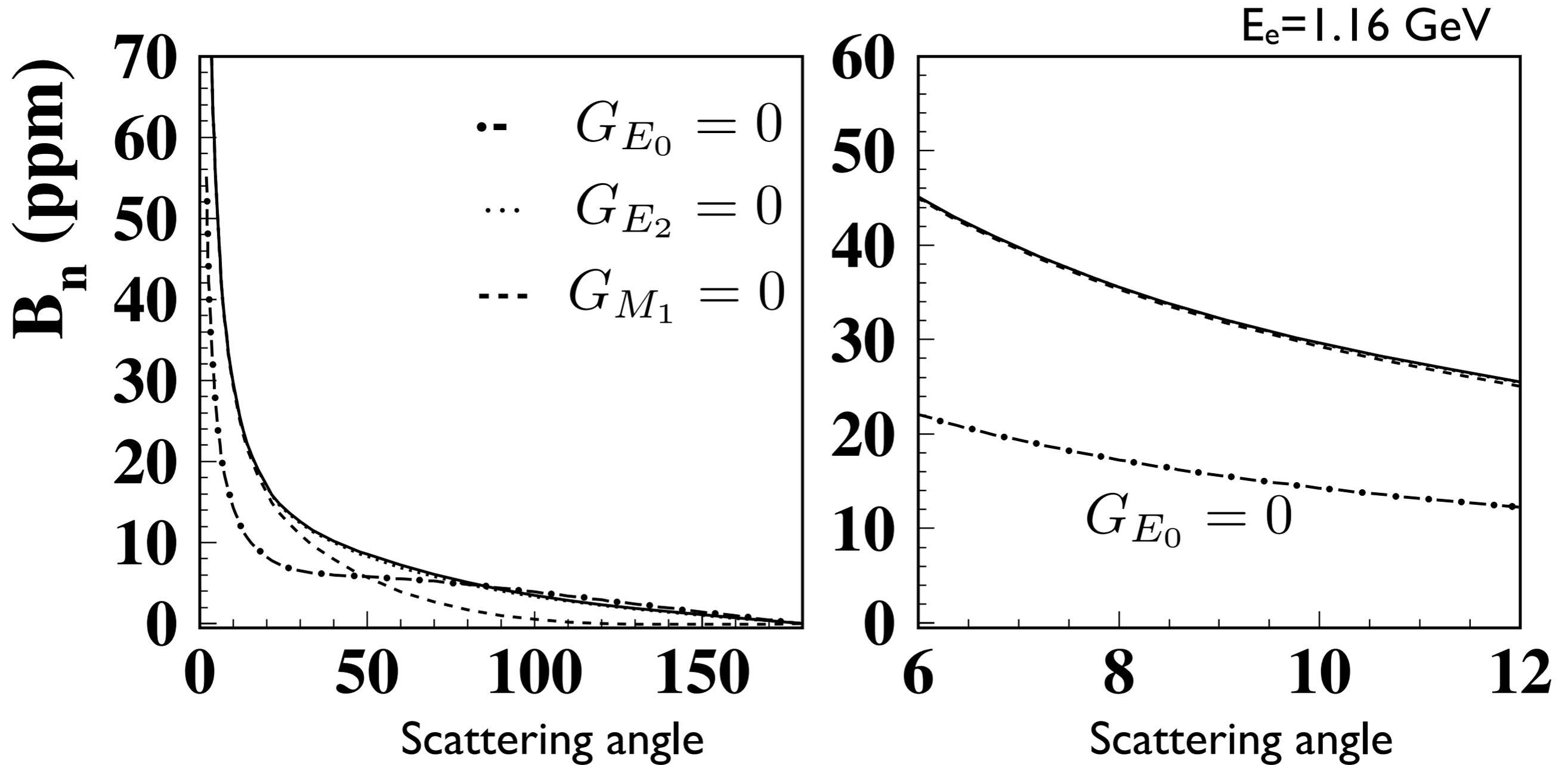
Asymmetry highest in forward direction where rates are highest, attractive for measurement.



