

# Flavor physics with charm and bottom baryons

Stefan Meinel



Jefferson Lab Theory Seminar, September 11, 2017

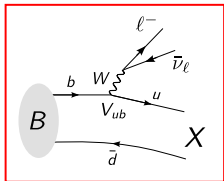
1  $b \rightarrow ul^{-}\bar{\nu}_e$  and  $b \rightarrow cl^{-}\bar{\nu}_e$

2  $b \rightarrow c\tau^{-}\bar{\nu}$

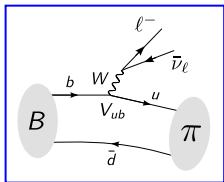
3  $b \rightarrow sl^{+}l^{-}$

4  $c \rightarrow sl^{-}\bar{\nu}_e$

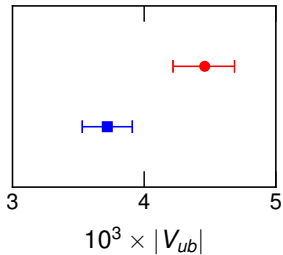
5  $c \rightarrow ul^{+}l^{-}$



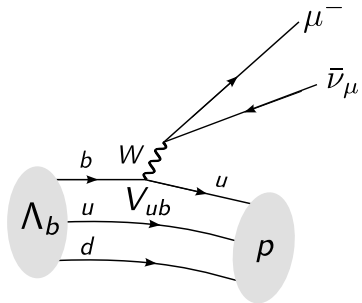
inclusive  $B \rightarrow X \ell \bar{\nu}_\ell$



exclusive  $B \rightarrow \pi \ell \bar{\nu}_\ell$



[Particle Data Group, 2016]



LHCb result:

[arXiv:1504.01568/Nature Physics 2015]

$$\frac{\int_{15 \text{ GeV}^2}^{q_{\text{max}}^2} \frac{d\Gamma(\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu)}{dq^2} dq^2}{\int_{7 \text{ GeV}^2}^{q_{\text{max}}^2} \frac{d\Gamma(\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu)}{dq^2} dq^2} = (1.00 \pm 0.04 \pm 0.08) \times 10^{-2}$$

$(q = p - p')$ .

To extract  $|V_{ub}/V_{cb}|$  from this, need

$$\begin{aligned} &\langle p | \bar{u} \gamma^\mu b | \Lambda_b \rangle, \quad \langle p | \bar{u} \gamma^\mu \gamma_5 b | \Lambda_b \rangle, \\ &\langle \Lambda_c | \bar{c} \gamma^\mu b | \Lambda_b \rangle, \quad \langle \Lambda_c | \bar{c} \gamma^\mu \gamma_5 b | \Lambda_b \rangle \end{aligned}$$

from lattice QCD.

$$\begin{aligned}
\langle p | \bar{u} \gamma^\mu b | \Lambda_b \rangle &= \bar{u}_p \left[ (m_{\Lambda_b} - m_p) \frac{q^\mu}{q^2} f_0(q^2) \right. \\
&\quad + \frac{m_{\Lambda_b} + m_p}{s_+} \left( p^\mu + p'^\mu - (m_{\Lambda_b}^2 - m_p^2) \frac{q^\mu}{q^2} \right) f_+(q^2) \\
&\quad \left. + \left( \gamma^\mu - \frac{2m_p}{s_+} p^\mu - \frac{2m_{\Lambda_b}}{s_+} p'^\mu \right) f_\perp(q^2) \right] u_{\Lambda_b},
\end{aligned}$$

$$\begin{aligned}
\langle p | \bar{u} \gamma^\mu \gamma_5 b | \Lambda_b \rangle &= -\bar{u}_p \gamma_5 \left[ (m_{\Lambda_b} + m_p) \frac{q^\mu}{q^2} g_0(q^2) \right. \\
&\quad + \frac{m_{\Lambda_b} - m_p}{s_-} \left( p^\mu + p'^\mu - (m_{\Lambda_b}^2 - m_p^2) \frac{q^\mu}{q^2} \right) g_+(q^2) \\
&\quad \left. + \left( \gamma^\mu + \frac{2m_p}{s_-} p^\mu - \frac{2m_{\Lambda_b}}{s_-} p'^\mu \right) g_\perp(q^2) \right] u_{\Lambda_b},
\end{aligned}$$

where  $s_\pm = (m_{\Lambda_b} \pm m_p)^2 - q^2$

# $\Lambda_b \rightarrow p \ell^- \bar{\nu}_\ell$ and $\Lambda_b \rightarrow \Lambda_c \ell^- \bar{\nu}_\ell$ form factors from lattice QCD with relativistic heavy quarks

[W. Detmold, C. Lehner, S. Meinel, arXiv:1503.01421/PRD 2015]

- Gauge field configurations generated by the RBC and UKQCD collaborations

[Y. Aoki *et al.*, arXiv:1011.0892/PRD 2011]

- $u$ ,  $d$ ,  $s$  quarks: domain-wall action

[D. Kaplan, hep-lat/9206013/PLB 1992; V. Furman and Y. Shamir, hep-lat/9303005/NPB 1995]

- $c$ ,  $b$  quarks: “relativistic heavy-quark action”

[A. El-Khadra, A. Kronfeld, P. Mackenzie, hep-lat/9604004/PRD 1997; Y. Aoki *et al.*, arXiv:1206.2554/PRD 2012]

- “Mostly nonperturbative” renormalization

[A. El-Khadra *et al.*, hep-ph/0101023/PRD 2001]

- $a \approx 0.11$  fm,  $0.085$  fm

- $230$  MeV  $\leq m_\pi \leq 350$  MeV

- Three-point functions with 12 source-sink separations

Orange square:  $a = 0.112$  fm,  $m_\pi = 336$  MeV

Purple asterisk:  $a = 0.085$  fm,  $m_\pi = 352$  MeV

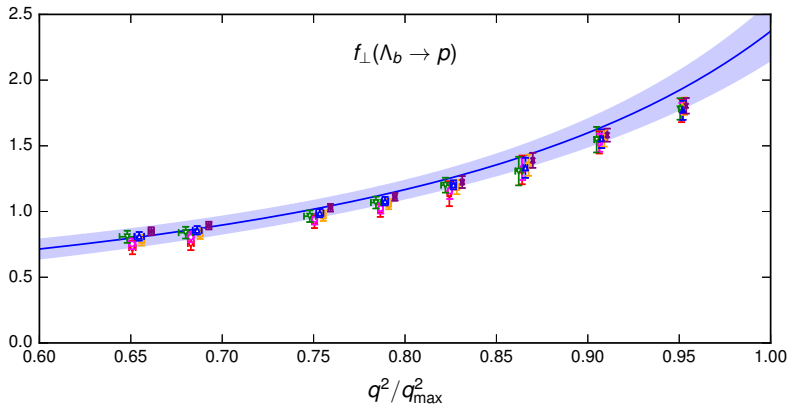
Blue shaded band:  $a = 0$ ,  $m_\pi = 135$  MeV

Pink square:  $a = 0.112$  fm,  $m_\pi = 270$  MeV

Blue asterisk:  $a = 0.085$  fm,  $m_\pi = 295$  MeV

Red square:  $a = 0.112$  fm,  $m_\pi = 245$  MeV

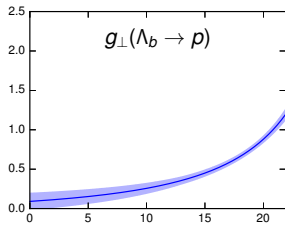
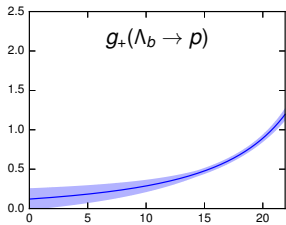
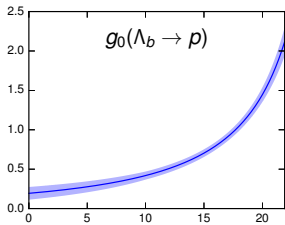
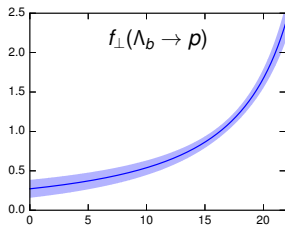
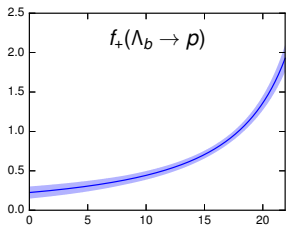
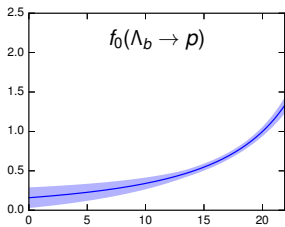
Green asterisk:  $a = 0.085$  fm,  $m_\pi = 227$  MeV



