

Novel calculation of the nucleon form factors with Dispersively Improved Chiral EFT

Jose Manuel Alarcón



Introduction

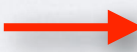
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 - Important to understand and solve the “Proton Radius Puzzle”.

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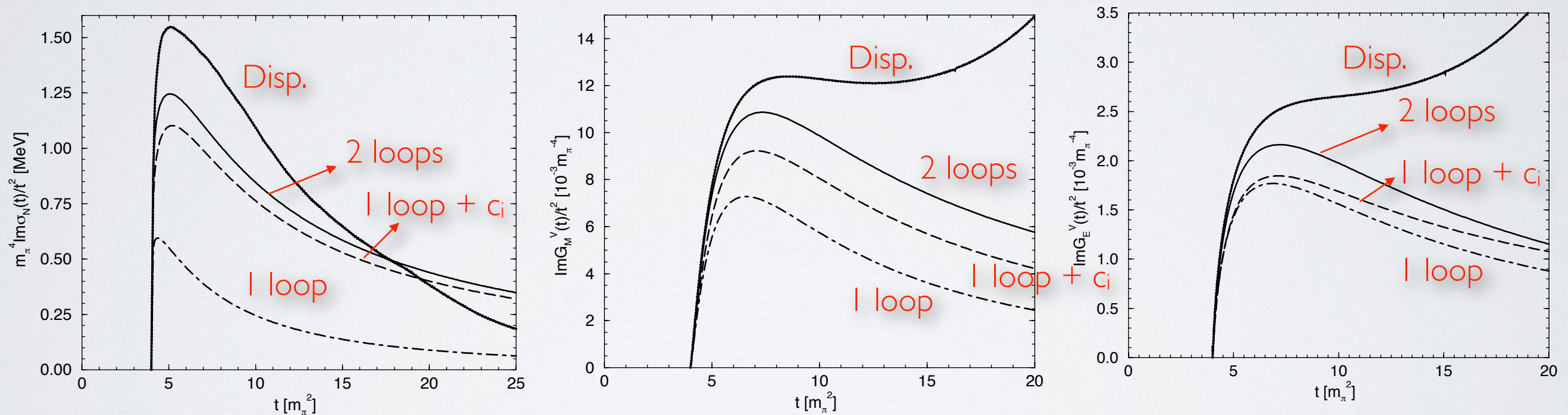
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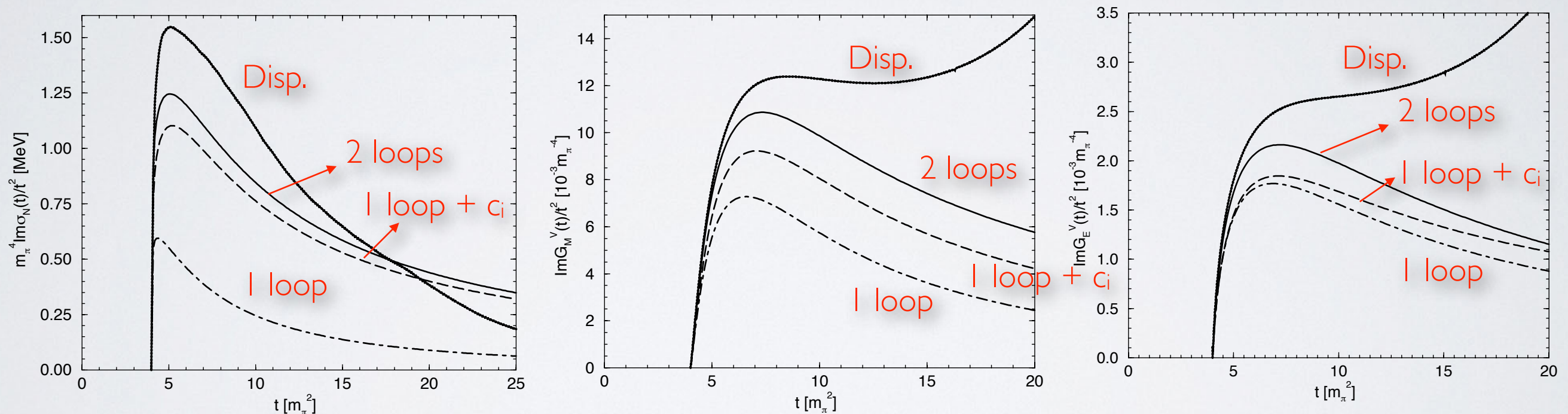
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- Higher order calculations become necessary \longrightarrow Unpractical