$\Delta$  intermediate more dominant at larger angles

B Pasquini, private communication

# $B_n$ asymmetry sensitivity to form factors



Backward angles dominated by magnetic form factor  $G_{M_1}$

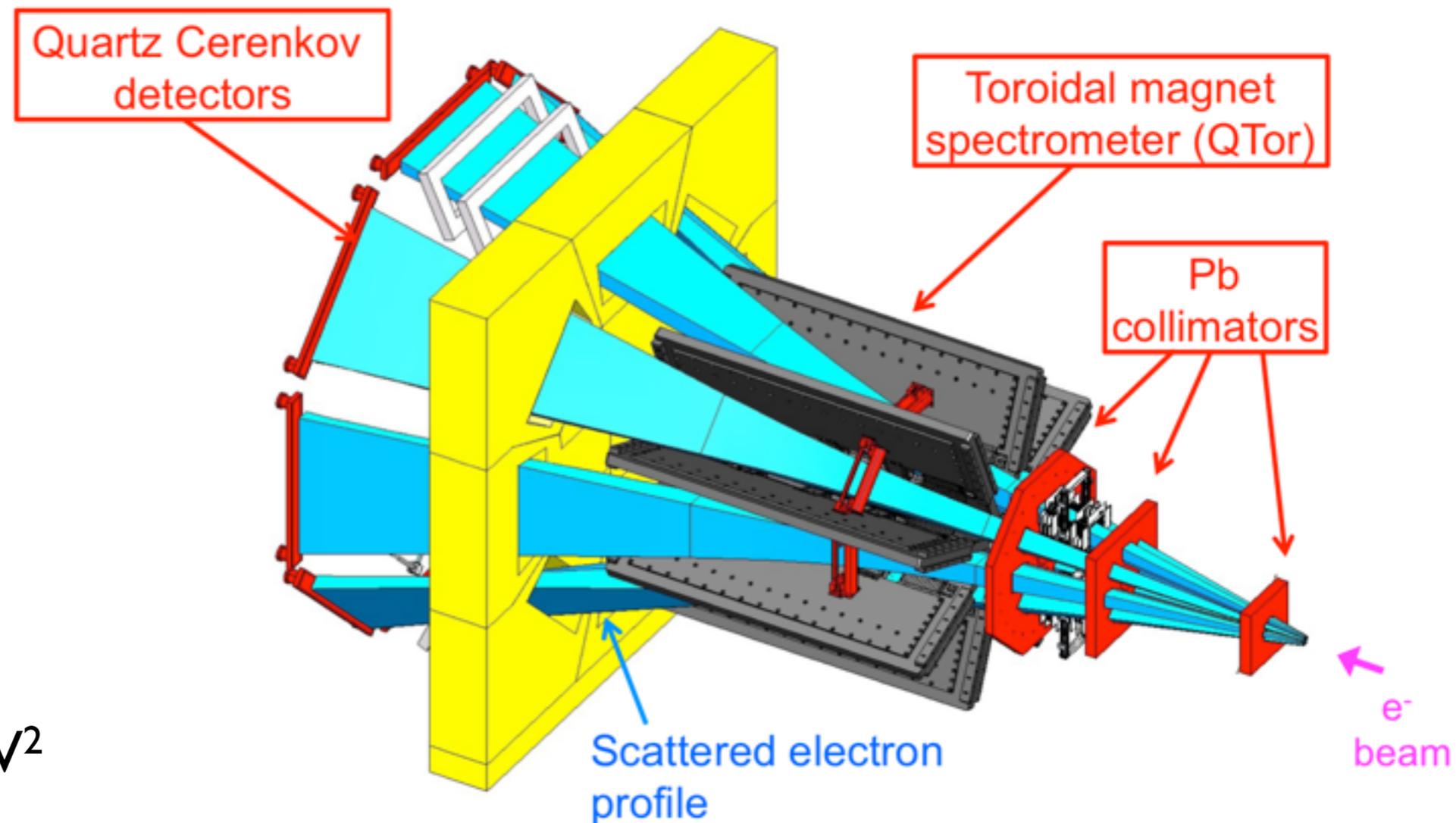
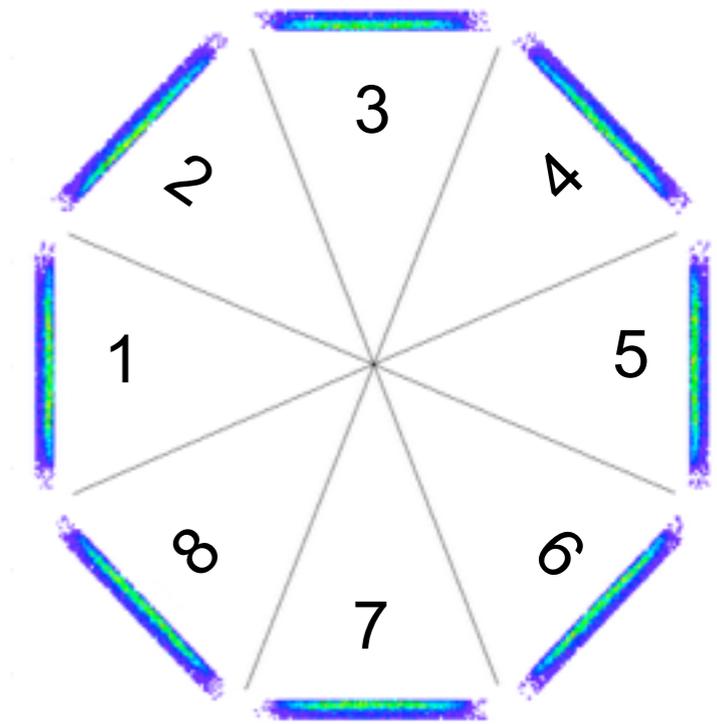
Forward angles dominated by charge form factor  $G_{E_0}$

