

# LHCb results on Tetra- and Penta-Quark candidates

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Oct 26, 2015  
at

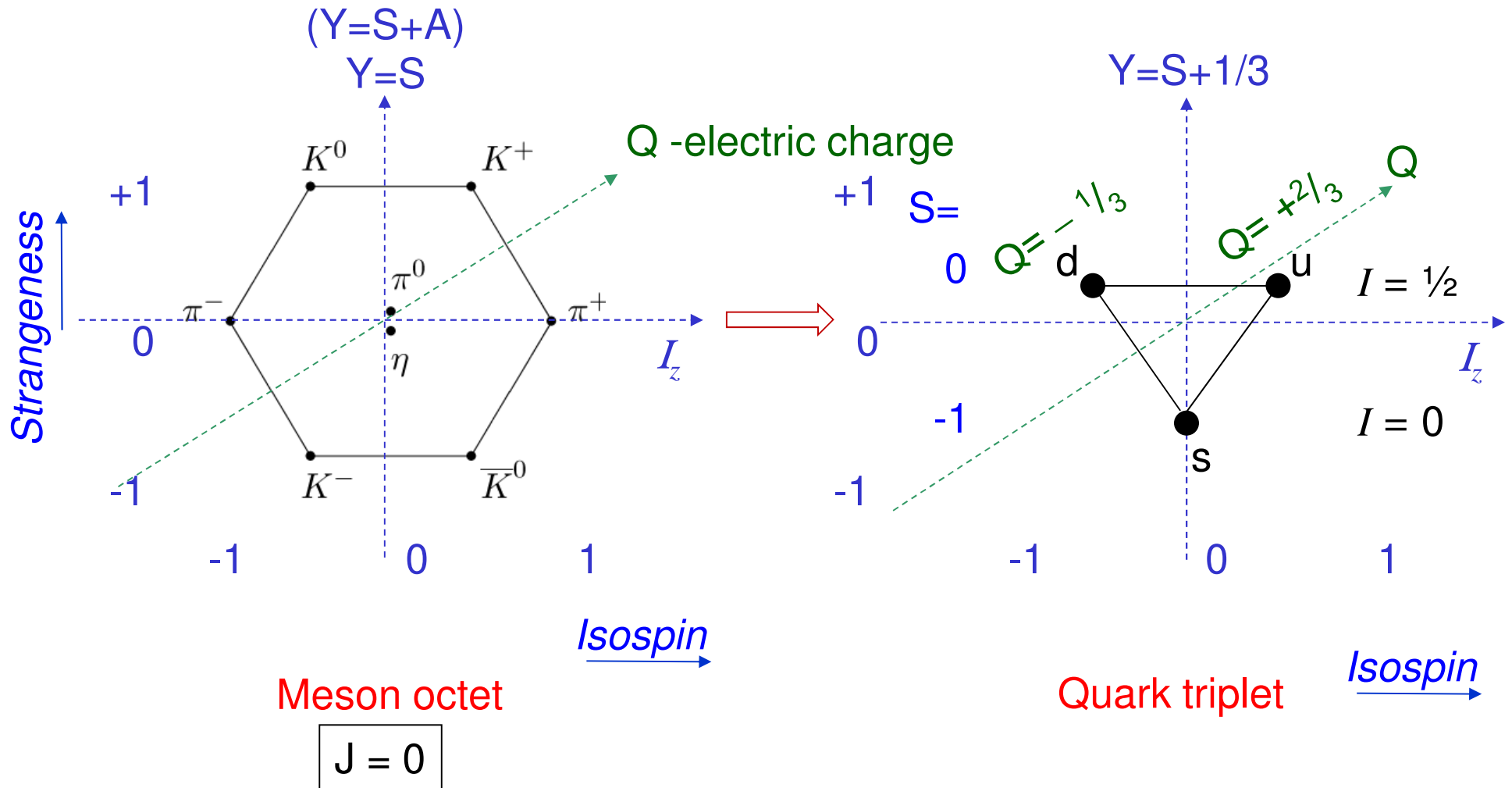


**Jefferson Lab**  
Thomas Jefferson National Accelerator Facility



# Quark hypothesis – SU(3) flavor symmetry

“Eightfold Way” symmetry – Gell-Mann 1961



(also  $J=1/2$  baryon octet and  $J=3/2$  decuplet)

- Quarks initially treated as mathematical abstractions

# “Exotic” mutiquark states conceived already at the birth of Quark Model

Volume 8, number 3

PHYSICS LETTERS

1 February 1964

## A SCHEMATIC MODEL OF BARYONS AND MESONS \*

M. GELL-MANN

*California Institute of Technology, Pasadena, California*

Received 4 January 1964

...

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u\frac{1}{3}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks"  $q$  and the members of the anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(q\bar{q}\bar{q})$ , etc. It is assumed that the lowest baryon configuration  $(qqq)$  gives just the representations 1, 8, and 10 that have been observed, while

8419/TH.412

21 February 1964

AN  $SU_3$  MODEL FOR STRONG INTERACTION SYMMETRY AND ITS BREAKING

II \*)

G. Zweig

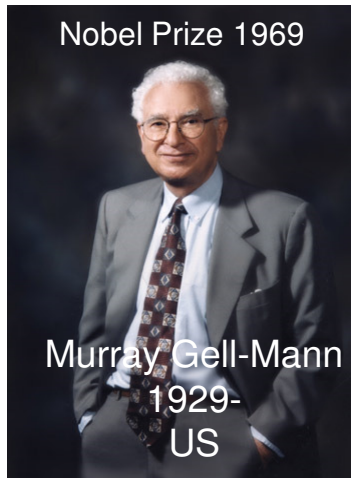
CERN---Geneva

\*) Version I is CERN preprint 8182/TH.401, Jan. 17, 1964.

...

- 6) In general, we would expect that baryons are built not only from the product of three aces,  $AAA$ , but also from  $\bar{A}AAAA$ ,  $A\bar{A}AAAA$ , etc., where  $\bar{A}$  denotes an anti-ace. Similarly, mesons could be formed from  $\bar{A}A$ ,  $\bar{A}AAA$  etc. For the low mass mesons and baryons we will assume the simplest possibilities,  $\bar{A}A$  and  $AAA$ , that is, "deuces and treys".

Nobel Prize 1969



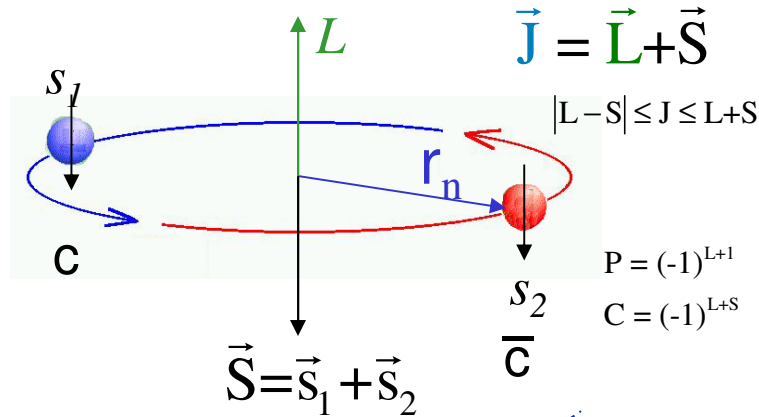
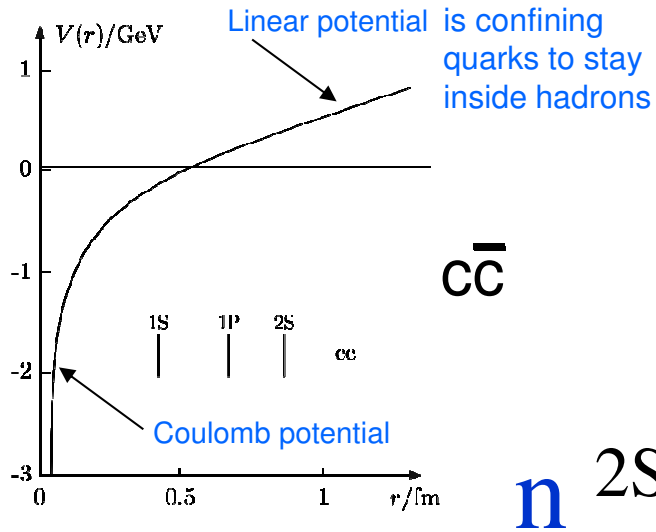
Murray Gell-Mann  
1929-  
US



George Zweig  
1937-  
US

# Charmonium – narrow (i.e. long-lived) states

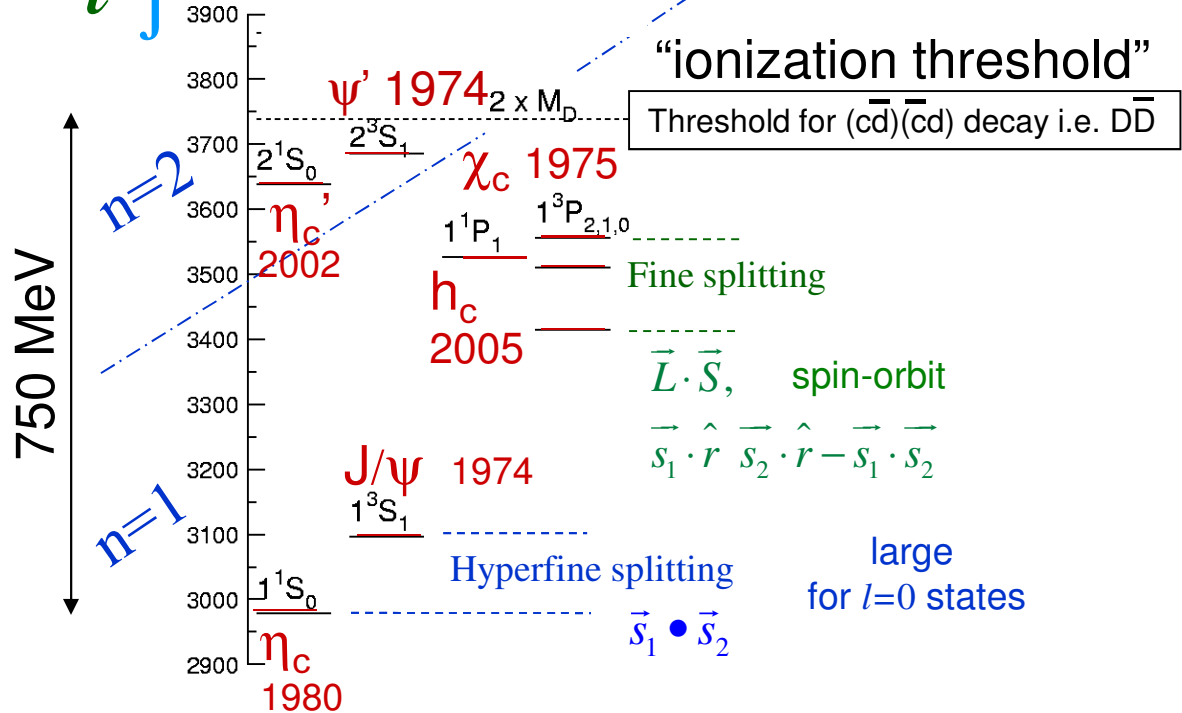
Non-relativistic quantum mechanics!



Forces between quarks are 10-100 times **stronger** than between nucleons!

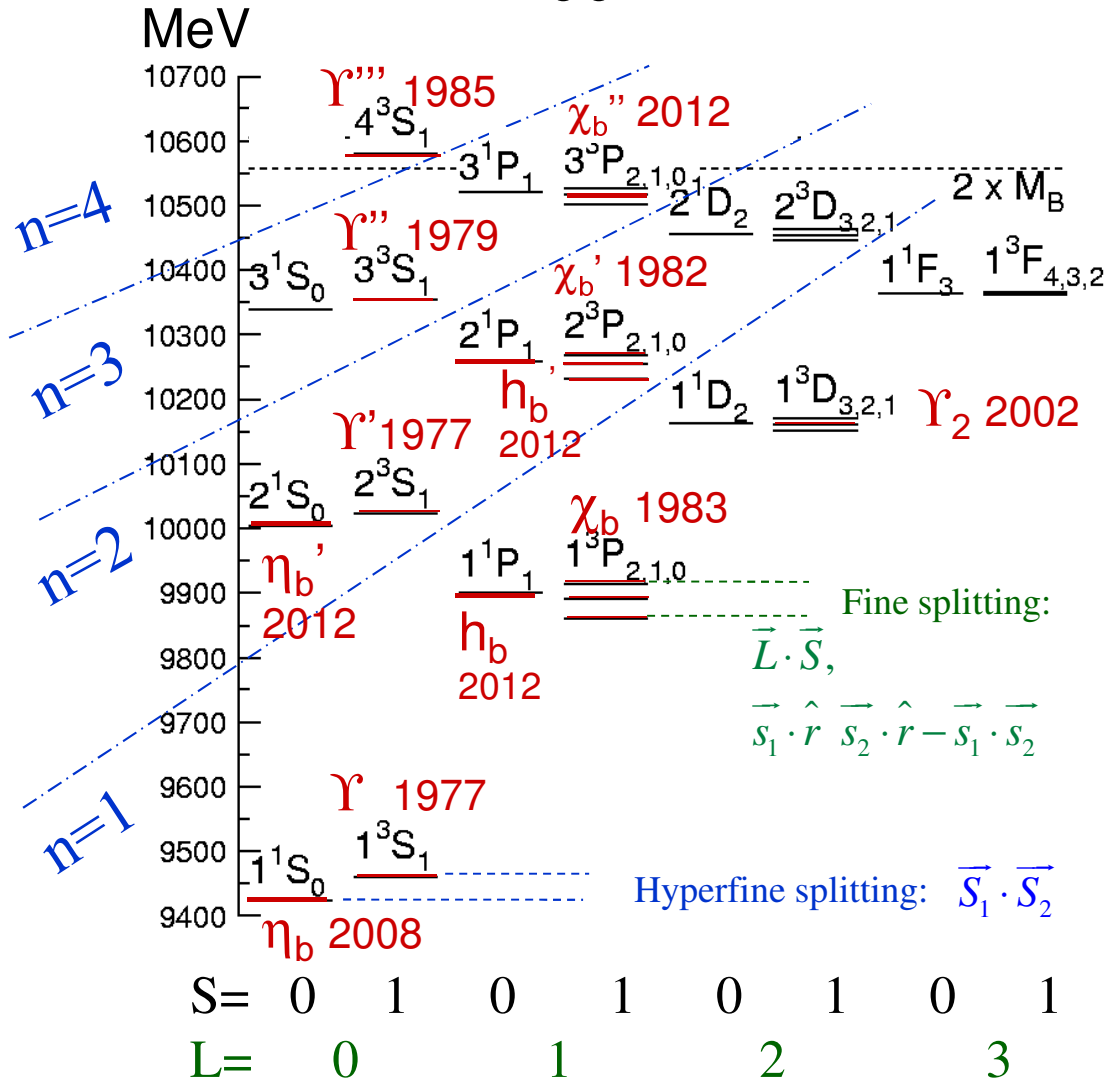
## 1974 November revolution:

- Quark Model and  $q\bar{q}$  hypothesis for mesons firmly established!
- However, near mass equality of light quarks was coincidental



# Bottomonium – narrow states

$b\bar{b}$



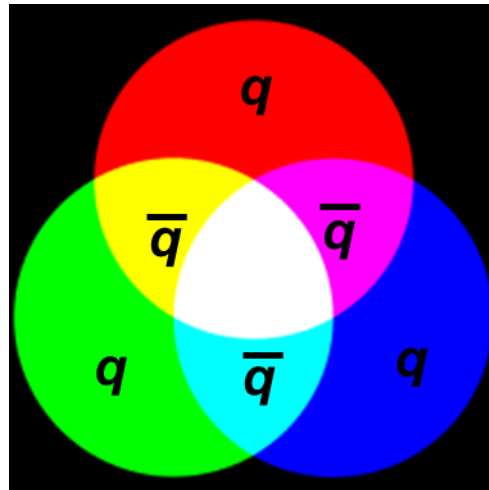
“ionization threshold” ( $B\bar{B}$ )

- Even more long-lived states

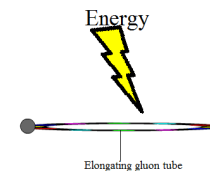
Impressive agreement between the observed states and  $b\bar{b}$  non-relativistic potential model

## SU(3) color symmetry

- Fundamental parts of  $SU(3)_{\text{flavor}}$  symmetry discovered by Gell-Mann & Zweig:
  - Quark flavor independence of strong interactions
  - Rules for making hadrons out of quarks – led to development of exact theory of strong interactions, QCD based on  $SU(3)_{\text{color}}$  symmetry

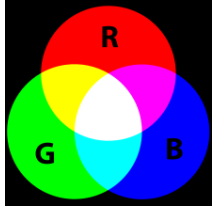


Breaking of color field flux tube by popping of  $q\bar{q}$  pair:



Strength of color interactions raises with separation of color charges  $\rightarrow$  confinement of color charge  $\rightarrow$  hadrons must be color neutral i.e. “white” ( $q\bar{q}$ ,  $qqq$ , ....)

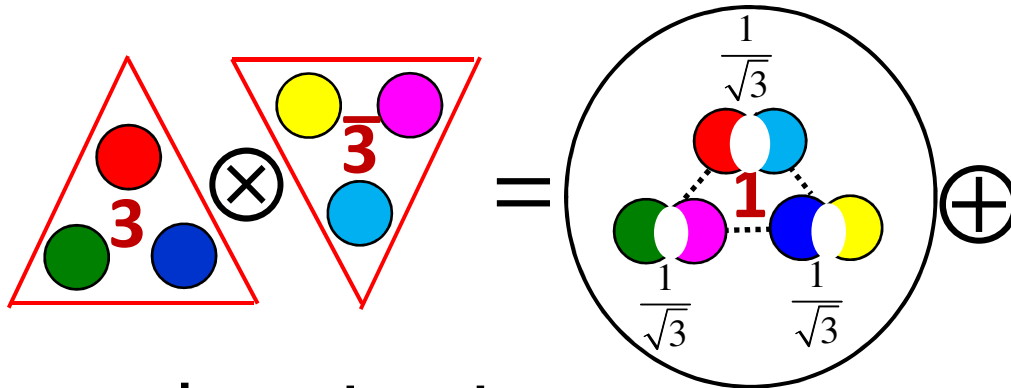
# Mesons from quarks & antiquarks in QCD



color triplet

color antitriplet

color singlet



quark antiquark

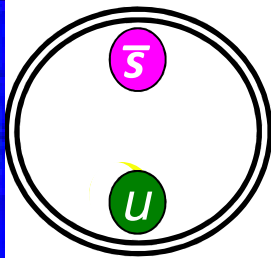
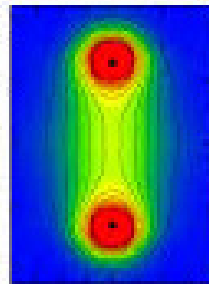
q

$\bar{q}$

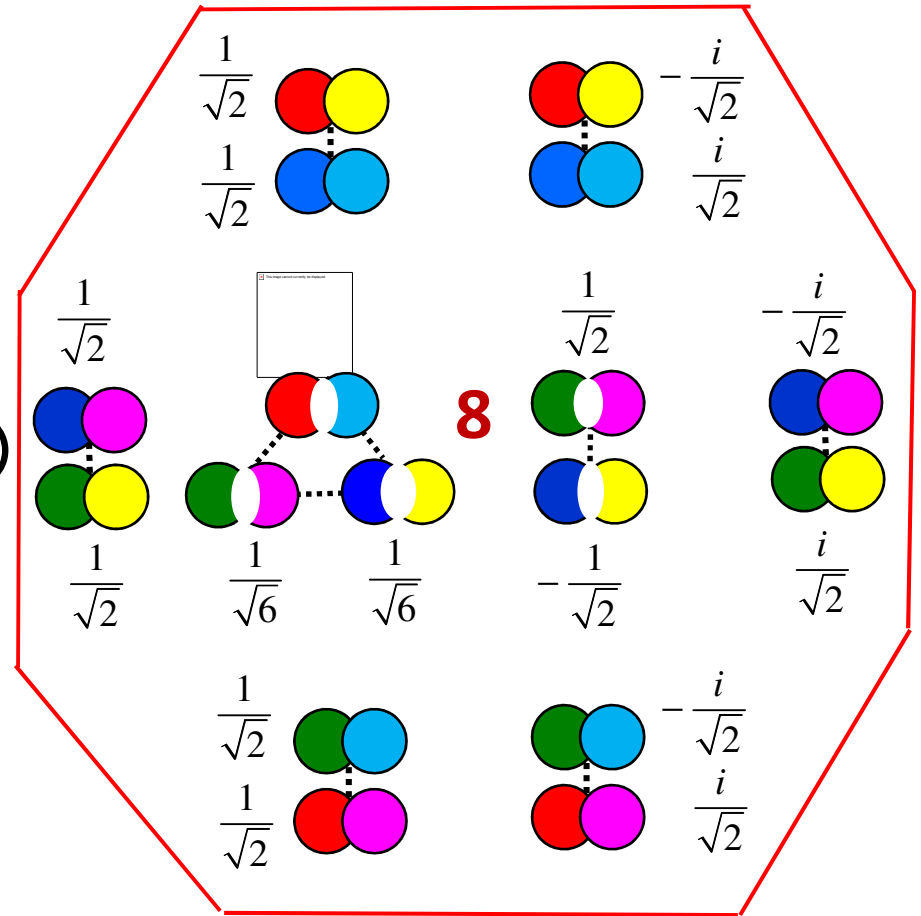
attractive color force

( $q\bar{q}$ ) meson  
e.g.  $K^+$

Color flux tube stretched between quark and antiquark with attractive potential



color octet

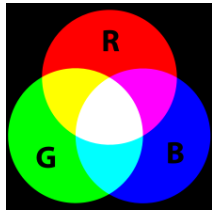


repulsive color force

quarks will pull apart in any octet configuration

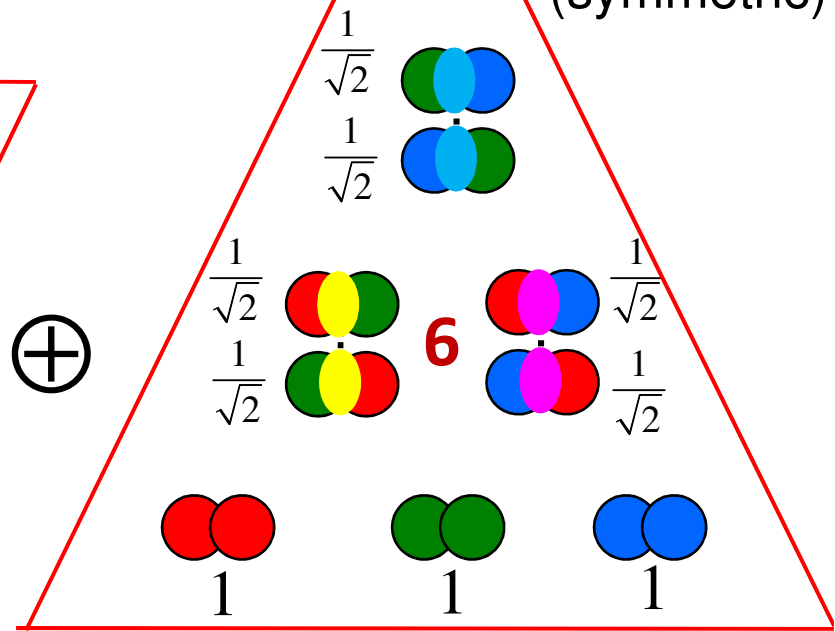
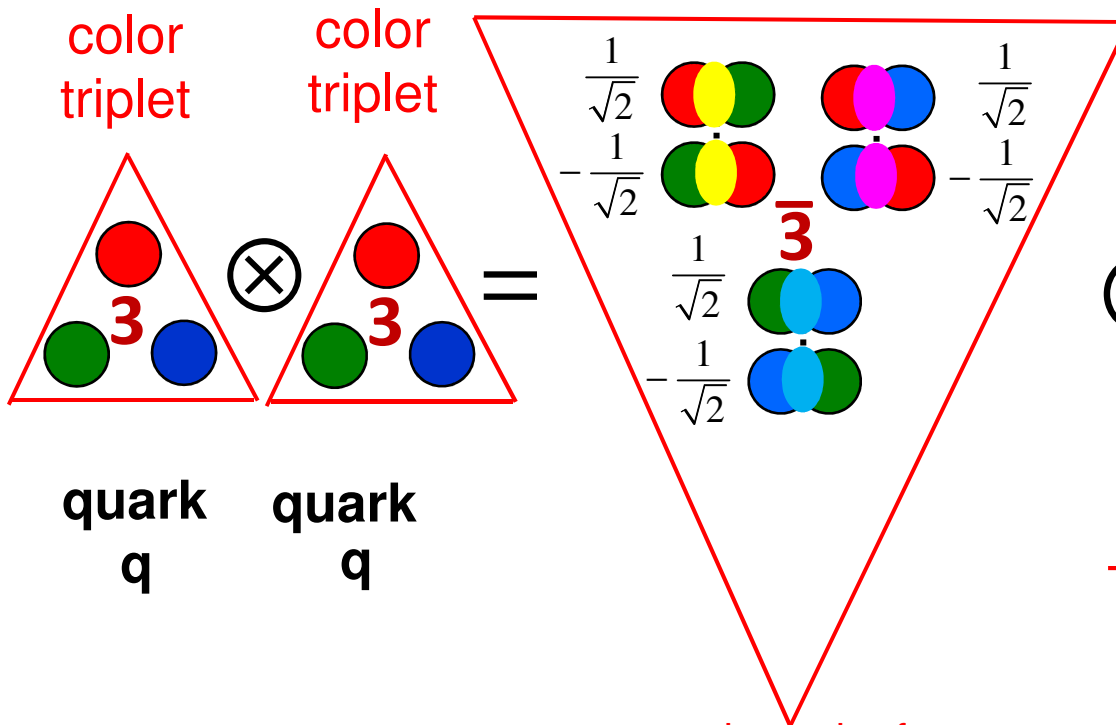
*gluons happen to belong to the color octet*

# (Colored) diquarks in QCD



(antisymmetric)  
color  
antitriplet

color  
sextet  
(symmetric)



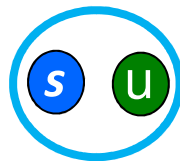
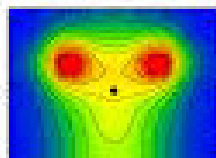
repulsive color force

attractive color force  
(half as strong as in the meson)

quarks will pull apart in any  
sextet configuration

## (qq) diquark

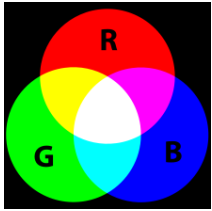
Color flux tube stretched between the quarks and extending to other color partners



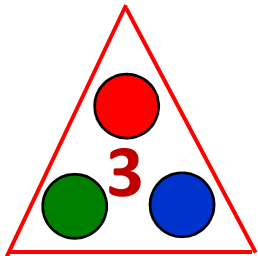
Not a particle, just a building block in QCD



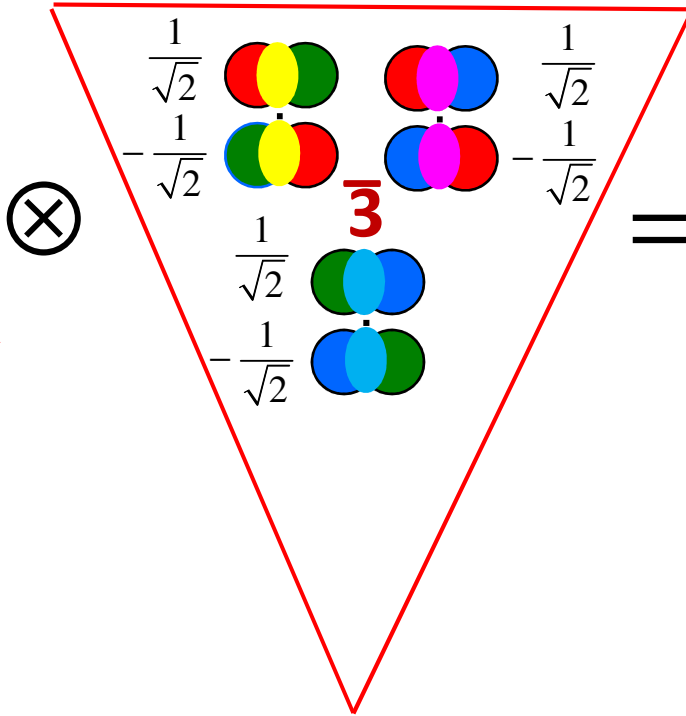
# Baryons from quarks and diquarks



color triplet

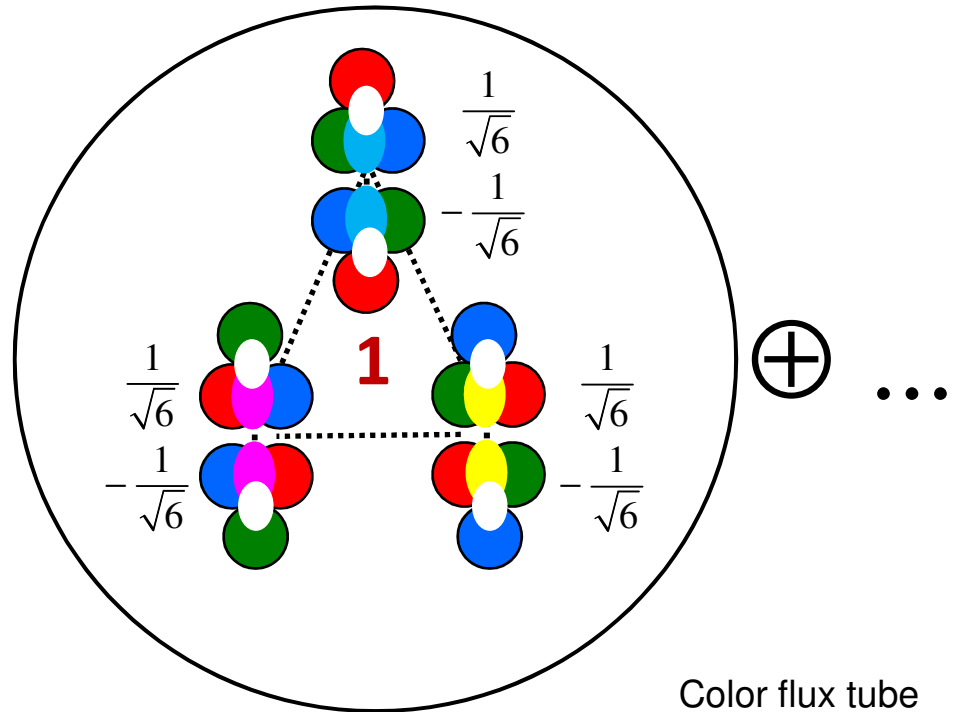


color antitriplet



attractive color force  
(qq) diquark

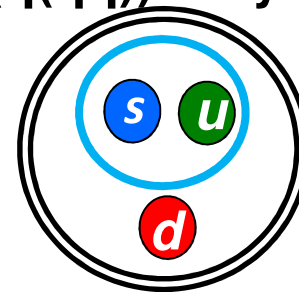
color singlet



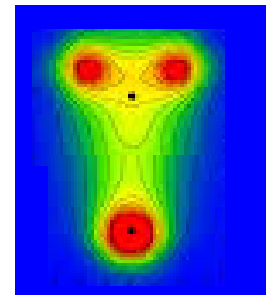
attractive color force  
(q(qq)) baryon

quark  
q

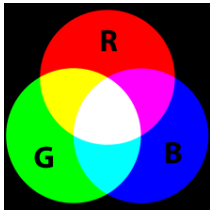
e.g.  $\Lambda$



Color flux tube stretched between the diquark and the third quark



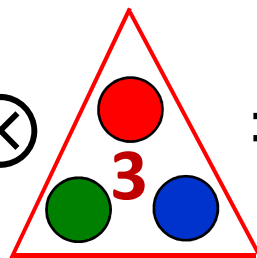
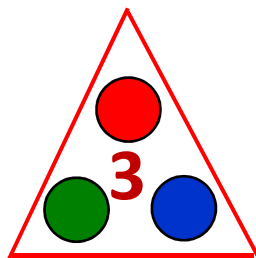
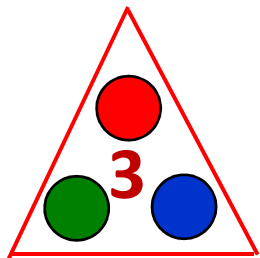
# Baryons directly from 3 quarks



