



Theory Seminar, 02/14/11

Fragmentation Functions and Spin-Dependent PDFs

Status & Prospects

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outline



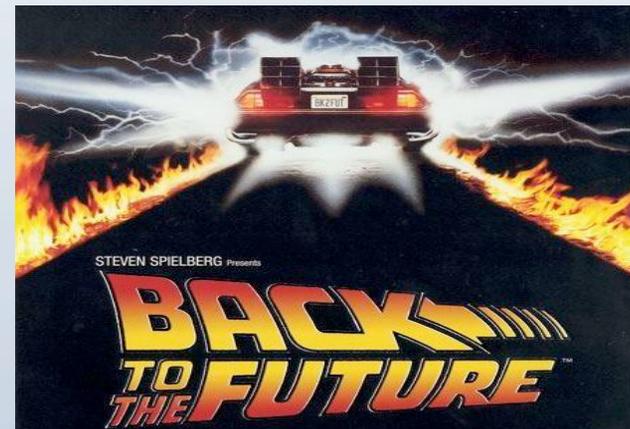
**ANATOMY OF A
GLOBAL QCD ANALYSIS
BRIEF OUTLINE**



**LONGITUDINAL SPIN STRUCTURE
STATUS, DSSV+, NEW DATA**



**FRAGMENTATION
STATUS, NEW RESULTS, NEW DATA**



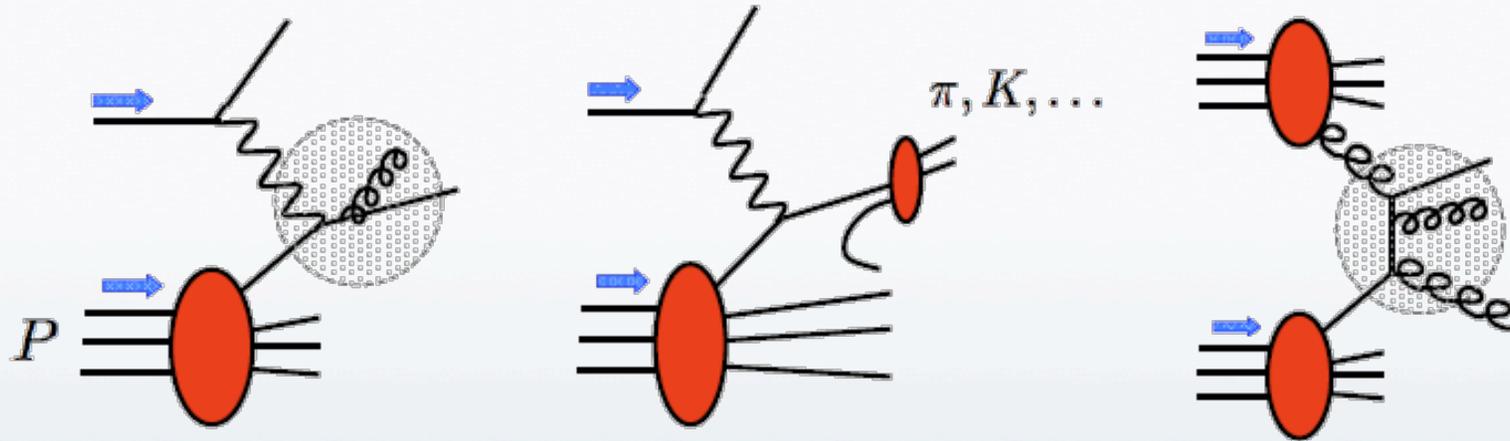
**FUTURE AVENUES
RHIC & OPPORTUNITIES AT AN EIC**



ANATOMY OF A GLOBAL QCD ANALYSIS

how to determine PDFs (and FFs) from data?

information on nucleon (spin) structure available from



DIS

SIDIS

hadron-hadron

task: extract reliable PDFs (or FFs) not just compare some curves to data

- all processes tied together: universality of pdfs & Q^2 - evolution
- each reaction provides insights into *different* aspects and kinematics
- need at least NLO for quantitative analyses; PDFs are not observables!
- information on PDFs "hidden" inside complicated (multi-)convolutions

a "global QCD analysis" is required

prerequisite: a reliable theoretical framework

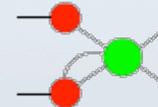
guiding principle: factorization

long-distance physics
 μ -dep. predicted by pQCD

$$\frac{d\sigma^{pp \rightarrow \pi X}}{dp_T d\eta} = \sum_{abc} \int dx_a dx_b dz_c f_a(x_a, \mu_f) f_b(x_b, \mu_f) D_c^\pi(z_c, \mu'_f) \times \frac{d\hat{\sigma}^{ab \rightarrow cX'}}{dp_T d\eta}(x_a P_a, x_b P_b, P^\pi / z_c, \mu_f, \mu'_f, \mu_r) + \mathcal{O}\left(\frac{\lambda}{p_T}\right)^n$$

short-distance physics
 calculable in pQCD as series in α_s

power corrections
 usually safely neglected

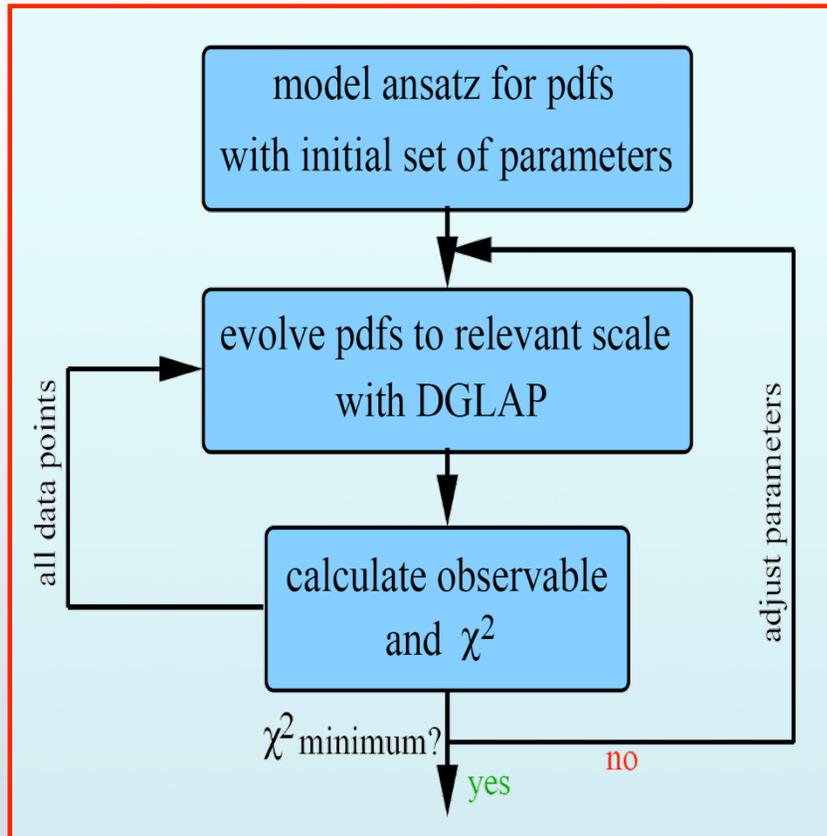


factorization ...

- ... separates physics happening at different time/distance scales
- ... introduces unphysical scales $\mu_{f,r}$ (leads to powerful RGE like DGLAP)
- ... requires presence of a hard scale (like Q in DIS or p_T in pp collisions)
- ... is an approximation - corrections are power suppressed
- ... leads to a successful quantitative description of many hard scattering proc's

outline of a global QCD analysis

start: choose fact. scheme (\overline{MS}, \dots) & pert. order (NLO, ...), select data sets, cuts, ...



flexible functional form to parametrize PDFs

$$f(x, \mu_0) = N x^\alpha (1-x)^\beta [1 + \kappa \sqrt{x} + \gamma x]$$

at some initial scale μ_0 (of order 1 GeV)

obtain PDFs at any $x, \mu > \mu_0$ relevant for comparing with data by solving evolution eqs.

compute DIS, pp, ... cross sections at NLO
judge goodness of current fit

$$\chi^2 = \sum_i \frac{(T_i - E_i)^2}{\delta E_i^2}$$

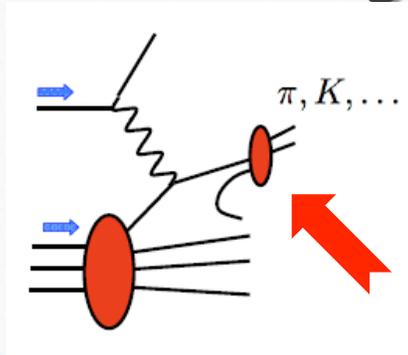
optimum set of parameters $\{\alpha_i, \beta_i, \dots\}$

recent achievement: also **quantify PDF uncertainties** and properly propagate them to any observable of interest



FRAGMENTATION

fragmentation functions: overview

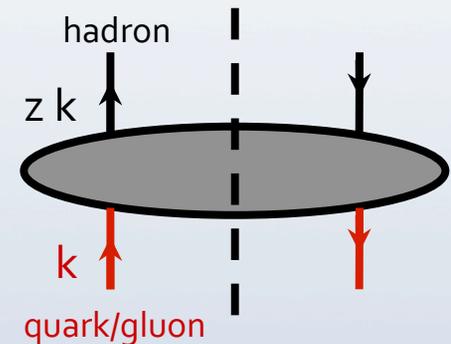


crucial for pQCD interpretation (factorization) of all data with detected (identified) hadrons, e.g., SIDIS (HERMES, COMPASS), $pp \rightarrow \pi X$ (PHENIX, ALICE, ...)

observation: all FFs based only on e^+e^- (LEP) data do a bad job here

some properties of $D_i^h(z, \mu)$ [very similar to PDFs]:

- **non-perturbative** but **universal**; pQCD predicts μ -dep.
- describe the *collinear* transition of a parton "i" into a massless hadron "h" carrying fractional momentum z



bi-local operator: $D(z) \simeq \int dy^- e^{iP^+ / zy^-} \text{Tr} \gamma^+ \langle 0 | \psi(y^-) |hX\rangle \langle hX| \bar{\psi}(0) |0\rangle$

Collins, Soper '81, '83

no inclusive final-state
no local OPE --> **no lattice formulation**

also: power corrections are much less developed and entwined with mass effects unlike for pdfs

timelike scale evolution of FFs

DGLAP
$$\frac{dD_i^h(z, \mu^2)}{d \ln \mu^2} = \int_z^1 \frac{dy}{y} P_{ji}^T(z, \alpha_s) D_j^h\left(\frac{z}{y}, \mu^2\right)$$

$$P_{ji}^T(z, \alpha_s) = \frac{\alpha_s}{4\pi} P_{ji}^{(0)T} + \left(\frac{\alpha_s}{4\pi}\right)^2 P_{ji}^{(1)T} + \left(\frac{\alpha_s}{4\pi}\right)^3 P_{ji}^{(2)T} + \dots$$

same as space-like
PDF evolution
Gribov-Lipatov relation

related to $P_{ij}^{(1)S}$ by
analytic continuation
Curci, Furmanski, Petronzio;
Floratos et al.; MS, Vogelsang

$P_{qq}^{(2)T}, P_{gg}^{(2)T}$ known
naive AC fails: π^2 terms
Moch, Vogt

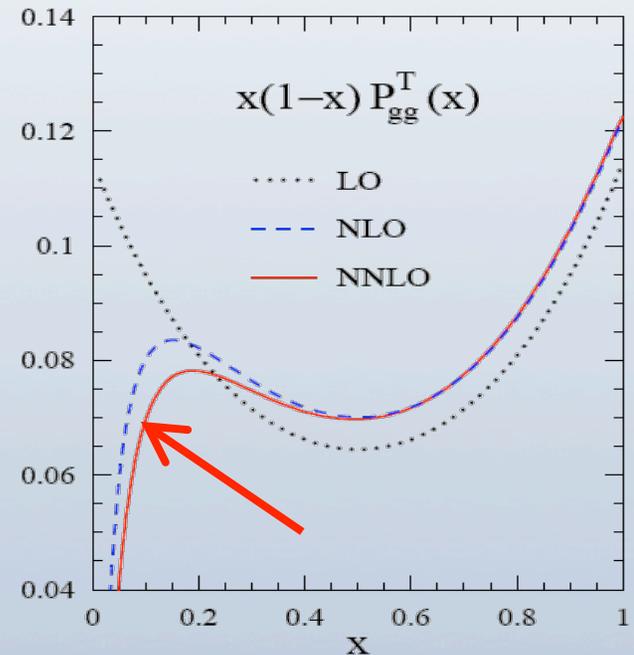
find

small- z behavior markedly different
from space-like case: much more singular

$$z P_{gg}^{(n)T} \propto \alpha_s^n \ln^{2n} z$$

has impact already at $z \simeq 0.1$

resummations ?





limitations for the use of FFs

- however, small z region completely spoiled by “mass effects”
[problem: hadron energy can be even smaller than its (neglected) mass]
→ need to introduce a cut on z , typically $z \gtrsim 0.05 \div 0.1$
- implies that sum rules are of limited practical use in fits of FFs
“energy-momentum conservation”: $\sum_h \int_0^1 z D_i^h(z, \mu) = 1$
(a parton fragments with 100% probability into *something* preserving its momentum)
- FFs are - by definition - inclusive quantities
→ can compute *inclusive distributions* of hadrons with momentum fractions z but *not* a cross section for a “leading hadron”
(under certain kin. conditions it might be a good approximation though)
- fragmentation is assumed to be independent of other colored particles
→ need a hard scale to be a valid approximation

DSS analysis: overview

D. de Florian, R. Sassot, MS
PRD 75 (2007) 114010
76 (2007) 074033

goal: provide NLO (LO) sets for pions, kaons, protons, charged hadrons from a **global fit** to e^+e^- , ep, and pp data on 1-hadron production

- requires a flexible functional form

$$D_i^h(z, 1 \text{ GeV}) = N_i z^{\alpha_i} (1-z)^{\beta_i} [1 + \gamma_i (1-z)^{\delta_i}]$$

- try to avoid assumptions on parameter space if possible

SU(2), SU(3) breaking: $D_{d+\bar{d}}^{\pi^+} = N D_{u+\bar{u}}^{\pi^+}$ $D_s^{\pi^+} = D_{\bar{s}}^{\pi^+} = N' D_{\bar{u}}^{\pi^+}$

only normalization shifts can be fitted

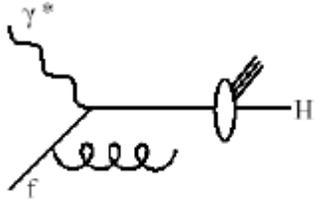
but data do not discriminate
between other unfavored FFs:

$$D_{\bar{u}}^{K^+} = D_s^{K^+} = D_d^{K^+} = D_{\bar{d}}^{K^+}$$

- like in PDF fits we allow for

- relative normalizations/shifts of data sets
- cuts: $z > 0.05$ pions, $z > 0.1$ otherwise
- extra "TH errors": scale uncertainty (pp); flavor tag; bin size, ...

good description of SIDIS multiplicities



HERMES data (not yet final)
A. Hillenbrand (thesis)

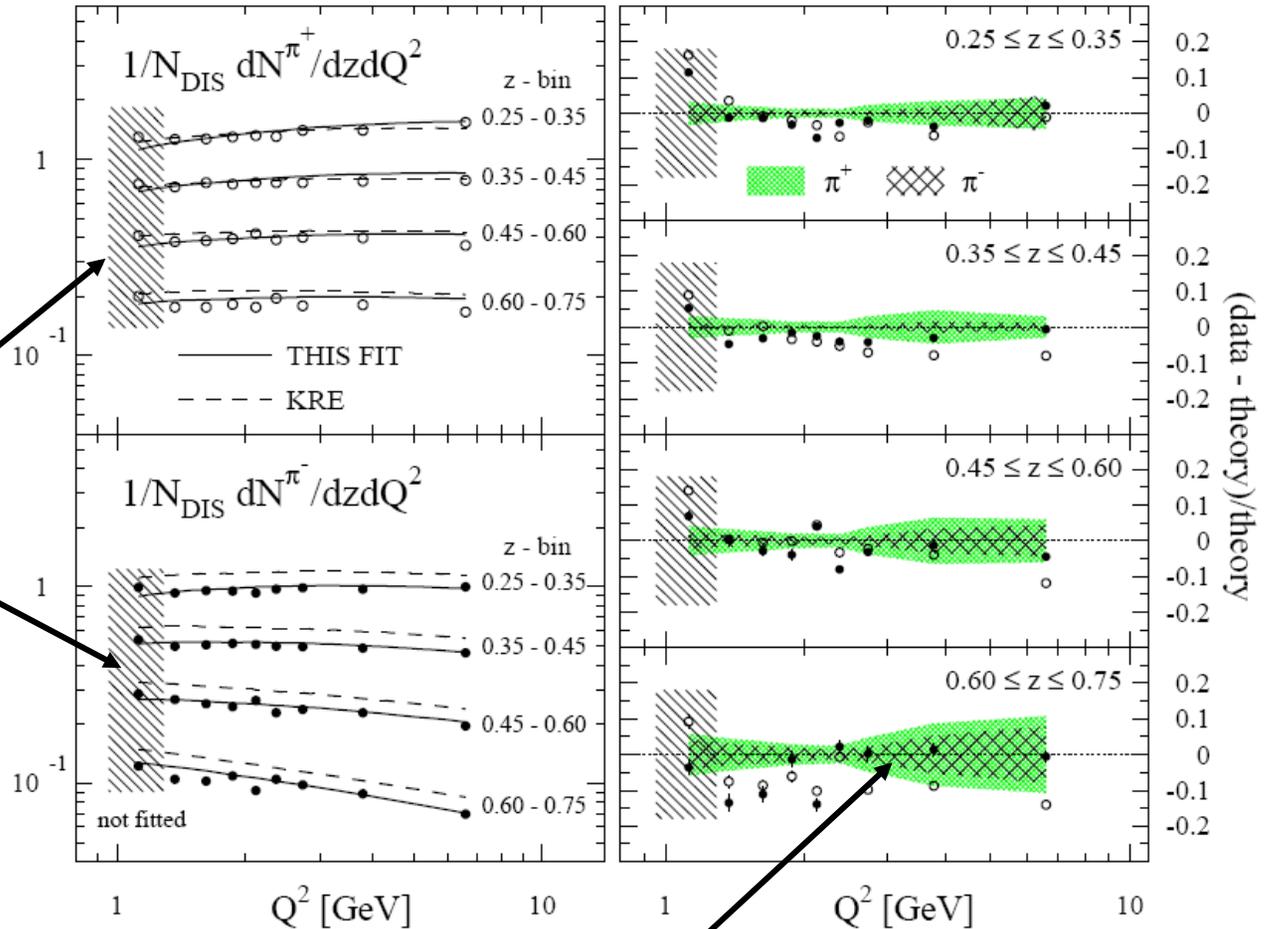
Kretzer's assumption

$$D_d^{\pi^+} \simeq (1-z) D_u^{\pi^+}$$

works for π^+
but not for π^-

π^+

π^-

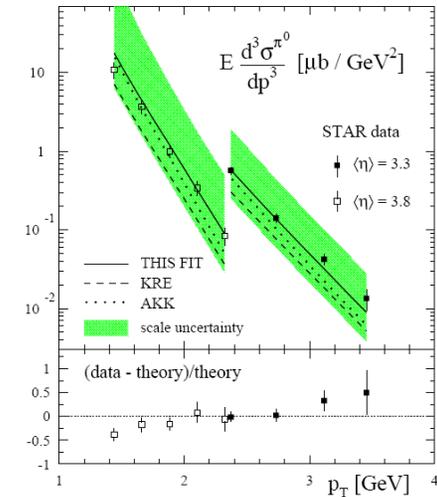
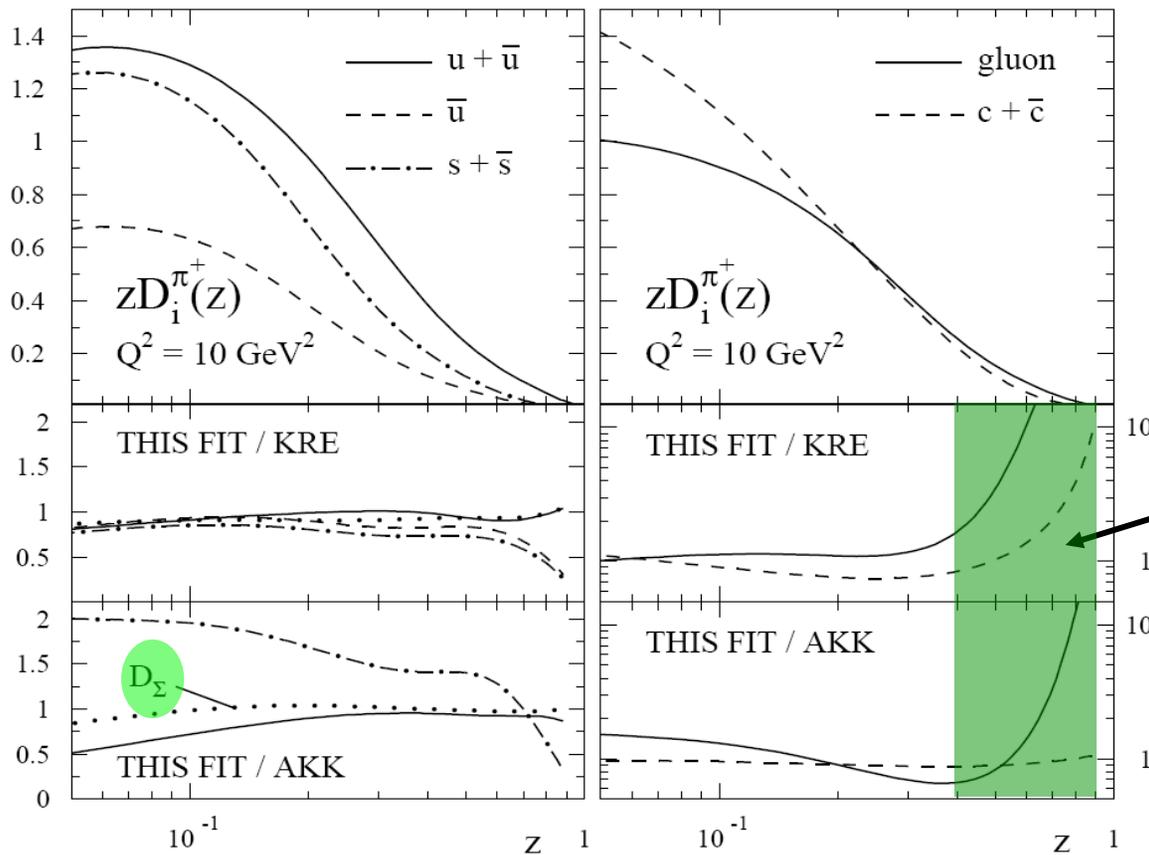


x, Q^2 range can be significantly extended at an EIC

shaded bands:
our estimate of
"Q²-binning effects"

meet the $D_i(z)$'s for pions

$\langle z \rangle \gtrsim 0.6$



z-range of
RHIC pp data
explains
differences in D_g

- singlet fragmentation D_Σ very similar (fixed by SIA at M_Z)
- u-frag. smaller than in AKK (due to SIDIS) ; compensated by larger D_s in SIA
- find: SU(2) violation $< 10\%$; SU(3) violation $\simeq 17\%$ (with large uncertainties)

charge symmetry violation ?