Form factors and their analytic structure

Form factors and their analytic structure

- Definitions.

$$\langle N(p', s') | O_\sigma(0) | N(p, s) \rangle = \sigma(t) \bar{u}(p', s') u(p, s)$$

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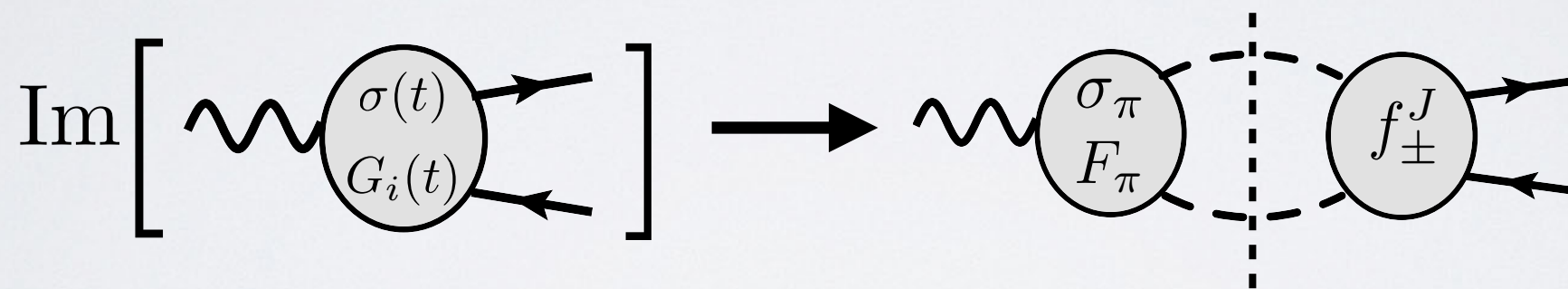
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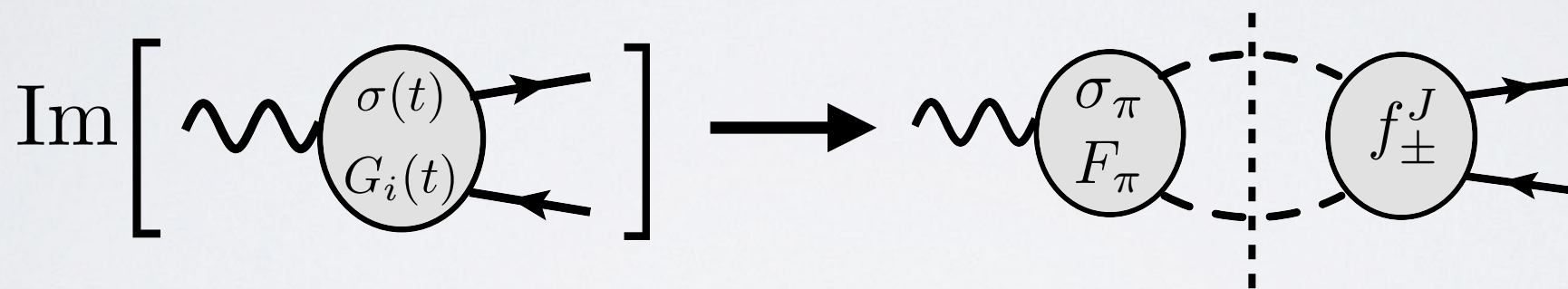
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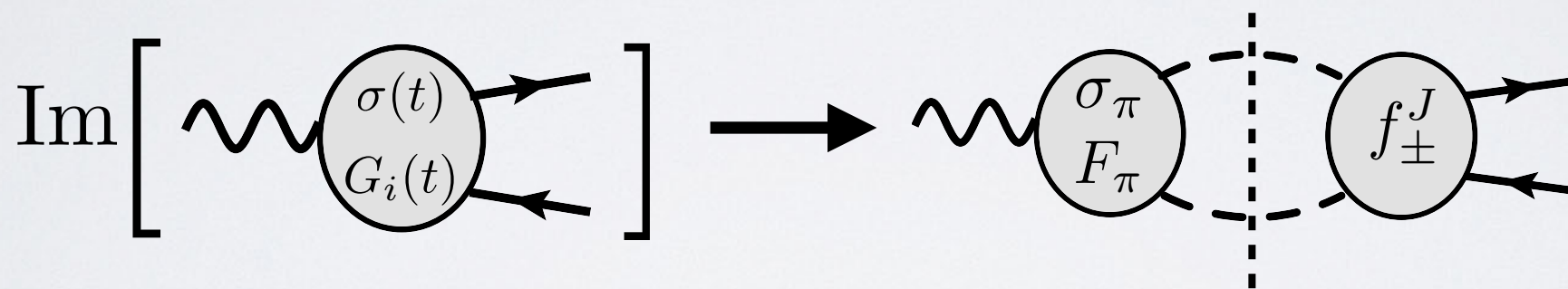
