

A theoretical approach to nuclear parton distributions

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Bio nPDFs SRCs EMC Applications DGLAP End Biographical sketch

- Adam Freese
- Born April 7, 1988
- Undergraduate education: Rensselaer Polytechnic Institute, 2006-2009, BS Physics
- Graduate education: Florida International University, 2010-ongoing (anticipated spring 2016), PhD Physics
- Thesis: Hard QCD processes in the nuclear medium
- Thesis adviser: Misak Sargsian

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- QCD evolution of superfast quarks AF and Misak Sargsian, arXiv:1511.06044 [hep-ph] (2015) (submitted to Phys. Rev. Lett.)
- Probing superfast quarks in nuclei through dijet production at the LHC

AF, Misak Sargsian, and Mark Strikman, European Journal of Physics C**75**, 534 (2015)

• Probing vector mesons in deuteron breakup reactions, AF and Misak Sargsian, Physical Review C88, 044604 (2013)

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Bio **nPDFs** SRCs EMC Applications DGLAP End Nuclear parton distributions

- PDF of the free proton has been studied by many experiments.
- The PDF of the nucleus requires further studies.
- The nuclear PDF is defined using a scaled momentum fraction

$$x_A = A \frac{p_{\text{parton}}^+}{p_A^+}$$

which allows $x_A > 1$.

• $x_A > 1$ is interesting because it is a purely nuclear effect.

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Convolution approach

nPDFs

• For moderate-to-high Q^2 (and $x \gtrsim 0.2$), a convolution equation can be derived:

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$$f_{i/A}(x_A, Q^2) = \sum_N \int_{x_A}^A d\alpha \int d^2 \mathbf{p}_\perp f_{i/N}^{(b)} \left(\frac{x_A}{\alpha}, \alpha, \mathbf{p}_\perp, Q^2\right) f_{N/A}(\alpha, \mathbf{p}_\perp)$$

Applications

- $f_{i/N}^{(b)}\left(\frac{x_A}{\alpha}, \alpha, \mathbf{p}_T, Q^2\right)$ is the **bound nucleon PDF**, which may differ from the free PDF due to medium effects.
- *f*_{N/A}(α, **p**_⊥) is the light cone fraction distribution (LCFD) of the nucleus; it describes nucleonic motion.
- This approach allows $x_A > 1$ depending on how large the LCFD is at $\alpha \gg 1$.
- Measurements of $x_A \gtrsim 1.3$ (meaning $k \gtrsim k_{\text{Fermi}}$) are likely to indicate short range correlations.

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Nuclear light cone fraction distribution

- The LCFD f_{N/A}(α, **p**_⊥) (N = p, n) describes the distribution of nucleons over (scaled) light cone momentum fractions α = A p_N⁺/p_A⁺.
- It satisfies **baryon number conservation** and **momentum conservation**:

$$\begin{split} &\sum_{N=p,n} \int_0^A d\alpha \int d^2 \mathbf{p}_\perp f_{N/A}(\alpha,\mathbf{p}_\perp) = A \\ &\sum_{N=p,n} \int_0^A d\alpha \int d^2 \mathbf{p}_T \alpha f_{N/A}(\alpha,\mathbf{p}_\perp) = A \end{split}$$

• It can be decomposed to parts that contribute to j removed nucleons in the final state:

$$f_{N/A}(\alpha, \mathbf{p}_T) = f_{N/A}^{(1)}(\alpha, \mathbf{p}_{\perp}) + f_{N/A}^{(2)}(\alpha, \mathbf{p}_{\perp}) + f_{N/A}^{(3)}(\alpha, \mathbf{p}_{\perp}) + \dots$$

• These contributions add incoherently because the final states are orthogonal.

• $f_{N/A}^{(1)}(\alpha, \mathbf{p}_{\perp})$ (one-nucleon removal) is due to the **mean field**.

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High-density fluctuations

- Removal of j > 1 nucleons is due to scattering from a short range correlation (SRC) of j nucleons.
- An SRC is a high-density cluster of nucleons localized to short distances (≤ 1 fm).
- Partons can become shared between nucleons in an SRC, allowing e.g. $x_A > 1$ for two-nucleon SRCs.
- SRCs dominate the LCFD above the Fermi momentum $(k \gtrsim 250 \text{ MeV}/c).$



Figure: Subedi et al., Science 320, 1576 (2008)

[arXiv:0908.1514]

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Short range correlations

SRCs

• A short range correlation (SRC) occurs when a few nucleons cluster closely, feeling only each others' influence.

