

# A path into TMD phenomenology

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Andrea Signori



# About the speaker

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## 2012 - Master student

“Hadron structure and QCD” group, Pavia U. (IT)  
Phenomenology of unpolarized TMDs at COMPASS

collaborators

A. Bacchetta [supervisor], M. Radici



## 2012 - Summer intern

DESY - Hermes collaboration (GE)

Transverse double spin asymmetry in inclusive hadron production

collaborators

G. Schnell [supervisor], A. Movsisyan

# About the speaker

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## 2012 - present | PhD candidate

Nikhef and Vrije Universiteit Amsterdam (NL)

Theory and phenomenology of TMDs

main collaborators

P.J. Mulders (supervisor), T. Kasemets, M. Ritzmann (VU, Nikhef)

A. Bacchetta, M. Radici (Pavia - IT)

M. Echevarria (Barcelona - ES)

C. Pisano (Antwerp - BE)

J.P. Lansberg (Orsay - FR)

The logo for Quantum Diaries, featuring the text "QUANTUM DIARIES" in a white, sans-serif font on a dark blue rectangular background. Below the text is a smaller line of text: "Thoughts on work and life from particle physicists from around the world."

QUANTUM DIARIES

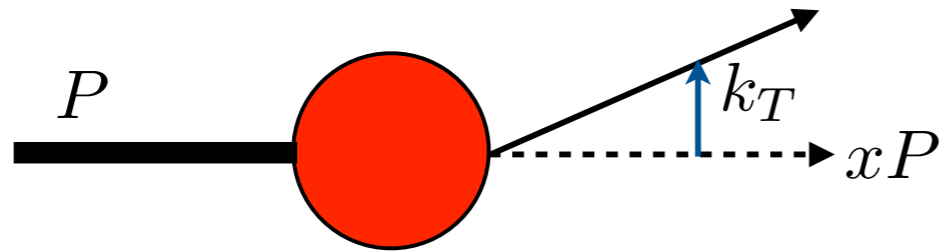
Thoughts on work and life from particle physicists from around the world.

## 2014 - present | blogger

“Quantum Diaries” (Interaction collaboration)

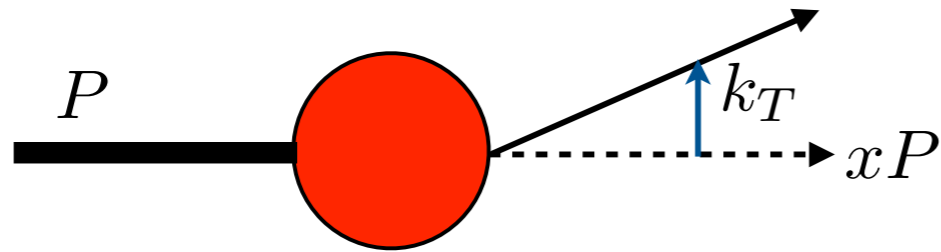
Thoughts on work and life from particle physicists around the world

# Quark TMD PDFs



extraction of a **quark**  
**not** collinear with the proton

# Quark TMD PDFs



extraction of a **quark**  
**not** collinear with the proton

a similar scheme  
holds for fragmentation  
and for gluons  
in Lorentz space

nucleon pol.

quark pol.

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

**spin-spin** and **spin-orbit**  
interactions

Twist-2 TMDs

# How to access TMDs ?

flavor structure of unpolarized quark TMDs

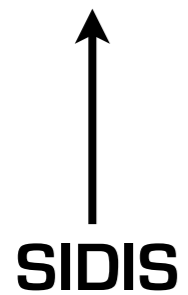


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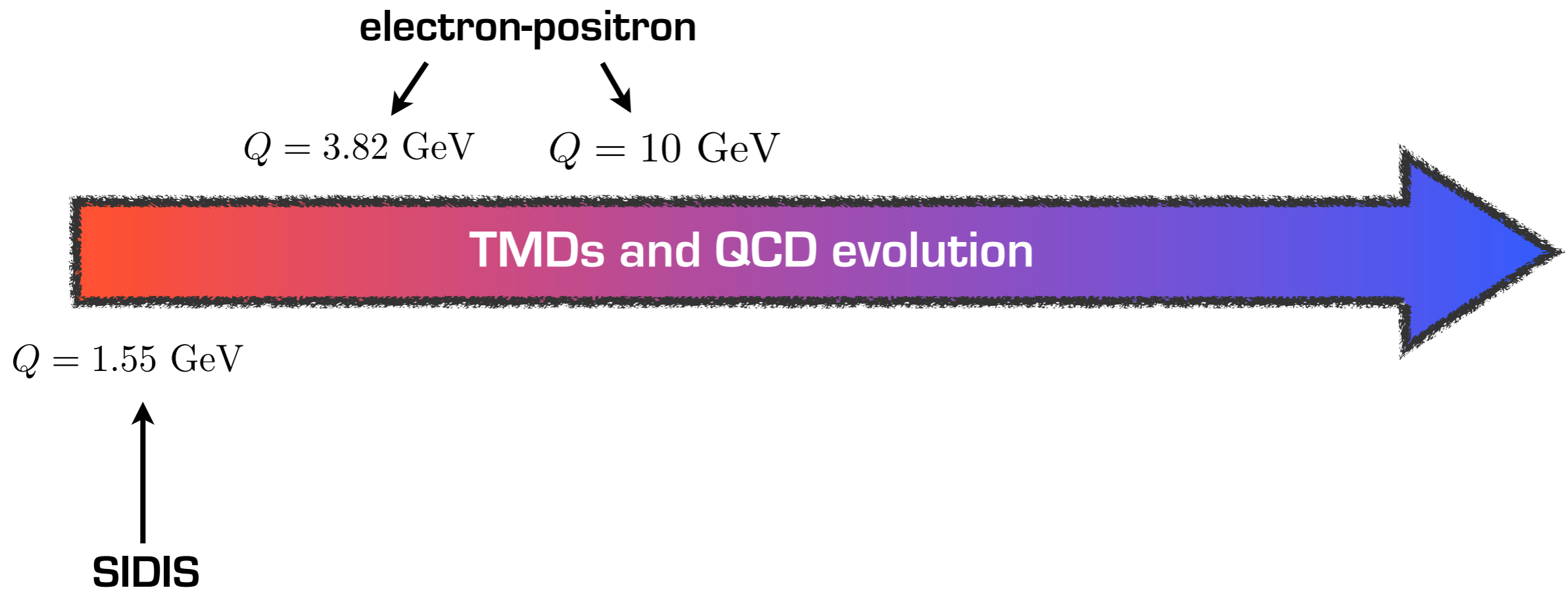


$Q = 1.55 \text{ GeV}$



# How to access TMDs ?

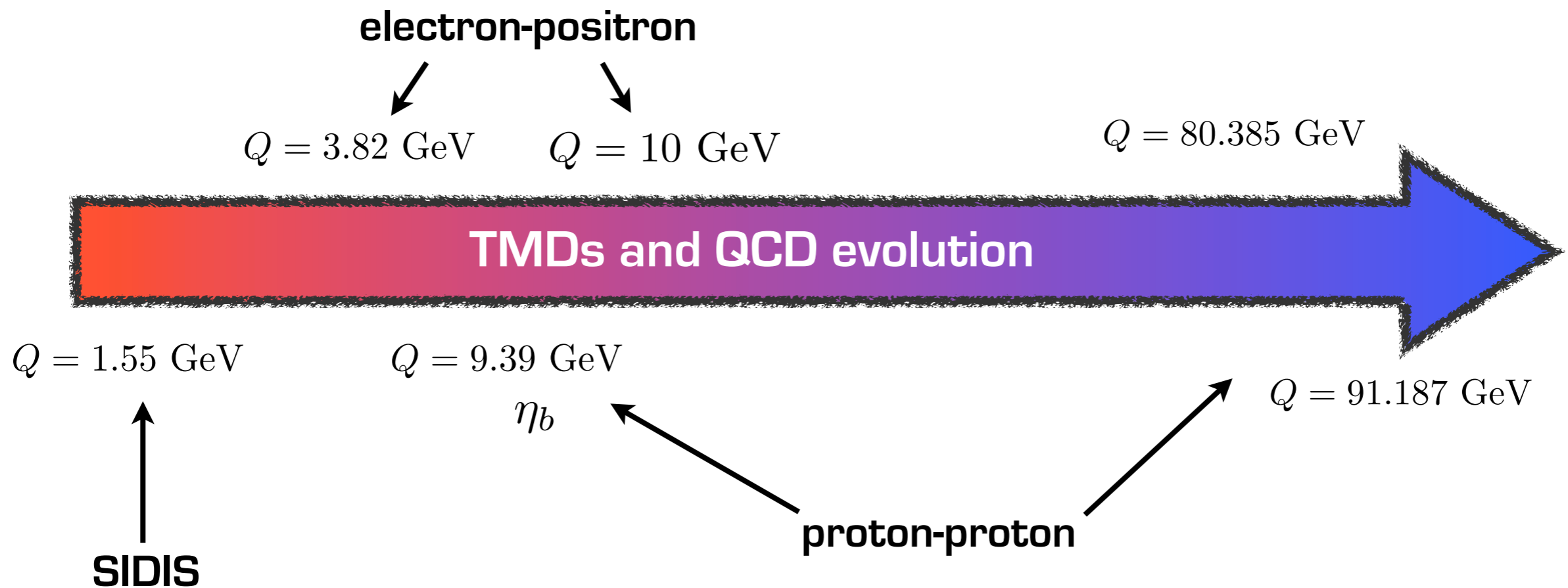
flavor structure of unpolarized quark TMDs





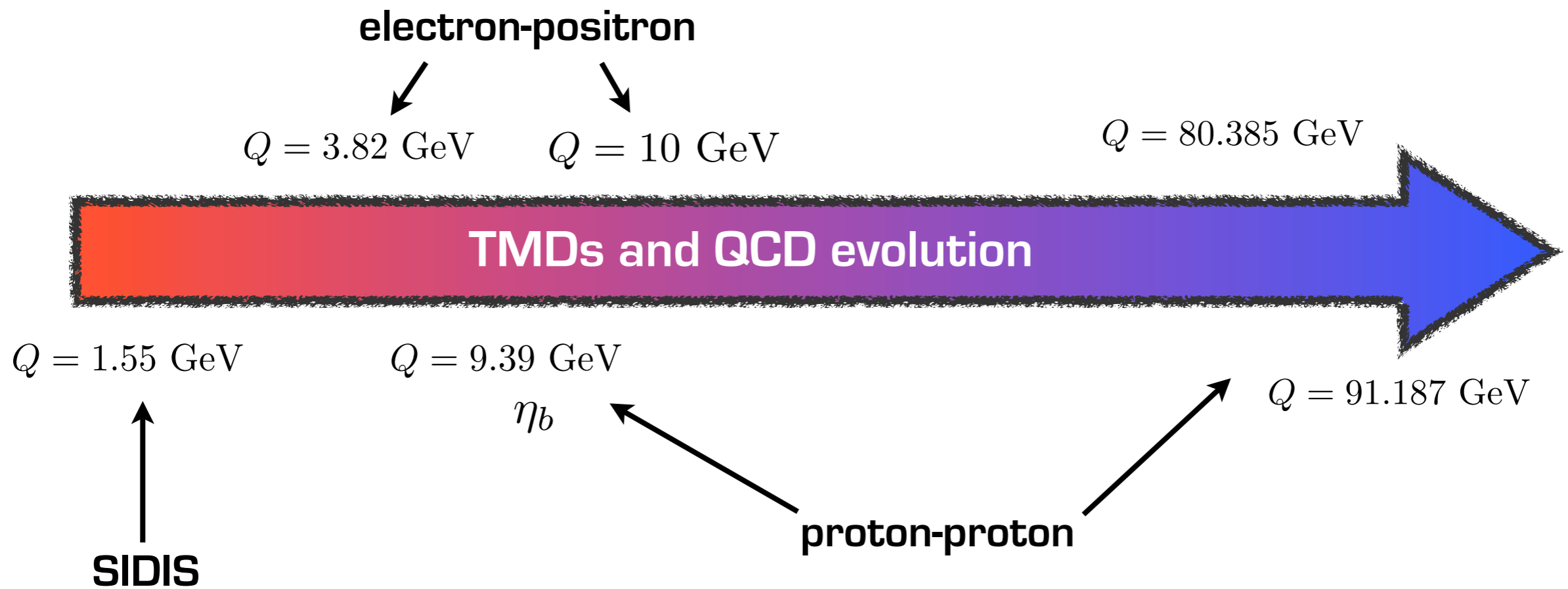
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flavor structure of unpolarized quark TMDs



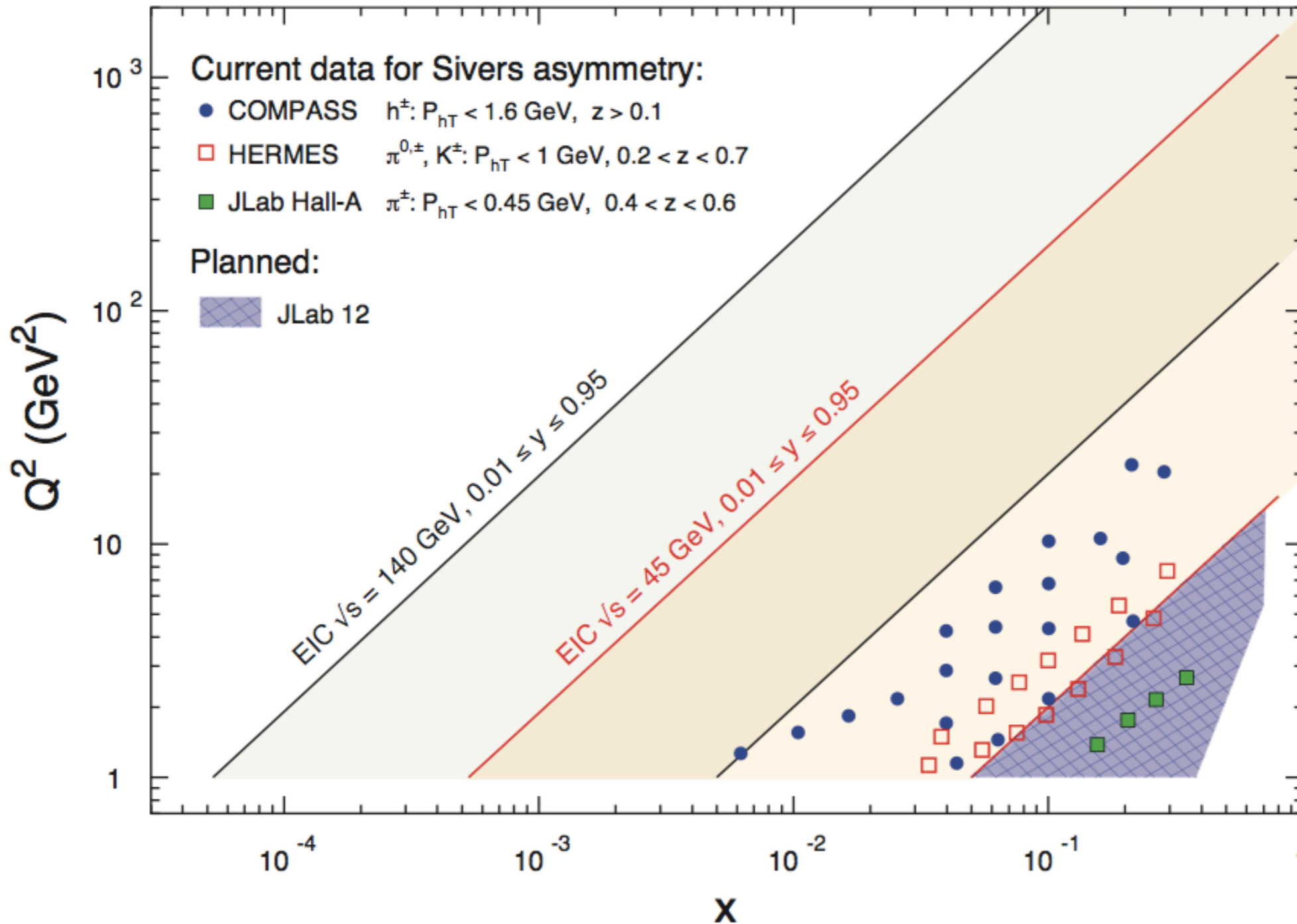
# How to access TMDs ?

flavor structure of unpolarized quark TMDs



... and **new TMDs** !

# How to access TMDs ?



**Jefferson Lab**

- high  $x$
- high luminosity and statistic
- multidimensional analysis

$$e^{\pm} + P/D \longrightarrow e^{\pm} + \pi^{\pm}/K^{\pm} + X$$

## TMDs at work in SIDIS

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references :

**AS**, Bacchetta, Radici, Schnell  
[10.1007/JHEP11\(2013\)194](https://arxiv.org/abs/10.1007/JHEP11(2013)194)

Bacchetta, Radici, **AS**  
[10.1142/S2010194514600209](https://arxiv.org/abs/10.1142/S2010194514600209)

# Transverse momenta

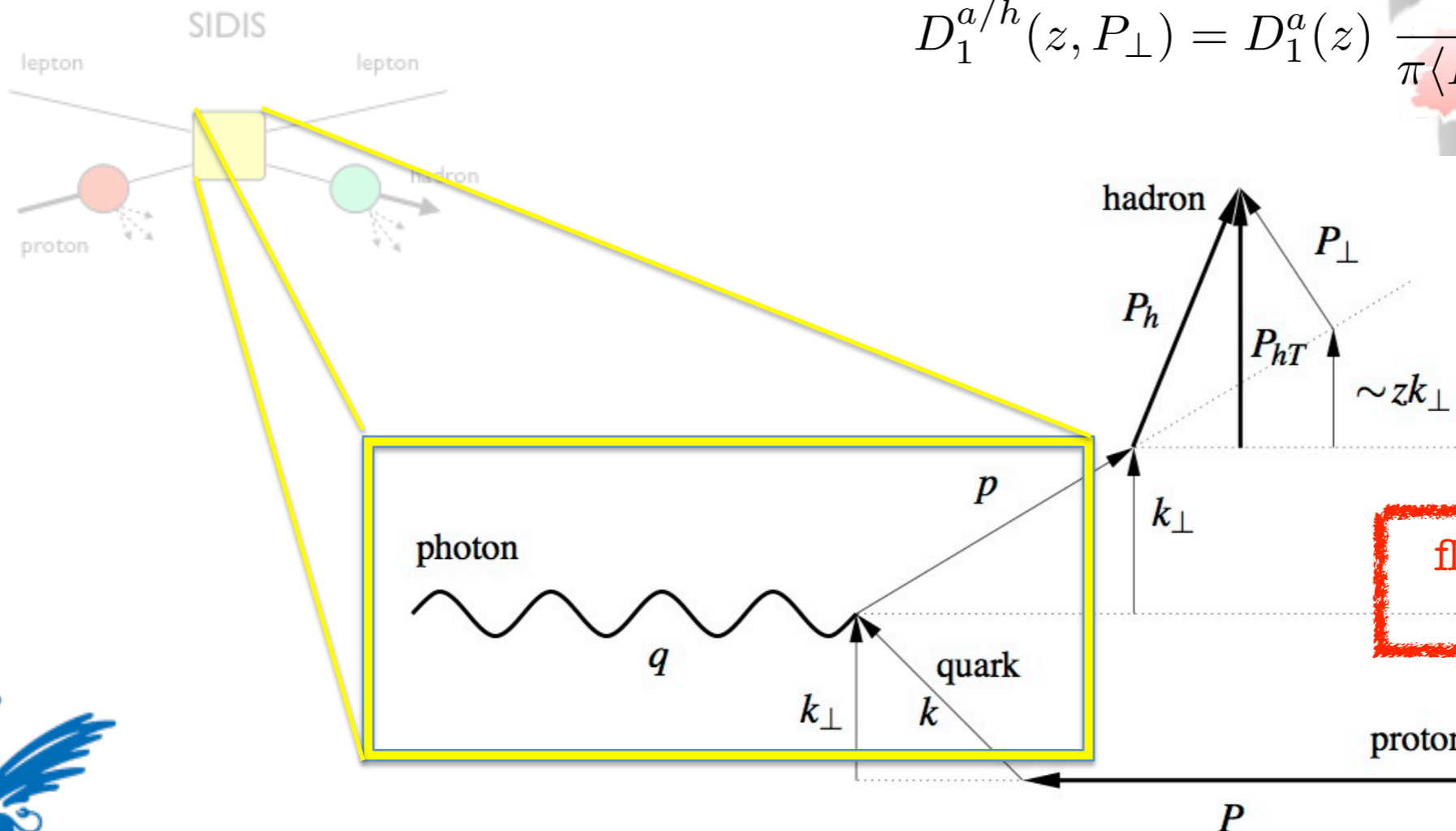
$$\sigma(P_{hT}^2) \sim \sum_a f_1^a(x, k_\perp^2) \otimes D_1^{a \rightarrow h}(z, P_\perp^2)$$

$$\langle P_{hT,q}^2 \rangle = z^2 \langle k_{\perp,q}^2 \rangle + \langle P_{\perp,q/h}^2 \rangle$$

Gaussian distributions

$$f_1^a(x, k_\perp) = f_1^a(x) \frac{1}{\pi \langle k_\perp^2 \rangle_a(x)} e^{-\frac{k_\perp^2}{\langle k_\perp^2 \rangle_a(x)}}$$

$$D_1^{a/h}(z, P_\perp) = D_1^a(z) \frac{1}{\pi \langle P_\perp^2 \rangle_{a/h}(z)} e^{-\frac{P_\perp^2}{\langle P_\perp^2 \rangle_{a/h}(z)}}$$



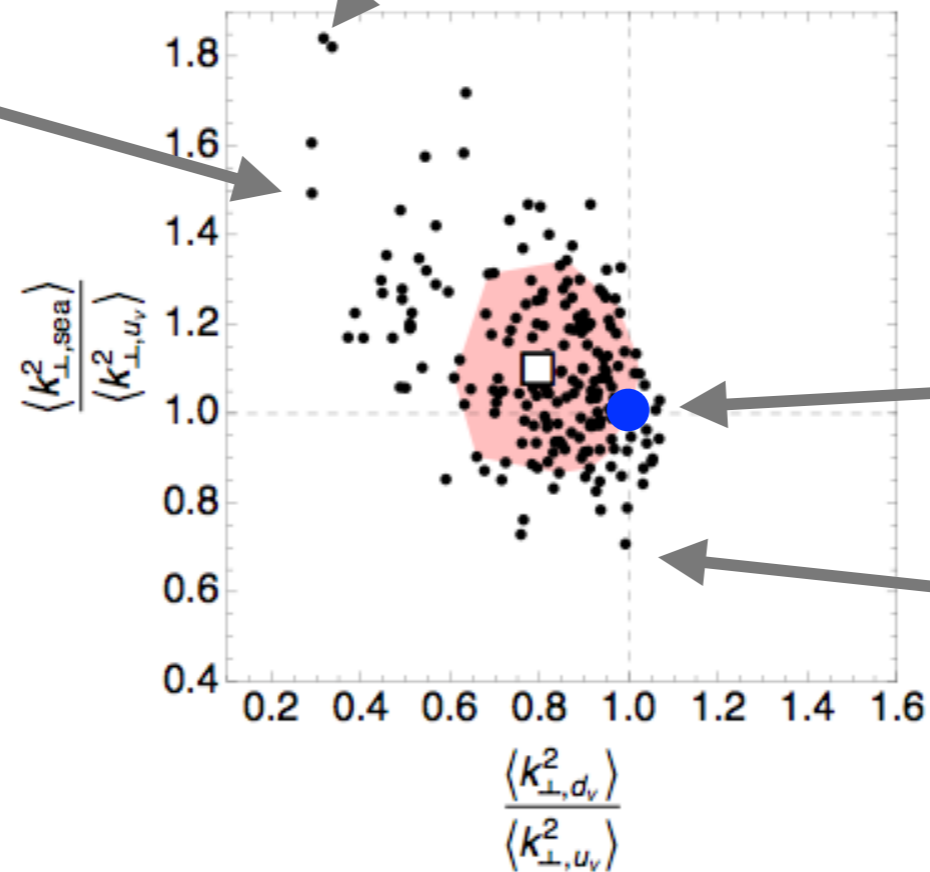
flavor- and kinematic-  
dependent widths

# Flavor dependent TMD PDFs

$$\langle k_{\perp,u_v}^2 \rangle \neq \langle k_{\perp,d_v}^2 \rangle \neq \langle k_{\perp,sea}^2 \rangle$$

replica 73  
 $\chi^2/\text{dof} = 1.70$

replica 149  
 $\chi^2/\text{dof} = 1.87$



replica 130  
 $\chi^2/\text{dof} = 1.77$

replica 186  
 $\chi^2/\text{dof} = 1.38$

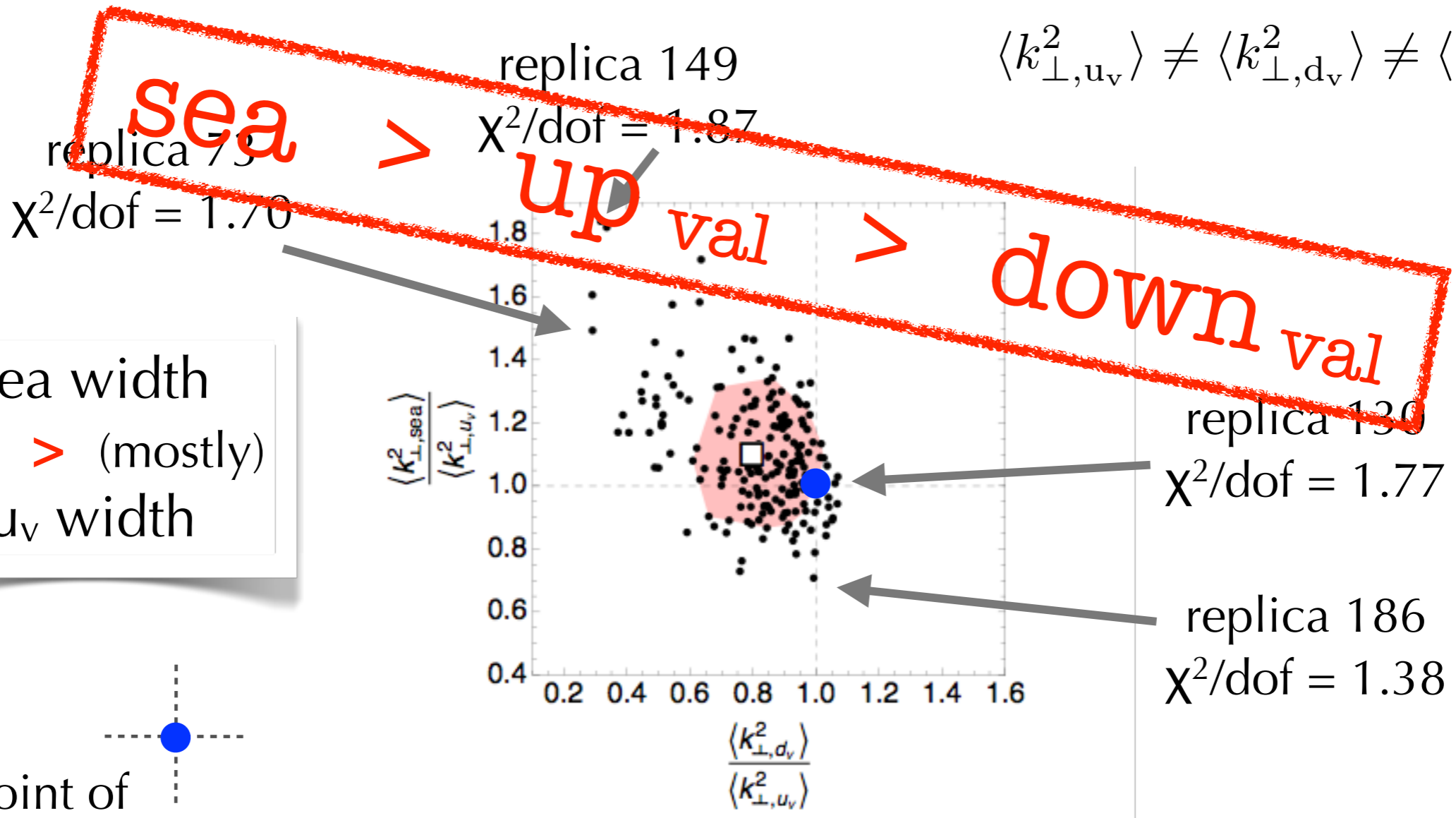
sea width  
 $>$  (mostly)  
 $u_v$  width

point of  
 no flavor dep.

$d_v$  width  $<$  (mostly)  $u_v$  width

# Flavor dependent TMD PDFs

$$\langle k_{\perp,u_v}^2 \rangle \neq \langle k_{\perp,d_v}^2 \rangle \neq \langle k_{\perp,sea}^2 \rangle$$



sea width  
 > (mostly)  
 $u_v$  width

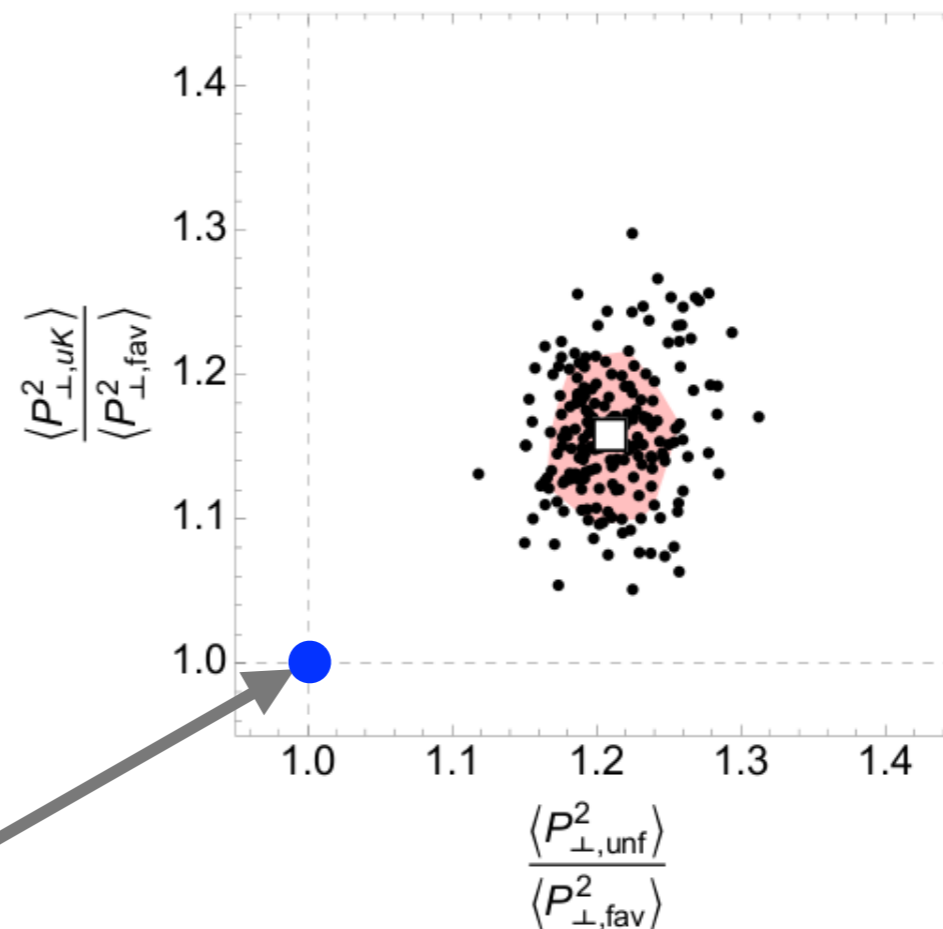
point of  
 no flavor dep.