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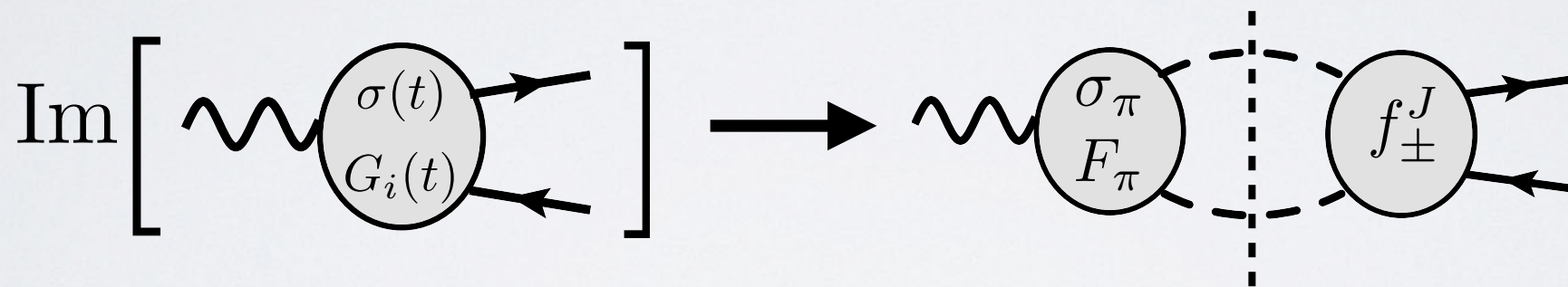
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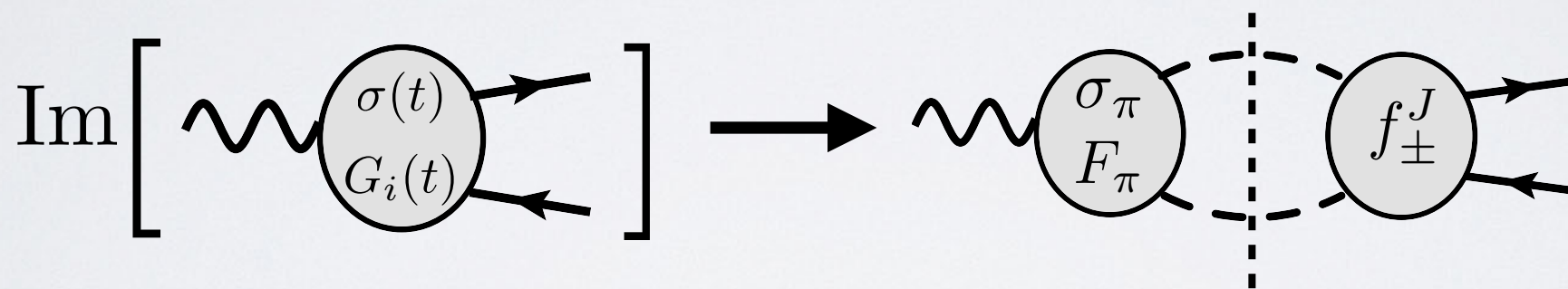
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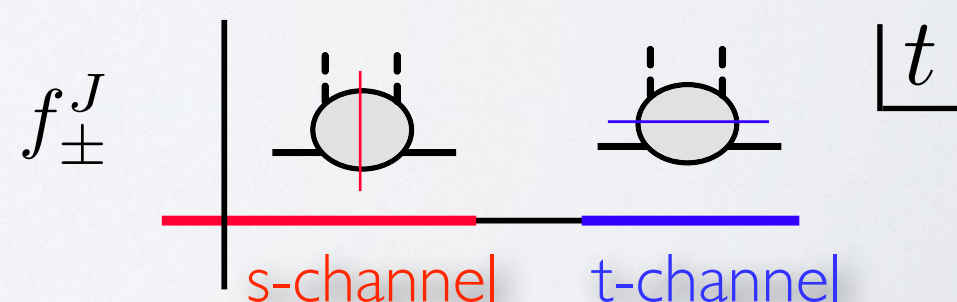
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 - NLO \longrightarrow Contact Terms (from πN , subtracting contribution of t-channel resonances from the \mathcal{C}_i [Bernard, Kaiser and Meißner, NPA 615 (1997)])