fit prefers a $\approx 9\%$ breaking (within large uncertainties!) driven by π^\pm multiplicities

small, large, or just about right

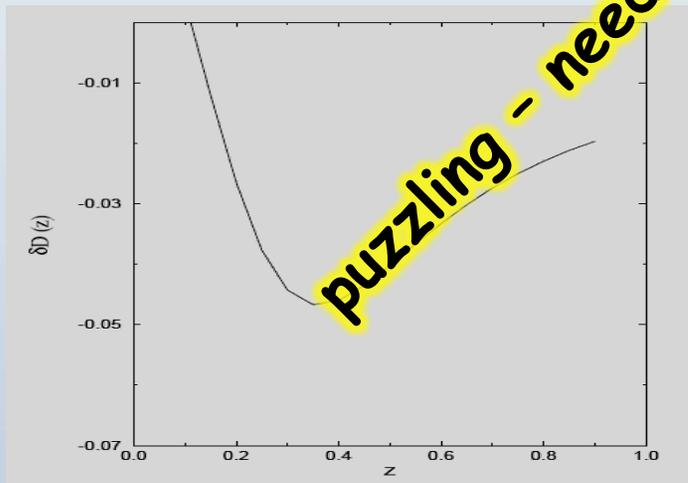
estimate magnitude in a simple model

define charge-symmetry breaking as

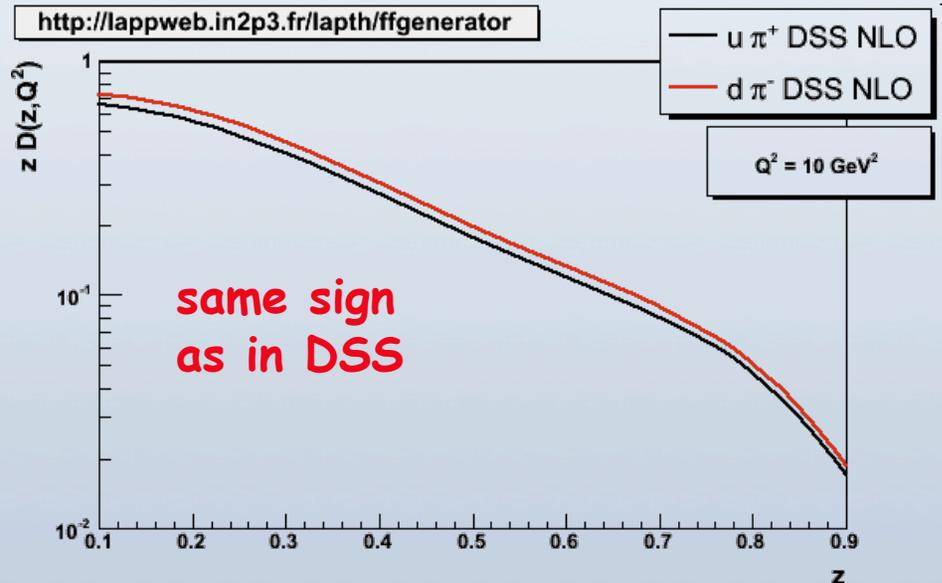
$$\delta D(z) = \frac{D_u^{\pi^+} - D_d^{\pi^-}}{D_u^{\pi^+}}$$

find $\delta D(z) < 0$ and $O(\text{few percent})$

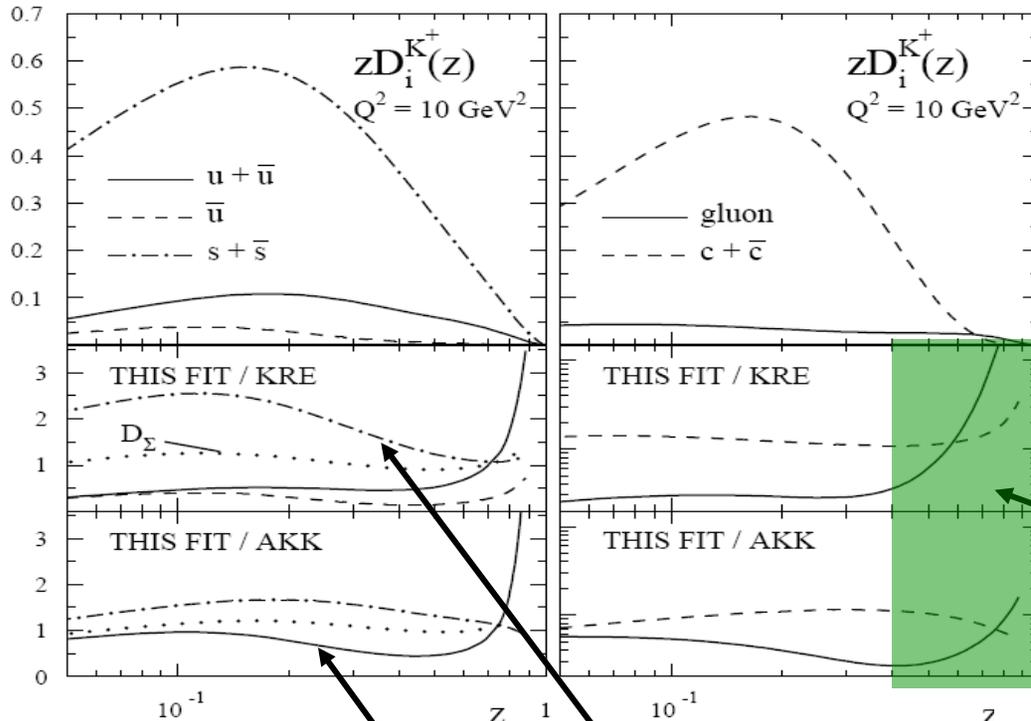
Londregan, Pang, Thomas
PRD54 (1996) 3154



puzzling - need precision data to settle this



meet the $D_i(z)$'s for kaons

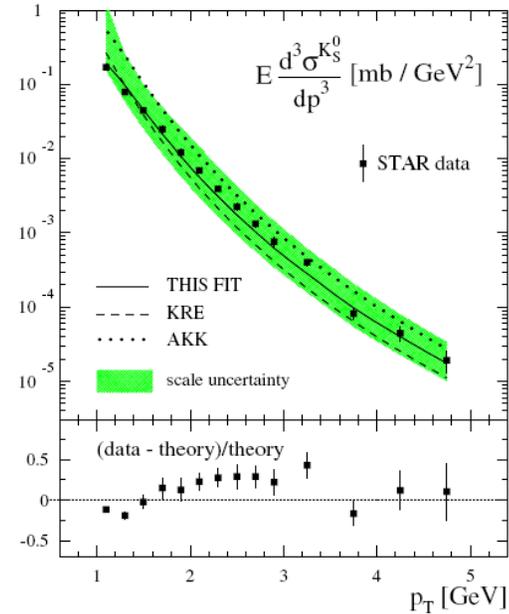


smaller u & larger s-frag.
required by SIDIS data

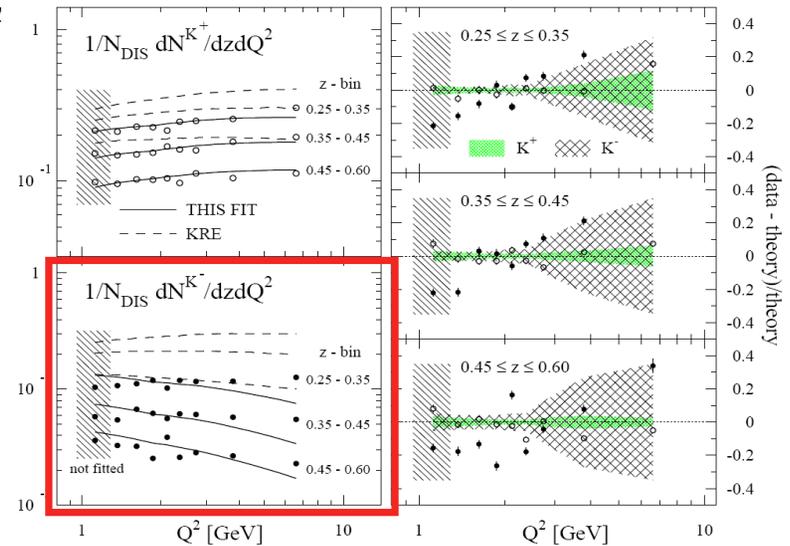
impact on PDF fits: Δs

note: some issues with K^- data (slope!)

await final HERMES data



again, RHIC pp data
explain different D_g



other recent fits of NLO FFs

table from arXiv:0804.2021 (ECT* FF workshop)

Name	Ref.	Species	Error	z_{\min}	Q^2 (GeV ²)
AKK	[4]	$\pi^\pm, K^\pm, K_s^0, p, \bar{p}, \Lambda, \bar{\Lambda}$	no	0.1	$2 - 4 \cdot 10^4$
AKK08	[5]	$\pi^\pm, K^\pm, K_s^0, p, \bar{p}, \Lambda, \bar{\Lambda}$	yes	0.05	$2 - 4 \cdot 10^4$
BKK	[6]	$\pi^+ + \pi^-, \pi^0, K^+ + K^-, K^0 + \bar{K}^0, h^+ + h^-$	no	0.05	$2 - 200$
BFG	[7]	γ	no	10^{-3}	$2 - 1.2 \cdot 10^4$
BFGW	[8]	h^\pm	yes ¹	10^{-3}	$2 - 1.2 \cdot 10^4$
CGRW	[9]	π^0	no	10^{-3}	$2 - 1.2 \cdot 10^4$
DSS	[10, 11]	$\pi^\pm, K^\pm, p, \bar{p}, h^\pm$	yes ²	0.05-0.1	$1 - 10^5$
DSV	[12]	polarized and unpolarized Λ	no	0.05	$1 - 10^4$
GRV	[13]	γ	no	0.05	≥ 1
HKNS	[14]	$\pi^\pm, \pi^0, K^\pm, K^0 + \bar{K}^0, n, p + \bar{p}$	yes	0.01 - 1	$1 - 10^8$
KKP	[15]	$\pi^+ + \pi^-, \pi^0, K^+ + K^-, K^0 + \bar{K}^0, p + \bar{p}, n + \bar{n}, h^+ + h^-$	no	0.1	$1 - 10^4$
Kretzer	[16]	$\pi^\pm, K^\pm, h^+ + h^-$	no	0.01	$0.8 - 10^6$

AKK08: Albino, Kniehl, Kramer

||

HKNS: Hirai, Kumano, Nagai, Sudoh

e^+e^- & pp data

impose isospin sym. for pions

Hessian method for uncertainties

fit hadron masses

large-z resummations

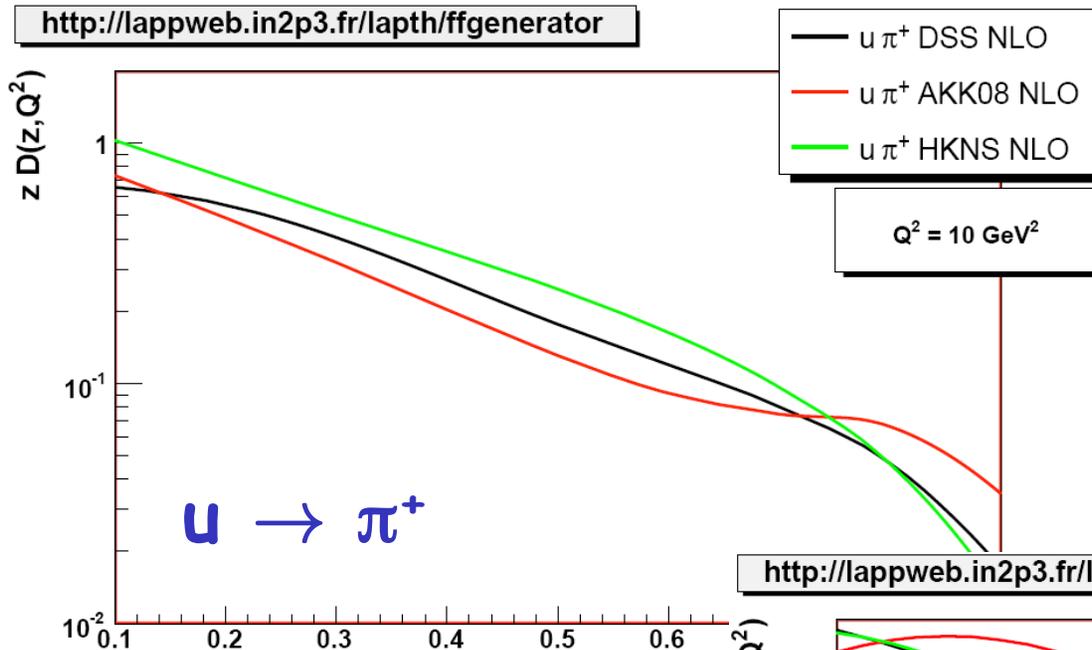
mass corrections (look ad hoc for pp)

e^+e^- data only

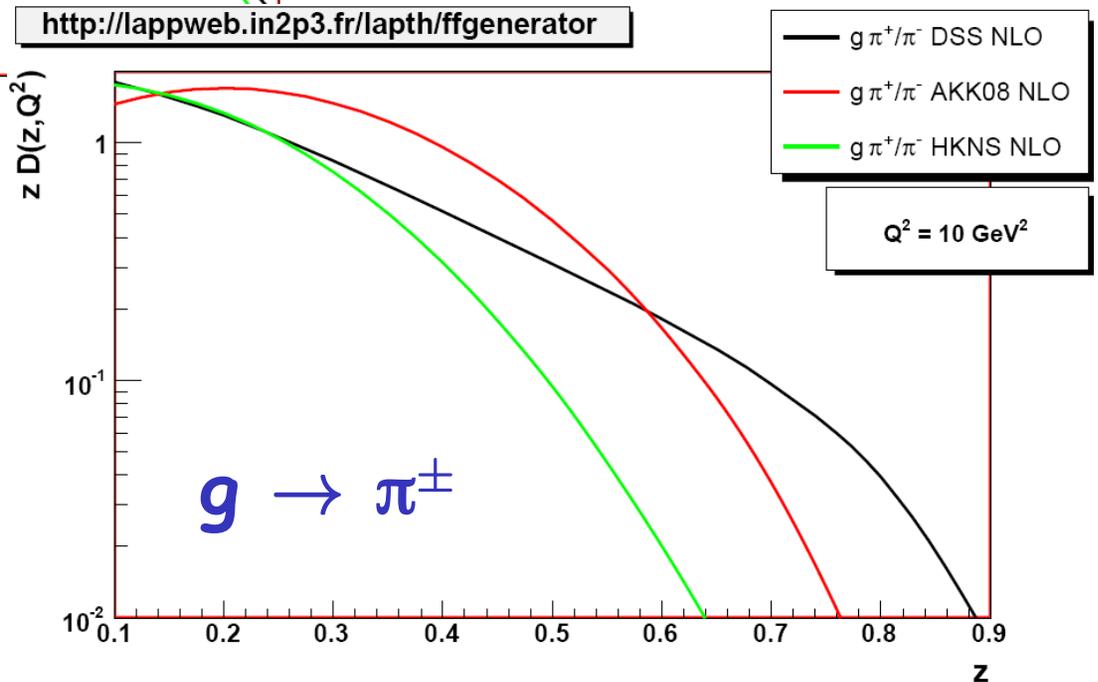
impose isospin sym. for pions

Hessian method for uncertainties

comparison with other pion FFs



making use of nice
online-plotting tool
 for fragmentation fcts
 F. Arleo, J.Ph. Guillet, M. Werlen



**faithful measure of
 uncertainties of FFs ?**

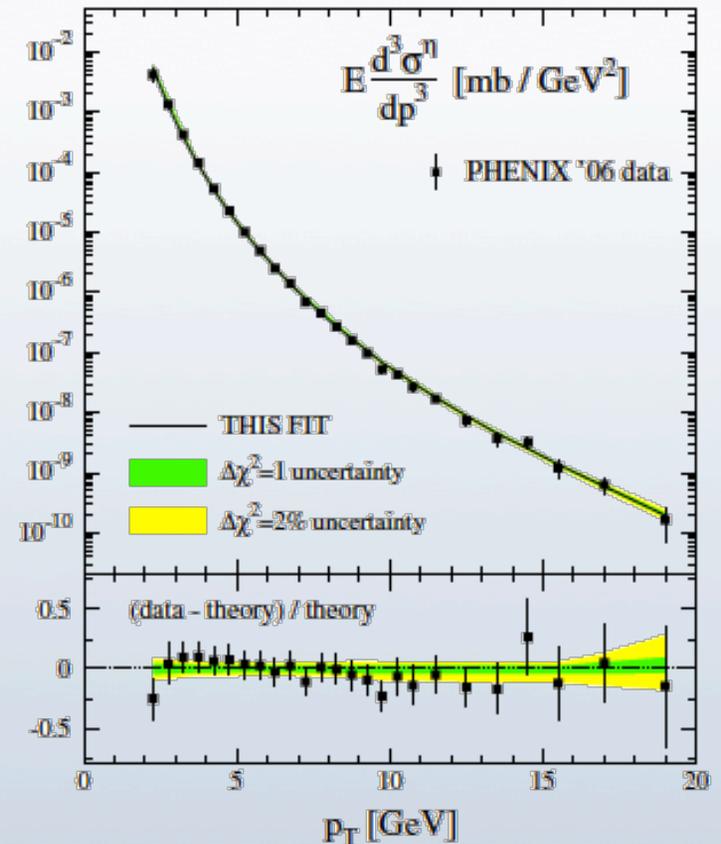
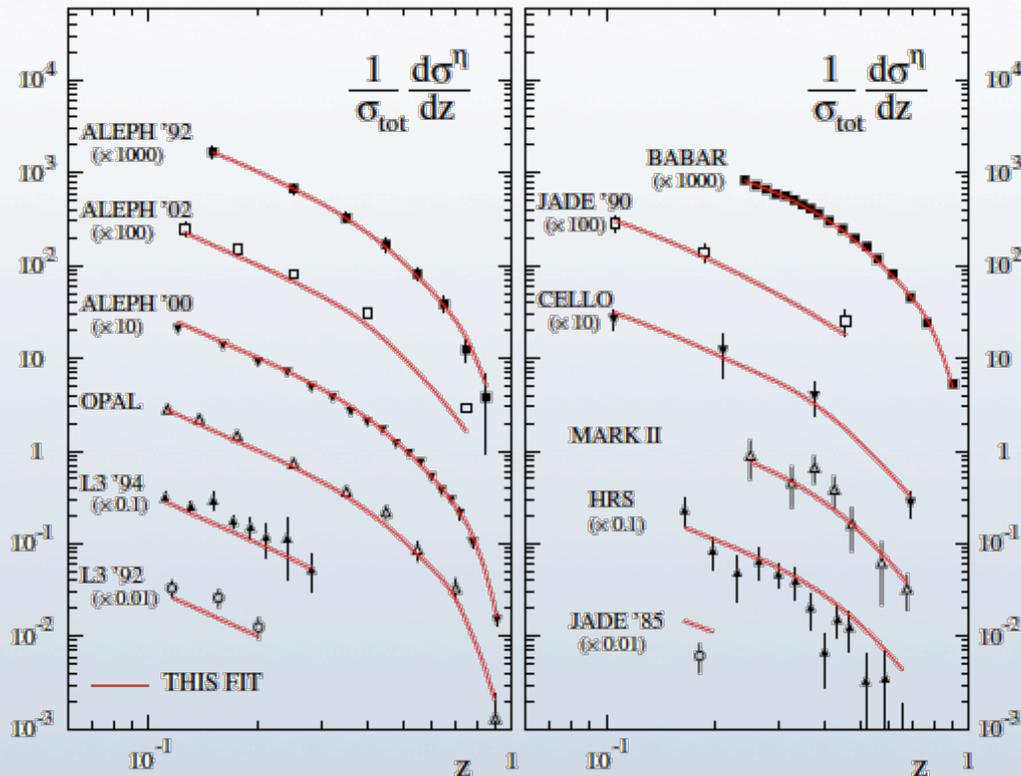
recall: DSS, AKK08, HKNS
 are based on different data sets
 and assumptions