B Pasquini, private communication

# Qweak Experiment

Designed to measure parity violation in ep scattering to order 10 parts per billion.

Measure transverse polarization asymmetry and inelastic asymmetry for background studies

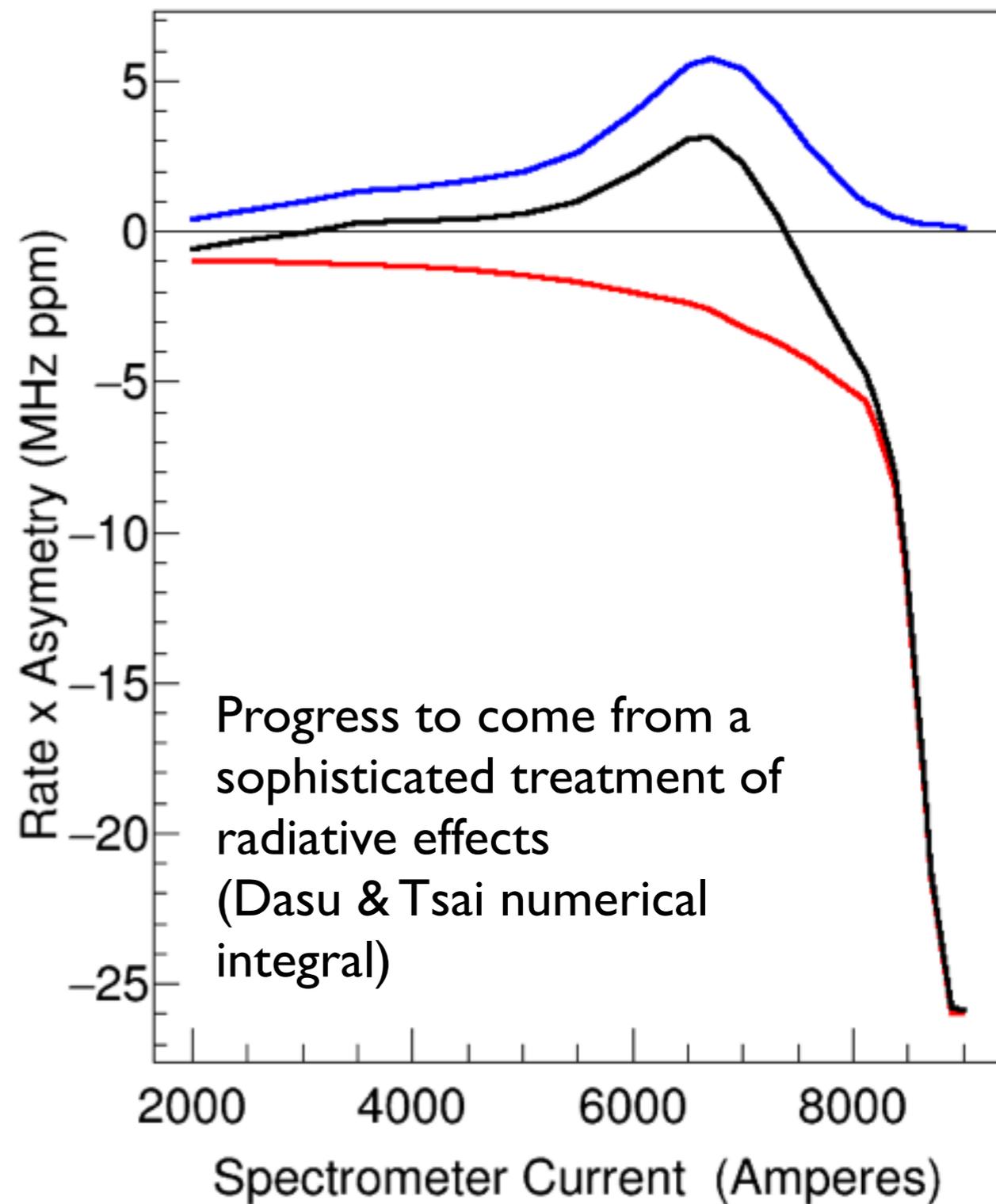
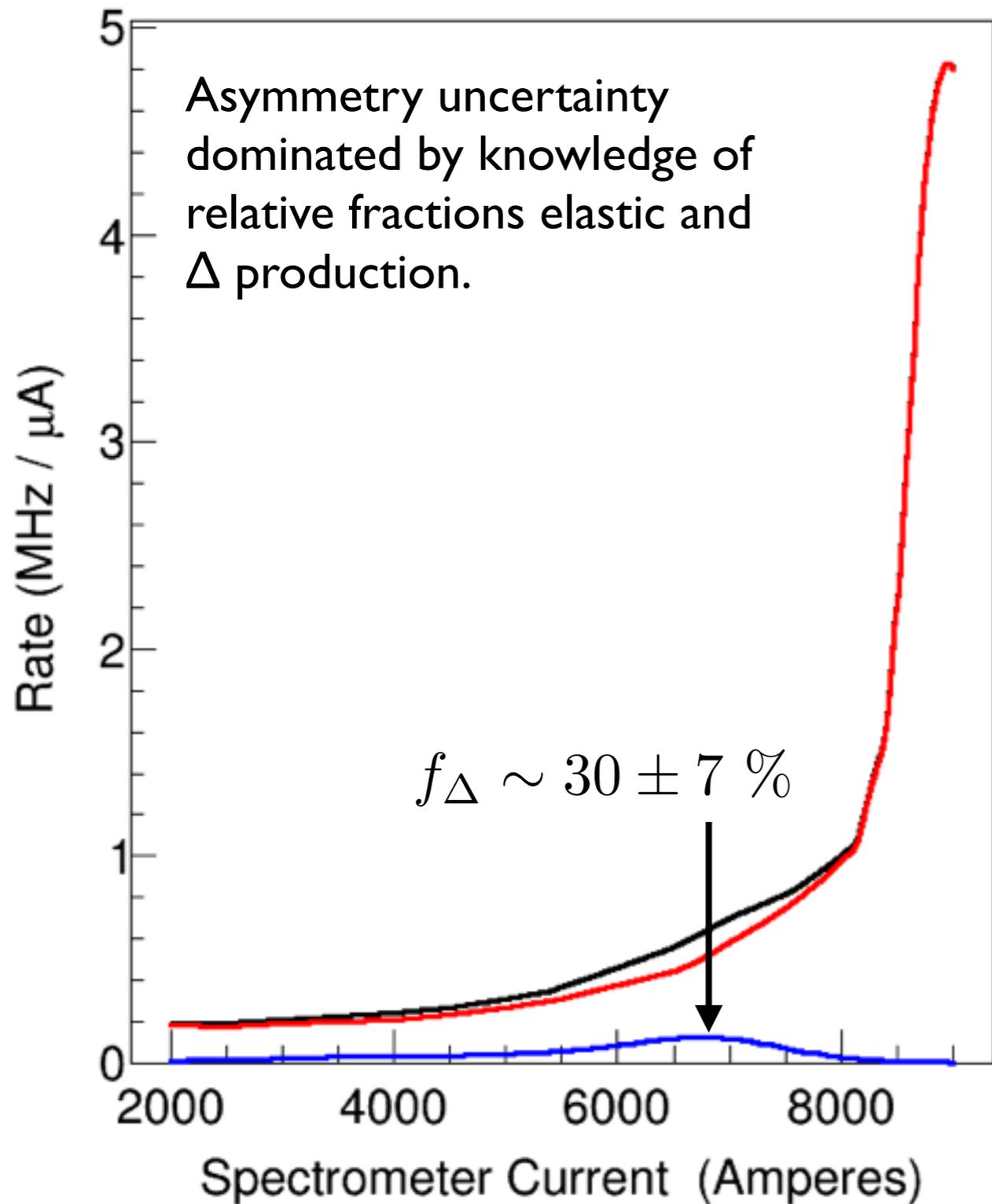