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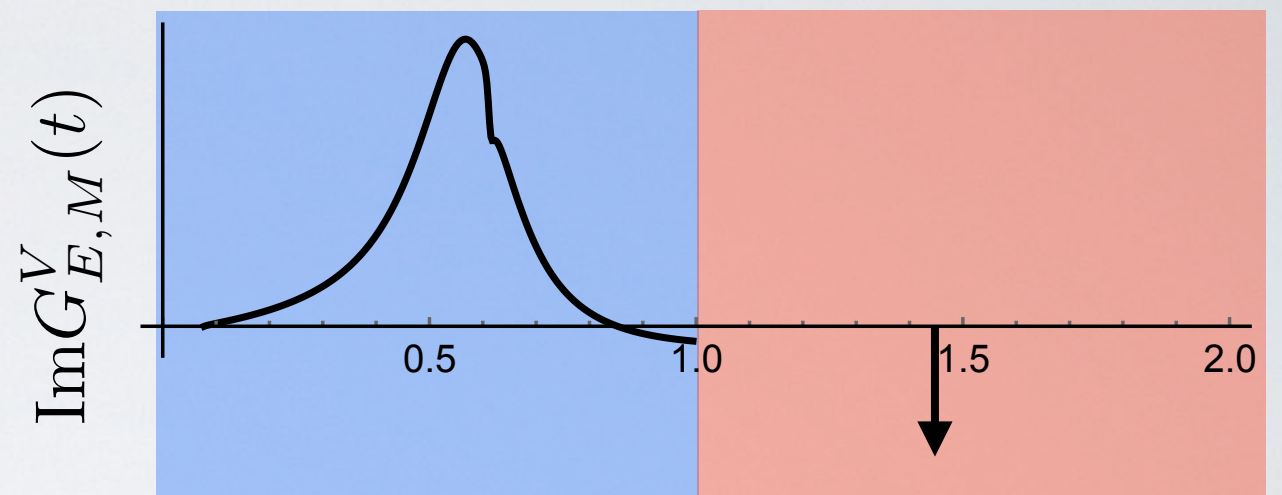
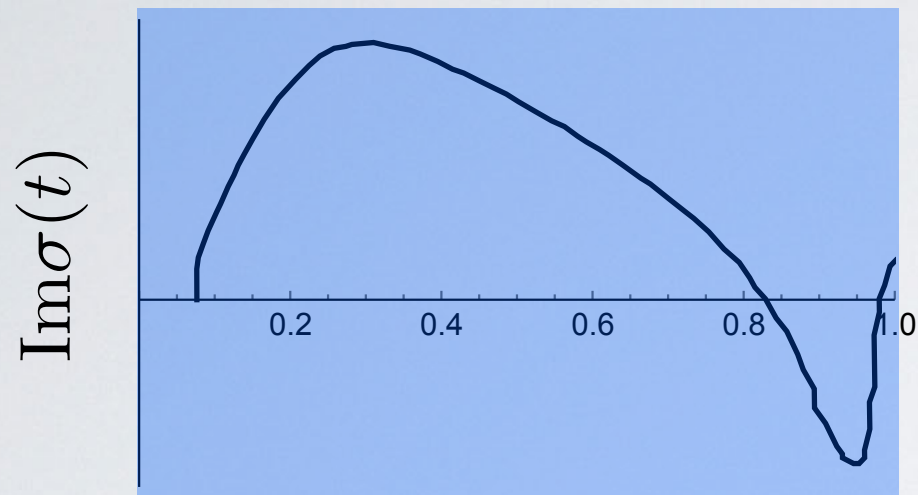
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 - NLO \longrightarrow Contact Terms (from πN , subtracting contribution of t-channel resonances from the \mathcal{C}_i [Bernard, Kaiser and Meißner, NPA 615 (1997)])
 - N2LO partially included \longrightarrow One unknown coefficient for each J_\pm^J .