latest addition to suite of FFs: eta

all light quark & antiquarks in wavefunction

$$|\eta\rangle \simeq |u\bar{u} + d\bar{d} - 2s\bar{s}\rangle$$

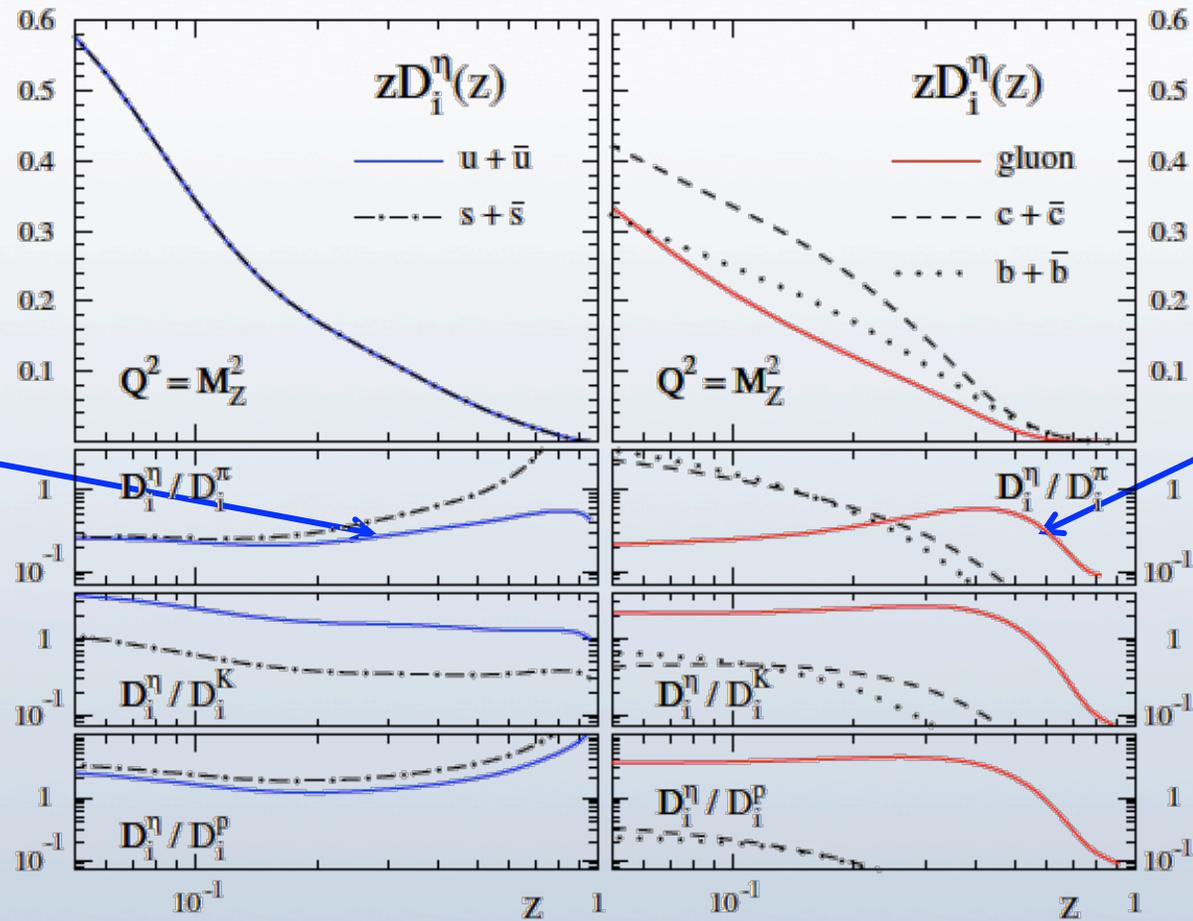
C. Aidala, F. Ellinghaus,
J. Seele, R. Sassot, MS
PR D83 (2011) 034002



complication: no c, b tagged e^+e^- data; no SIDIS data $\rightarrow \eta$ FF less well constrained

eta fragmentation functions

forced to assume (lack of data): $D_u^\eta = D_{\bar{u}}^\eta = \dots = D_s^\eta$



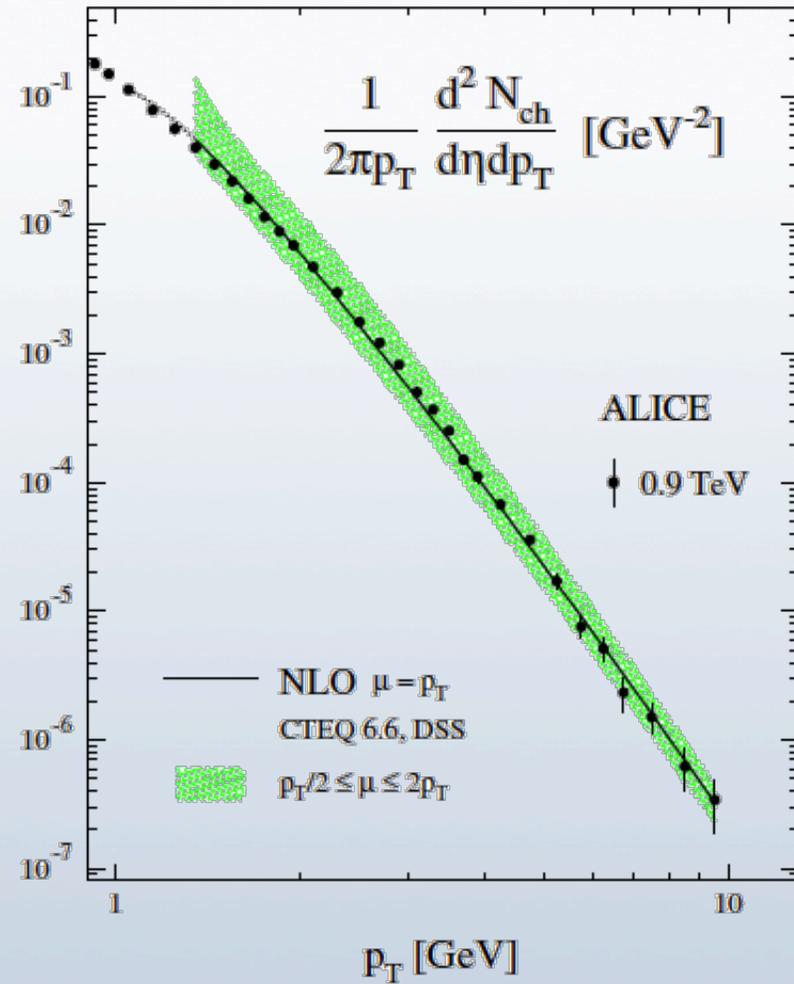
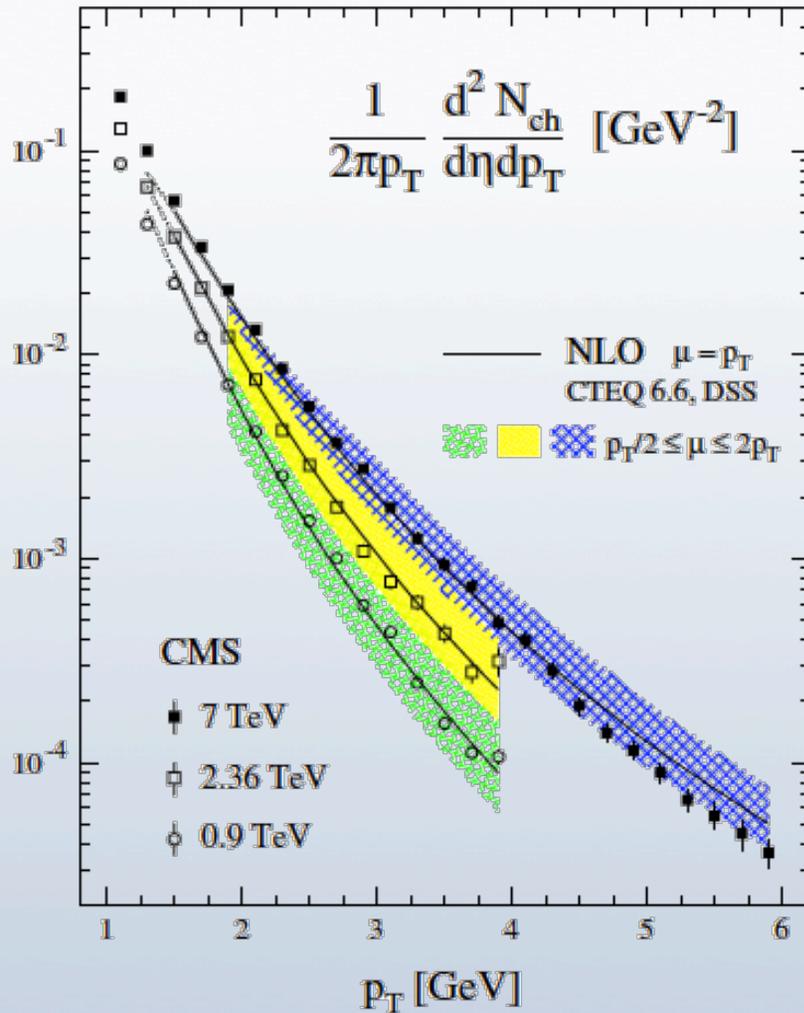
reflects z-dep.
of η/π ratio in
 e^+e^- collisions
(probes mainly D_q)

η/π ratio in pp
roughly $\frac{1}{2}$
(probes mainly
 D_g at large z)

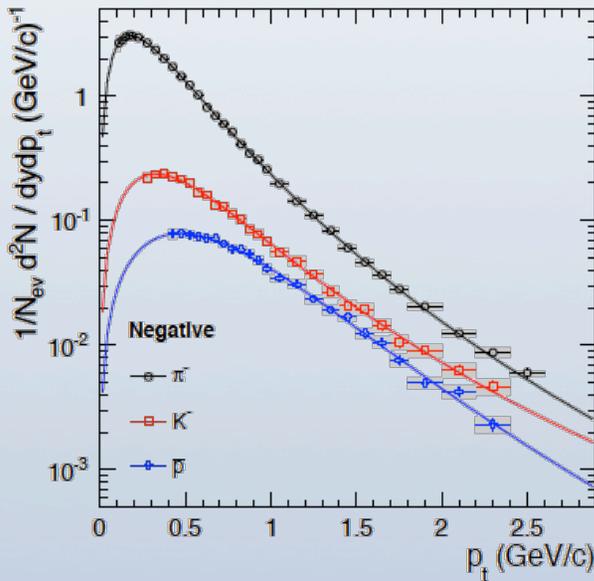
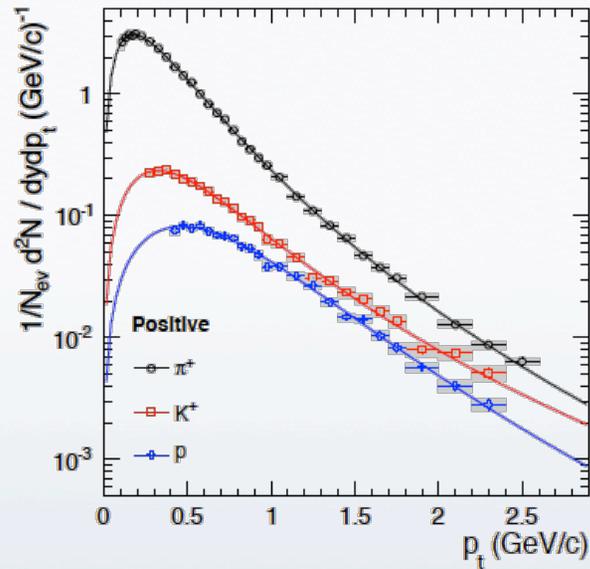
towards DSS 2 : new data sets

- DSS doing well for 1st charged hadron spectra from the LHC

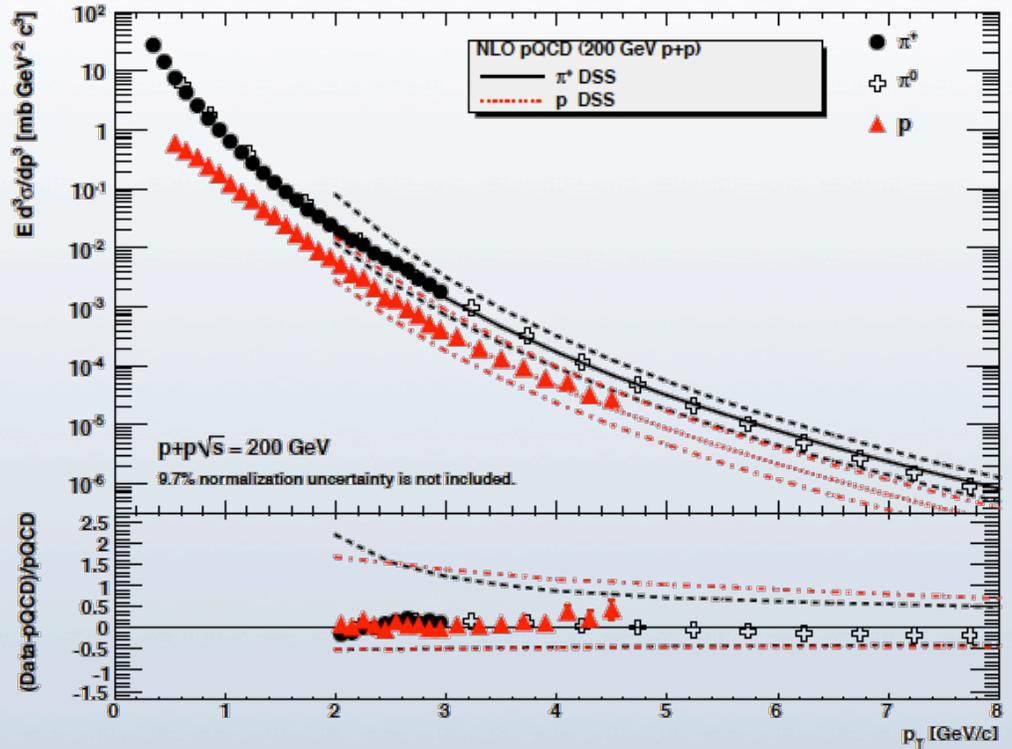
R. Sassot, MS, P. Zurita



new identified hadron spectra



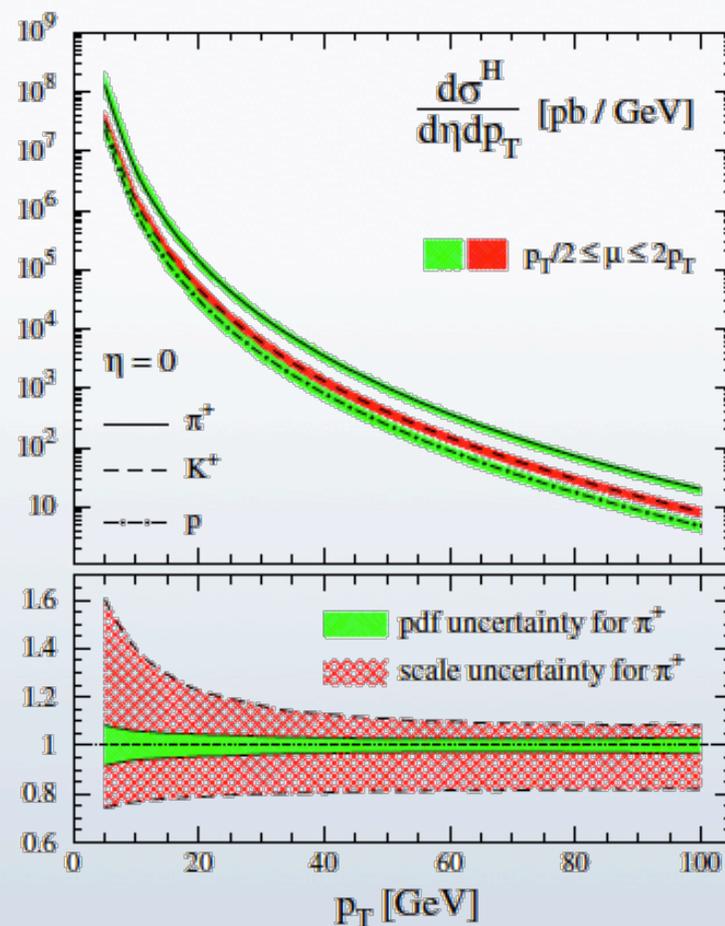
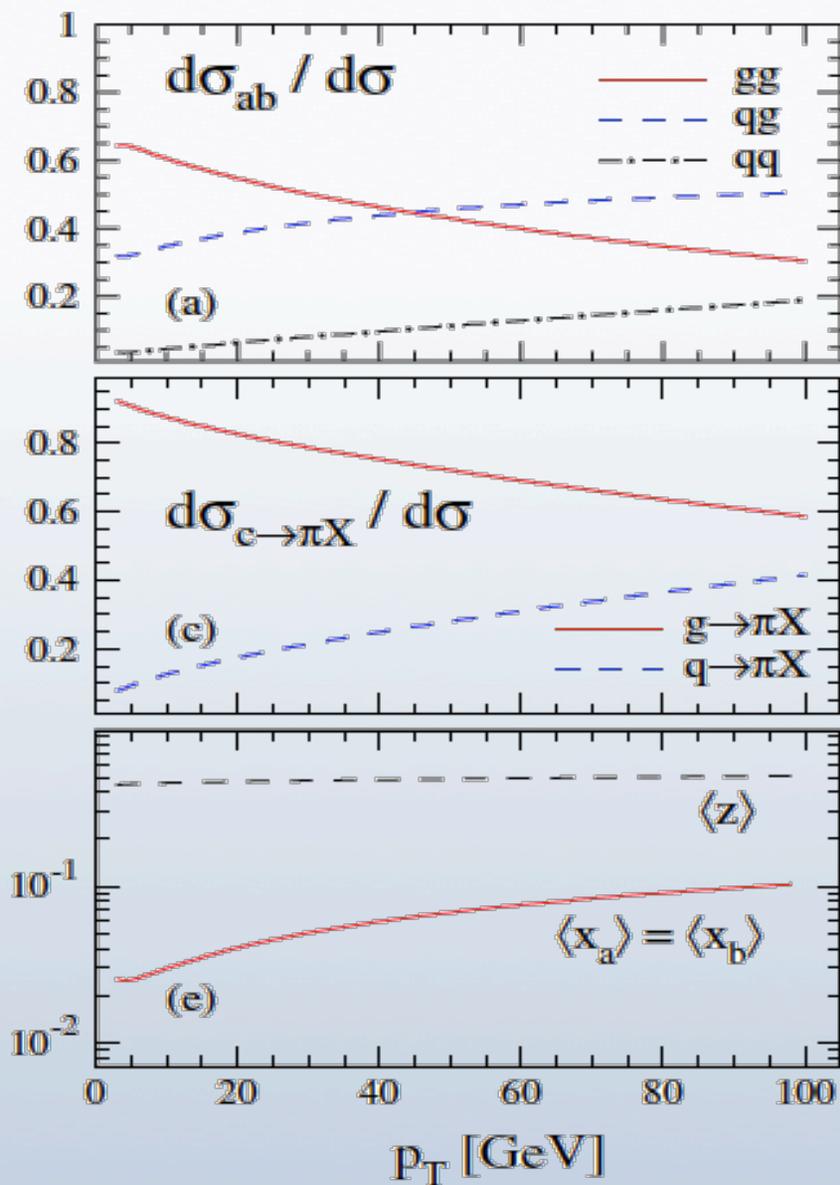
PHENIX: 200 & 62.4 GeV pp, [arXiv:1102.0753](https://arxiv.org/abs/1102.0753)



much more to come from the LHC

FFs from pp data

R. Sassot, MS, P. Zurita

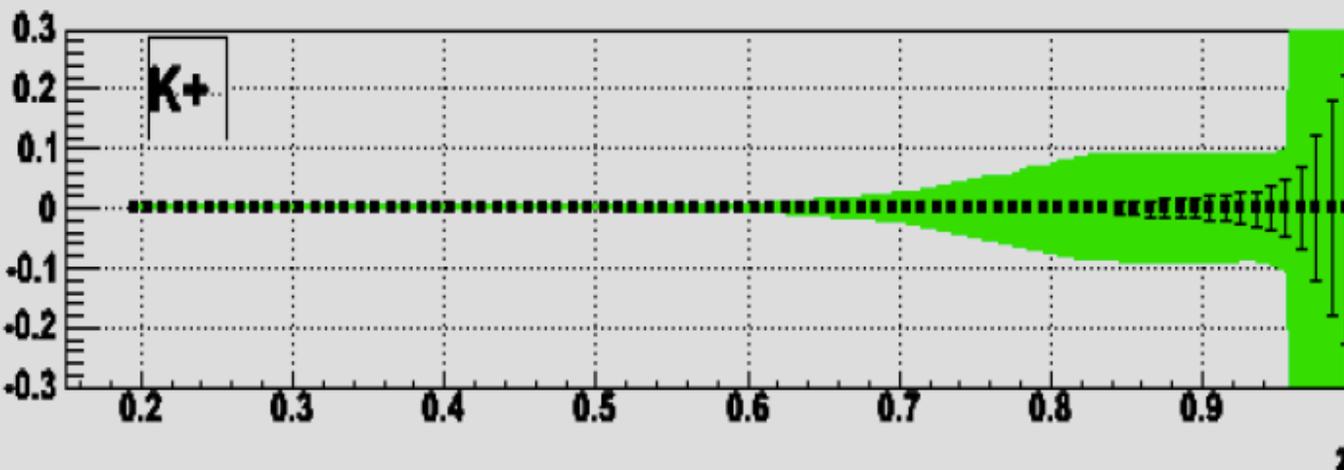
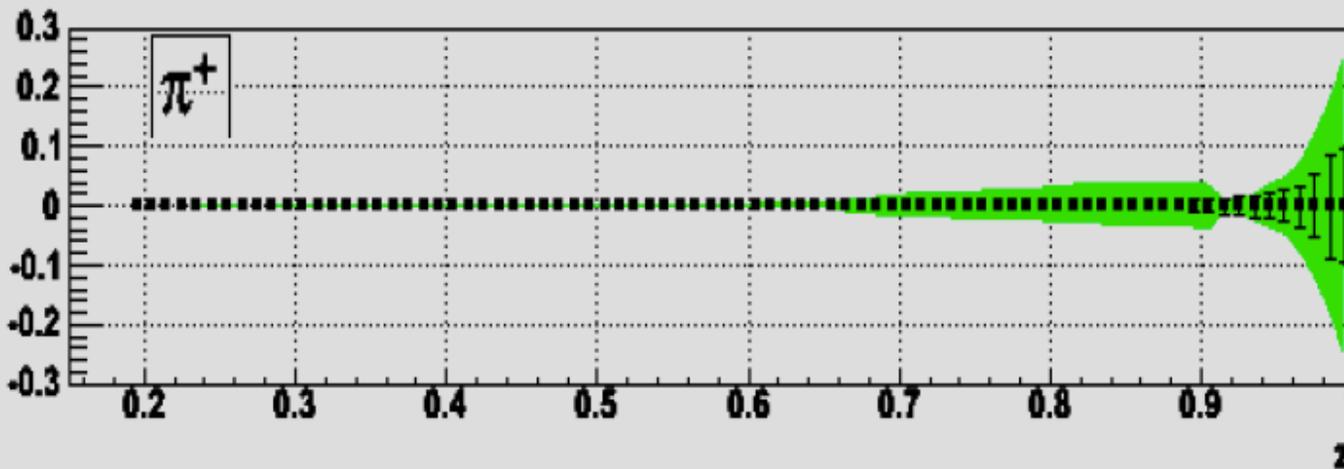