## $\Delta$ kinematics

- $\langle E \rangle = 1.16 \text{ GeV}$
- $\langle W \rangle \sim 1.2 \text{ GeV}$
- $\langle \theta \rangle \sim 8.3^\circ$
- $\langle Q^2 \rangle \sim 0.02 \text{ GeV}^2$

# Qweak $\Delta$ Production

Thick target, very forward kinematics — significant contribution from radiated elastic scattering



# Measured Asymmetries

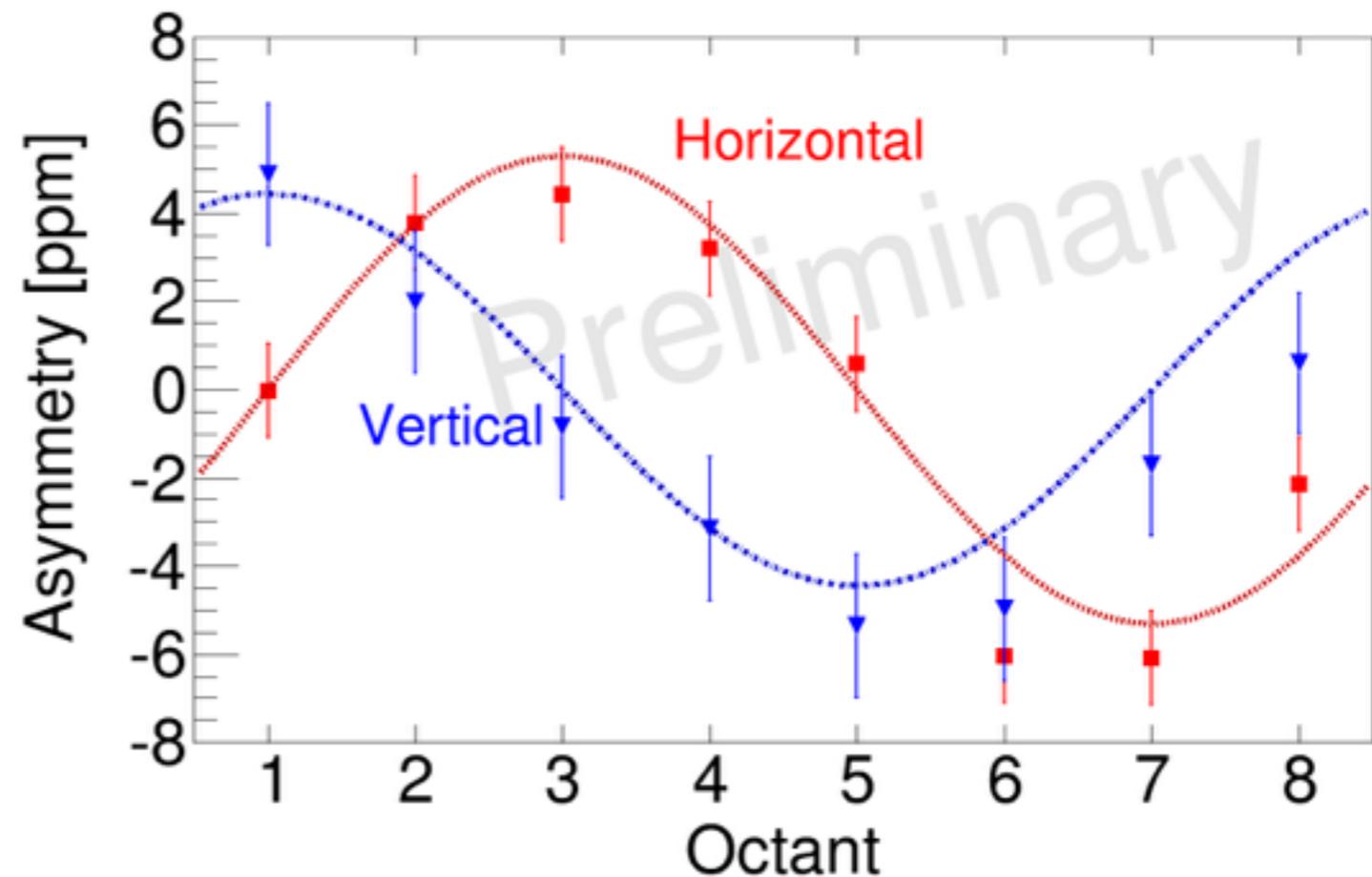
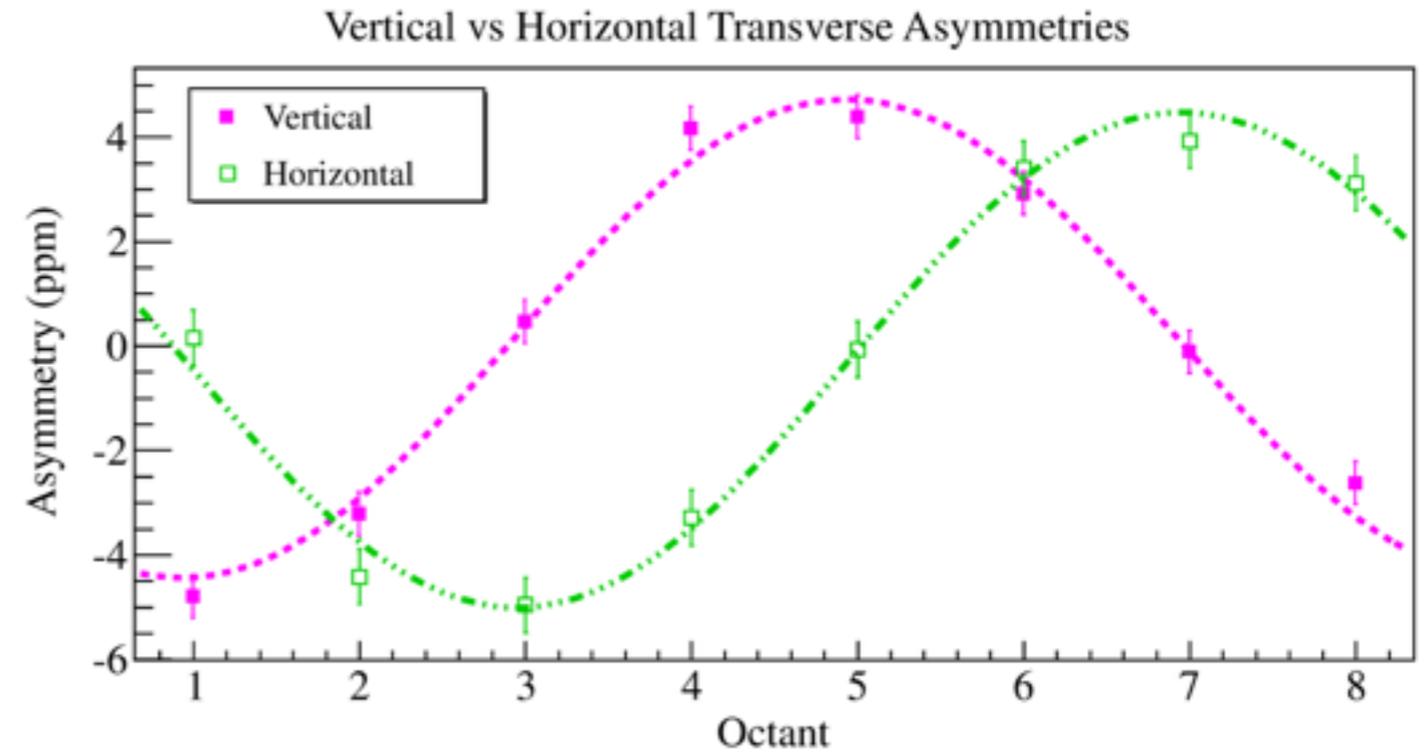
Measurement at elastic peak

$$B_n = -5.30 \pm 0.17 \text{ ppm}$$

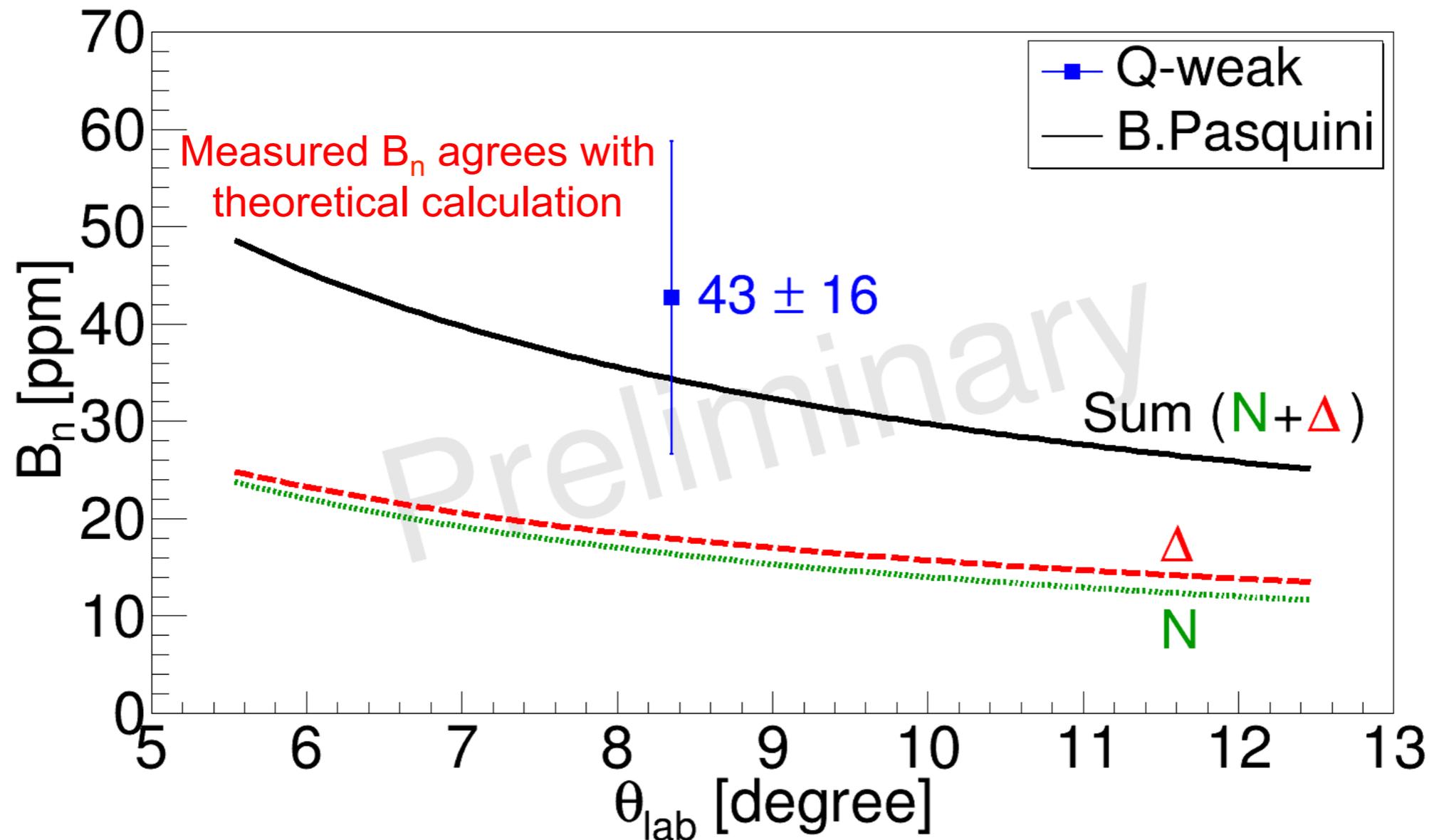
AIP Conf. Proc. 1560, 583 (2013) Waidyawansa