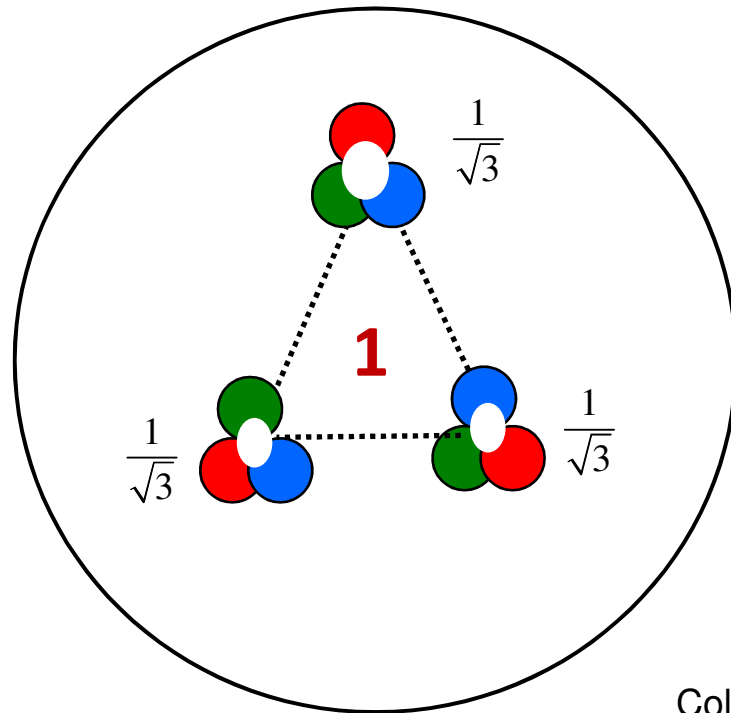
color triplet

color triplet

color triplet

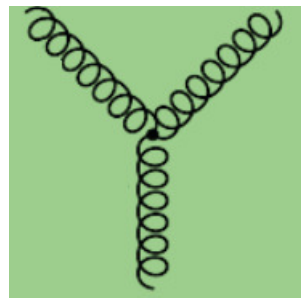


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...

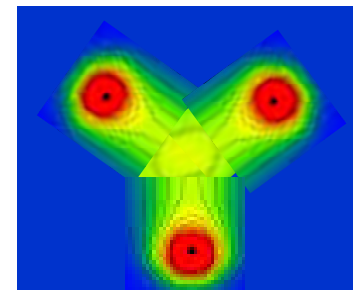
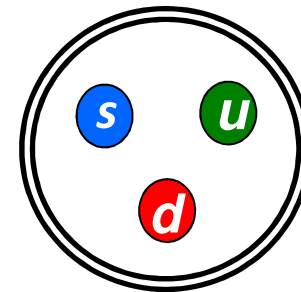
in QCD gluons can couple to each other



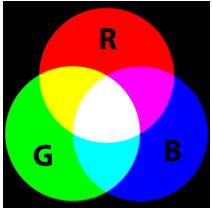
attractive color force  
(qqq) baryon

Color flux tube stretched between three quarks

Different forms of quark configurations in a baryon can coexist. Relative importance of diquarks can depend on quark flavors.



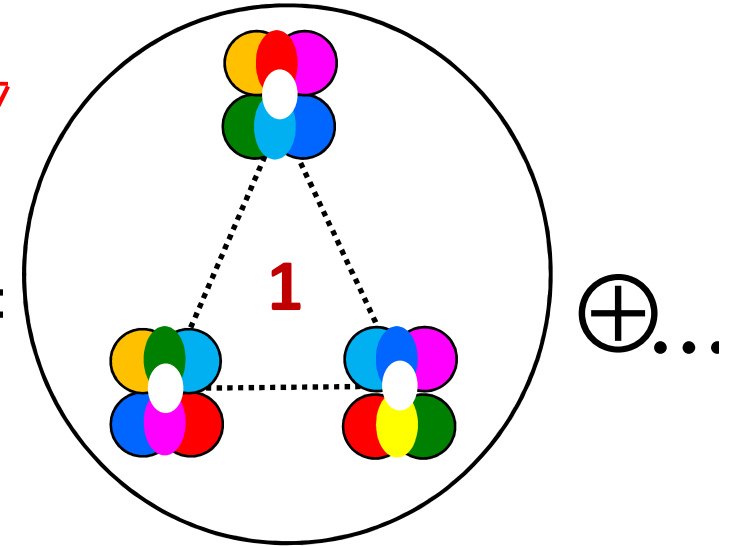
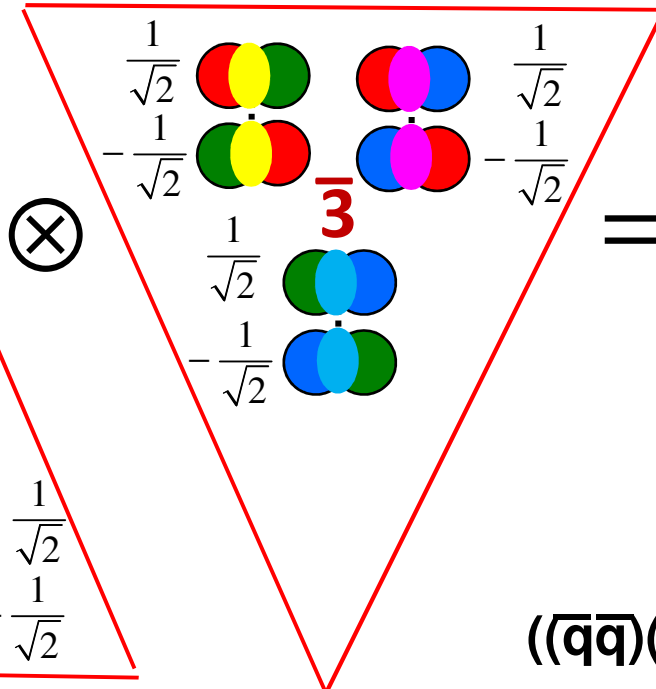
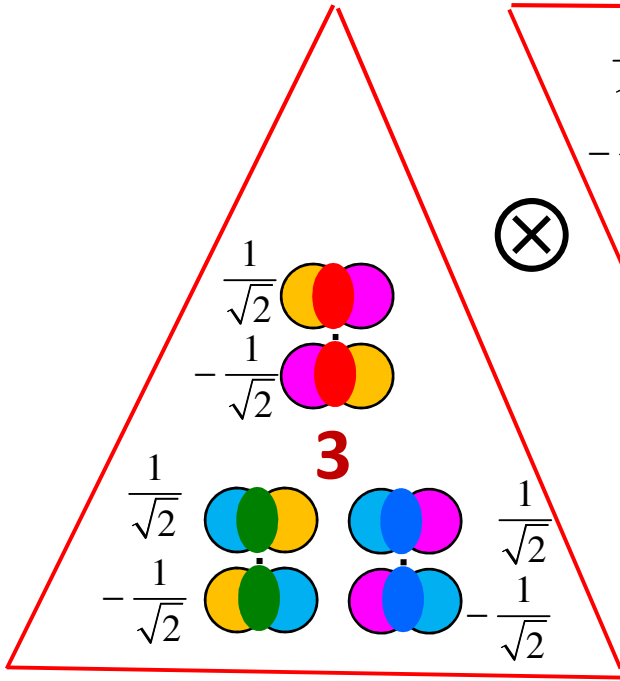
# Tetraquarks from diquarks and diantiquarks



color triplet

color antitriplet

color singlet



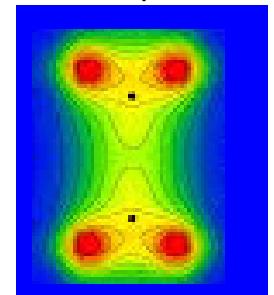
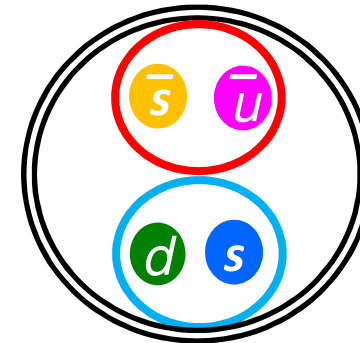
attractive color force  
 $(\bar{q}q)$  diantiquark

attractive color force  
 $(qq)$  diquark

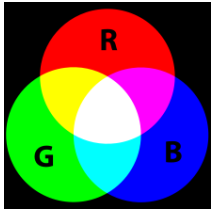
attractive color force

$(\bar{q}\bar{q})(qq)$  tetraquark

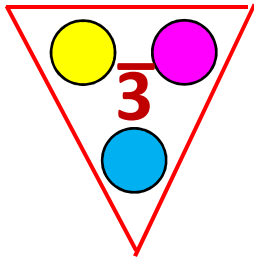
Color flux tube stretched between the diquark and diantiquark



# (Colored) triquarks from antiquarks and diquarks

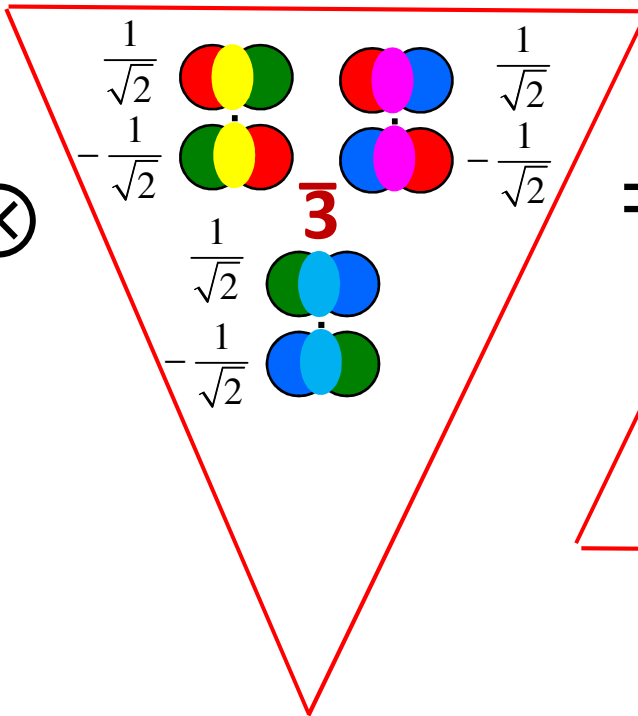


color  
antitriplet



⊗

color  
antitriplet

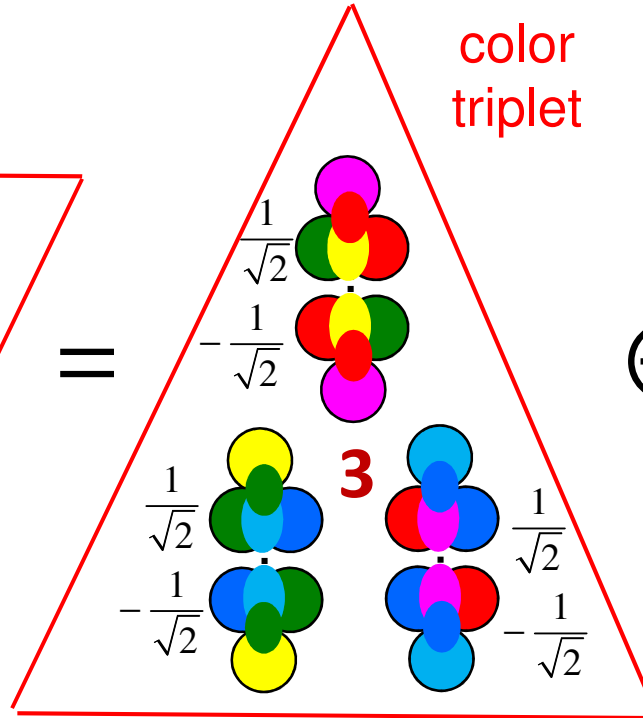


attractive color force

(qq) diquark

=

color  
triplet



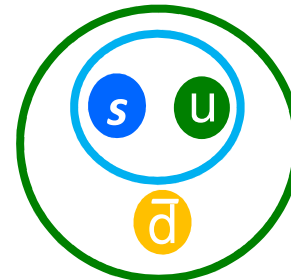
attractive color force

(q̄(qq)) triquark

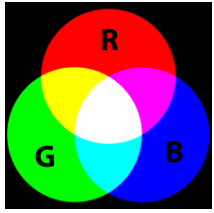
⊕

...

q̄  
antiquark



Not a particle, just a  
building block in  
QCD

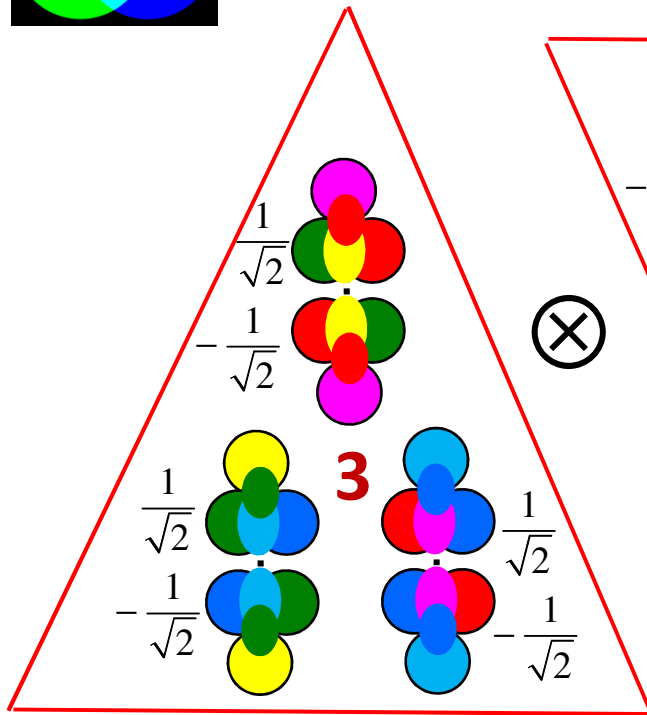


# Pentaquark from triquarks and diquarks

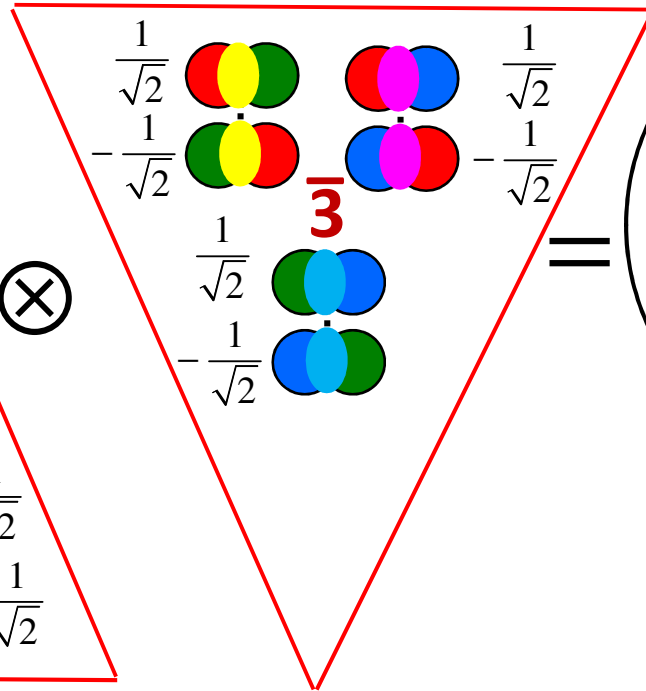
color triplet

color antitriplet

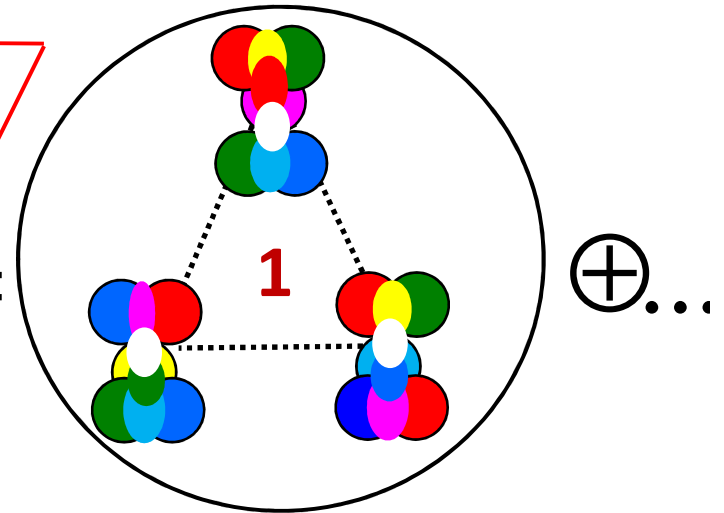
color singlet



$\otimes$



=

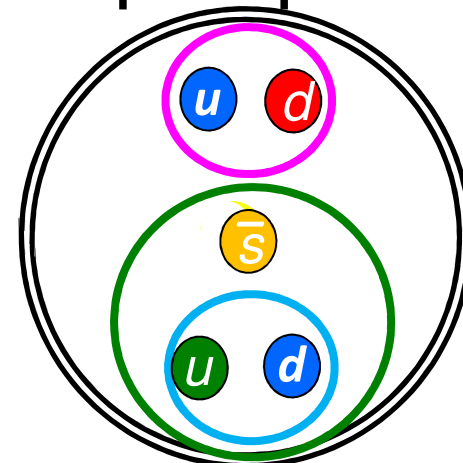


$\oplus \dots$

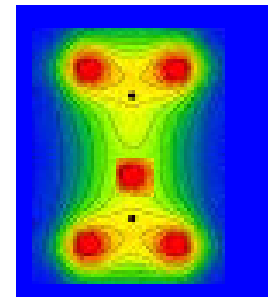
attractive color force  
 $(\bar{q}(qq))$  triquark

attractive color force  
 $(qq)$  diquark

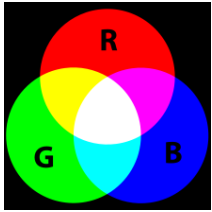
attractive color force  
 $((\bar{q}(qq))(qq))$   
pentaquark



Color flux tube stretched between the triquark and diquark



# Pentaquark directly from two diquarks and antiquark

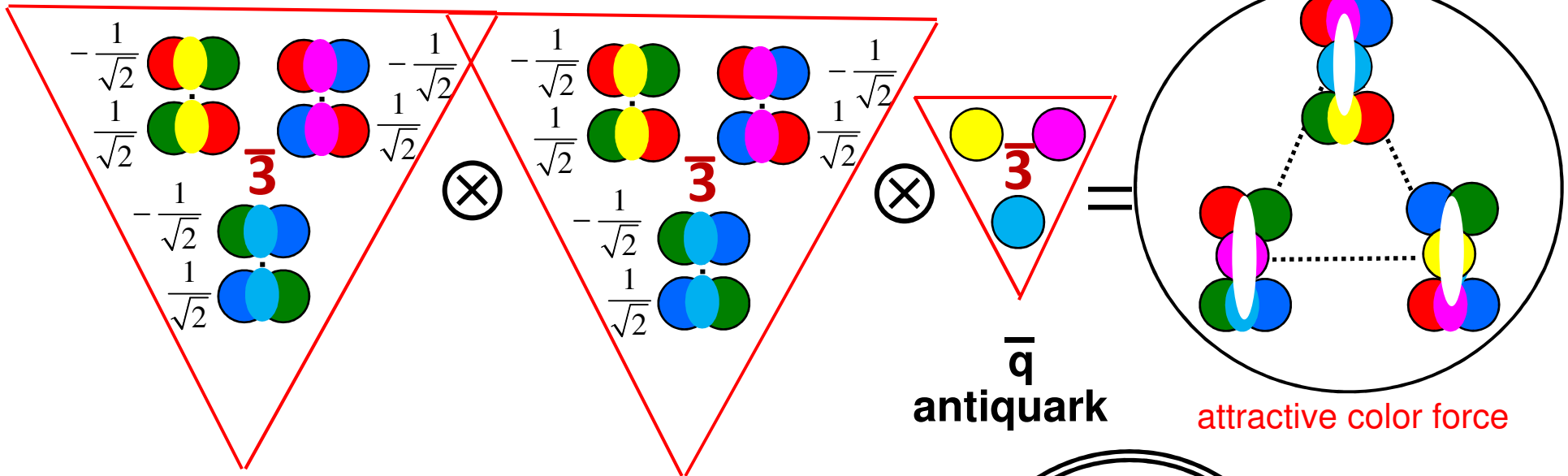


color antitriplet

color antitriplet

color antitriplet

color singlet



attractive color force  
**((qq) diquark**

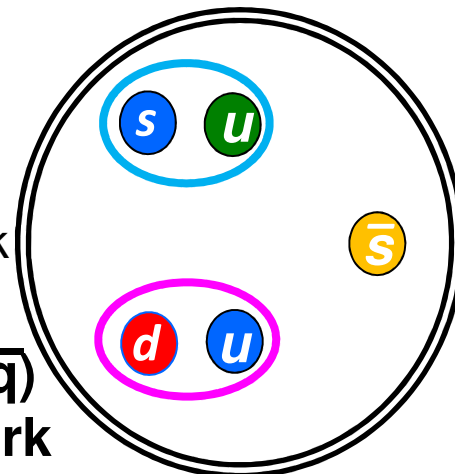
attractive color force  
**((qq) diquark**

**q**  
antiquark

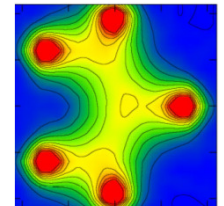
attractive color force

Different forms of quark configurations in a pentaquark can coexist. Modeling of pentaquarks is complicated.

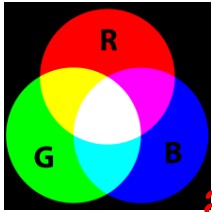
**((qq)(qq)q-bar)**  
pentaquark



Color flux tube stretched between the diquarks and antiquark



# Hexaquark directly from three diquarks

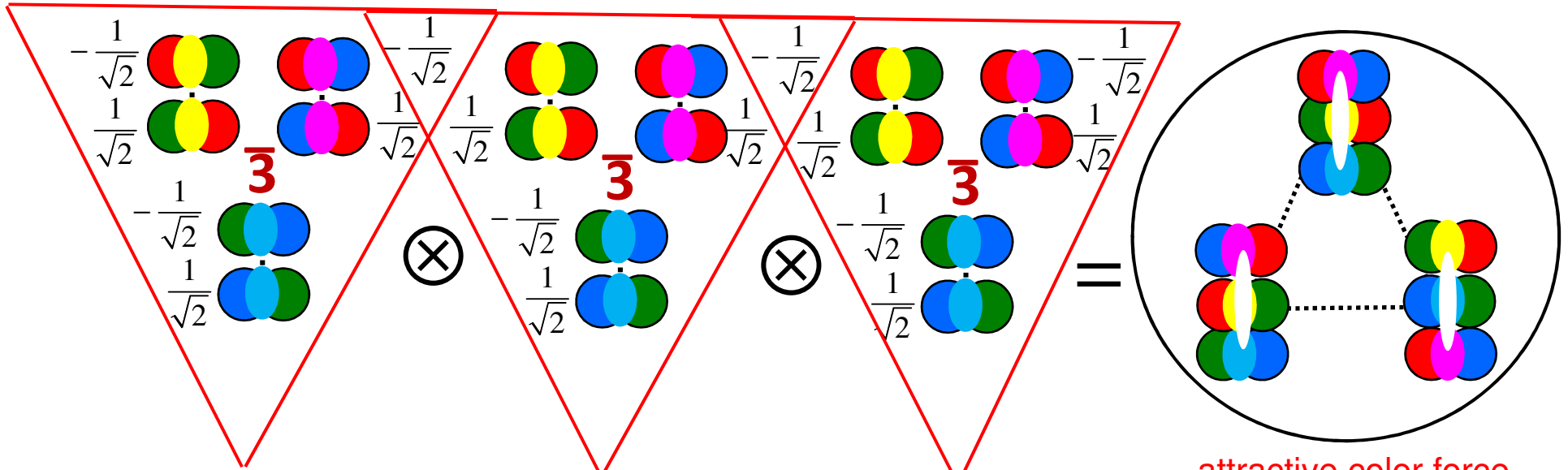


color  
antitriplet

color  
antitriplet

color  
antitriplet

color  
singlet



attractive  
color force

attractive  
color force

attractive  
color force

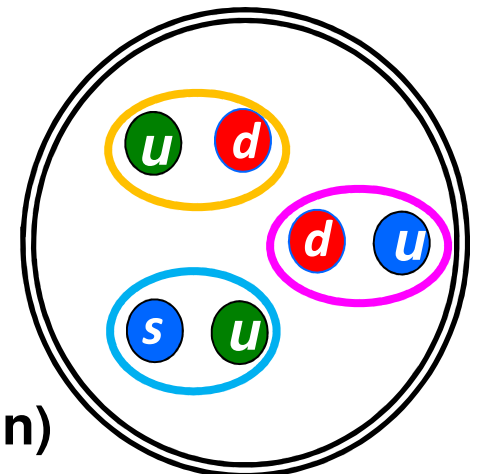
attractive color force

**((qq) diquark**

**((qq) diquark**

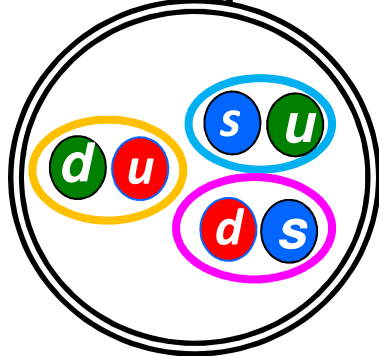
**((qq) diquark**

**((qq)(qq)(qq))  
hexaquark (dibaryon)**



# Tightly and loosely bound multiquark states

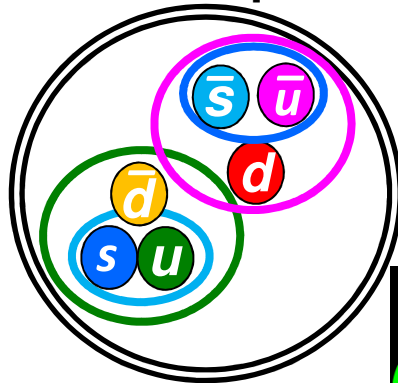
$((s\bar{q})(sq))(qq)$   
hexaquark



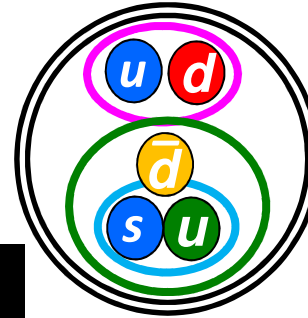
**dihyperon**

predicted by Jaffe to be stable  
PRL 38,195(1977)

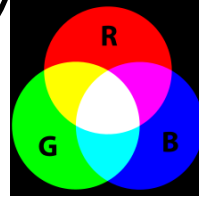
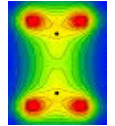
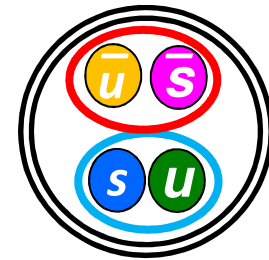
$((\bar{q}(sq))(q(\bar{s}\bar{q})))$   
hexaquark



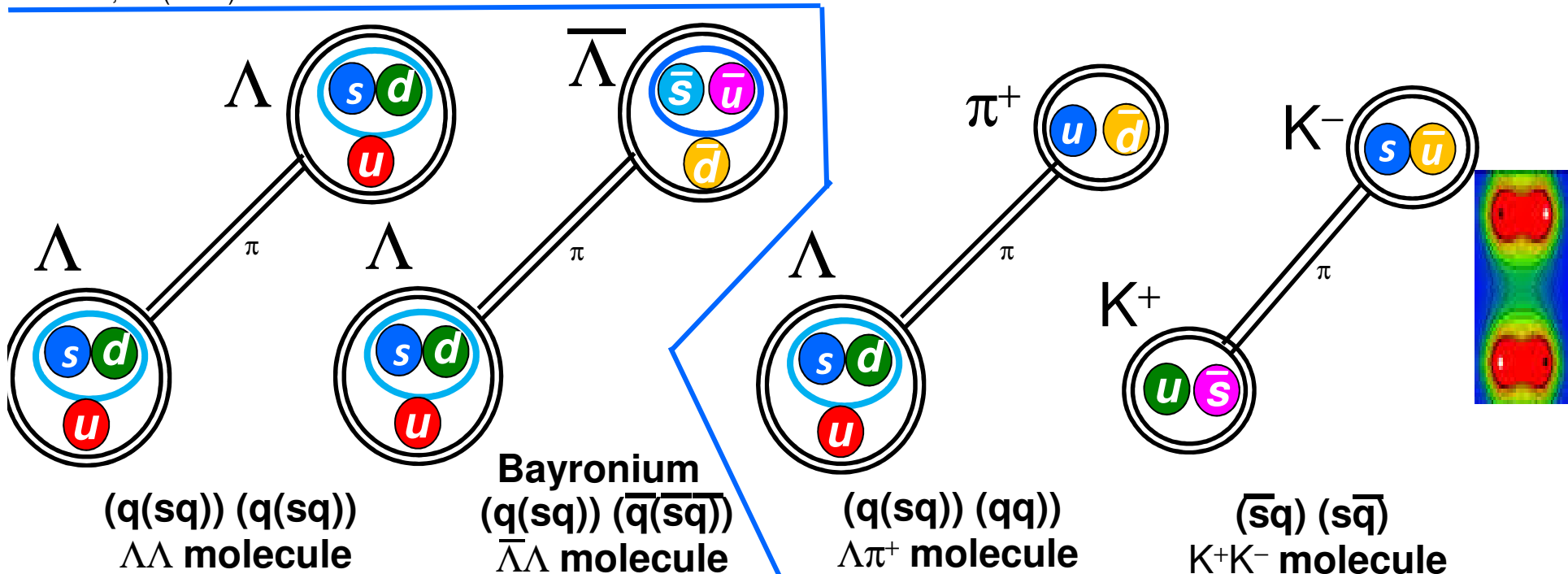
$((\bar{q}(sq))(qq))$   
pentaquark



$((\bar{s}\bar{q})(sq))$   
tetraquark



Any of these states would be considered an "exotic" hadron.