$d_v$  width < (mostly)  $u_v$  width

# Flavor dependent TMD FFs

$$\begin{aligned} \langle P_{\perp, u \rightarrow \pi^+}^2 \rangle &= \langle P_{\perp, \bar{d} \rightarrow \pi^+}^2 \rangle = \langle P_{\perp, \bar{u} \rightarrow \pi^-}^2 \rangle = \langle P_{\perp, d \rightarrow \pi^-}^2 \rangle \equiv \langle P_{\perp, \text{fav}}^2 \rangle, \\ \langle P_{\perp, u \rightarrow K^+}^2 \rangle &= \langle P_{\perp, \bar{u} \rightarrow K^-}^2 \rangle \equiv \langle P_{\perp, uK}^2 \rangle, \\ \langle P_{\perp, \bar{s} \rightarrow K^+}^2 \rangle &= \langle P_{\perp, s \rightarrow K^-}^2 \rangle \equiv \langle P_{\perp, sK}^2 \rangle, \\ \langle P_{\perp, \text{all others}}^2 \rangle &\equiv \langle P_{\perp, \text{unf}}^2 \rangle. \end{aligned}$$

$q \rightarrow \pi$  favored width  
 $<$   
 $q \rightarrow K$  favored width



● point of  
 no flavor dep.

$q \rightarrow \pi$  favored width  $<$  unfavored

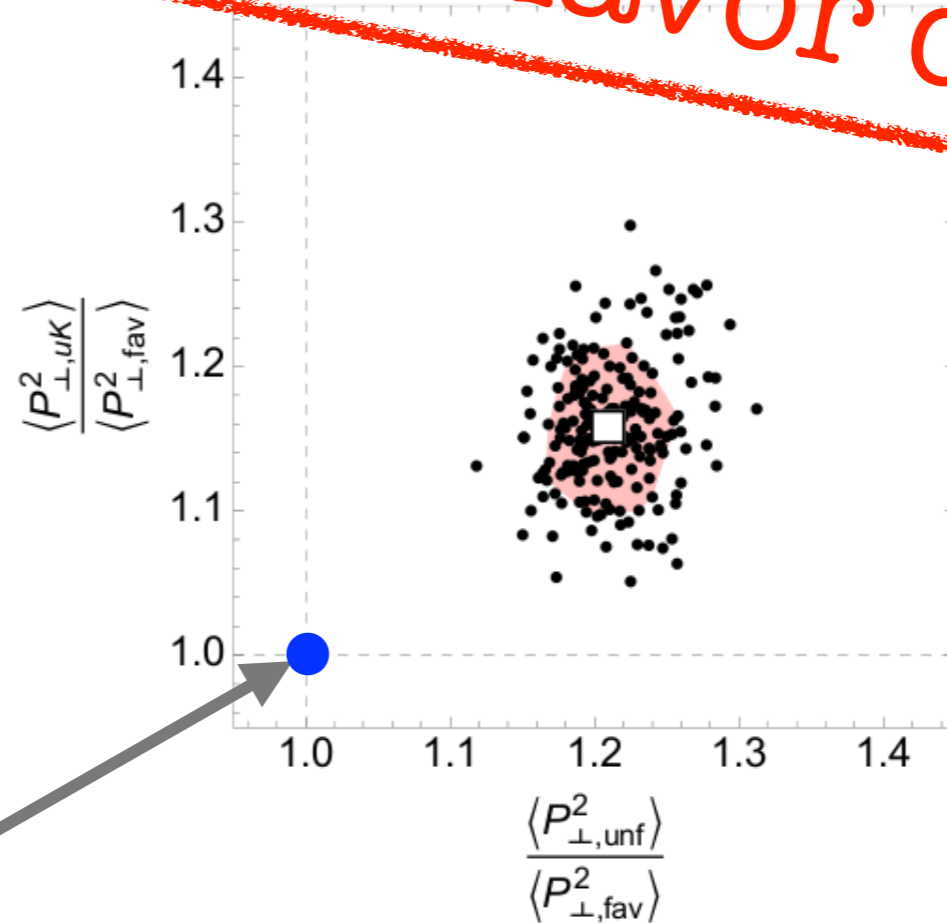


# Flavor dependent TMD FFs

$$\begin{aligned} \langle P_{\perp, u \rightarrow \pi^+}^2 \rangle &= \langle P_{\perp, \bar{d} \rightarrow \pi^+}^2 \rangle = \langle P_{\perp, \bar{u} \rightarrow \pi^-}^2 \rangle = \langle P_{\perp, d \rightarrow \pi^-}^2 \rangle \equiv \langle P_{\perp, \text{fav}}^2 \rangle \\ \langle P_{\perp, u \rightarrow K^+}^2 \rangle &= \langle P_{\perp, \bar{u} \rightarrow K^-}^2 \rangle \equiv \langle P_{\perp, uK}^2 \rangle, \\ \langle P_{\perp, \bar{s} \rightarrow K^+}^2 \rangle &= \langle P_{\perp, s \rightarrow K^-}^2 \rangle \equiv \langle P_{\perp, sK}^2 \rangle, \\ \langle P_{\perp, \text{all others}}^2 \rangle &\equiv \langle P_{\perp, \text{unf}}^2 \rangle. \end{aligned}$$

good evidence for flavor dep.

$q \rightarrow \pi$  favored width  
 $<$   
 $q \rightarrow K$  favored width



● point of no flavor dep.

$q \rightarrow \pi$  favored width  $<$  unfavored

# TMDs at work in $e^+e^-$

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references :

Bacchetta, Echevarria, Mulders, Radici, **AS**

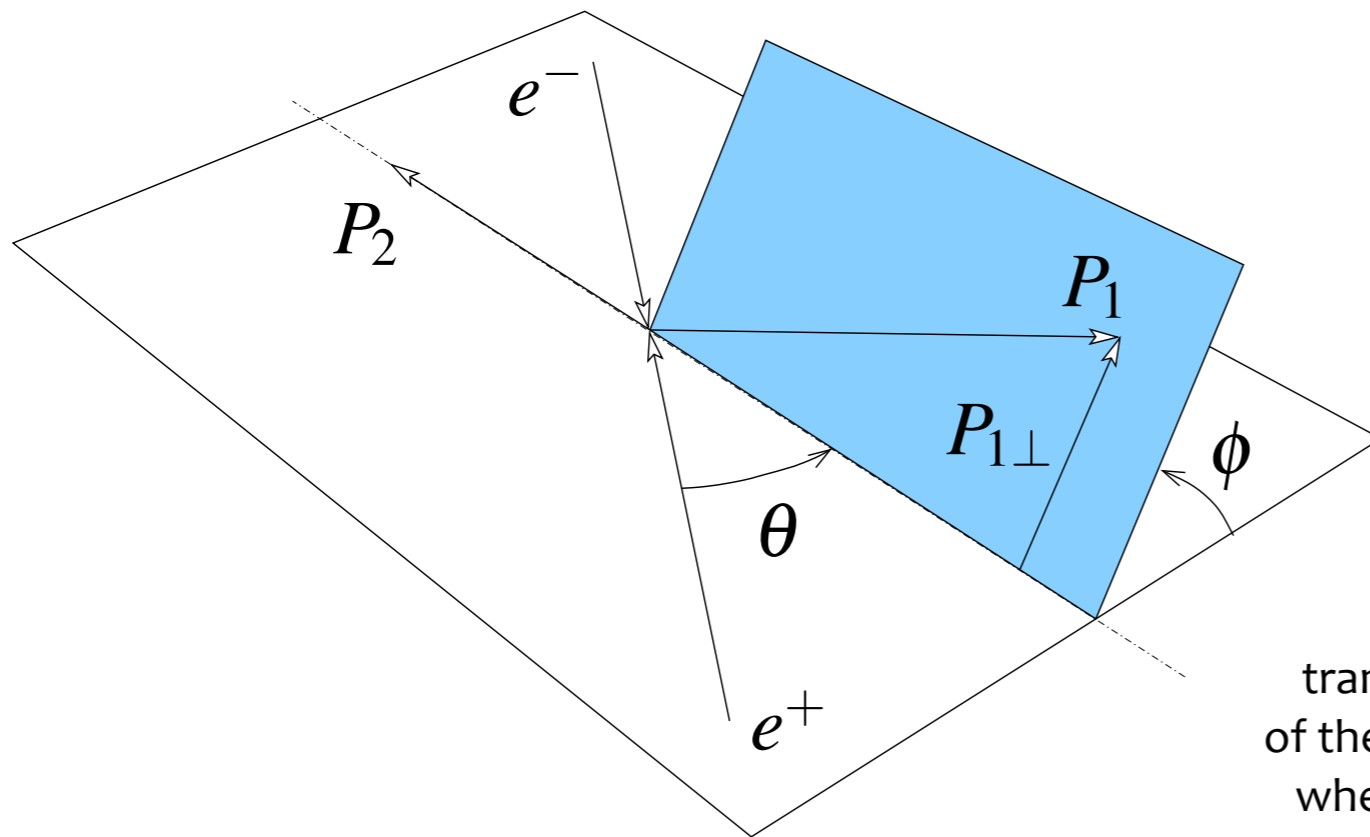
[10.1007/JHEP11\(2015\)076](https://arxiv.org/abs/1506.07623)

Bacchetta, Echevarria, Radici, **AS**

[10.1142/S201019451560023X](https://arxiv.org/abs/1506.07623)

[10.1051/epjconf/20158502016](https://arxiv.org/abs/1506.07623)

# Kinematics and observables



e+e- CM frame:  
production of **two back-to-back jets**  
with leading hadrons h1 and h2

h1 only has transverse momentum wrt to z

$$q_T^\mu = -\frac{P_{1\perp}^\mu}{z_1} + O\left(\frac{M^2}{Q^2}\right)$$

transverse momentum of the photon in the frame where h1,2 are collinear

transverse momentum of h1 wrt photon

The observable: **normalized multiplicity**,  
**poorly sensitive to perturbative corrections**

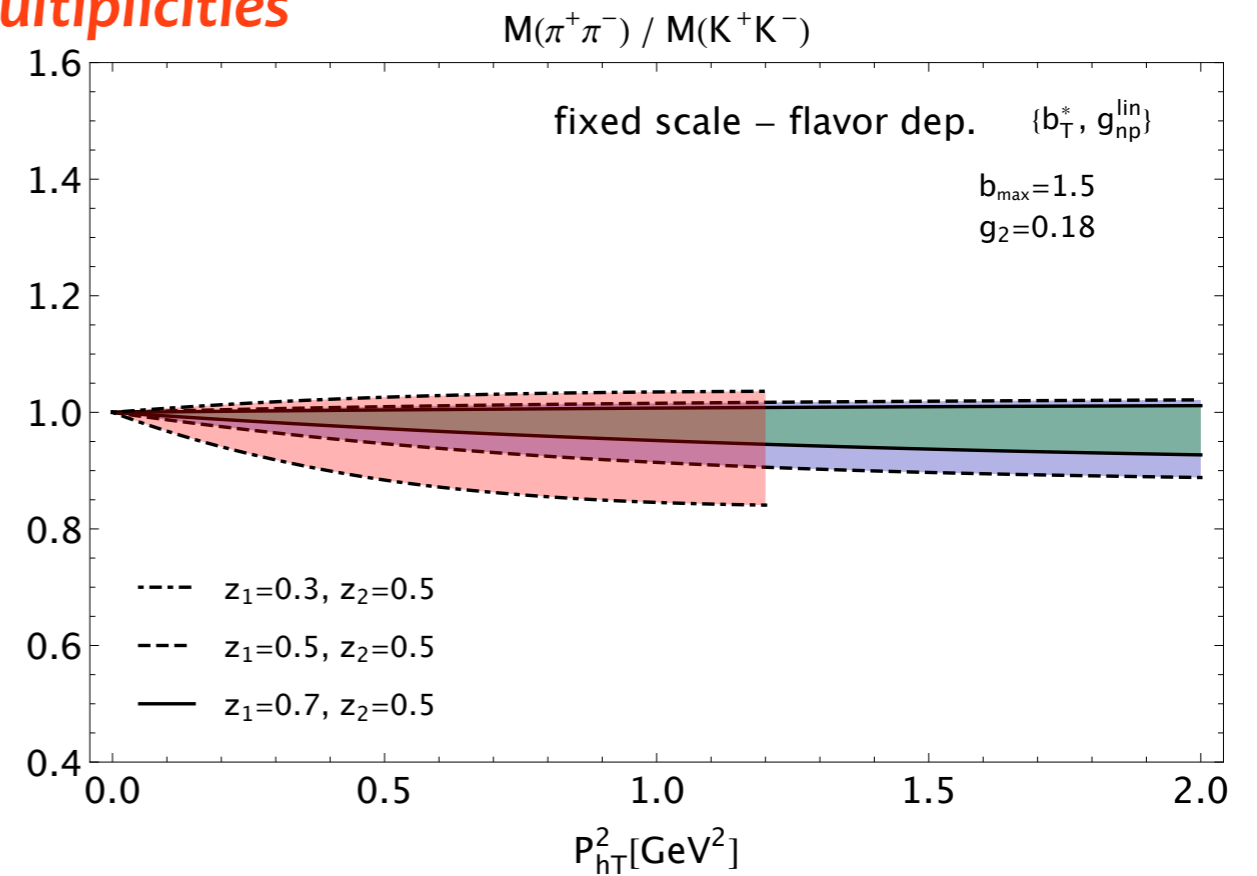
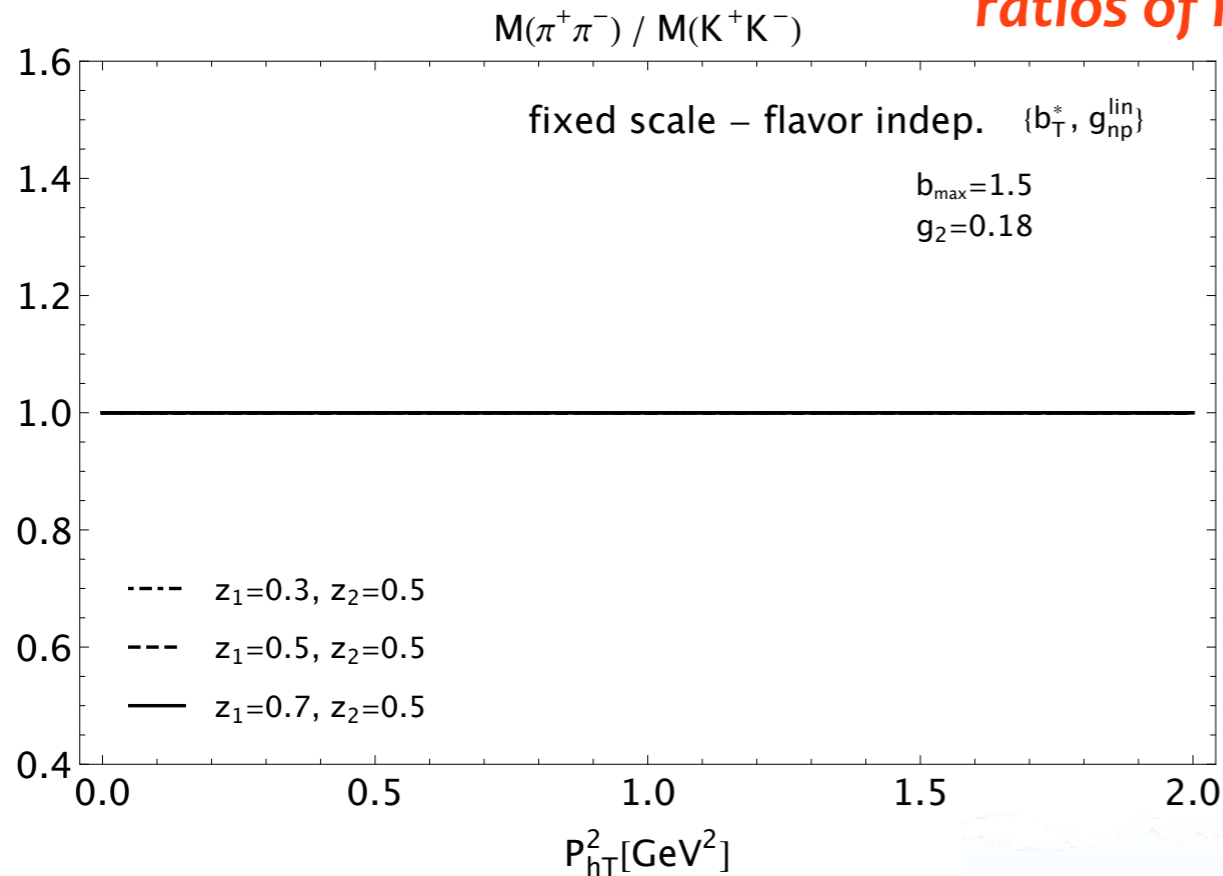
$$M^{h_1 h_2}(z_1, z_2, q_T^2, y) / M^{h_1 h_2}(z_1, z_2, 0, y)$$

Multiplicity,  
defined as in SIDIS

$$M^{h_1 h_2}(z_1, z_2, q_T^2, y) = \frac{d\sigma^{h_1 h_2}}{dz_1 dz_2 dq_T^2 dy} / \frac{d\sigma^{h_1}}{dz_1 dy}$$

# Partonic flavor

## ratios of multiplicities



being **flavor independent**  
they factor out and cancel:

no  $q_T$  dependence is left

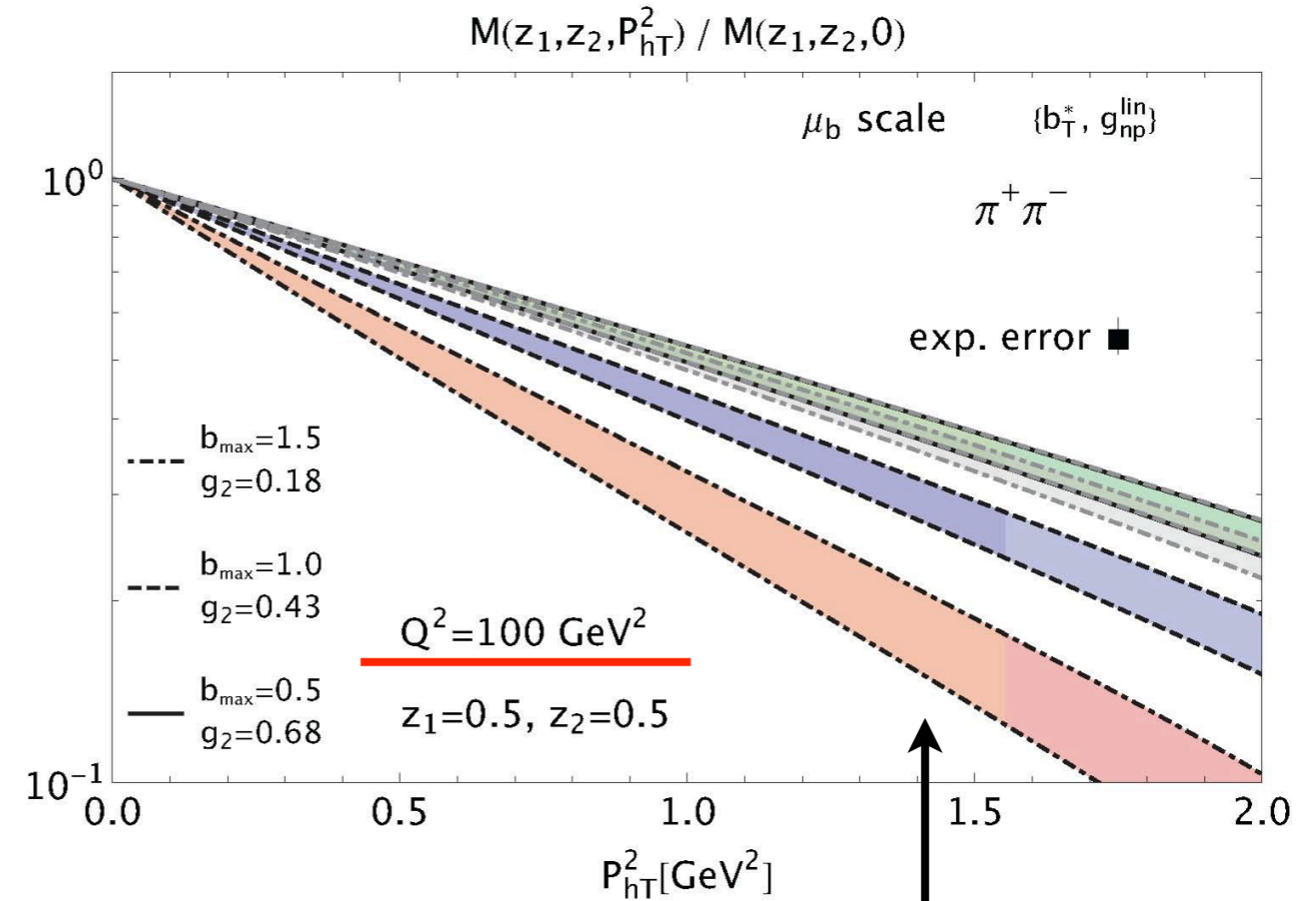
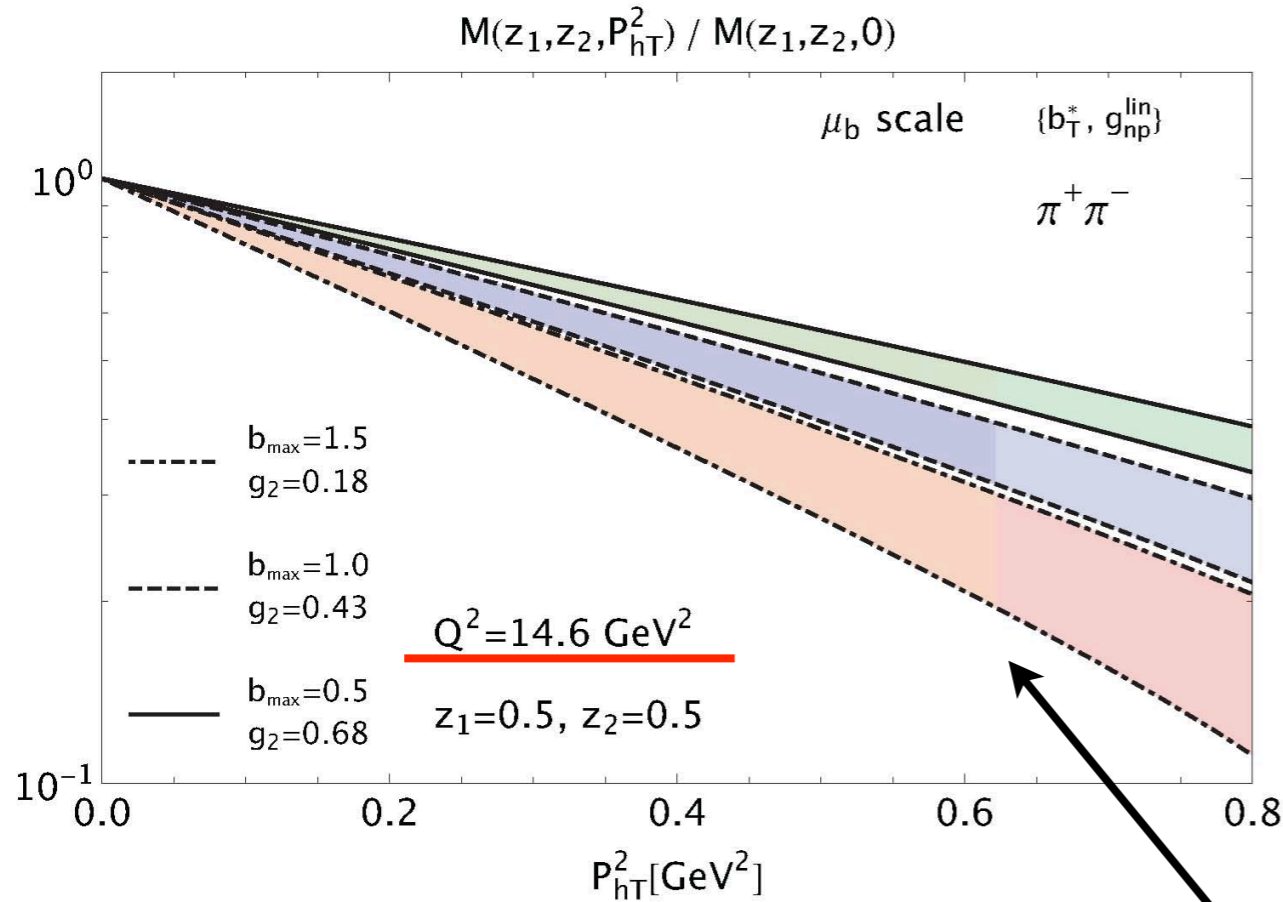
the transverse momentum  
dependence is described  
**ONLY** by the  
Gaussian distributions

$$d_1^{q \rightarrow h}(z, Q_i) e^{-\frac{\langle k_T^2 \rangle_{q \rightarrow h}(z)}{4} b_T^2}$$

being **flavor dependent**  
they combine and give a  
specific  $q_T$  dependence

band width result from  
intrinsic flavor dependence

# Evolution



model-dependent pieces

$$D_1^{a \rightarrow h}(z, b_T; Q) \sim e^{S_P} (C \otimes d_1) e^{-\frac{\langle P_{\perp}^2 \rangle_a(z)}{4z^2} b_T^2} e^{-\frac{g_2}{4} b_T^2 \ln Q^2}$$

**intrinsic transverse momentum**  
(flavor, kinematics)

**non-pert. evolution**  
(soft gluon emission)

# TMDs at work in pp

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references :

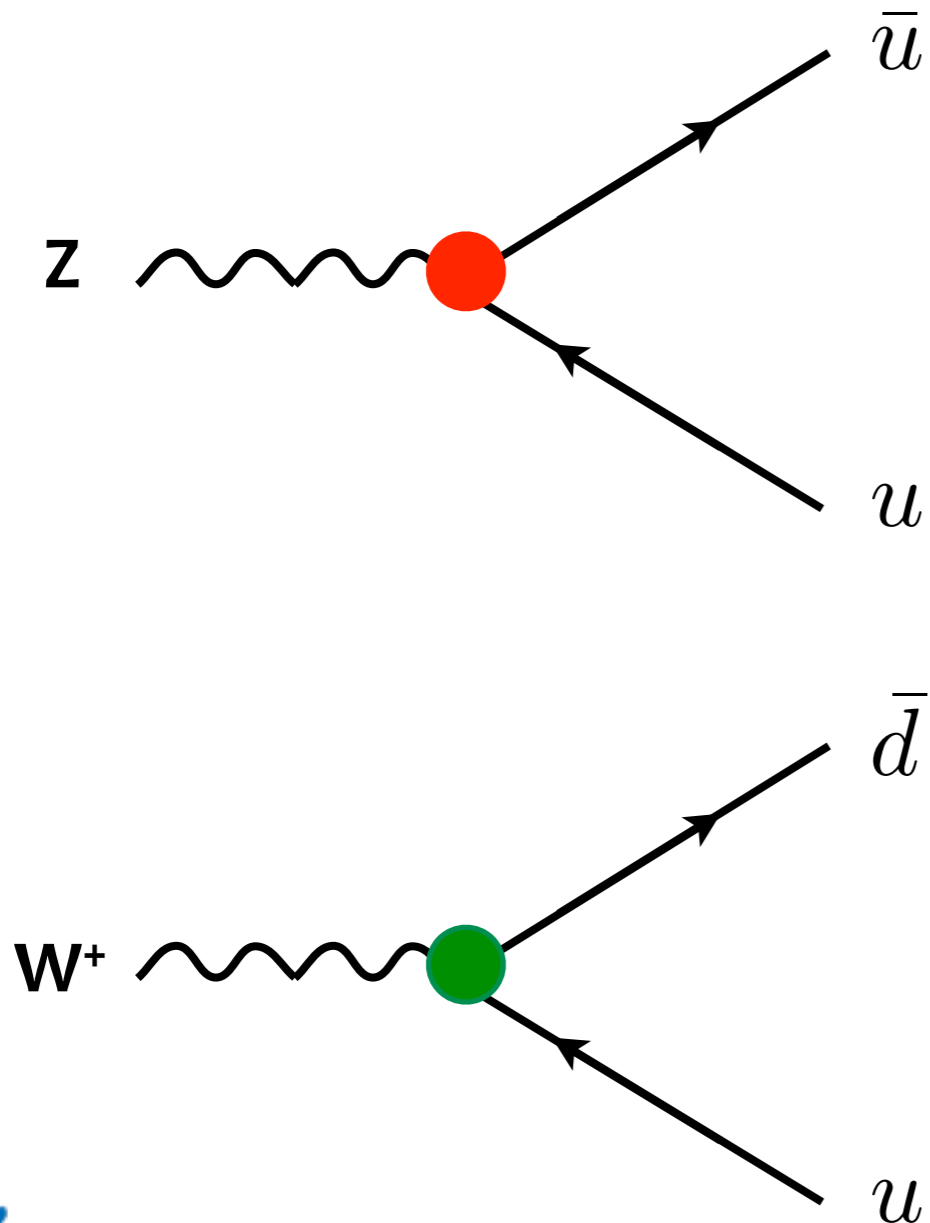
**AS** et al.