Measurement at  $\Delta$  peak

$$B_{\text{raw}} = 5.1 \pm 0.4 \text{ ppm}$$



# $B_n$ Asymmetry Extraction



Expect a significant decrease in uncertainty as radiative effects are understood. Similar available at 0.877 GeV.

More data is available at 1.60 GeV with different background fractions.

# PVA4 at Mainz

PVA4 at Mainz

First results expected during 2015.

$\theta = 30\text{-}40$  degrees

855 MeV:  $\delta A = 2.1$  ppm (stat)

1508 MeV:  $\delta A = 5.1$  ppm (stat)

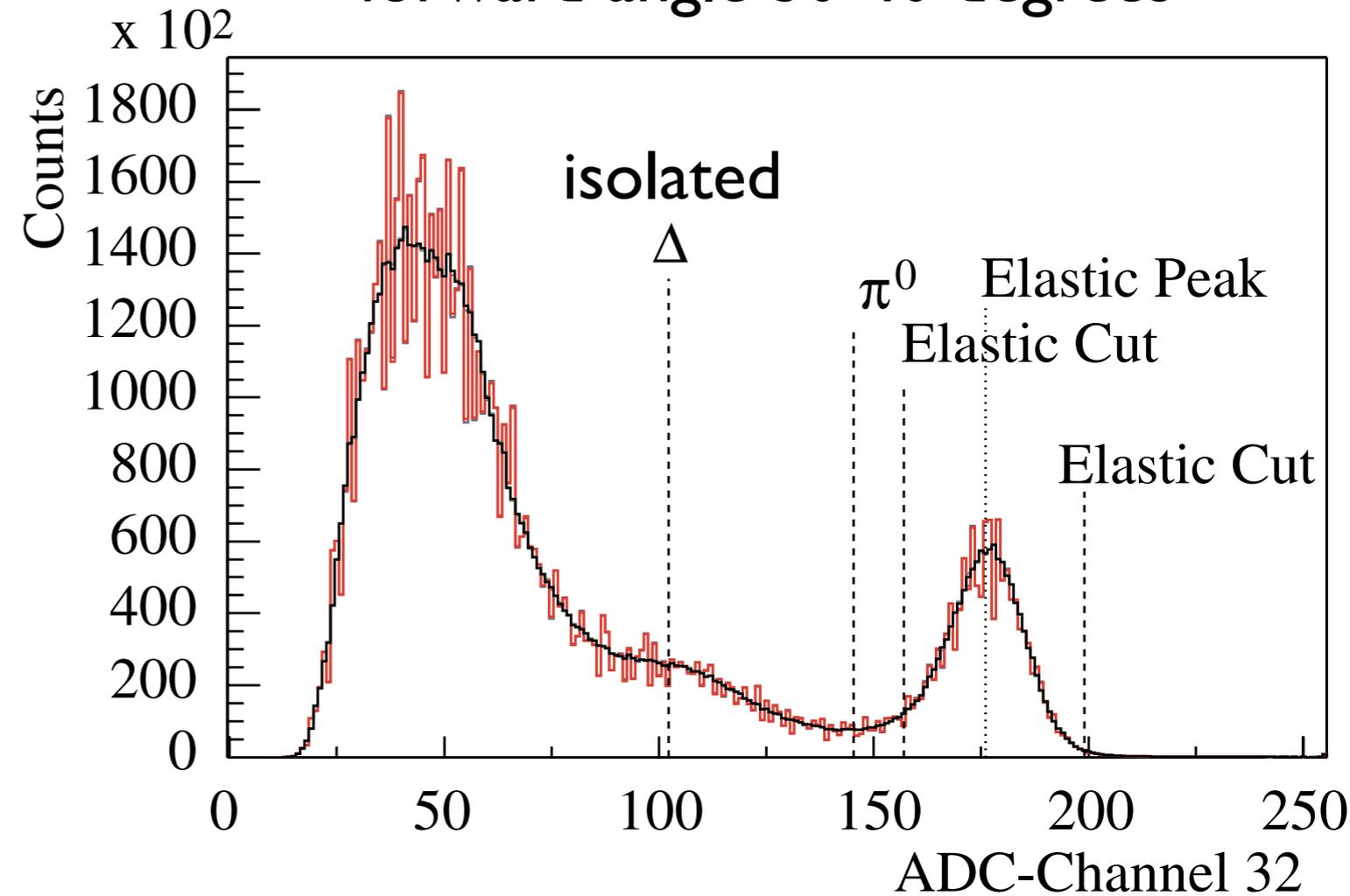
Potential data at:

420 MeV, 510 MeV, 570 MeV

$\theta = 30\text{-}40$  degrees

420 MeV,  $\theta = 140\text{-}150$  degrees

PVA4 raw spectrum,  $E=854$  MeV  
forward angle 30-40 degrees



PRL 93 (2004) 022002

Sebastian Baunack, private communication

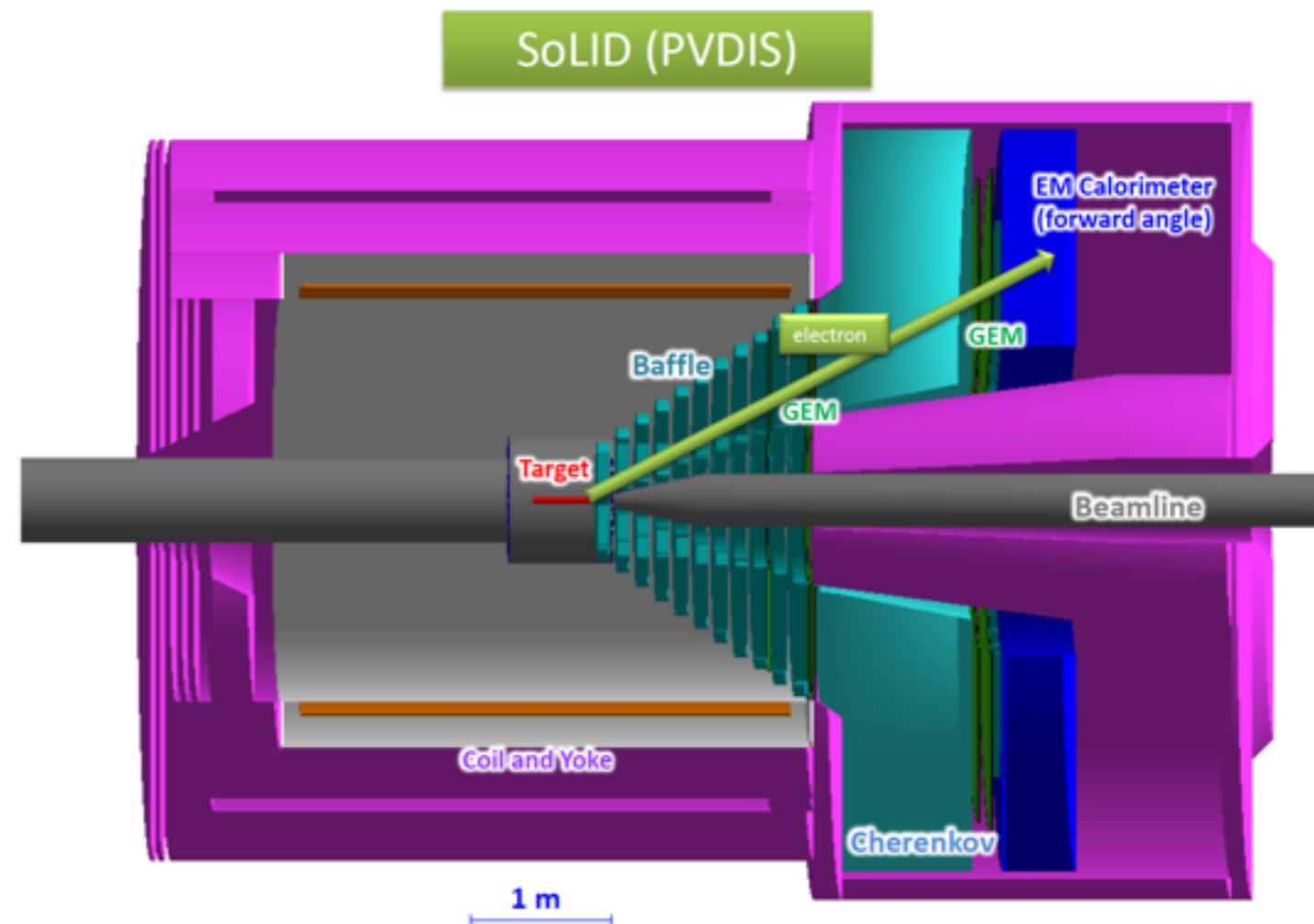
# Future Measurements

- AI at Mainz
- Cornell-BNL FFAG-ERL Test Accelerator
- Low Energy Recirculating Facility (LERF)
- SOLID at Jefferson Lab.

Intense Electron Beams  
Workshop,  
Cornell University,  
June 17-19 2015

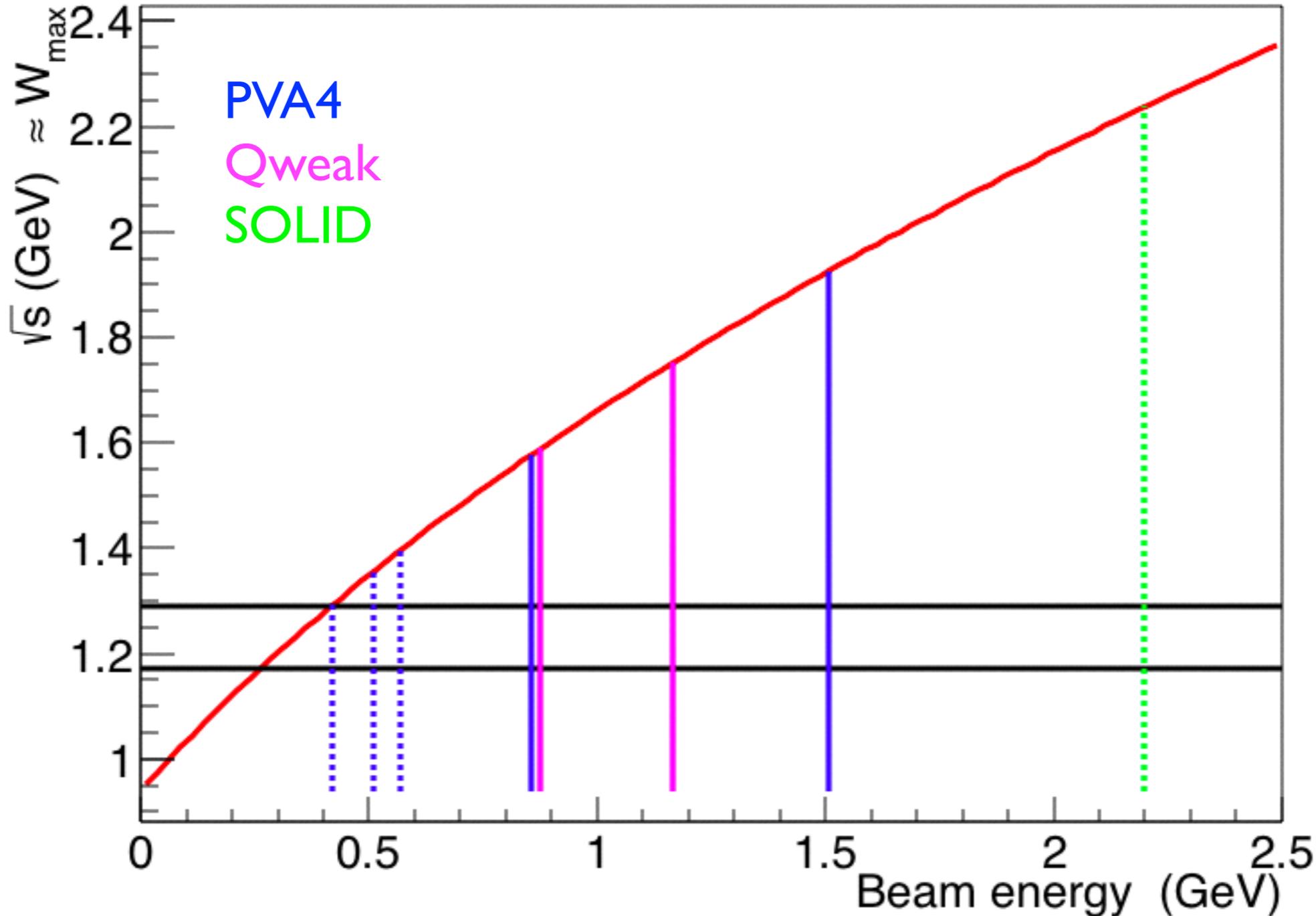
$20^\circ - 35^\circ$ ,  $\delta p/p \sim 2\%$   
some regions 10's of kHz/mm<sup>2</sup>,  
(Extremely high rate capabilities)

FOM (scattering rate,  
asymmetry and interpretability)  
increase to lower energy.