Form factors and their analytic structure

- J_{\pm}^J is used to reconstruct the spectral functions up to $t < 1 \text{ GeV}^2$

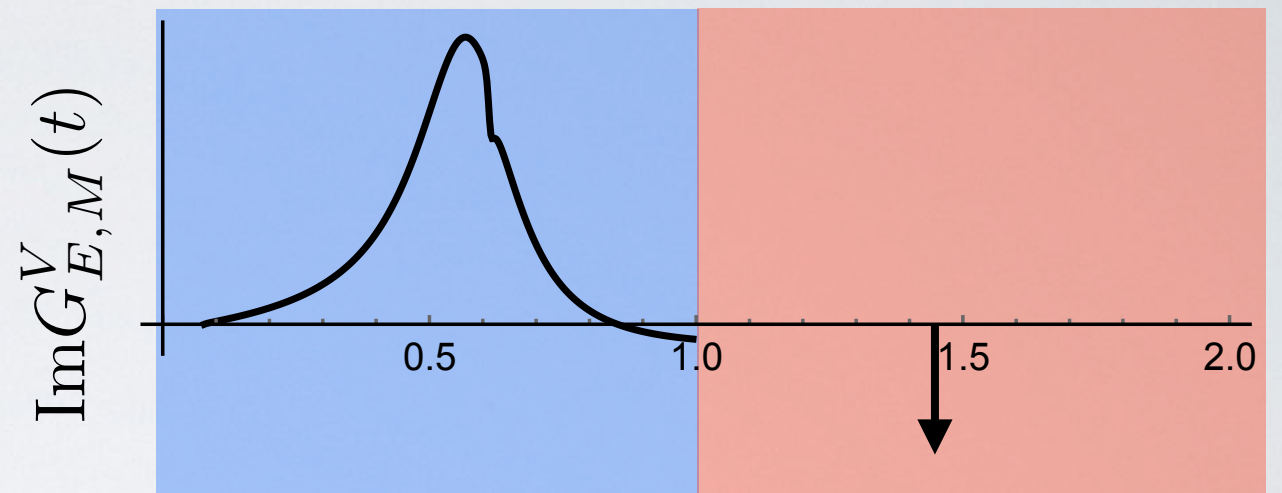