Combined chiral/continuum/kinematic extrapolation using modified z-expansion

[C. Bourrely, I. Caprini, L. Lellouch, arXiv:0807.2722/PRD 2009]

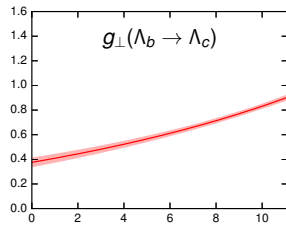
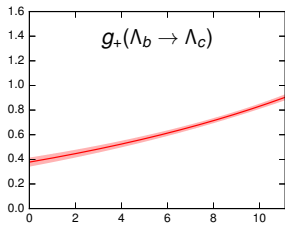
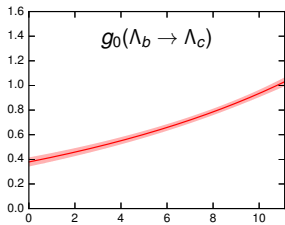
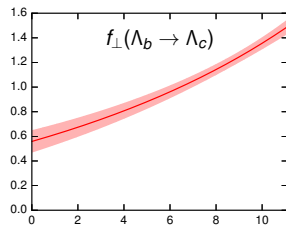
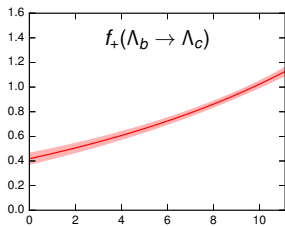
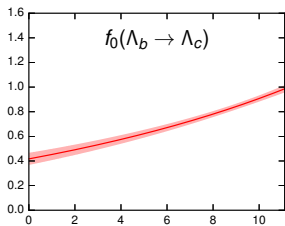




$q^2$  (GeV<sup>2</sup>)

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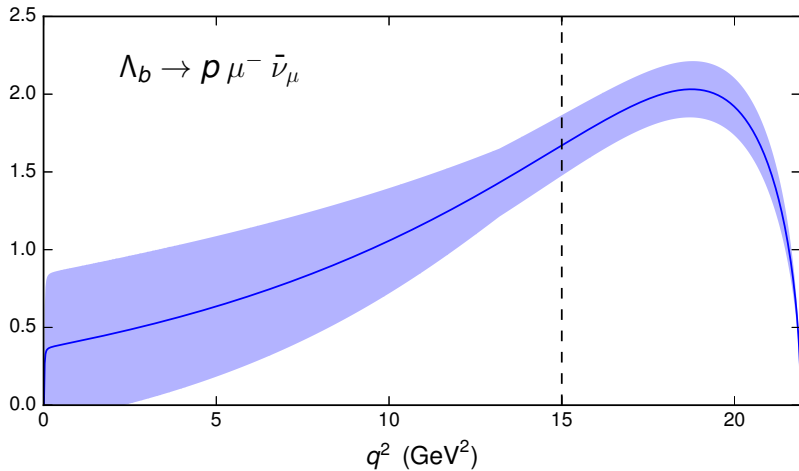


$q^2$  (GeV<sup>2</sup>)

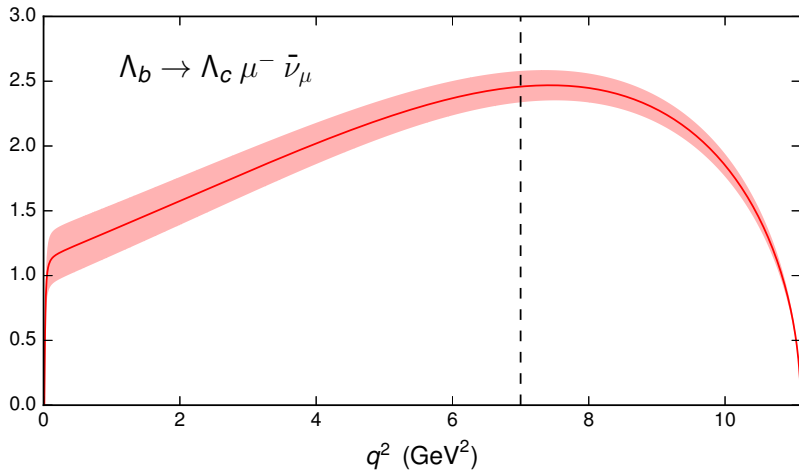
$q^2$  (GeV<sup>2</sup>)

$q^2$  (GeV<sup>2</sup>)

$$\frac{d\Gamma/dq^2}{|V_{ub}|^2} \text{ (ps}^{-1} \text{ GeV}^{-2}\text{)}$$



$$\frac{d\Gamma/dq^2}{|V_{cb}|^2} \text{ (ps}^{-1} \text{ GeV}^{-2}\text{)}$$



$$\frac{|V_{cb}|^2 \int_{15 \text{ GeV}^2}^{q_{\text{max}}^2} \frac{d\Gamma(\Lambda_b \rightarrow p \mu^- \bar{\nu}_\mu)}{dq^2} dq^2}{|V_{ub}|^2 \int_{7 \text{ GeV}^2}^{q_{\text{max}}^2} \frac{d\Gamma(\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu)}{dq^2} dq^2}$$

$= 1.471 \pm 0.095_{\text{stat.}} \pm 0.109_{\text{syst.}}$

Systematic uncertainties in the ratio of decay rates:

Finite volume	4.9 %
Continuum extrapolation	2.8 %
Chiral extrapolation	2.6 %
RHQ parameters	2.3 %
Matching & improvement	2.1 %
Isospin breaking/QED	2.0 %
Scale setting	1.8 %
z expansion	1.3 %
<b>Combined</b>	<b>7.3 %</b>

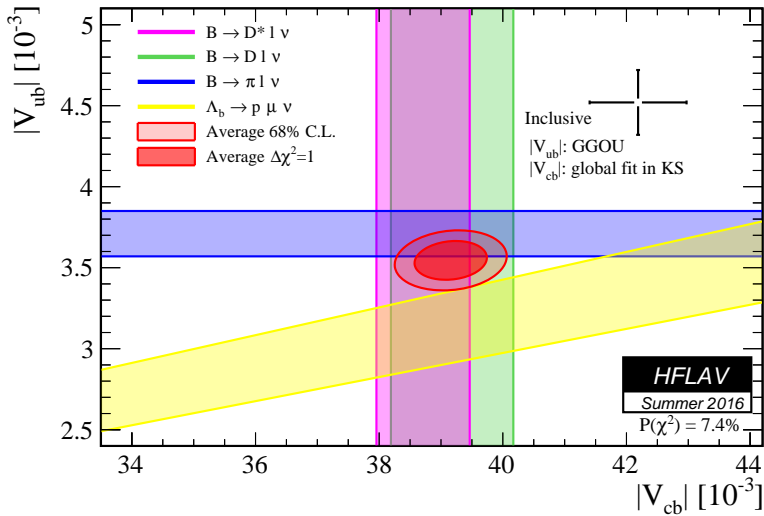
Note: the combined uncertainty takes into account the correlations between the individual uncertainties

Combine with LHCb measurement:

$$\frac{|V_{ub}|}{|V_{cb}|} = 0.083 \pm 0.004_{\text{expt}} \pm 0.004_{\text{lat}}$$

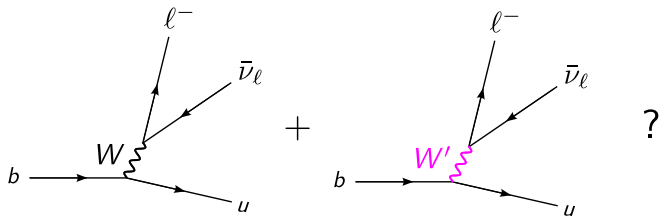
[LHCb Collaboration, arXiv:1504.01568/Nature Physics 2015]

$|V_{ub}|, |V_{cb}|$  status





Right-handed  $b \rightarrow u$  currents beyond the Standard Model?