[10.5506/APhysPoIB.46.2501](#)

Bacchetta, Mulders, Radici, Ritzmann, **AS**  
[in preparation](#)

Echevarria, Kasemets, Lansberg, Pisano, **AS**  
[in preparation](#)

# Quark TMDs at the LHC

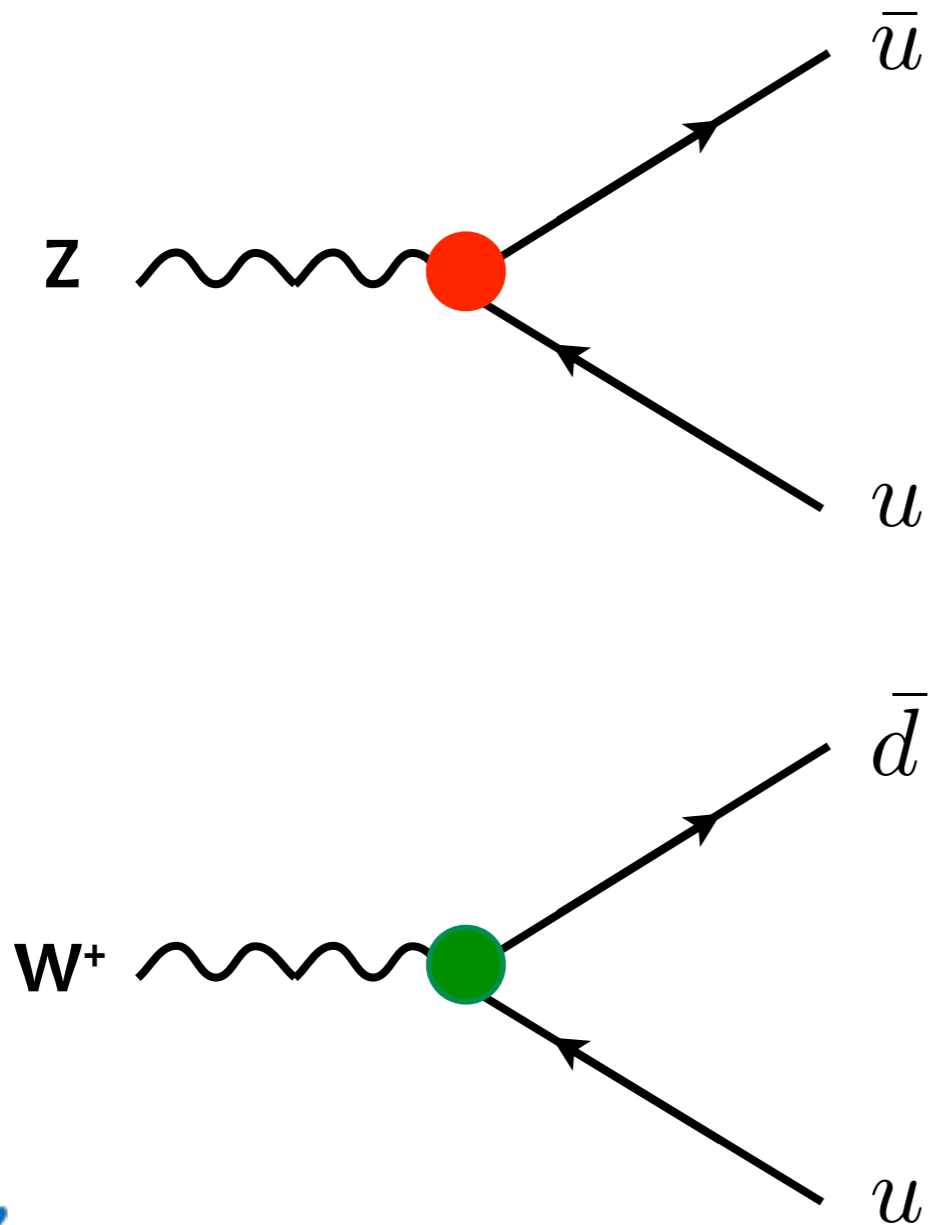


$$\frac{d\sigma^{Z/W^\pm}}{dq_T} \sim \text{FT} \sum_{i,j} \exp \left\{ -g_{ij} b_T^2 \right\}$$

$$g_{ij} \sim \langle k_T^2 \rangle_i + \langle k_T^2 \rangle_j + \text{soft gluons}$$

$g$  comes from 2 TMD PDFs  
and **controls the position of the peak**

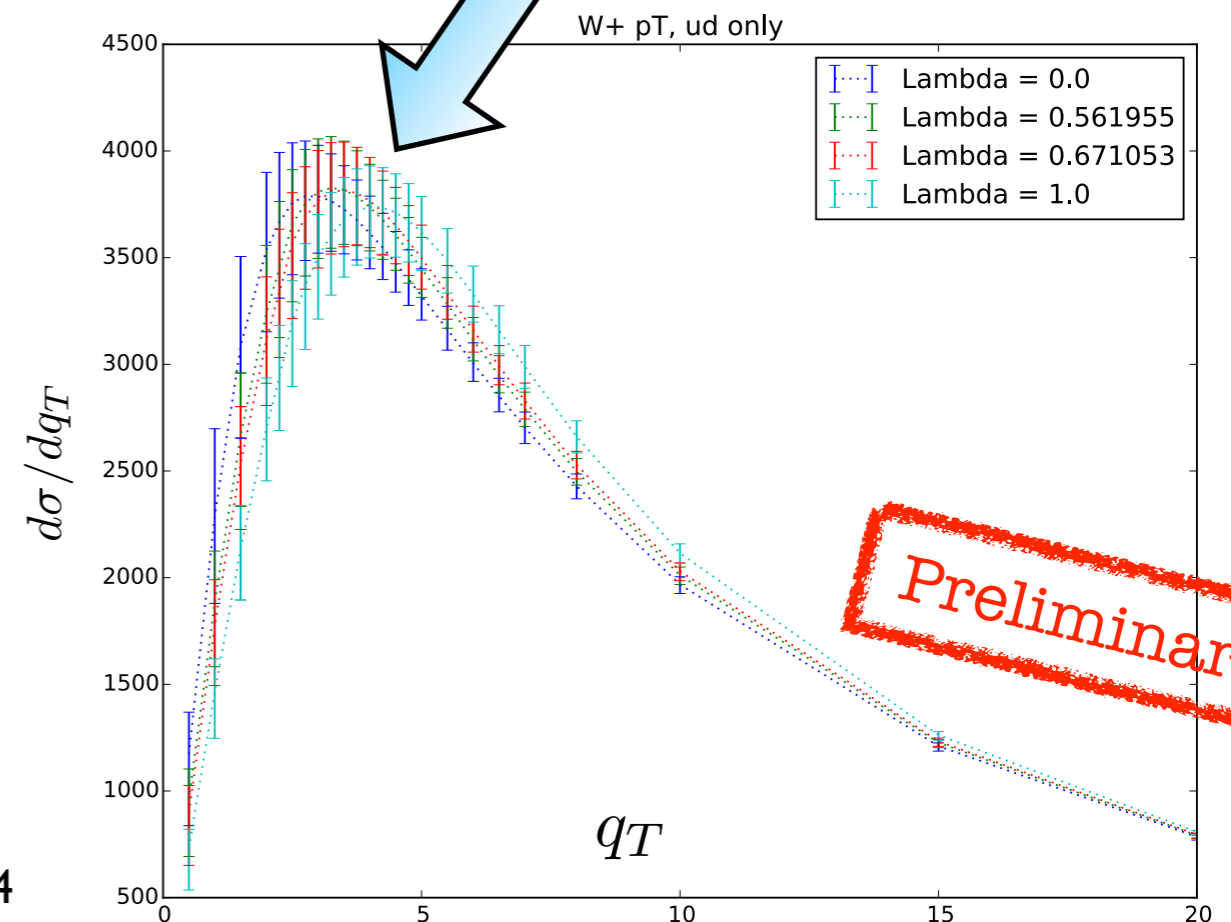
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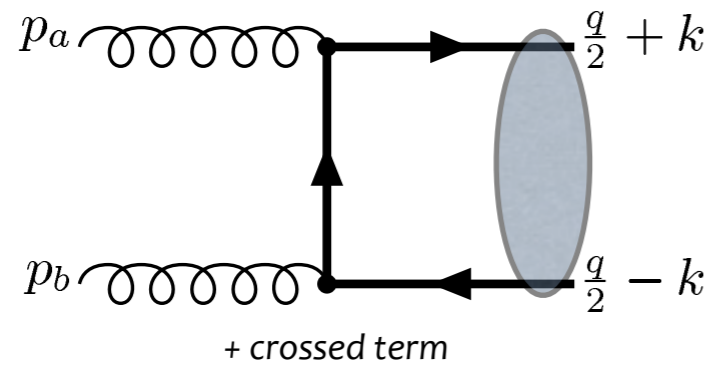
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# Gluon TMDs at work

(heavy) **quarkonium** production



$$P_A + P_B \rightarrow \eta_b(q_T) + X$$

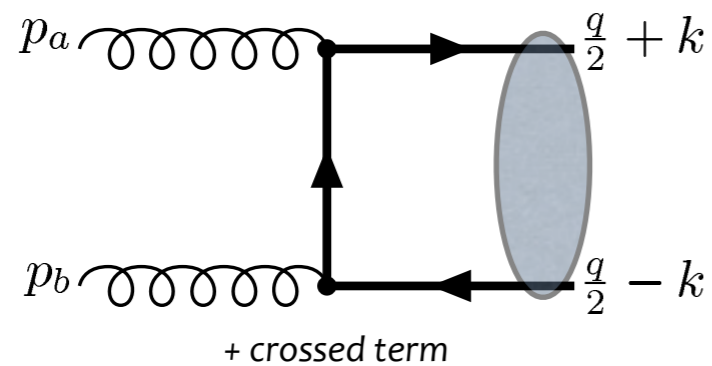
$$m_{\eta_b} = 9.39 \text{ GeV}$$

low/medium energy process:  
we could **extract**  
information on the **non perturbative**  
part of gluon TMDs

but ... does **TMD factorization** hold?

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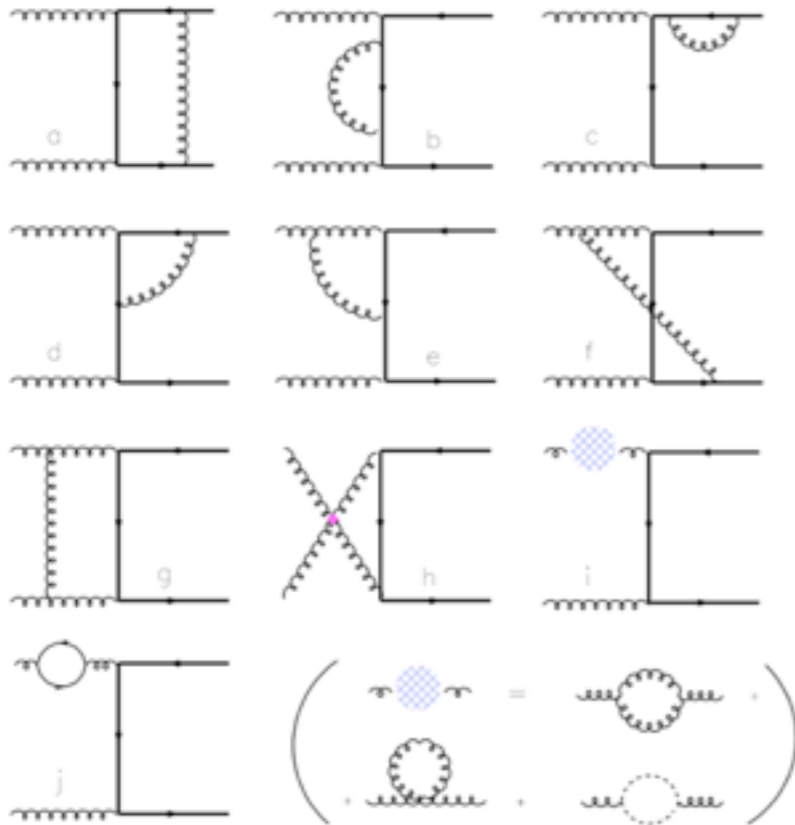
but ... does **TMD factorization** hold?

namely, are we **allowed** to use such an expression?

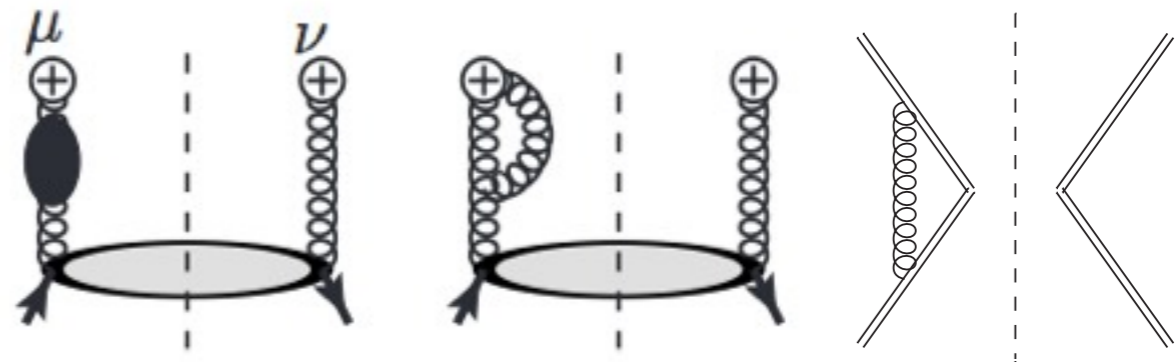
$$\frac{d\sigma}{dq_T} \sim f_1^{g/A} f_1^{g/B} |\mathcal{M}|^2$$

# Factorization

$$\text{QCD} \rightarrow \text{NRQCD} \oplus \text{SCET}_{q_T}$$



**Philosophy**: check (at NLO) if the **structure** of the IR divergencies is the same in the two expressions.



$$\sigma^{\text{virt},(1)} \longleftrightarrow \left\{ \mathcal{H} \tilde{f}_1^g/A \tilde{f}_1^g/B \right\}_{\text{virt}}^{(1)}$$

? same IR ?

**no:**

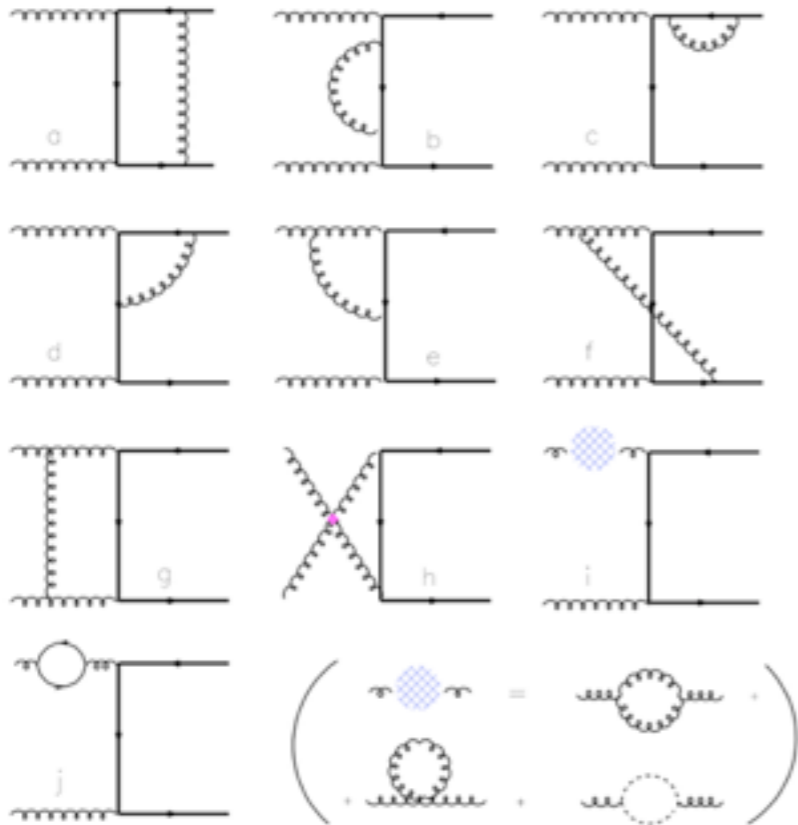
TMD fact. does not reproduce the physical (=QCD) result

**yes:**

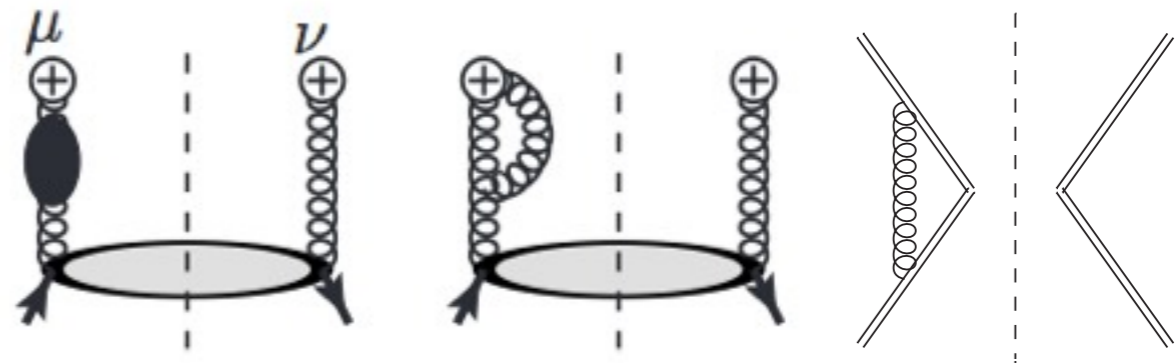
TMD fact. reproduces the physical result and the hard part can be calculated by subtraction

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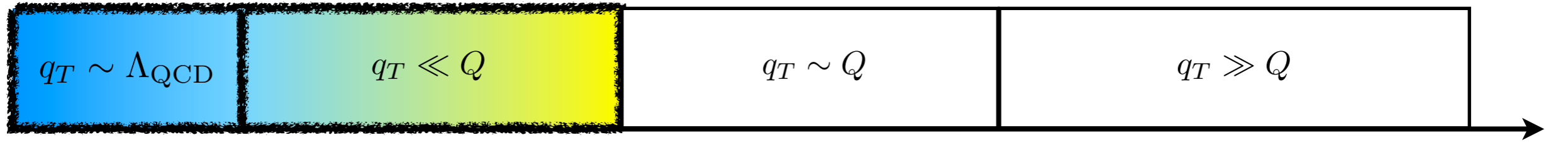
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**Yes!**

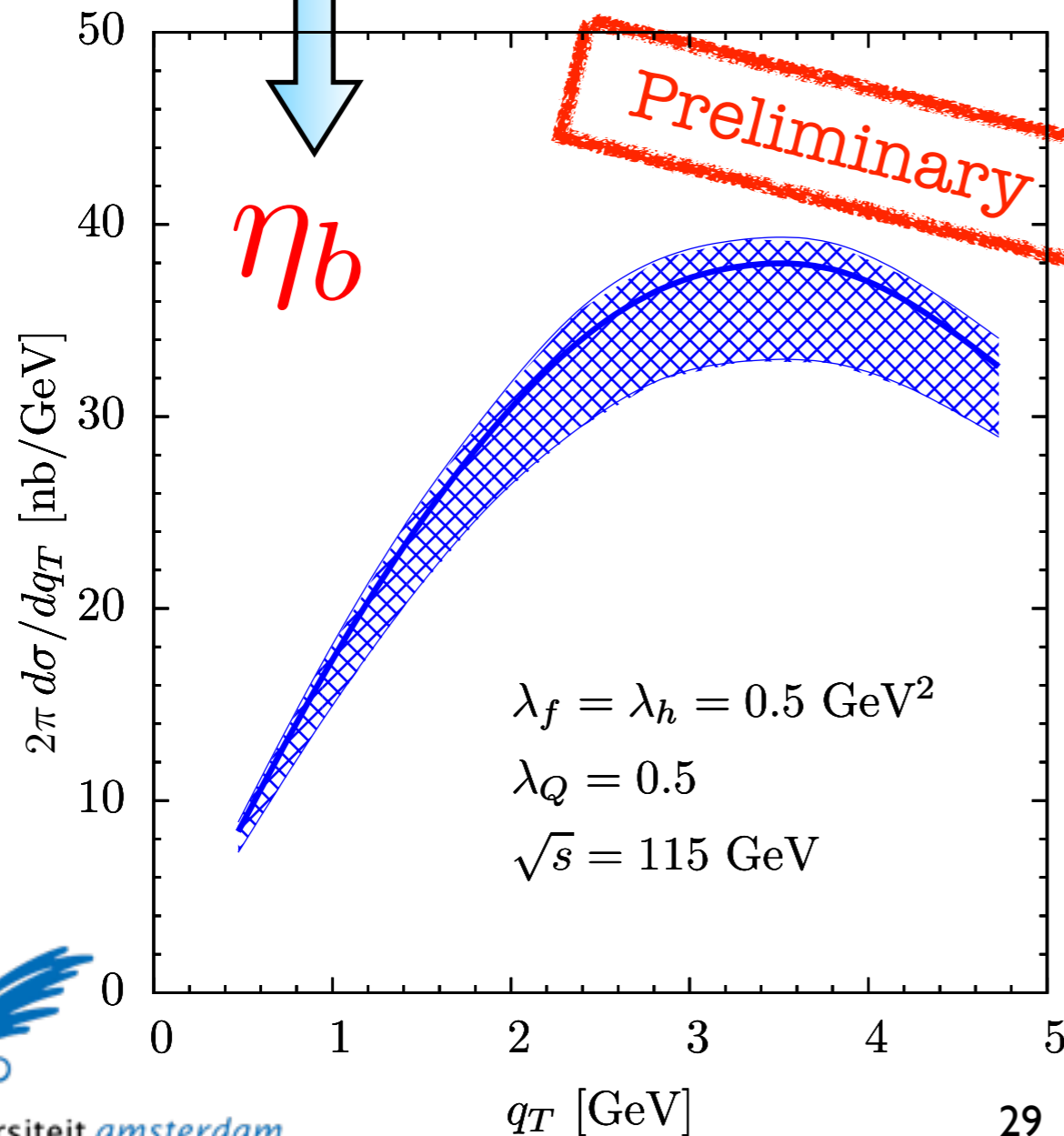
**yes:**

TMD fact. reproduces the physical result and the hard part can be calculated by subtraction

# Unpolarized phenomenology



$$q_T < M(\eta_b)/2$$



$$\frac{d\sigma_{UU}}{dq_T} \sim \{C[f_1^g f_1^g] - C[h_1^{\perp g} h_1^{\perp g}]\}$$

NRQCD from *Phys. Rev. D* 70, 054014  
(Maltoni/Polosa)

$$e^{-b_T^2 (\lambda_f/h + \lambda_Q \ln Q^2)}$$

Gaussian **model** at low  $q_T$

**We need data at low  $q_T$ !**

# New TMD structures

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references :

**AS** et al.

[10.5506/APhysPolB.46.2501](#)

Boer, Echevarria, Mulders, J. Zhou

[arXiv:1511.03485](#)

Amsterdam group

[in preparation](#)

# Gluons in spin 1 hadrons

TMDs	quarks	gluons
spin 1/2	✓	✓
spin 1	✓	?

## gluons in spin 1/2

$$\Phi^{\mu\nu}(k; P, S) \sim \text{F.T.} \langle PS | F^{+\mu}(0) U_{[0,\xi]} F^{+\nu}(\xi) U'_{[\xi,0]} | PS \rangle_{LF} \longrightarrow 8 \text{ functions at leading twist}$$

## gluons in spin 1

$$\Phi^{\mu\nu}(k; P, S, \underline{T}) \sim \text{F.T.} \langle PST | F^{+\mu}(0) U_{[0,\xi]} F^{+\nu}(\xi) U'_{[\xi,0]} | PST \rangle_{LF}$$

as for quarks,  
we expect more structures

# Pomerons from the gauge connection ?

TMDs	quarks	gluons	nothing (non partonic)
spin 1/2	✓	✓	✓?
spin 1	✓	?	?

link with  
small-x physics

gluons in spin 1/2

$$\Phi^{\mu\nu}(k; P, S) \sim \text{F.T.} \langle PS | F^{+\mu}(0) U_{[0,\xi]} F^{+\nu}(\xi) U'_{[\xi,0]} | PS \rangle_{LF}$$

removing the gluon fields from the gluon correlator:

$$\delta(x) \Phi(k_T; P, S, n) \sim \text{F.T.} \langle PS | U^{\square} | PS \rangle_{LF} \longrightarrow e(k_T) - \frac{\mathbf{k}_T \times \mathbf{S}_T}{M} e_T^{\perp}(k_T)$$

“pomeron”

“odderon”

exchange of color-singlet objects

only the gauge loop



# Conclusions

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- 1) There is **much to learn** about TMDs, and the **12 GeV program** at JLab is an excellent playground
- 2) **How to access TMDs?** Flexible and rich **models** + **perturbative** information (**TMD factorization** and **evolution**)
- 3) SIDIS data suggest a **flavor dependence** in the intrinsic transverse momentum of partons; this opens the path to **yet unexplored effects**
- 4) we can find its footprints in **e+e- annihilation** and it might have a non-negligible **impact on Z/W $\pm$  production**
- 5) **new structures** can be introduced: factorization, universality, evolution, phenomenology, ...

# Backup slides

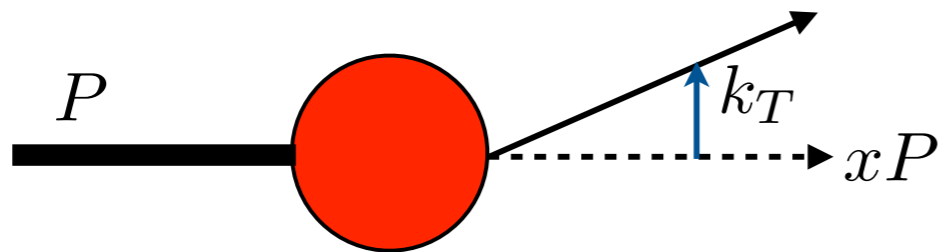
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how can we **access TMDs**  
in the “best” possible way ?

# Quark TMD PDFs



$$\Phi_{ij}(k; P, S) \sim \text{F.T.} \langle PS | \bar{\psi}_j(0) U_{[0,\xi]} \psi_i(\xi) | PS \rangle_{LF}$$



↑  
extraction of a **quark**  
**not** collinear with the proton

←  
quark pol.

nucleon pol.

	U	L	T
U	$f_1$		$h_1^\perp$
L		$g_{1L}$	$h_{1L}^\perp$
T	$f_{1T}^\perp$	$g_{1T}$	$h_1, h_{1T}^\perp$

add references

**spin-spin** and **spin-orbit**  
interactions

a similar scheme  
holds for gluons  
in Lorentz space

Twist-2 TMDs

# Gluon TMD PDFs



$$\Phi^{\mu\nu}(k; P, S) \sim \text{F.T.} \langle PS | F^{+\mu}(0) U_{[0,\xi]} F^{n\nu}(\xi) U'_{[\xi,0]} | PS \rangle_{LF}$$

hermiticity, parity,  
time-reversal  
invariance

<b>GLUONS</b>	<i>unpolarized</i>	<i>circular</i>	<i>linear</i>
<b>U</b>	$f_1^g$		$h_1^{\perp g}$
<b>L</b>		$g_{1L}^g$	$h_{1L}^{\perp g}$
<b>T</b>	$f_{1T}^{\perp g}$	$g_{1T}^g$	$h_{1T}^g, h_{1T}^{\perp g}$

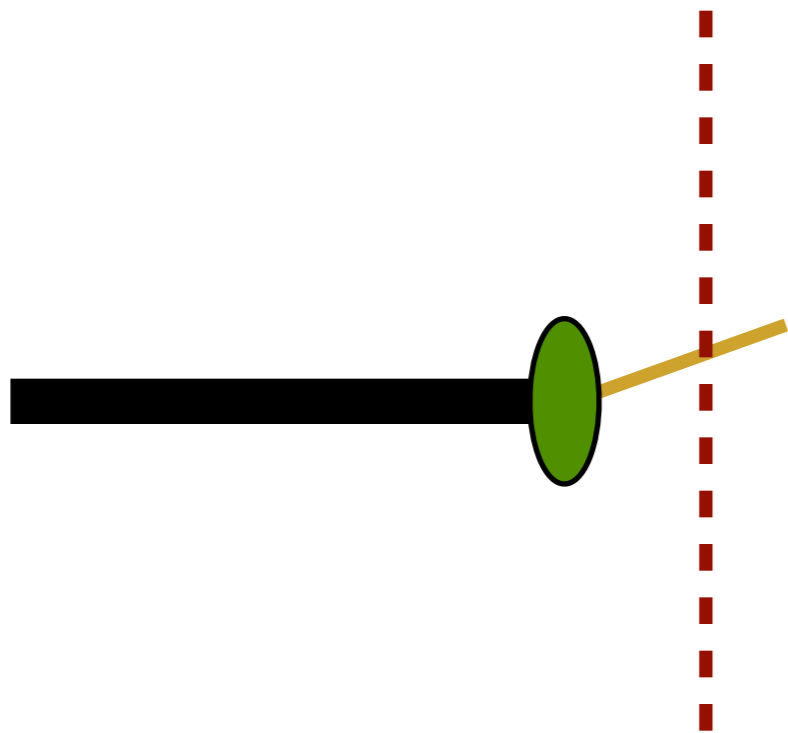
Mulders, Rodriguez  
PRD 63 (2001)