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Applications

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- 2N SRCs occur when two nucleons are closely spaced.
- Due to the small distance, their relative momentum is huge—SRCs dominate when $k \gtrsim 250$ MeV (Fermi momentum).
- The result is a fat tail not reproduced by mean field models.



nPDFs

Two-nucleon SRCs

- The behavior of 2N correlations is universal between nuclei.
- There are scaling plateaus for x ≥ 1.4 in the ratio of 2σ_{eA} to Aσ_{ed}
- There is asymmetric momentum sharing between protons and neutrons, suggesting dominance of *pn* pairs in 2N SRCs.
- 2N SRCs behave like a scaled version of the deuteron momentum distribution, so we use

$$f_{N/A}^{(2)}(\alpha, \mathbf{p}_{\perp}) = \frac{a_2(A)}{2\chi_N} \frac{|\psi_d(k)|^2}{\alpha(2-\alpha)} E_k \Theta(k-k_F)$$

where χ_N is the relative fraction of the nucleon type, and

$$k=\sqrt{\frac{m^2+p_{\perp}^2}{\alpha(2-\alpha)}-m^2}$$

is the internal light cone momentum.

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Figure: Fomin et al. PRL 108, 092502 (2012) [arXiv:1107.3583]









- We model 3N SRCs as arising from two subsequent 2N SRCs.
- Model accounts for pn dominance. ۲
- Characteristic topology on right. ٢
- Effective Feynman rules with effective vertices used.

- 3N correlations are expected to exist for $\alpha > 2$ (and $x_A > 2$).
- Experimental status in quasi-elastic scattering experiments is uncertain and contradictory.



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Three-nucleon SRCs

Three-nucleon SRCs are expected to exist for $\alpha > 2$. Our calculation has found:

$$f_{N/A}^{(3)}(\alpha, \mathbf{p}_{\perp}) = \{a_2(A)\}^2 \frac{1}{\alpha} \int \frac{d\alpha_3 d^2 \mathbf{p}_{3\perp}}{\alpha_3(3 - \alpha - \alpha_3)} \left\{ \frac{3 - \alpha_3}{2(2 - \alpha_3)} \right\}^2$$
$$\overline{|\psi_d(k_{23})|^2} \Theta(k_{23} - k_F) \overline{|\psi_d(k_{12})|^2} \Theta(k_{12} - k_F)$$



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Medium Modifications

• Let's try using the $f_{N/A}(x, Q^2)$ we've found and a free nucleon PDF.



•
$$\mathcal{R} = \frac{2}{A} \frac{\sigma_{eA}(x,Q^2)}{\sigma_{ed}(x,Q^2)}$$

- A free nucleon parametrization[†] is used.
- [†]: Bodek and Ritchie, Phys. Rev. **D**24, 1400 (1981).

- The fit is bad, so medium modification is needed.
- The fit with SRCs is worse, so SRCs must be more highly modified.

EMC effect: in-medium modification



Figure from Gomez et al., PRD 49, 4348 (1994).

- The dip in this ratio has been seen in many experiments.
- First seen by European Muon Collaboration in 1983; called the EMC effect.
- Strength of effect proportional to local nuclear density.
- Streight of effect believed to be proportional to nucleon virtuality, and thus to p^2 .
- Effect may thus be stronger in exclusive reactions where probed nucleon's p^2 is not integrated over.
- More modification expected in SRCs; nucleons in SRCs have higher momentum.

For estimation, I use one example of a medium modification model.

- The nucleon's internal wave function includes configurations of many sizes.
- It includes configurations that are tiny compared to average nucleon sizes.
- These are called **p**oint like **c**onfigurations.
- PLCs are more transparent to the strong nuclear force than average-sized configurations.
- They are suppressed in strongly-interacting media, since systems tend towards lower-energy states.



Average-sized configuration: not suppressed



Point-like configuration: suppressed

A suppression of small configurations means a suppression of high momentum (and high x) in the PDF; at $x \gtrsim 0.6$:

$$f_{i/N}^{(\text{bound})}(x,Q^2,p^2) = \frac{1}{(1+z)^2} f_{i/N}^{(\text{free})}(x,Q^2) \qquad \qquad z = \frac{p^2/m_N^2 + 2\epsilon_A}{\Delta E_A}$$

 ϵ_A is binding energy per nucleon and ΔE_A a characteristic nucleon excitation energy

This is called the color screening model of the EMC effect. cf. Frankfurt and Strikman, Nucl. Phys. **B**250 (1985), 143

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Color screening model

- The color screening model fits the EMC data well.
- Sample: ⁵⁶Fe at $Q^2 = 10$ GeV². Data are from papers by Gomez and Albert.
- The low- $x \lesssim 0.2$ is due to different dynamics (outside the scope of this research).