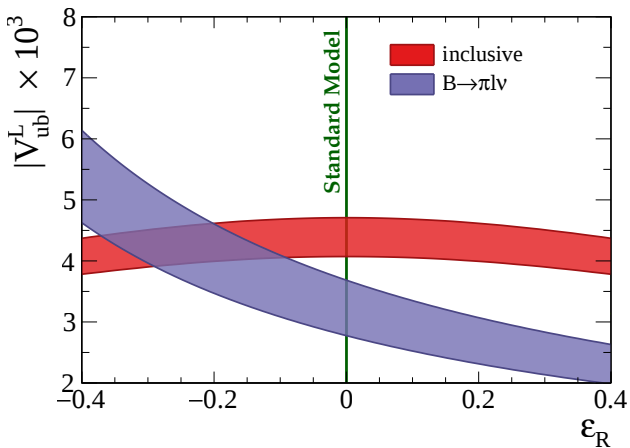
This could replace

$$V_{ub} \underbrace{\bar{u}_L \gamma^\mu b_L}_{V-A}$$

by

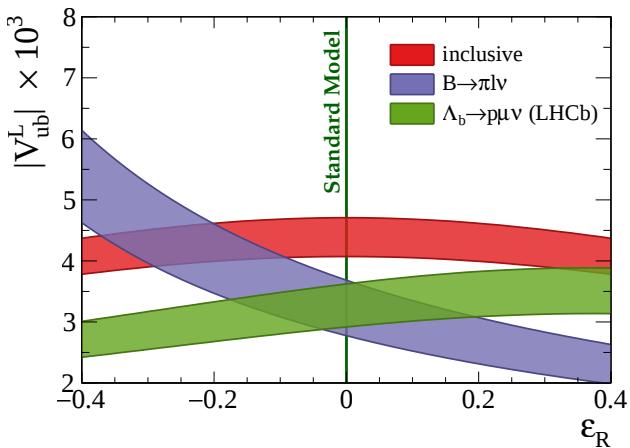
$$V_{ub}^L \left( \underbrace{\bar{u}_L \gamma^\mu b_L}_{V-A} + \epsilon_R \underbrace{\bar{u}_R \gamma^\mu b_R}_{V+A} \right)$$

Process	Vector current	Axial vector current
$B \rightarrow \pi l \bar{\nu}_l$	✓	✗
$B \rightarrow X_u l \bar{\nu}_l$	✓	✓
$\Lambda_b \rightarrow p l \bar{\nu}_l$	✓	✓



(using 2014 PDG values)

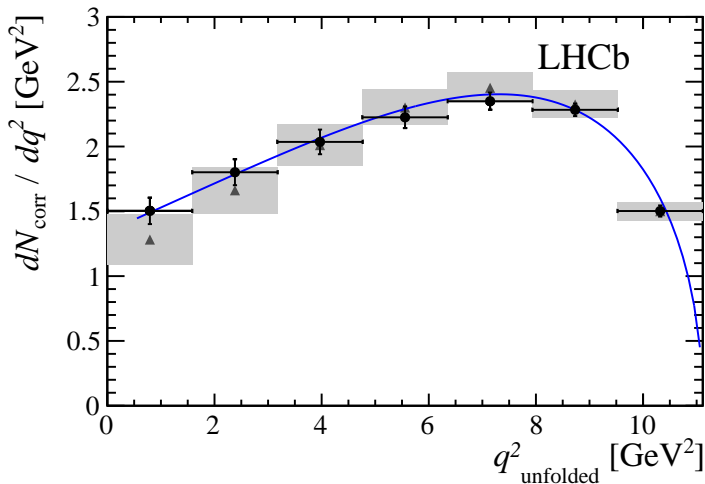
[LHCb Collaboration, arXiv:1504.01568/Nature Physics 2015]



(using 2014 PDG values;  $\Lambda_b \rightarrow p \mu \bar{\nu}$  result normalized using  $|V_{cb}|_{\text{excl.}}$ )

[LHCb Collaboration, arXiv:1504.01568/Nature Physics 2015]

# Measurement of the shape of the $\Lambda_b \rightarrow \Lambda_c \mu \bar{\nu}$ differential decay rate



1  $b \rightarrow ul^- \bar{\nu}_e$  and  $b \rightarrow cl^- \bar{\nu}_e$

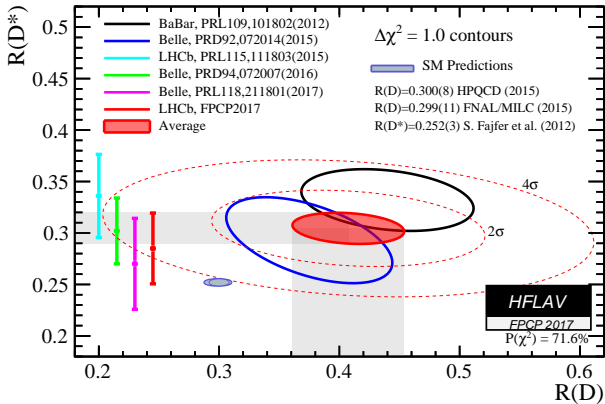
2  $b \rightarrow c\tau^- \bar{\nu}$

3  $b \rightarrow sl^+ l^-$

4  $c \rightarrow sl^- \bar{\nu}_e$

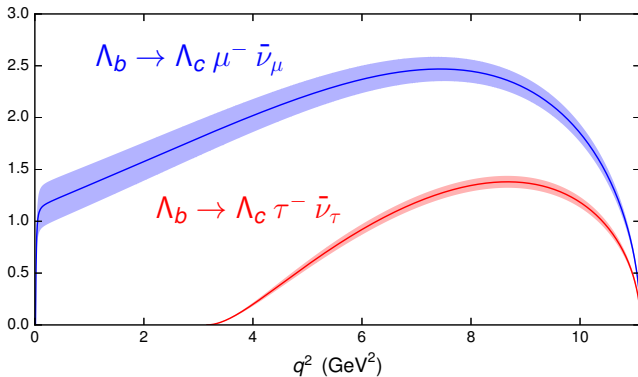
5  $c \rightarrow ul^+ l^-$







$$\frac{d\Gamma/dq^2}{|V_{cb}|^2} \quad (\text{ps}^{-1} \text{ GeV}^{-2})$$



Standard-model prediction:

$$R[\Lambda_c]^{\text{SM}} = \frac{\Gamma(\Lambda_b \rightarrow \Lambda_c \tau^- \bar{\nu}_\tau)}{\Gamma(\Lambda_b \rightarrow \Lambda_c \mu^- \bar{\nu}_\mu)} = 0.3328 \pm 0.0074 \pm 0.0070$$

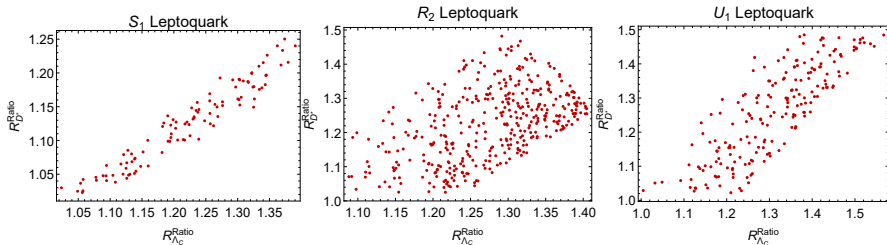
LHCb analysis is underway!