- dominated by gluons up to fairly large p_T
- probes mainly z values around $0.4 \div 0.5$
- scale uncertainties larger than PDF unc.

upcoming precision e^+e^- data from B factories

BELLE: projected relative stat. and sys. uncertainties

M. Leitgab @ DIS 2010



$$e^+e^- \rightarrow HX$$
$$Q^2 \simeq 100 \text{ GeV}$$

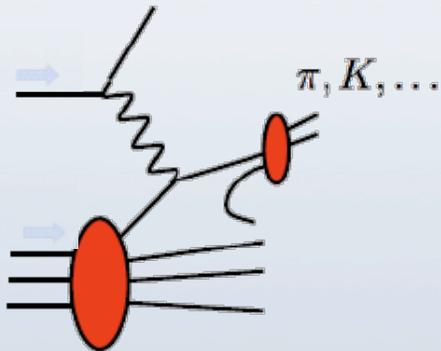
- data will allow for precision studies of scaling violations $\rightarrow D_g$
- unique access to FFs at large z

hadronization in a nuclear medium

- increasing number of data available: clear indication of non-trivial A dependence
 - SIDIS off nuclei (**HERMES**) show strong "hadron attenuation" ($R < 1$)
 - dAu data (**BRAHMS, PHENIX, STAR**) show both $R < 1$ and $R > 1$ ("Cronin effect")

Q: how far can one push factorization & universality

R. Sassot, MS, P. Zurita
PRD81 (2010) 054001



$$\begin{array}{ccc} f_{i/p}(x, Q^2) & \rightarrow & f_{i/A}(x, Q^2) \\ \text{vacuum/nucleon} & & \text{nuclei} \\ D_{i/p}^H(z, Q^2) & \rightarrow & D_{i/A}^H(z, Q^2) \end{array}$$

complication:

- no straightforward probe ($= e^+e^-$) for nFFs - always entangled with nPDFs
use "known" **nDS (EPS)** nPDFs to isolate medium effects in the initial state

medium modified pion FFs

R. Sassot, MS, P. Zurita
PRD81 (2010) 054001

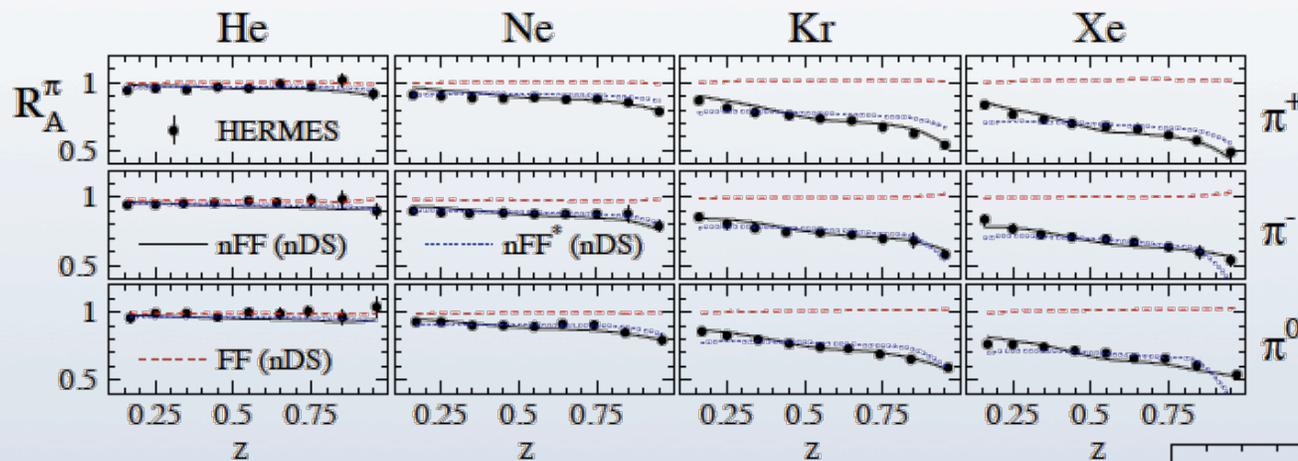
choose a "convolutional approach"

$$D_{i/A}^H(z, Q_0^2) \equiv \int_z^1 dy W_i(y, A) D_{i/p}^H\left(\frac{z}{y}, Q_0^2\right)$$

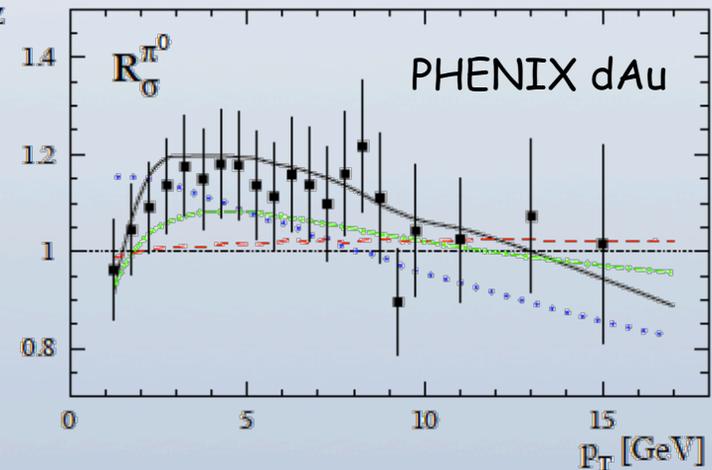
"weight fct" from DSS
to be fitted global analysis

find:

- $D_{q/A}$: suppression incr. with A
- $D_{g/A}$: enhanced around $z \approx 0.5$



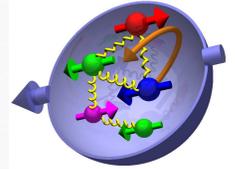
- only nPDFs does not work well (dashed lines)
- medium effect in initial & final-state (solid lines) works very well





LONGITUDINAL SPIN STRUCTURE OF THE NUCLEON

special interest in polarized PDFs



holy grail: proton spin sum - a key measurement at an EIC ?

$A^+=0$ gauge version

Jaffe, Manohar; Ji; ...

$$\frac{1}{2}\hbar = \langle P, \frac{1}{2} | J_{\text{QCD}}^z | P, \frac{1}{2} \rangle = \sum_q \frac{1}{2} S_q^z + S_g^z + \sum_q L_q^z + L_g^z$$

total u+d+s
quark spin

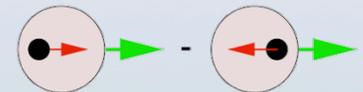
gluon
spin

angular
momentum

“quotable” properties of the nucleon

$$\Delta f(x) \equiv f_+^{N+}(x) - f_-^{N+}(x)$$

- requires good knowledge of $\Delta g(x)$ and $\Delta \Sigma(x)$ for a given Q^2
not to mention orbital angular momentum (OAM)



- low x needed to capture most of the 1st moment integrals, e.g. $S_g = \int_0^1 \Delta g(x) dx$

- however, should not focus too much on one moment; want to know full x -dep. !

- picture emerging from present data still rather fuzzy and inconclusive

DSSV analysis - highlights



1st global QCD analysis of polarized PDFs; consistently performed at NLO



flexible functional form $x\Delta f_j(x, 1 \text{ GeV}) = N_j x^{\alpha_j} (1-x)^{\beta_j} [1 + \kappa_j \sqrt{x} + \gamma_j x]$ possible nodes

assumptions on parameter space avoided as much as possible

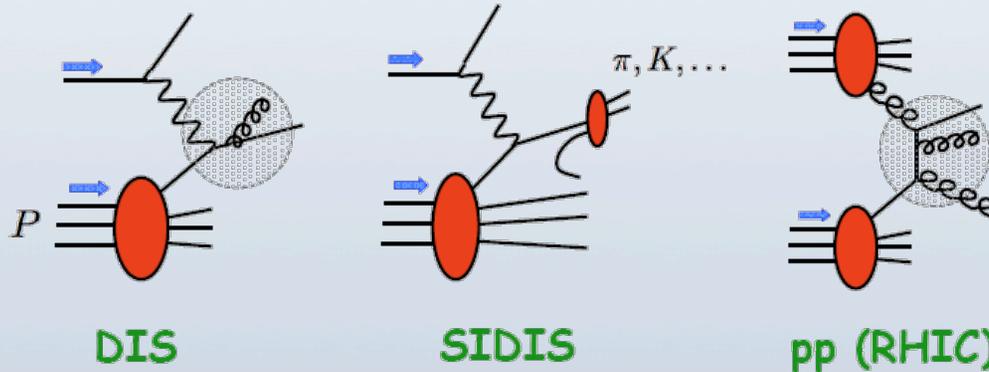
fit respects, however, constraints on 1st moments

$$\begin{aligned} \Delta u_{\text{tot}} - \Delta d_{\text{tot}} &= (F + D)[1 + \epsilon_{\text{SU}(2)}] \\ \Delta u_{\text{tot}} + \Delta d_{\text{tot}} - 2\Delta s_{\text{tot}} &= (3F - D)[1 + \epsilon_{\text{SU}(3)}] \end{aligned}$$

small



excellent description of world data



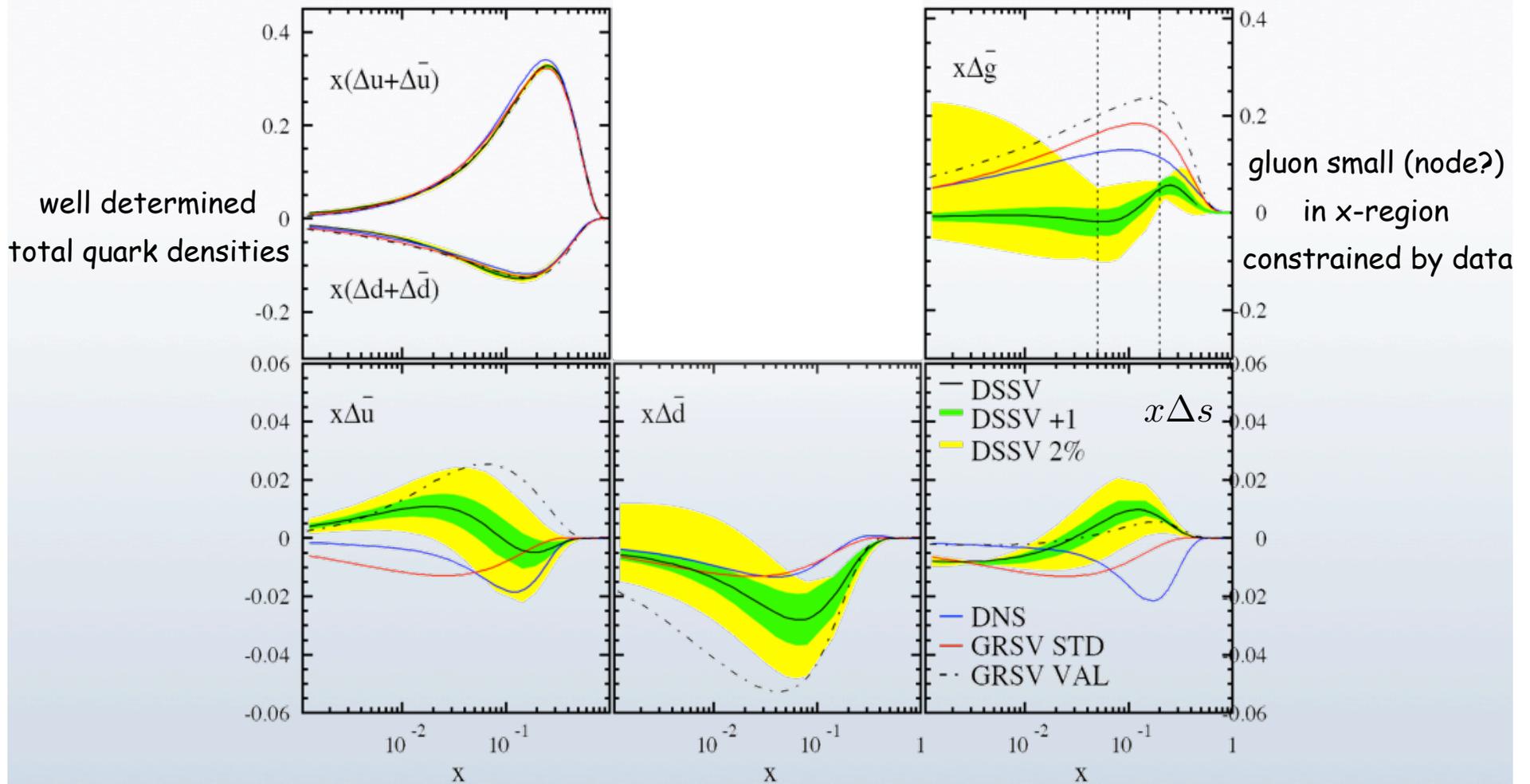
$(\chi^2 / \text{d.o.f.} \simeq 0.88)$



estimates of PDF uncertainties with Lagrange multipliers & Hessian method

DSSV: de Florian, Sassot, MS, Vogelsang; PRL101 (2008) 072001; PRD80 (2009) 034030

DSSV analysis - emerging picture



indications for non-trivial sea quark polarizations $\Delta \bar{u} > 0$
 $\Delta \bar{d} < 0$

surprising strangeness polarization (also found in lattice QCD; sizable SU(3) breaking?)

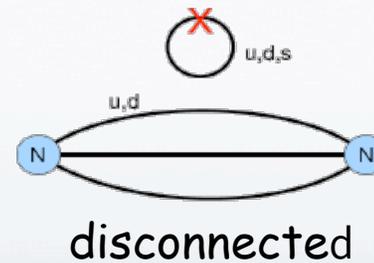
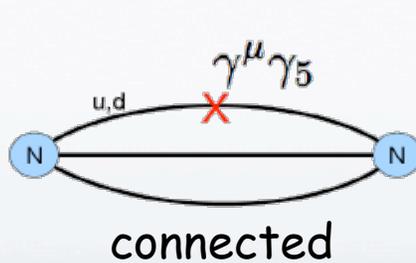
Bali et al., 0811.0807; 0911.2407

flavor separation only from SIDIS; depends on fragmentation functions (global NLO fit by DSS)
 de Florian, Sassot, MS

strangeness conundrum

1st attempts to compute disconnected (sea) contributions on the lattice

Bali, Collins, Schafer, arXiv:0811.0807v2; 0911.2407



find: $\frac{1}{2} \int_0^1 [\Delta s + \Delta \bar{s}](x) dx = -0.01 \pm 0.007$

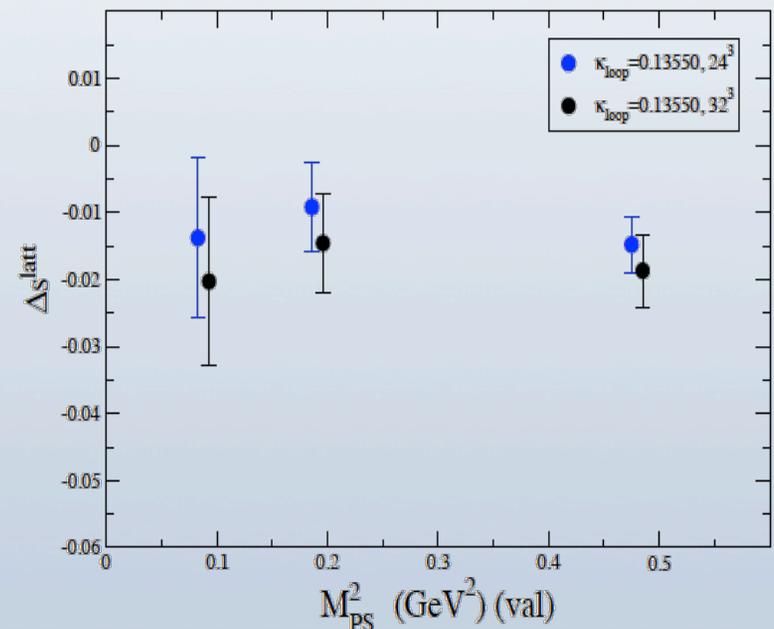
[DSSV w/ SU(3): -0.06 !!]

issues: not renormalized yet, continuum extrapolation, ...

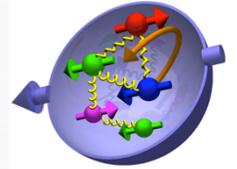
SU(3) strongly broken ?

perhaps $\Delta s = -\Delta \bar{s}$?

assumed SU(3) symmetry certainly debatable
at 20÷30 % level M. Savage @ INT 10-3



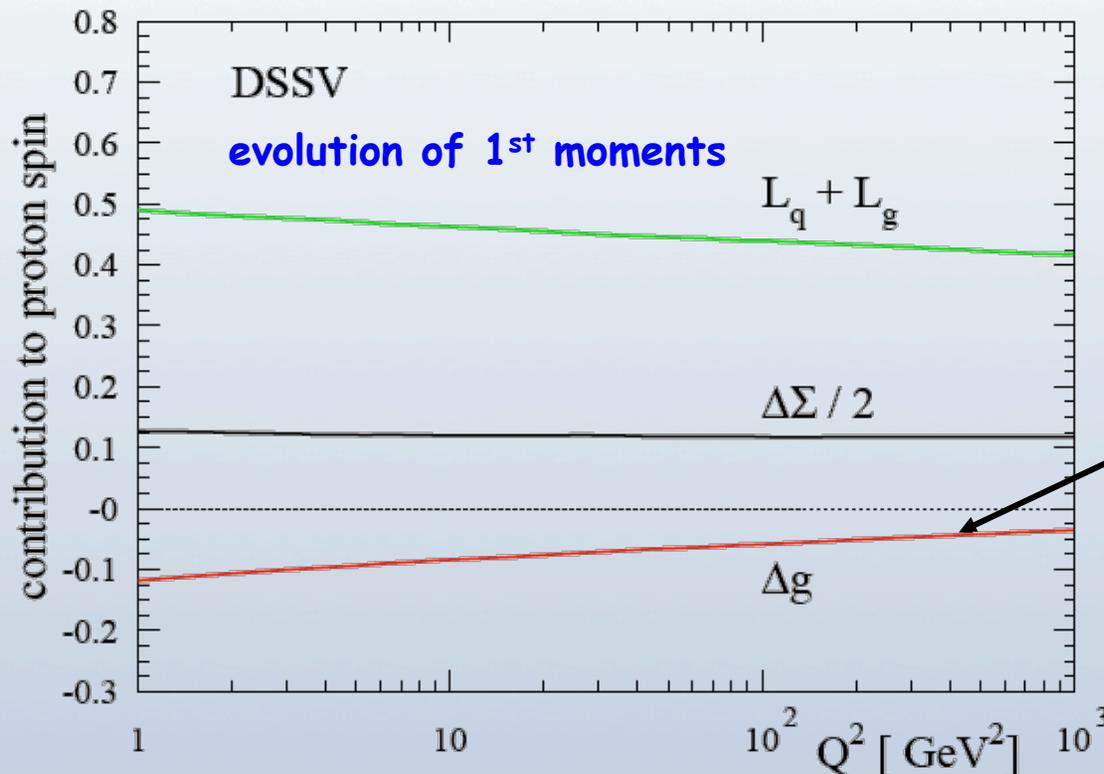
an observation about the spin sum rule



DSSV fit has the property that **proton spin is almost entirely OAM for all Q^2**

recall (at LO)
$$\frac{d}{d \ln(\mu^2)} \begin{pmatrix} \Delta\Sigma \\ \Delta g \end{pmatrix} = \frac{\alpha_s}{2\pi} \begin{pmatrix} 0 & 0 \\ \frac{3}{2}C_F & \frac{1}{2}\beta_0 \end{pmatrix} \begin{pmatrix} \Delta\Sigma \\ \Delta g \end{pmatrix}$$

in general, Δg evolves logarithmically but there is a "static solution" (in LO)



DSSV Δg is close to "static solution"

$$\Delta g \simeq -0.15$$

where $d\Delta g/d \ln \mu = 0$

any deeper reason for that?

meanwhile, new data became available ...