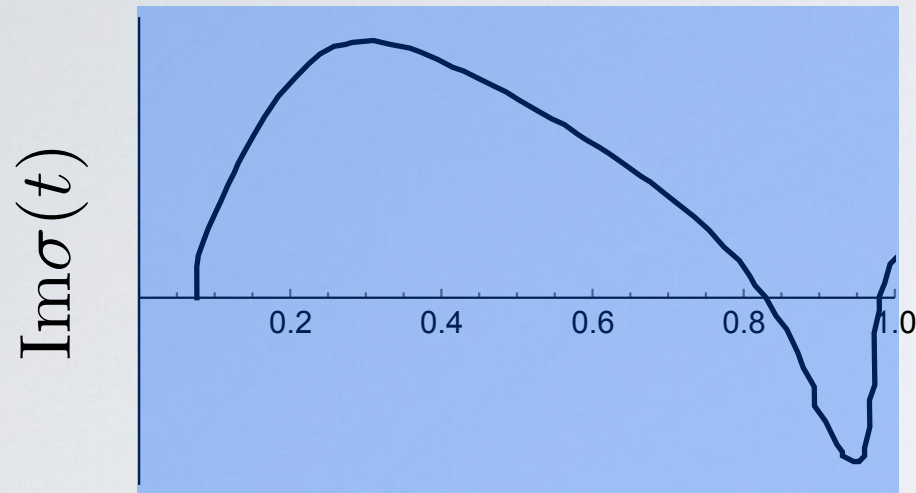
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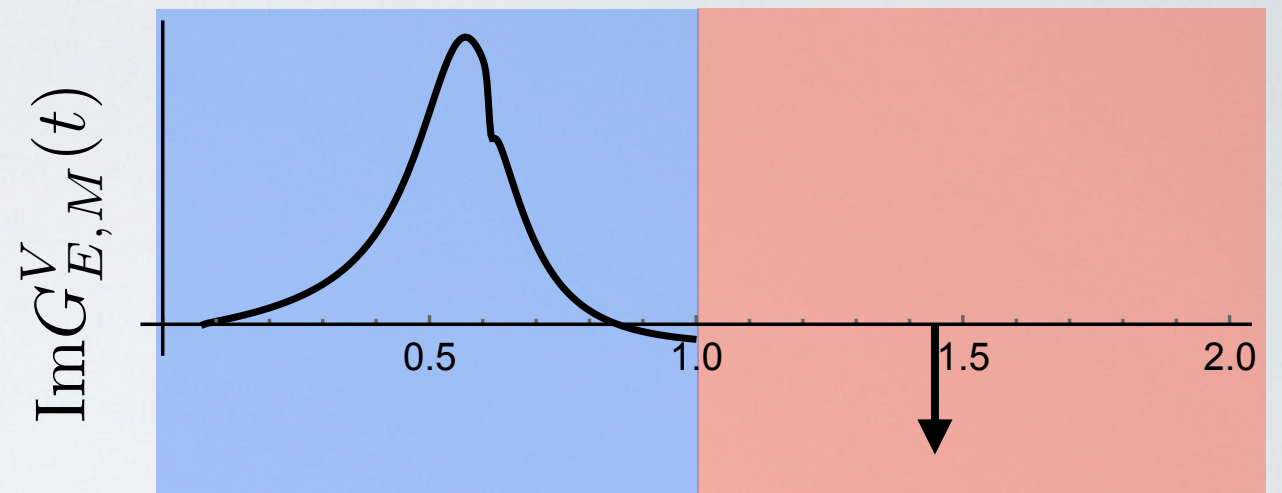
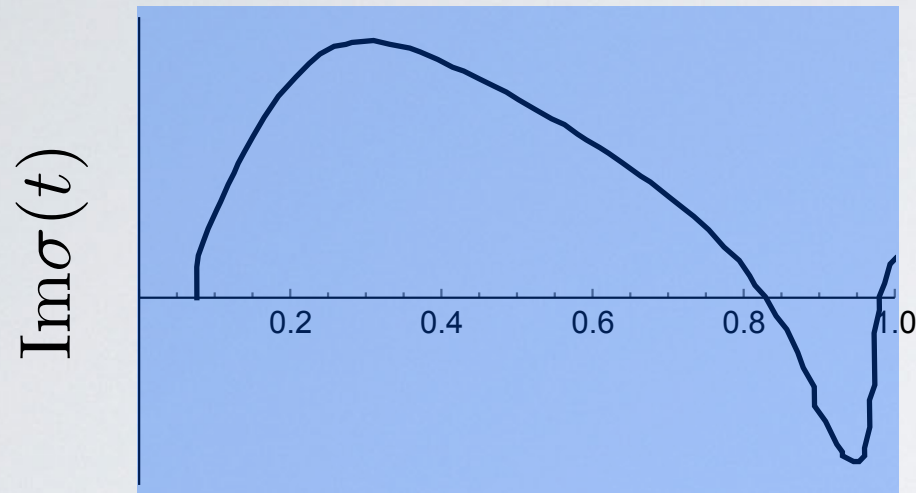