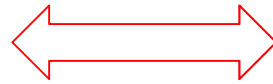
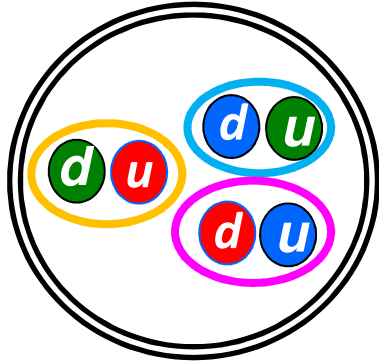




# Tightly versus loosely bound multiquark systems



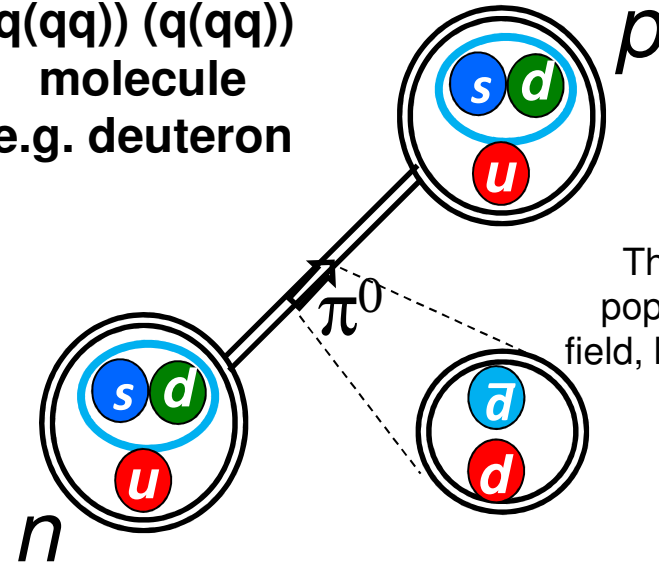
$((q\bar{q})(q\bar{q})(q\bar{q}))$   
hexaquark (dibaryon)



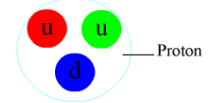
The same  
quark content

Quite different  
spectroscopy

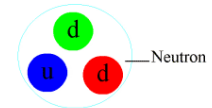
$(q(q\bar{q})) (q(q\bar{q}))$   
molecule  
e.g. deuteron



These quarks  
pop-out of gluon  
field, later annihilat



Proton

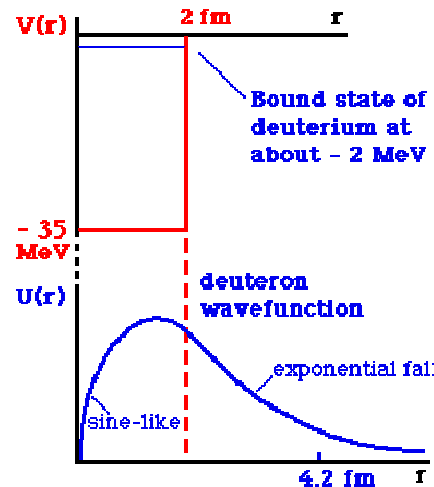


Neutron

Molecular forces can be described  
as exchange of a pion

- Rich excitation spectrum, in principle, possible:
  - $n, l, S$
  - hundreds of MeV in energy between different excitations
  - high  $\vec{J} = \vec{L} + \vec{S}$  values possible

Such structures may be extremely unstable (wide).  
No firm input from lattice QCD (yet) which, if any, multiquark structures form well defined bound states.



Difficult to get more than one state ( $n=1, l=0$ ).

$$M = M_1 + M_2 - (\text{a few MeV})$$

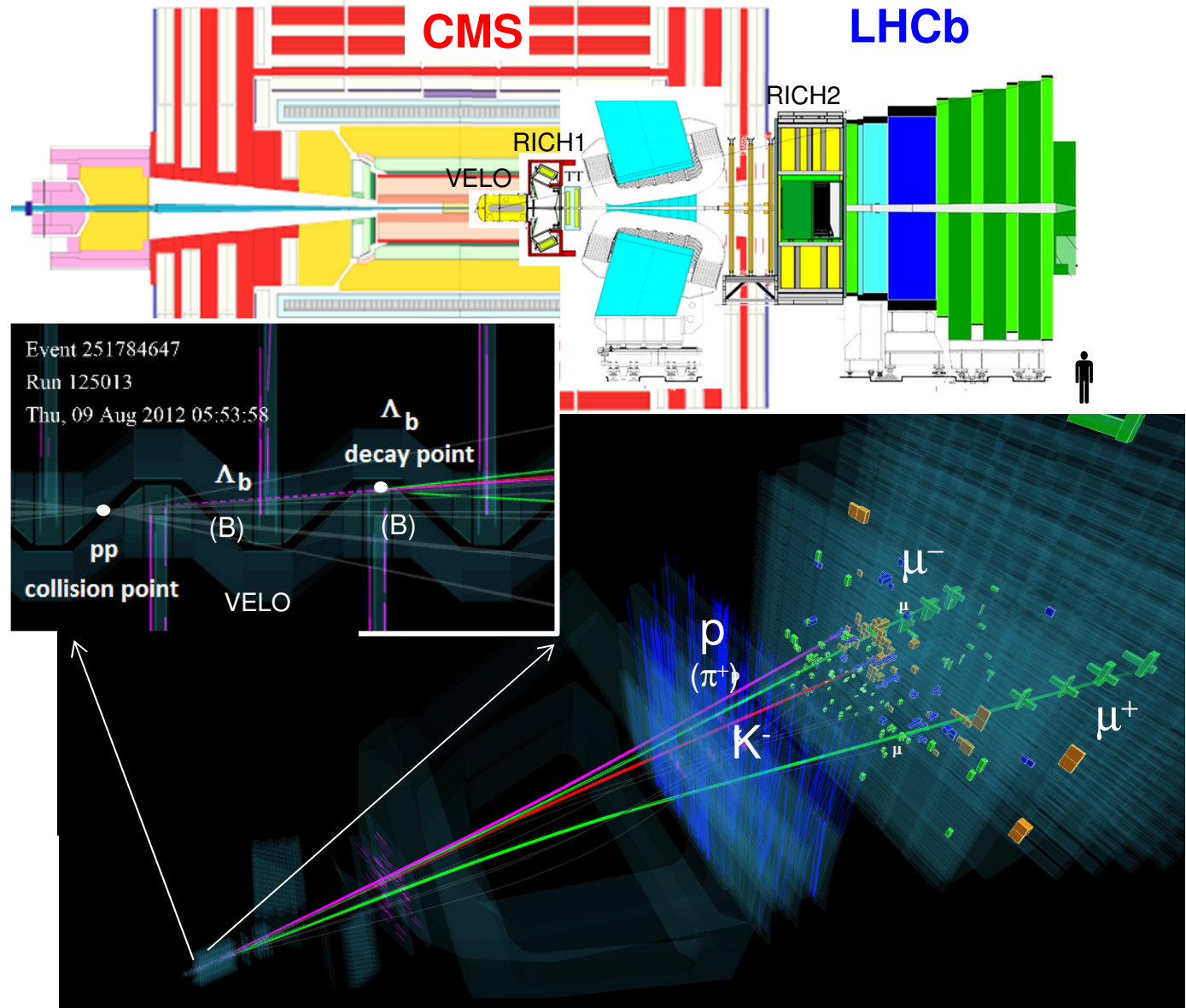
$$J^P = (J_1 \otimes J_2)^{P_1 P_2}$$

$$\Gamma \sim \max(\Gamma_1, \Gamma_2)$$

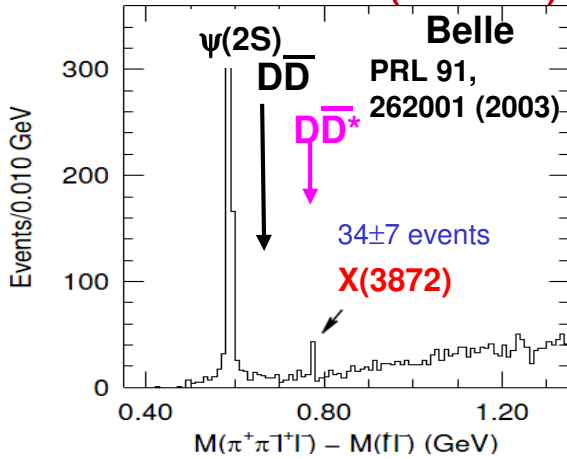


# LHCb: first dedicated b,c detector at hadronic collider

- Advantages over  $e^+e^-$  B-factories (Belle, BaBar):
  - ~1000x larger b production rate
  - **produce b-baryons at the same time as B-mesons**
  - long visible lifetime of b-hadrons (no backgrounds from the other b-hadron)
- Advantages over ATLAS, CMS, CDF, D0:
  - RICH detectors for  $\pi/K/p$  discrimination (smaller backgrounds)
  - Small event size allows large trigger bandwidth (up to 5 kHz in Run I); all devoted to flavor physics



# X(3872) – discovered in 2003

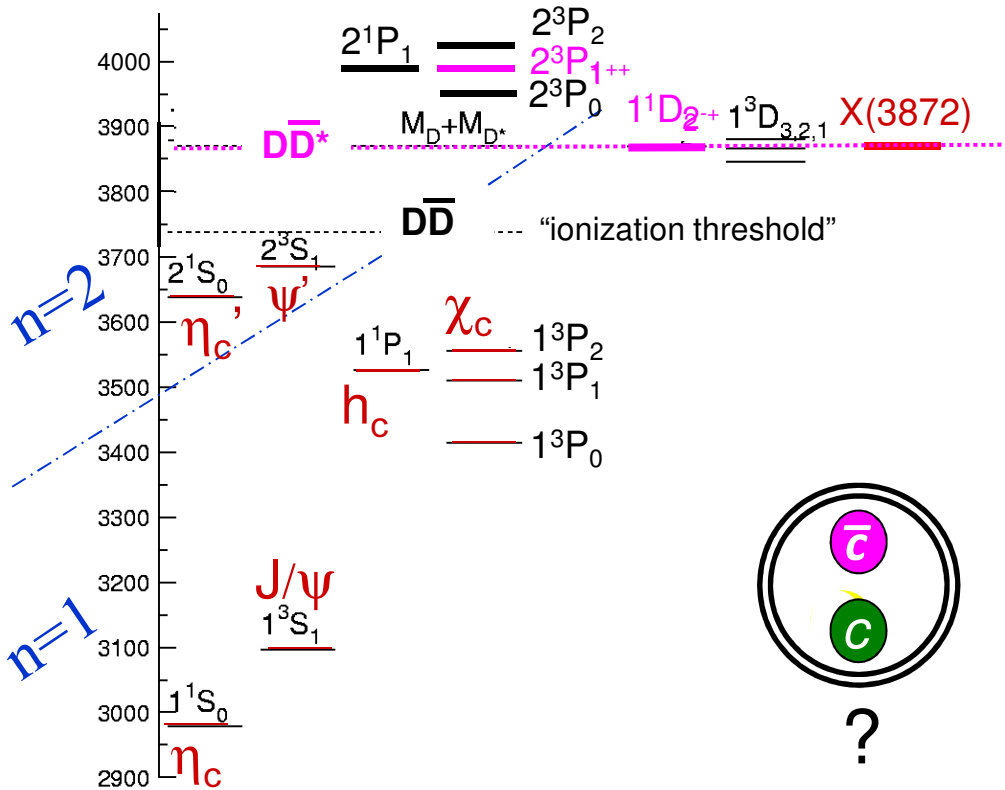
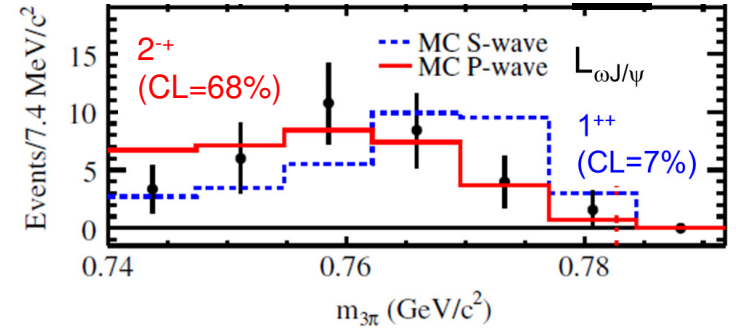


$B \rightarrow X(3872)K$ ,  
 $X(3872) \rightarrow J/\psi \rho^0$ , (isospin violating decays)  
 $\rho^0 \rightarrow \pi^+\pi^-$ ,  $J/\psi \rightarrow l^+l^-$

$\Gamma_{X(3872)} < 1.2$  MeV  
 very narrow

$B \rightarrow X(3872)K$ ,  
 $X(3872) \rightarrow J/\psi \omega$ ,  
 $\omega \rightarrow \pi^0 \pi^+ \pi^-$ ,  $J/\psi \rightarrow l^+ l^-$

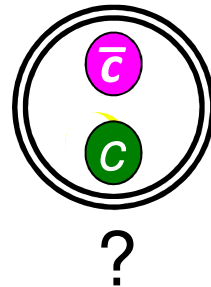
**BaBar**  
PR D82,  
011101 (2010)



“ionization threshold”  
 for states which cannot  
 decay to  $DD$ :  $1^{++}, 2^+$

$$M_{X(3872)} - [M_{D^0} + M_{D^{*0}}] = -0.11 \pm 0.19 \text{ MeV}$$

Mass indistinguishable  
 from  $D^0 \bar{D}^{*0}$  thresholds

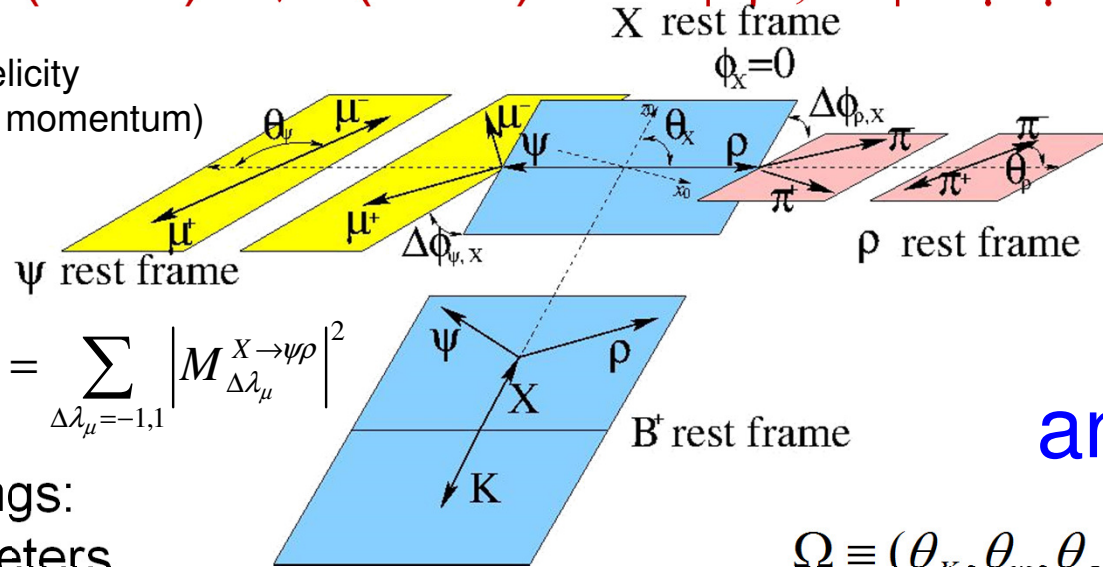


BaBar data preferred  $J^P=2^-$   
 (without ruling out  $1^{++}$ ) from the  
 shape of  $m_{3\pi}$  distribution  $\rightarrow$   
 $\eta(1^1D_2) c\bar{c}$  state?

# Helicity amplitudes for



λ – particle helicity  
(spin projection onto its momentum)



# 5D analysis

$$\left| M(\Omega | J_X, A_{\lambda_\psi, \lambda_\rho}^{J_X}) \right|^2 = \sum_{\Delta\lambda_\mu = -1, 1} \left| M_{\Delta\lambda_\mu}^{X \rightarrow \psi\rho} \right|^2$$

Helicity couplings:  
nuisance parameters

$$\Omega \equiv (\theta_X, \theta_\psi, \theta_\rho, \Delta\phi_{\psi, X}, \Delta\phi_{\rho, X})$$

$$M_{\Delta\lambda_\mu}^{X \rightarrow \psi\rho} = \sum_{\lambda_\psi = -1, 0, 1} \sum_{\lambda_\rho = -1, 0, 1} A_{\lambda_\psi, \lambda_\rho}^{J_X} D_{0, \lambda_\psi - \lambda_\rho}^{J_X}(0, \theta_X, 0)^* D_{\lambda_\psi, \Delta\lambda_\mu}^1(\Delta\phi_{\psi, X}, \theta_\psi, 0)^* D_{\lambda_\rho, 0}^1(\Delta\phi_{\rho, X}, \theta_\rho, 0)^*$$

$$A_{\lambda_\psi, \lambda_\rho}^{J_X} = \sum_L \sum_S B_{L, S}^{J_X} \begin{pmatrix} J_\psi & J_\rho & S \\ \lambda_\psi & -\lambda_\rho & \lambda_\psi - \lambda_\rho \end{pmatrix} \begin{pmatrix} L & S & J_X \\ 0 & \lambda_\psi - \lambda_\rho & \lambda_\psi - \lambda_\rho \end{pmatrix} \text{Clebsch-Gordan coefficients}$$

$$|J_\psi - J_\rho| \leq S \leq J_\psi + J_\rho$$

$$S = 0, 1, 2$$

$$|J_X - S| \leq L \leq J_X + S$$

$$P_X = P_\psi P_\rho (-1)^L = (-1)^L$$

(P-conservation  
since strong decay)

Number of  $B_{LS}$  coupling equals number of independent  $A_{\lambda_\psi, \lambda_\rho}$  couplings (1-5 depending on  $J_X$ ) – no gain, unless high  $L$  values neglected

# Determination of $J^{PC}$ for $X(3872)$

Belle 711 fb<sup>-1</sup>  
 173±16 events  
 PRD84(2011)052004

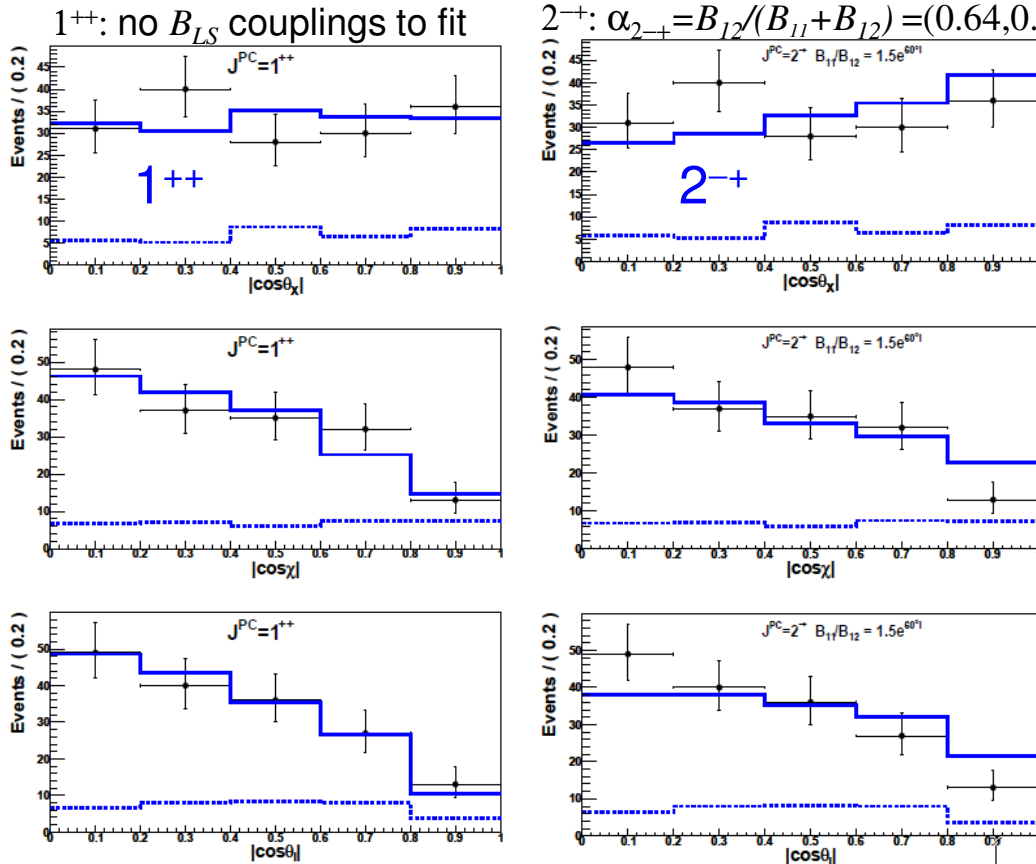
3 x 1D  $\chi^2$  analysis  
 ( $L=L_{min}$ )

LHCb 1 fb<sup>-1</sup> (2011 data)

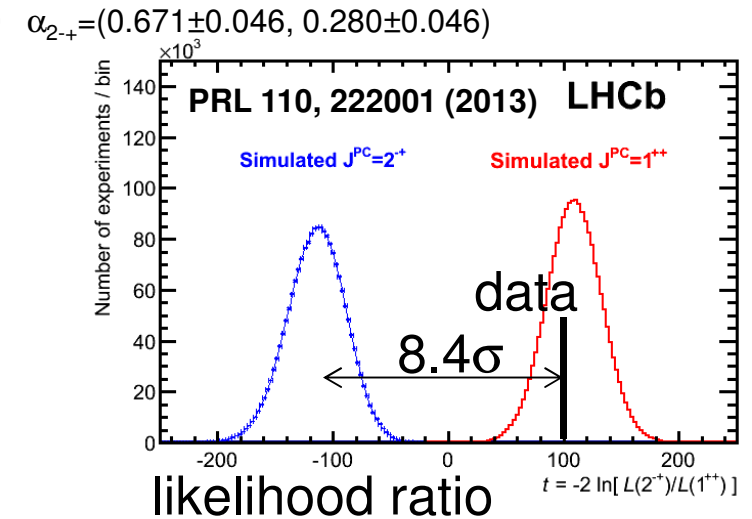
313±26 events

$\sqrt{313/173} = 1.3$  small gain is statistical errors

5D unbinned likelihood ratio analysis



Could not distinguish between  $1^{++}$  and  $2^{-+}$



Very clear separation between  $1^{++}$  and  $2^{-+}$   
 The data choose  $1^{++}$

- It is important to analyze data in all sensitive dimensions simultaneously. Angular correlations by far more powerful than 1D projections.

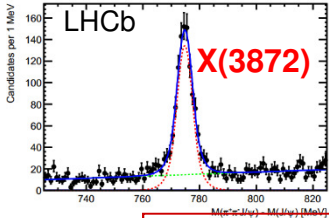
# 2015 update to X(3872) $J^{PC}$ determination

LHCb 3 fb<sup>-1</sup> (2011+2012 data)

1011±38 events

PRD92, 011102 (2015)

(all  $L$  values allowed)



LHCb 2015

Many more amplitudes to fit

$J^{PC}$	all $L$	minimal $L$
$0^{-+}$	$B_{11}$	$B_{11}$
$0^{++}$	$B_{00}, B_{22}$	$B_{00}$
$1^{-+}$	$B_{10}, B_{11}, B_{12}, B_{32}$	$B_{10}, B_{11}, B_{12}$
$1^{++}$	$B_{01}, B_{21}, B_{22}$	$B_{01}$
$2^{-+}$	$B_{11}, B_{12}, B_{31}, B_{32}$	$B_{11}, B_{12}$
$2^{++}$	$B_{02}, B_{20}, B_{21}, B_{22}, B_{42}$	$B_{02}$
$3^{-+}$	$B_{12}, B_{30}, B_{31}, B_{32}, B_{52}$	$B_{12}$
$3^{++}$	$B_{21}, B_{22}, B_{41}, B_{42}$	$B_{21}, B_{22}$
$4^{-+}$	$B_{31}, B_{32}, B_{51}, B_{52}$	$B_{31}, B_{32}$
$4^{++}$	$B_{22}, B_{40}, B_{41}, B_{42}, B_{62}$	$B_{22}$

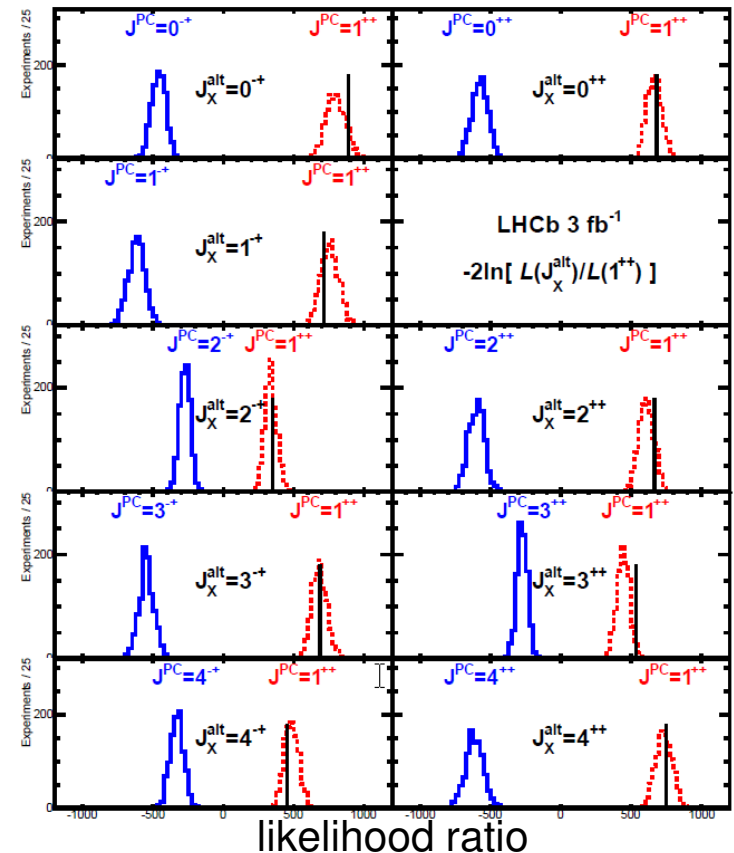
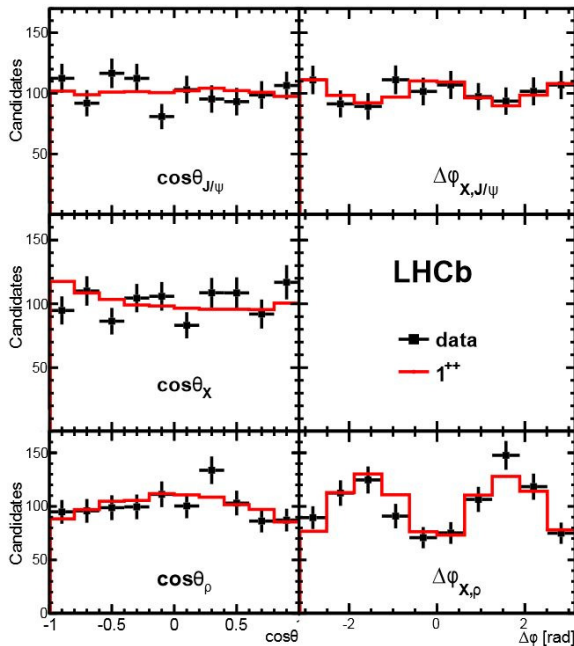
CDF 2007

LHCb 2013

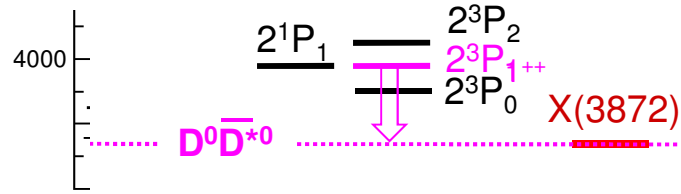
$J^{PC} = 1^{++}$  at  $16\sigma$

$$f_D = \frac{\int |\mathcal{M}(\Omega)_D|^2 d\Omega}{\int |\mathcal{M}(\Omega)_{S+D}|^2 d\Omega}$$

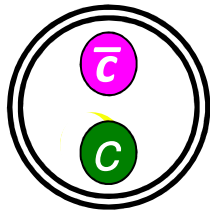
<4% at 95% CL



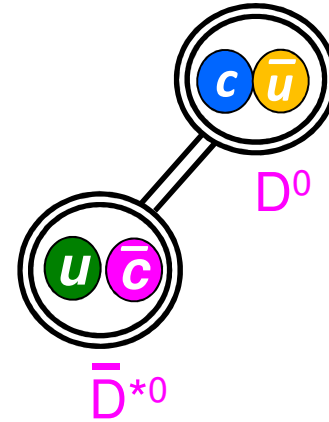
# X(3872) interpretation



$$M_{X(3872)} - [M_{D^0} + M_{D^{*0}}] = -0.11 \pm 0.19 \text{ MeV}$$



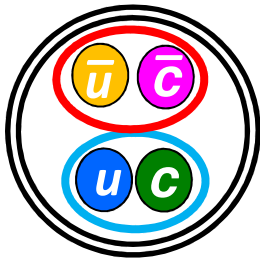
$\chi_c(2^3P_1)$  “attracted” by  $D^0 \bar{D}^{*0}$  threshold?