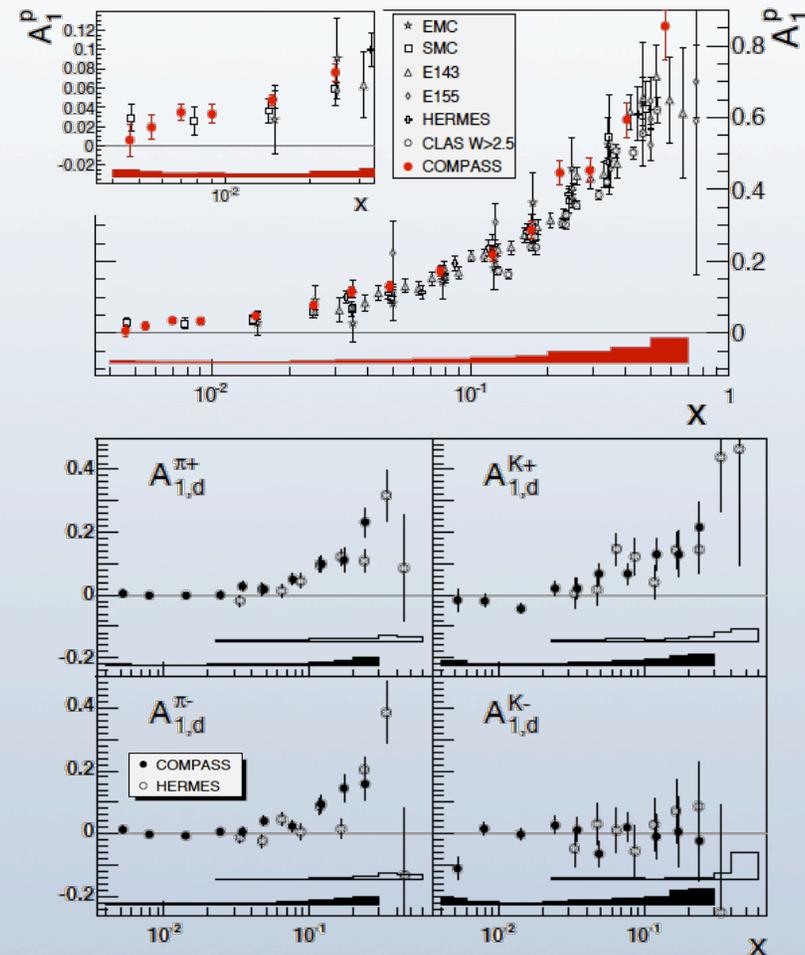
- how well are we doing ?
- refit/new analysis necessary ?
- impact on uncertainties ?

- **DIS:** A_1^p from **COMPASS**
arXiv:1001.4654

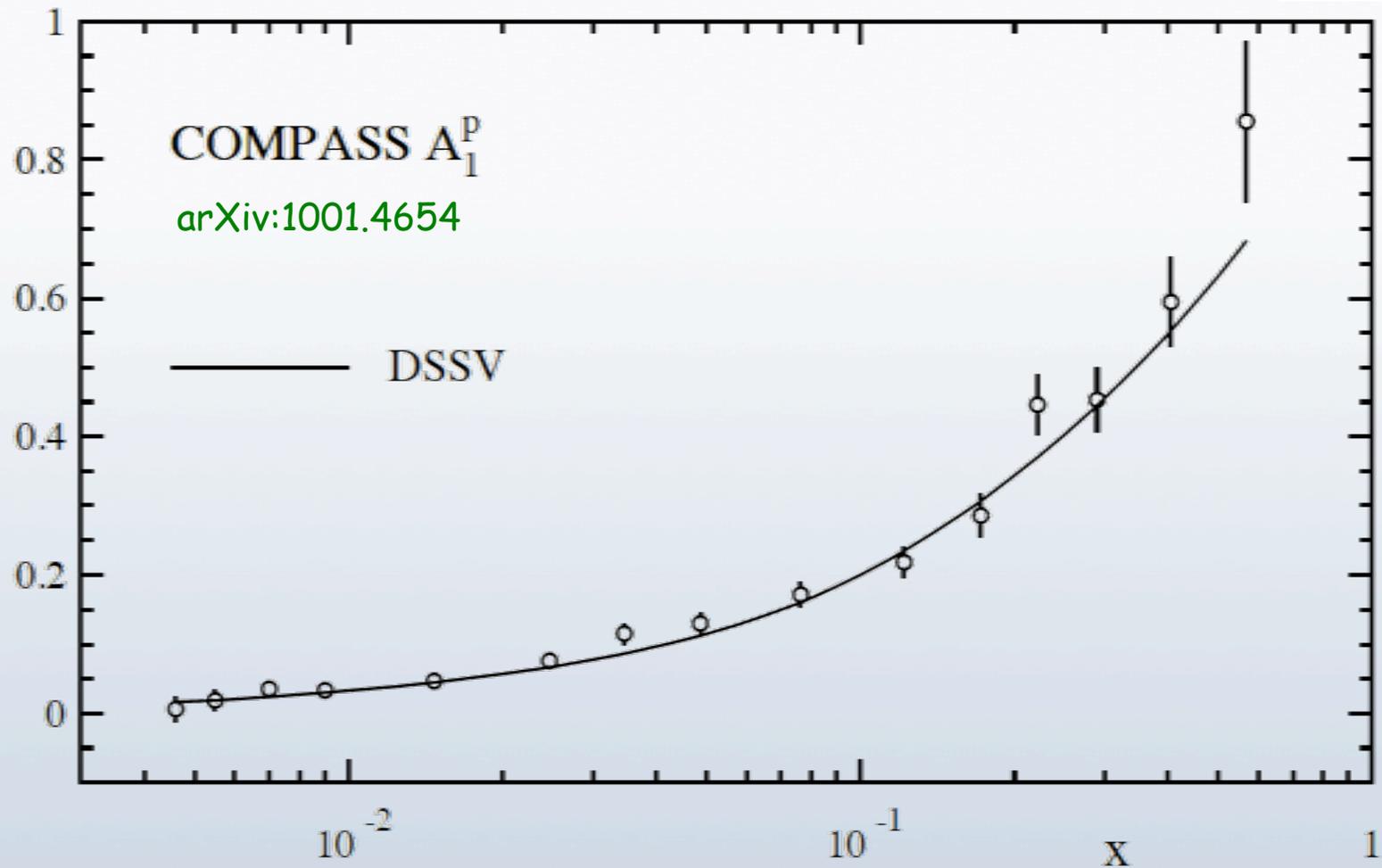
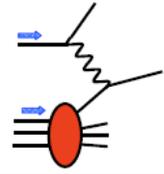
- **SIDIS:** $A_{1,d}^{\pi,K}$ from **COMPASS**
arXiv:0905.2828

- **SIDIS:** $A_{1,p}^{\pi,K}$ from **COMPASS**
arXiv:1007.4061

extended x coverage w.r.t. **HERMES**

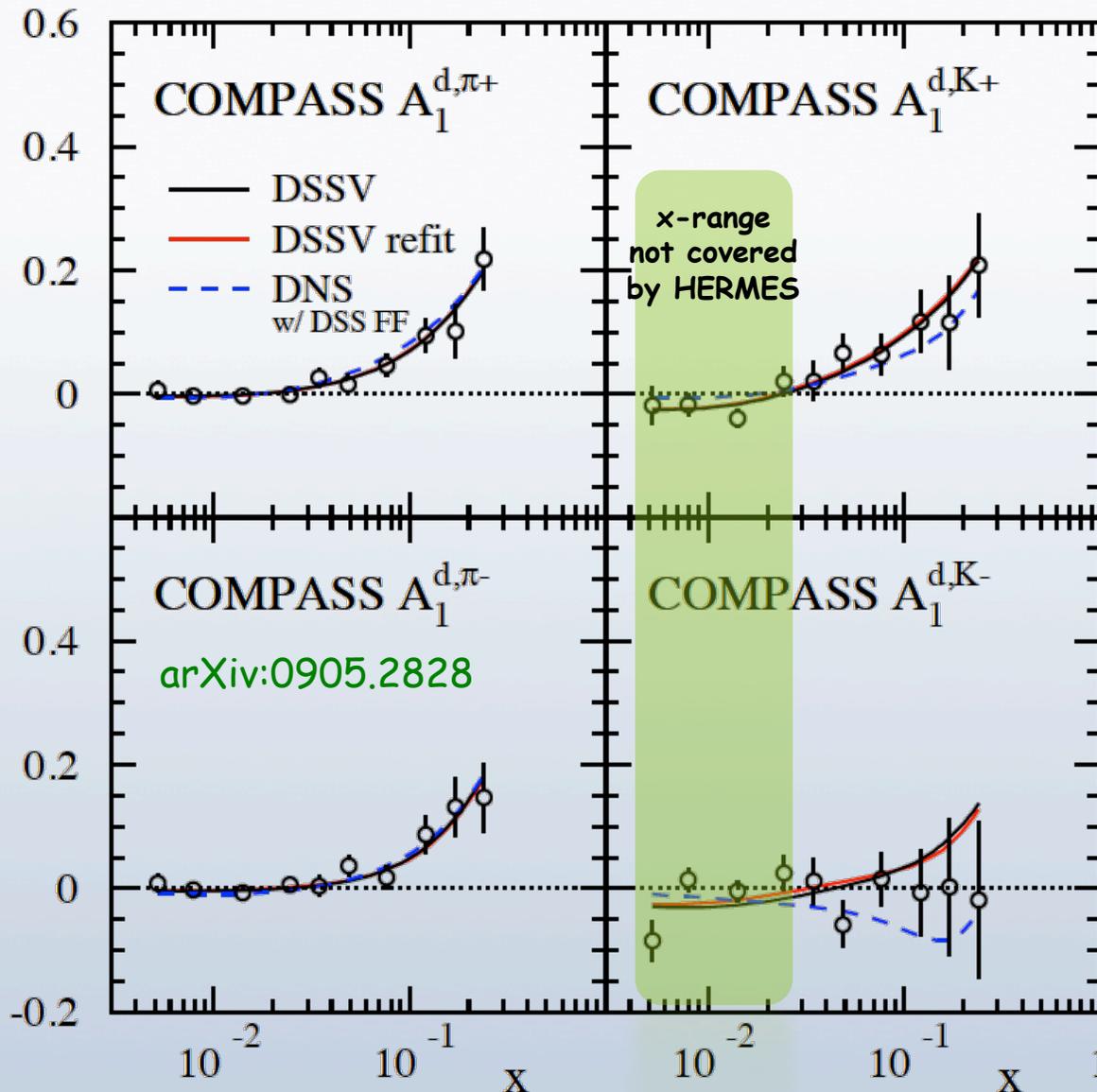
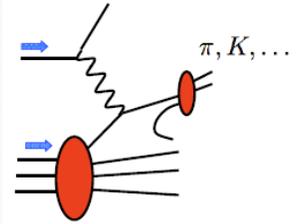


coping with new data: DIS A_1^P



✓ DSSV does a very good job: 15 points, $\chi^2 = 14.2$

coping with new data: SIDIS $A_1^{d,\pi,K}$



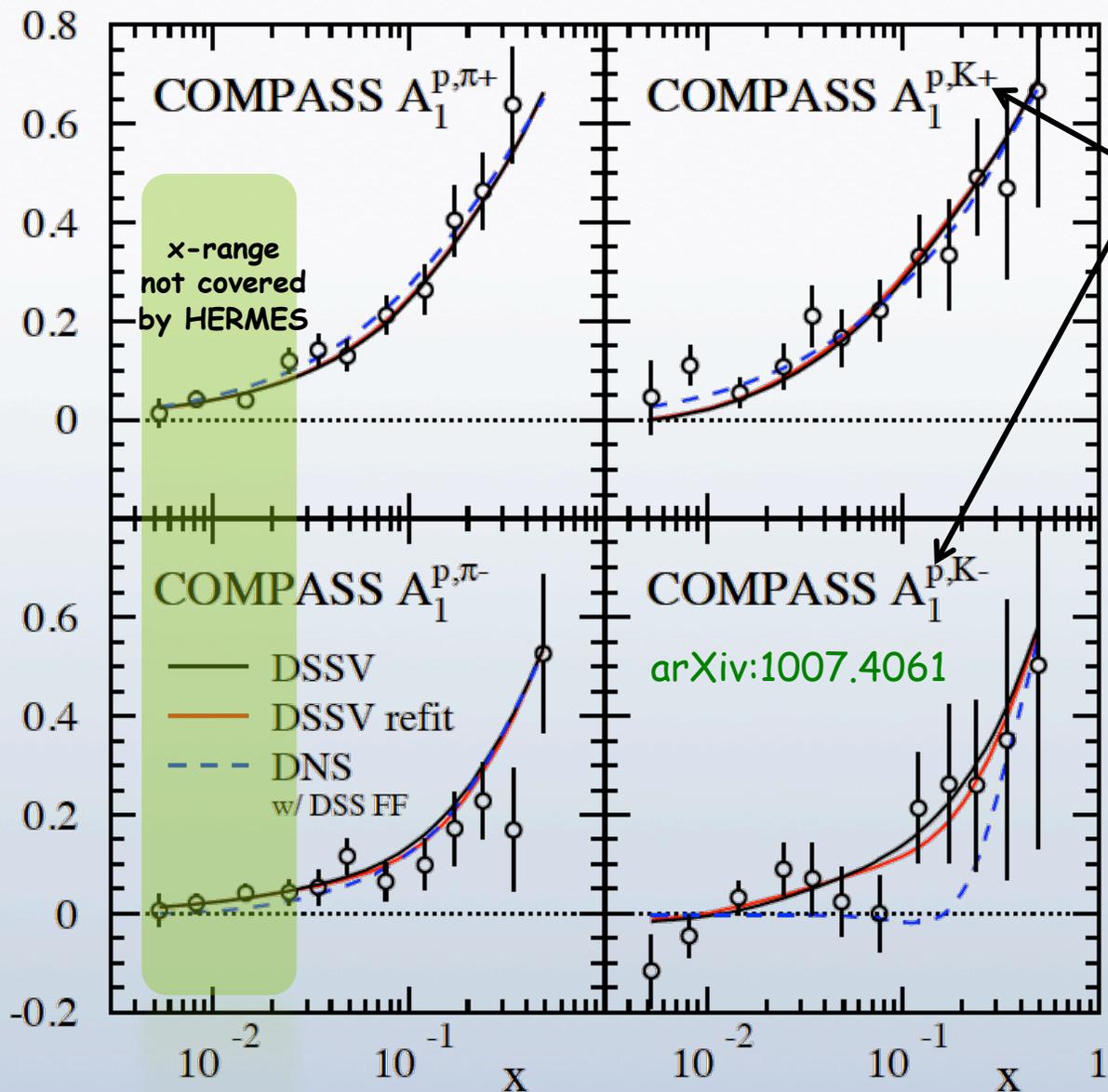
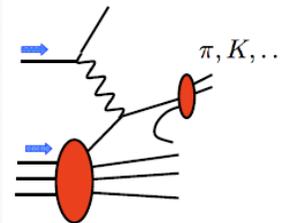
✓ DSSV works well:
no surprises at small x

χ^2 numerology[‡]:

	DSSV 08 data sets	with $A_1^{d,\pi,K}$
DSSV 08	392.5	420.8
DSSV+		418.9

[‡] the branch of knowledge that deals with the occult significance of numbers

coping with new data: SIDIS $A_1^{p,\pi,K}$



1st kaon data on p-target
(not available from HERMES)

χ^2 numerology:

	DSSV 08 data sets	with $A_1^{p\&d,\pi,K}$
DSSV 08	392.5	456.4
DSSV+		453.0

✓ no refit required

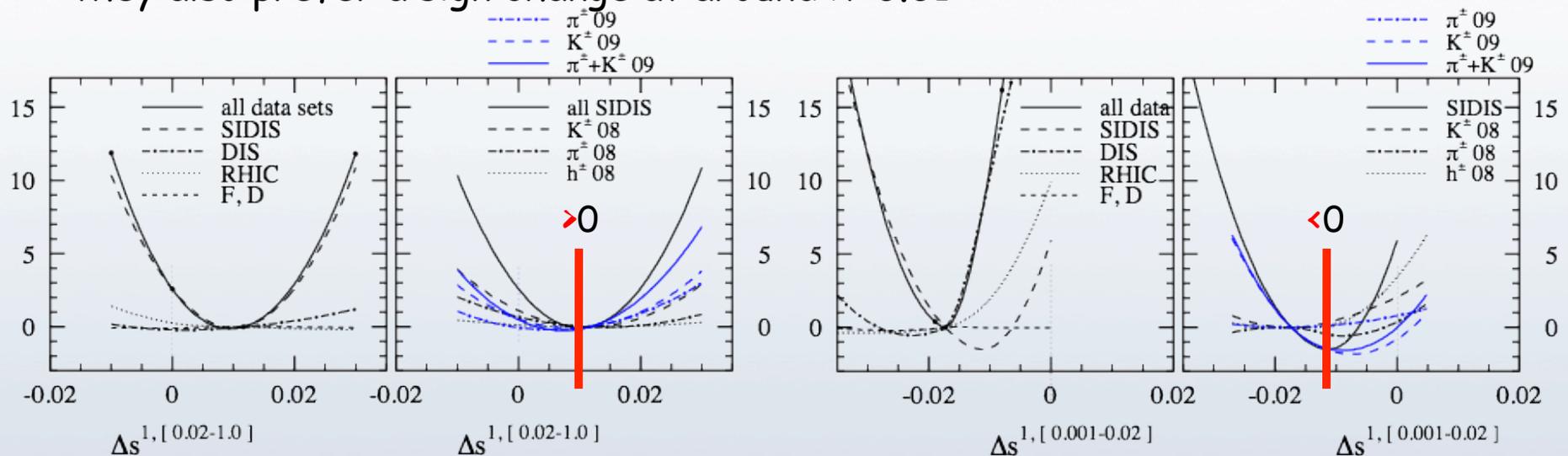
($\Delta\chi^2=1$ does not reflect faithful PDF uncertainties)

- trend for somewhat less polarization of sea quarks; $\Delta\bar{u} - \Delta\bar{d} \neq 0$ less significant

Δs revisited: impact of COMPASS data

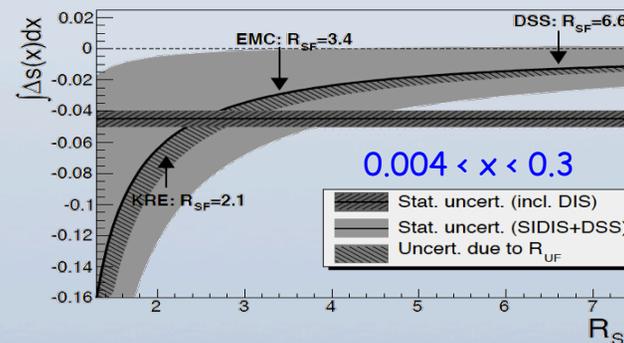
current value for $\Delta\Sigma$ strongly depends on assumptions on low- x behavior of Δs

- new COMPASS data support small/positive $\Delta s(x)$ at $x > 0.01$
- they also prefer a sign change at around $x=0.01$



- but large negative 1st moment entirely driven by assumptions on SU(3)
- caveat: dependence on FFs

$$R_{SF} \equiv \frac{\int D_{\bar{s}}^{K^+}(z) dz}{\int D_u^{K^+}(z) dz}$$



COMPASS

comparison with latest LSS'10 analysis

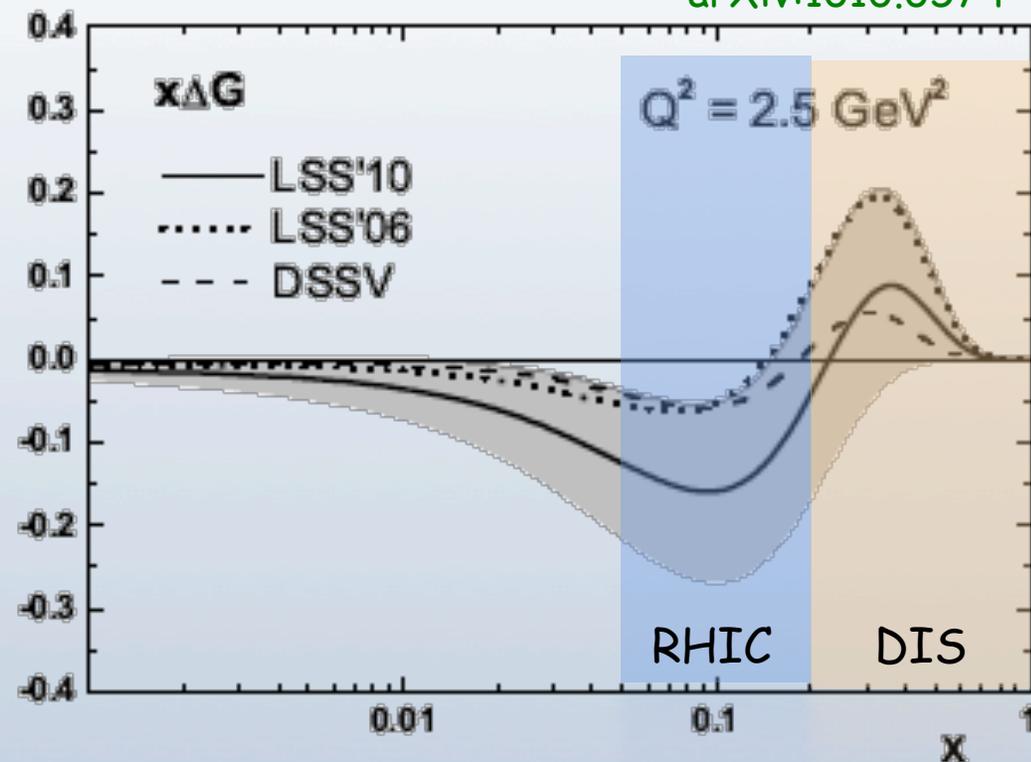
Leader, Sidorov, Stamenov

- fit based on latest DIS/SIDIS data only
- resulting PDFs largely a carbon-copy of DSSV
- **striking**: also gluon very similar (node!) but *w/o* using RHIC pp data

why?