# Summary of measurements

Maximum hadronic mass in loop



# Summary

- The beam normal single spin asymmetry in  $\Delta$  production is sensitive to the  $\Delta$  elastic form-factors.
- Measurement of beam asymmetries is a robust, mature technique.
- Might allow for experimental testing of  $\Delta$  elastic form-factor calculations.
- Theoretical studies needed to determine sensitivity.
- Future measurements may be possible using parity-violation apparatus.

## Acknowledgements:

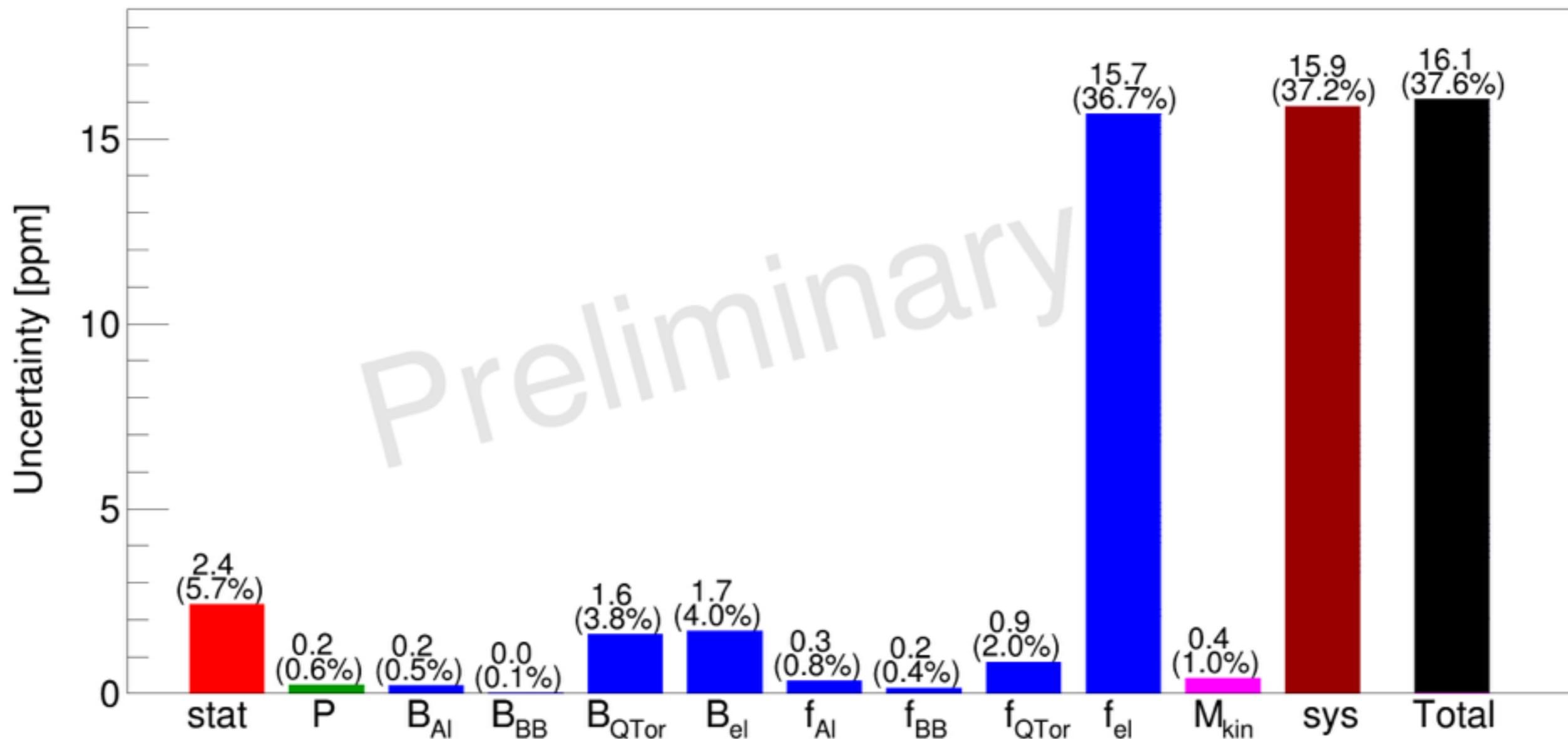
Barbara Pasquini, Carl Carlson, for helpful theoretical discussions.

Sebastian Baunack for Mainz data update.