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Applications of nuclear PDFs

$$f_{i/A}(x_A, Q^2) = \sum_N \int_{x_A}^A d\alpha \int d^2 \mathbf{p}_\perp f_{i/N}^{(b)} \left(\frac{x_A}{\alpha}, \alpha, \mathbf{p}_\perp, Q^2\right) f_{N/A}(\alpha, \mathbf{p}_\perp)$$

- This formalism for nuclear PDFs has many potential applications:
 - **()** Dijet production in pA collisions (to probe SRCs).
 - \bigcirc eA scattering (inclusive and semi-inclusive) at high (EIC) energies.
 - **③** Drell-Yan processes in pA collisions.
- I will focus on pA collisions at LHC energies here.

cf. AF, Sargsian, and Strikman, Eur. Phys. J. C **75**, 534 (2015) [arXiv:1411.6605] for a detailed account.

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- $pA \rightarrow 2$ jets + X occurs (at leading order) through a two-body to two-body partonic reaction.
- The reaction is described by four kinematic parameters: E_0 (energy per proton), η_3 , η_4 , and p_T .
- From these, the light cone momentum fractions x of the initial partons are:

1
$$x_p = \frac{p_T}{2E_0} (e^{+\eta_3} + e^{+\eta_4})$$
 from proton.

2
$$x_A = \frac{Ap_T}{2ZE_0} (e^{-\eta_3} + e^{-\eta_4})$$
 from nucleus.

• Since the motion of N is unknown and variable, all parameters (e.g. rapidities) are given in the collider reference frame.

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Large x_A at the LHC

The big question is: can we find large x_A at the LHC? (Would indicate SRCs.)

$$x_A = \frac{Ap_T}{2ZE_0} \left(e^{-\eta_3} + e^{-\eta_4} \right)$$

Since $\eta_4 < 0$ and $\eta_3 > 0$ are most likely, we should look for:

- Large p_T .
- Small $|\eta_3|$. Jet from proton should be central.
- Large |η₄|. Jet from nucleus should be forward.



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• The cross section for $pA \rightarrow 2$ jets + X factorizes as such:

$$\sigma_{pA} = \sum_{ijkl} \int_0^1 dx_p \int_0^A dx_A f_{i/p}(x_p, Q^2) f_{j/A}(x_A, Q^2) \hat{\sigma}_{ij \to kl}$$

- $Q^2 = p_T^2$ (transverse jet momentum) minimizes NLO, N²LO, etc. corrections.
- This leads to a differential cross section of

$$\frac{d^3\sigma_{pA}}{d\eta_3 d\eta_4 dp_T^2} = \frac{1}{16\pi} \frac{1}{\left(4E_0^2 \frac{Z}{A}\right)^2} \frac{f_{i/p}(x_p, p_T^2)}{x_p} \frac{f_{j/A}(x_A, p_T^2)}{x_A} \frac{\overline{\left|\mathcal{M}_{ij\to kl}\right|^2}}{1+\delta_{kl}}$$

- $\mathcal{M}_{ij \to kl}$ is the tree-level matrix element for a parton-level process.
- The main theoretical issue is the nuclear PDF $f_{j/A}(x, p_T^2)$.
- But this is found by evolving the moderate-Q² nPDF found previously.

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Bio nPDFs SRCs EMC Applications DGLAP End Evolving medium-modified PDFs

- The color screening model was developed at moderate $Q^2 \sim 10 \text{ GeV}^2$.
- For nuclear PDFs at high Q^2 (e.g. 10^4 GeV^2), use QCD evolution.



The EMC effect evolves little, but fast parton motion evolves a lot.
 Since fast partons lose some of their x, the PDF shifts to the left with evolution.
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Numerical estimates of dijet cross section

Numerical estiamtes of the three-fold cross section



SRCs significantly increase differential cross section at x_A ≥ 1.
Medium modifications suppress cross section at high x_A.

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We have numerical predictions for the integrated cross section.

	Unmodified (SRCs)	Modified (no SRCs)	Modified (SRCs)
All x_A	$7.8~\mu{ m b}$	$6.8 \ \mu b$	$6.9~\mu \mathrm{b}$
$0.6 < x_A < 0.7$	$0.94 \ \mu b$	$0.73 \ \mu \mathrm{b}$	$0.72 \ \mu \mathrm{b}$
$0.7 < x_A < 0.8$	$0.38 \ \mu \mathrm{b}$	$0.25 \ \mu b$	$0.27 \ \mu \mathrm{b}$
$0.8 < x_A < 0.9$	$0.17 \ \mu b$	$0.07 \ \mu \mathrm{b}$	$0.08~\mu{ m b}$
$0.9 < x_A < 1$	36 nb	14 nb	21 nb
$1 < x_A$	12 nb	2.3 nb	5.7 nb

The expected yield for $x_A > 1$ events at the LHC is 200 events for a month of run time.