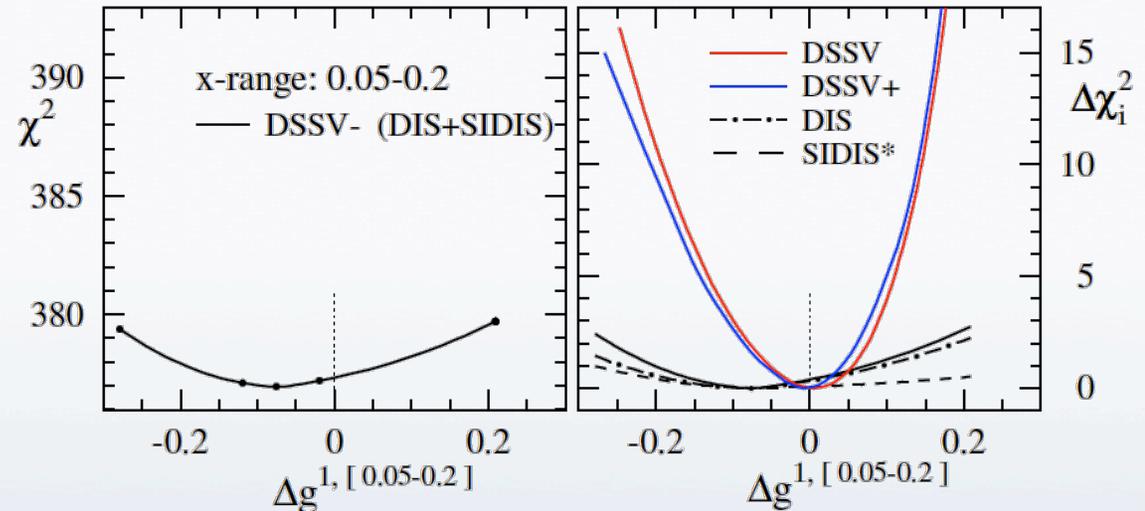
arXiv:1010.0574

look into χ^2 profiles with LM

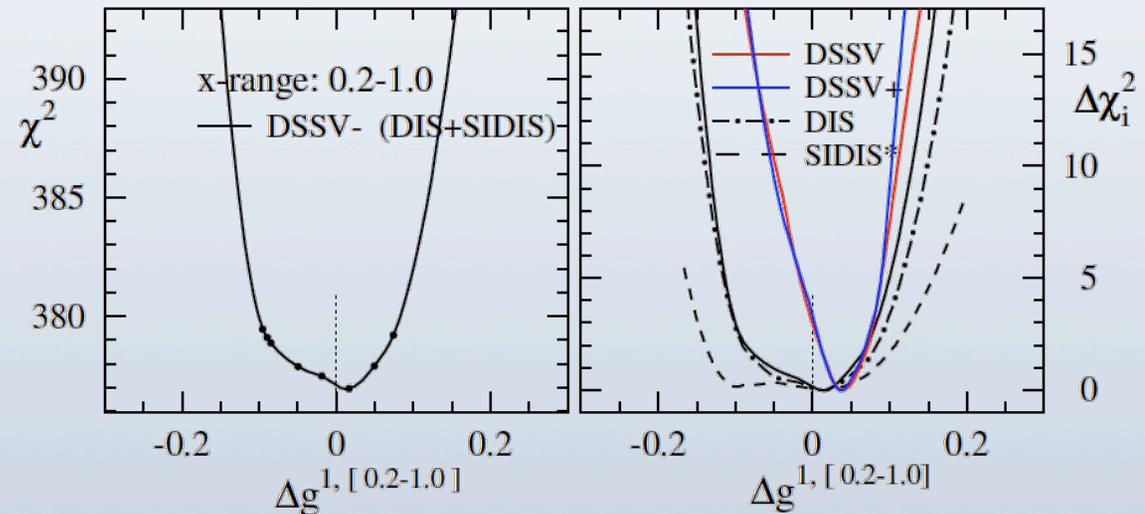


Δg and RHIC data

truncated moment
("RHIC pp region")



truncated moment
("high x")



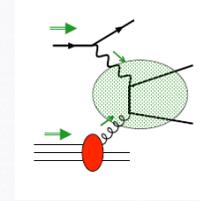
bottom line

- **RHIC pp data clearly needed**
- new (SI)DIS data do not change much for Δg
- trend for positive Δg at large x (as before)

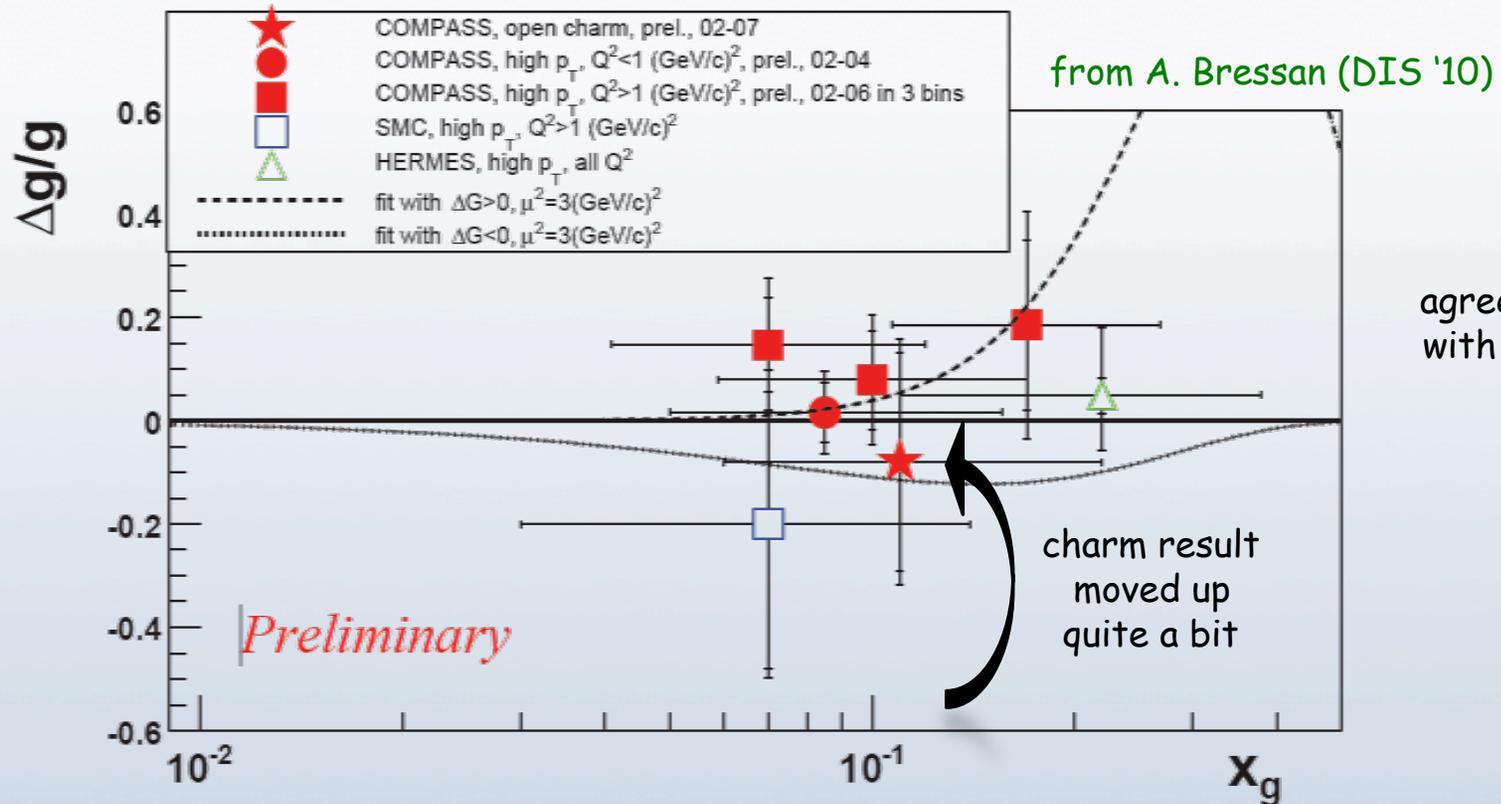
Δg from fixed target experiments

idea: study processes sensitive to **photon-gluon-fusion**

data available for one/two hadron production, charm

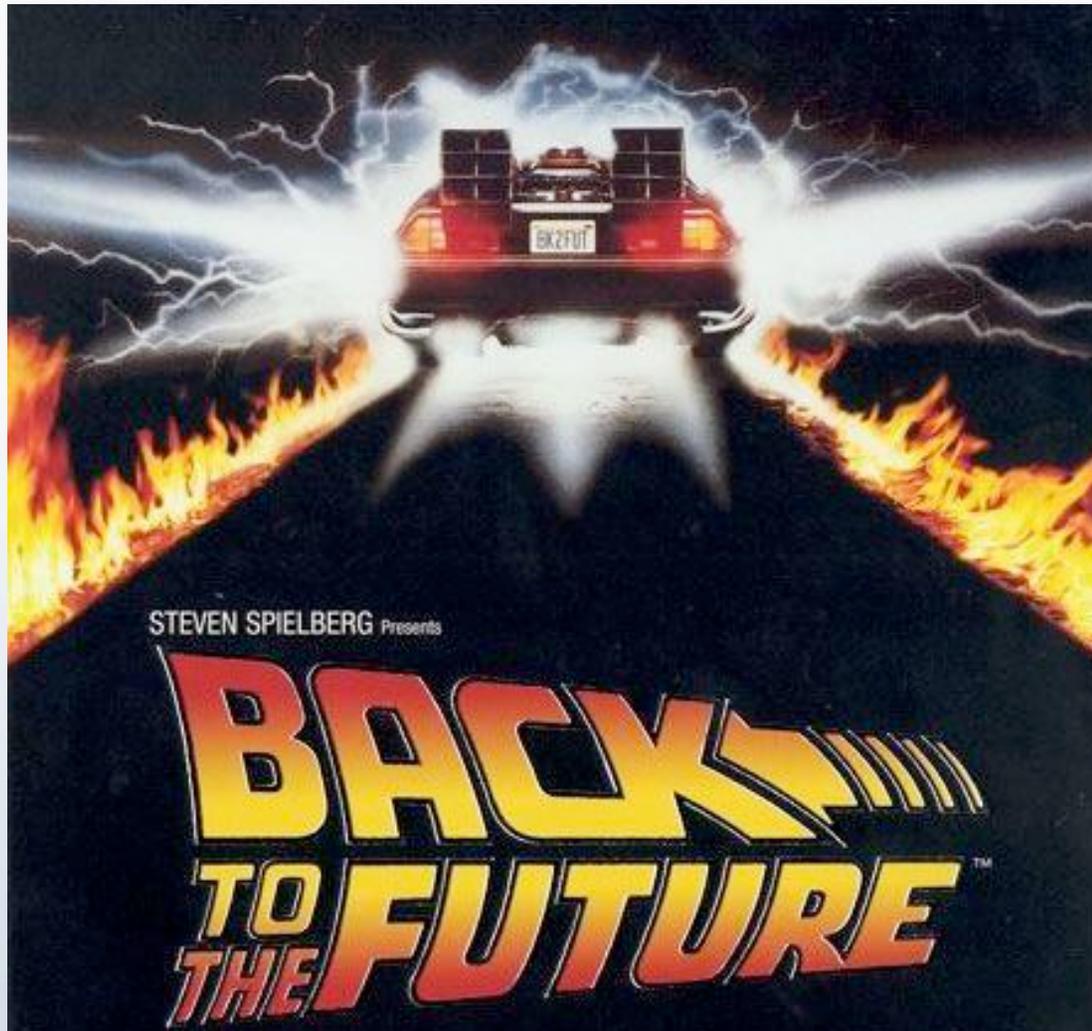


COMPASS,
HERMES,
SMC, E155



NLO results just emerging: [but nothing available for $Q^2 \neq 0$]

Jäger, MS, Vogelsang; Bojak, MS; Riedl, Schäfer, MS; Hendlmeier, Schäfer, MS

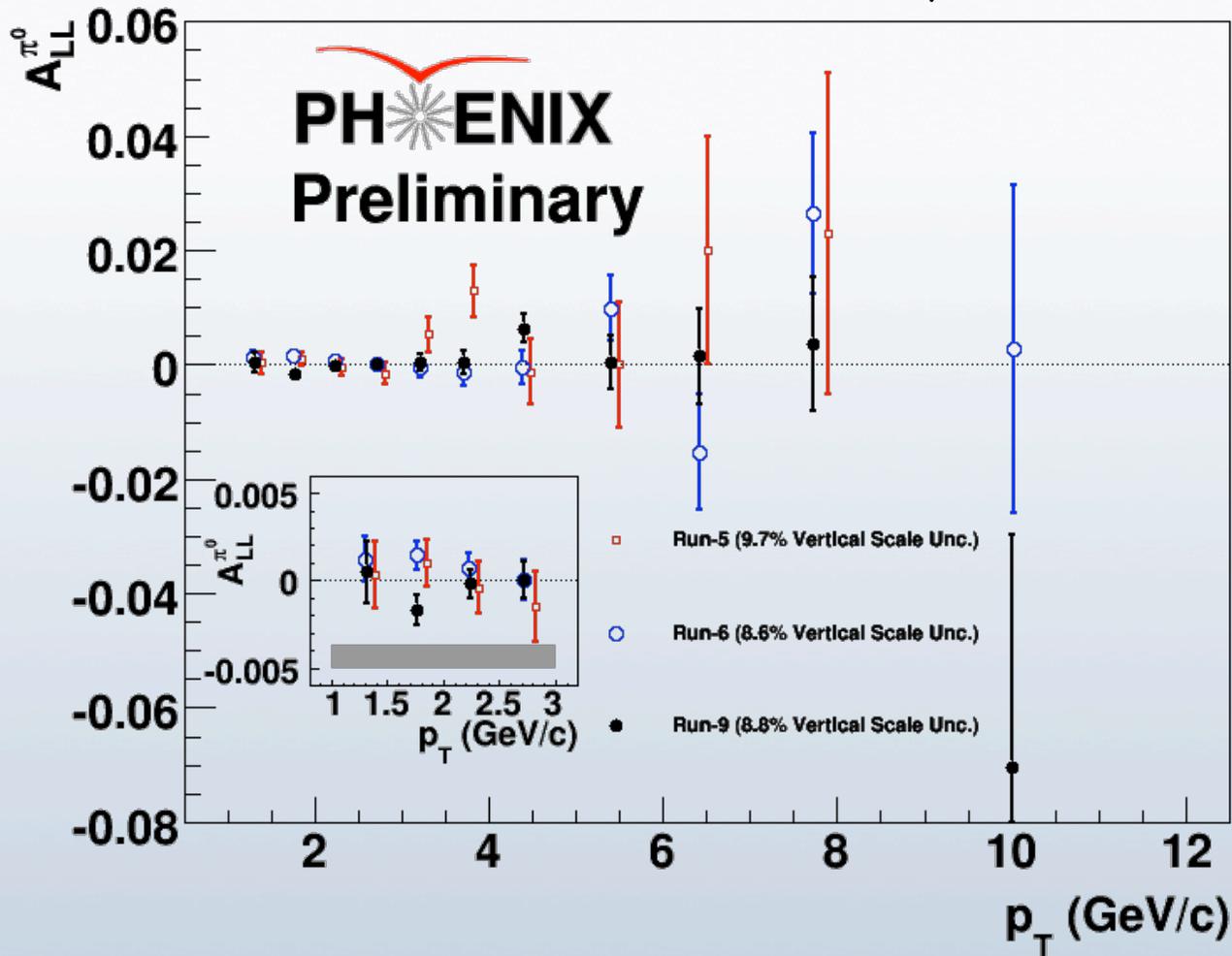


FUTURE AVENUES

RHIC & BEYOND

RHIC: improved single-inclusive observables

as presented at DIS'10



- A_{LL} for π^0 from "run 9" even closer to zero than before

Δg from jet-jet correlations

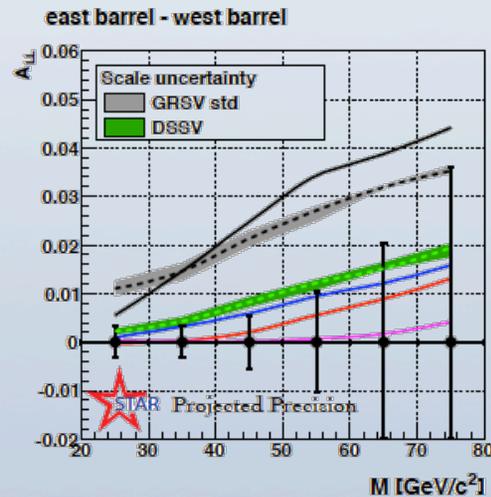
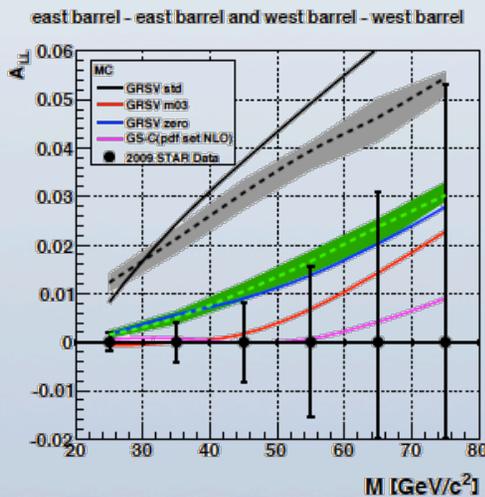
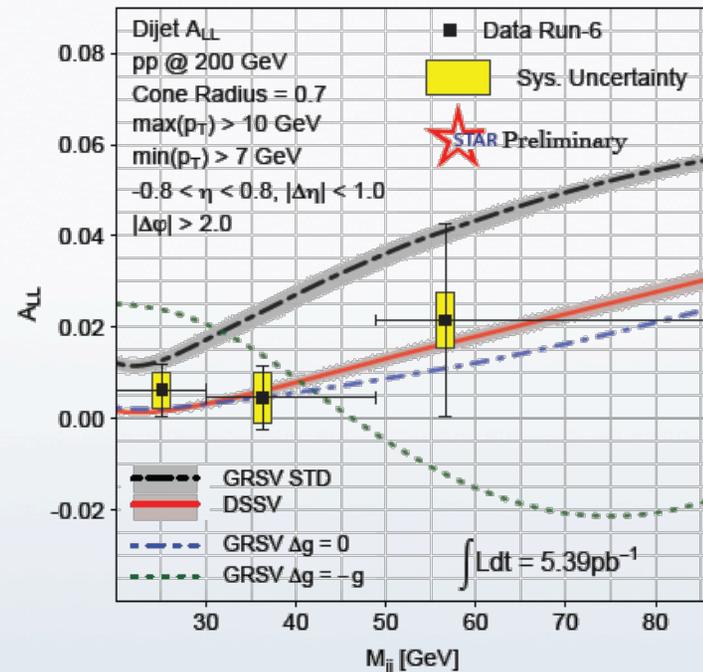
as presented at DNP'10

- particle correlations allow for a more precise mapping of x dependence

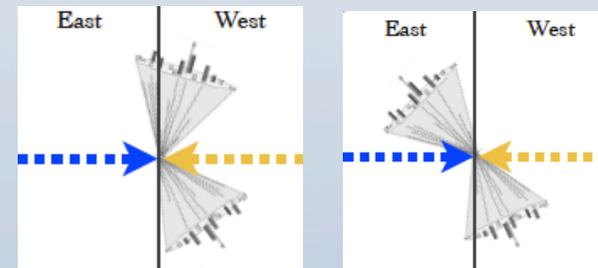
$$x_{1,2} = \frac{p_T}{\sqrt{S}} (e^{\pm\eta_3} + e^{\pm\eta_4})$$

$$M^2/S = x_1 x_2$$

- NLO corrections available for dijets
de Florian, Frixione, Signer, Vogelsang
- Mellin technique in place to include upcoming data in DSSV analysis



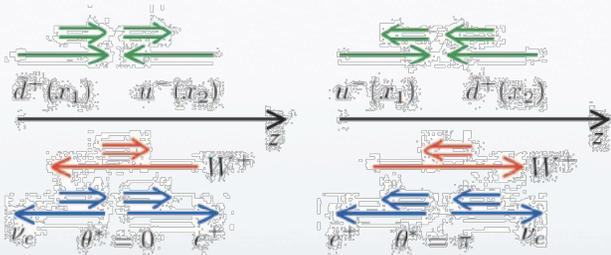
- projections for run 9



u, d quarks from W boson production

key measurement at RHIC

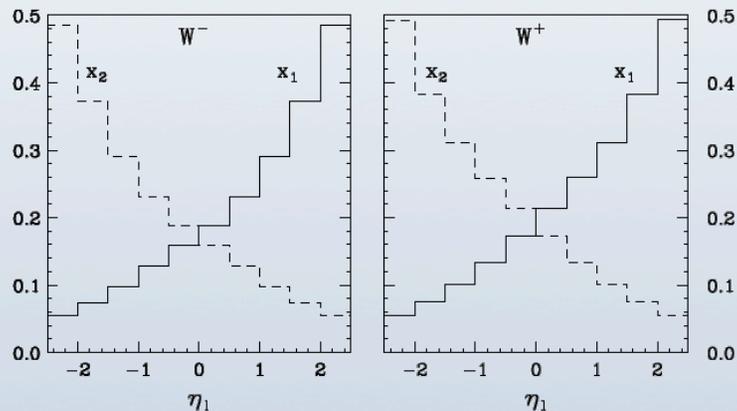
- based on parity violation: W's couple only to one parton helicity



study
single spin
asymmetries

$$A_L^{W^-} \approx - \frac{\Delta d(x_1)\bar{u}(x_2) - \Delta\bar{u}(x_1)d(x_2)}{d(x_1)\bar{u}(x_2) + \bar{u}(x_1)d(x_2)}$$