$L=0$

Meson-meson molecule?  
essentially no binding energy?

mixture?



tightly bound **tetraquark** “attracted” by  $D \bar{D}^*$  threshold ?

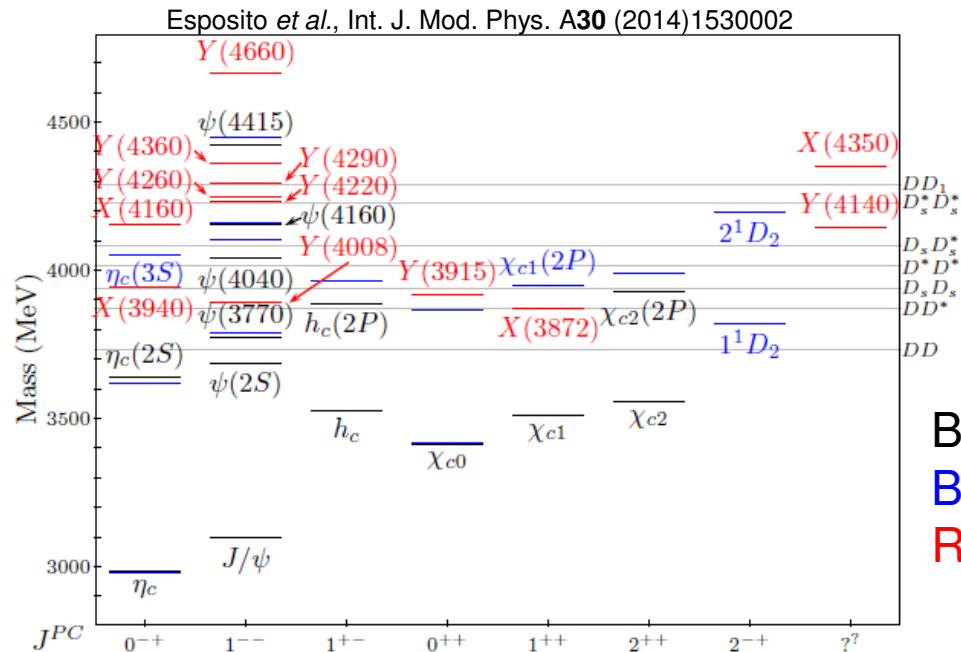
e.g. L. Maiani, F. Piccinini, A.D. Polosa, V. Riquer, PRD **89** (2014) 114010

$$[cu]_{S=1} [\bar{c}\bar{u}]_{S=0} + [cu]_{S=0} [\bar{c}\bar{u}]_{S=1}$$



# Growing XY zoo

- Many more neutral states at higher masses of the charmonium system have been discovered since then, which are candidates for exotic hadrons (none as narrow as X(3872))



Black: Observed conventional  $c\bar{c}$  states  
 Blue: Predicted conventional  $c\bar{c}$  states  
 Red: Exotic state candidates with  $c\bar{c}$  inside

- Many of them await experimental confirmation.
- Many of them discovered near  $D_{(s)}^{(*)}\bar{D}_{(s)}^{(*)}$  thresholds.
- No single model can explain all of them.

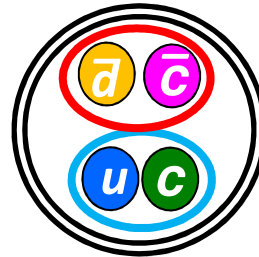
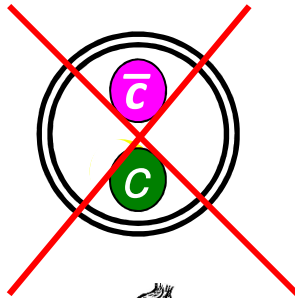
# Z(4430)<sup>+</sup> discovery and its importance

Phys.Rev.Lett. 100, 142001 (2008)

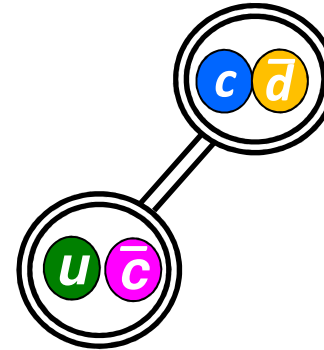
Observation of a resonance-like structure in the  $\pi^\pm\psi'$  mass distribution in exclusive  $B \rightarrow K\pi^\pm\psi'$  decays

The screenshot shows a web page from KEK (High Energy Accelerator Research Organization) dated November 13, 2007. The page title is "Belle Discovers a New Type of Meson". The header includes navigation links like "Press Release", "Top", "Access", "For Visitors", "Map & Guide", "Document", "Site Map", and "Search". The main content area is partially visible, showing the title and date.

neutral

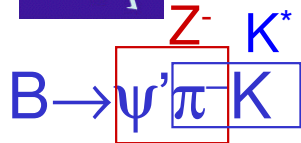


charged



**Z(4430)<sup>-</sup> previous measurements**

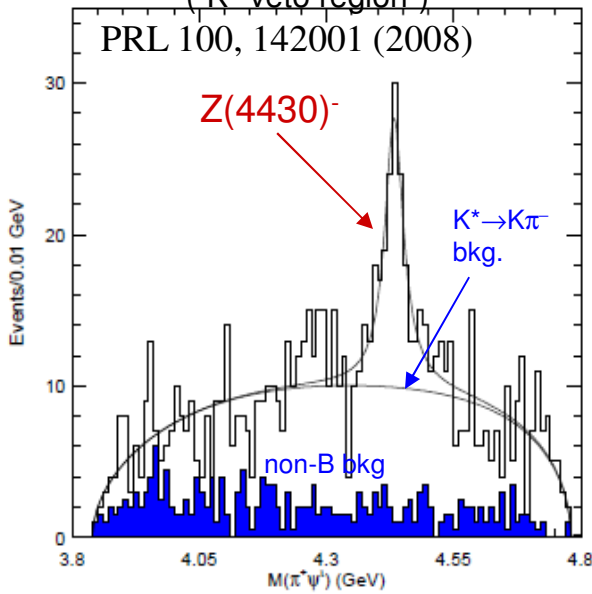
[  $\psi' \equiv \psi(2S)$  ]



**Belle 2008**

1D  $M(\psi'\pi^-)$  mass fit

("K\* veto region")



$M(Z) = 4433 \pm 4 \pm 2 \text{ MeV}$

$\Gamma(Z) = 45^{+18}_{-13} {}^{+30}_{-13} \text{ MeV}$

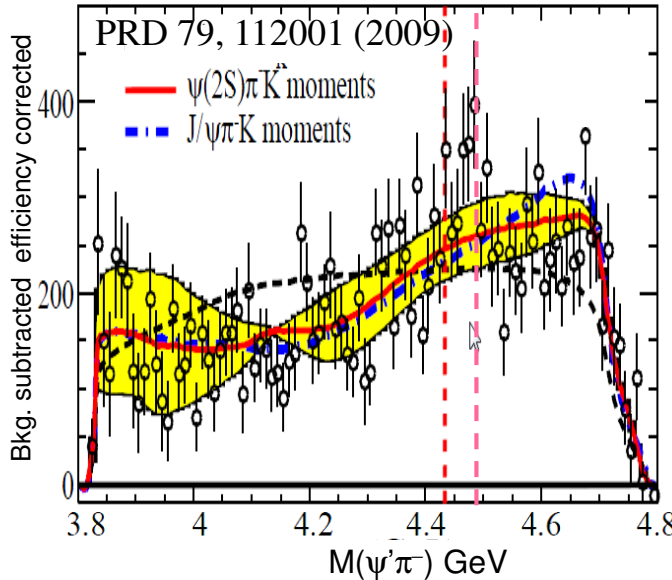
significance  $6.5\sigma$

Ad hoc assumption about the  $K^* \rightarrow K\pi^-$  background shape.

**BaBar 2009**

Harmonic moments of  $K^*$ s (2D) reflected to  $M(\psi'\pi^-)$

Belle 1D4D



BaBar did not confirm Z(4430)<sup>-</sup> in B sample comparable to Belle.

*Did not numerically contradict the Belle results.*

Almost **model independent** approach to  $K^* \rightarrow K\pi^-$  backgrounds.

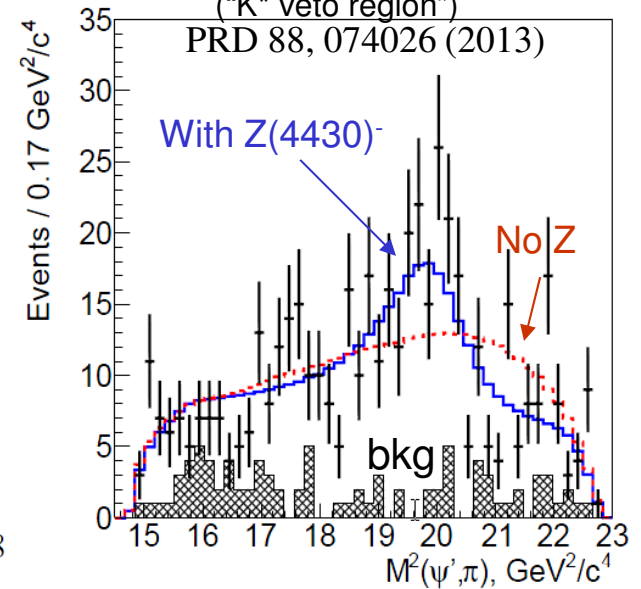
**Belle 2013**

(2D amplitude fit in 2009)

4D amplitude fit

(subsample with  $\psi' \rightarrow l^+l^-$ )

$0.996 \text{ GeV}/c^2 < M(K,\pi) < 1.332 \text{ GeV}/c^2$  ("K\* veto region")



$M(Z) = 4485^{+22}_{-22} {}^{+28}_{-11} \text{ MeV}$

$\Gamma(Z) = 200^{+41}_{-46} {}^{+26}_{-35} \text{ MeV}$

$6.4\sigma$  ( $5.6\sigma$  with sys.)

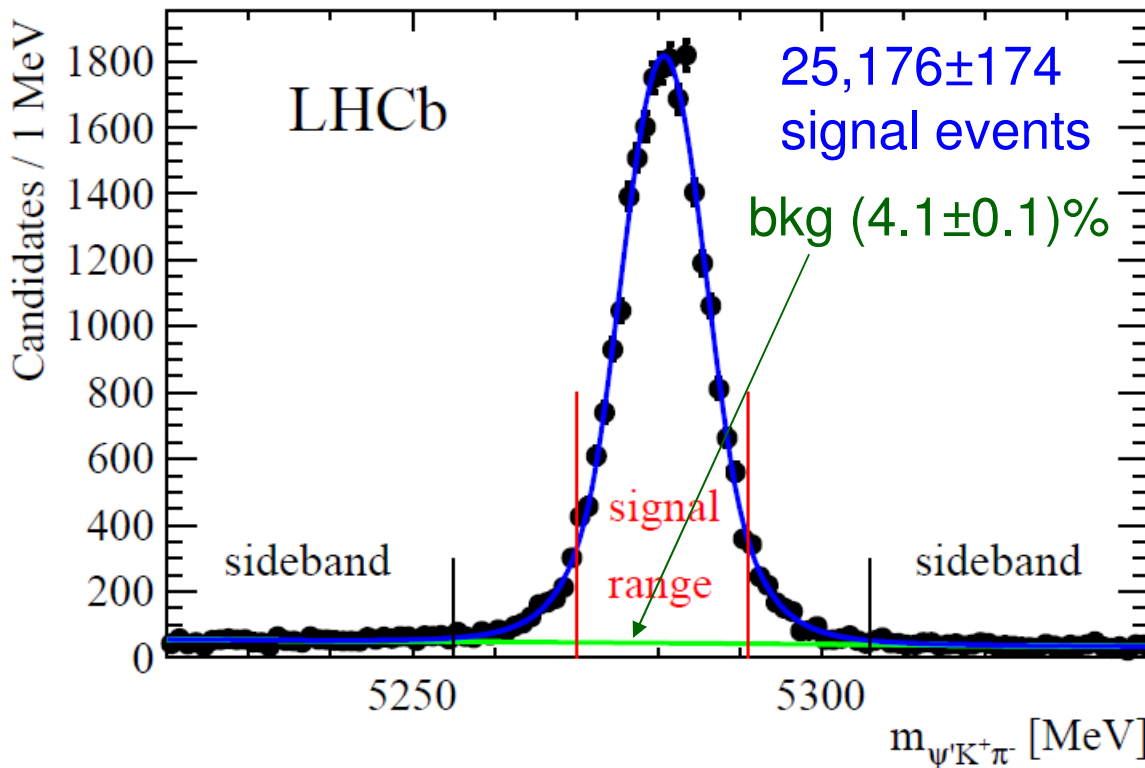
$J^P=1^+$  preferred by  $>3.4\sigma$

**Model dependent** approach to  $K^* \rightarrow K\pi^-$  backgrounds. Higher statistical sensitivity.

## Z(4430)<sup>+</sup> in LHCb

LHCb-PAPER-2014-014 PRL 112, 222002 (2014)

- $B^0 \rightarrow \psi' K^+ \pi^-$ ,  $\psi' \rightarrow \mu^+ \mu^-$  ( $3 \text{ fb}^{-1}$ )



vs

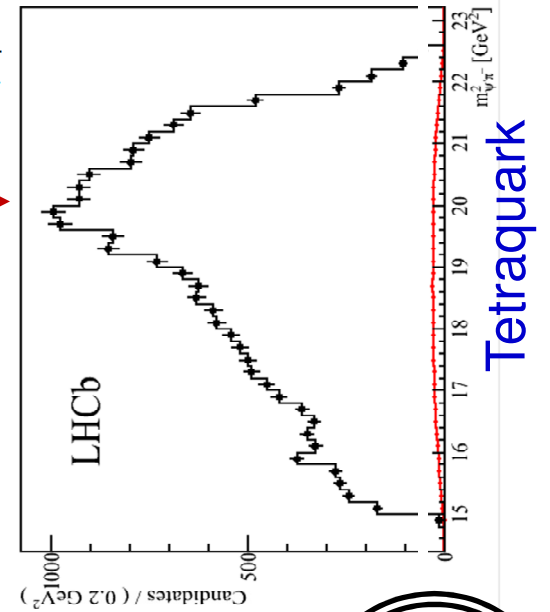
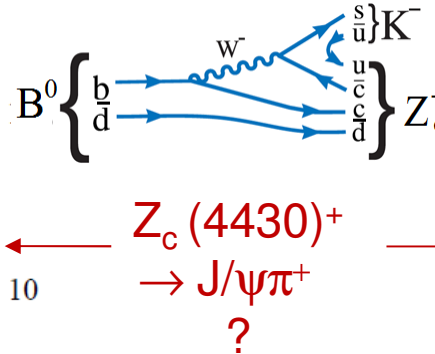
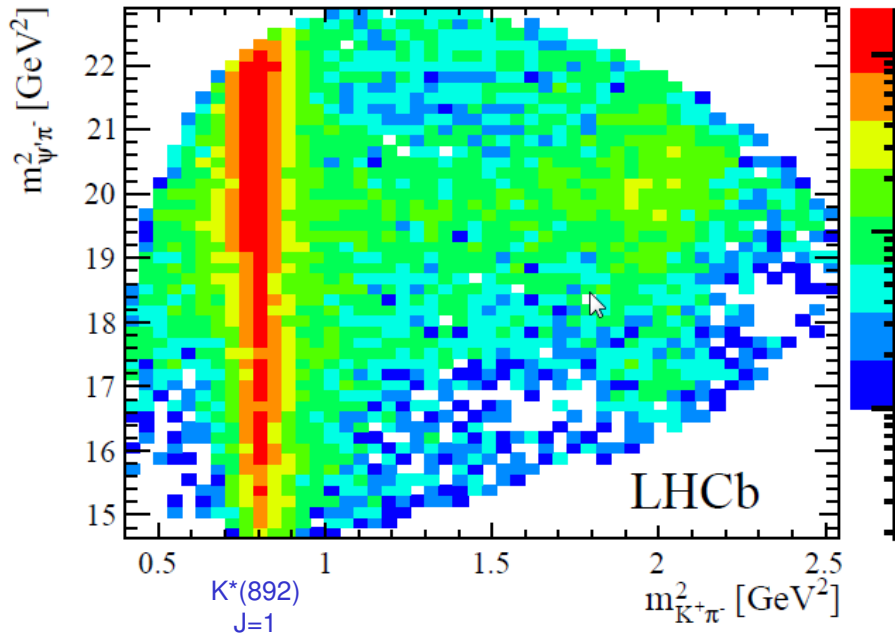
*Belle*:  $2,010 \pm 50$

*BaBar*:  $2,021 \pm 53$

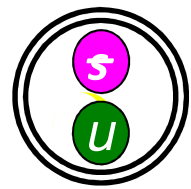
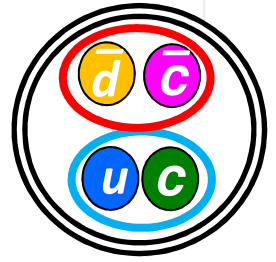
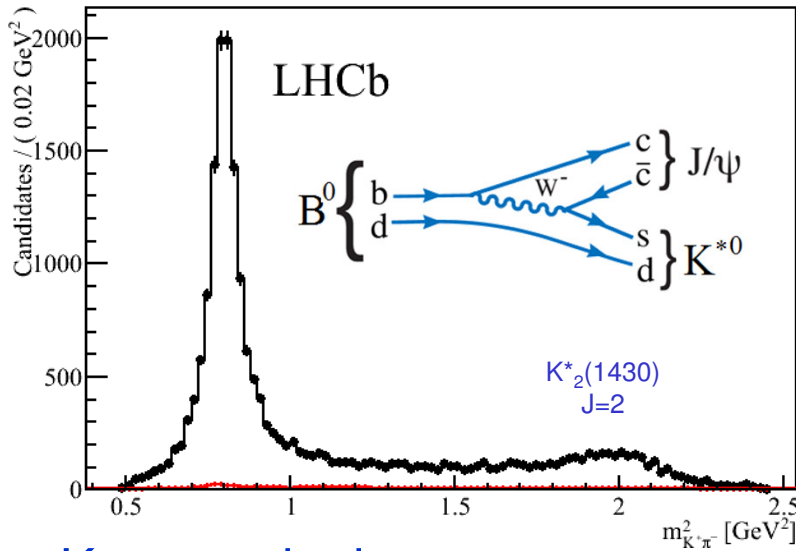
vs. bkg in *Belle*: 7.8%

An order of magnitude larger signal statistics than in Belle or BaBar thanks to hadronic production of b-quarks at LHC.

Even smaller non-B background than at the  $e^+e^-$  experiments thanks to excellent performance of the LHCb detector (vertexing, PID)



Tetraquark



Kaon excitations

Is it a reflection of interfering  $K^*$ 's  $\rightarrow \pi^+ K^-$  ?  
 Proper amplitude analysis necessary to check

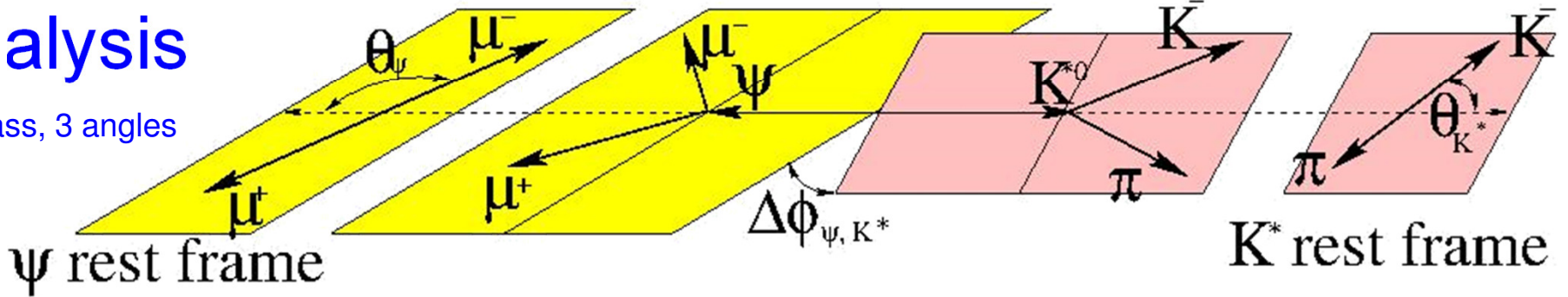
# Amplitude Analysis of $B^0 \rightarrow \psi' \pi^+ K^-$ , $\psi' \rightarrow \mu^+ \mu^-$

$$\left| M(m_{K\pi}, \Omega | A_{\lambda_\psi}^{B \rightarrow \psi K_n^*}) \right|^2 = \sum_{\Delta\lambda_\mu = -1, 1} \left| M_{\Delta\lambda_\mu}^{K^*} \right|^2$$

$\Omega \equiv (\theta_{K^*}, \theta_\psi, \Delta\phi_{\psi, K^*})$   $B^0$  rest frame

## 4D analysis

1 mass, 3 angles



$$M_{\Delta\lambda_\mu}^{K^*} = \sum_n \sum_{\lambda_\psi = -1, 0, 1} A_{\lambda_\psi}^{B \rightarrow \psi K_n^*} D_{\lambda_\psi, 0}^{J_{K^*}}(0, \theta_{K^*}, 0)^* R(m_{K\pi} | M_{K_n^*}, \Gamma_{K_n^*}) D_{\lambda_\psi, \Delta\lambda_\mu}^1(\Delta\phi_{\psi, K^*}, \theta_\psi, 0)^*$$

1-3 independent **complex** helicity couplings per  $K_n^*$  resonance

Breit-Wigner amplitude:

$$R(m | M_x, \Gamma_x) = \frac{B_{L_b}^i(p, p_0, d) \left(\frac{p}{M_B}\right)^{L_b} B_{L_x}^i(q, q_0, d) \left(\frac{q}{m}\right)^{L_x}}{M_x^2 - m^2 - iM_x \Gamma(m)} \quad \Gamma(m) = \Gamma_x \left(\frac{q}{q_0}\right)^{2L_x+1} \frac{M_x}{m} B_{L_x}^i(q, q_0, d)^2$$

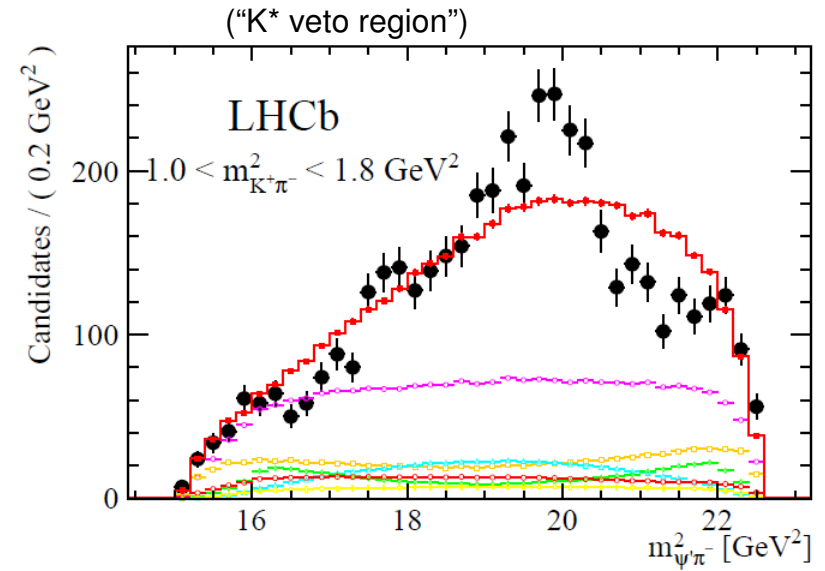
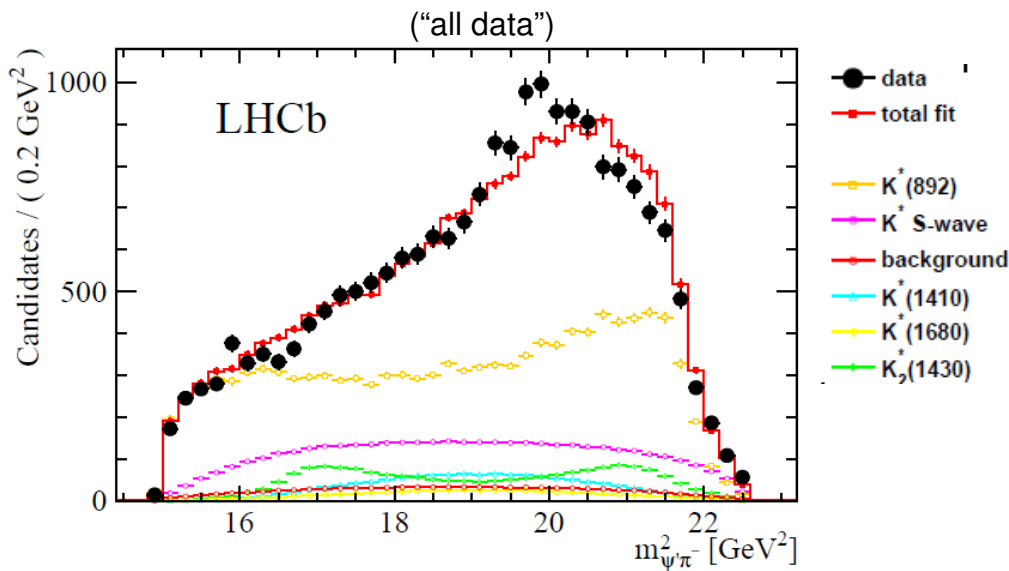
Blatt-Weisskopf functions

$n = 0^+ : K_0^*(800), K_0^*(1430), NR; \quad 1^- : K^*(892), K^*(1410), K^*(1680) \quad 2^+ : K_2^*(1430) \quad (3^- : K_3^*(1780))$

# of fit parameters: **32**

# Amplitude fits without $Z(4430)^-$

# of fit parameters: 32



- The  $\chi^2$  p-value  $< 2 \times 10^{-6}$



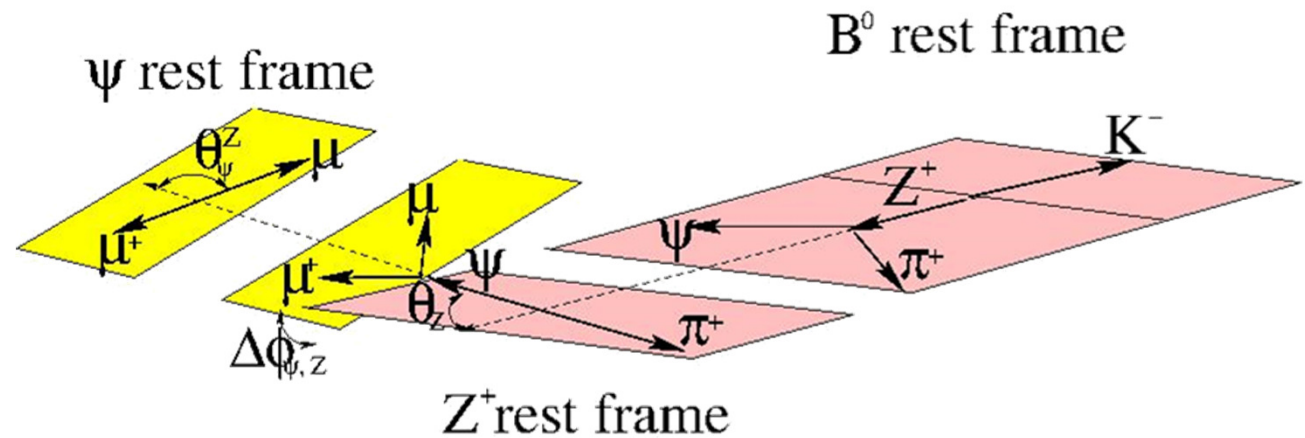
- The data cannot be adequately described with the  $J \leq 3$   $K^*$  contributions alone

# Amplitude Analysis of $B^0 \rightarrow \psi' \pi^+ K^-$ , $\psi' \rightarrow \mu^+ \mu^-$

$$\left| M(m_{K\pi}, \Omega \mid M_Z, \Gamma_Z, J_Z, A_{\lambda_\psi}^{Z \rightarrow \psi\pi}, A_{\lambda_\psi}^{B \rightarrow \psi K^*}) \right|^2 = \sum_{\Delta\lambda_\mu = -1, 1} \left| M_{\Delta\lambda_\mu}^{K^*} + e^{i\Delta\lambda_\mu \alpha_\mu} M_{\Delta\lambda_\mu}^Z \right|^2$$