LEADING  
TWIST

**spin-spin** and **spin-orbit** interactions  
between the proton and its constituents

# Transverse momentum spectrum

**intrinsic**  
transverse  
momentum

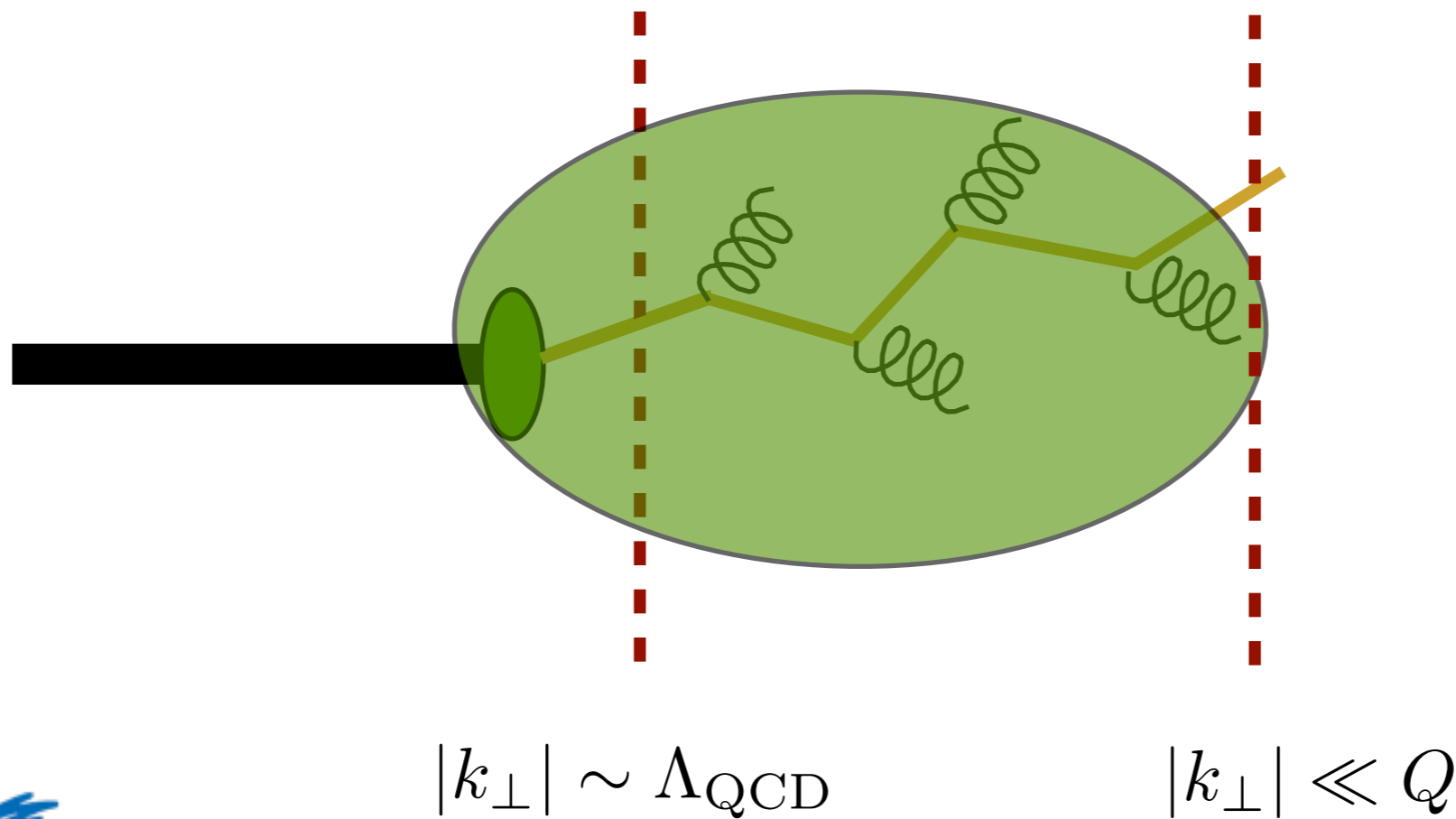


$$|k_{\perp}| \sim \Lambda_{\text{QCD}}$$

# Transverse momentum spectrum

**intrinsic**  
transverse  
momentum

**soft and collinear**  
gluon radiation

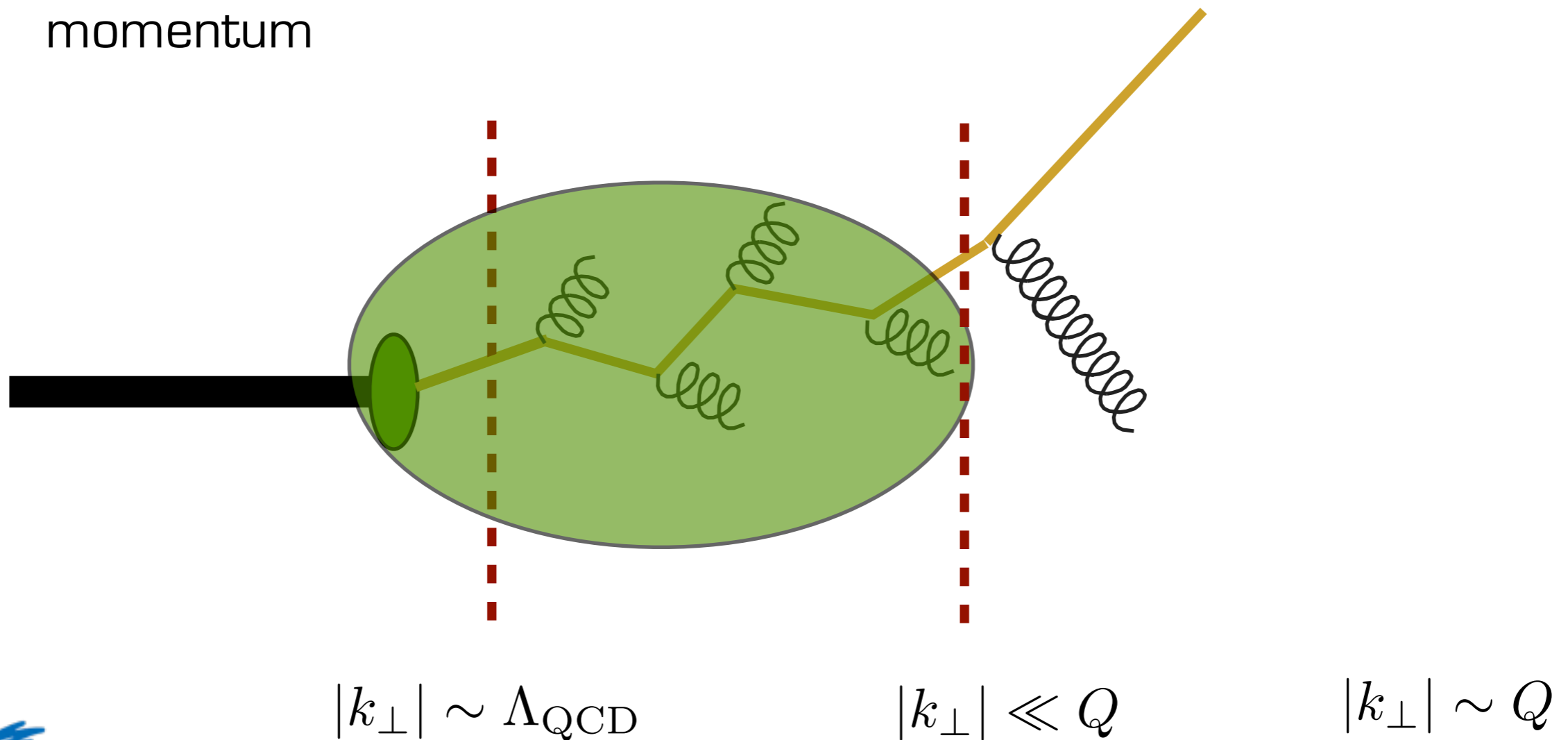


# Transverse momentum spectrum

**intrinsic**  
transverse  
momentum

**soft and collinear**  
gluon radiation

**hard**  
gluon radiation



# Transverse momentum spectrum

OPE - matching coefficient

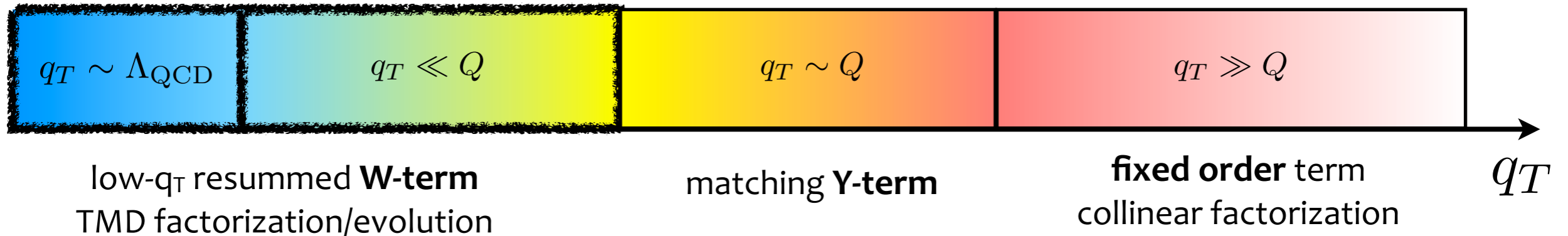
$$\tilde{T}_{g/A}(x, b_T; \mu, \zeta) = \sum_{j=q, \bar{q}, g} \tilde{C}_{g/j}^T(x, b_T; \mu, \zeta) \otimes t_{j/A}(x; \mu) + \mathcal{O}(b_T \Lambda_{QCD})$$

TMD PDF

medium/high  $q_T$   
Sudakov form factor  
+ perturbative tail

PDF

intrinsic low  $q_T$   
(model)



transverse momentum spectrum of physical observables



# Transverse momentum spectrum

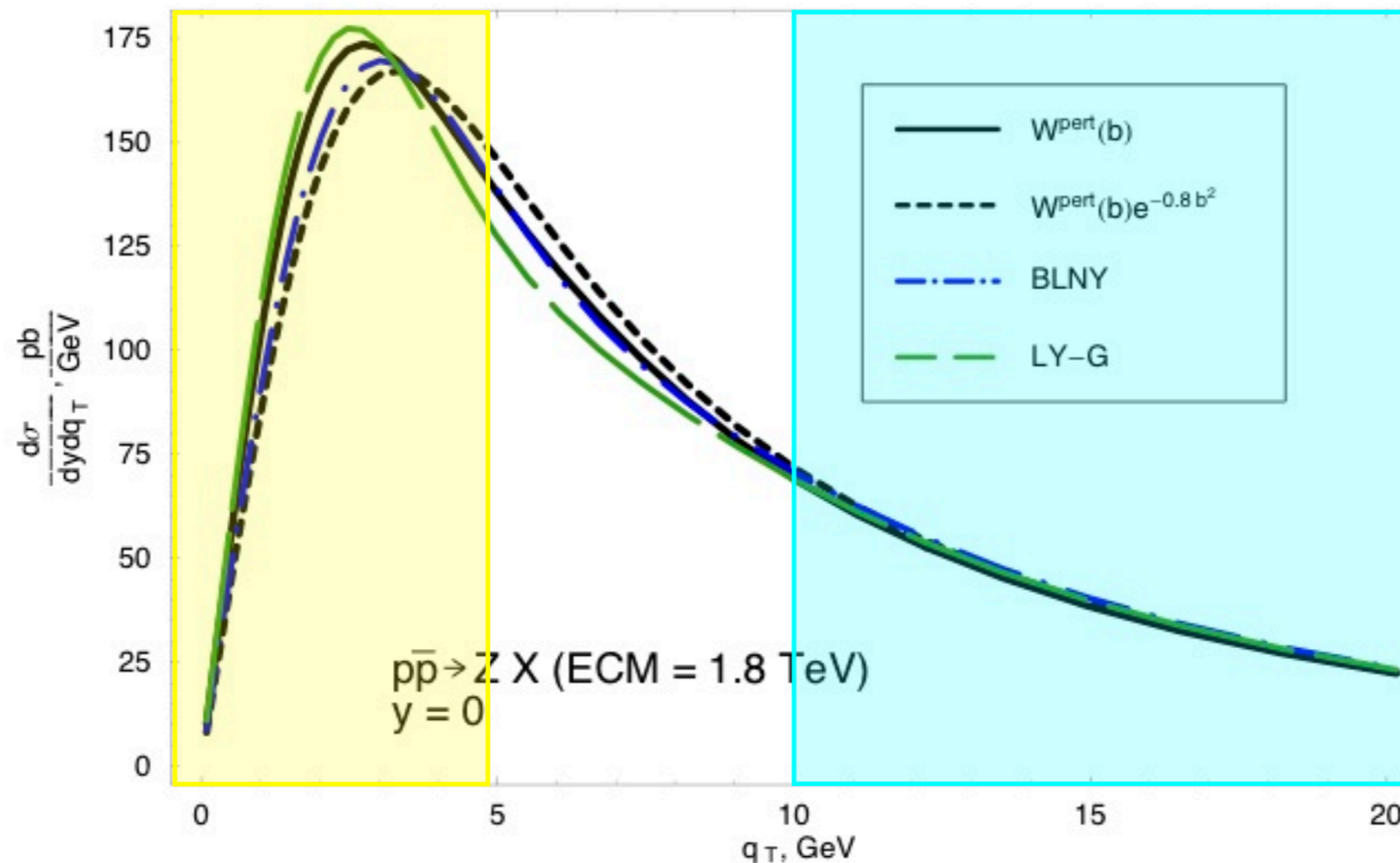
TMDs generate the  $q_T$  dep. of cross sections : but **how in practice** ?

**intrinsic** momentum +  
**soft/coll.** gluon radiation

correct the color code

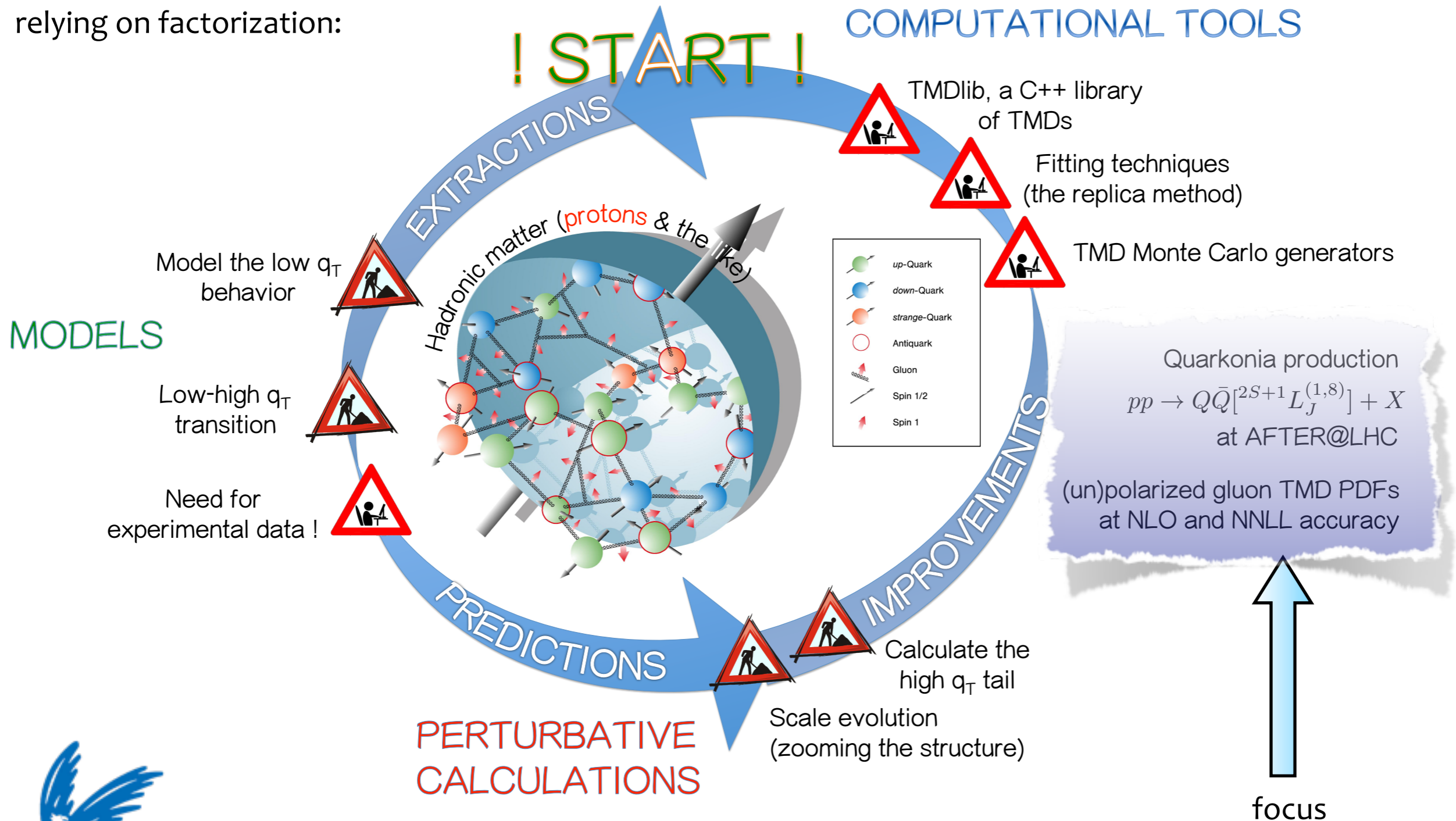
matching

**hard** gluon radiation



# The road to TMD phenomenology

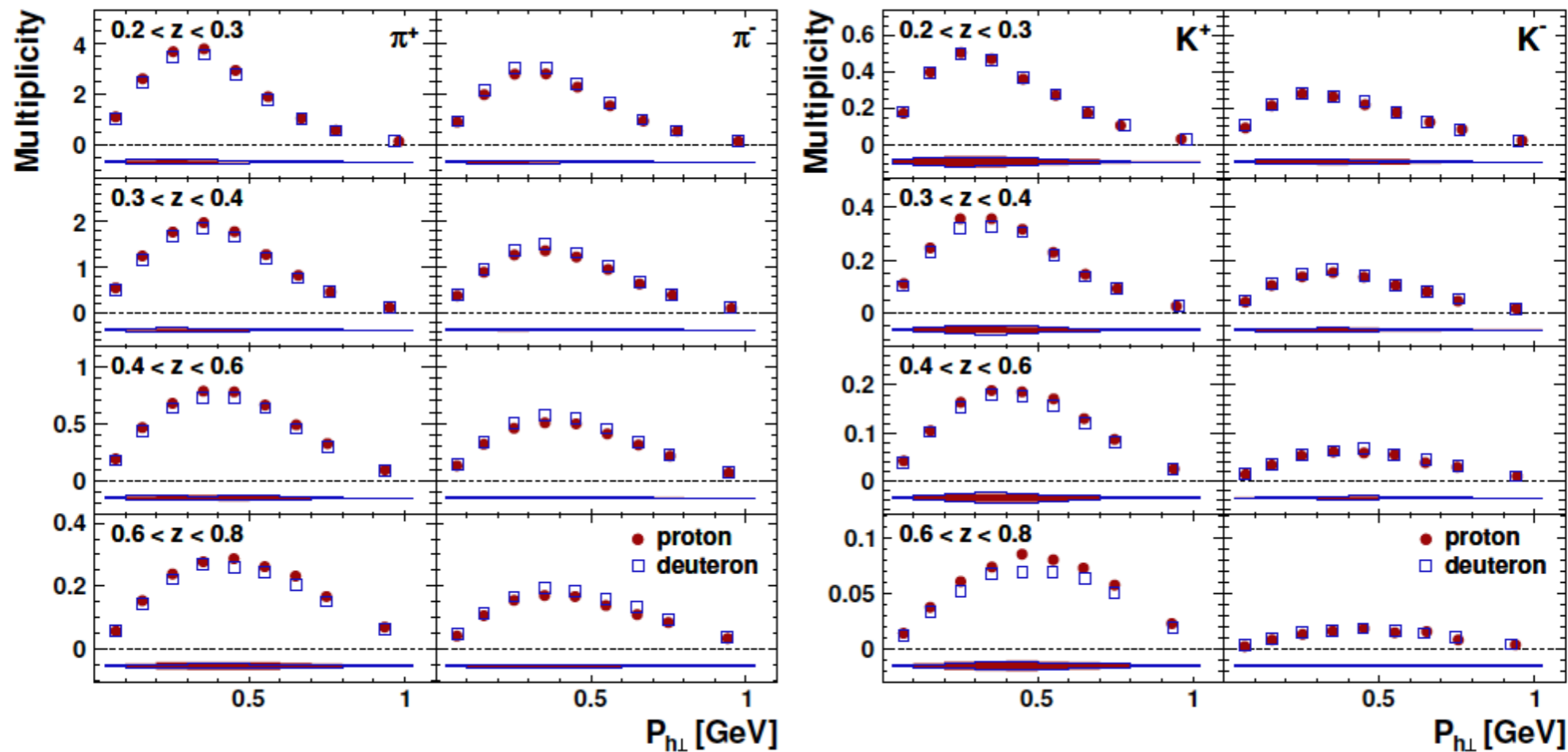
relying on factorization:



# SIDIS @ Hermes

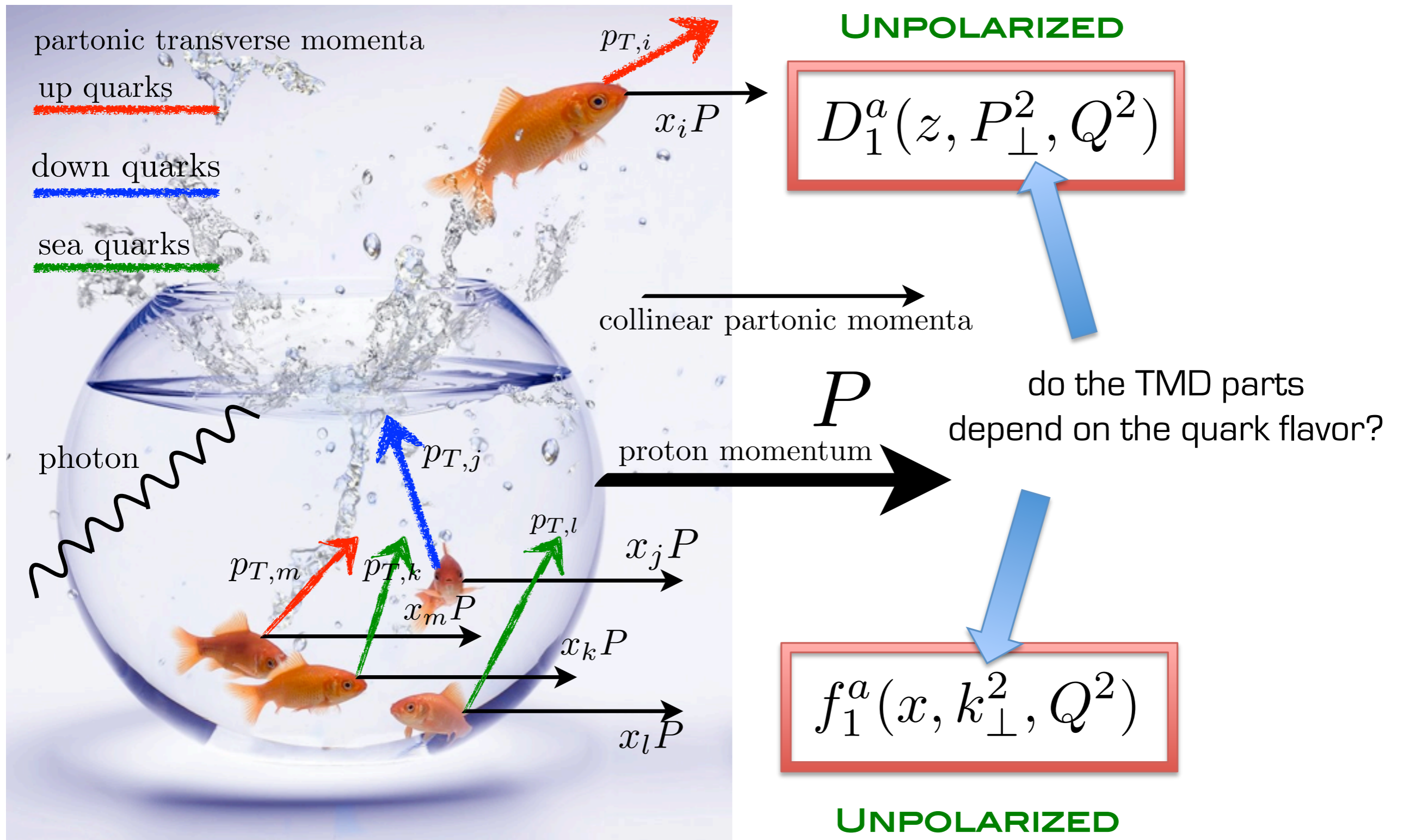


$$e^{\pm} + \boxed{P/D} \rightarrow e^{\pm} + \{ \pi^{\pm} / K^{\pm} \} + X$$



Intrinsic flavor dependence: a way to account for differences between cross sections related to different final state hadrons

# Flavor in transverse momentum



# Kinematic dependence

---

$$\langle \mathbf{k}_{\perp, q}^2 \rangle(x) = \widehat{\langle \mathbf{k}_{\perp, q}^2 \rangle} \frac{(1-x)^\alpha x^\sigma}{(1-\hat{x})^\alpha \hat{x}^\sigma}$$

$$\widehat{\langle \mathbf{k}_{\perp, q}^2 \rangle} = \langle \mathbf{k}_{\perp, q}^2 \rangle(\hat{x} = 0.1)$$

---

$$\langle \mathbf{P}_{\perp, q \rightarrow h}^2 \rangle(z) = \widehat{\langle \mathbf{P}_{\perp, q \rightarrow h}^2 \rangle} \frac{(z^\beta + \delta)(1-z)^\gamma}{(\hat{z}^\beta + \delta)(1-\hat{z})^\gamma}$$

$$\widehat{\langle \mathbf{P}_{\perp, q \rightarrow h}^2 \rangle} = \langle \mathbf{P}_{\perp, q \rightarrow h}^2 \rangle(\hat{z} = 0.5)$$

# Best fit parameters

Parameters for TMD PDFs					
	$\langle \hat{k}_{\perp, d_v}^2 \rangle$ [GeV <sup>2</sup> ]	$\langle \hat{k}_{\perp, u_v}^2 \rangle$ [GeV <sup>2</sup> ]	$\langle \hat{k}_{\perp, sea}^2 \rangle$ [GeV <sup>2</sup> ]	$\alpha$ (random)	$\sigma$ (random)

5 parameters

interval [0,2]

interval [-0.3,0.1]

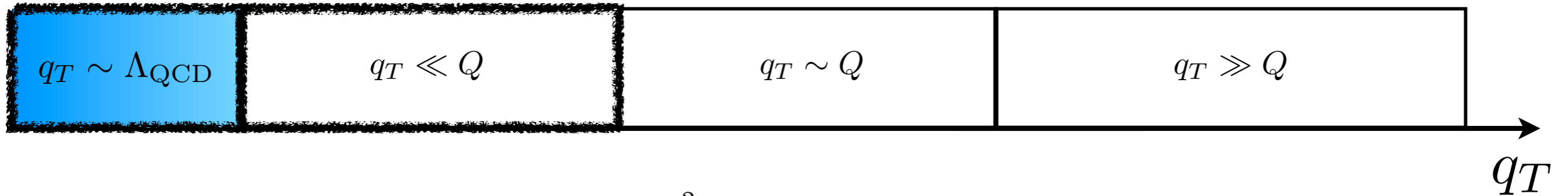
Parameters for TMD FFs							
	$\langle \hat{P}_{\perp, fav}^2 \rangle$ [GeV <sup>2</sup> ]	$\langle \hat{P}_{\perp, unf}^2 \rangle$ [GeV <sup>2</sup> ]	$\langle \hat{P}_{\perp, sK}^2 \rangle$ [GeV <sup>2</sup> ]	(random)	$\beta$	$\delta$	$\gamma$

7 parameters

interval [0.125,0.250]

# Parton model picture

TMD region



$$f_1^a(x, k_T) = f_1^a(x) \frac{1}{\pi \langle k_T^2 \rangle_a(x)} e^{-\frac{k_T^2}{\langle k_T^2 \rangle_a(x)}}$$

$$\langle Q^2 \rangle = 2.4 \text{ GeV}^2$$

neglect QCD evo = parton model

$$D_1^{a/h}(z, P_\perp) = D_1^a(z) \frac{1}{\pi \langle P_\perp^2 \rangle_{a/h}(z)} e^{-\frac{P_\perp^2}{\langle P_\perp^2 \rangle_{a/h}(z)}}$$

Flavor and kinematic dependent widths

$$\langle k_{\perp, u_v}^2 \rangle \neq \langle k_{\perp, d_v}^2 \rangle \neq \langle k_{\perp, \text{sea}}^2 \rangle$$

$$\langle P_{\perp, u \rightarrow \pi^+}^2 \rangle = \langle P_{\perp, \bar{d} \rightarrow \pi^+}^2 \rangle = \langle P_{\perp, \bar{u} \rightarrow \pi^-}^2 \rangle = \langle P_{\perp, d \rightarrow \pi^-}^2 \rangle \equiv \langle P_{\perp, \text{fav}}^2 \rangle,$$

$$\langle P_{\perp, u \rightarrow K^+}^2 \rangle = \langle P_{\perp, \bar{u} \rightarrow K^-}^2 \rangle \equiv \langle P_{\perp, uK}^2 \rangle,$$

$$\langle P_{\perp, \bar{s} \rightarrow K^+}^2 \rangle = \langle P_{\perp, s \rightarrow K^-}^2 \rangle \equiv \langle P_{\perp, sK}^2 \rangle,$$

$$\langle P_{\perp, \text{all others}}^2 \rangle \equiv \langle P_{\perp, \text{unf}}^2 \rangle.$$



# The replica method

---

200 **statistical replicas** of **HERMES** data

A fit is performed on each replica

200 best-fit values for the parameters

clean access to uncertainties

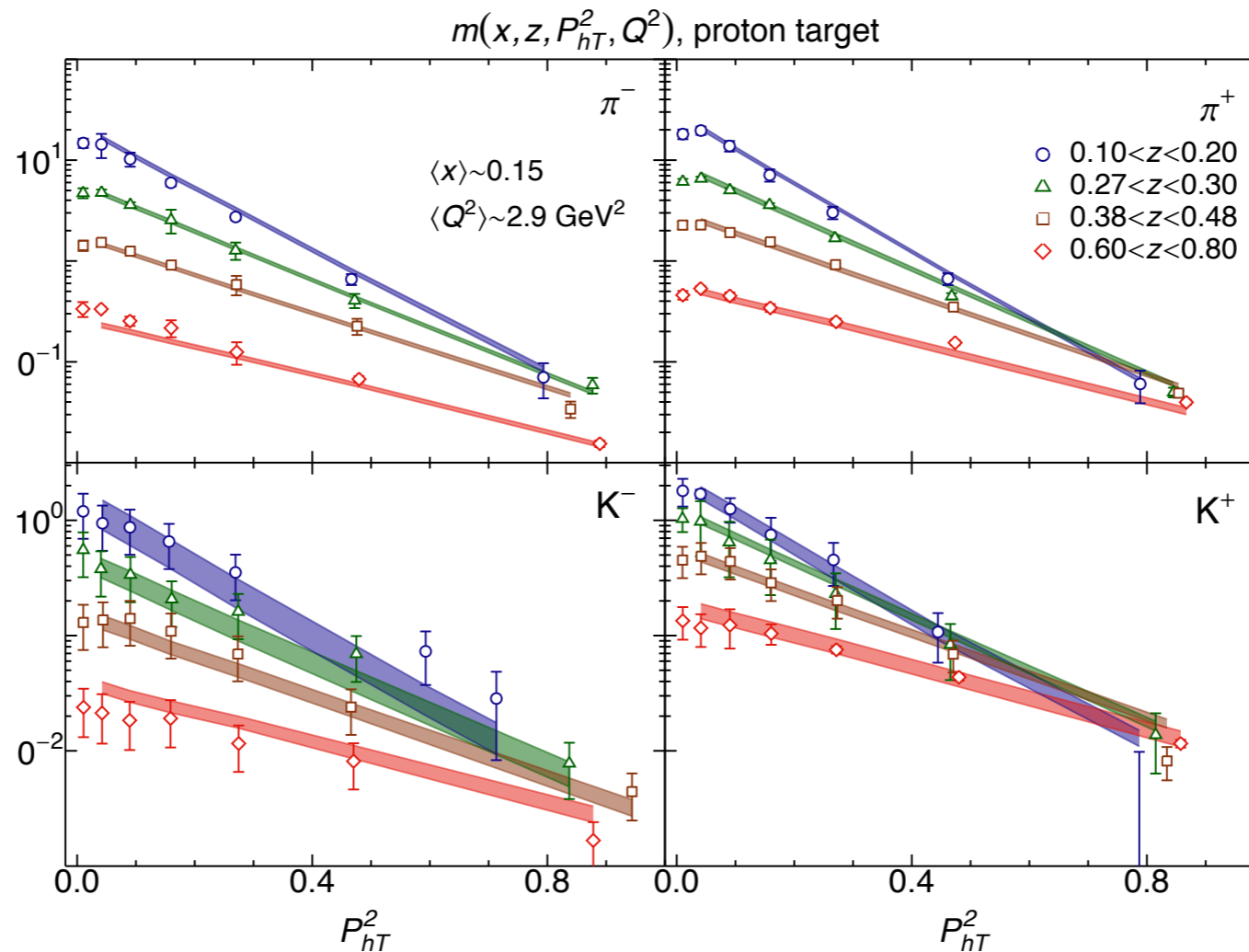
We get a **distribution**, not a single value;  
**physically richer**