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Bio nPDFs SRCs EMC Applications DGLAP End QCD evolution for nuclei

• A modified version of the DGLAP equation is used for nPDFs:

$$\frac{\partial f_{i/A}(x_A, Q^2)}{\partial \log(Q^2)} = \sum_j \frac{\alpha_s}{2\pi} \int_{x_A}^A \frac{dy}{y} f_{j/A}(y, Q^2) P_{ij}\left(\frac{x}{y}\right)$$

where P_{ij} are the Altarelli-Parisi splitting functions.

- The upper integration limit is A rather than 1.
- This means $x_A > 1$ partons at low Q^2 can become $x_A < 1$ partons as Q^2 is increased.
- This also gives a way of making $x_A > 1$ predictions at very high Q^2 using lower- Q^2 , high-precision measurements.

Evolution of structure functions

• Evolution of the structure function

$$F_{2A}(x_A, Q^2) = \sum_i e_i^2 \left(q_{i/A}(x_A, Q^2) + \bar{q}_{i/A}(x_A, Q^2) \right)$$

Applications

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is relevant to connecting moderate- and high- Q^2 DIS experiments.

 At leading order, and at x ≥ 0.2 where gluons can be neglected, we derive a single evolution equation for F_{2A}(x, Q²):

$$\frac{\partial F_{2A}(x,Q^2)}{\partial \log Q^2} = \frac{\alpha_s}{2\pi} \left\{ 2\left(1 + \frac{4}{3}\log\left(1 - \frac{x}{A}\right)\right) F_{2A}(x,Q^2) + \frac{4}{3} \int_{x/A}^1 \frac{dz}{1-z} \left(\frac{1+z^2}{z} F_{2A}\left(\frac{x}{z},Q^2\right) - 2F_{2A}(x,Q^2)\right) \right\}$$

• This is a **model-independent** way of connecting high- x_A DIS measurements at different Q^2 .

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- $F_{2A}(x, Q^2)$ evolution can connect high-precision JLab measurements on ¹²C to high- Q^2 measurements from the BCDMS and CCFR collaborations.
- JLab measurements from Hall C are done at Q^2 from 2-9 GeV².
- Target mass corrections and higher-twist corrections must be accounted for.
- TMCs are accounted for by ξ -scaling; we evolve $F_{2A}^{LT}(\xi_A, Q^2)$, where:

$$\xi_A = \frac{2x_A}{1 + \sqrt{1 + \frac{4x_A^2 M_A^2}{A^2 Q^2}}}$$

- ξ -scaling as a TMC method minimizes Q^2 dependence of the data.
- HT corrections are accounted for with a fit:

$$F_{2A}^{\rm HT}(x_A, Q^2) = \left(1 + \frac{C(\xi_A)}{Q^2}\right) F_{2A}^{\rm LT}(x_A, Q^2)$$

• HT fit accommodates any differences between TMC methods.

Example: evolution of the ${}^{12}C$ structure function

- $x_A > 1$ evolution can connect JLab¹ measurements for ¹²C to high- Q^2 measurements from BCDMS² and CCFR³.
- In this case, target mass corrections and higher-twist corrections are also accounted for.
- Dashed curves are QCD evolution of a parametrization from the JLab group.
- Solid curves are QCD evolution where target mass and higher-twist corrections have been accounted for.
- The evolved curves fall between the contradictory CCFR and BCDMS data.
- ¹ Fomin et al., PRL105, 212502 (2010)
 ² Benvenuti et al., Z. Phys. C 63, 29 (1994)
 ³ Vakili et al., PRD61, 052003 (2000)

See AF and Sargsian, [arXiv:1511.06044], for more detail.



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Summary and outlook

- $\bullet\,$ This formalism has other potential applications besides pA collisions:
 - \bigcirc eA scattering (inclusive and semi-inclusive) at high (EIC) energies.
 - **2** Drell-Yan processes in pA and AA collisions.
- \bullet PDFs for other nuclei besides $^{56}\mathrm{Fe}$ and $^{208}\mathrm{Pb}$ can be calculated.
 - We will perform a fully theoretical calculation for ¹²C to supplement the evolution calculation from JLab measurements.
 - We have a realistic wave function for ³He to which this formalism will also be applied.
- It should be possible to generalize this to semi-inclusive DIS, in order to investigate nuclear transverse momentum distributions.

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