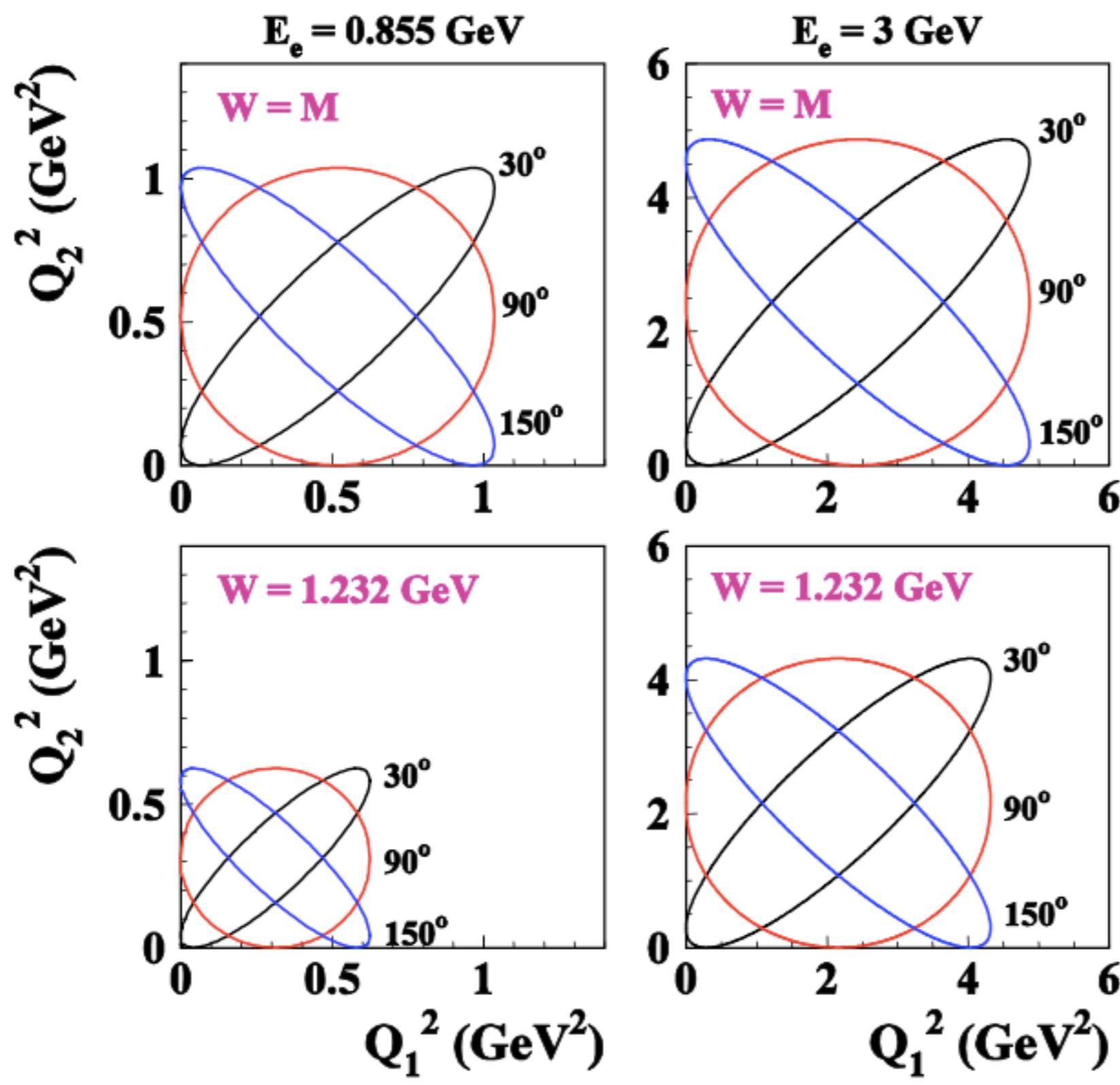
The Qweak Collaboration.

# Additional Material

# Error Budget



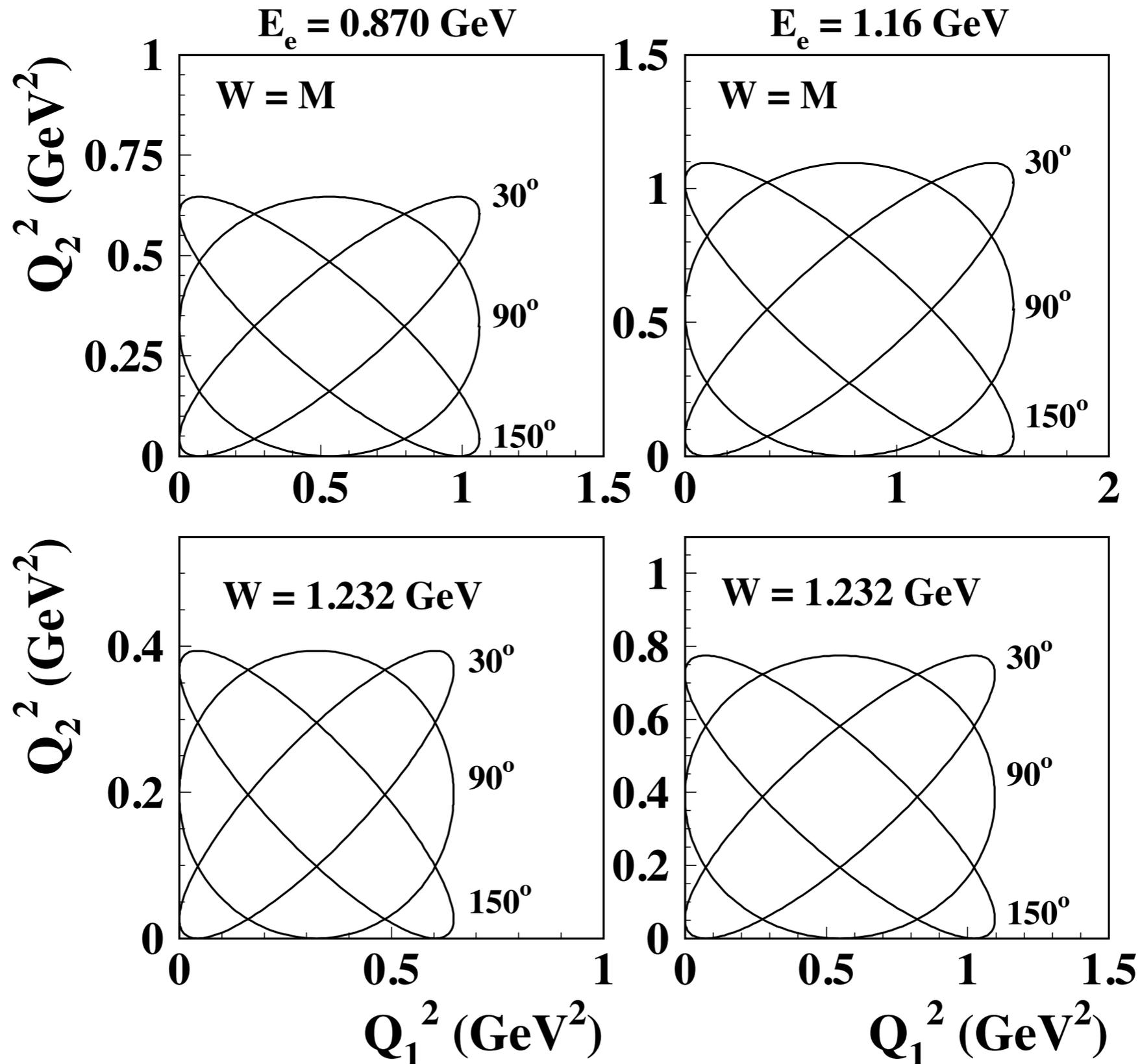
# Photon momenta elastic scattering



Elastic contribution

Inelastic contribution

# Photon momenta $\Delta$ production



# Intermediate states do not interfere (1st order)

$$M = \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \dots$$

$N$                    $\Delta$

$$\sigma = \left| \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \dots \right|^2$$

$N$                    $\Delta$

$$\sigma = \left| \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} \right|^2 + 2 \left( \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} \right) * \left( \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \dots \right) + \left| \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \dots \right|^2$$

$N$                    $\Delta$                    $N$                    $\Delta$

$$\sigma_{\uparrow} - \sigma_{\downarrow} = \left| \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} \right|_{[\uparrow - \downarrow]}^2 + 2 \left( \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} \right) * \left( \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \dots \right)_{[\uparrow - \downarrow]}$$

$N$                    $\Delta$

$$\sigma_{\uparrow} - \sigma_{\downarrow} = 2 \left( \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} \right) * \left( \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \begin{array}{|c|} \hline \text{---} \\ \hline \text{---} \\ \hline \end{array} + \dots \right)_{[\uparrow - \downarrow]}$$

$N$                    $\Delta$