## 4D analysis

1 mass, 3 angles  
all derivable from the  $K^*$  variables



$$M_{\Delta\lambda_\mu}^Z = \sum_{\lambda_\psi = -1, 0, 1} A_{\lambda_\psi}^{Z \rightarrow \psi\pi} D_{\lambda_\psi, \lambda_\psi}^{J_Z}(0, \theta_Z, 0)^* R(m_{\psi\pi} \mid M_Z, \Gamma_Z) D_{\lambda_\psi, \Delta\lambda_\mu}^1(\Delta\phi_{\psi, Z}, \theta_\psi^Z, 0)^*$$

1 independent **complex** helicity coupling after  $L=L_{min}$

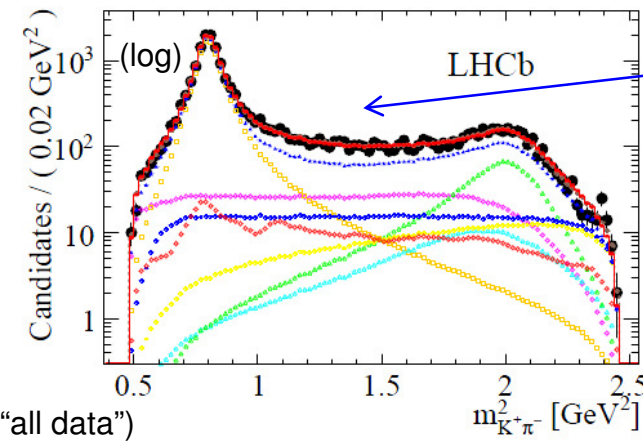
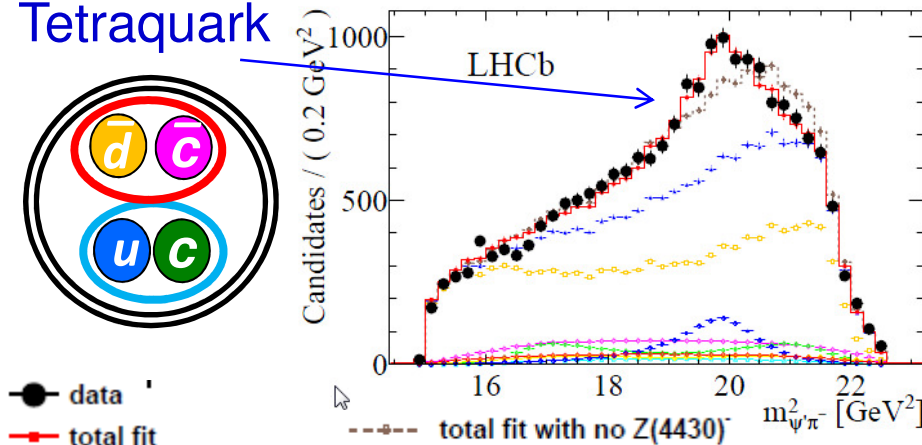
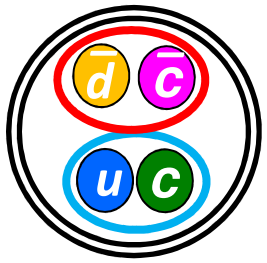
# of fit parameters: 32 + 4 = 36



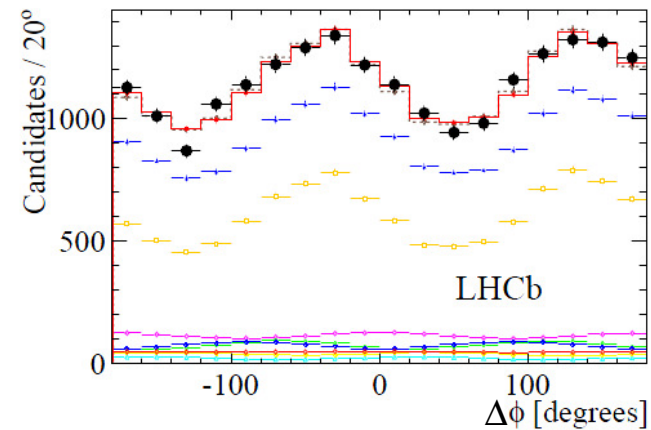
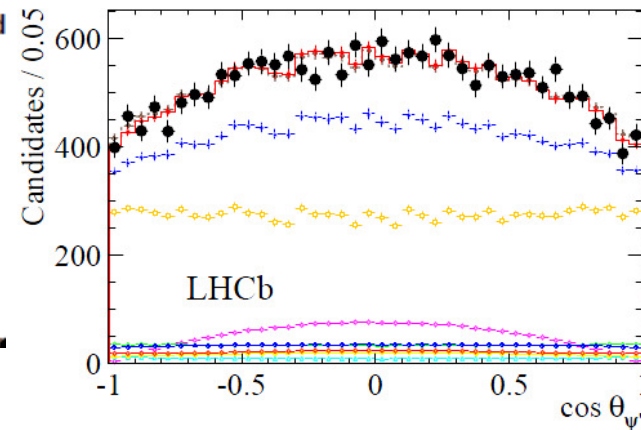
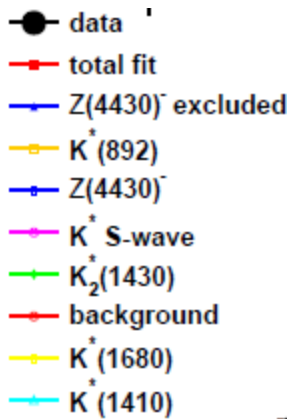
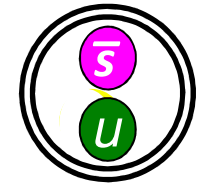
# Amplitude fits with $J^P=1^+$ $Z(4430)^+$

# of fit parameters:  $32 + 4 = 36$

Tetraquark



Kaon excitations

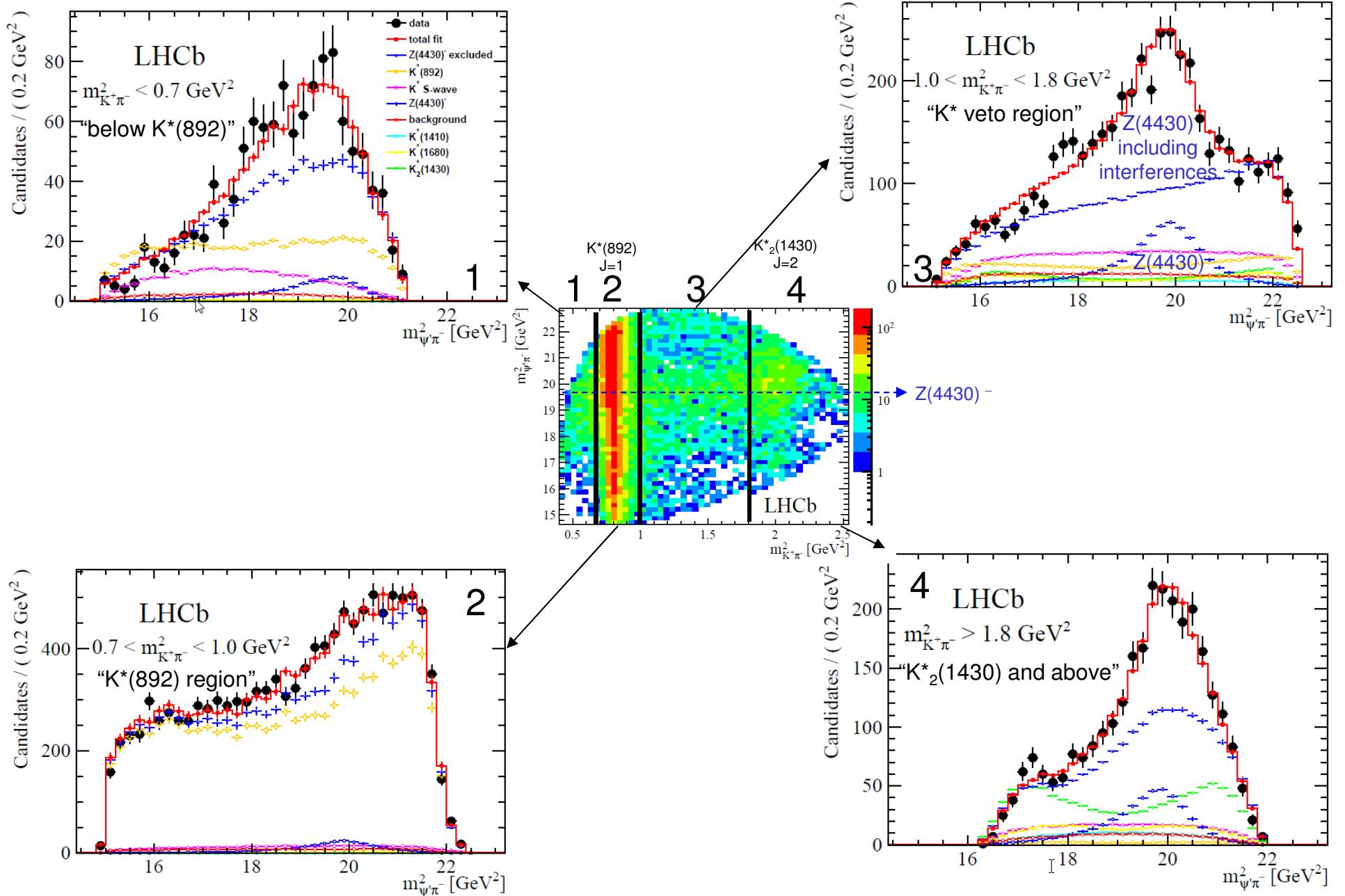


- The  $\chi^2$  p-value = 12%



- The data are well described when  $J^P=1^+$   $Z(4430)^+$  is included in the fit
- $Z(4430)^+$  significances from  $\Delta(-2\ln L)$  is  $18.7\sigma$  ( $13.9\sigma$  with systematic variations)

# Amplitude fits with $J^P=1^+$ $Z(4430)^-$



## Z(4430)<sup>-</sup> parameters: LHCb vs Belle

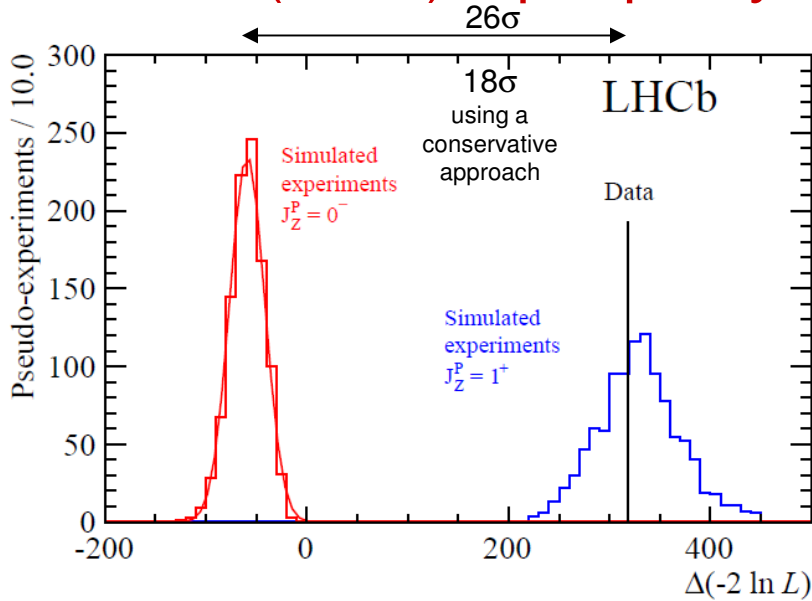
	LHCb	Belle	Amplitude fractions [%] (statistical errors only)	
			Contribution	
$M(Z)$ [MeV]	$4475 \pm 7_{-25}^{+15}$	$4485 \pm 22_{-11}^{+28}$	$S$ -wave total	$10.8 \pm 1.3$
$\Gamma(Z)$ [MeV]	$172 \pm 13_{-34}^{+37}$	$200_{-46-35}^{+41+26}$	NR	$0.3 \pm 0.8$
$f_Z$ [%]	$5.9 \pm 0.9_{-3.3}^{+1.5}$	$10.3_{-3.5-2.3}^{+3.0+4.3}$	$K_0^*(800)$	$3.2 \pm 2.2$ $5.8 \pm 2.1$
$f_Z^I$ [%] (with interferences)	$16.7 \pm 1.6_{-5.2}^{+2.6}$		$K_0^*(1430)$	$3.6 \pm 1.1$ $1.1 \pm 1.4$
Significance	$> 13.9\sigma$	$> 5.2\sigma$	$K^*(892)$	$59.1 \pm 0.9$ $63.8 \pm 2.6$
			$K_2^*(1430)$	$7.0 \pm 0.4$ $4.5 \pm 1.0$
			$K_1^*(1410)$	$1.7 \pm 0.8$ $4.3 \pm 2.3$
			$K_1^*(1680)$	$4.0 \pm 1.5$ $4.4 \pm 1.9$
			Z(4430) <sup>-</sup>	$5.9 \pm 0.9$ $10.3_{-3.5}^{+3.0}$

(new large systematic effect included by LHCb)

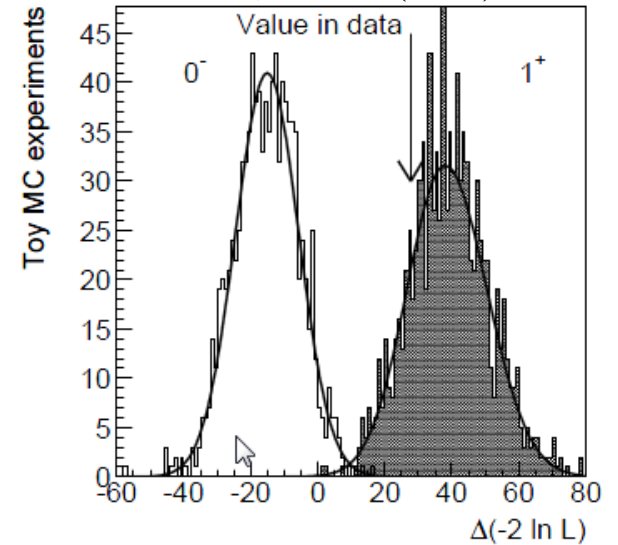
(not in the default fit  $K_3^*(1780)$   $0.5 \pm 0.2$  )

- Overall excellent consistency between LHCb and Belle
- Errors substantially improved

# Z(4430)<sup>+</sup> spin-parity analysis



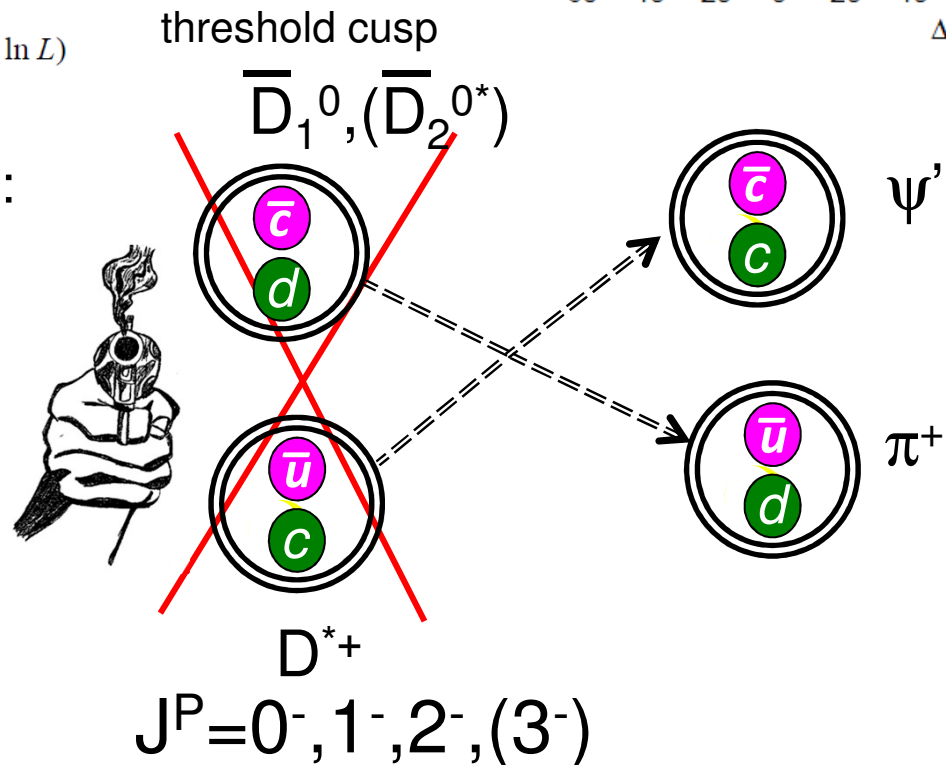
Belle  
PRD 88, 074026 (2013)



Including systematic variations:

Disfavored $J^P$	Rejection level relative to $1^+$	
	LHCb	Belle
$0^-$	$9.7\sigma$	$3.4\sigma$
$1^-$	$15.8\sigma$	$3.7\sigma$
$2^+$	$16.1\sigma$	$5.1\sigma$
$2^-$	$14.6\sigma$	$4.7\sigma$

- $J^P=1^+$  now established beyond any doubt



# Hadronic resonances – Argand diagram

Forced harmonic oscillator:

$$m \frac{d}{dt} \left( \frac{dx}{dt} \right) = -kx$$

Restoring force

Damping force:

$$-b \frac{dx}{dt}$$

$$-F_0 \cos(\omega_{\text{ext}} t)$$

Driving force

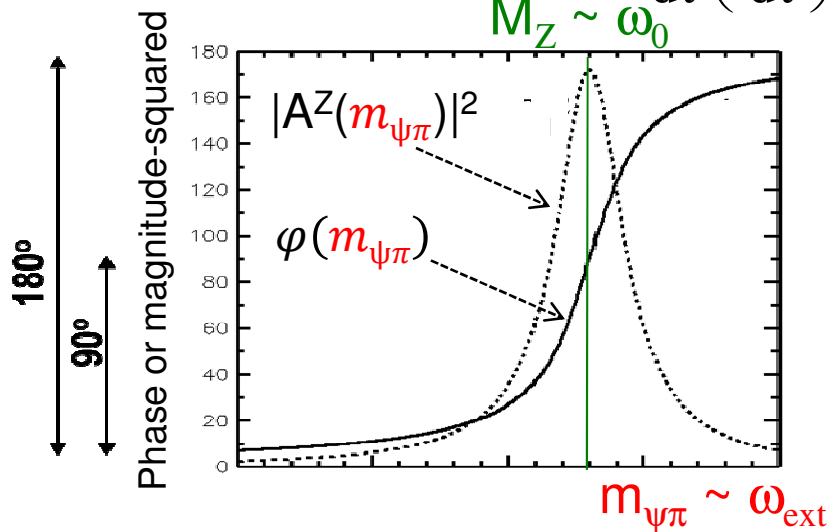
resonant frequency:  $\omega_0 = \sqrt{\frac{k}{m}}$

damping factor:  $\gamma = \frac{b}{2m}$

driving frequency  $\omega_{\text{ext}}$   
phase lag  $\phi$

$$x(t) \xrightarrow{t \rightarrow \infty} \frac{F_0 / m}{\sqrt{(\omega_0^2 - \omega_{\text{ext}}^2)^2 + (2\gamma\omega_{\text{ext}})^2}} \cos(\omega_{\text{ext}} t + \phi)$$

$$\phi = \text{atan} \left( \frac{2\gamma\omega_{\text{ext}}}{\omega_0^2 - \omega_{\text{ext}}^2} \right)$$



DEMO

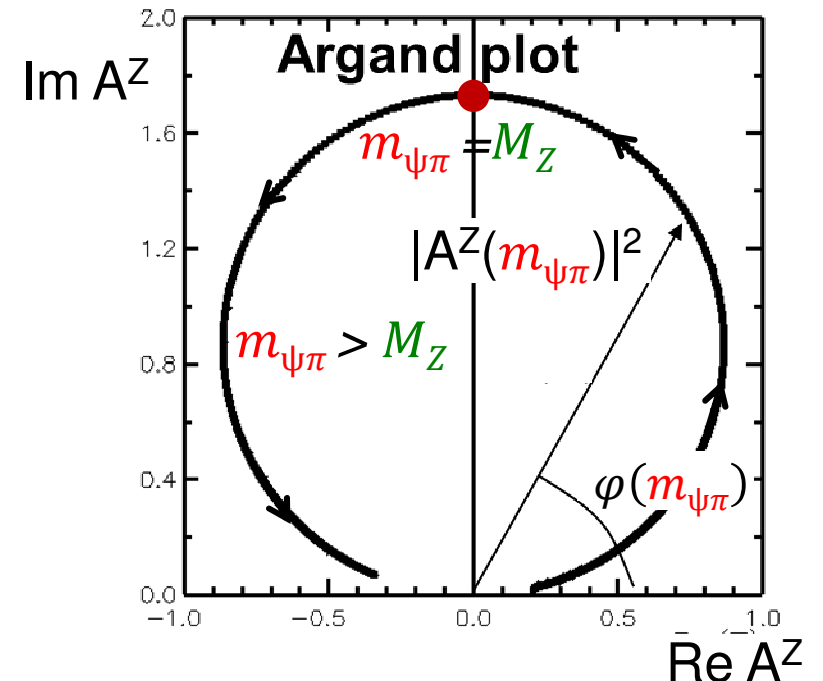
$$A^Z(m_{\psi\pi}) \sim \frac{1}{M_Z^2 - m_{\psi\pi}^2 - i M_Z \Gamma_Z} = |A^Z(m_{\psi\pi})| e^{i\phi(m_{\psi\pi})}$$

$$|A^Z(m_{\psi\pi})|^2 \sim \frac{1}{(M_Z^2 - m_{\psi\pi}^2)^2 + (M_Z \Gamma_Z)^2}$$

$$\phi(m_{\psi\pi}) = \text{atan} \left( \frac{M_Z \Gamma_Z}{M_Z^2 - m_{\psi\pi}^2} \right)$$

Breit-Wigner amplitude

- $m_{\psi\pi} \sim \omega_{\text{ext}}$  driving frequency
- $M_Z \sim \omega_0$  resonance frequency
- $\Gamma_Z = \hbar / \tau_Z \sim \gamma/2$  dumping factor (mass indeterminacy)

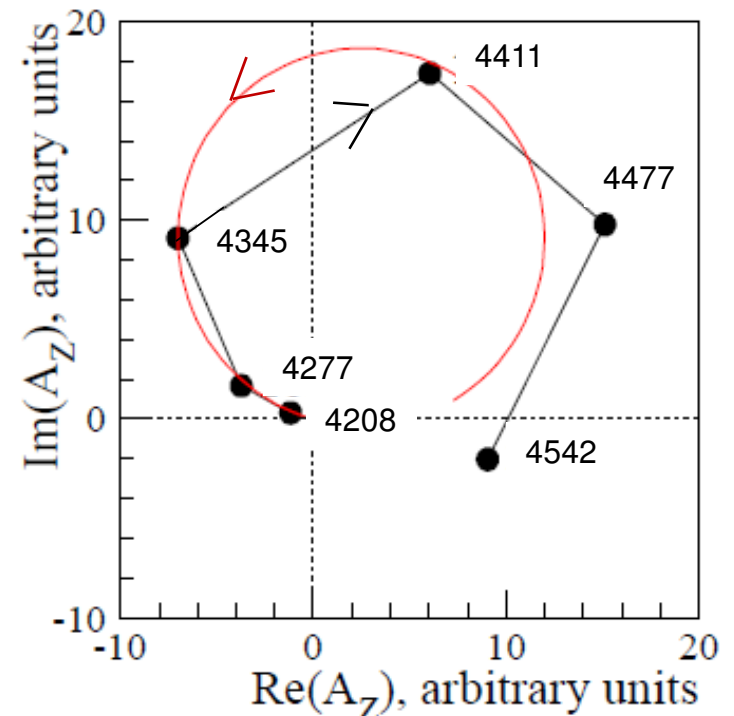
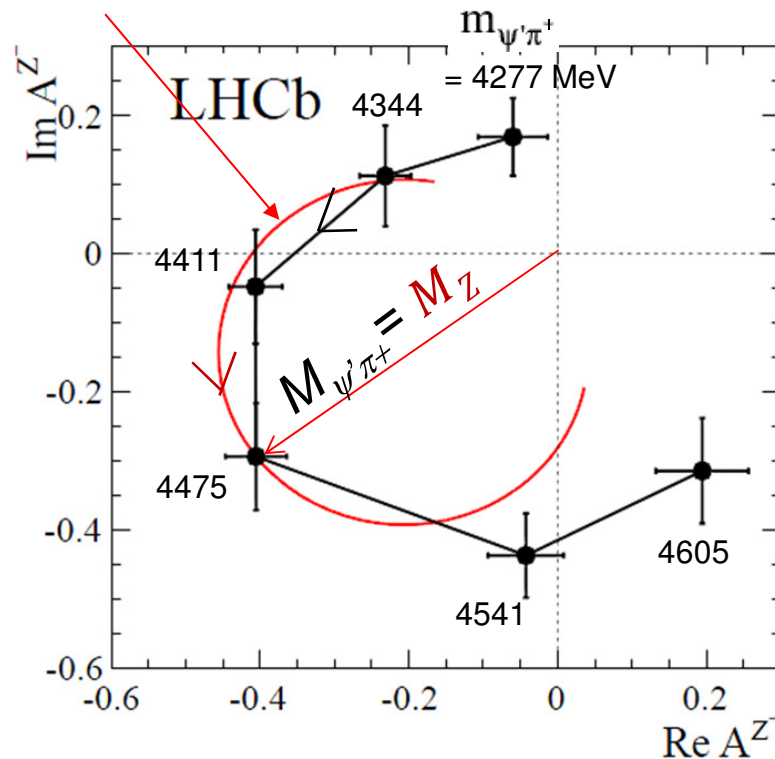
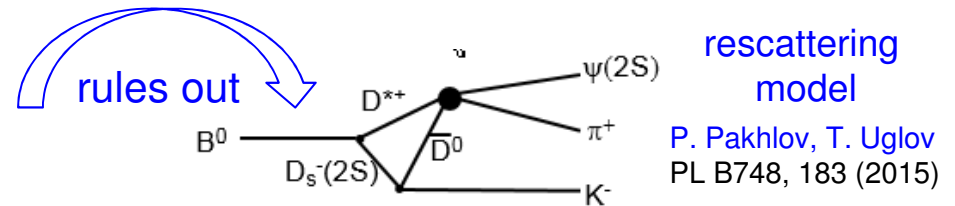


# Argand diagram of $Z(4430)^+$

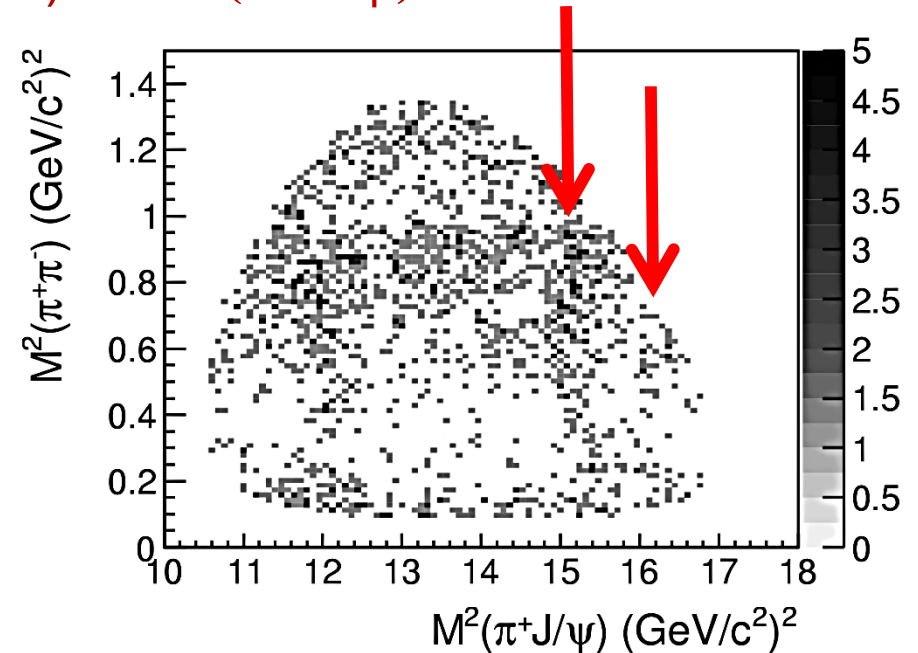
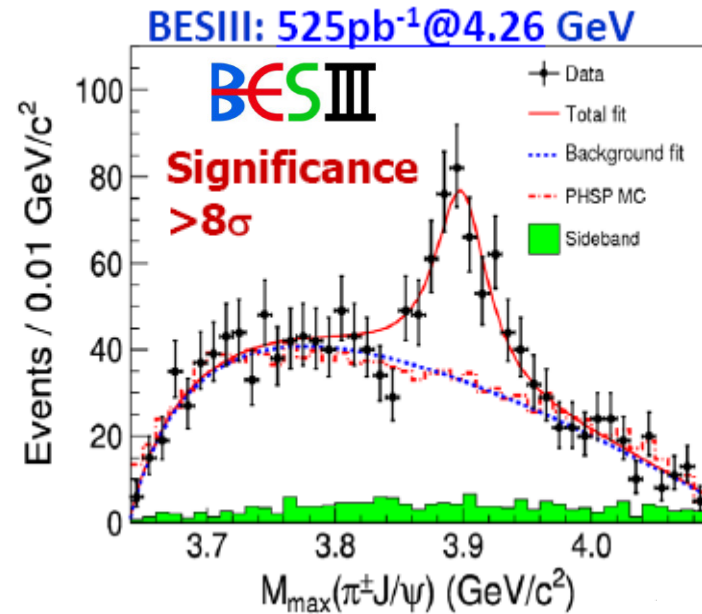
- Thanks to the large data statistics LHCb has been able to extract Argand diagram of  $Z(4430)^+$  amplitude from its interference with the  $K^*$  amplitudes:

$$\frac{1}{M_Z^2 - m_{\psi'\pi^+}^2 - i M_Z \Gamma_Z}$$

Breit-Wigner amplitude



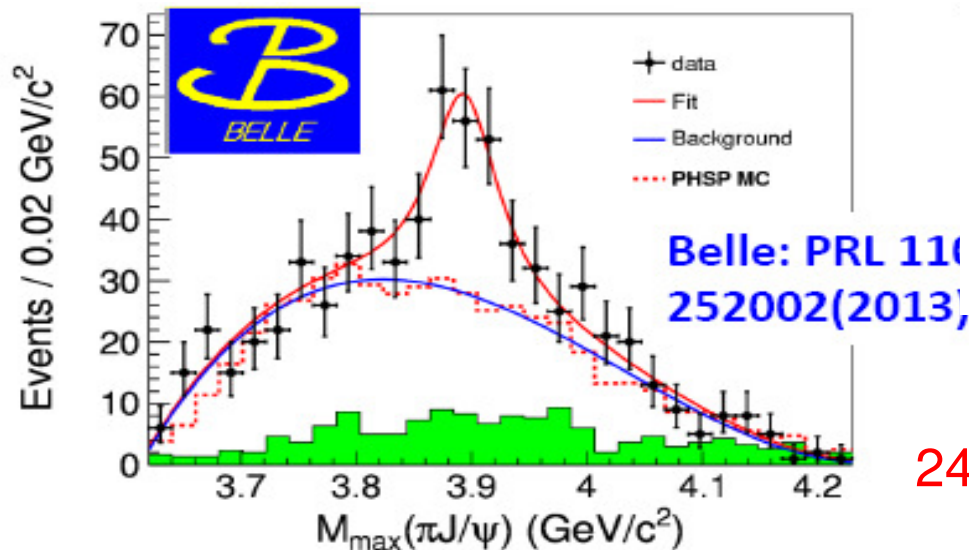
# Previously confirmed $Z_c^+$ state: $Z_c(3900)^+$ $e^+e^- \rightarrow Y(4260) \rightarrow \pi^-(\pi^+J/\psi)$