# BSM phenomenology of $\Lambda_b \rightarrow \Lambda_c \tau \bar{\nu}$

[A. Datta, S. Kamali, S. Meinel, A. Rashed, arXiv:1702.02243/JHEP 2017]

Example: Leptoquark models

	spin	$SU(3)_c$	$SU(2)_L$	$U(1)_{Y=Q-T_3}$
$S_1$	0	$\bar{3}$	1	1/3
$R_2$	0	3	2	7/6
$U_1$	1	3	1	2/3



$$R_{D^*}^{\text{Ratio}} = \frac{R[D^*]^{\text{SM+NP}}}{R[D^*]^{\text{SM}}}, \quad R_{\Lambda_c}^{\text{Ratio}} = \frac{R[\Lambda_c]^{\text{SM+NP}}}{R[\Lambda_c]^{\text{SM}}}$$

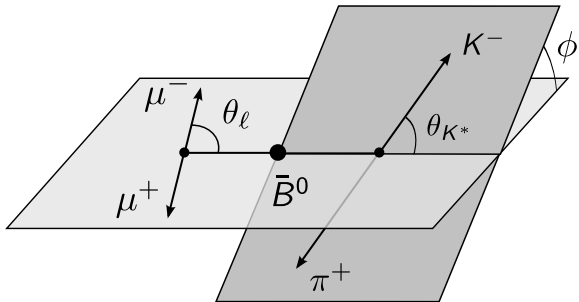
1  $b \rightarrow ul^{-}\bar{\nu}_e$  and  $b \rightarrow cl^{-}\bar{\nu}_e$

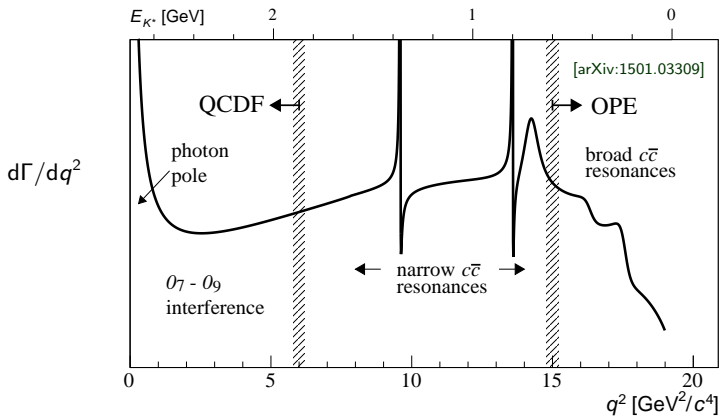
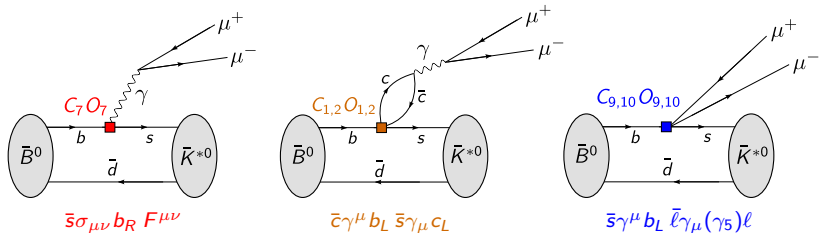
2  $b \rightarrow c\tau^{-}\bar{\nu}$

3  $b \rightarrow sl^{+}l^{-}$

4  $c \rightarrow sl^{-}\bar{\nu}_e$

5  $c \rightarrow ul^{+}l^{-}$

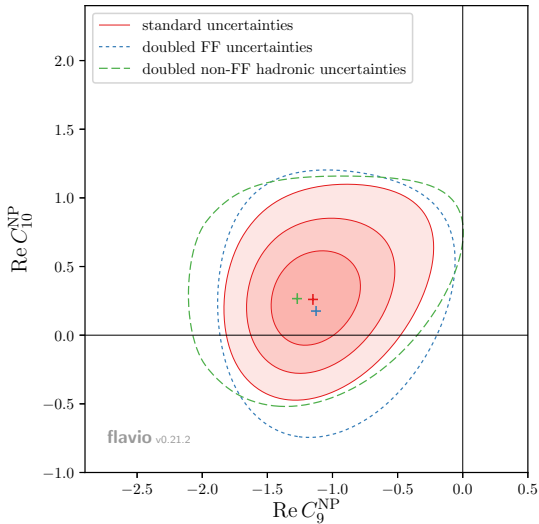




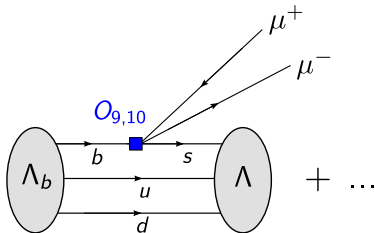
Fit of  $C_i^{\text{NP}} = C_i - C_i^{\text{SM}}$

to experimental data for mesonic  $b \rightarrow s\mu^+\mu^-$  decays

[W. Altmannshofer, C. Niehoff, P. Stangl, D. Straub, arXiv:1703.09189/EPJC 2017]



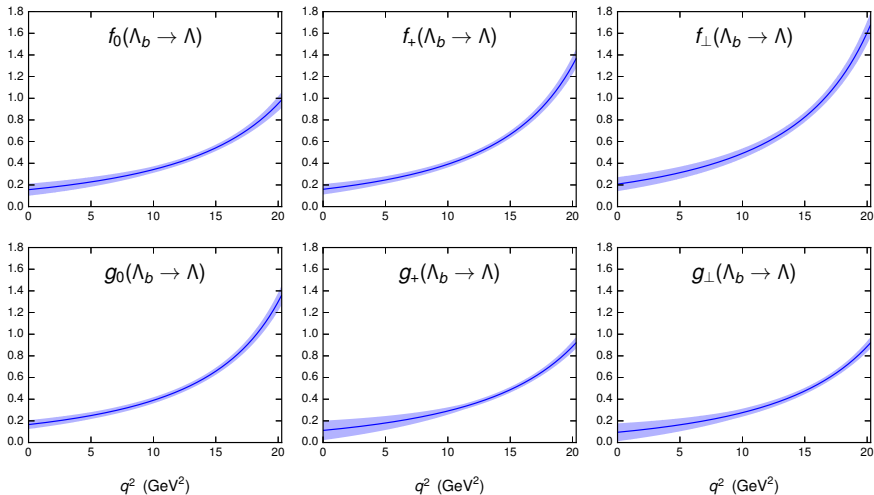
Complementary information can be obtained from  $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$



Combines the best aspects of  $B \rightarrow K^* \mu^+ \mu^-$  and  $B \rightarrow K \mu^+ \mu^-$ :

$\Lambda$  has nonzero spin and is stable under strong interactions.

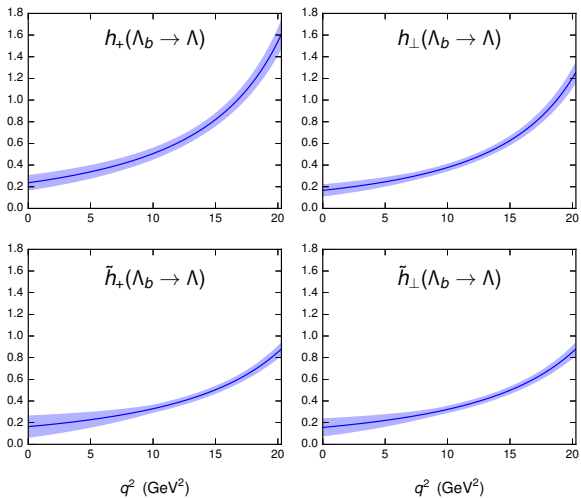
## $\Lambda_b \rightarrow \Lambda$ vector and axial vector form factors



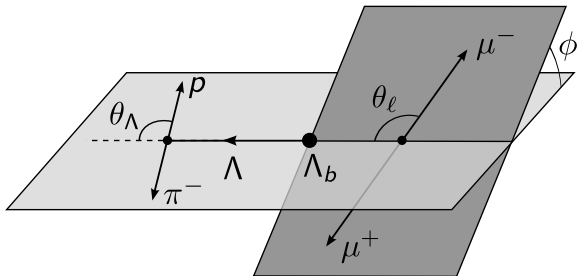
[W. Detmold and S. Meinel, arXiv:1602.01399/PRD 2016]



## $\Lambda_b \rightarrow \Lambda$ tensor form factors



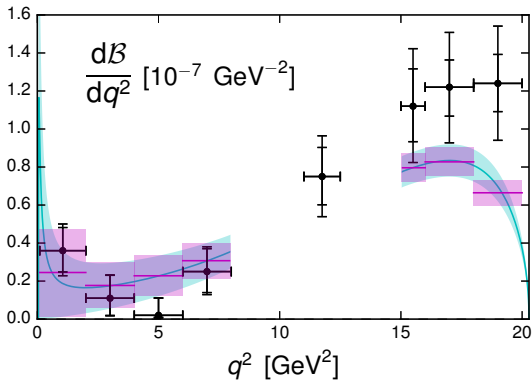
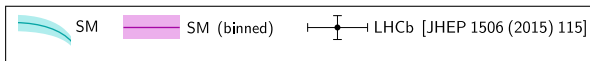
[W. Detmold and S. Meinel, arXiv:1602.01399/PRD 2016]