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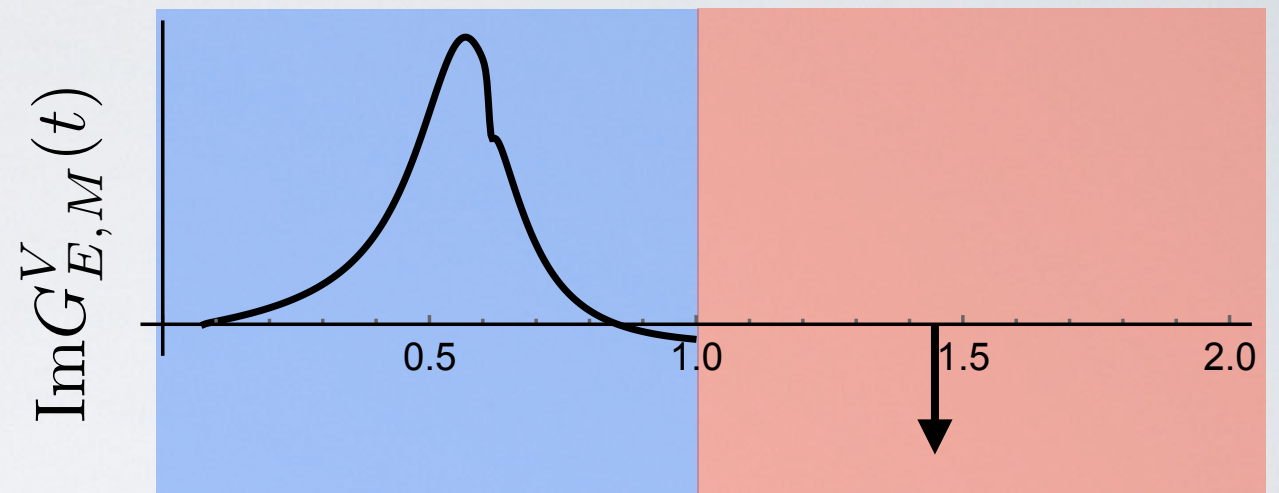
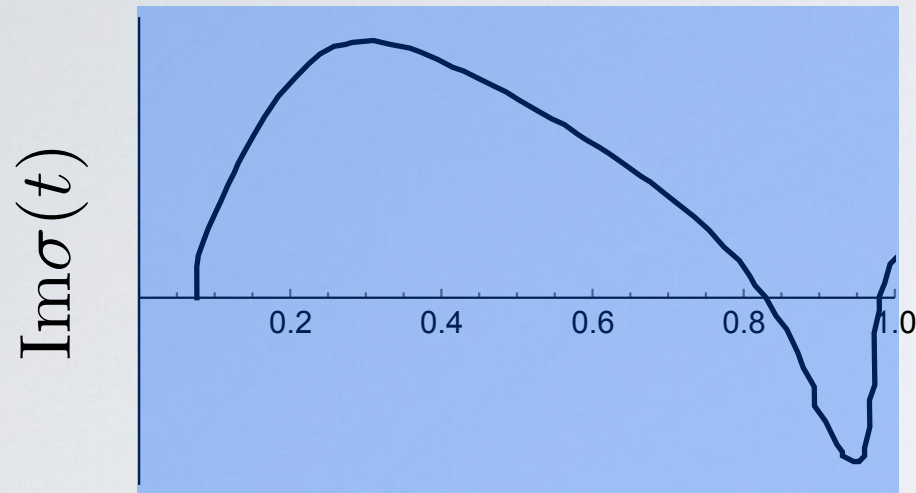
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