BESIII: PRL110, 252001 (2013)

- $M = 3899.0 \pm 3.6 \pm 4.9 \text{ MeV}$
- $\Gamma = 46 \pm 10 \pm 20 \text{ MeV}$
- $307 \pm 48 \text{ events}$

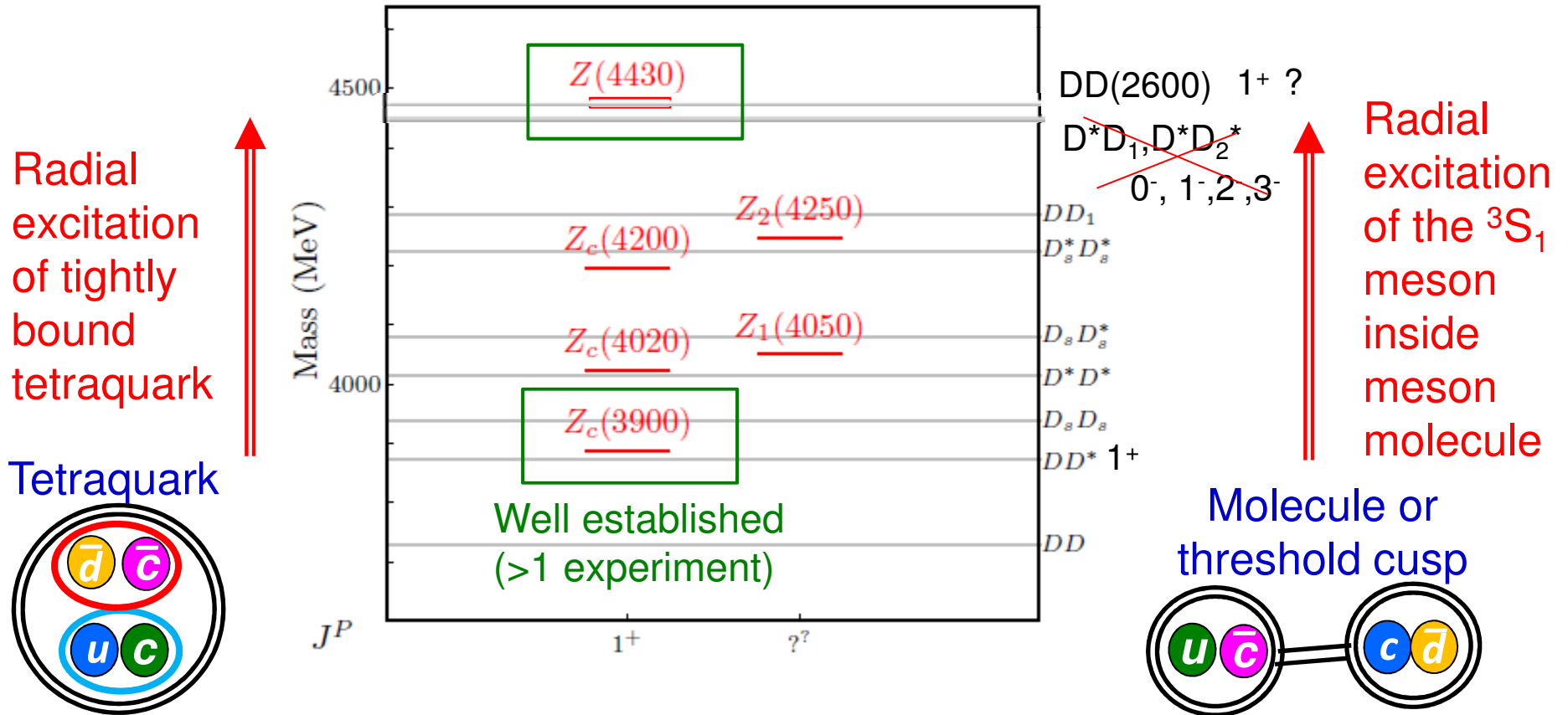
(no Argand diagram analysis)



$24 \pm 6 \text{ MeV}$  above the  $D\bar{D}^*$  threshold

# Z(4430)<sup>+</sup> and other Z<sub>c</sub><sup>+</sup> states

- The only threshold still at play for Z(4430)<sup>+</sup>: DD(2600) if D(2600) exists (needs confirmation!) and if it is 1<sup>-</sup> states (2<sup>3</sup>S<sub>1</sub>)
- Other charged Z<sub>c</sub><sup>+</sup>, Z<sub>b</sub><sup>+</sup> states are near D<sup>(\*)</sup>D̄<sup>(\*)</sup>, B<sup>(\*)</sup>B̄<sup>(\*)</sup> thresholds



Diquark states can be “attracted” towards the mesonic-pair threshold masses

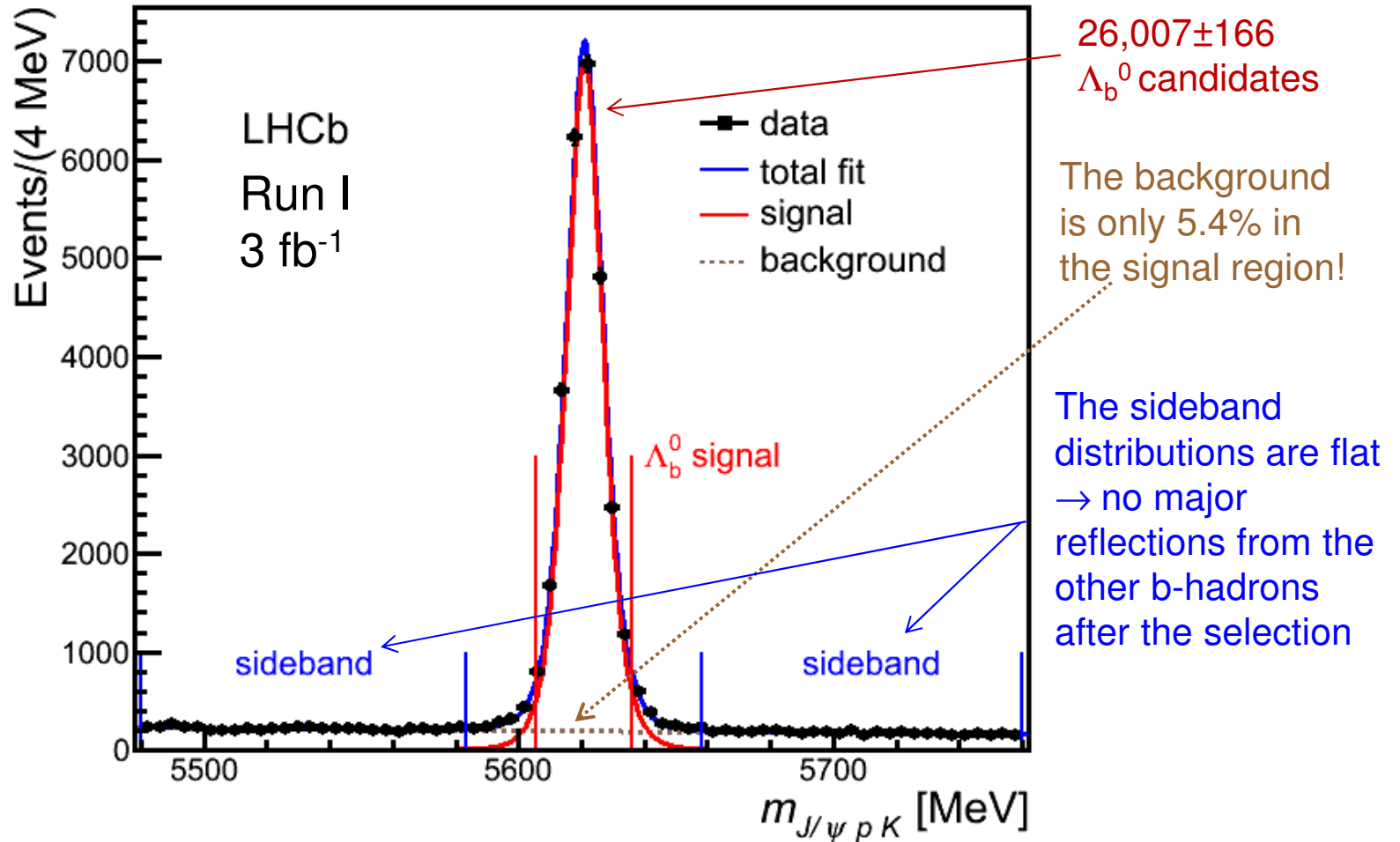
Meson molecules should be a few MeV below the threshold, Meson-meson cusps alone should be exactly at the thresholds.

Z<sub>c</sub>(3900)<sup>+</sup> is 24±6 MeV above the DD̄<sup>\*</sup> threshold (favors tetraquark picture)



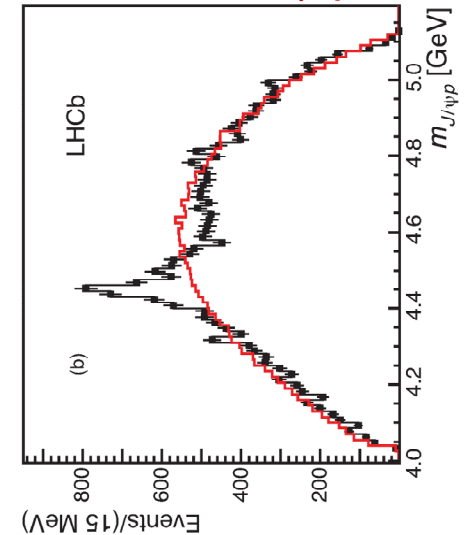
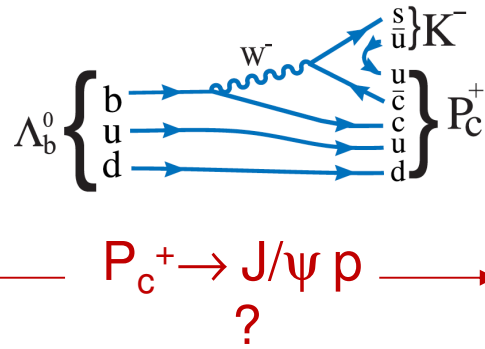
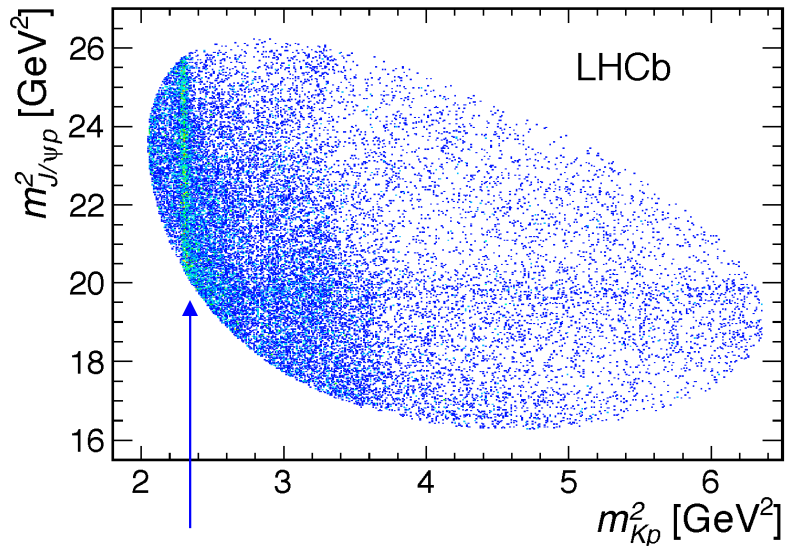
# LHCb $\Lambda_b^0 \rightarrow J/\psi p K^-$

LHCb-PAPER-2015-029, arXiv:1507.03414, PRL 115, 07201



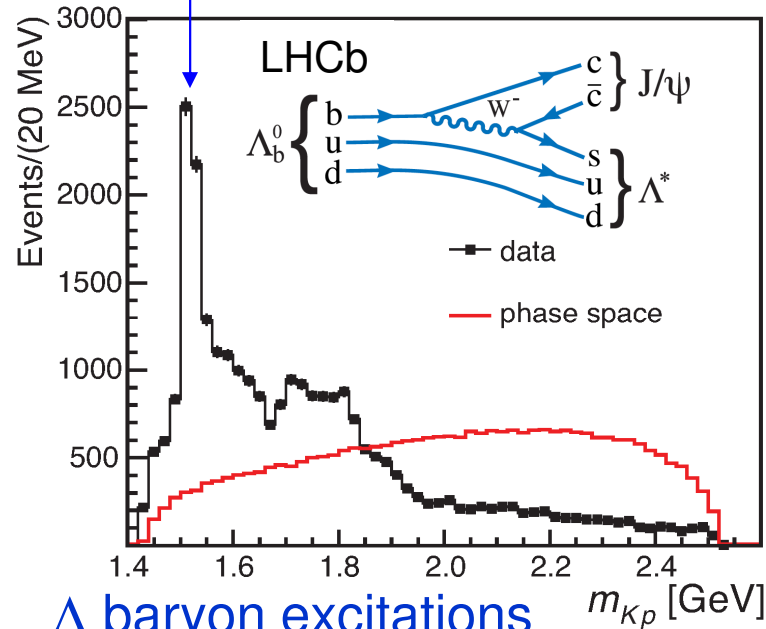
- The decay first observed by LHCb and used to measure  $\Lambda_b^0$  lifetime (LHCb-PAPER-2013-032, PRL 111, 102003)

# $\Lambda_b^0 \rightarrow J/\psi p K^-$ : unexpected structure in $m_{J/\psi p}$

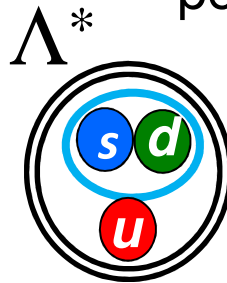


Exotic pentaquark

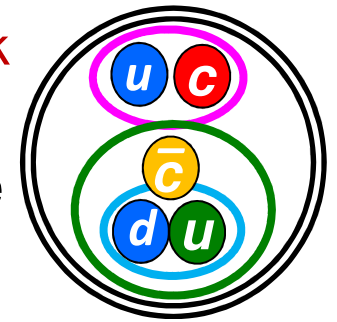
$\Lambda(1520)$  and other  $\Lambda^*$ 's  $\rightarrow p K^-$



$\Lambda$  baryon excitations



- Unexpected, narrow peak in  $m_{J/\psi p}$
- Ignored in LHCb for more than 2 years. We, like almost everybody else, did not believe in pentaquarks:



assumed to be a reflection of interfering  $\Lambda^*$ 's  $\rightarrow p K^-$  ?

Proper amplitude analysis absolutely necessary to check

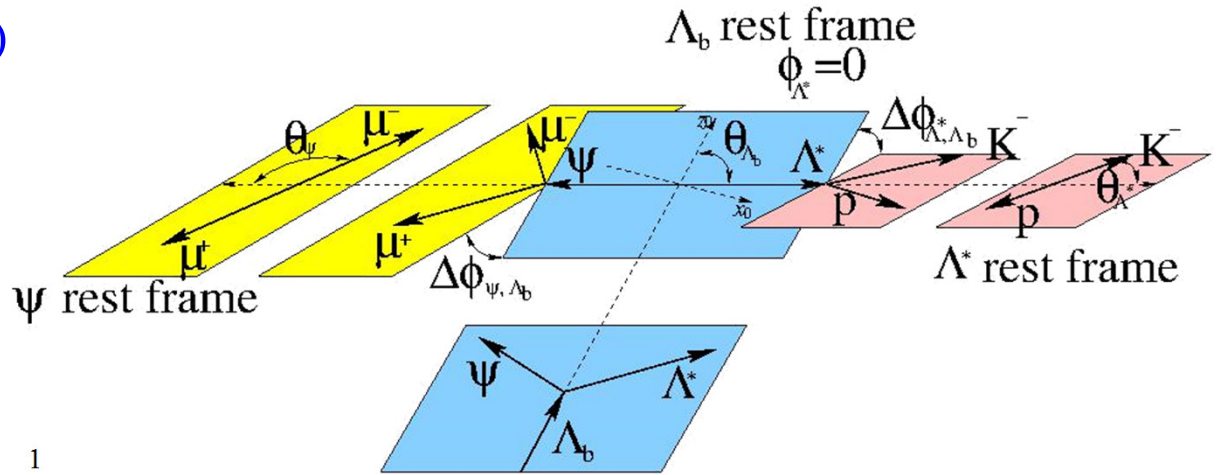
# Amplitude Analysis of $\Lambda_b \rightarrow J/\psi p K^-$ , $J/\psi \rightarrow \mu^+ \mu^-$

$$\left| M(m_{Kp}, \Omega | A_{\lambda_\psi, \lambda_\Lambda^*}^{\Lambda_b \rightarrow \psi \Lambda_n^*}, A_{\lambda_p}^{\Lambda_n^* \rightarrow pK^-}) \right|^2 = \sum_{\lambda_{\Lambda_b} = -1/2, +1/2} \sum_{\lambda_p = -1/2, +1/2} \sum_{\Delta\lambda_\mu = -1, 1} \left| M_{\lambda_{\Lambda_b}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} \right|^2$$

$$\Omega \equiv (\theta_{\Lambda_b}, \theta_{\Lambda^*}, \Delta\phi_{\Lambda^*, \Lambda_b}, \theta_\psi, \Delta\phi_{\psi, \Lambda_b})$$

6D  
analysis

1 mass, 5 angles



$$M_{\lambda_{\Lambda_b}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} = \sum_n \sum_{\lambda_\Lambda} \sum_{\lambda_\psi = -1, 0, 1} A_{\lambda_\psi, \lambda_\Lambda^*}^{\Lambda_b \rightarrow \psi \Lambda_n^*} D_{\lambda_{\Lambda_b}, \lambda_{\Lambda^*} - \lambda_\psi}^{\frac{1}{2}}(0, \theta_{\Lambda^*}, 0)^* \text{ LAB frame}$$

$$A_{\lambda_p}^{\Lambda_n^* \rightarrow pK^-} D_{\lambda_{\Lambda^*}, \lambda_p}^{J_{\Lambda^*}}(\Delta\phi_{\Lambda^*, \Lambda_b}, \theta_{K^*}, 0)^* R(m_{Kp} | M_{\Lambda_n^*}, \Gamma_{\Lambda_n^*}) D_{\lambda_\psi, \Delta\lambda_\mu}^1(\Delta\phi_{\psi, \Lambda_b}, \theta_\psi, 0)^*$$

4-6 independent **complex** helicity couplings per  $\Lambda_n^*$  resonance

# $\Lambda^*$ resonance model

All known  $\Lambda^*$  states  
from KN scattering  
experiments

No high- $J^P$  high-mass states

limit  $L$

All states, all  $L$

State	$J^P$	$M_0$ (MeV)	$\Gamma_0$ (MeV)	# Reduced	# Extended
$\Lambda(1405)$	$1/2^-$	$1405.1_{-1.0}^{+1.3}$	$50.5 \pm 2.0$	3	4
$\Lambda(1520)$	$3/2^-$	$1519.5 \pm 1.0$	$15.6 \pm 1.0$	5	6
$\Lambda(1600)$	$1/2^+$	1600	150	3	4
$\Lambda(1670)$	$1/2^-$	1670	35	3	4
$\Lambda(1690)$	$3/2^-$	1690	60	5	6
$\Lambda(1800)$	$1/2^-$	1800	300	4	4
$\Lambda(1810)$	$1/2^+$	1810	150	3	4
$\Lambda(1820)$	$5/2^+$	1820	80	1	6
$\Lambda(1830)$	$5/2^-$	1830	95	1	6
$\Lambda(1890)$	$3/2^+$	1890	100	3	6
$\Lambda(2100)$	$7/2^-$	2100	200	1	6
$\Lambda(2110)$	$5/2^+$	2110	200	1	6
$\Lambda(2350)$	$9/2^+$	2350	150	0	6
$\Lambda(2585)$	$5/2^-?$	$\approx 2585$	200	0	6

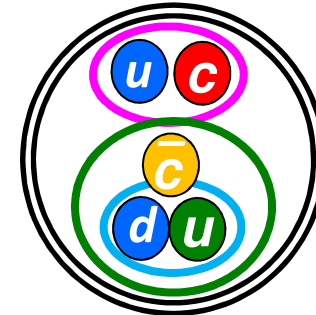
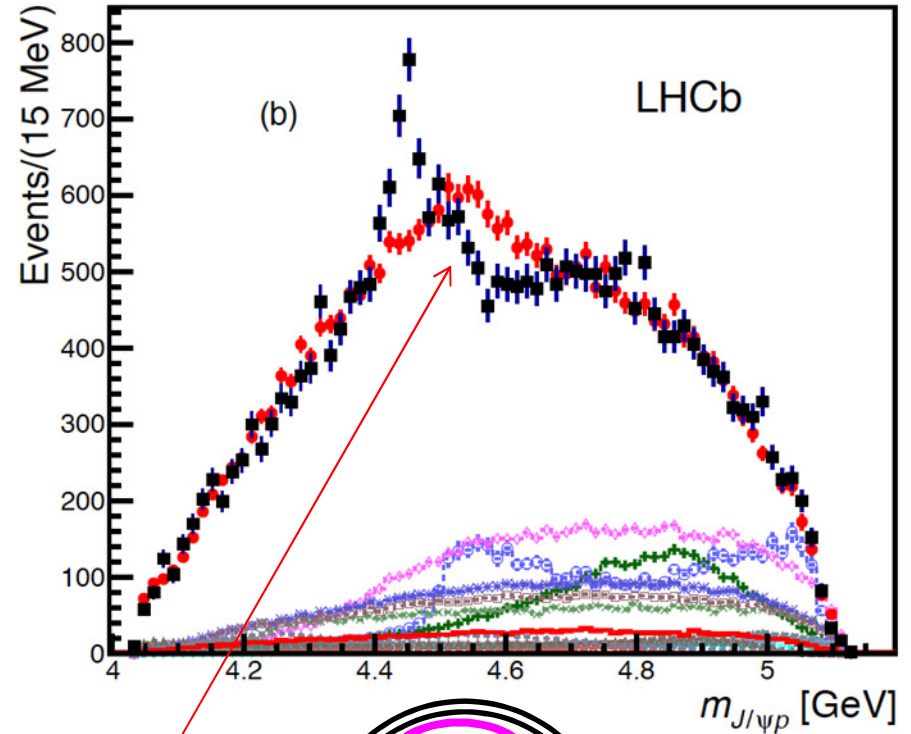
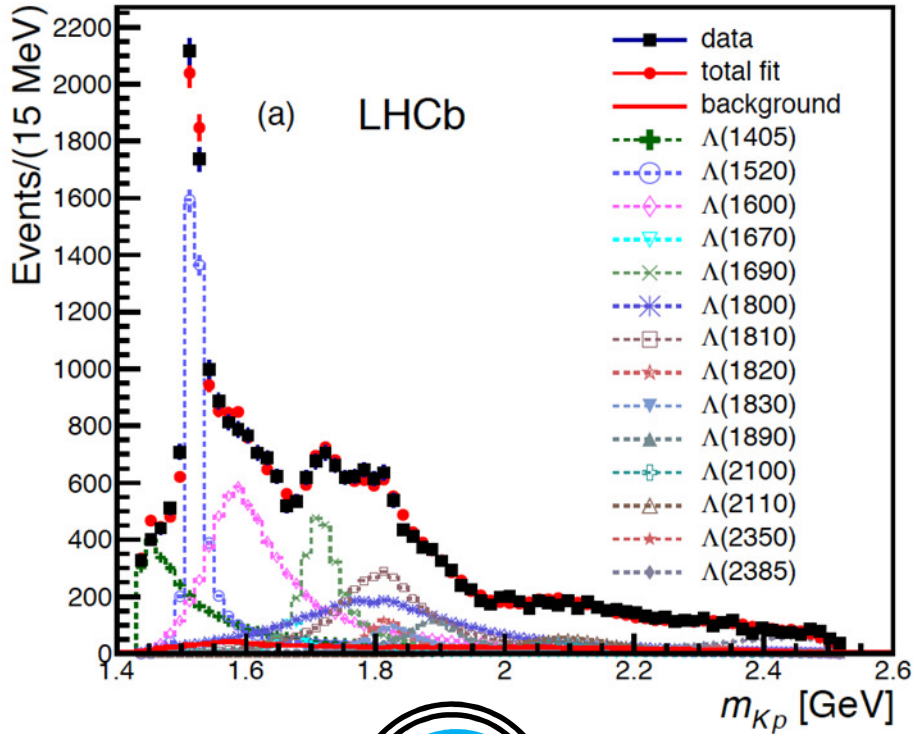
# of fit parameters:

64

146

# Fit with $\Lambda^* \rightarrow pK^-$ contributions only

# of fit parameters: 146



- Include all known  $\Lambda$  excitations:
- $m_{Kp}$  looks fine, but not  $m_{J/\psi p}$

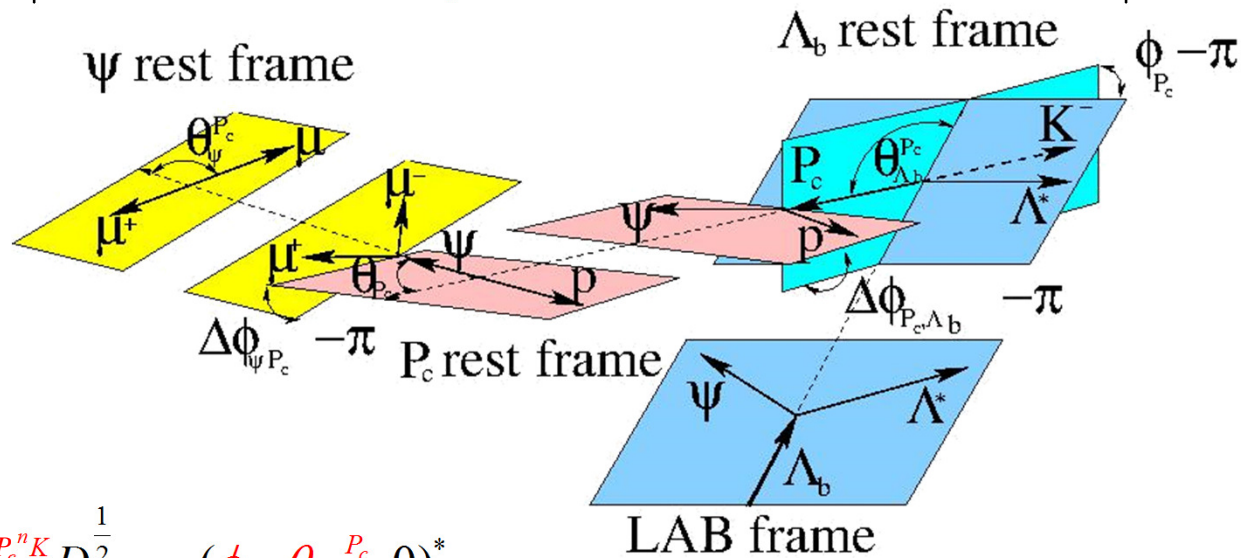
# Amplitude Analysis of $\Lambda_b \rightarrow J/\psi p K^-$ , $J/\psi \rightarrow \mu^+ \mu^-$

$$\left| M(m_{Kp}, \Omega | M_{P_c^n}, \Gamma_{P_c^n}, J_{P_c^n}, A_{\lambda_{P_c^n}}^{\Lambda_b \rightarrow P_c^n K}, A_{\lambda_\psi, \lambda_p}^{P_c^n \rightarrow \psi p}, A_{\lambda_\psi, \lambda_\Lambda^*}^{\Lambda_b \rightarrow \psi \Lambda^*}, A_{\lambda_p}^{\Lambda^* \rightarrow p K}) \right|^2 =$$

$$\sum_{\lambda_{\Lambda_b} = -1/2, +1/2} \sum_{\lambda_p = -1/2, +1/2} \sum_{\Delta\lambda_\mu = -1, 1} \left| M_{\lambda_{\Lambda_b}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} + e^{i\Delta\lambda_\mu \alpha_\mu} \sum_{\lambda_p^{P_c} = -1/2, +1/2} d_{\lambda_p^{P_c}, \lambda_p}^{\frac{1}{2}}(\theta_p) M_{\lambda_{\Lambda_b}, \lambda_p^{P_c}, \Delta\lambda_\mu}^{P_c} \right|^2$$