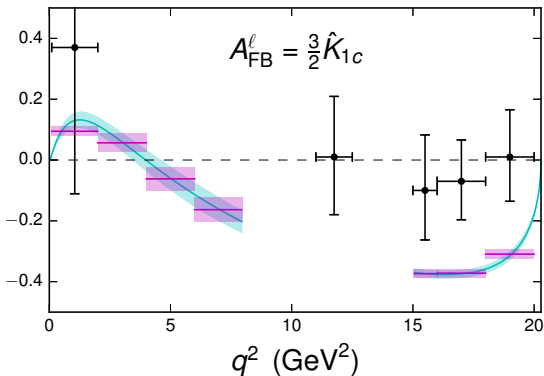
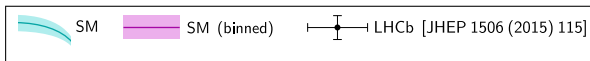
For unpolarized  $\Lambda_b$ :

$$\begin{aligned} \frac{d^4\Gamma}{dq^2 d\cos\theta_\ell d\cos\theta_\Lambda d\phi} &= \frac{3}{8\pi} \left[ (K_{1ss} \sin^2\theta_\ell + K_{1cc} \cos^2\theta_\ell + K_{1c} \cos\theta_\ell) \right. \\ &\quad + (K_{2ss} \sin^2\theta_\ell + K_{2cc} \cos^2\theta_\ell + K_{2c} \cos\theta_\ell) \cos\theta_\Lambda \\ &\quad + (K_{3sc} \sin\theta_\ell \cos\theta_\ell + K_{3s} \sin\theta_\ell) \sin\theta_\Lambda \sin\phi \\ &\quad \left. + (K_{4sc} \sin\theta_\ell \cos\theta_\ell + K_{4s} \sin\theta_\ell) \sin\theta_\Lambda \cos\phi \right] \end{aligned}$$

$$\Rightarrow \frac{d\Gamma}{dq^2} = 2K_{1ss} + K_{1cc}$$



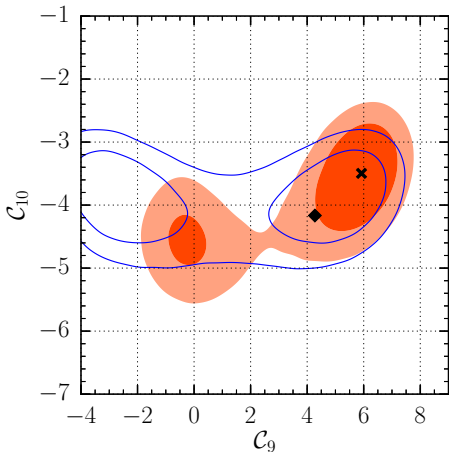
Hint of an excess at high  $q^2$  – contrary to mesonic  $b \rightarrow s\mu^+\mu^-$  decays.



3 $\sigma$  discrepancy at high  $q^2$ .

Using  $\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$  data within a Bayesian analysis of  $|\Delta B| = |\Delta S| = 1$  decays

Constraint	Scenario		
	SM( $\nu$ -only)	(9, 10)	(9, 9', 10, 10')
$\Lambda_b \rightarrow \Lambda \mu^+ \mu^-$	Pull value [ $\sigma$ ]		
$\langle \mathcal{B} \rangle_{15,20}$	+0.86	-0.17	-0.08
$\langle F_L \rangle_{15,20}$	+1.41	+1.41	+1.41
$\langle A_{\text{FB}}^\ell \rangle_{15,20}$	+3.13	+2.60	+0.72
$\langle A_{\text{FB}}^\Lambda \rangle_{15,20}$	-0.26	-0.24	-1.08
$\bar{B}_s \rightarrow \mu^+ \mu^-$	Pull value [ $\sigma$ ]		
$\int \mathcal{B}(\tau) d\tau$	-0.72	+0.75	+0.37
$\bar{B} \rightarrow X_s \ell^+ \ell^-$	Pull value [ $\sigma$ ]		
$\langle \mathcal{B} \rangle_{1,6}$ (BaBar)	+0.47	-0.26	-0.10
$\langle \mathcal{B} \rangle_{1,6}$ (Belle)	+0.17	-0.35	-0.24
	$\chi^2$ at best-fit point		
	13.40	9.60	3.87



[S. Meinel and D. van Dyk, arXiv:1603.02974/PRD 2016]

Opposite shift in  $C_9$  compared to fits of only mesonic decays!

- Statistical fluctuation?
- Breakdown of OPE for charm-loop effects?

# Overview of exclusive $b \rightarrow sl^+l^-$ decays

	Probes all Dirac structures	Final hadron QCD-stable	Charged hadrons from $b$ -decay vertex	LQCD Refs.
$B^+ \rightarrow K^+l^+l^-$	✗	✓	✓	[1, 2, 3, 4]
$B^0 \rightarrow K^{*0}(\rightarrow K^+\pi^-)l^+l^-$	✓	✗	✓	[5, 6, 7]
$B_s \rightarrow \phi(\rightarrow K^+K^-)l^+l^-$	✓	✗	✓	[5, 6, 7]
$\Lambda_b^0 \rightarrow \Lambda^0(\rightarrow p^+\pi^-)l^+l^-$	✓	✓	✗	[8, 9, 10]
$\Lambda_b^0 \rightarrow \Lambda^{*0}(\rightarrow p^+K^-)l^+l^-$	✓	✗	✓	[11]

[1] C. Bouchard *et al.*, arXiv:1306.2384/PRD 2013

[2] C. Bouchard *et al.*, arXiv:1306.0434/PRL 2013

[3] J. A. Bailey *et al.*, arXiv:1509.06235/PRD 2016

[4] D. Du *et al.*, arXiv:1510.02349/PRD 2016

[5] R. R. Horgan, Z. Liu, S. Meinel, M. Wingate, arXiv:1310.3722/PRD 2014

[6] R. R. Horgan, Z. Liu, S. Meinel, M. Wingate, arXiv:1310.3887/PRL 2014

[7] J. Flynn, A. Jüttner, T. Kawanai, E. Lizarazo, O. Witzel, arXiv:1511.06622/PoS 2015

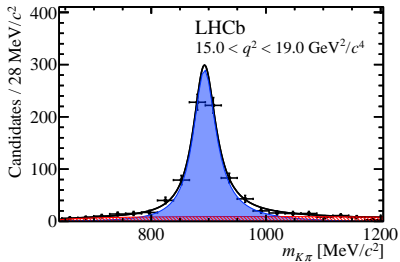
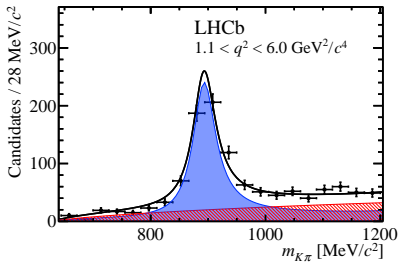
[8] W. Detmold, C.-J. D. Lin, S. Meinel, M. Wingate, arXiv:1212.4827/PRD 2013

[9] W. Detmold, S. Meinel, arXiv:1602.01399/PRD 2016

[10] S. Meinel, D. van Dyk, arXiv:1603.02974/PRD 2016

[11] S. Meinel, G. Rendon, arXiv:1608.08110/PoS 2016

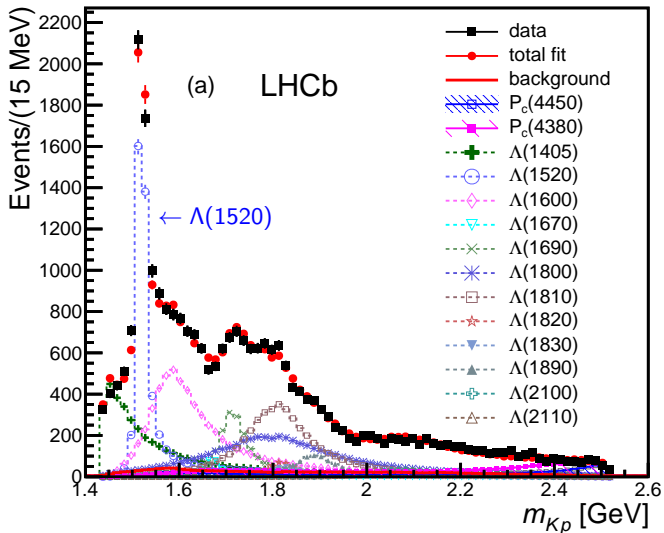
The  $K^*(892)$  resonance in  $B^0 \rightarrow K^+ \pi^- \mu^+ \mu^-$