More complete exploration of the minima in  
the space of fit parameters



# Fits of multiplicities

proton target    global  $\chi^2 / \text{d.o.f.} = 1.63 \pm 0.12$   
 no flavor dep.                       $1.72 \pm 0.11$



$\pi^-$   
 $1.80 \pm 0.27$   
 $1.83 \pm 0.25$

$\pi^+$   
 $2.64 \pm 0.21$   
 $2.89 \pm 0.23$

$K^-$   
 $0.78 \pm 0.15$   
 $0.87 \pm 0.16$

$K^+$   
 $0.46 \pm 0.07$   
 $0.43 \pm 0.07$

# Best fit values

68% confidence intervals of best-fit parameters for TMD FFs in the different scenarios

Parameters for TMD FFs				
	Default	$Q^2 > 1.6 \text{ GeV}^2$	Pions only	Flavor-indep.
$\langle \hat{P}_{\perp, \text{fav}}^2 \rangle [\text{GeV}^2]$	$0.15 \pm 0.04$	$0.15 \pm 0.04$	$0.16 \pm 0.03$	$0.18 \pm 0.03$
$\langle \hat{P}_{\perp, \text{unf}}^2 \rangle [\text{GeV}^2]$	$0.19 \pm 0.04$	$0.19 \pm 0.05$	$0.19 \pm 0.04$	$0.18 \pm 0.03$
$\langle \hat{P}_{\perp, sK}^2 \rangle [\text{GeV}^2]$	$0.19 \pm 0.04$	$0.19 \pm 0.04$	-	$0.18 \pm 0.03$
$\langle \hat{P}_{\perp, uK}^2 \rangle [\text{GeV}^2]$	$0.18 \pm 0.05$	$0.18 \pm 0.05$	-	$0.18 \pm 0.03$
$\beta$	$1.43 \pm 0.43$	$1.59 \pm 0.45$	$1.55 \pm 0.27$	$1.30 \pm 0.30$
$\delta$	$1.29 \pm 0.95$	$1.41 \pm 1.06$	$1.20 \pm 0.63$	$0.76 \pm 0.40$
$\gamma$	$0.17 \pm 0.09$	$0.16 \pm 0.10$	$0.15 \pm 0.05$	$0.22 \pm 0.06$

# Conclusions - SIDIS

o) SIDIS (Hermes) multiplicities are also **compatible with flavor dependent configurations** in the intrinsic transverse momentum of partons

1) on average : sea > u-val > d-val & unf > fav( $\pi$ ), fav(K) > fav( $\pi$ )

2) Despite not producing dramatic effects on SIDIS, the flavor decomposition of TMDs **opens the way to yet unexplored effects**

3) flavor dependence in TMD FFs can be **investigated at e+e- experiment**, together with information on the non-perturbative evolution

4) we need to look at different observables with multi-D kinematic ranges

# Implementation of evolution

$$\frac{d\sigma^{h_1 h_2}}{dz_1 dz_2 dq_T^2 dy} \sim H(Q^2, \mu) \longrightarrow 1, \text{ no alpha corrections}$$

$$\times \sum_q e_q^2 \int_0^\infty db_T b_T J_0(q_T b_T) \left[ z_1^2 D_1^{q \rightarrow h_1}(z_1, b_T; \mu, \zeta_1) z_2^2 D_1^{\bar{q} \rightarrow h_2}(z_2, b_T; \mu, \zeta_2) + (q \leftrightarrow \bar{q}) \right]$$

$$+ Y(\cancel{q_T^2/Q^2}) + \mathcal{O}(\cancel{M^2/Q^2})$$

no high  $q_T$  tail  
(collinear factorization)

no higher twist

$$D_1^{q \rightarrow h}(z, b_T; \mu, \zeta) = \underbrace{[C \otimes d_1^{q \rightarrow h}]}_{\text{small } b_T / \text{medium } k_T} + \underbrace{\mathcal{O}(b_T \Lambda_{\text{QCD}})}_{\text{high } b_T / \text{small } k_T}$$

flavor and kinematic dependent Gaussian model  
(JHEP 1311 (2013) 194)

$$e^{-\frac{\langle k_T^2 \rangle_{q/h}(z)}{4} b_T^2}$$

LO and NLL pert. Sudakov quark form factor

OPE coefficients are delta on the flavors

models for non-pert. Sudakov quark f.f.

models for the small/high  $b_T$  separation

$$g_{\text{np}}^{\text{lin}/\log}(b_T^2; g_2) \quad \hat{b}_T(b_T; b_{\text{max}}) = \{b_T^*, b_T^\dagger\}$$

# Implementation of evolution

$$b_T^* = \frac{b_T}{\sqrt{1 + \frac{b_T^2}{b_{\max}^2}}} \xrightarrow{b_T \rightarrow \infty} b_{\max}$$

$$b_T^\dagger = b_{\max} \left\{ 1 - \exp \left[ -\frac{b_T^4}{b_{\max}^4} \right] \right\}^{\frac{1}{4}} \xrightarrow{b_T \rightarrow \infty} b_{\max}$$



two different ways  
to **approach**  $b_{\max}$ ,  
the point where we **stop**  
trusting the perturbative result

for  $b$  larger than  $b_{\max}$   
a **model** is needed  
also in the evolution



$b_{\max}$  and  $g_2$   
are **anticorrelated**  
parameters

$$g_{\text{np}}^{\text{lin}}(b_T^2; g_2) = \frac{g_2}{4} b_T^2$$

$$g_{\text{np}}^{\text{log}}(b_T^2; g_2) = g_2 \ln \left( 1 + \frac{b_T^2}{4} \right)$$

see also [PhysRevD.91.074020](#)  
(Collins, Rogers)

# ... factorization scale (evolution scheme)

$$\sigma^{\text{F.O.}} \sim \ln \frac{Q}{q_T} \xrightarrow[\text{at scale } \mu]{\text{factorization}}$$

factorization in a nutshell

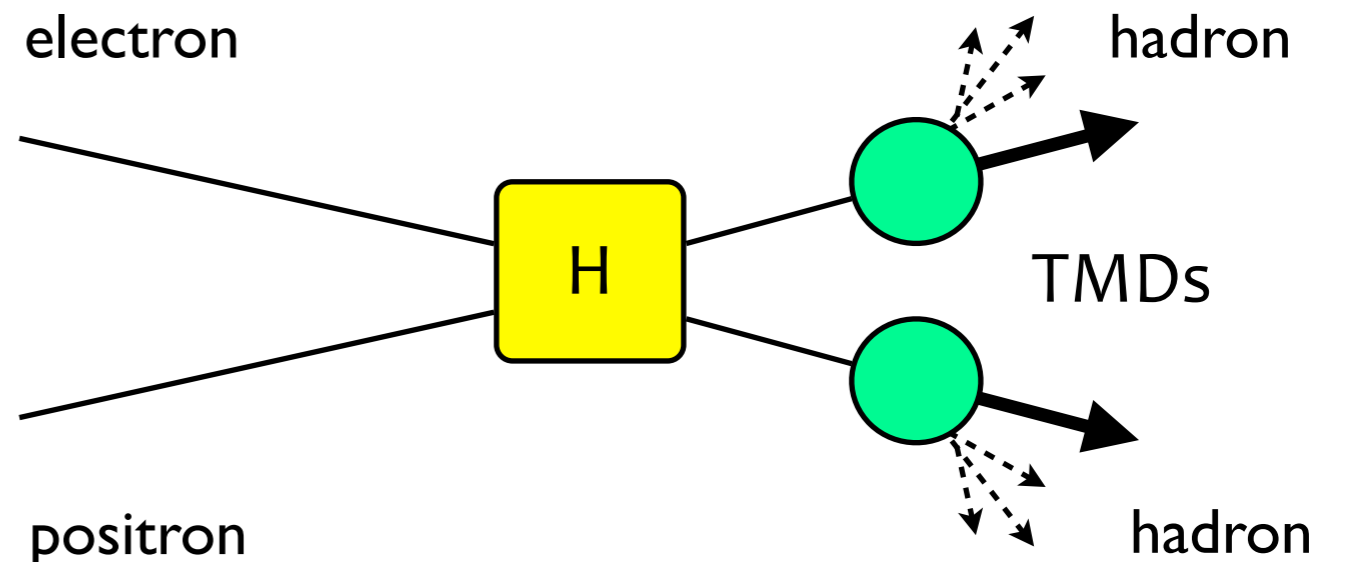
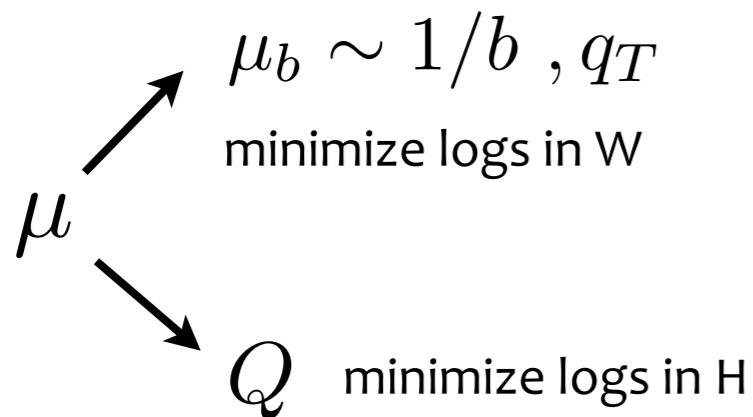
$$\ln \frac{Q}{\mu} \cdot \frac{\mu}{\mu_b} = \ln \frac{Q}{\mu} + \ln \frac{\mu}{\mu_b}$$

hard part H

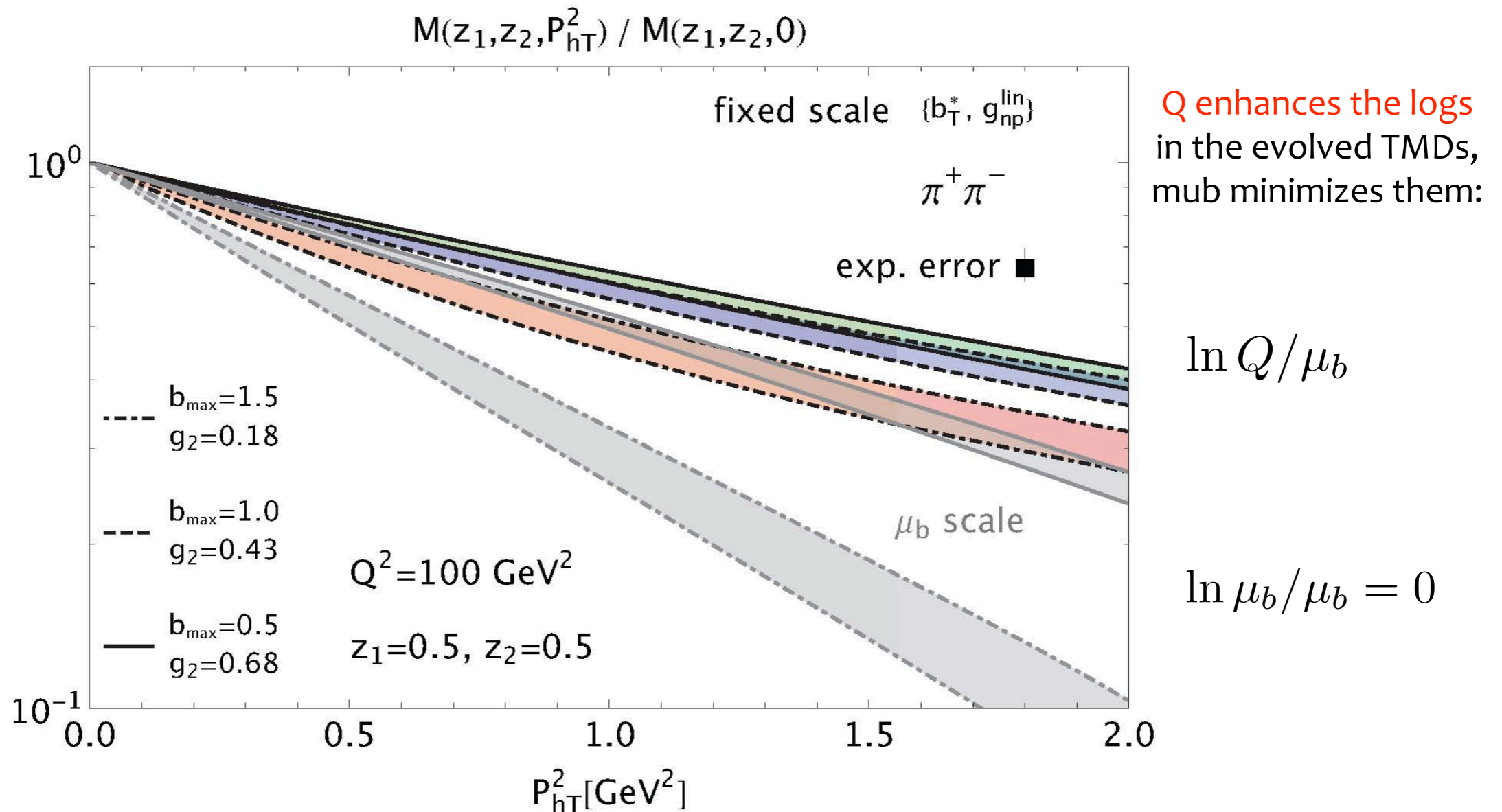
perturbative part of W term (TMDs)

Different choices are possible for the factorization scale, with different implications:

resumming these logarithms we get a finite cross section at low  $q_T$



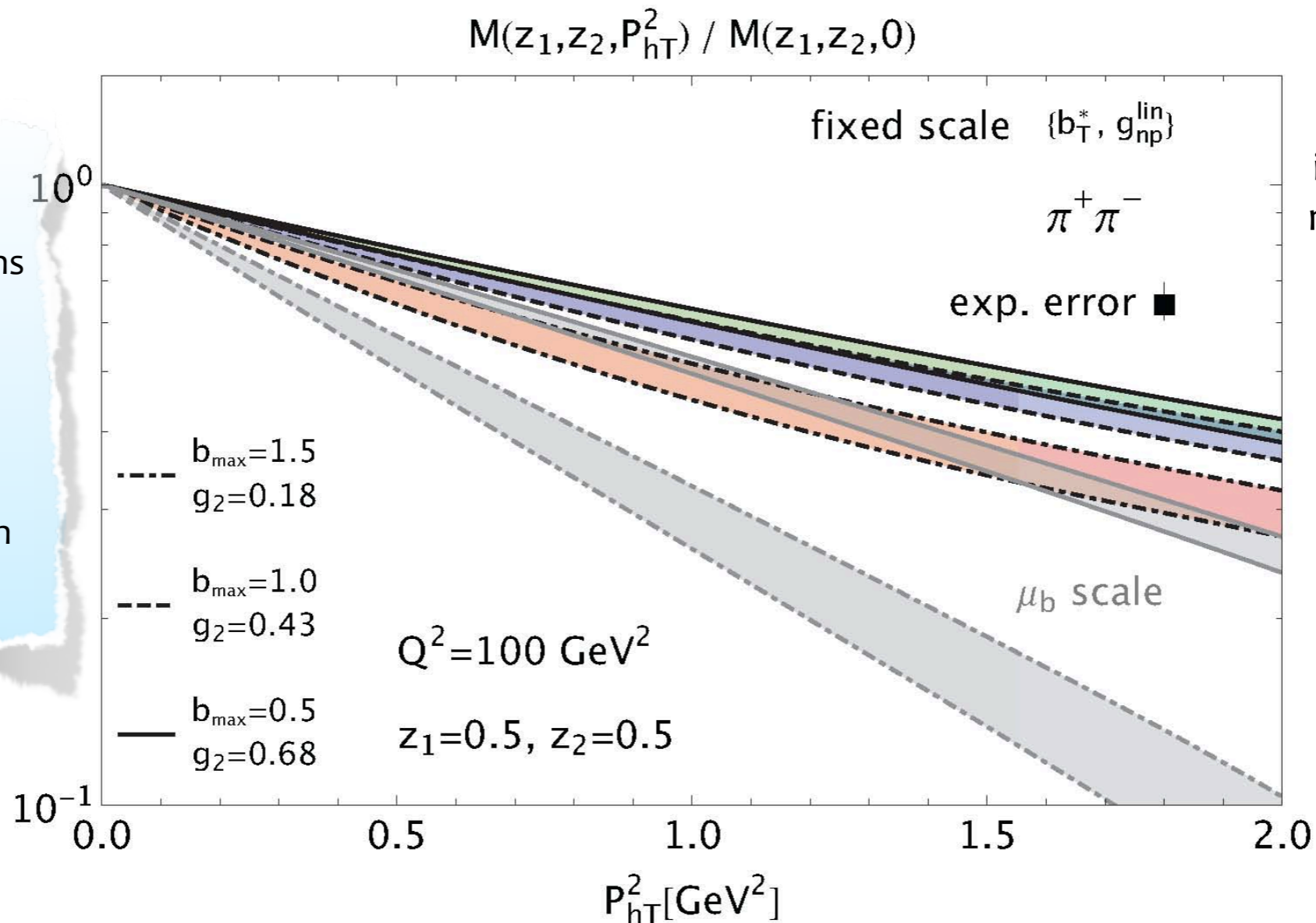
# ... factorization scale (evolution scheme)



using  $Q$  rather than  $\mu_b$   
 we get very different predictions

overall effect: larger distributions,  
 more perturbative content

# ... factorization scale (evolution scheme)



Q enhances the logs  
 in the evolved TMDs,  
 $\mu_b$  minimizes them:

overlap between  
 the two prescriptions  
 for different NP  
 parameters

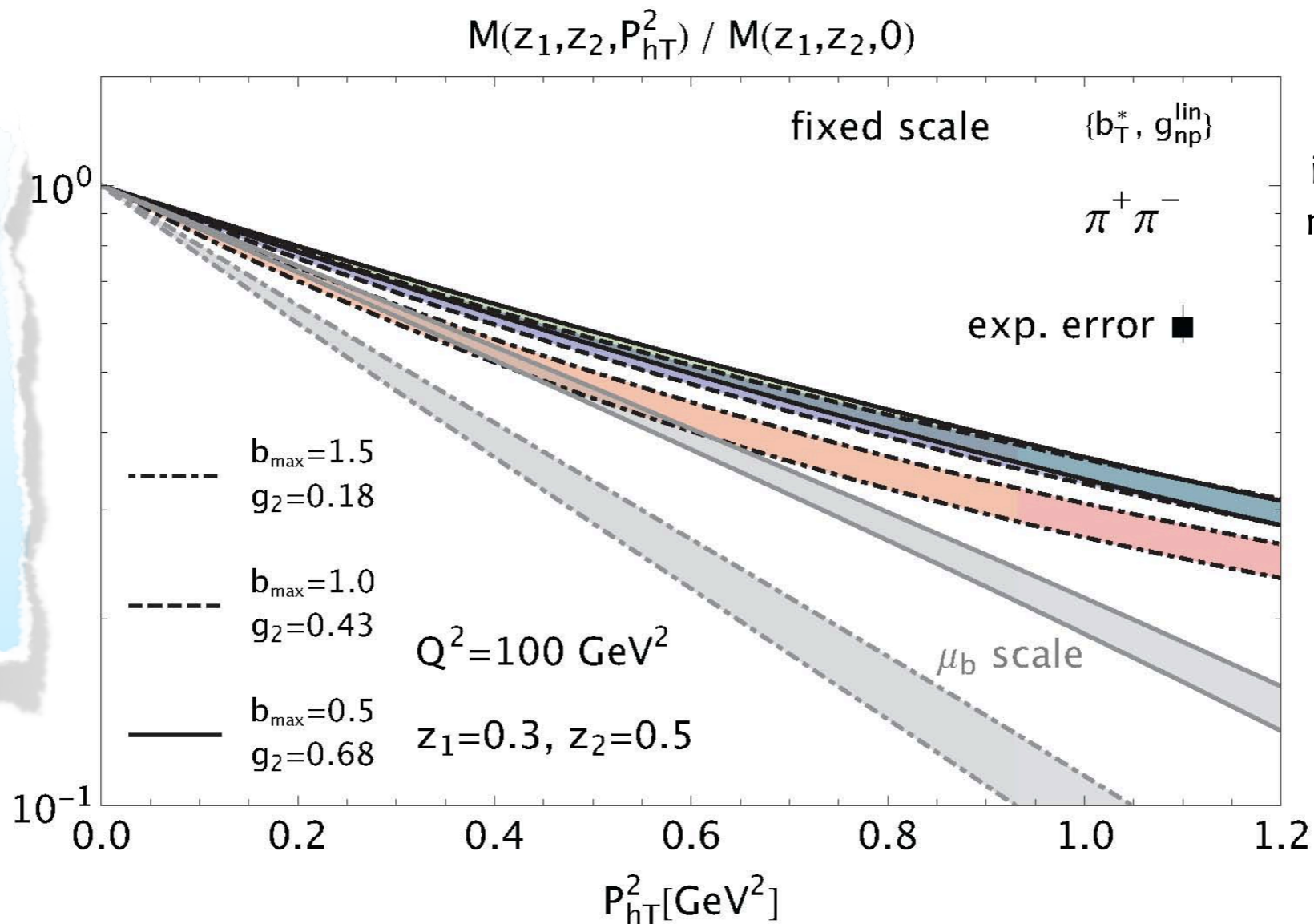
can't we distinguish  
 them?

using Q rather than  $\mu_b$   
 we get very different predictions

overall effect: larger distributions,  
 more perturbative content



# ... factorization scale (evolution scheme)



**Q enhances the logs** in the evolved TMDs,  $\mu_b$  minimizes them:

Yes, but only taking into account the  $z$  dependence too!

it requires **combined information** on  $P_{1\perp}$  and  $z_1, z_2$

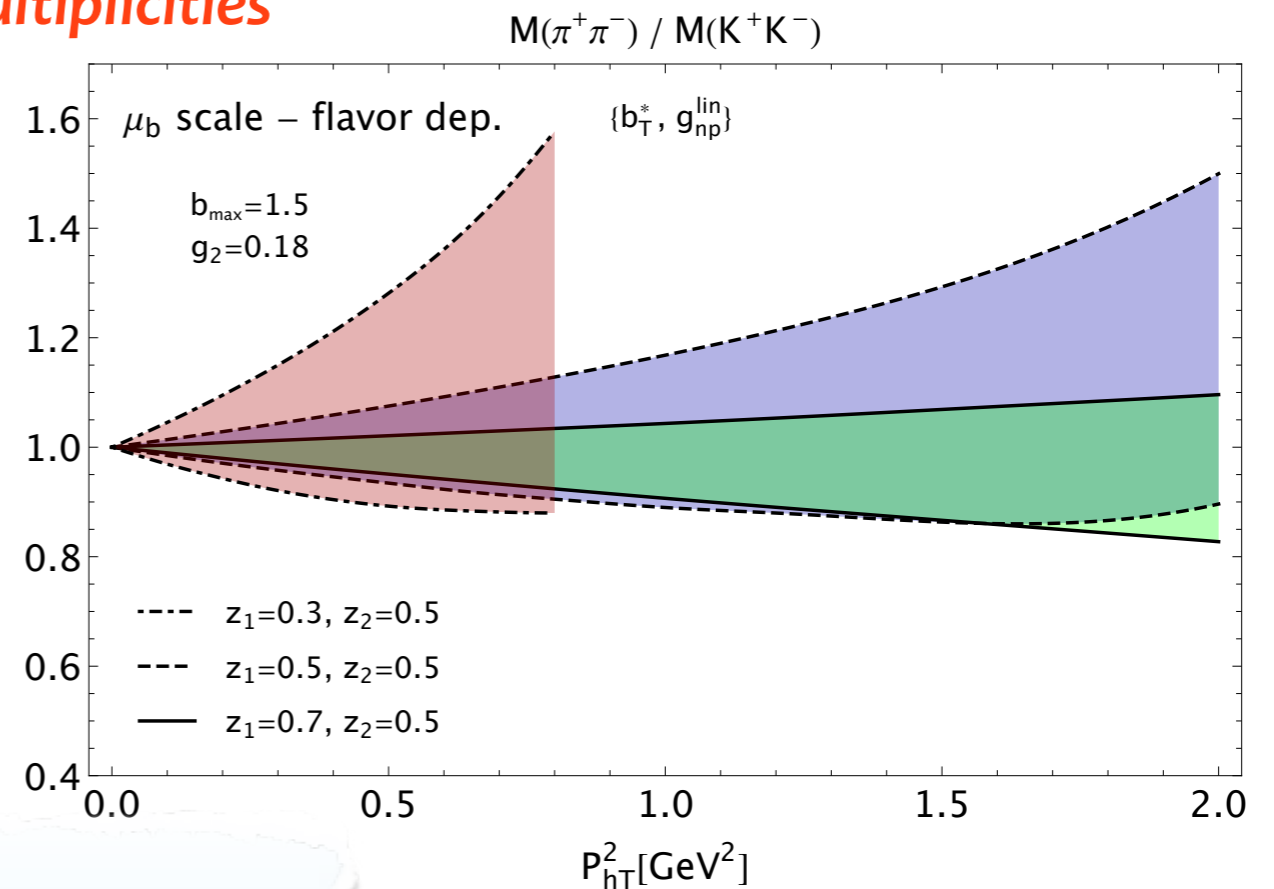
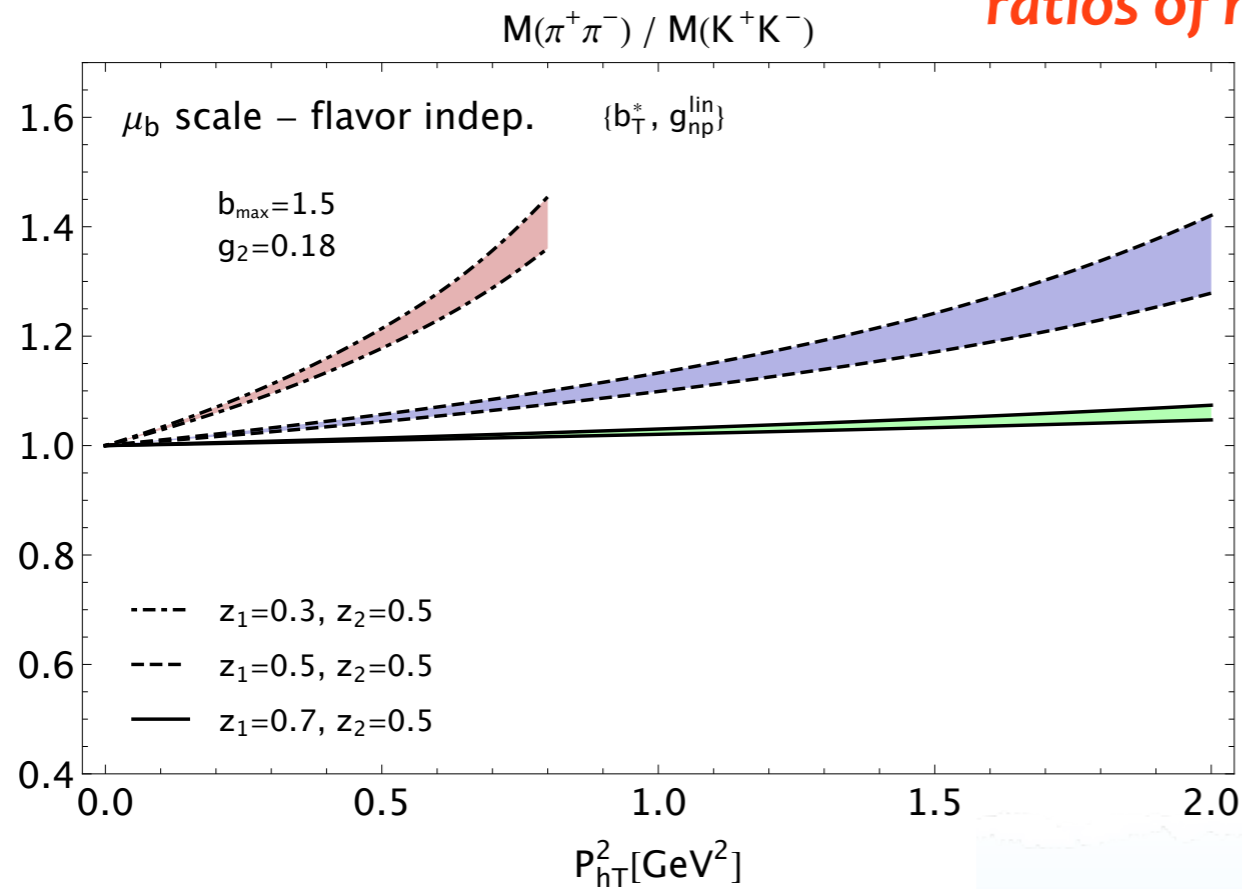
using **Q** rather than  $\mu_b$  we get very **different** predictions

overall effect: **larger** distributions, more perturbative content

# ... partonic flavor

*mu\_b scale evolution*

## ratios of multiplicities



this is the effect of the **perturbative flavor dependence ONLY:**

it is induced by RGE equations with flavor dependent initial conditions (collinear FF)

the transverse momentum dependence is described **BOTH** by the input NP Gaussian distributions and the collinear FF