## 6D analysis

1 mass, 6+2 angles  
all derivable from the  $\Lambda^*$  variables



$$M_{\lambda_{\Lambda_b}, \lambda_p, \Delta\lambda_\mu}^{P_c} = \sum_n \sum_{\lambda_{P_c}} \sum_{\lambda_\psi = -1, 0, 1} A_{\lambda_{P_c}}^{\Lambda_b \rightarrow P_c^n K} D_{\lambda_{\Lambda_b}, \lambda_{P_c^n}}^{\frac{1}{2}}(\phi_{P_c}, \theta_{\Lambda^*}^{P_c}, 0)^*$$

$$A_{\lambda_\psi, \lambda_p}^{P_c^n \rightarrow \psi p} D_{\lambda_{P_c^n}, \lambda_\psi - \lambda_p}^{J_{P_c^n}}(\Delta\phi_{P_c, \Lambda_b}, \theta_{P_c}, 0)^* R(m_{\psi p} | M_{P_c^n}, \Gamma_{P_c^n}) D_{\lambda_\psi, \Delta\lambda_\mu}^1(\Delta\phi_{\psi, P_c}, \theta_{\psi}^{P_c}, 0)^*$$

↑  
3-4 independent **complex** helicity couplings per  $P_c^n$  resonance

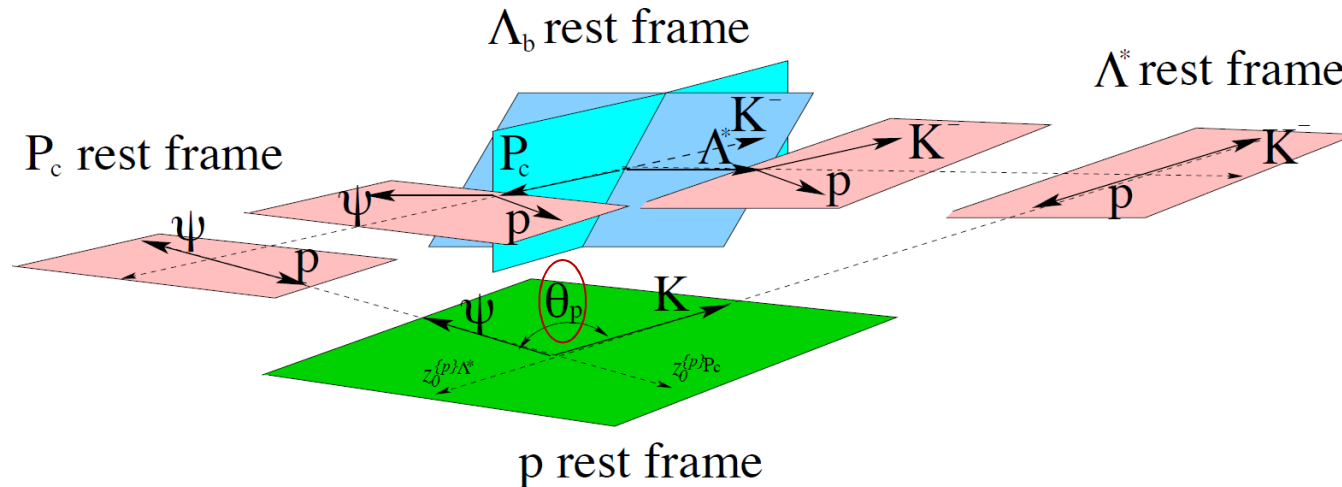
# $\Lambda^*$ Plus $P_c^+$ Matrix Element

2 additional angles to align the muon and proton helicity frames between the  $\Lambda^*$  and  $P_c^+$  decay chains

also derivable from the  $\Lambda^*$  decay variables

$$\left| M(m_{Kp}, \Omega | M_{P_c^n}, \Gamma_{P_c^n}, J_{P_c^n}, A_{\lambda_{P_c^n}}^{\Lambda_b \rightarrow P_c^n K}, A_{\lambda_\psi, \lambda_p}^{P_c^n \rightarrow \psi p}, A_{\lambda_\psi, \lambda_{\Lambda^*}}^{\Lambda_b \rightarrow \psi \Lambda^*}, A_{\lambda_p}^{\Lambda^* \rightarrow p K}) \right|^2 =$$

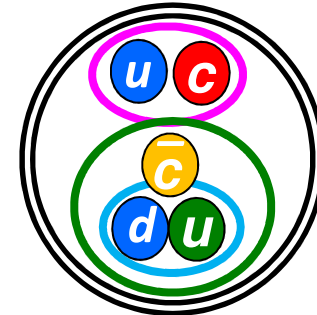
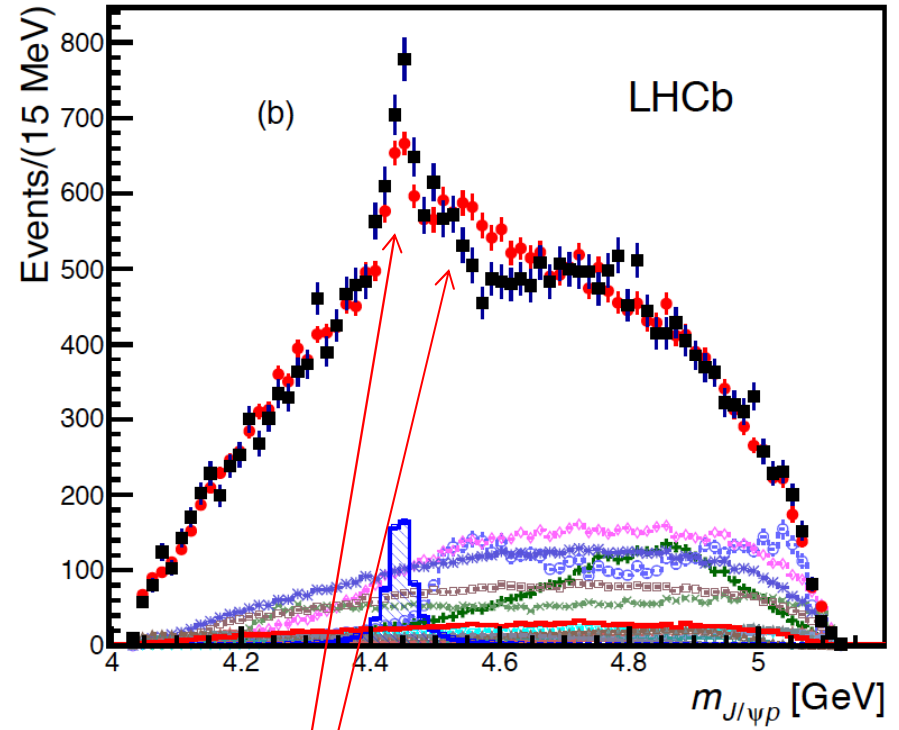
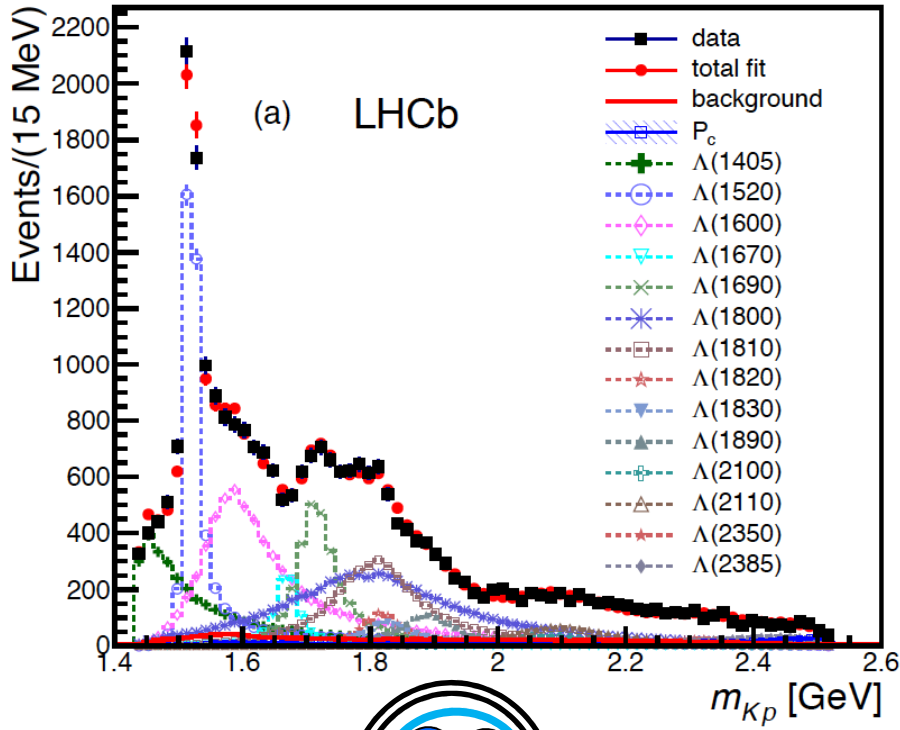
$$\sum_{\lambda_{\Lambda_b} = -1/2, +1/2} \sum_{\lambda_p = -1/2, +1/2} \sum_{\Delta\lambda_\mu = -1, 1} \left| M_{\lambda_{\Lambda_b}, \lambda_p, \Delta\lambda_\mu}^{\Lambda^*} + e^{i\Delta\lambda_\mu \alpha_\mu} \sum_{\lambda_p^{P_c} = -1/2, +1/2} d_{\lambda_p^{P_c}, \lambda_p}^{\frac{1}{2}}(\theta_p) M_{\lambda_{\Lambda_b}, \lambda_p^{P_c}, \Delta\lambda_\mu}^{P_c} \right|^2$$



- Without this realignment can't describe  $\Lambda^*$  plus  $P_c^+$  interferences properly
- They integrate out to zero in full phase-space but present in the differential 6D fit-PDF

# Fit with $\Lambda^*$ 's and one $P_c^+ \rightarrow J/\psi p$ state

# of fit parameters:  $146 + 10 = 156$

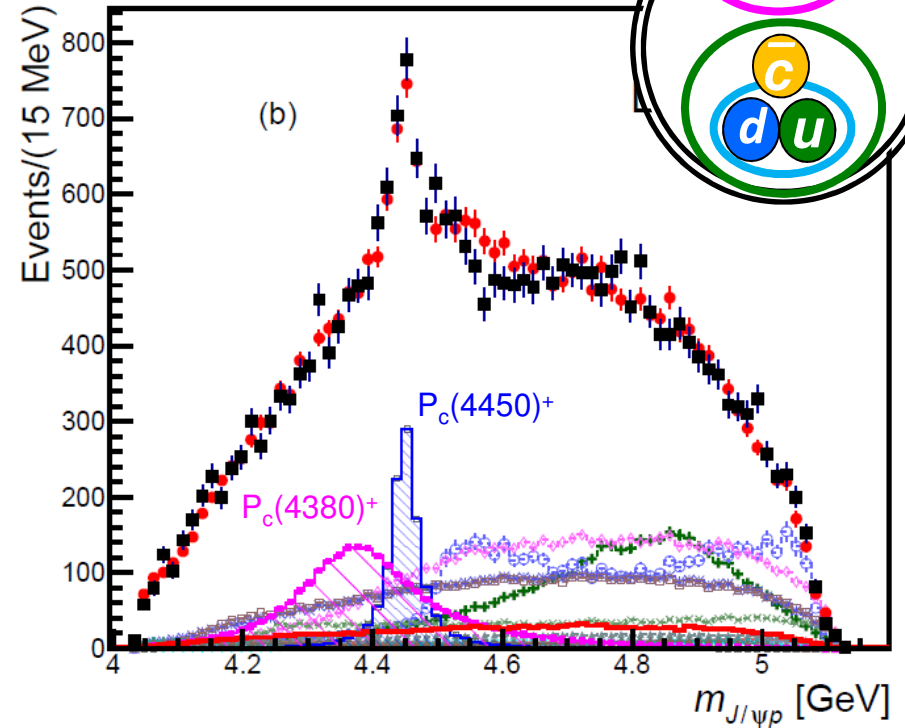
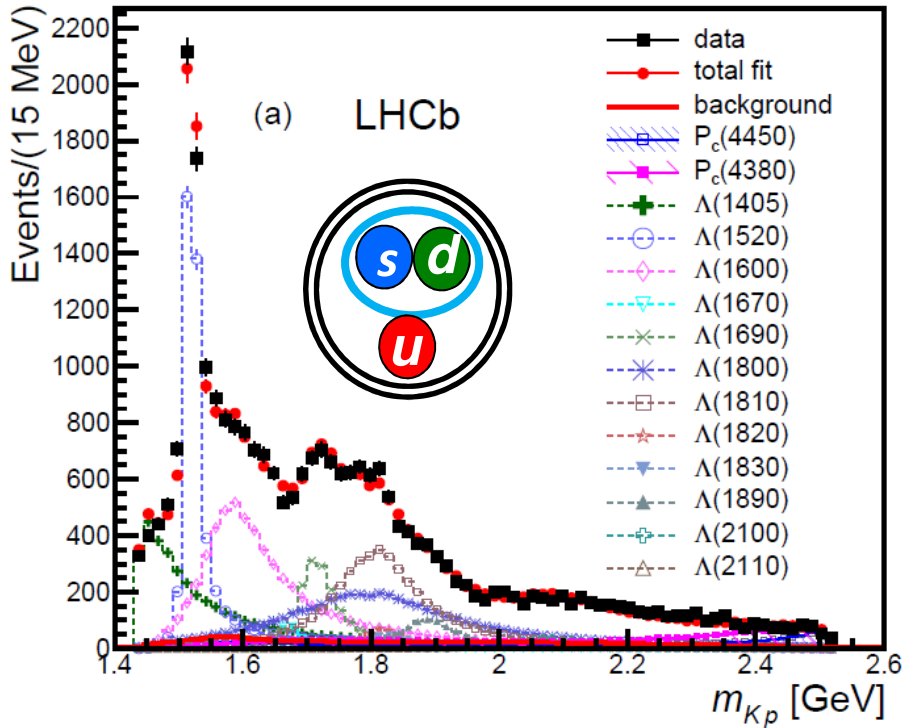


- Try all  $J^P$  of  $P_c^+$  up to  $7/2^\pm$
- Best fit has  $J^P = 5/2^\pm$ . Still not a good fit



# Fit with $\Lambda^*$ 's and two $P_c^+ \rightarrow J/\psi p$ states

# of fit parameters:  $64_C + 20 = 84$



- Obtain good fits even with the reduced  $\Lambda^*$  model

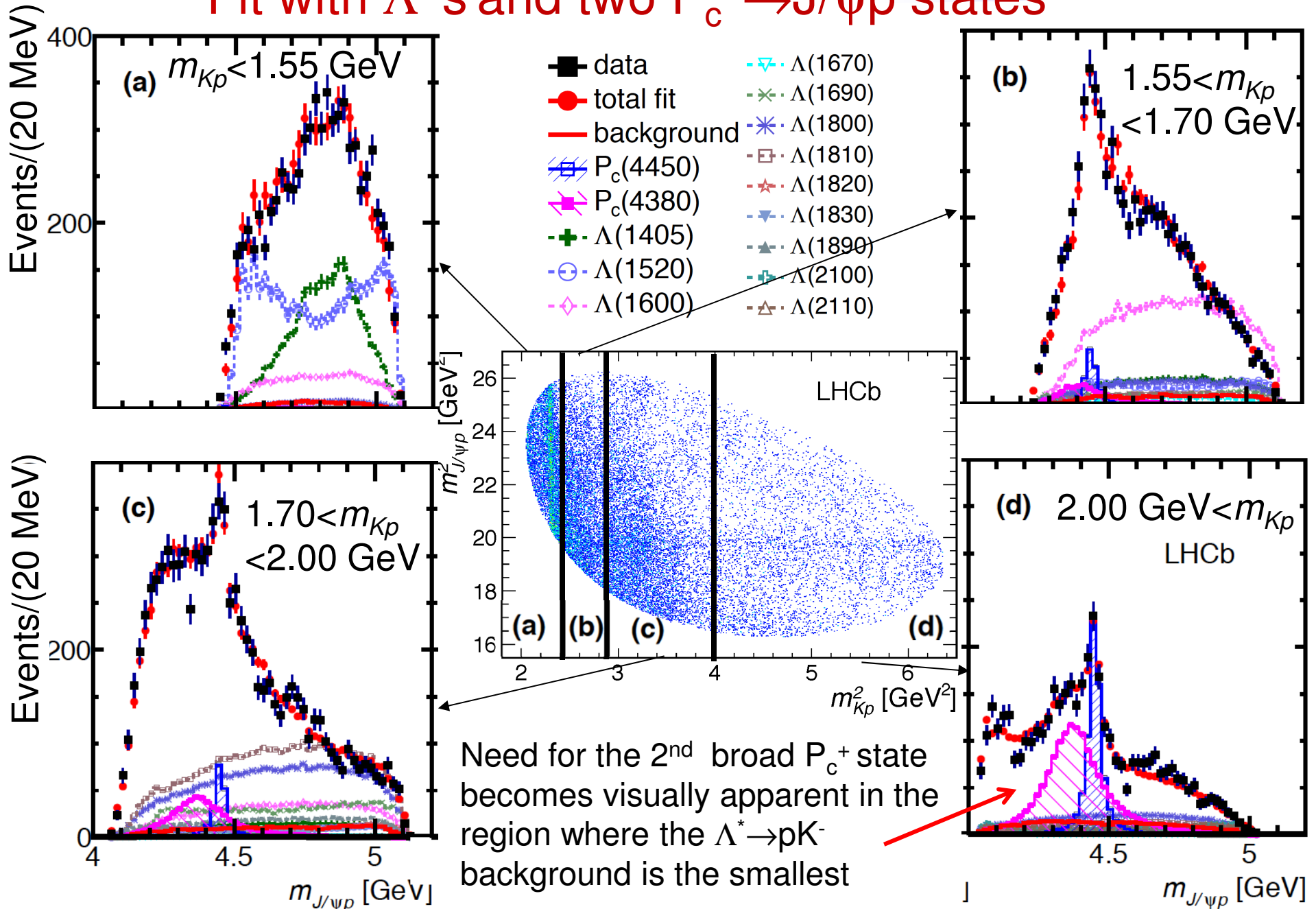
State	Mass (MeV)	Width (MeV)	Fit fraction (%)	Significance
$P_c(4380)^+$	$4380 \pm 8 \pm 29$	$205 \pm 18 \pm 86$	$8.4 \pm 0.7 \pm 4.2$	$9\sigma$
$P_c(4450)^+$	$4449.8 \pm 1.7 \pm 2.5$	$39 \pm 5 \pm 19$	$4.1 \pm 0.5 \pm 1.1$	$12\sigma$

- Best fit has  $J^P = (3/2^-, 5/2^+)$ , also  $(3/2^+, 5/2^-)$  &  $(5/2^+, 3/2^-)$  are preferred

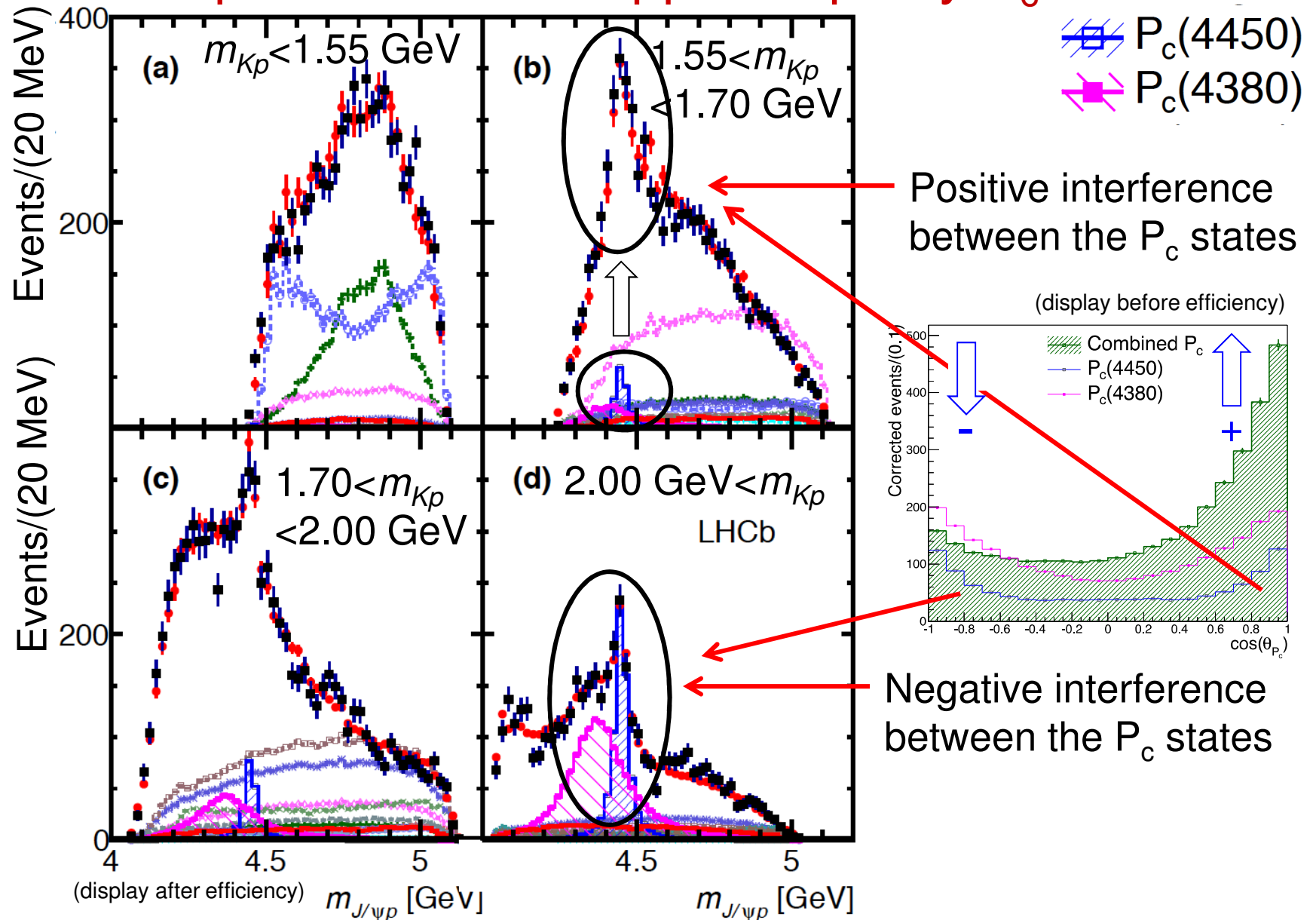
## Statistical significances

- Fit improves greatly, for 1  $P_c$   $\Delta(-2\ln\mathcal{L})=14.7^2$ , adding the 2<sup>nd</sup>  $P_c$  improves by  $11.6^2$ , for adding both together  $\Delta(-2\ln\mathcal{L})=18.7^2$
- Simulations of pseudoexperiments are used to turn the  $\Delta(-2\ln\mathcal{L})$  values to significances:
  - significance of  $P_c(4450)^+$  state is  $12\sigma$
  - significance of  $P_c(4380)^+$  state is  $9\sigma$
  - combined significance of the two  $P_c^+$  states is  $15\sigma$
- This includes the dominant systematic uncertainties, coming from difference between extended and reduced  $\Lambda^*$  model results.

# Fit with $\Lambda^*$ 's and two $P_c^+ \rightarrow J/\psi p$ states



# Data preference for opposite parity $P_c^+$ states

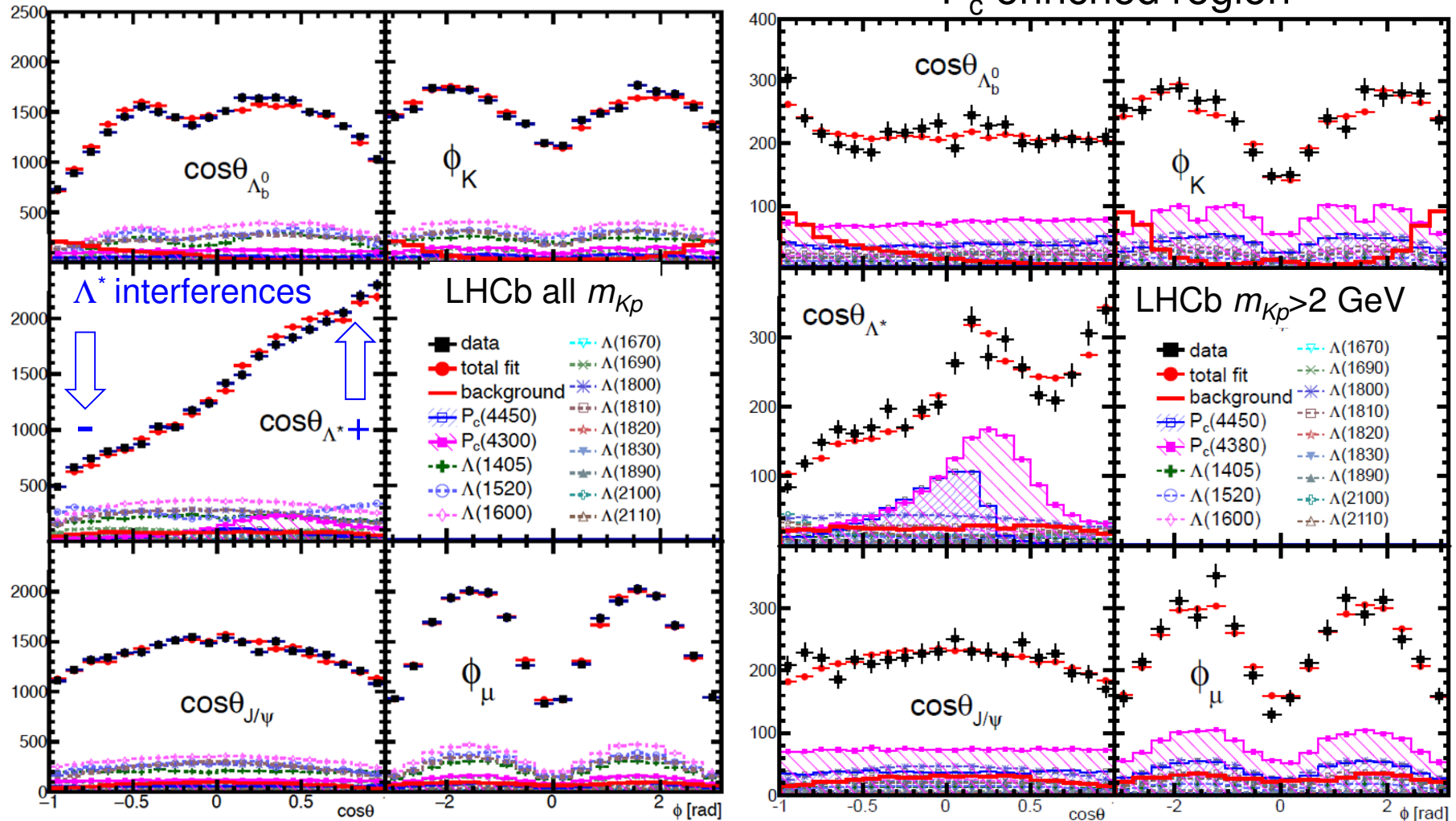


- This interference pattern only for states with opposite parity

# Angular distributions

All data

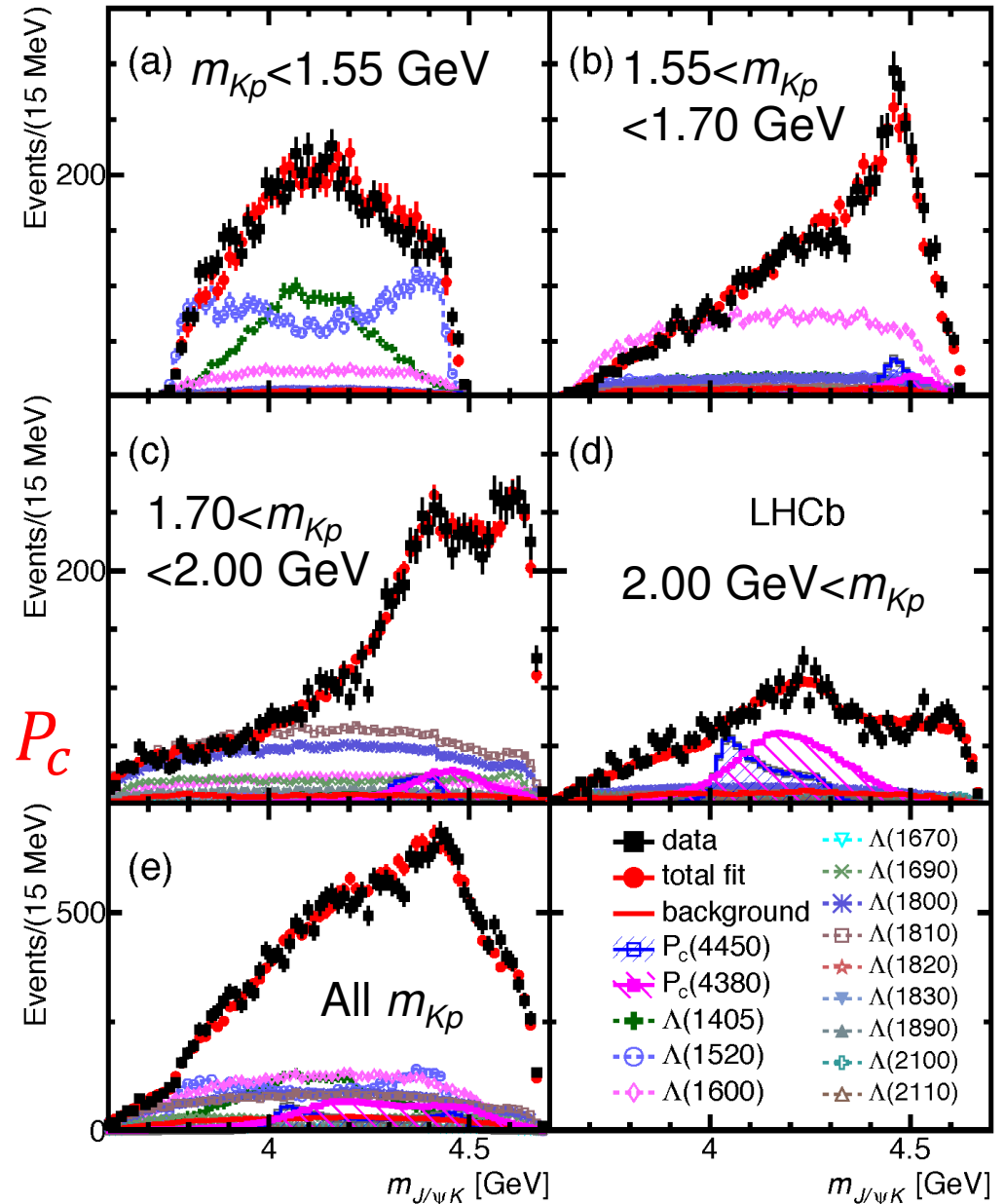
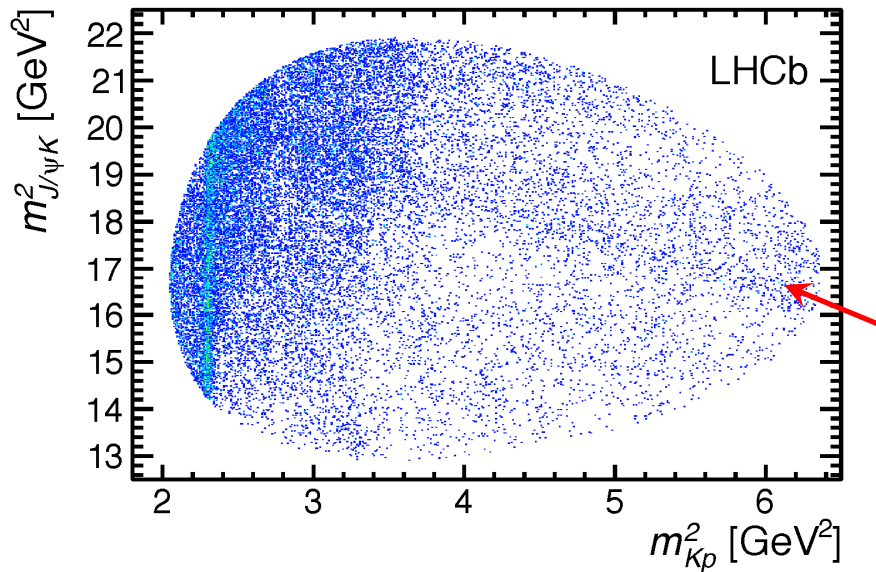
$P_c$  enriched region



- Good description of the data in all 6 dimensions!