- RHIC: can detect only decay leptons; lepton rapidity most suited observable

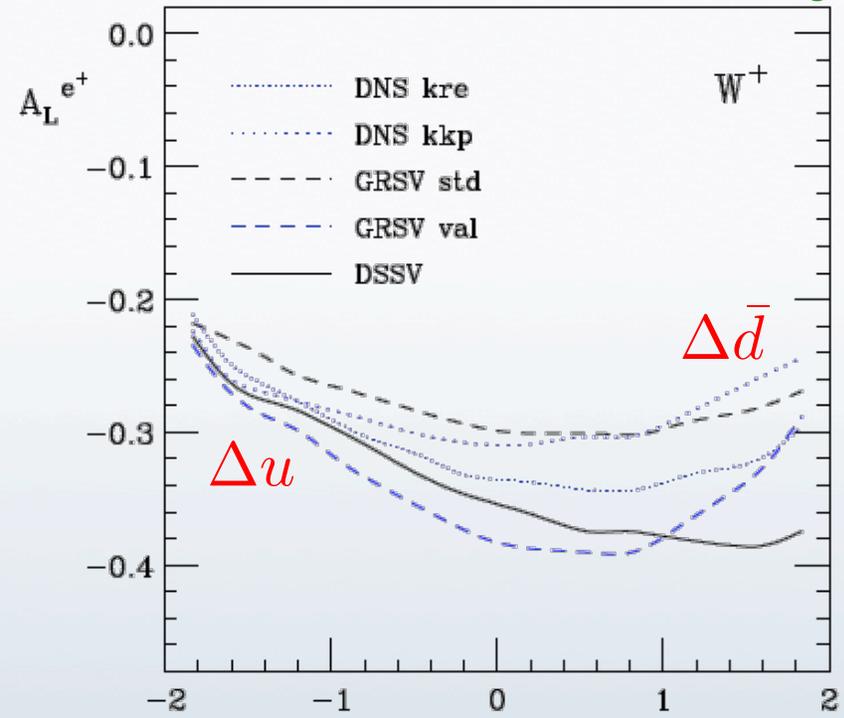
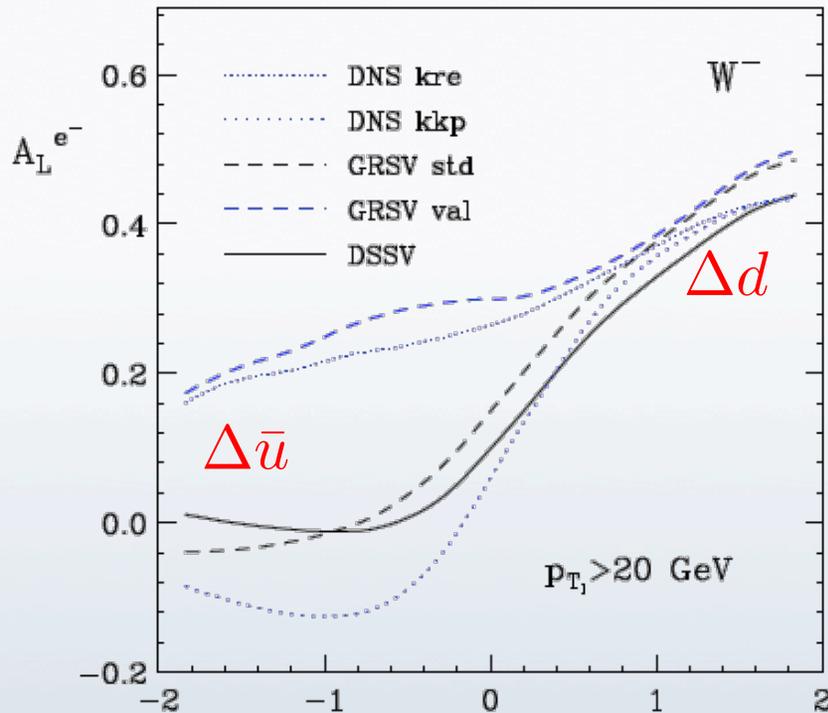


- strong correlation with $x_{1,2}$
- allows for flavor separation for $x > 0.07$
- new versatile NLO MC code "CHE" available
de Florian, Vogelsang, arXiv:1003.4533

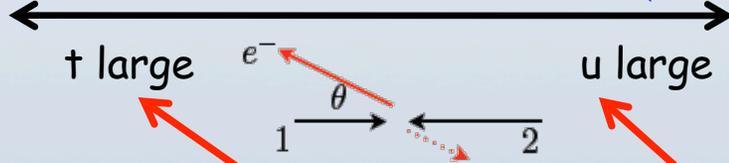
- 500 GeV program at RHIC started in 2009 - 1st results ("proof of principle")

expectations for A_L^e

de Florian, Vogelsang



$$\hat{t}^2 \simeq (1 + \cos \theta)^2 \qquad \eta_1 \qquad \hat{u}^2 \simeq (1 - \cos \theta)^2$$



$$\Delta \bar{u}(x_1) d(x_2) (\hat{t}^2) + \Delta d(x_1) \bar{u}(x_2) (-\hat{u}^2)$$

strong sensitivity to $\Delta \bar{u}$



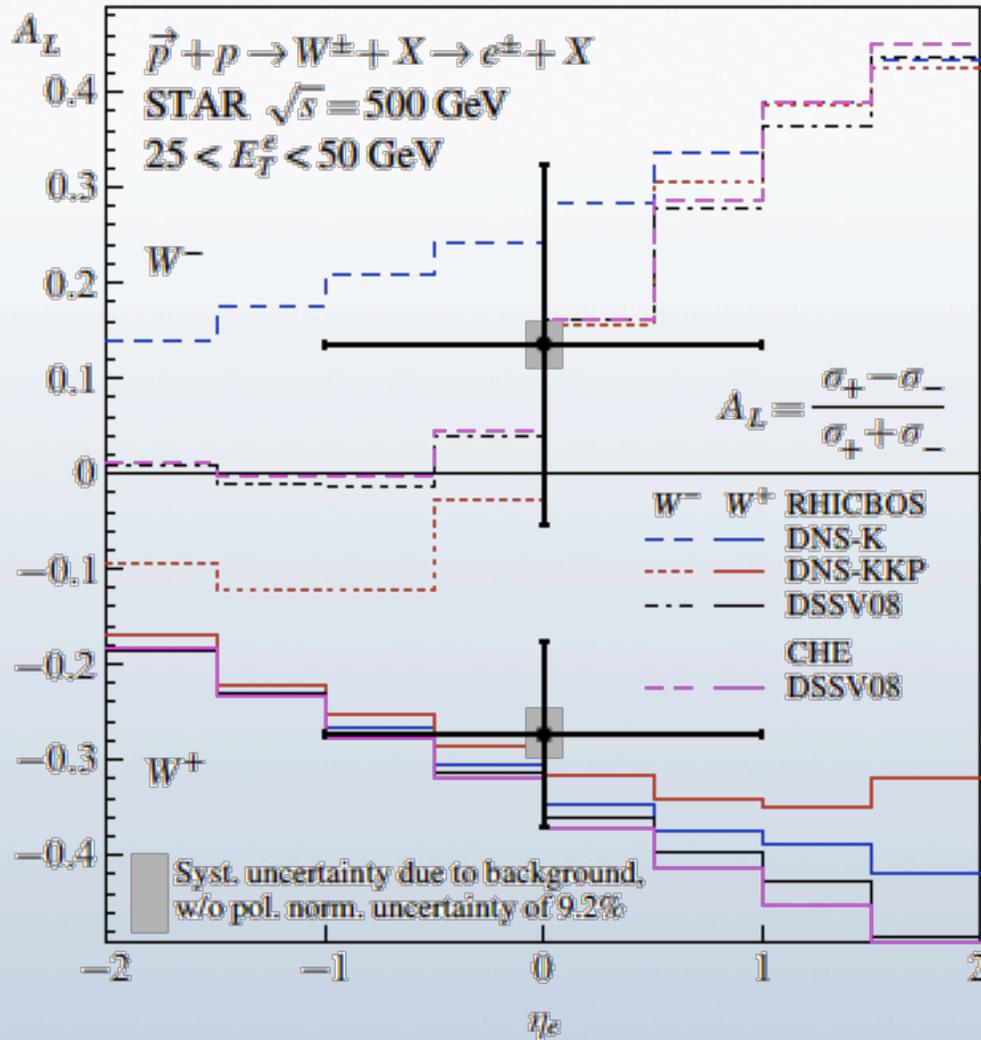
$$\Delta \bar{d}(x_1) u(x_2) (\hat{u}^2) + \Delta u(x_1) \bar{d}(x_2) (-\hat{t}^2)$$

limited sensitivity to $\Delta \bar{d}$

1st results from PHENIX and STAR

arXiv:1009.0505

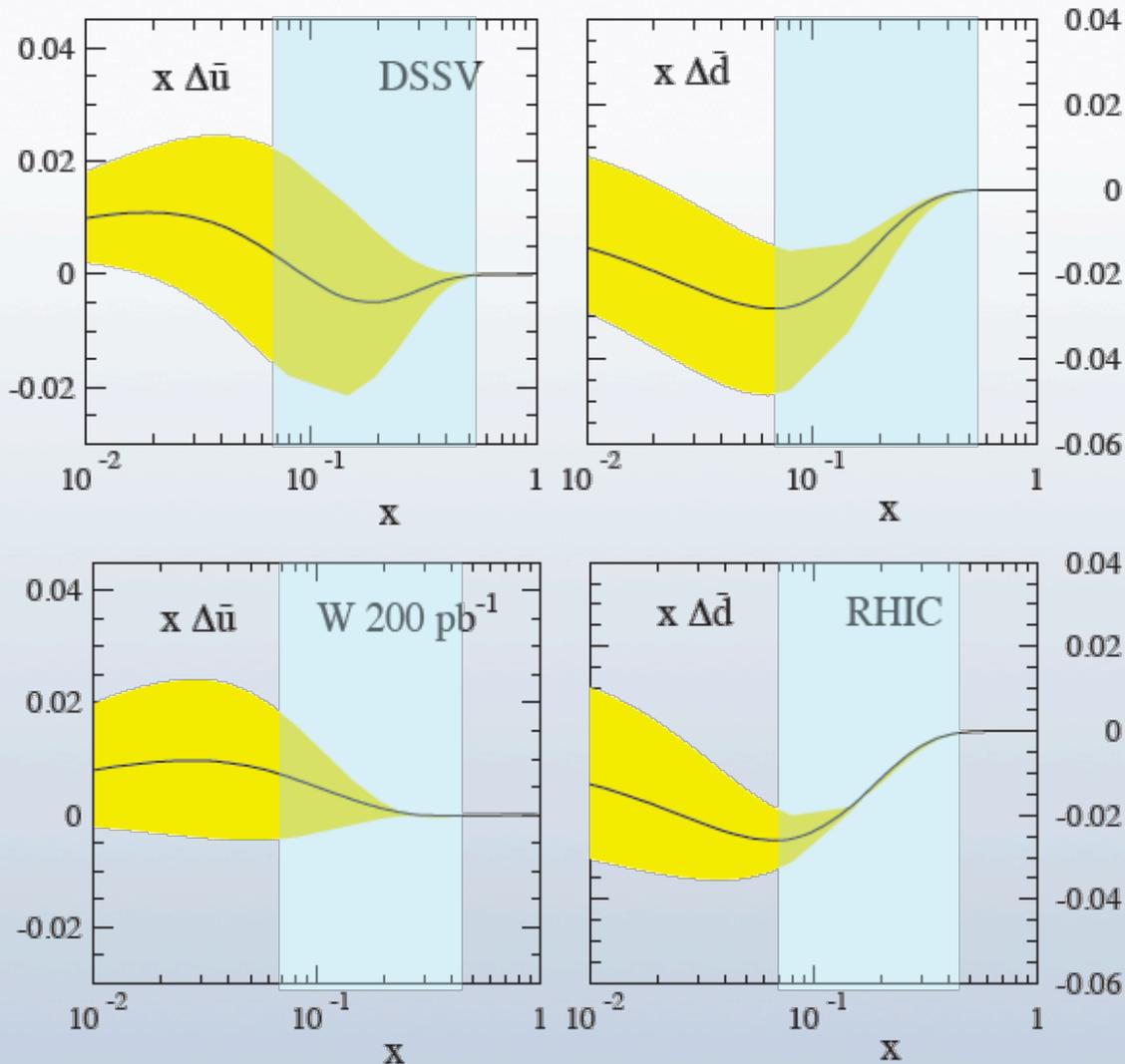
arXiv:1009.0326



- no impact on fits yet
“proof of principle”

W program @ RHIC: what can we learn?

✓ "CHE" integrates nicely into DSSV global analysis code based on Mellin moments



$\Delta\chi^2 = 2\%$ uncertainty bands of DSSV analysis

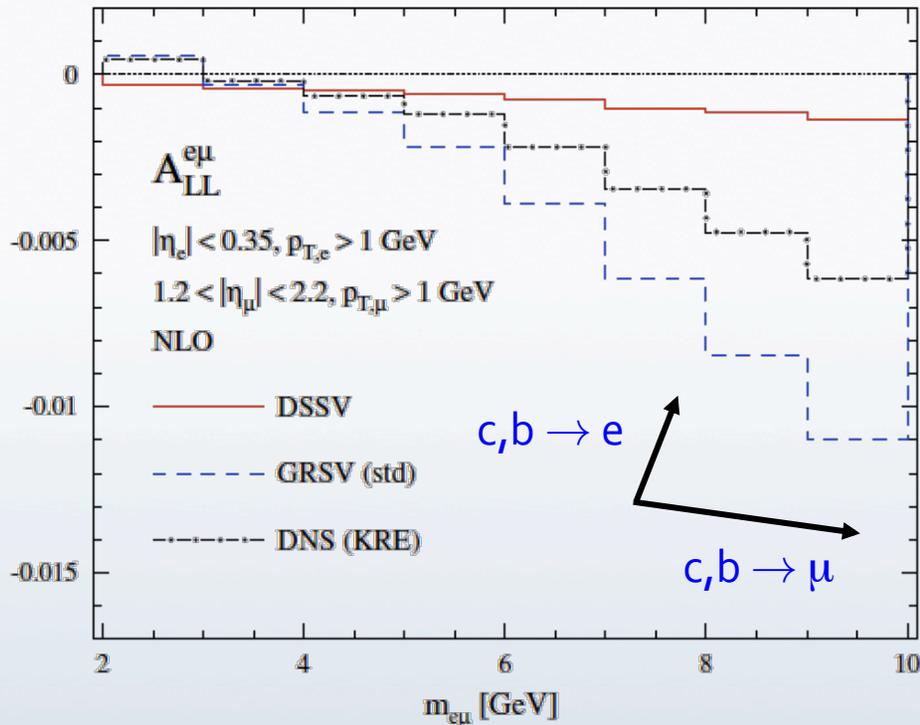
simulated impact of RHIC W boson data on global fit

- ✓ reduction of uncertainties for $0.07 < x < 0.4$
- ✓ can test consistency of low Q^2 SIDIS data in that x regime

future: heavy quark correlations

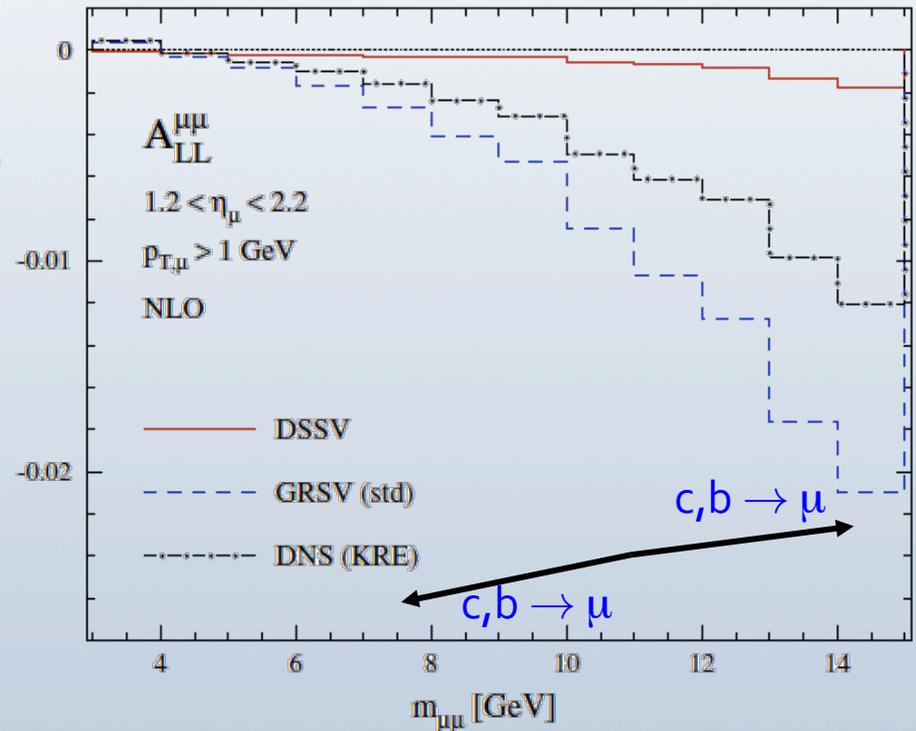
forward-central e- μ coincidences

- best suited heavy flavor observables to explore nucleon spin structure
- different hard scatt. dynamics than jets
- clear correlation between A_{LL} and Δg
- full NLO MC available [Riedl, Schafer, MS](#)



forward-backward μ - μ coincidences

luminosities of a **few hundred pb^{-1}** are required for meaningful measurements at $m_{e\mu, \mu\mu}$ up to 10-15 GeV



opportunities for spin physics studies at an EIC

so far, our knowledge on polarized (SI)DIS is based on fixed target experiments

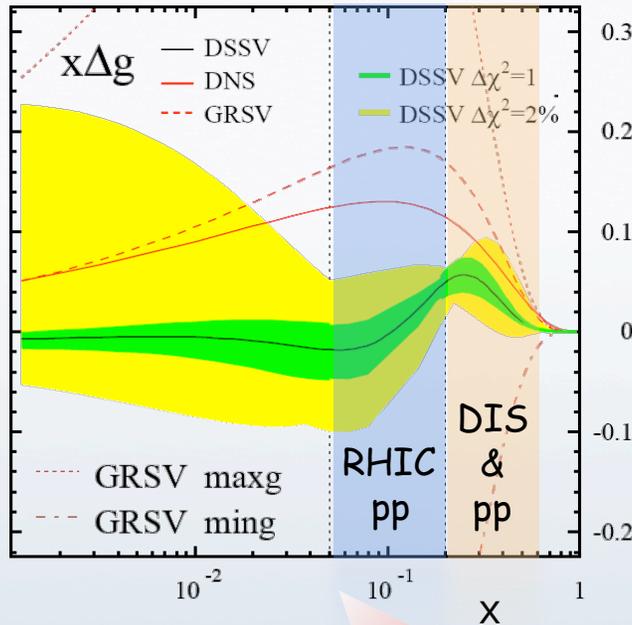
many "weak spots" & room for new "spin surprises":

- small x region: crucial for all sum rules ("proton spin", "Bjorken", ...) **unknown**
- flavor separation: SU(2) breaking, strangeness **largely unknown**
- electro-weak effects/structure fcts. **never measured**
- full understanding of transverse spin phenomena **still in early stages**
- issues with factorization for Sivers fct. **intriguing**
- role of orbital angular momentum **largely unknown**
- plus: spin phenomena in diffraction, photoproduction, hadronization, ...