[LHCb Collaboration, arXiv:1606.04731/JHEP 2016]



$\Lambda^*$  resonances in  $\Lambda_b \rightarrow K^- p^+ \mu^+ \mu^-$  at  $q^2 = m_{J/\psi}^2$



$\Lambda(1520) \ 3/2^-$  $I(J^P) = 0(\frac{3}{2}^-)$  Status: \*\*\*\*

### $\Lambda(1520)$ MASS

<u>VALUE (MeV)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>1519.5 ±1.0</b>	<b>OUR ESTIMATE</b>			

### $\Lambda(1520)$ WIDTH

<u>VALUE (MeV)</u>	<u>EVTS</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>15.6 ±1.0</b>	<b>OUR ESTIMATE</b>			

### $\Lambda(1520)$ DECAY MODES

Mode	Fraction ( $\Gamma_i/\Gamma$ )
$\Gamma_1 \ N\bar{K}$	(45 ±1 ) %
$\Gamma_2 \ \Sigma\pi$	(42 ±1 ) %
$\Gamma_3 \ \Lambda\pi\pi$	(10 ±1 ) %
$\Gamma_4 \ \Sigma(1385)\pi$	
$\Gamma_5 \ \Sigma(1385)\pi(\rightarrow \Lambda\pi\pi)$	
$\Gamma_6 \ \Lambda(\pi\pi)_S\text{-wave}$	
$\Gamma_7 \ \Sigma\pi\pi$	( 0.9 ±0.1 ) %
$\Gamma_8 \ \Lambda\gamma$	( 0.85±0.15) %
$\Gamma_9 \ \Sigma^0\gamma$	

Naive treatment as if it were a stable particle in the following.

## Helicity form factors for $\Lambda_b \rightarrow \Lambda(1520)$

Vector current:

$$\langle \Lambda^*(p', s') | \bar{s} \gamma^\mu b | \Lambda_b(p, s) \rangle$$

$$\begin{aligned}
 &= \bar{u}_\lambda(p', s') \left[ f_0 \frac{(m_{\Lambda_b} - m_{\Lambda^*}) p^\lambda q^\mu}{m_{\Lambda_b} q^2} \right. \\
 &\quad + f_+ \frac{(m_{\Lambda_b} + m_{\Lambda^*}) p^\lambda (q^2 (p^\mu + p'^\mu) - (m_{\Lambda_b}^2 - m_{\Lambda^*}^2) q^\mu)}{m_{\Lambda_b} q^2 s_+} \\
 &\quad + f_\perp \left( \frac{p^\lambda \gamma^\mu}{m_{\Lambda_b}} - \frac{2 p^\lambda (m_{\Lambda_b} p'^\mu + m_{\Lambda^*} p^\mu)}{m_{\Lambda_b} s_+} \right) \\
 &\quad \left. + f_{\perp'} \left( \frac{p^\lambda \gamma^\mu}{m_{\Lambda_b}} - \frac{2 p^\lambda p'^\mu}{m_{\Lambda_b} m_{\Lambda^*}} + \frac{2 p^\lambda (m_{\Lambda_b} p'^\mu + m_{\Lambda^*} p^\mu)}{m_{\Lambda_b} s_+} + \frac{s_- g^{\lambda\mu}}{m_{\Lambda_b} m_{\Lambda^*}} \right) \right] u(p, s)
 \end{aligned}$$

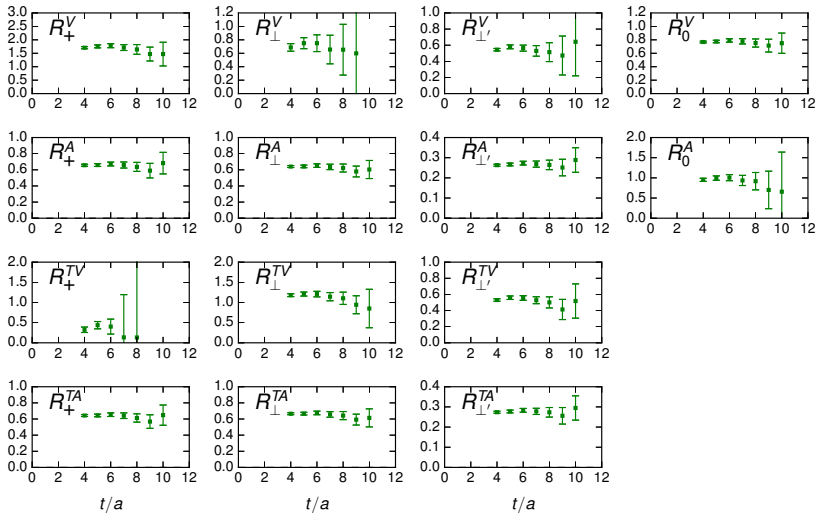
$$\text{where } s_\pm = (m_{\Lambda_b} \pm m_{\Lambda^*})^2 - q^2$$

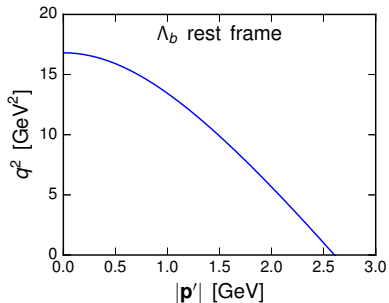
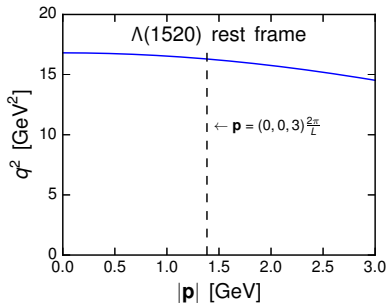
Similar for axial-vector current ( $g_0, g_+, g_\perp, g_{\perp}'$ )

and tensor current ( $h_+, h_\perp, h_{\perp}', \tilde{h}_+, \tilde{h}_\perp, \tilde{h}_{\perp}'$ )

Lattice calculation in  $\Lambda(1520)$  rest frame.

Preliminary results at  $\mathbf{p}_{\Lambda_b} = (0, 0, 3) \frac{2\pi}{L}$  ( $\approx 1.4$  GeV):





Plan to use moving-NRQCD action for  $b$  quark to reach higher  $\mathbf{p}_{\Lambda_b}$ .

[R. R. Horgan *et al.*, arXiv:0906.0945/PRD 2009]

1  $b \rightarrow ul^{-}\bar{\nu}_e$  and  $b \rightarrow cl^{-}\bar{\nu}_e$

2  $b \rightarrow c\tau^{-}\bar{\nu}$

3  $b \rightarrow sl^{+}l^{-}$

4  $c \rightarrow sl^{-}\bar{\nu}_e$

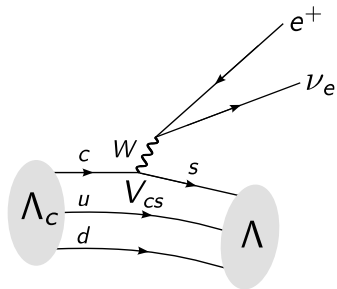
5  $c \rightarrow ul^{+}l^{-}$

BES III Collaboration, 2015:

First direct measurements of  $\Lambda_c$  branching fractions at  $e^+e^- \rightarrow \Lambda_c\bar{\Lambda}_c$  threshold.  
Including

$$\mathcal{B}(\Lambda_c \rightarrow \Lambda e^+ \nu_e) = (3.63 \pm 0.38 \pm 0.20)\%$$

[arXiv:1510.02610/PRL 2015]



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Including

$$\mathcal{B}(\Lambda_c \rightarrow \Lambda e^+ \nu_e) = (3.63 \pm 0.38 \pm 0.20) \% \quad [\text{arXiv:1510.02610/PRL 2015}]$$

From the introduction of their paper:

Since the first observation of the  $\Lambda_c^+$  baryon in  $e^+e^-$  annihilations at the Mark II experiment [4] in 1979, much theoretical effort has been applied towards the study of its SL decay properties. However, predictions of the branching fraction (BF)  $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)$  in different theoretical models vary in a wide range from 1.4% to 9.2% [5–15], depending on the choice of various  $\Lambda_c^+$  wave function models and the nature of decay dynamics. In addition, theoretical calculations prove to be quite challenging for lattice quantum chromodynamics (LQCD) due to the complexity of form factors, which describes the hadronic part of the decay dynamics in  $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$  [16]. Thus, an accurate measurement of  $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)$  is a key ingredient in calibrating LQCD calculations, which, in turn, will play an important role in understanding different  $\Lambda_c^+$  SL decays.