# No need for exotic $J/\psi K^-$ contributions

- $J/\psi K^-$  system is well described by the  $\Lambda^*$  and  $P_c^+$  reflections.



## Systematic uncertainties

Source	$M_0$ (MeV)		$\Gamma_0$ (MeV)		Fit fractions (%)			
	low	high	low	high	low	high	$\Lambda(1405)$	$\Lambda(1520)$
Extended vs. reduced	21	0.2	54	10	3.14	0.32	1.37	0.15
$\Lambda^*$ masses & widths	7	0.7	20	4	0.58	0.37	2.49	2.45
Proton ID	2	0.3	1	2	0.27	0.14	0.20	0.05
$10 < p_p < 100$ GeV	0	1.2	1	1	0.09	0.03	0.31	0.01
Nonresonant	3	0.3	34	2	2.35	0.13	3.28	0.39
Separate sidebands	0	0	5	0	0.24	0.14	0.02	0.03
$J^P$ ( $3/2^+$ , $5/2^-$ ) or ( $5/2^+$ , $3/2^-$ )	10	1.2	34	10	0.76	0.44		
$d = 1.5 - 4.5$ GeV $^{-1}$	9	0.6	19	3	0.29	0.42	0.36	1.91
$L_{\Lambda_b^0}^{P_c} \Lambda_b^0 \rightarrow P_c^+ (\text{low/high}) K^-$	6	0.7	4	8	0.37	0.16		
$L_{P_c} P_c^+ (\text{low/high}) \rightarrow J/\psi p$	4	0.4	31	7	0.63	0.37		
$L_{\Lambda_b^0}^{\Lambda^*} \Lambda_b^0 \rightarrow J/\psi \Lambda^*$	11	0.3	20	2	0.81	0.53	3.34	2.31
Efficiencies	1	0.4	4	0	0.13	0.02	0.26	0.23
Change $\Lambda(1405)$ coupling	0	0	0	0	0	0	1.90	0
Overall	29	2.5	86	19	4.21	1.05	5.82	3.89
sFit/cFit cross check	5	1.0	11	3	0.46	0.01	0.45	0.13

- Uncertainties in the  $\Lambda^*$  model dominate

## Additional cross-checks

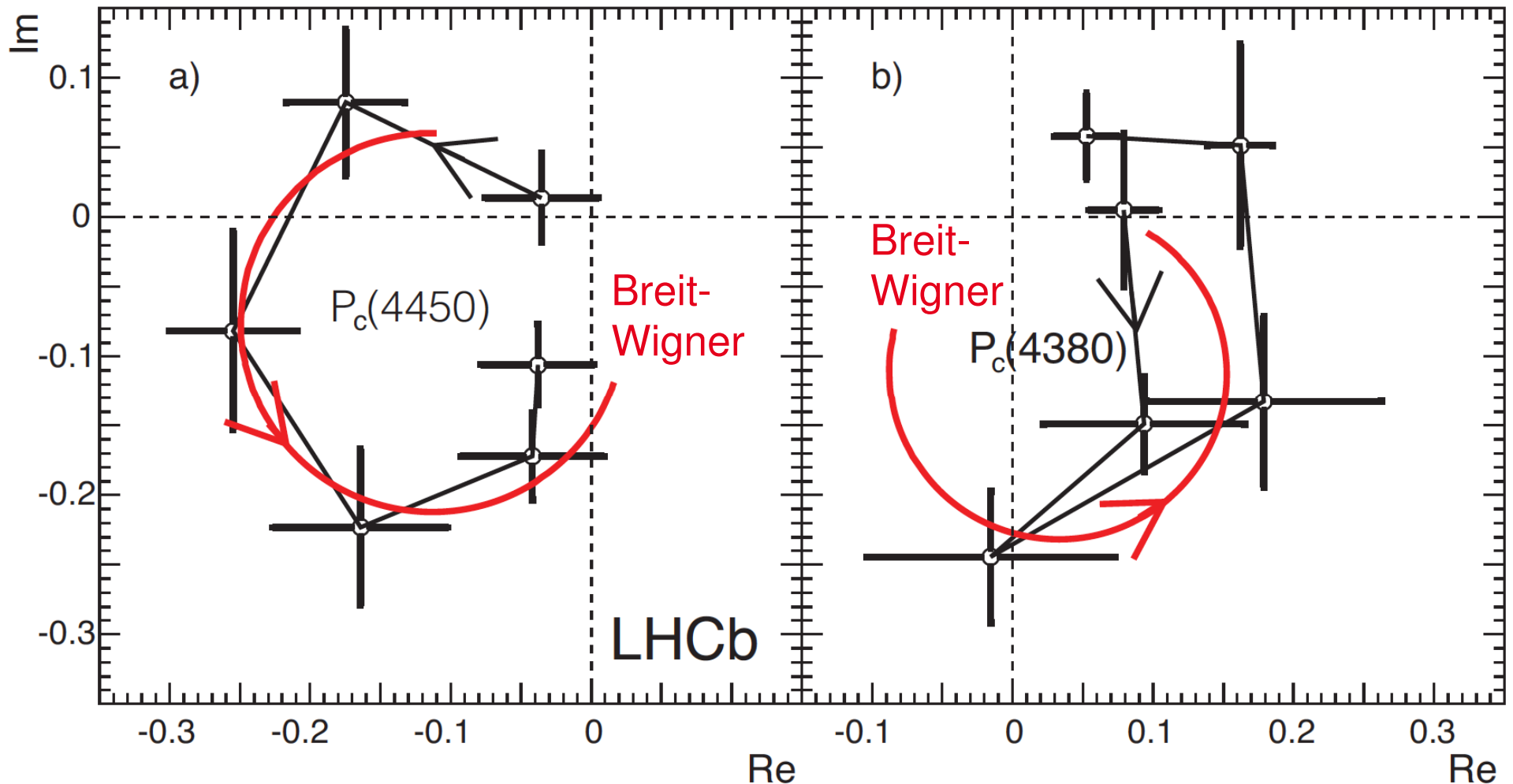
- Many additional cross-checks have been done. Some are listed here:
  - The same  $P_c^+$  structure found using very different selections by different LHCb teams
  - Two independently coded fitters using different background subtractions (cFit & sFit)
  - Split data shows consistency: 2011/2012, magnet up/down,  $\bar{\Lambda}_b/\Lambda_b$ ,  $\Lambda_b(p_T \text{ low})/\Lambda_b(p_T \text{ high})$
  - Extended model fits tried without  $P_c$  states, but with two additional high mass  $\Lambda^*$  resonances allowing masses & widths to vary, or 4 non-resonant terms of J up to 3/2



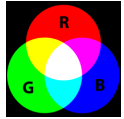
# Argand diagrams

PRL 115, 07201 (2015)

$P_c^+$  amplitudes for 6  $m_{J/\psi p}$  bins between  $+\Gamma$  &  $-\Gamma$  around the resonance mass

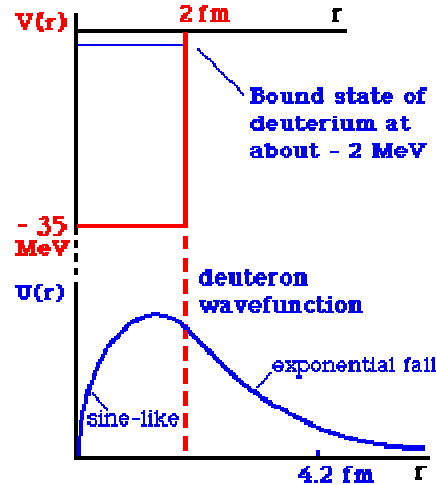
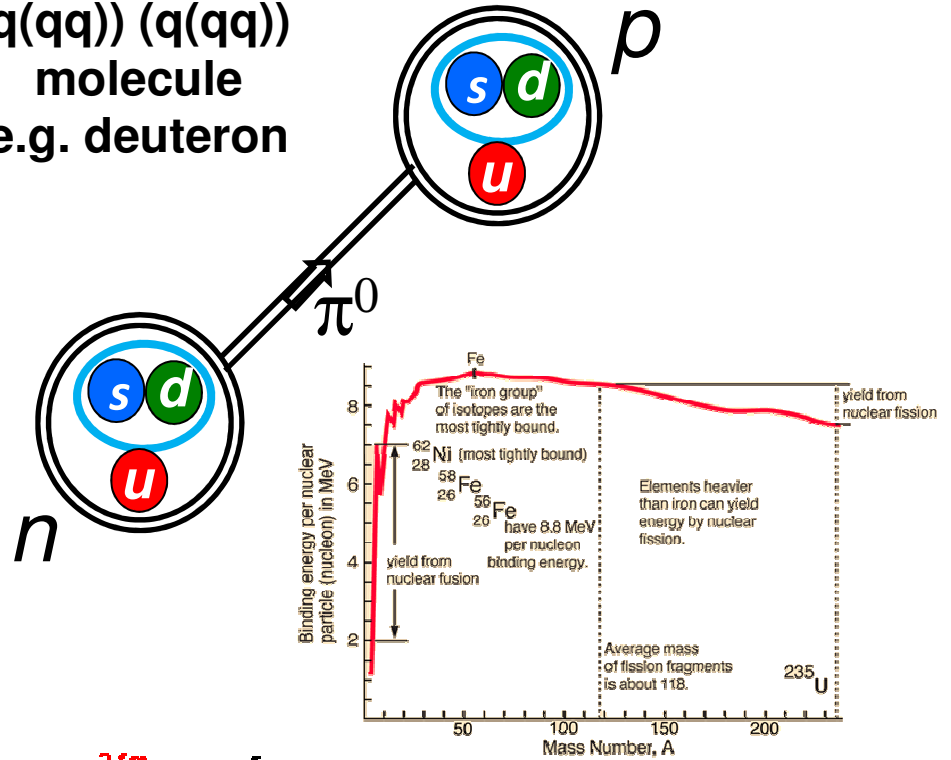
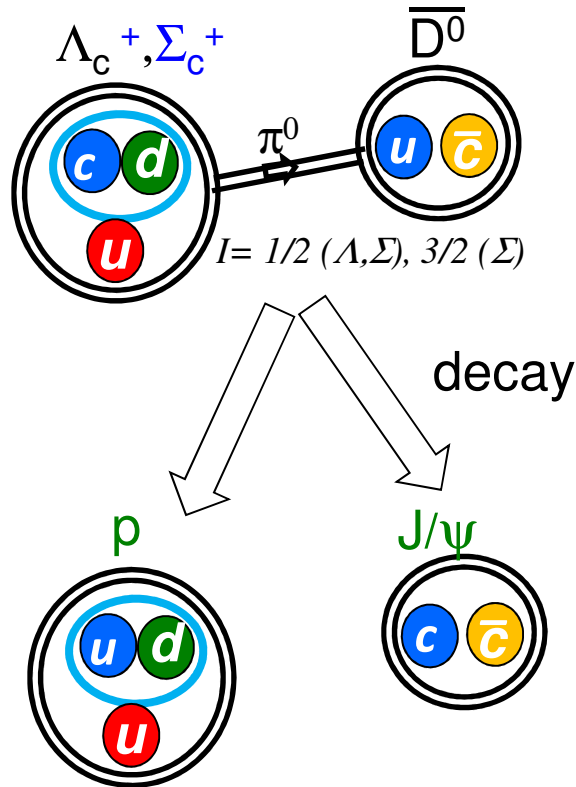


- Good evidence for the resonant character of  $P_c(4450)^+$
- The errors for  $P_c(4380)^+$  are too large to be conclusive



# Molecular states?

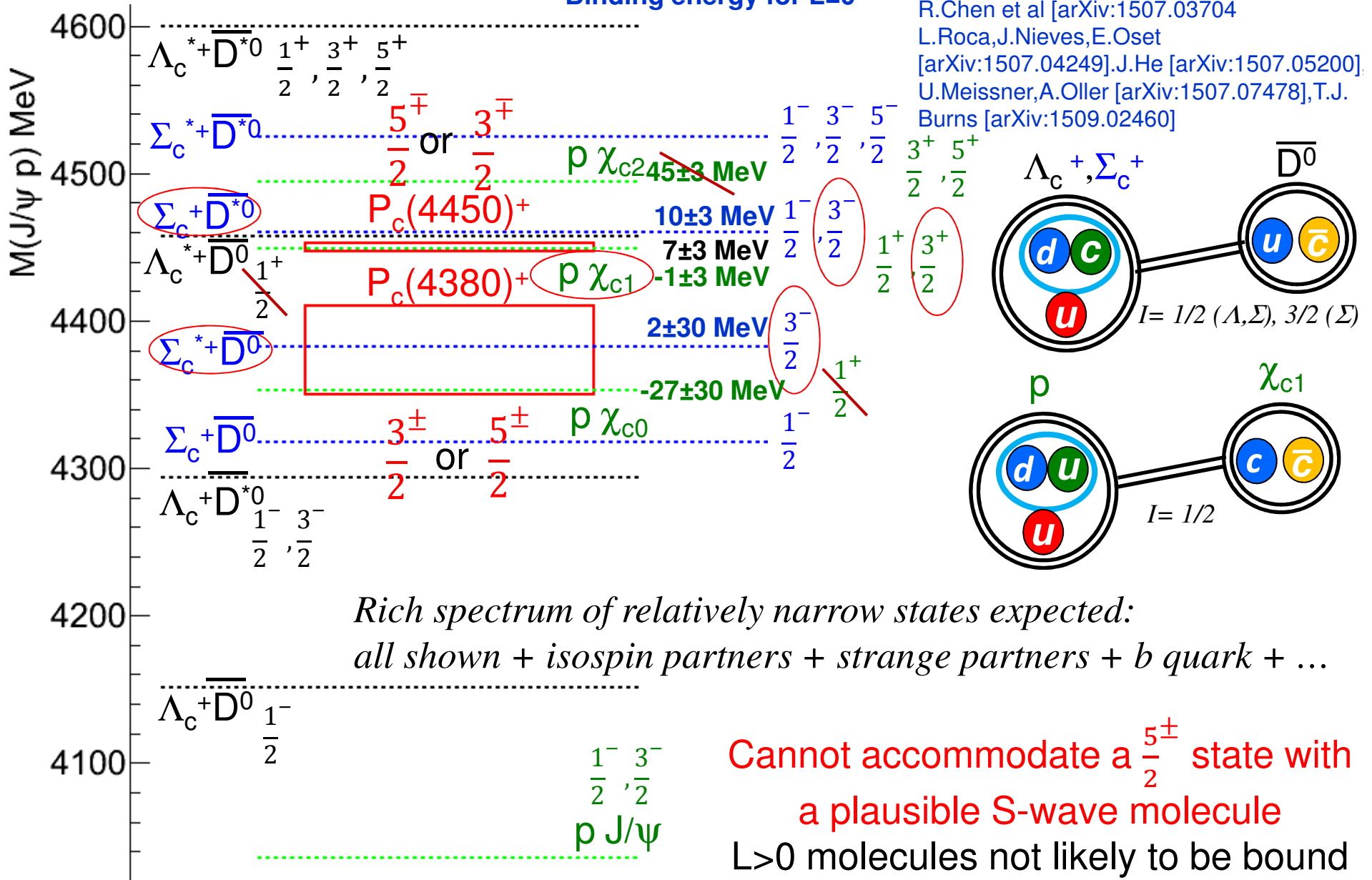
(q(qq)) (q(qq))  
molecule  
e.g. deuteron



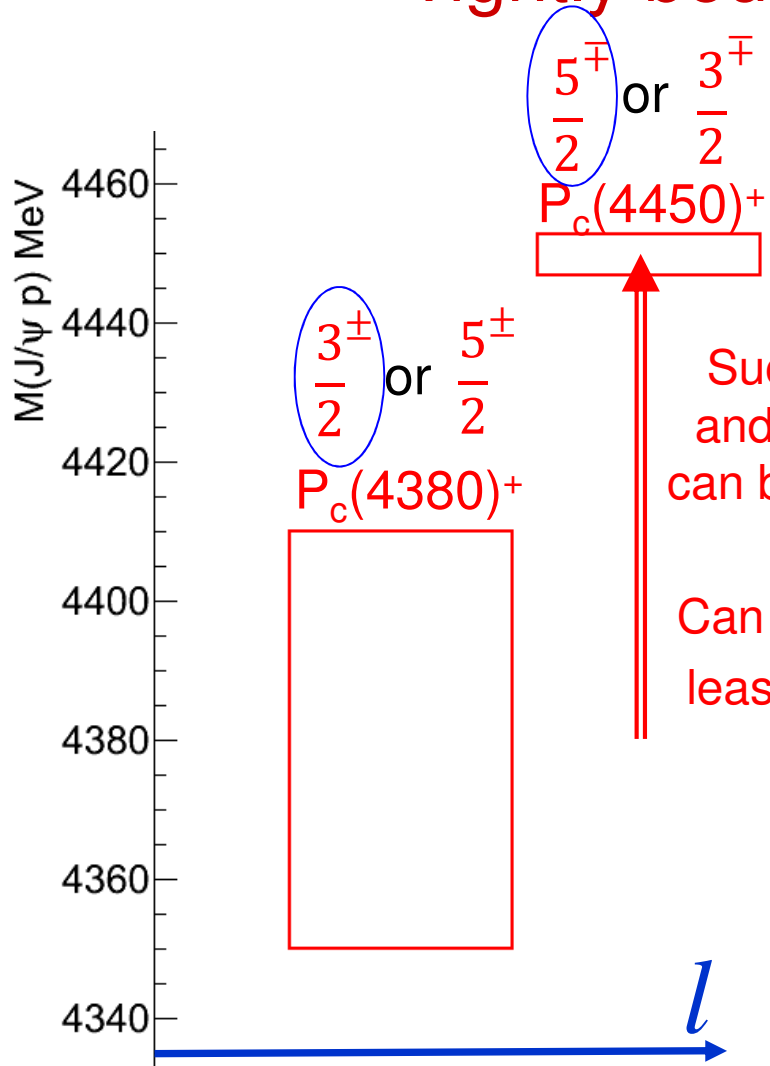
Difficult to get more than one state ( $n=1, l=0$ ).  
 $M = M_1 + M_2 - (\text{a few MeV})$   
 $J^P = (J_1 \otimes J_2)^{P_1 P_2}$   
 $\Gamma \sim \max(\Gamma_1, \Gamma_2)$

# Baryon-meson molecules?

Binding energy for L=0



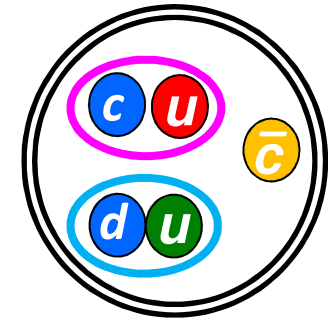
# Tightly bound pentaquarks?



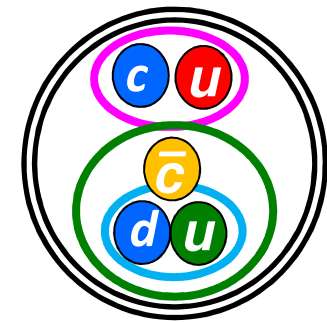
Maiani, Polosa, Riquer [arXiv:1507.04980],  
 Anisovich et al [arXiv:1507.07652, 1509.04898],  
 Li, He, He [arXiv:1507.08252],  
 Ghosh et al [arXiv:1508.00356]

Such mass difference  
 and the opposite parity  
 can be explained by  $\Delta l=1$

Can accommodate  $\frac{5^\pm}{2}$  when at  
 least one diquark in  $S=1$  state



R. Lebed [arXiv:1507.05867]



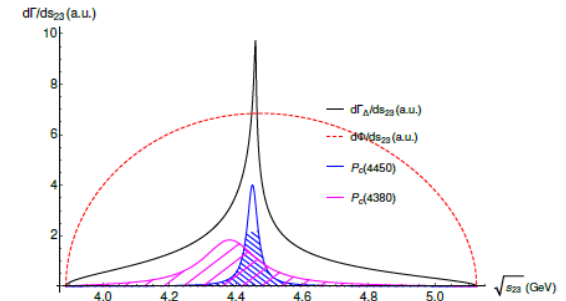
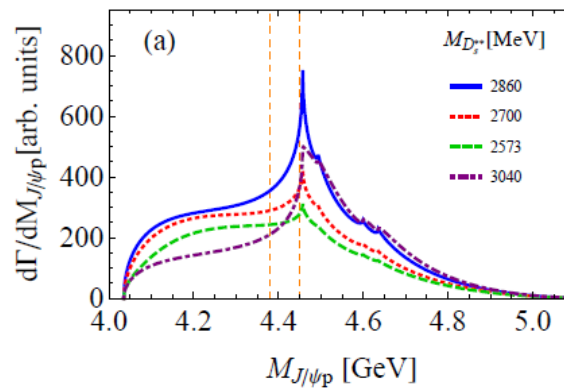
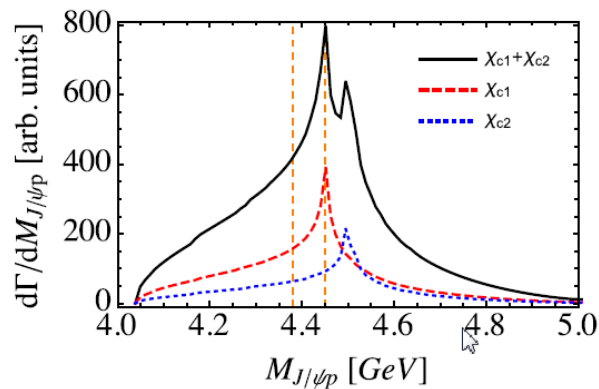
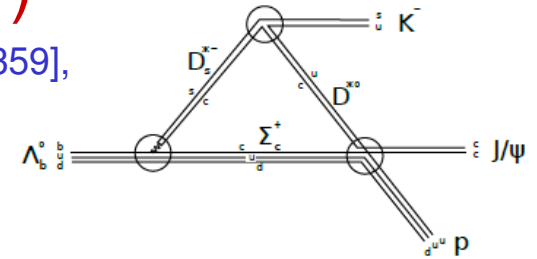
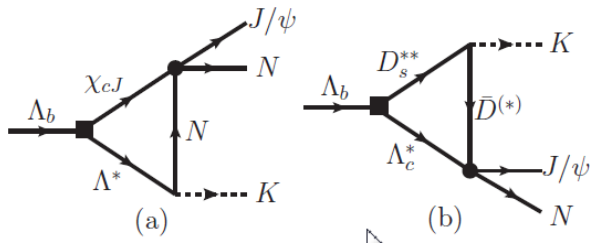
*Rich spectrum of states expected:  
 $S=0$  (lower  $J$ ) +  $l + n +$  isospin partners  
 + strange partners +  $b$  quark + ...*

e.g.  $\bar{c}[cu]_{S=1} [ud]_{S=0} (l=1)$

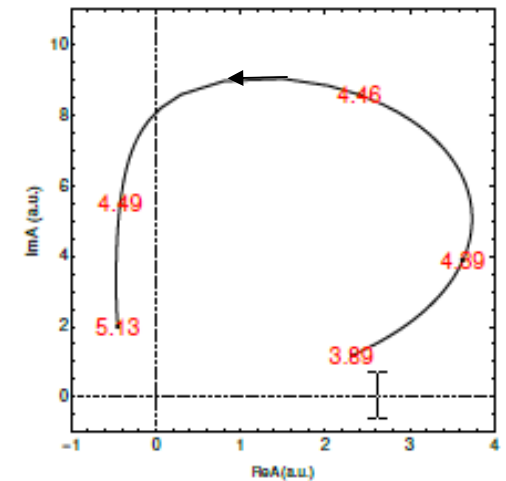
$\bar{c}[cu]_{S=1} [ud]_{S=1} (l=0)$

# Rescattering (triangular singularity)

Z.-H.Liu,Q.Wang,Q.Zhao [arXiv:1507.05359],  
 M. Mikhashenko [arXiv:1507.06552],  
 A. Szczepaniak [arXiv:1510.01789]



- Conventional hadrons produced and then rescatter (rearrange quarks) to produce a peak in the exotic channel. Peaking structures related to mass thresholds.
- Ad hoc parameter values to generate desired structures.
- Can sometimes arrange for the resonant-like phase running.
- Given proliferation of thresholds, why aren't they everywhere?
- Not clear these models can describe decay angles distributions – predictions and tests on the data are needed.
- In the past, many resonances which are well established by now, were proposed to be rescattering effects (e.g.  $a_1(1260)$ ).

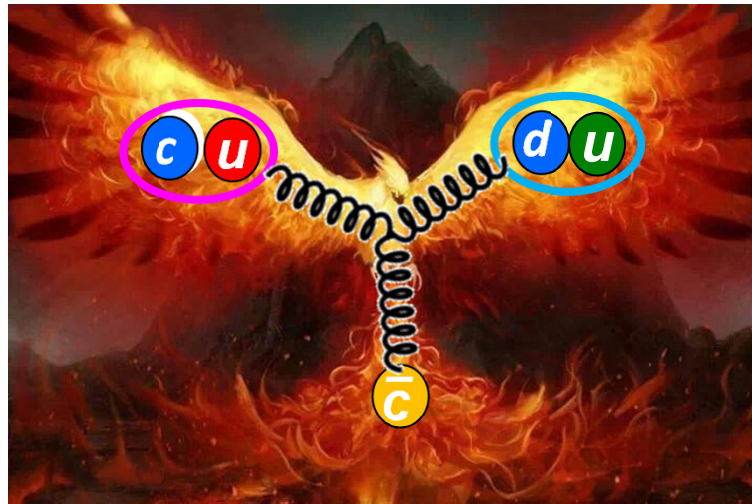


## Outlook to the future

- At present there are many plausible explanations for the observed  $P_c^+$  states.
- The main competition is between tightly bound models based on diquark substructure, loosely bound molecules and rescattering effects.
- Clarifying  $J^P$  values and resonant nature of the discovered  $P_c^+$  states with more statistics will be very important.
- All models predict many other related states to exist. Different models predict different mass spectra. **We badly need to discover more elements of future periodic table of such states!**
- Interactions forming pentaquark states must also play a role in tetraquark states. It is important to pursue both spectroscopies together!
- Searches for states with even more quarks e.g. sextquarks (i.e. dibaryons) interesting.
- **We can do more to test the diquark idea in ordinary baryons! Need experimentalists to do better on identifying all excited baryons.**
- So far the most compelling tetraquark and pentaquark candidates have been discovered with hidden charm inside ( $c\bar{c}$ ). The other heavy quark systems should also be creating bound structures ( $b\bar{b}$ ,  $b\bar{c}$ ,  $c\bar{c}c$ , ...)
- **We are only at the beginning of hopefully very interesting road ahead...**

## Conclusion

- Two pentaquark candidates decaying to  $J/\psi p$  observed by LHCb with overwhelming significance in a state of the art amplitude analysis: they will not go away!



Frank Wilczek's tweet on 7/14/15: "Pentaquarks rise from the ashes: a phoenix pair"

Pentaquark candidates rise from the ashes for the 2<sup>nd</sup> time.

- LHC resurrects them: should not be a surprise given baryon cross-sections.

$c\bar{c}$  pair inside:

- Given the history of Quark Model should not be a surprise either.

**Hopefully true July 2015 revolution!**

- The simplicity of lower mass excitations of mesons and baryons, which led us to the discovery of quarks via  $q\bar{q}$ ,  $qqq$  structures, also misled us to believe that we had already understood hadronic structures. Much experimental and theoretical work remains to be done to achieve this goal.