**repeat full HERA program in polarized high energy ep scattering
with good particle ID & ability to measure exclusive processes**

teaser I: what can be achieved for Δg ?

recall:

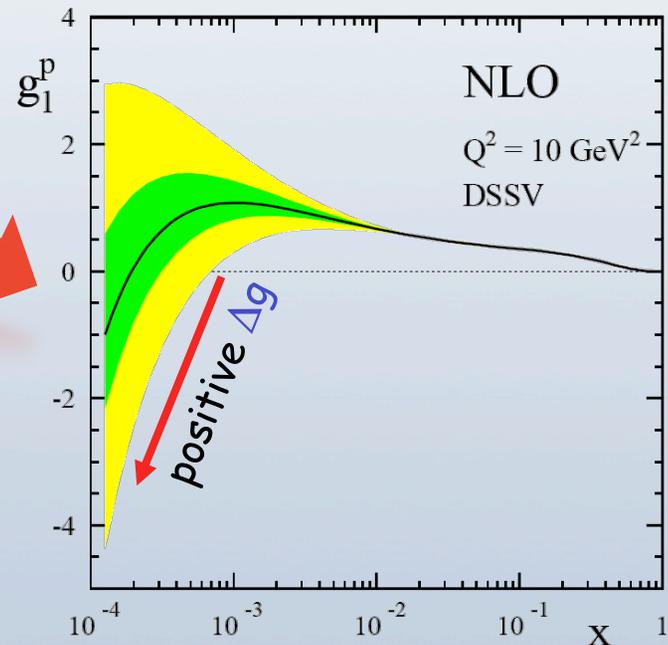


DSSV global fit
de Florian, Sassot,
MS, Vogelsang

- low x behavior unconstrained
- no reliable error estimate for 1st moment $\int_0^1 dx \Delta g(x, Q^2)$ (entering spin sum rule)
- find $\int_{0.05}^{0.2} dx \Delta g(x, Q^2) \approx 0$

pQCD scaling violations

$$\frac{dg_1}{d \log(Q^2)} \propto -\Delta g(x, Q^2)$$

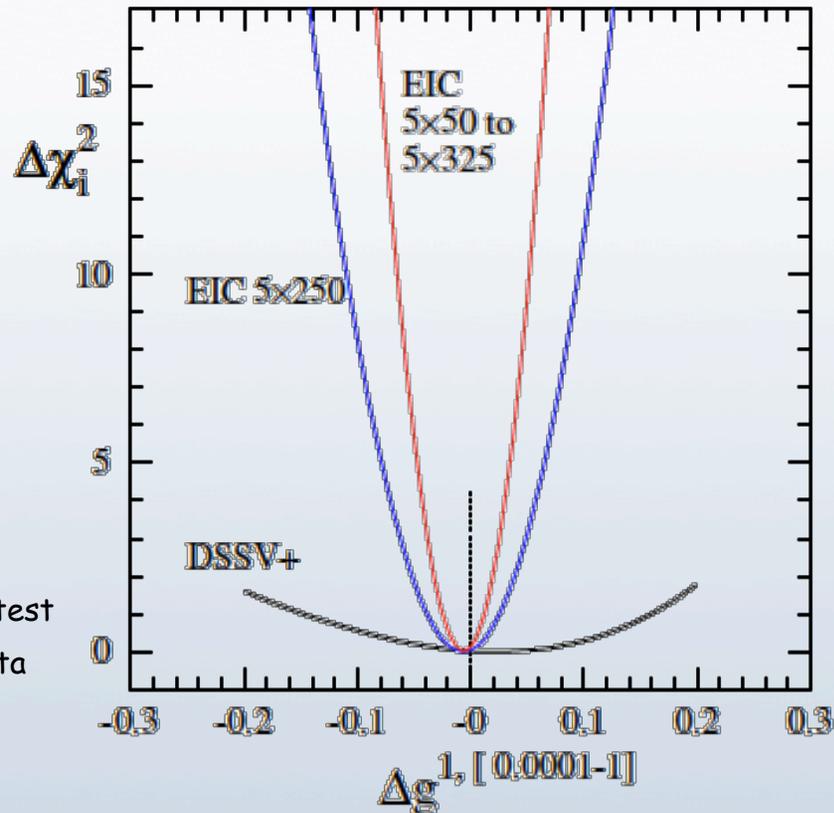


what can be achieved for Δg ? - cont'd

how effective are scaling violations at the EIC...

(studies based on simulated data for stage-1 [5x50, 5x100, 5x250, 5x325])

Sassot, MS



DSSV+ includes also latest
COMPASS (SI)DIS data
(no impact on DSSV Δg)



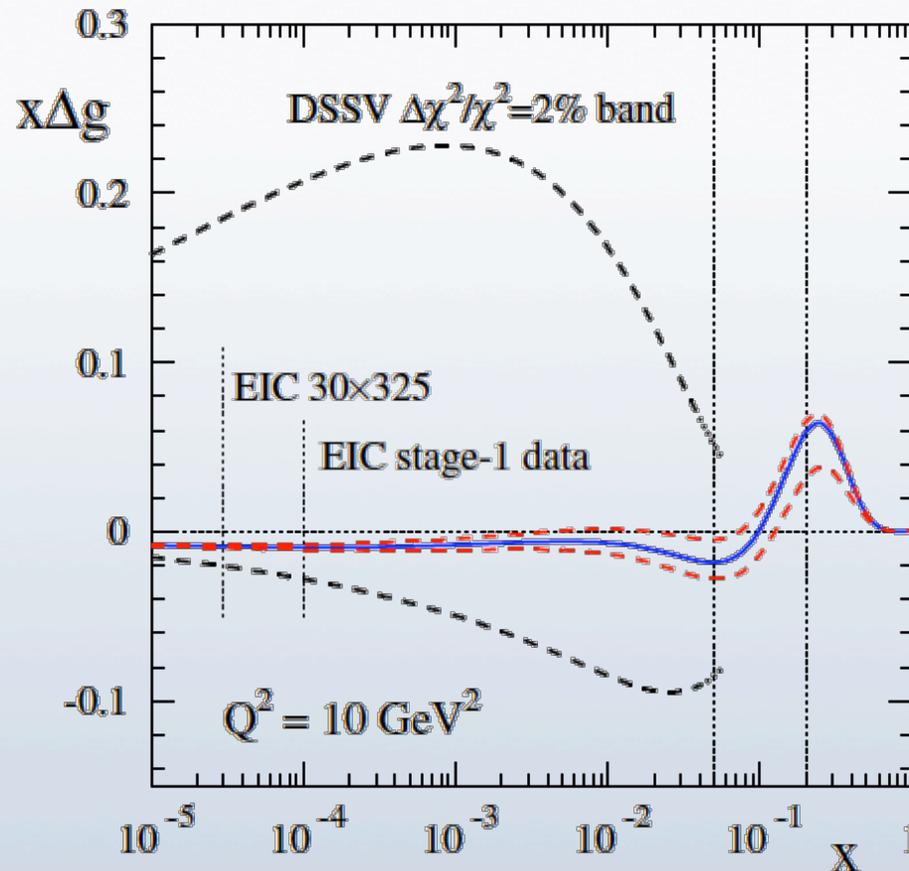
χ^2 profile slims down
significantly already
for EIC stage-1
(one month of running)

- with 30x325 one can reach down to $x \approx 3 \times 10^{-5}$ (impact needs to be studied)

what can be achieved for Δg ? - cont'd

what about the uncertainties on the x-shape ...

Sassot, MS



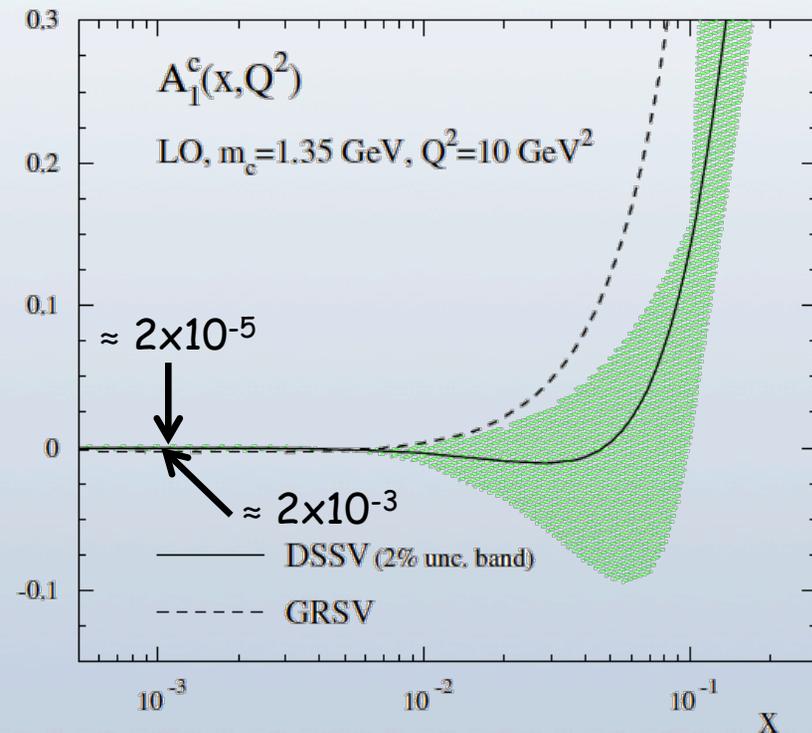
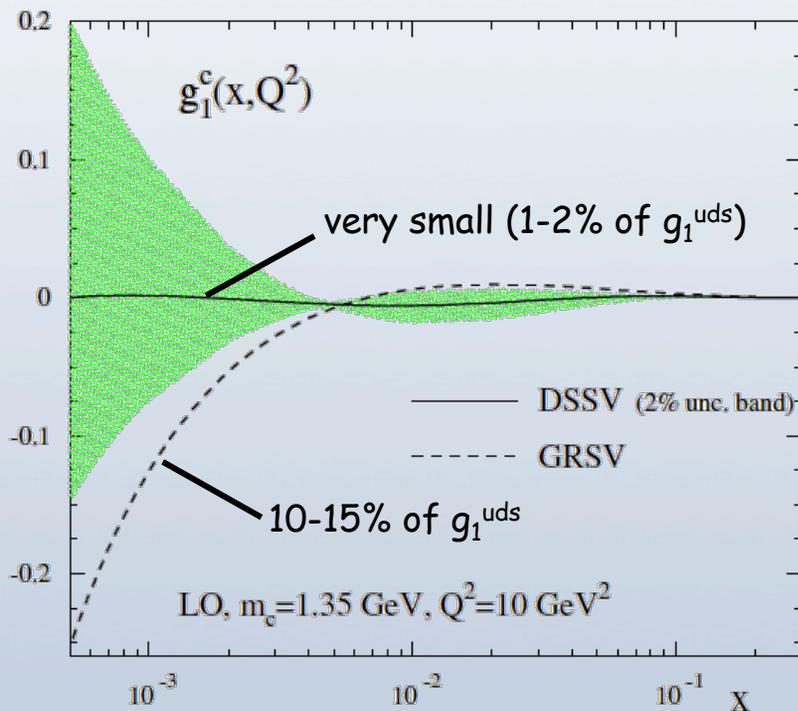
... wow - cool!

- even with flexible DSSV x-shape we can now determine $\int_0^1 dx \Delta g(x, Q^2)$ up to ± 0.07
- work in progress: try weird x-shapes below $x = 10^{-4}$ to improve/check error estimate

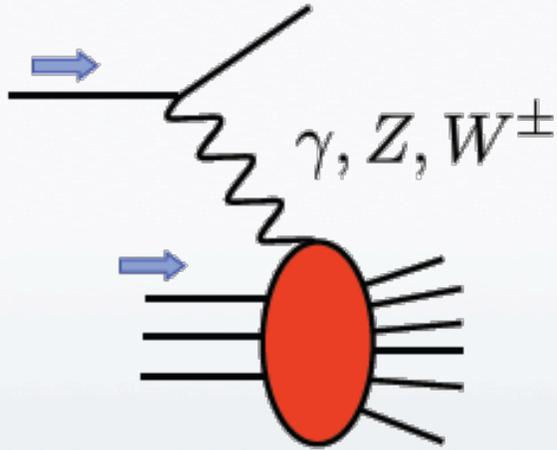
issue: charm contribution to g_1

- so far safely ignored: $\ll 1\%$ to existing g_1 fixed-target data
- relevance at an EIC depends strongly on size of Δg
- need massive Wilson coefficients (charm not massless for most of EIC kinematics)
so far only known to LO (NLO is work in progress [Kang, MS](#))

some expectations: (needs to be studied in detail)



teaser II: electroweak effects at high Q^2



at high enough Q^2 electroweak probes become relevant

- neutral currents (γ , Z exchange, γZ interference)
- charged currents (W exchange)

parameterized by new structure functions which probe combinations of PDFs different from photon exchange

--> **flavor decomposition without SIDIS, e-w couplings**

hadron-spin averaged case: studied to some extent at HERA (limited statistics)

hadron-spin difference:

contains
e-w propagators
and couplings

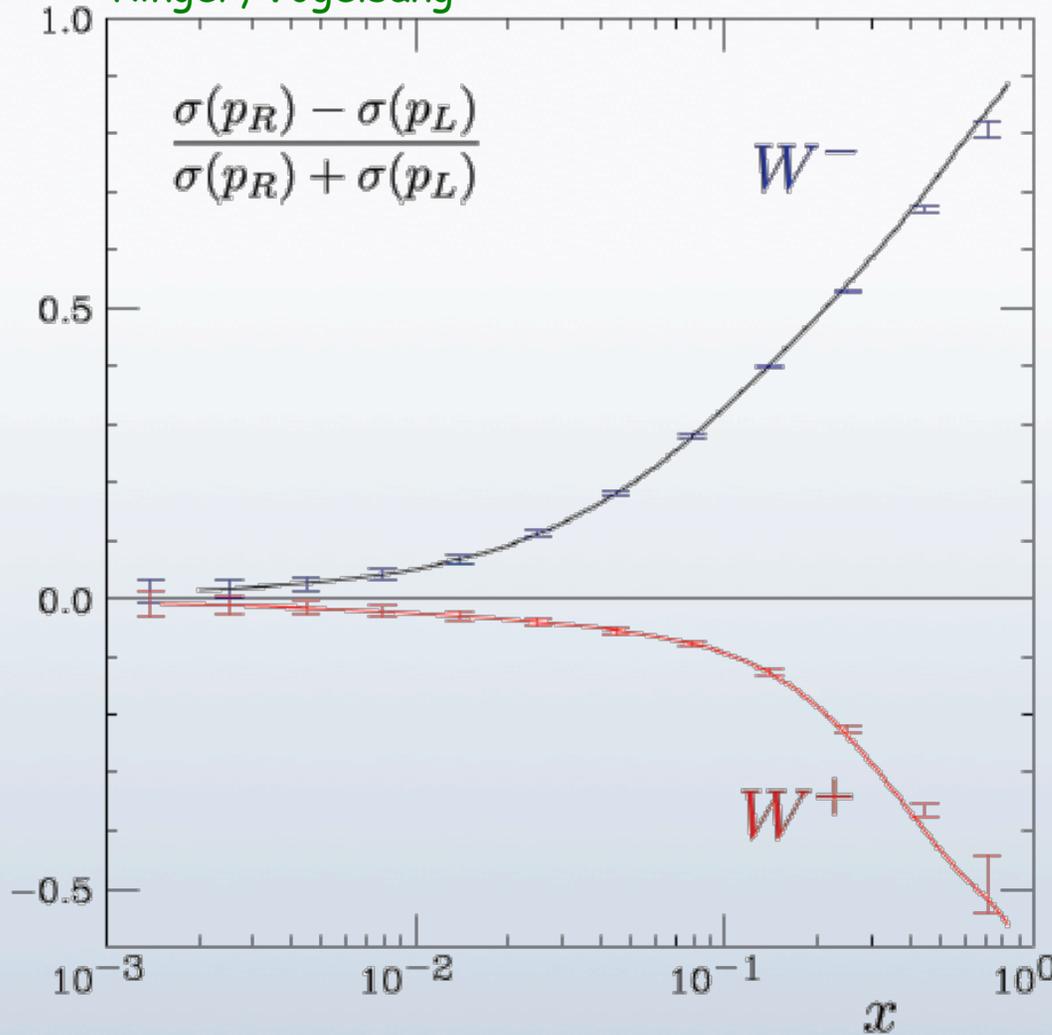
Wray; Derman; Weber, MS, Vogelsang;
Anselmino, Gambino, Kalinowski;
Blumlein, Kochelev; Forte, Mangano, Ridolfi; ...

$$\frac{d\Delta\sigma^{e^\mp, i}}{dx dy} = \frac{4\pi\alpha^2}{xyQ^2} \left[\pm y(2-y)x\hat{g}_1^i - (1-y)\hat{g}_4^i - y^2x\hat{g}_5^i \right] \quad i = \text{NC, CC}$$

unexplored so far - unique opportunity for an EIC

feasibility - 1st exploratory studies

Ringer, Vogelsang



20 × 250 GeV

$Q^2 > 1 \text{ GeV}^2$

$0.1 < y < 0.9$

10 fb⁻¹

DSSV PDFs

very promising!

even doable with
5x250 GeV

$$A^{W^-} = \frac{(\Delta u + \Delta c) - (1 - y)^2(\Delta \bar{d} + \Delta \bar{s})}{(u + c) + (1 - y)^2(\bar{d} + \bar{s})} \quad A^{W^+} = \frac{(1 - y)^2(\Delta d + \Delta s) - (\Delta \bar{u} + \Delta \bar{c})}{(1 - y)^2(d + s) + (\bar{u} + \bar{c})}$$

other opportunities in polarized DIS

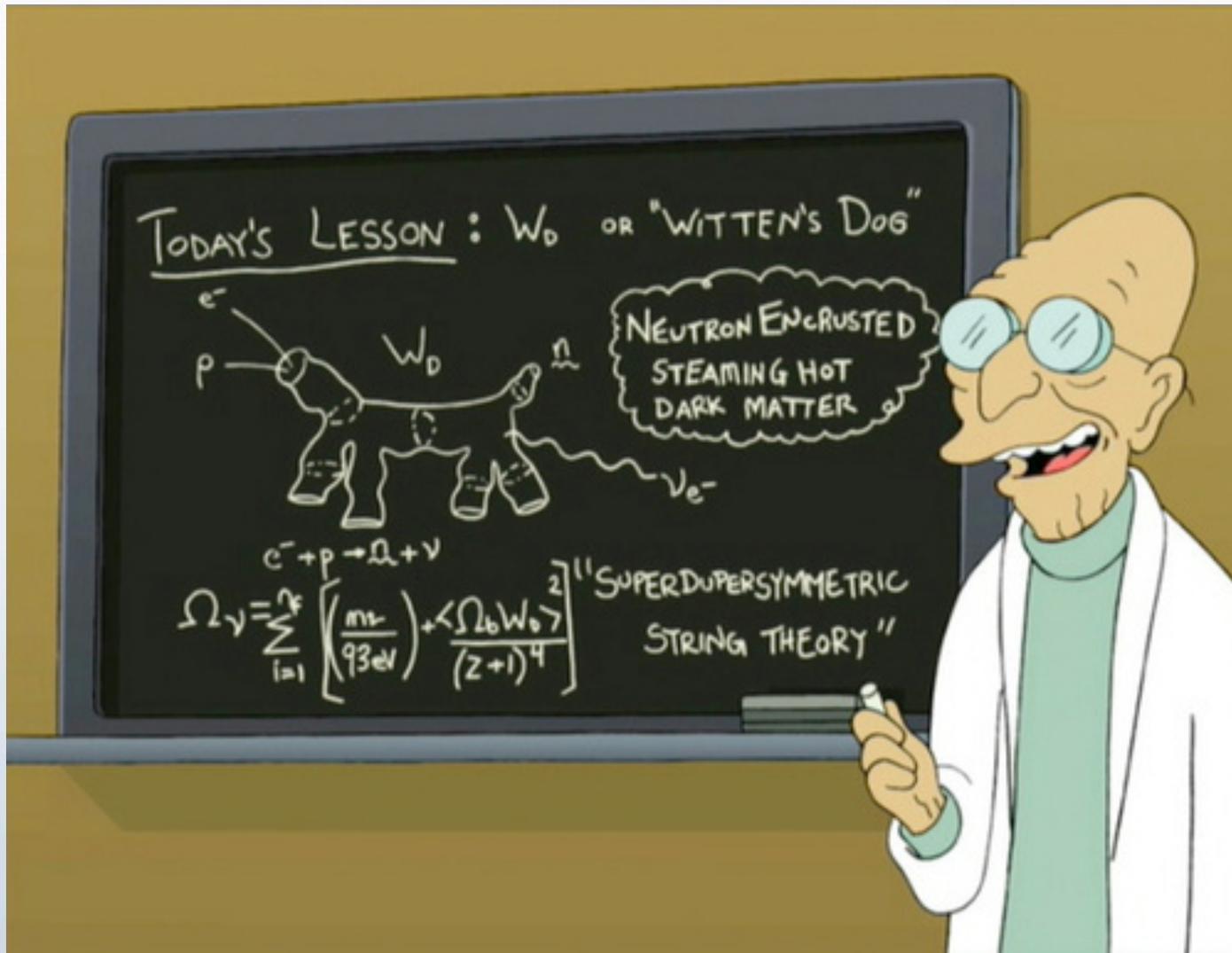
- in 10+ years the NNLO corrections will be available (needed to match precision of data) Moch, Vogt, ...
- watch out for surprises at small-x = deviations from DGLAP (expected to set in earlier than in unpol. DIS; showing up as tension in global fit (?)) Bartels, Ermolaev, Ryskin; Greco, Troyan; ...
- strong coupling from scaling violations (needs to be worked out / quantified)

• Bjorken sum rule:
$$\int_0^1 dx [g_1^p(x, Q^2) - g_1^n(x, Q^2)] = \frac{1}{6} C_{Bj} [\alpha_s(Q^2)] g_A$$

- C_{Bj} known to $O(\alpha_s^4)$ Kodaira; Gorishny, Larin; Larin, Vermaseren; Baikov, Chetyrkin, Kühn, ...
- but not a tool to determine α_s (1% change in α_s translates in 0.08% change of Bj sum)
- experimental challenge: effective neutron beam (^3He), very precise polarimetry, ...
- theor. motivation for precision measurement: **Crewther relation**

non-trivial relation of two seemingly unrelated quantities

$$\text{Adler function } D(Q^2) \text{ in } e^+e^- \begin{array}{c} \xleftrightarrow{\sim 1 + \frac{\beta(\alpha_s)}{\alpha_s} K(\alpha_s)} \\ \text{deviation from} \\ \text{exact conformal symmetry} \end{array} \text{ Bj sum } C_{Bj}(Q^2) \text{ in DIS}$$



SUMMARY

final remarks



FFs are in good shape - many new data sets available/upcoming
watch out for updated DSS sets & more detailed uncertainty studies



DSSV describes all new polarized data sets well - no refit needed
still many open questions: strangeness, flavor separation, 1st moments, ...



global QCD analyses are an ongoing effort:
more data sets/processes; further improvements (e.g. on uncertainties)



many opportunities at a future EIC:
small x behavior of Δg , electro-weak effects, ...