# $\Lambda_c \rightarrow \Lambda \ell^+ \nu_\ell$ form factors and decay rates from lattice QCD with physical quark masses

[S. Meinel, PRL **118**, 082001 (2017)]

- RBC/UKQCD ensembles with 2 + 1 flavors of domain-wall fermions  
[Y. Aoki *et al.*, arXiv:1011.0892/PRD2011; T. Blum *et al.*, arXiv:1411.7017/PRD2016]
- Charm action: anisotropic clover  
[Z. Brown, W. Detmold, S. Meinel, K. Orginos, arXiv:1409.0497/PRD2014]
- $c \rightarrow s$  currents: “Mostly nonperturbative” renormalization  
[A. El-Khadra *et al.*, hep-ph/0101023/PRD2001],  
one-loop coefficients computed by Christoph Lehner  
[C. Lehner, arXiv:1211.4013/PoS2012]
- Three-point functions with 12 source-sink separations

$N_s^3 \times N_t$	$a$ [fm]	$am_{u,d}$	$m_\pi$ [MeV]	$am_s^{(\text{val})}$	$m_{\eta_s}^{(\text{val})}$ [MeV]
$48^3 \times 96$	0.1142(15)	0.00078	139(2)	0.0362	693(9)
$24^3 \times 64$	0.1119(17)	0.005	336(5)	0.04	761(12)
$24^3 \times 64$	0.1119(17)	0.005	336(5)	0.03	665(10)
$32^3 \times 64$	0.0849(12)	0.004	295(4)	0.03	747(10)
$32^3 \times 64$	0.0848(17)	0.006	352(7)	0.03	749(14)

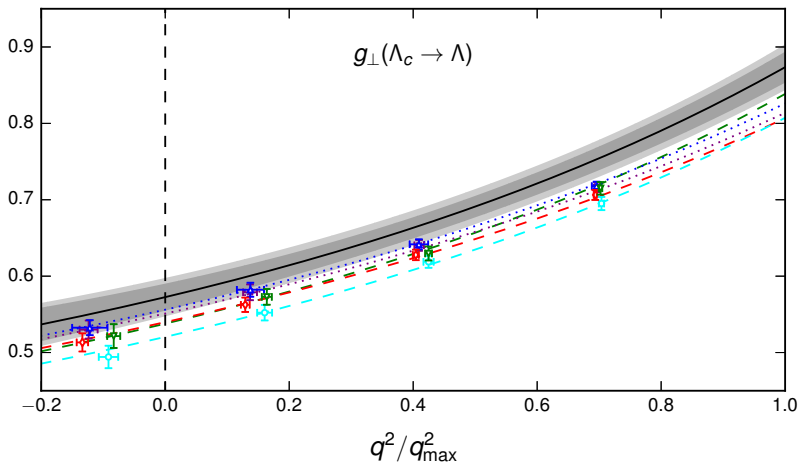
## Combined chiral/continuum/kinematic extrapolation using modified z-expansion

[C. Bourrely, I. Caprini, L. Lellouch, arXiv:0807.2722/PRD 2009]

$$z(q^2) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}, \quad t_+ = (m_D + m_K)^2, \quad t_0 = (m_{\Lambda_c} - m_\Lambda)^2$$

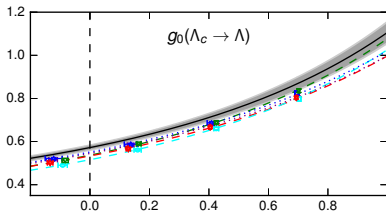
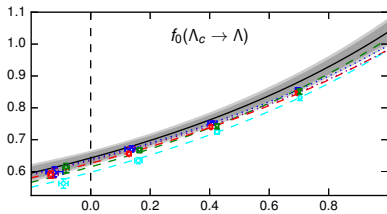
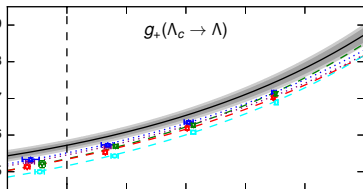
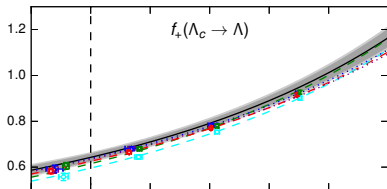
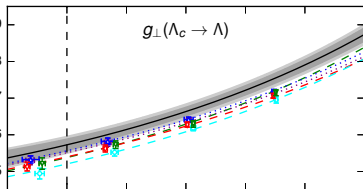
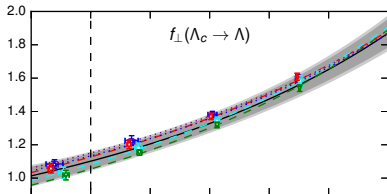
Nominal fit:

$$f(q^2) = \frac{1}{1 - q^2/(m_{\text{pole}}^f)^2} \left[ a_0^f \left( 1 + c_0^f \frac{m_\pi^2 - m_{\pi,\text{phys}}^2}{\Lambda_\chi^2} + c_{s,0}^f \frac{m_{\eta_s}^2 - m_{\eta_s,\text{phys}}^2}{\Lambda_\chi^2} \right) + a_1^f z(q^2) + a_2^f [z(q^2)]^2 \right] \times \left[ 1 + b^f a^2 |\mathbf{p}'|^2 + d^f a^2 \Lambda_{\text{QCD}}^2 \right]$$



Inner band: statistical uncertainty from nominal fit only

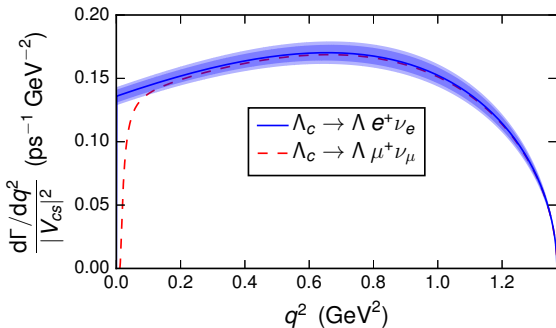
Outer band: includes systematic uncertainty estimated using higher-order fit



$q^2/q_{\max}^2$

$q^2/q_{\max}^2$

Predicted differential and total decay rates without  $|V_{cs}|^2$ :



$$\frac{\Gamma(\Lambda_c \rightarrow \Lambda \ell^+ \nu_\ell)}{|V_{cs}|^2} = \begin{cases} 0.2007(71)(74) \text{ ps}^{-1}, & \ell = e, \\ 0.1945(69)(72) \text{ ps}^{-1}, & \ell = \mu. \end{cases}$$

Taking the indirectly determined  $|V_{cs}| = 0.97344(15)$  from UTFit and  $\tau_{\Lambda_c} = 0.200(6)$  ps from PDG, the branching fractions predicted by lattice QCD are

$$\mathcal{B}(\Lambda_c \rightarrow \Lambda \ell^+ \nu_\ell) = \begin{cases} 0.0380(19)_{\text{LQCD}(11)\tau_{\Lambda_c}}, & \ell = e, \\ 0.0369(19)_{\text{LQCD}(11)\tau_{\Lambda_c}}, & \ell = \mu. \end{cases}$$

These agree with the BESIII measurements

[arXiv:1510.02610/PRL 2015; arXiv:1611.04382/PLB 2017]

$$\mathcal{B}(\Lambda_c \rightarrow \Lambda \ell^+ \nu_\ell)_{\text{BESIII}} = \begin{cases} 0.0363(43), & \ell = e, \\ 0.0349(53), & \ell = \mu. \end{cases}$$

Alternatively, we can use the lattice QCD results together with the BESIII measurements and  $\tau_{\Lambda_c}$  to determine  $|V_{cs}|$ :

$$|V_{cs}| = 0.949(24)_{\text{LQCD}}(51)_{\text{Exp.}} \quad \text{from } \Lambda_c \rightarrow \Lambda \ell^+ \nu_\ell.$$