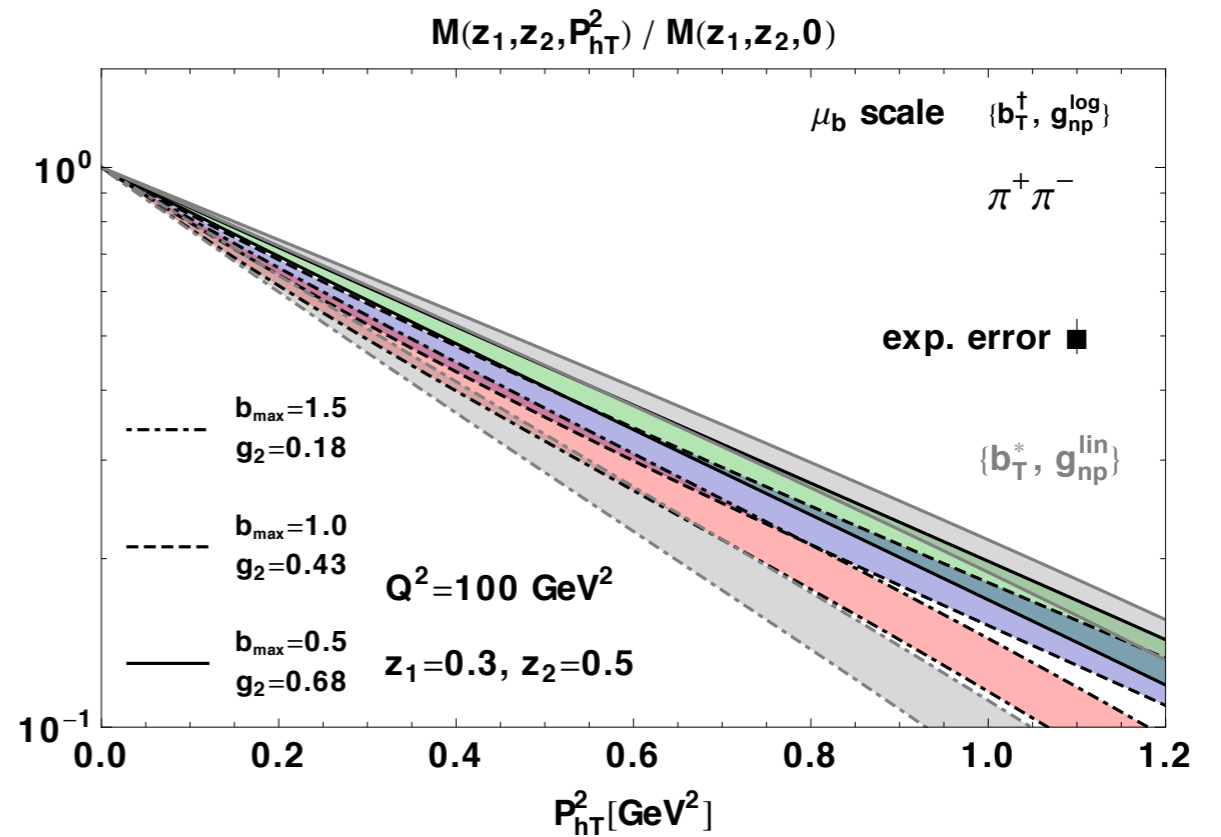
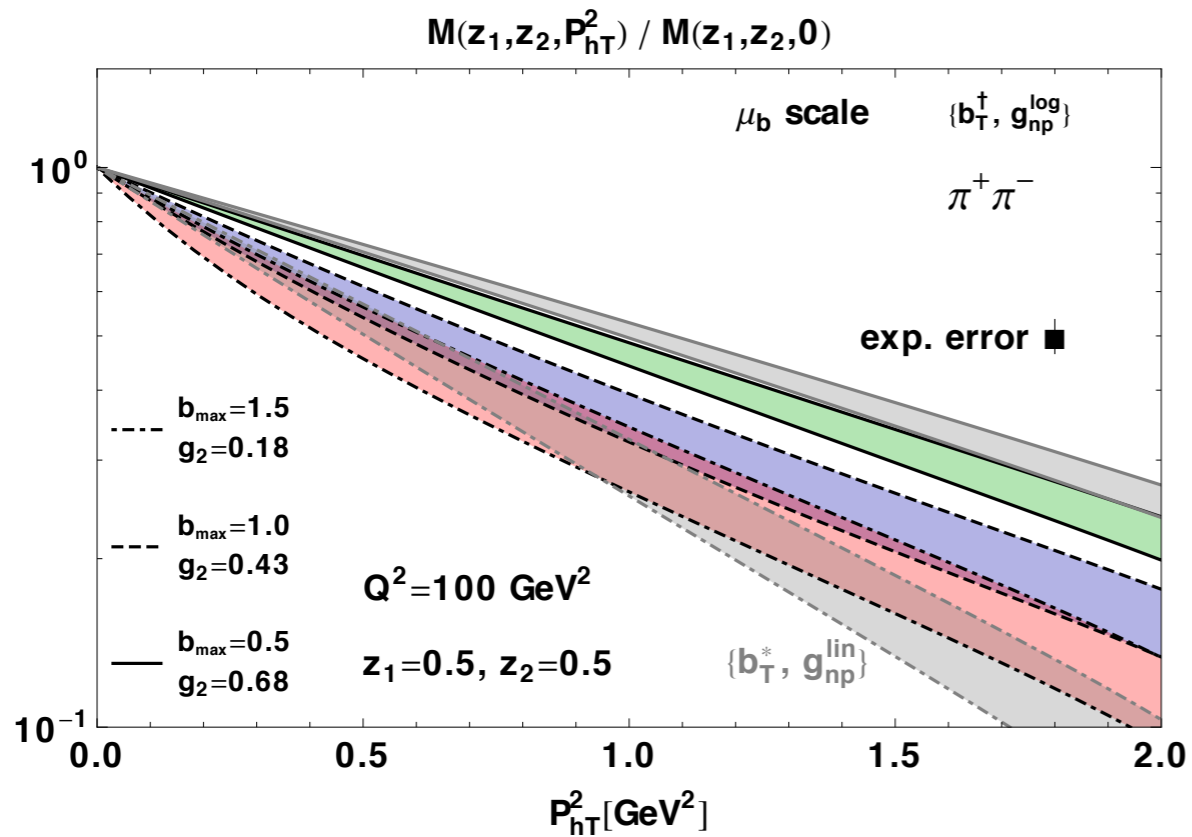
$$d_1^{q \rightarrow h}(z, \mu_b(b_T)) e^{-\frac{\langle k_T^2 \rangle_{q \rightarrow h}(z)}{4} b_T^2}$$

larger effect, combination of **perturbative and NP flavor dependence**

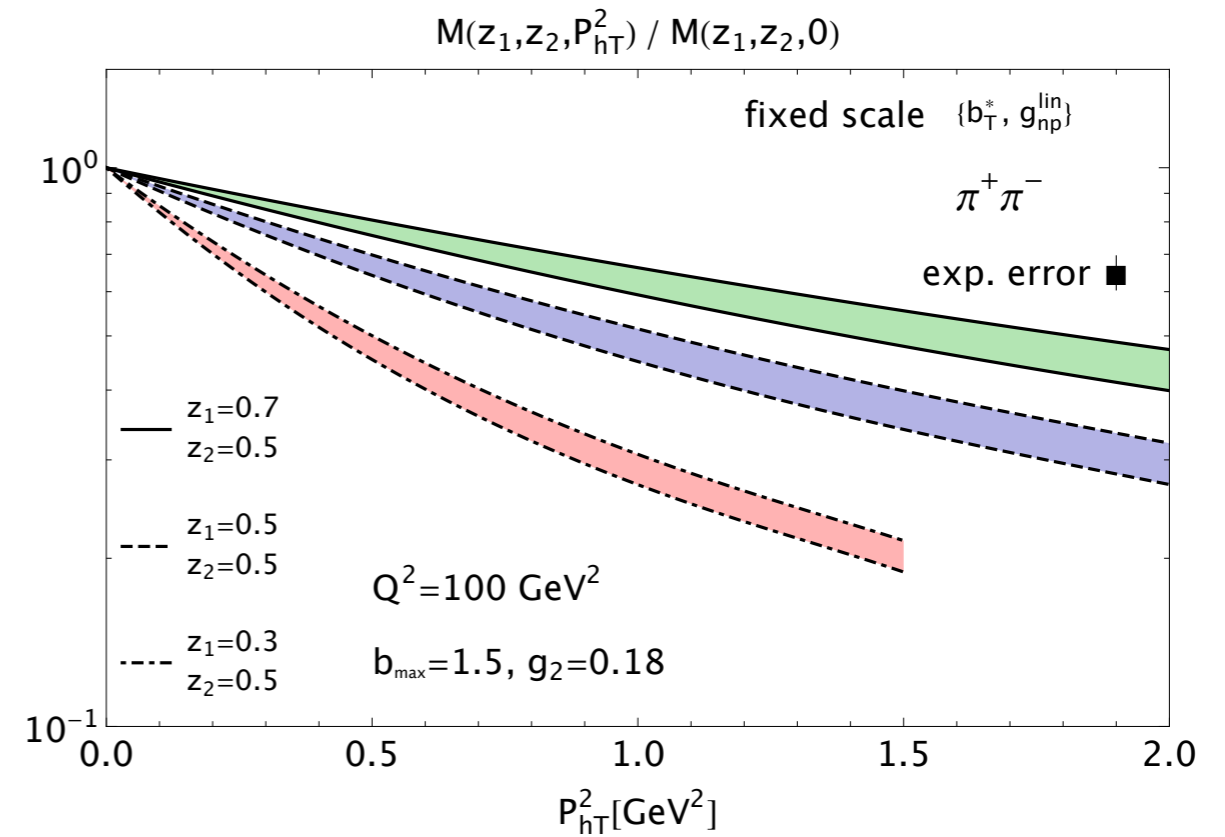
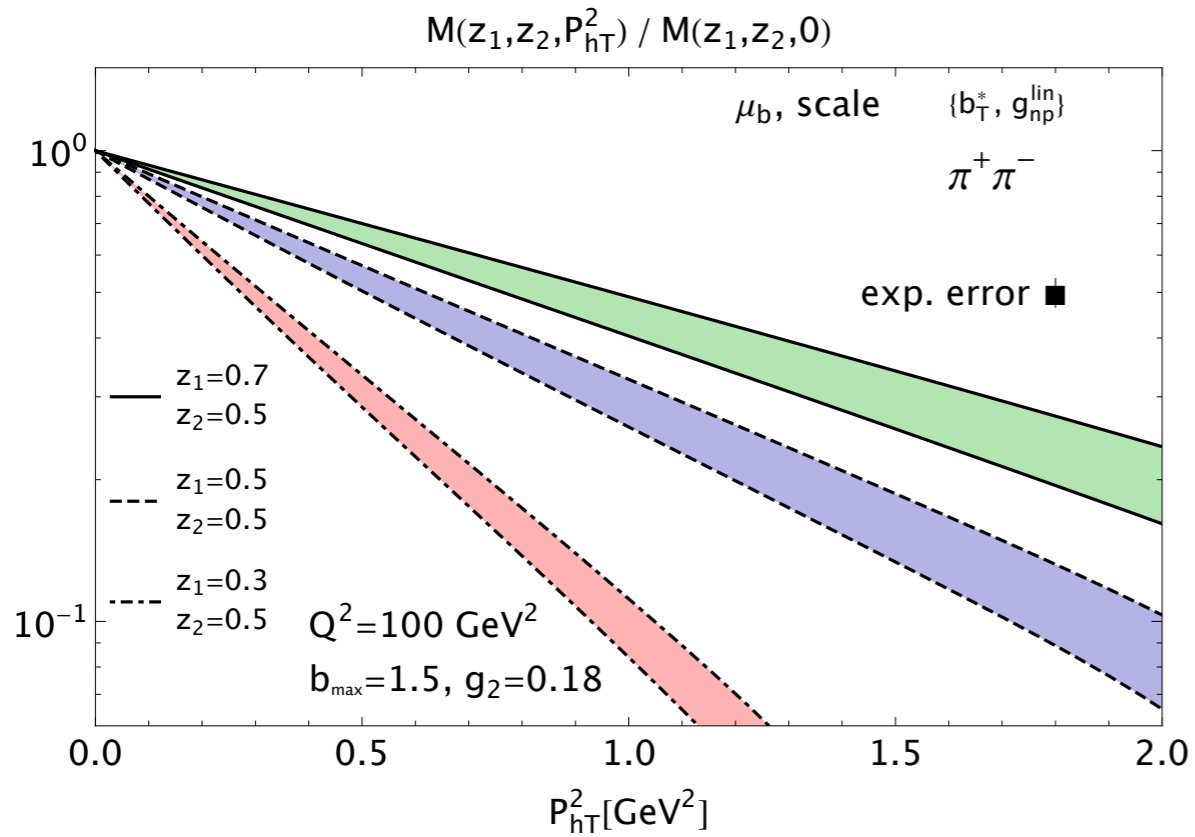
but the two are difficult to disentangle!

*exp. data may be useful to discriminate among the replicas*

# ... transition low/medium $q_T$



# ... collinear energy fractions $z_{1,2}$



# Conclusions - e+e-

## *Five take-home messages :*

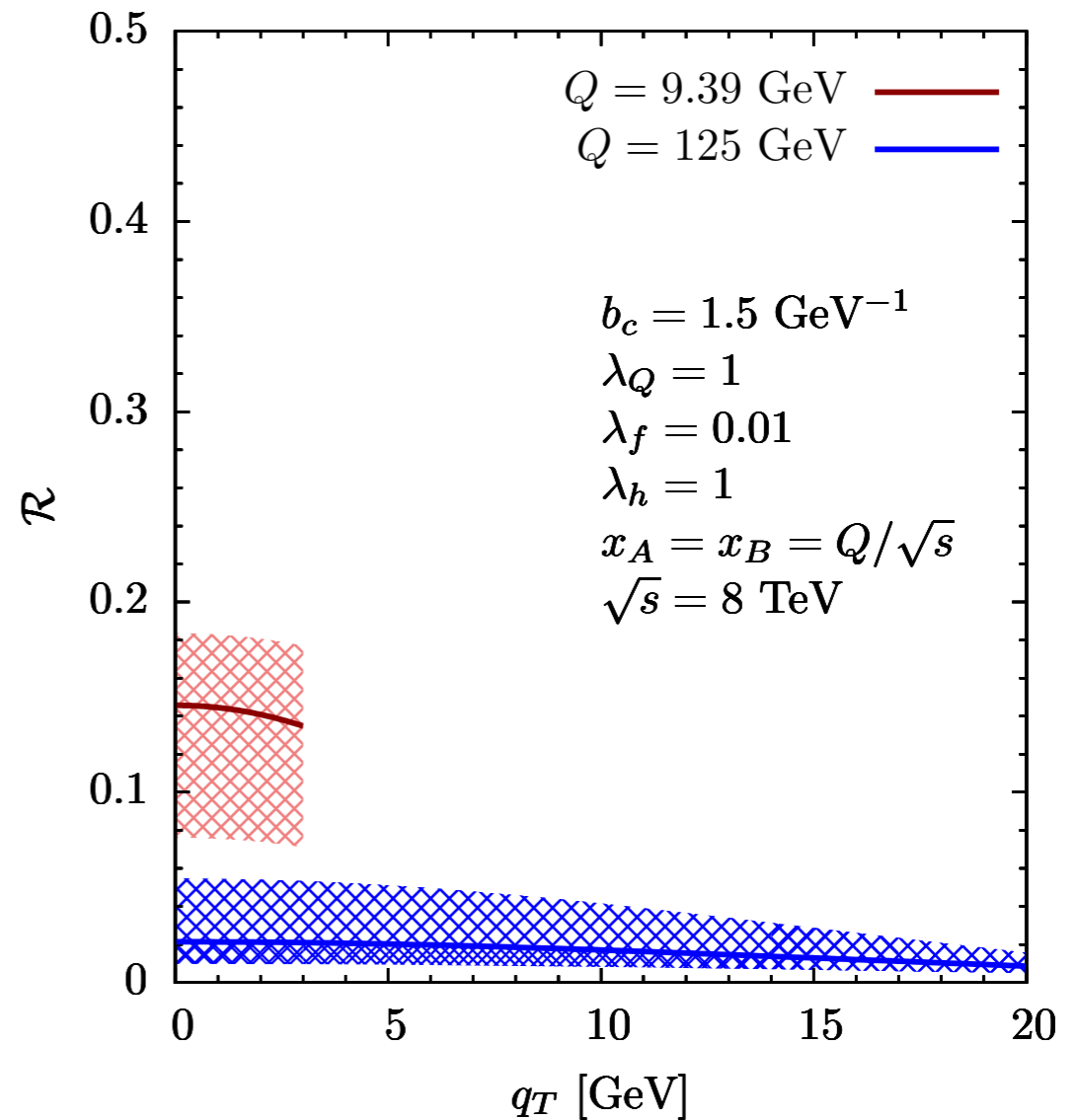
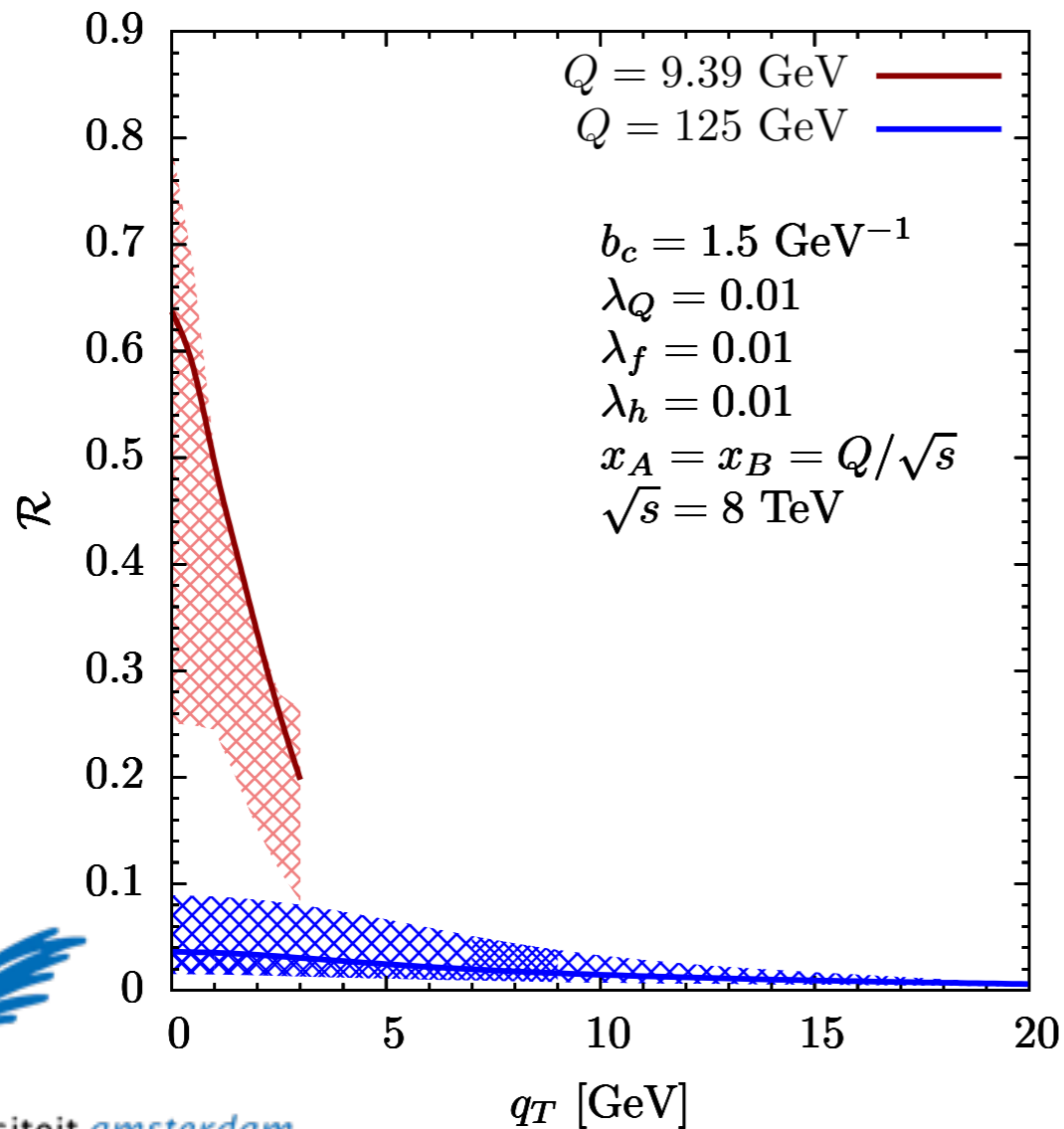
- o) The way we implement QCD evolution **affects the extraction** of non-perturbative information - [very important]
- 1) At Belle scale ( $100 \text{ GeV}^2$ ) we can discriminate **evolution schemes** and pin down non-perturbative **evolution parameters** ( $g_2$ ,  $b_{\text{max}}$ )
- 2) Annihilations at BES scale ( $14.6 \text{ GeV}^2$ ) can be very useful to **select non-perturbative intrinsic parameters** of TMD FFs
- 3) Annihilations to different final states  $\{\pi, K\}$  can be useful to **constrain flavor dependence** of TMD FFs
- 4) knowledge of unpolarized TMD FFs helps in constraining both **(un)polarized TMD PDFs** and **polarized TMD FFs**

# Linearly polarized **vs** unpolarized

$$\mathcal{R}(q_T; Q) = \frac{\mathcal{C} \left[ \begin{array}{cc} h_1^{\perp g/A} & h_1^{\perp g/B} \end{array} \right]}{\mathcal{C} \left[ \begin{array}{cc} f_1^{g/A} & f_1^{g/B} \end{array} \right]}$$

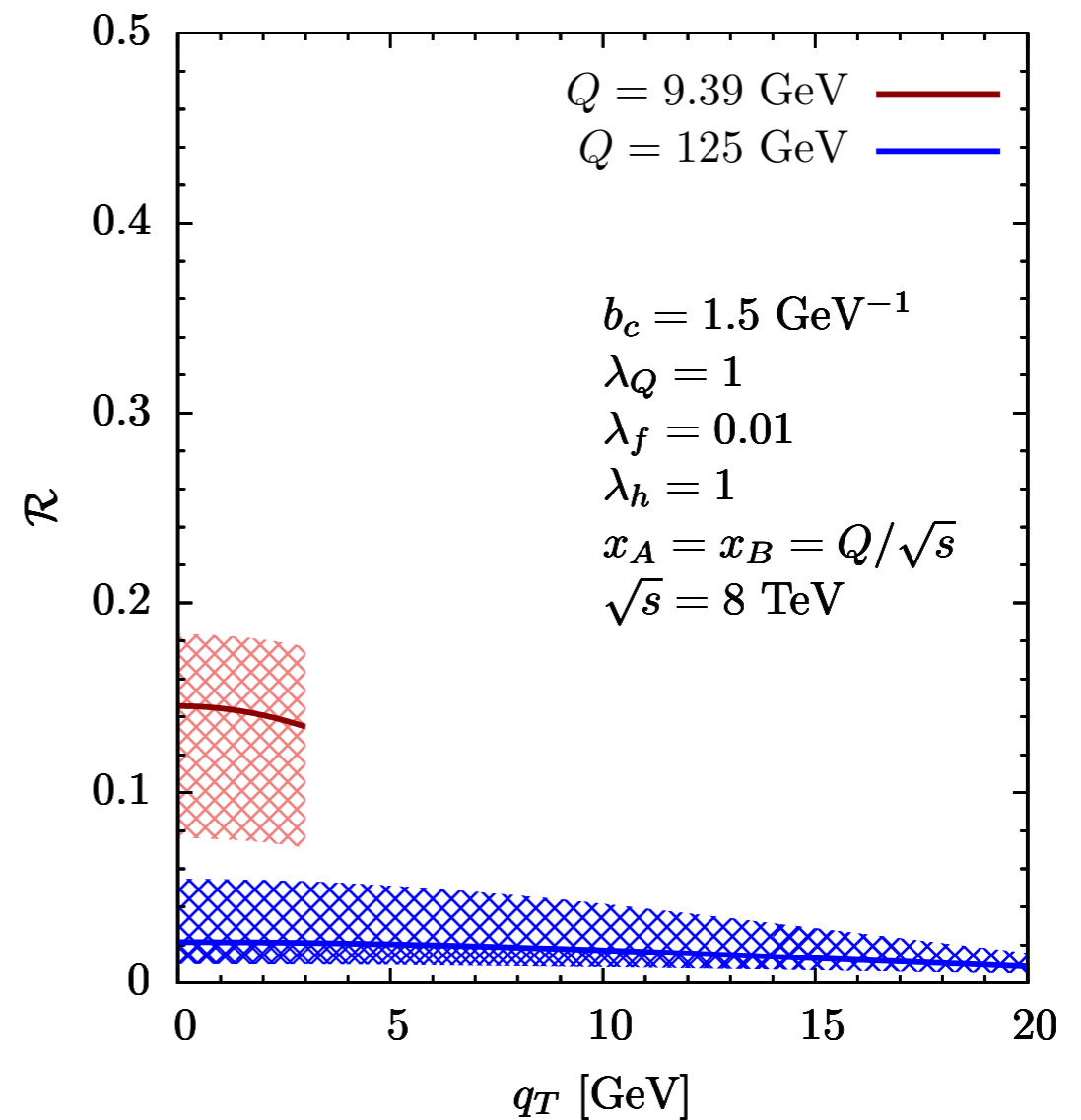
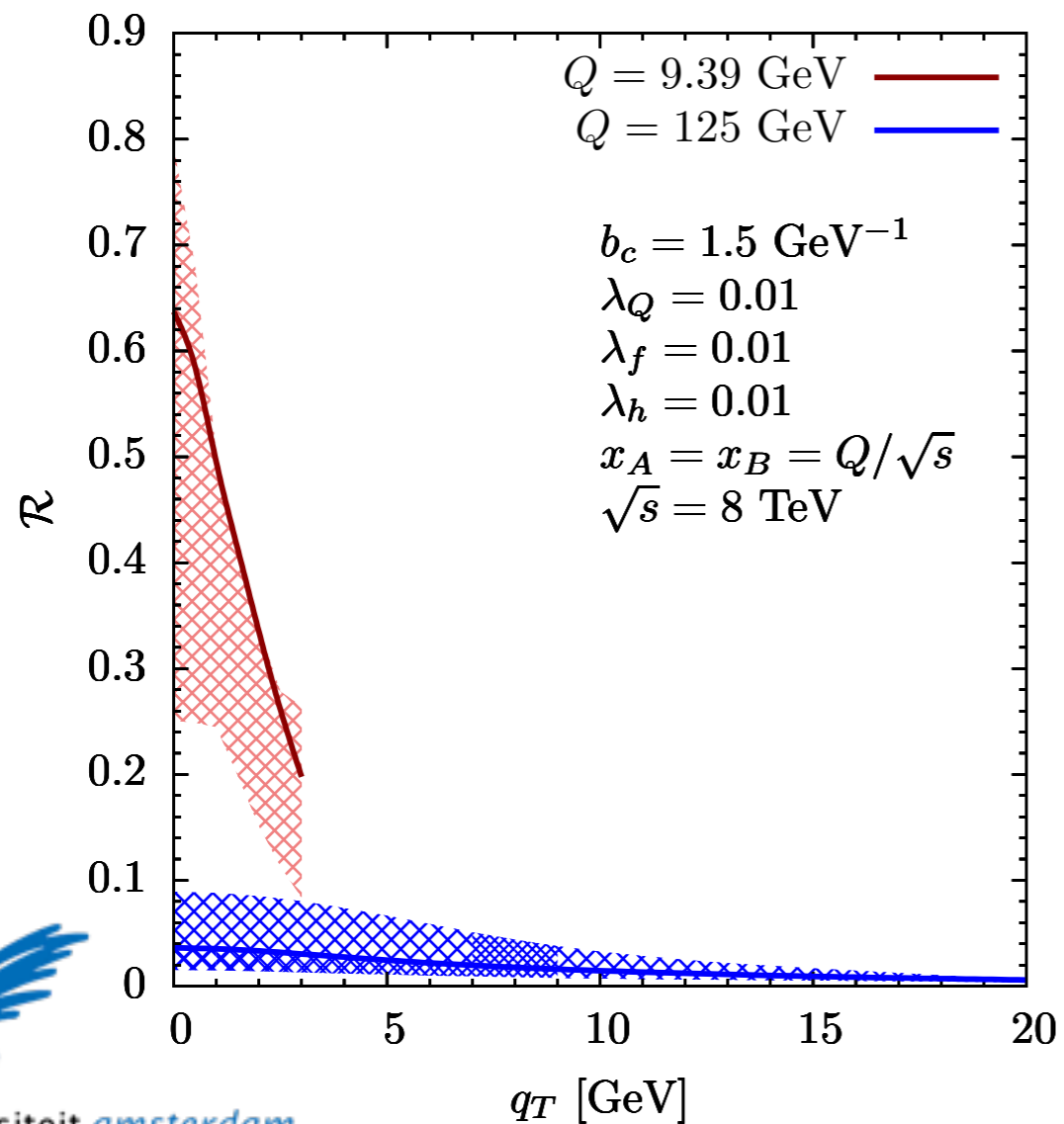
quarkonium - low energy