For comparison:

$$|V_{cs}| = \begin{cases} 1.008(5)_{\text{LQCD}}(16)_{\text{Exp.}} & \text{from } D_s \rightarrow \ell^+ \nu_\ell \text{ [1, 2],} \\ 0.975(25)_{\text{LQCD}}(7)_{\text{Exp.}} & \text{from } D \rightarrow K \ell^+ \nu_\ell \text{ [1, 3],} \\ 0.975(38)_{\text{LQCD}}(4)_{\text{Exp.}} & \text{from } D \rightarrow K \ell^+ \nu_\ell \text{ [4],} \\ 0.978(35)_{\text{LQCD+Exp.}} & \text{from } D \rightarrow K \ell^+ \nu_\ell \text{ [5]} \end{cases}$$

[1] S. Aoki *et al.* (FLAG), arXiv:1607.00299/EPJC 2017

[2] A. Bazavov *et al.* (Fermilab Lattice and MILC), arXiv:1407.3772/PRD 2014

[3] H. Na *et al.* (HPQCD), arXiv:1008.4562/PRD 2010

[4] V. Lubicz *et al.* (ETMC), arXiv:1706.03017

[5] L. Riggio, G. Salerno, S. Simula, arXiv:1706.03657

1  $b \rightarrow ul^- \bar{\nu}_e$  and  $b \rightarrow cl^- \bar{\nu}_e$

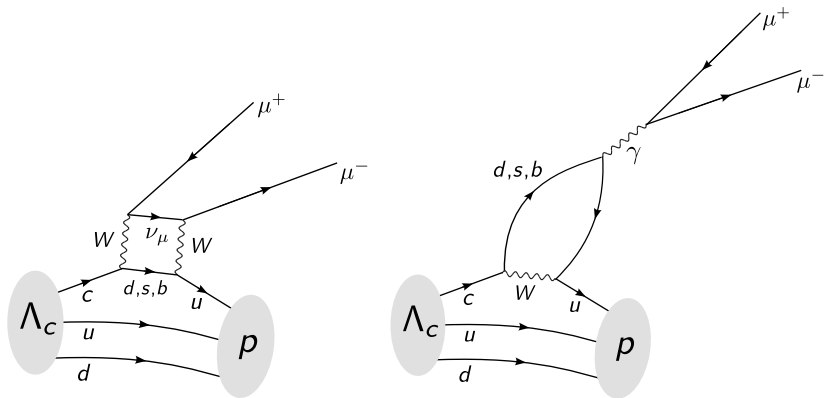
2  $b \rightarrow c\tau^- \bar{\nu}$

3  $b \rightarrow sl^+ l^-$

4  $c \rightarrow sl^- \bar{\nu}_e$

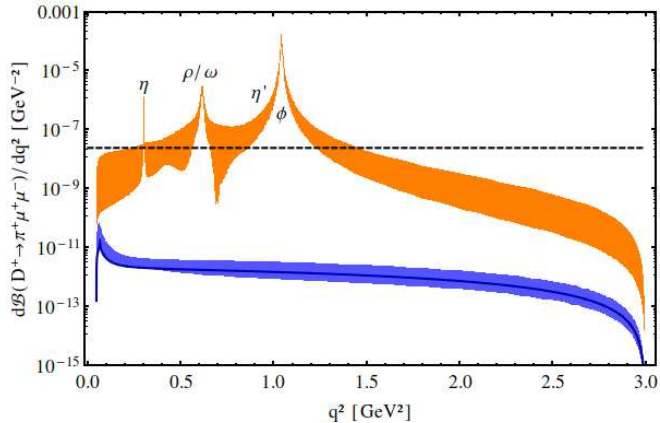
5  $c \rightarrow ul^+ l^-$





Interesting for LHCb!

$c \rightarrow u \mu^+ \mu^-$  decays are dominated by resonant contributions from nonlocal matrix elements.

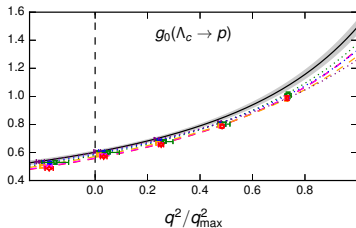
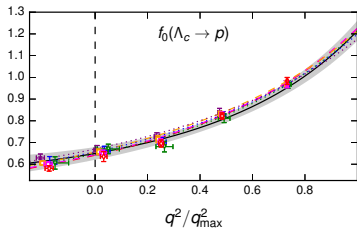
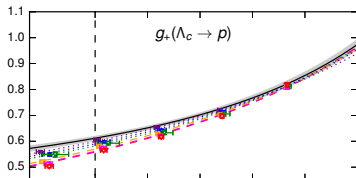
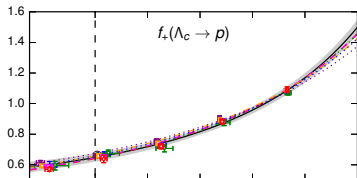
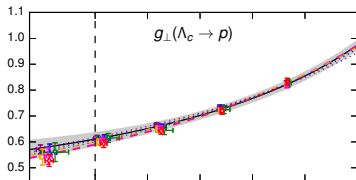
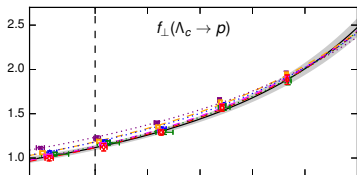


[S. de Boer, G. Hiller, arXiv:1510.00311/PRD 2016]

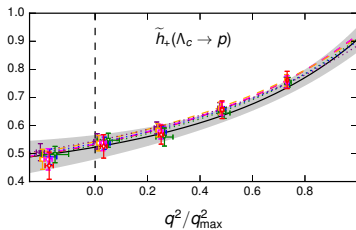
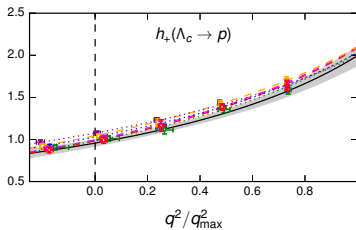
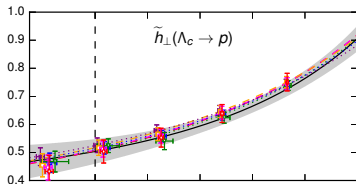
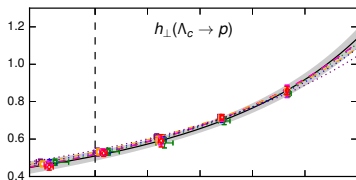
Why are the short-distance  $\Lambda_c \rightarrow p$  form factors still useful?

- BSM couplings could be much larger than SM couplings.  
Lepton-flavor-violating modes such as  $\Lambda_c \rightarrow p e^+ \mu^-$  are short-distance only.
- $\Lambda_c \rightarrow p$  form factors are useful as input for factorization approximation of  $\Lambda_c \rightarrow p V(\rightarrow \ell^+ \ell^-)$
- Study  $m_Q$ -dependence of  $\Lambda_Q \rightarrow p$  form factors  
(previous lattice calculations:  $m_Q = m_b, m_Q = \infty$ )
- Charged-current decay  $\Lambda_c \rightarrow n \ell^+ \nu_\ell$

Vector and axial vector form factors – preliminary; only stat. uncertainty shown



Tensor form factors – preliminary; only stat. uncertainty shown



## Conclusions and Outlook

- Thanks to the LHC and LQCD,  $\Lambda_b$  decays are providing new information on important puzzles in flavor physics:
  - $|V_{ub}|$  and  $|V_{cb}|$  exclusive-inclusive discrepancy
  - New physics in  $b \rightarrow c\tau\bar{\nu}$  transitions?
  - New physics in  $b \rightarrow s\ell^+\ell^-$  transitions?
- The lattice QCD calculation of the  $\Lambda_c \rightarrow \Lambda\ell^+\nu_\ell$  decay rate agrees with the BESIII measurement. Valuable cross-check.
- Currently finalizing analysis of  $\Lambda_c \rightarrow p$  form factors, and thinking about phenomenology.
- Higher-precision lattice calculations of  $\Lambda_b \rightarrow \Lambda_c, \Lambda, p$  form factors and studies of new decay channels are underway.
- More LHCb measurements are coming.