higgs - high energy



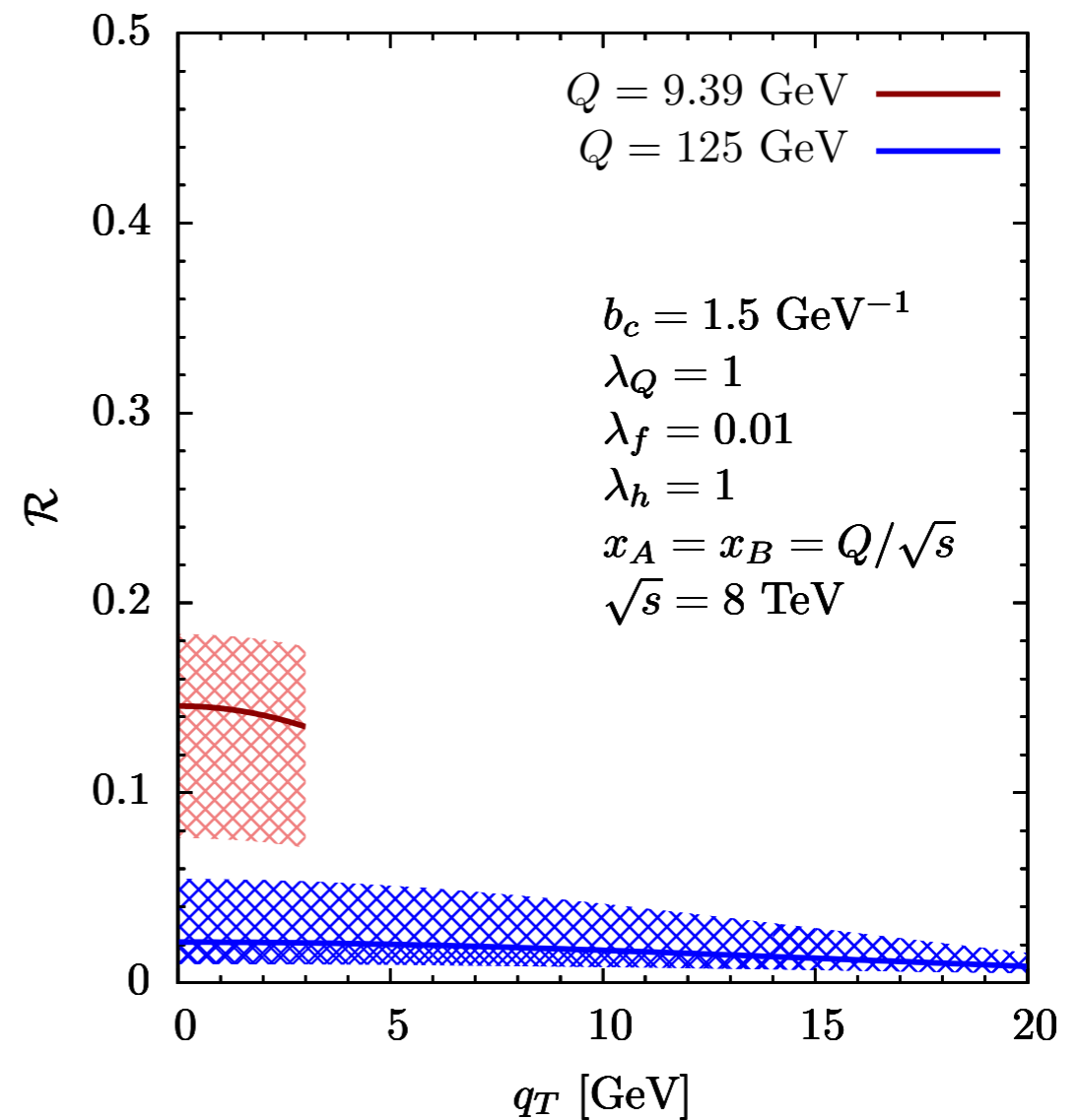
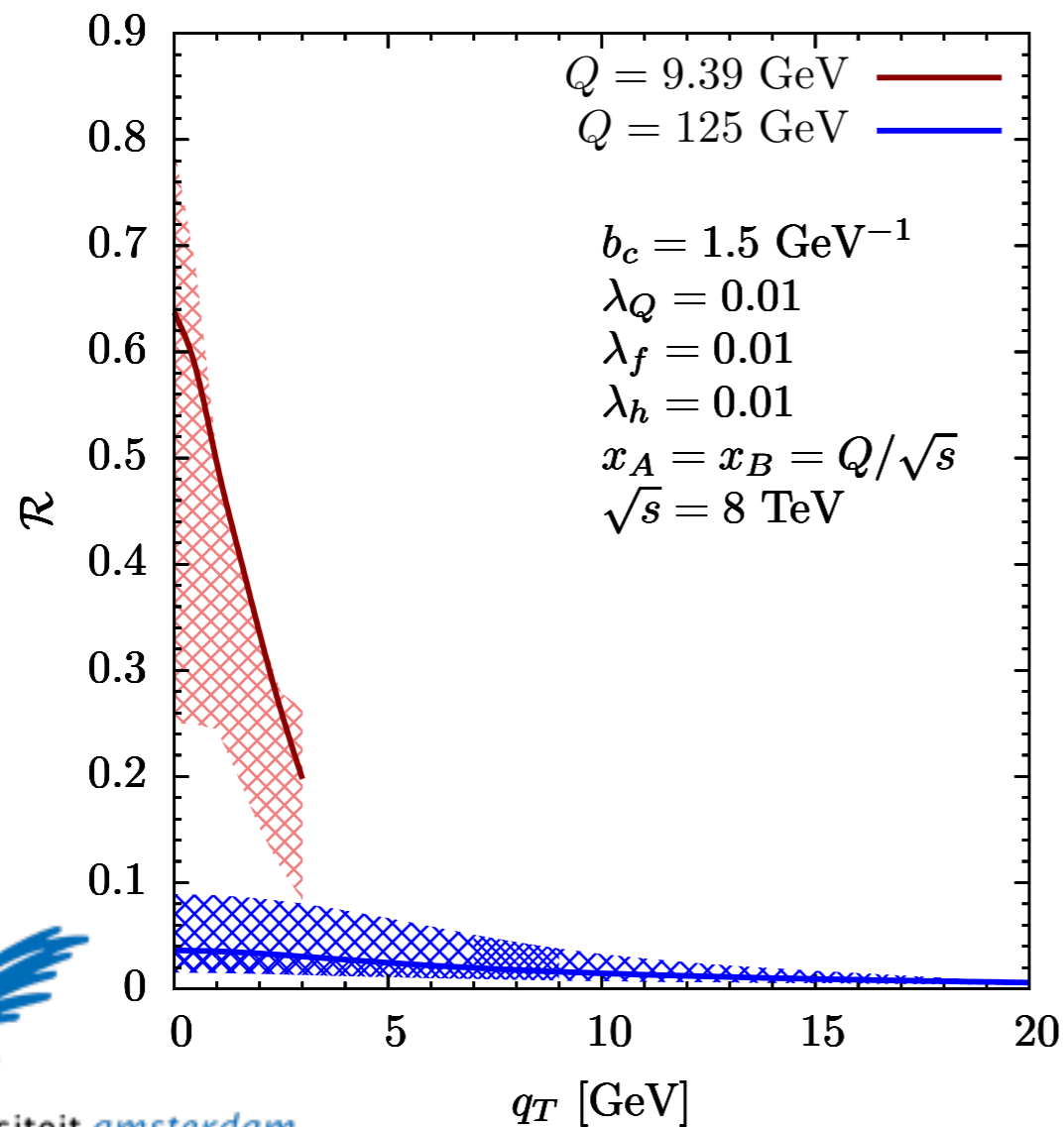
# Linearly polarized vs unpolarized

Nonperturbative physics  
enhanced at low  $Q$



# Linearly polarized vs unpolarized

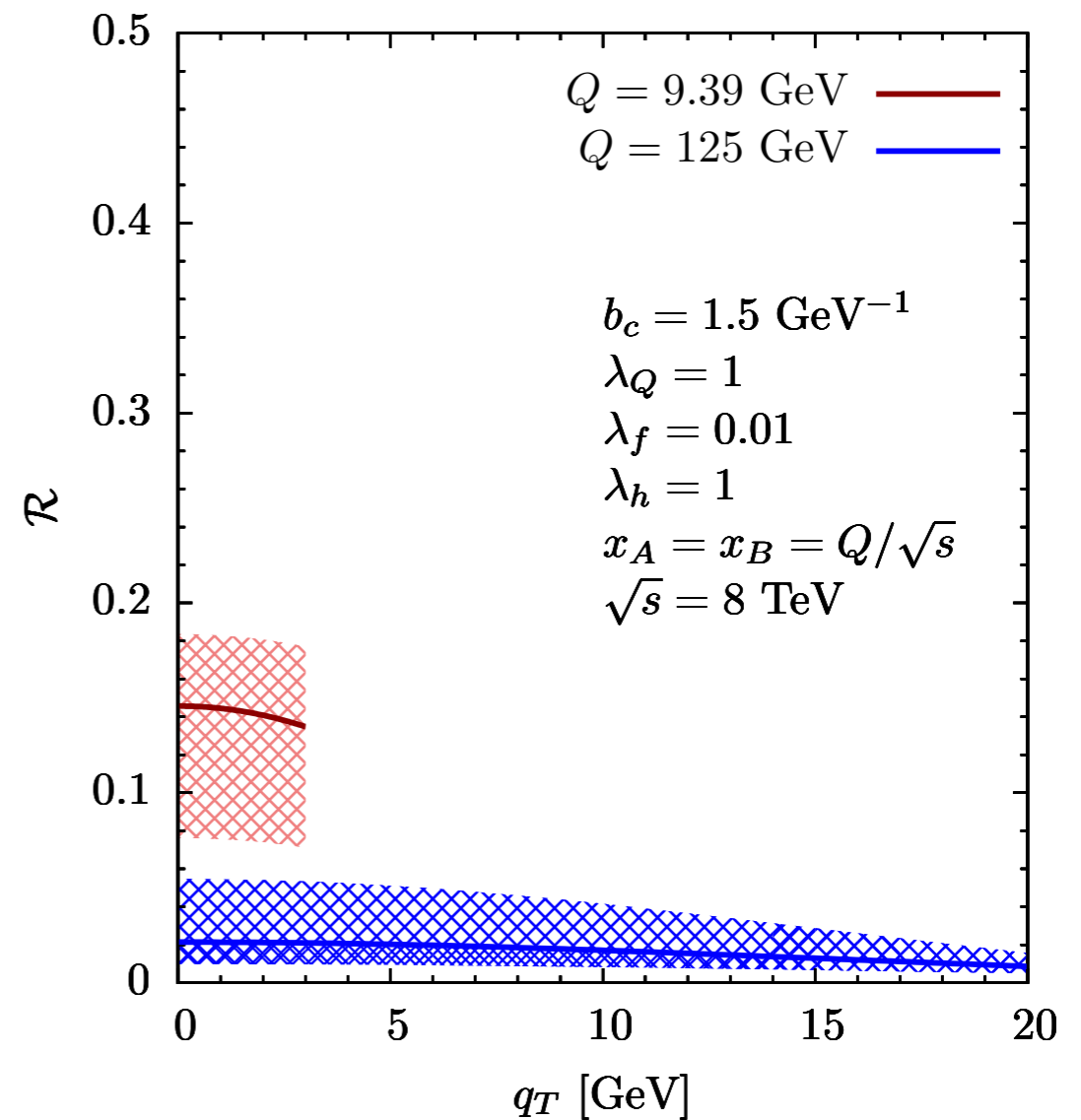
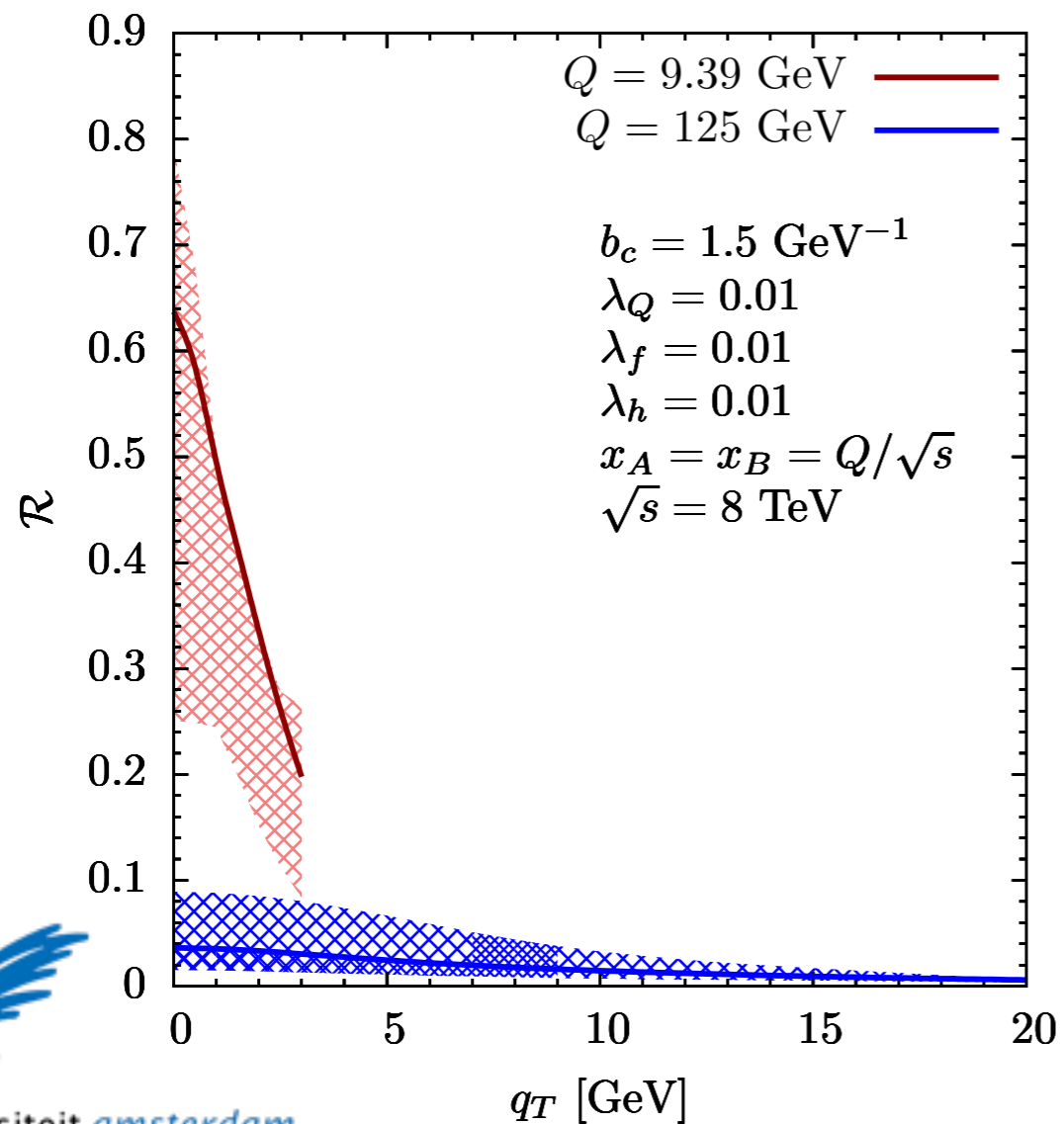
lin. pol. gluons :  
10% - 70% at low  $Q$





# Linearly polarized vs unpolarized

lin. pol. gluons :  
1% - 9% at high  $Q$



# SCET in a nutshell

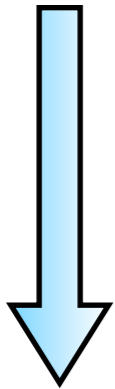
- 1) It is an **effective theory** of QCD
- 2) based on a systematic **expansion** of the QCD lagrangian in powers of small parameters
- 3) describes QCD interaction among low and high energy modes on the base of **separate lagrangians** for (ultra)soft and (anti)collinear modes
- 5) ASSUMPTION : SCET reproduces the IR structure of QCD ; need for a “matching” coefficient
- 6) useful to implement resummation | good for phenomenology

$$\mathcal{L}_{\text{QCD}} \longleftrightarrow \mathcal{L}_n + \mathcal{L}_{\bar{n}} + \mathcal{L}_{\text{soft}}$$

**Philosophy** : check if the **structure of the IR divergencies** is the same as in ‘full’ QCD. If so, the SCET-factorized form works as QCD, namely **factorization is “established”**

# A multistep matching process

QCD

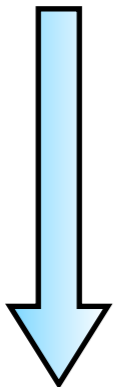


*factorization* of the cross section  
in terms of **TMD PDFs**

spin-independent  
**matching coefficient:**  
(square root of “hard part”)

$$C_H$$

NRQCD  $\oplus$  SCET <sub>$q_T$</sub>



*re-factorization* of TMD PDFs  
on the basis of **PDFs**

spin-dependent  
**matching coefficient:**  
(OPE Wilson coeffs.)

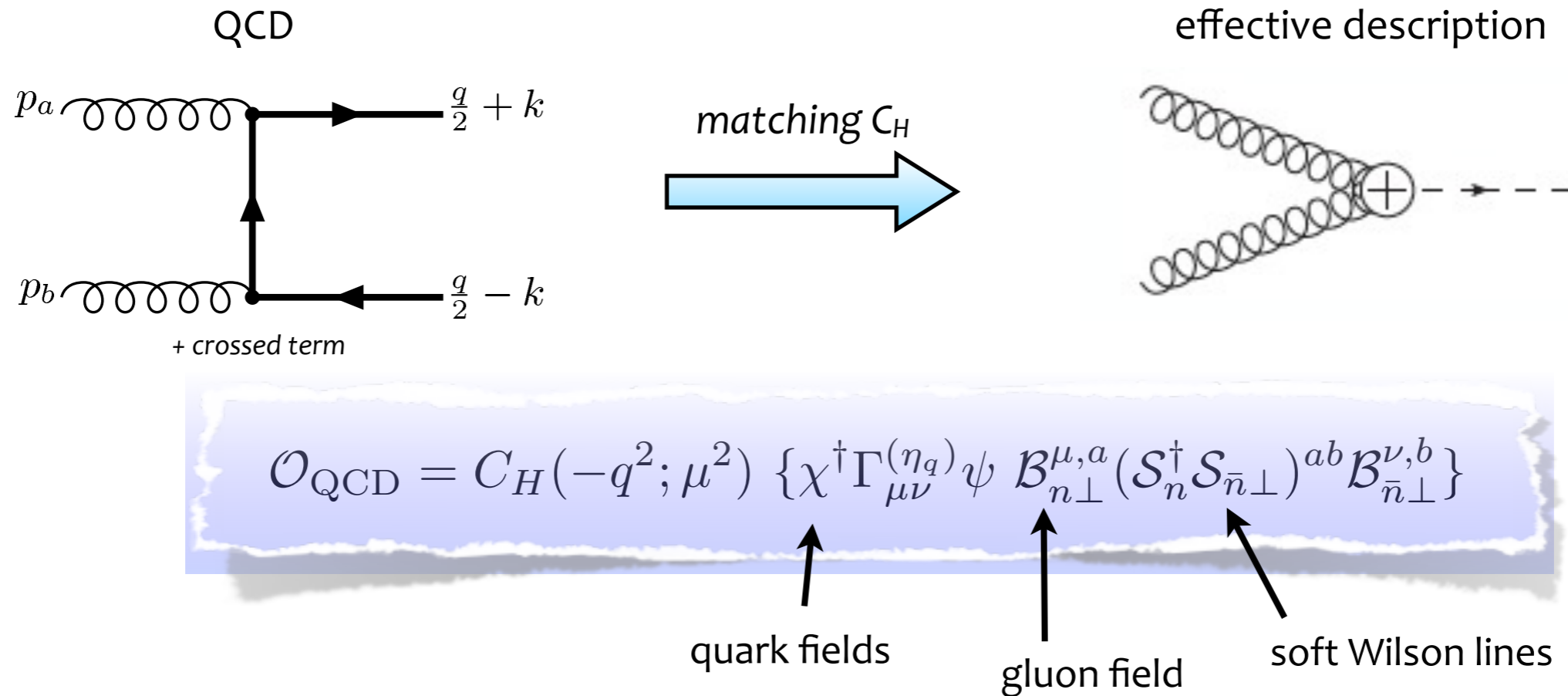
$$\tilde{C}_{g/j}^T$$

NRQCD  $\oplus$  SCET <sub>$\Lambda_{\text{QCD}}$</sub>



# 1 : factorization

$$\text{QCD} \rightarrow \text{NRQCD} \oplus \text{SCET}_{q_T}$$



$$d\sigma = \frac{1}{2s} \frac{d^3q}{(2\pi)^3 2E_q} \int d^4y e^{-iq \cdot y} \sum_X \langle PS_A, \bar{P}S_B | \mathcal{O}(y) | X + \eta_q \rangle \langle X + \eta_q | \mathcal{O}(0) | PS_A, \bar{P}S_B \rangle$$

# 1 : factorization

QCD  $\rightarrow$  NRQCD  $\oplus$  SCET $_{q_T}$

$$\frac{d\sigma}{dyd^2q_\perp} \sim \mathcal{O}^{q\bar{q}}(\eta_q) |C_H|^2 \Gamma_{\mu\alpha}^\dagger \Gamma_{\nu\beta}$$

$$\times \hat{\text{FT}} \left[ \tilde{G}_{g/A}^{\mu\nu}(x_A, b_T, S_A; \mu, \zeta_A) \tilde{G}_{g/B}^{\alpha\beta}(x_B, b_T, S_B; \mu, \zeta_B) \right]$$

$$+ \mathcal{O}(q_T/M)$$

gluon correlators in IPS  
(see M. Echevarría's talk)

TMD factorization region

medium/high  $q_T$  corrections

1)  $|CH|^2$  is the “hard part”: at this point still not known

2) NRQCD matrix element

$$\mathcal{O}^{q\bar{q}}(\eta_q) = |\langle 0 | \chi^\dagger \psi(y) | \eta_q \rangle|^2 = \frac{N_c}{2\pi} |R_{nl}(0)|^2 [1 + \mathcal{O}(v^4)]$$

3) Gamma structure fixed to reproduce the LO QCD result

$$\Gamma_{\mu\nu} = \frac{\alpha_s \pi}{3\sqrt{M}} \frac{2\sqrt{2}\epsilon_{\mu\nu}^\perp}{\sqrt{(d-2)(d-3)}} \sqrt{N_c^2 - 1}$$

**but no pole structure yet:** go to next order!

# 1 : factorization

QCD  $\rightarrow$  NRQCD  $\oplus$  SCET<sub>qT</sub>

$$\frac{\sigma^v}{\sigma_{\text{Born}}}\Big|_{\text{ren}} = \frac{\alpha_s}{2\pi} \left[ -2 \frac{C_A}{\epsilon_{\text{IR}}^2} - \frac{2}{\epsilon_{\text{IR}}} \left( \frac{\beta_0}{2} + C_A \ln \frac{\mu^2}{M^2} \right) + 2C_F \frac{\pi^2}{2v} - C_A \ln^2 \frac{\mu^2}{M^2} + 2C_A \left( 1 + \frac{\pi^2}{3} \right) + 2C_F \left( -5 + \frac{\pi^2}{4} \right) \right]$$

Coulomb singularity absorbed by NRQCD matrix element

renormalization takes care of UV

$$\tilde{f}_1^g = \frac{\alpha_s}{2\pi} \left[ \frac{C_A}{\epsilon_{\text{UV}}^2} + \frac{1}{\epsilon_{\text{UV}}} \left( \frac{\beta_0}{2} + C_A \ln \frac{\mu^2}{\zeta_A} \right) - \frac{C_A}{\epsilon_{\text{IR}}^2} - \frac{1}{\epsilon_{\text{IR}}} \left( \frac{\beta_0}{2} + C_A \ln \frac{\mu^2}{\zeta_A} \right) \right]$$

X 2 TMDs

**Yes!**

SCET correctly reproduces QCD at NLO

$$\mathcal{H} = \left[ \sigma^{\text{virt},(1)} - \left\{ \tilde{f}_1^{g/A} \tilde{f}_1^{g/B} \right\}_{\text{virt}}^{(1)} \right]$$

on-shell renormalization scheme

$$\mathcal{H} = 1 + \frac{\alpha_s}{2\pi} \left[ -C_A \ln^2 \frac{\mu^2}{M^2} + 2C_A \left( 1 + \frac{\pi^2}{3} \right) + 2C_F \left( -5 + \frac{\pi^2}{4} \right) \right]$$

see Phys. Rev. D 70, 054014  
(Maltoni&Polosa),

Phys.Rev. D48 (1993) (Kuhn&Mirkes)

**Useful**

# 2 : re-factorization

$$\text{NRQCD} \oplus \{ \text{SCET}_{q_T} \rightarrow \text{SCET}_{\Lambda_{\text{QCD}}} \}$$

OPE - matching coefficient

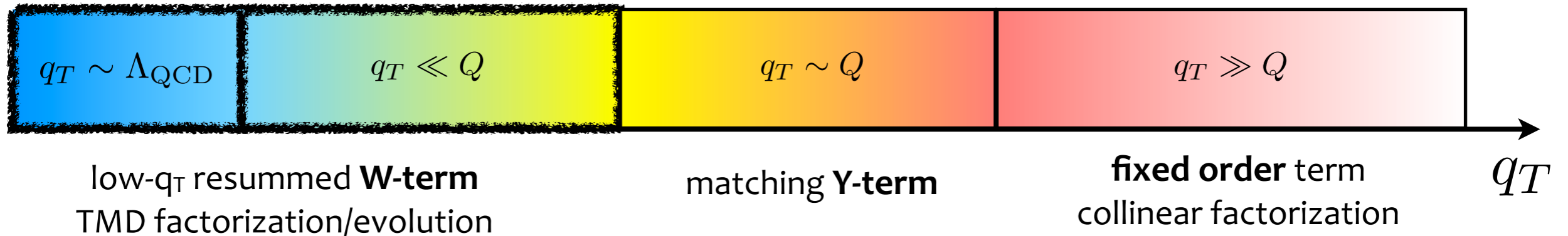
$$\tilde{T}_{g/A}(x, b_T; \mu, \zeta) = \sum_{j=q, \bar{q}, g} \tilde{C}_{g/j}^T(x, b_T; \mu, \zeta) \otimes t_{j/A}(x; \mu) + \mathcal{O}(b_T \Lambda_{\text{QCD}})$$

TMD PDF

medium/high  $q_T$   
Sudakov form factor  
+ perturbative tail

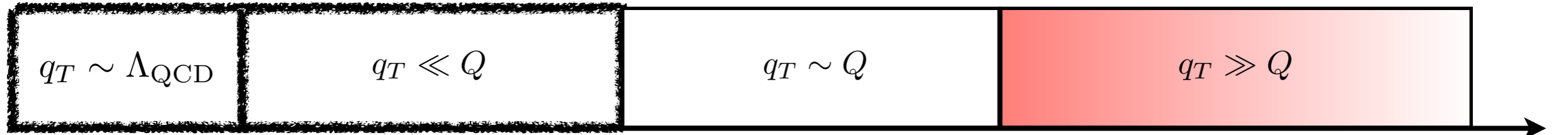
PDF

intrinsic low  $q_T$   
(model)



transverse momentum spectrum of physical observables

# Unpolarized phenomenology



high  $q_T$  spectrum

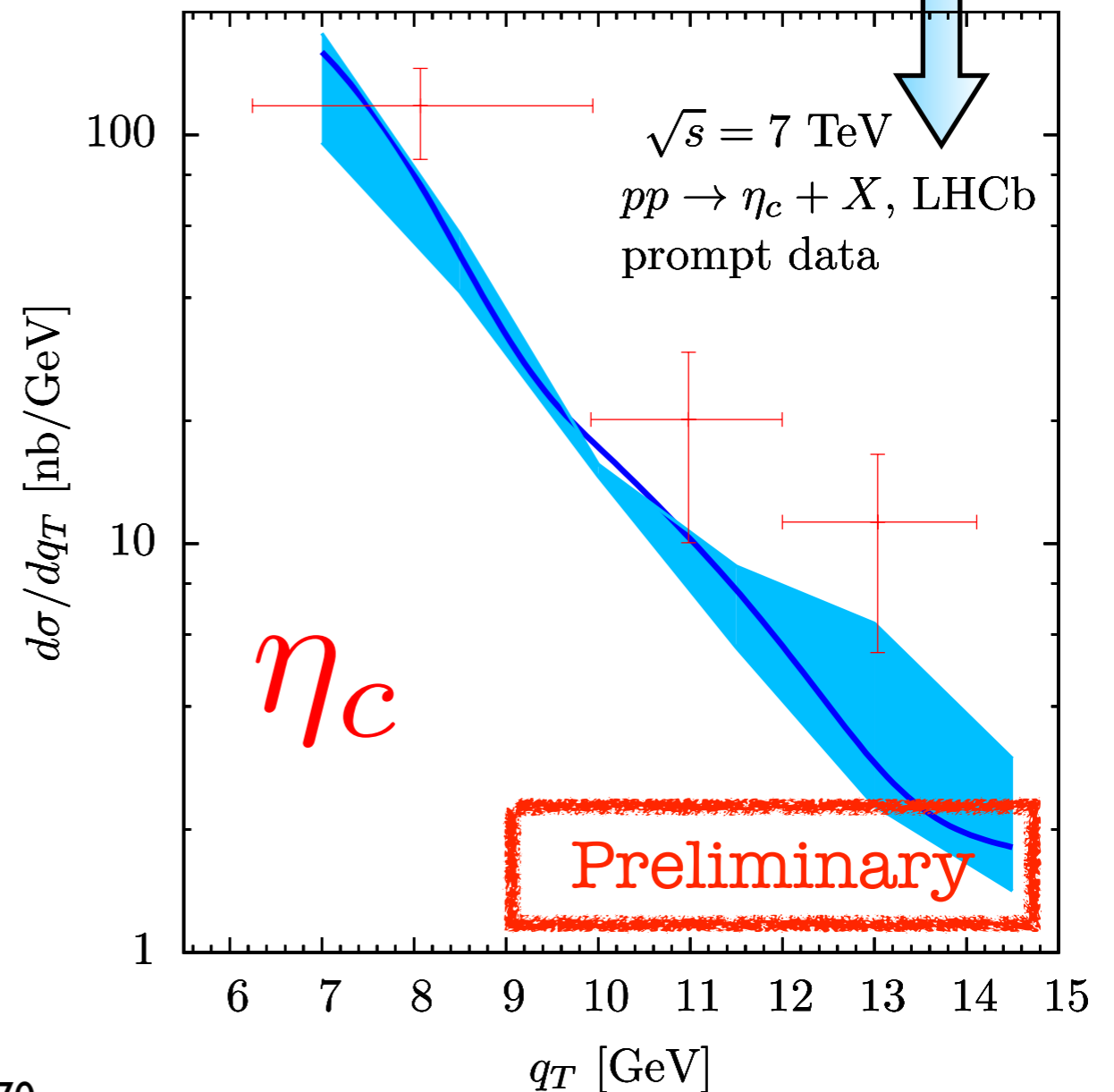
**LHCb data**

Eur. J. Phys. C75 (2015) 311

partonic calculation from  
Phys.Rev. D48 (1993) 179-189  
(Kuhn&Mirkes)

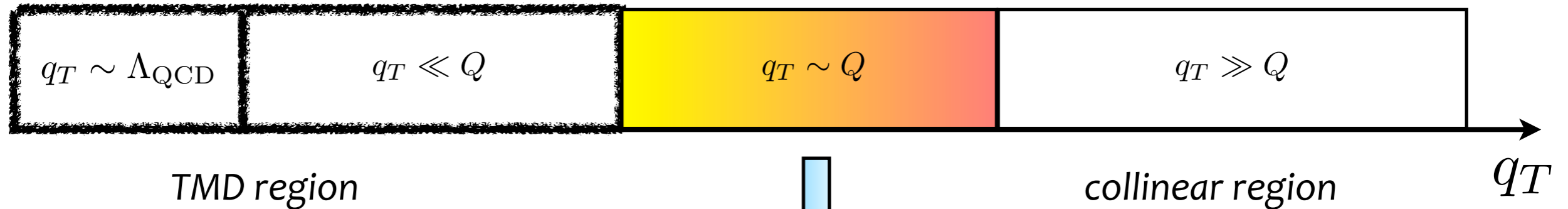
NRQCD from Phys. Rev. Lett. 114, 092004

collinear factorization





# Unpolarized phenomenology



**Y term :**

matching between  
low and high transverse momenta

(see O. Gonzalez's talk)

$$Y = \frac{d\sigma^{q_T \gg Q}}{dq_T} - \frac{d\sigma^{\text{ASY}}}{dq_T}$$

On the to-do list!

# Conclusions

---

- 1) **Factorization** for  $q_T$  spectrum of quarkonium has been established at NLO using the SCET methodology
- 2) we can make solid **predictions** for (un)polarized TMD cross sections for LHC, RHIC, AFTER@LHC
- 3) implementing perturbative content we can set the grounds for the **extraction** of information about the **proton structure** (provided that we'll get data!)

# The gluon Sivers effect

$$f_{1T}^{g\perp}$$

Review Boer-Lorcé-Pisano-Zhou  
Message : the effect is **not constrained!**

usual argument : since **BSM** holds,  
we know it should be suppressed

two **objections**:

- 1) the **numerical extractions** are strongly model dependent and performed at LO
- 2) we know that any gluon Sivers is given by the sum of two universal gluon Sivers function (**process dependence**), one of each is constrained by BSM and the other not (since the momentum operator is C-even, the C- even function is constrained, but the C-odd on no

then there is need for **improved predictions and extractions**: we need the theoretical tools



# SCET gluon fields

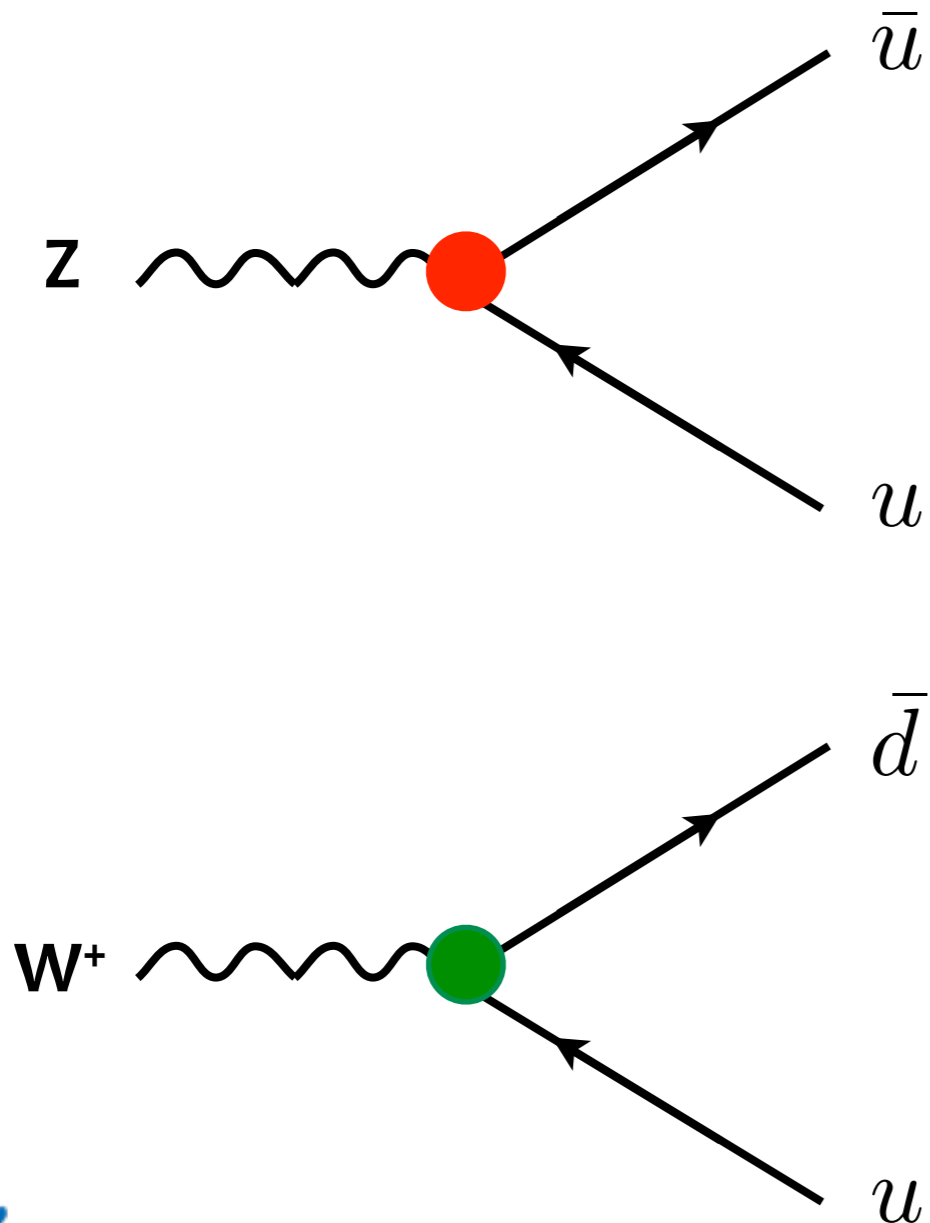
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$$\mathcal{B}_{n\perp}^\mu = \frac{1}{g} [\bar{n} \cdot \mathcal{P} W_n^\dagger i D_{n\perp}^\mu W_n]$$

$$W_n(x) = P \exp \left[ \int_{-\infty}^0 ds \bar{n} \cdot A_n^a(x + \bar{n}s) t^a \right]$$

$$\mathcal{S}_n(x) = P \exp \left[ \int_{-\infty}^0 ds n \cdot A_s^a(x + ns) t^a \right]$$

# Quark TMDs at the LHC

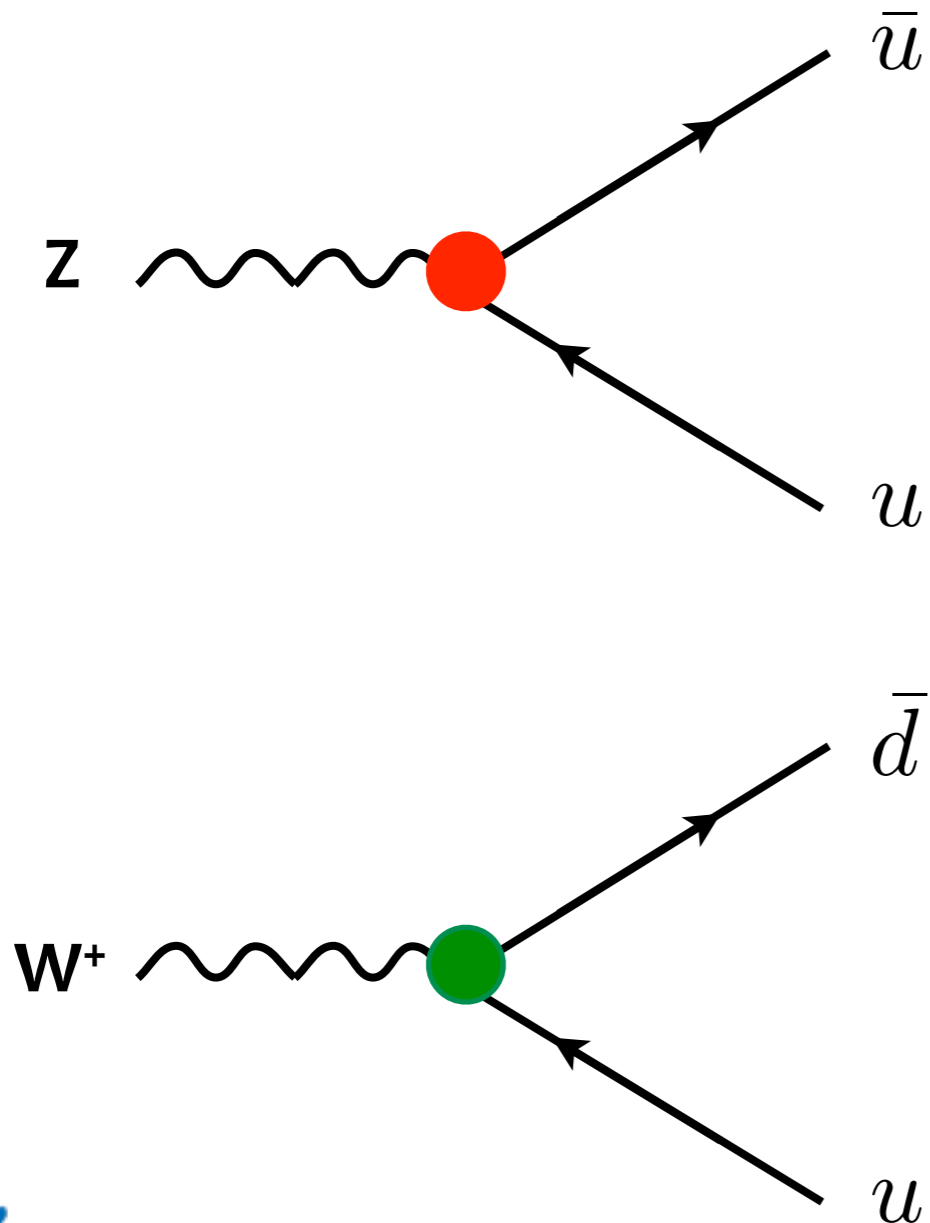


$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

$$\sim \mathcal{C} \left[ \begin{array}{cc} f_1^{q/A} & f_1^{q/B} \end{array} \right] \pm \mathcal{C} \left[ \begin{array}{cc} h_1^{\perp q/A} & h_1^{\perp q/B} \end{array} \right]$$

unpolarized quarks                      transv. polarized quarks

# Quark TMDs at the LHC



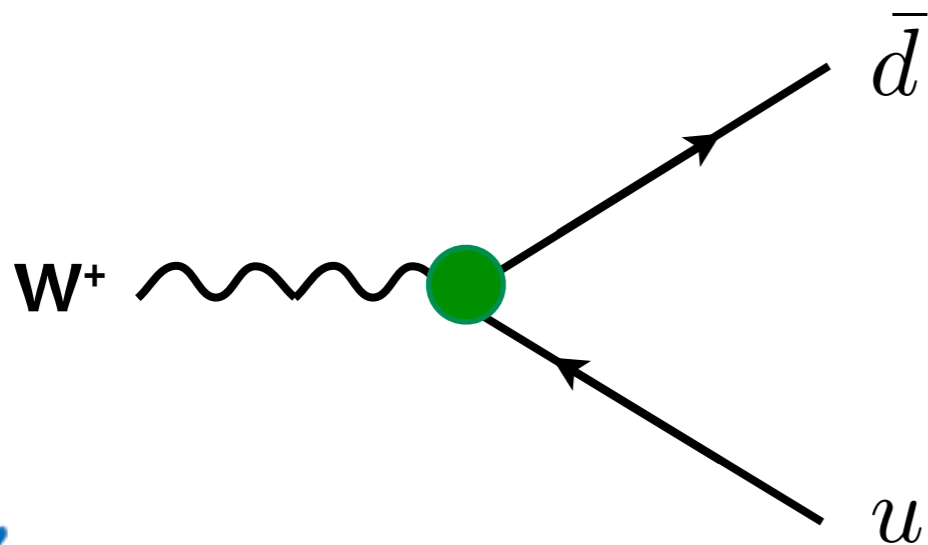
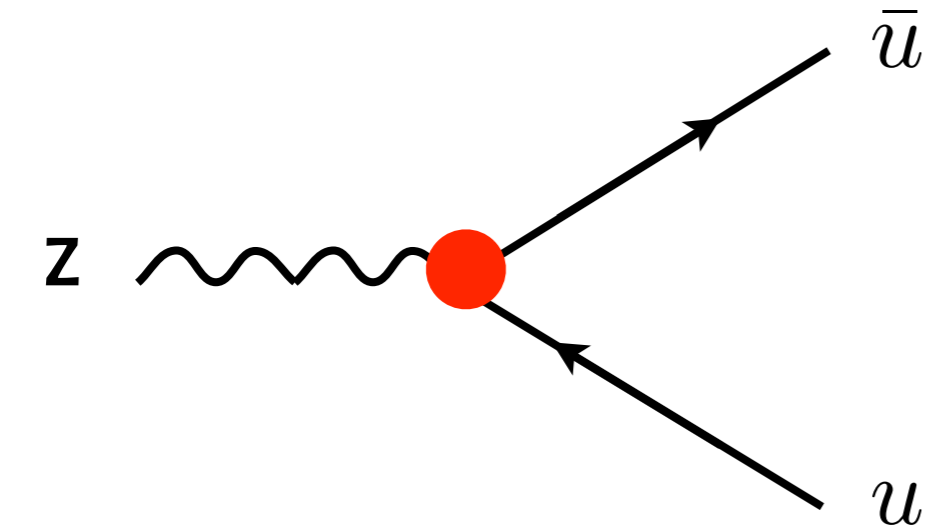
$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

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unpolarized quarks transv. polarized quarks

~~no sufficient knowledge~~


# Quark TMDs at the LHC



$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

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unpolarized quarks
~~transv. polarized quarks~~

  
 focus on the  
**flavor structure**  
 of the NP part

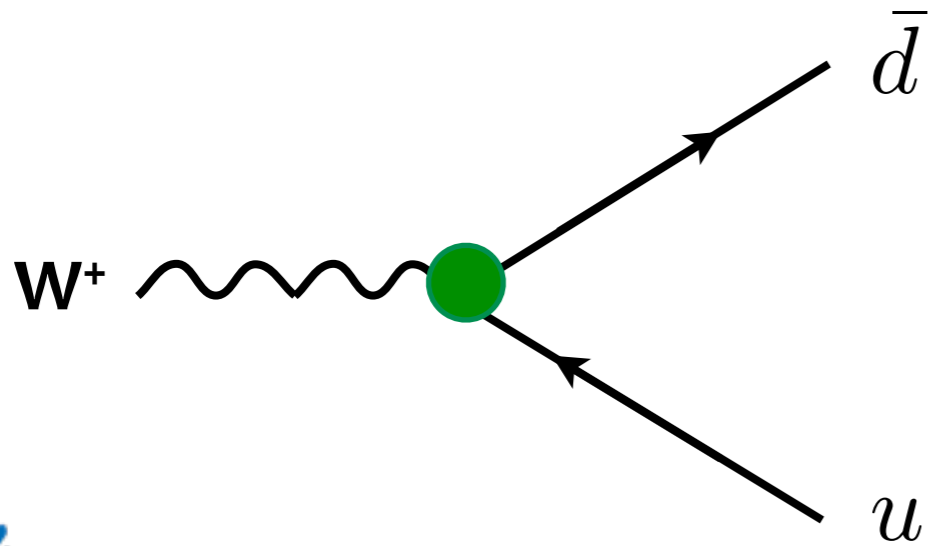
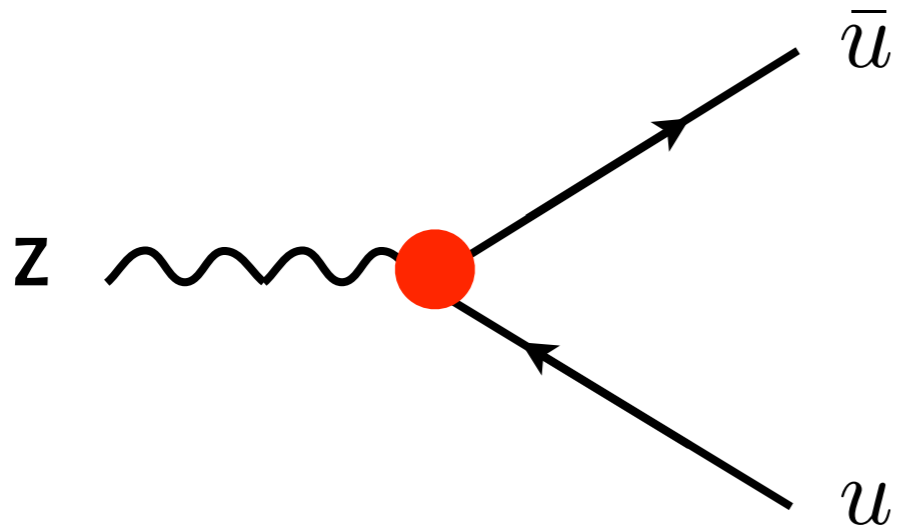
~~no sufficient knowledge~~

Intrinsic  $\langle k_T \rangle$  effects **have been measured on Z data**  
 and used to predict the W  $q_T$  spectrum,  
**assuming they are the same.**

This is not optimal, because  
 the intrinsic contributions are, in principle,  
**different in Z and  $W^\pm$  production**



# Quark TMDs at the LHC



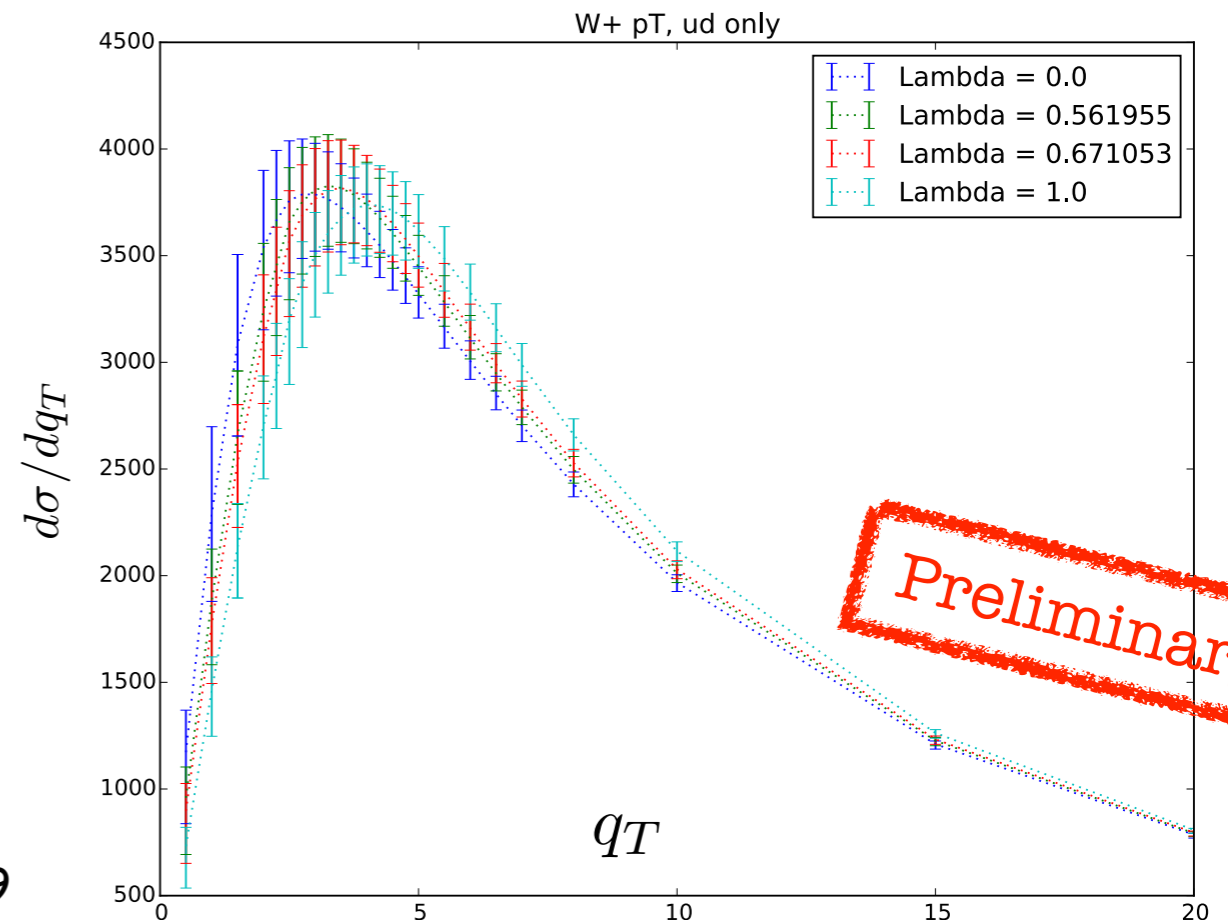
$$\frac{d\sigma}{dq_T} \sim \Phi_A^U \Phi_B^U |\mathcal{M}|^2$$

$$\sim \mathcal{C} \left[ \begin{array}{cc} f_1^{q/A} & f_1^{q/B} \end{array} \right] \pm \mathcal{C} \left[ \begin{array}{cc} h_1^{\perp q/A} & h_1^{\perp q/B} \end{array} \right]$$

unpolarized quarks
transv. polarized quarks

focus on the  
**flavor structure**  
 of the NP part

no sufficient knowledge



# W mass determination @ CDF

PhysRevD.89.072003

TABLE X: Uncertainties on  $M_W$  (in MeV) as resulting from charged-lepton transverse-momentum fits in the  $W \rightarrow \mu\nu$  and  $W \rightarrow e\nu$  samples. The last column reports the portion of the uncertainty that is common in the  $\mu\nu$  and  $e\nu$  results.

Source	$p_T^l$ fit uncertainties		
	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Common
Lepton energy scale	7	10	5
Lepton energy resolution	1	4	0
Lepton efficiency	1	2	0
Lepton tower removal	0	0	0
Recoil scale	6	6	6
Recoil resolution	5	5	5
Backgrounds	5	3	0
PDFs	9	9	9
<b><math>W</math> boson <math>p_T</math></b>	<b>9</b>	<b>9</b>	<b>9</b>
Photon radiation	4	4	4
Statistical	18	21	0
Total	25	28	16

TABLE XI: Uncertainties on  $M_W$  (in MeV) as resulting from neutrino-transverse-momentum fits in the  $W \rightarrow \mu\nu$  and  $W \rightarrow e\nu$  samples. The last column reports the portion of uncertainty that is common in the  $\mu\nu$  and  $e\nu$  results.

Source	$p_T^\nu$ fit uncertainties		
	$W \rightarrow \mu\nu$	$W \rightarrow e\nu$	Correlation
Lepton energy scale	7	10	5
Lepton energy resolution	1	7	0
Lepton efficiency	2	3	0
Lepton tower removal	4	6	4
Recoil scale	2	2	2
Recoil resolution	11	11	11
Backgrounds	6	4	0
PDFs	11	11	11
<b><math>W</math> boson <math>p_T</math></b>	<b>4</b>	<b>4</b>	<b>4</b>
Photon radiation	4	4	4
Statistical	22	25	0
Total	30	33	18

$$M_W = 80.387 \pm 0.019 \text{ GeV}$$

controlled **mainly**  
by soft gluons

# W mass determination @ D0

PhysRevD.89.012005

TABLE VI: Systematic uncertainties on  $M_W$  (in MeV). The section of this paper where each uncertainty is discussed is given in the Table.

Source	Section	$m_T$	$p_T^e$	$E_T$
Experimental				
Electron Energy Scale	VIC4	16	17	16
Electron Energy Resolution	VIC5	2	2	3
Electron Shower Model	VIC	4	6	7
Electron Energy Loss	VICD	4	4	4
Recoil Model	VICD3	5	6	14
Electron Efficiency	VICB10	1	3	5
Backgrounds	VICIII	2	2	2
$\Sigma(\text{Experimental})$		18	20	24
W Production and Decay Model				
PDF	VIC	11	11	14
QED	VICB	7	7	9
Boson $p_T$	VICIA	2	5	2
$\Sigma(\text{Model})$		13	14	17
Systematic Uncertainty (Experimental and Model)		22	24	29
W Boson Statistics	VICIX	13	14	15
Total Uncertain				33

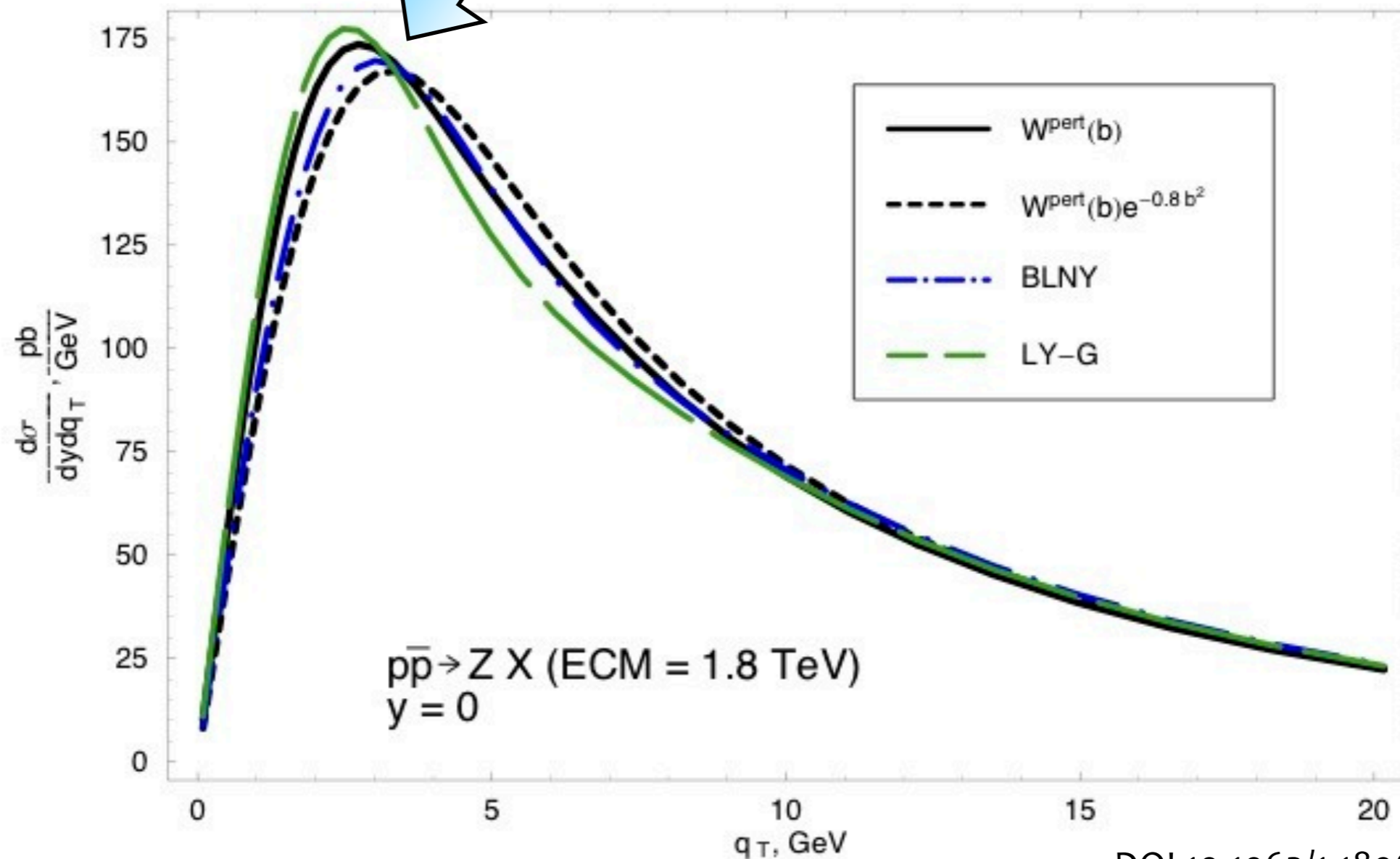
Are there *yet unexplored uncertainties* on the Z/W transverse spectrum?

# Nonperturbative effects

$$\frac{d\sigma^{Z/W^\pm}}{dq_T} \sim \text{FT} \sum_{i,j} \exp \left\{ -g_{ij} b_T^2 \right\}$$

$$g_{ij} \sim \langle k_T^2 \rangle_i + \langle k_T^2 \rangle_j + \text{soft gluons}$$

$g$  comes from 2 TMD PDFs  
and **controls the position of the peak**



DOI 10.1063/1.1896698

# Impact on the peak

We study flavor dependent configurations that *respect the experimental constraint on Z producing different distributions for W±*

$$g_{ij}(Z) : [\text{GeV}^2] \quad 0.7 = u + \bar{u} = 0.2 + 0.5 \\ = d + \bar{d} = 0.3 + 0.4 \\ = \dots = 0.6 + 0.1 = \dots$$

$$g_{ij}(W) : [\text{GeV}^2] \quad 0.6 = u + \bar{d} = 0.2 + 0.4 = \dots$$

**Preliminary**

shifts of peak position in GeV

$$\mu_R = \mu_c/2, 2\mu_c$$

pdf (90% cl)

$$\alpha_S = 0.121, 0.115$$

$$\Lambda_{NP} = 0.7, 0.5 \quad (\langle k_{\perp}^2 \rangle = 1.0, 1.96)$$

non-universal  $\langle k_{\perp}^2 \rangle$  (maximal  $W^+$  effect)

non-universal  $\langle k_{\perp}^2 \rangle$  (maximal  $W^-$  effect)

	$W^+$		$W^-$		$Z$	
	+0.30	-0.09	+0.29	-0.06	+0.23	-0.05
	<u>+0.03</u>	-0.05	<u>+0.06</u>	-0.02	+0.05	-0.02
	+0.14	-0.12	+0.14	-0.14	+0.15	-0.15
	+0.16	-0.16	+0.16	-0.14	+0.16	-0.15
	<u>+0.09</u>			-0.06	$\pm 0$	
		-0.03	<u>+0.05</u>		$\pm 0$	

MESSAGE:

the **uncertainty** on the peak position **is not negligible**



# (Un)polarized cross sections

TMDs known at NLO, NNLL

$$\frac{d\sigma_{UU}}{dq_T} \sim \left\{ \mathcal{C}[f_1^g f_1^g] - \mathcal{C}[h_1^{\perp g} h_1^{\perp g}] \right\}$$

unpolarized gluons

lin. polarized gluons

RHIC  
relativistic heavy ion collider



rich phenomenology

$$\frac{d\sigma_{UL}}{dq_T} = 0 \quad \text{by parity arguments}$$

$$\frac{d\sigma_{UT}}{dq_T} \sim \left\{ \mathcal{C}[f_1^g f_{1T}^{\perp g}] + \mathcal{C}[h_1^{\perp g} h_{1T}^g] + \mathcal{C}[h_1^{\perp g} h_{1T}^{\perp g}] \right\}$$

gluon **Sivers**

gluon **pretzelosity/1**

gluon **pretzelosity/2**

gluon Sivers, pretzelosity 1/2 : OPE still unknown

# Conclusions

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o) Phenomenology suggests a **flavor dependence** in the intrinsic transverse momentum of partons; this opens the way to **yet unexplored effects**

1) it might have a non-negligible **impact on Z/W $\pm$  production**

2) are there contributions from transversely polarized quarks ? (Boer-Mulders effect still not included)

3) **3D proton structure is of interest for high-energy physics:** nonperturbative effects should be extracted and their impact tested