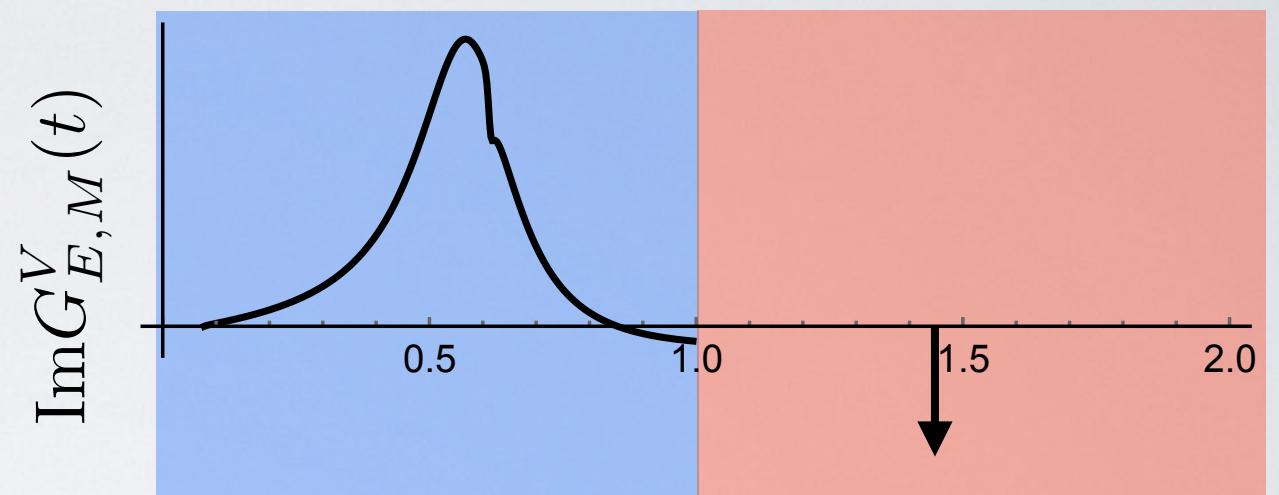
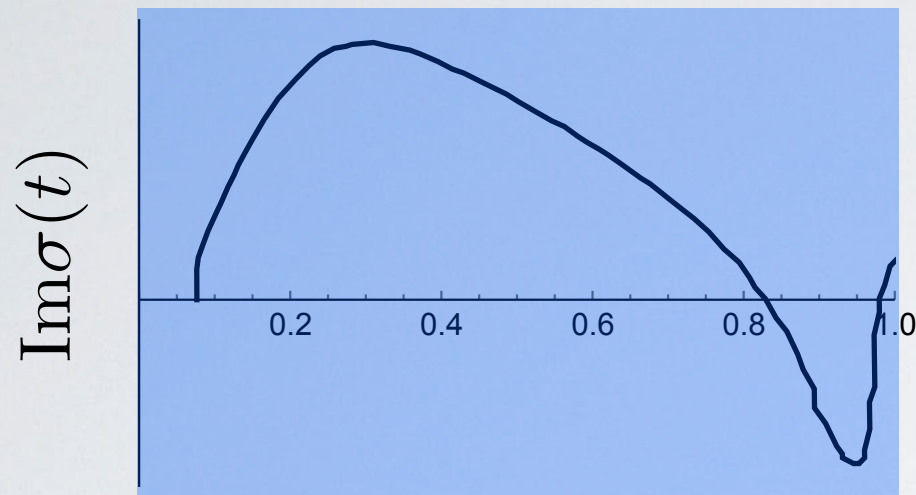
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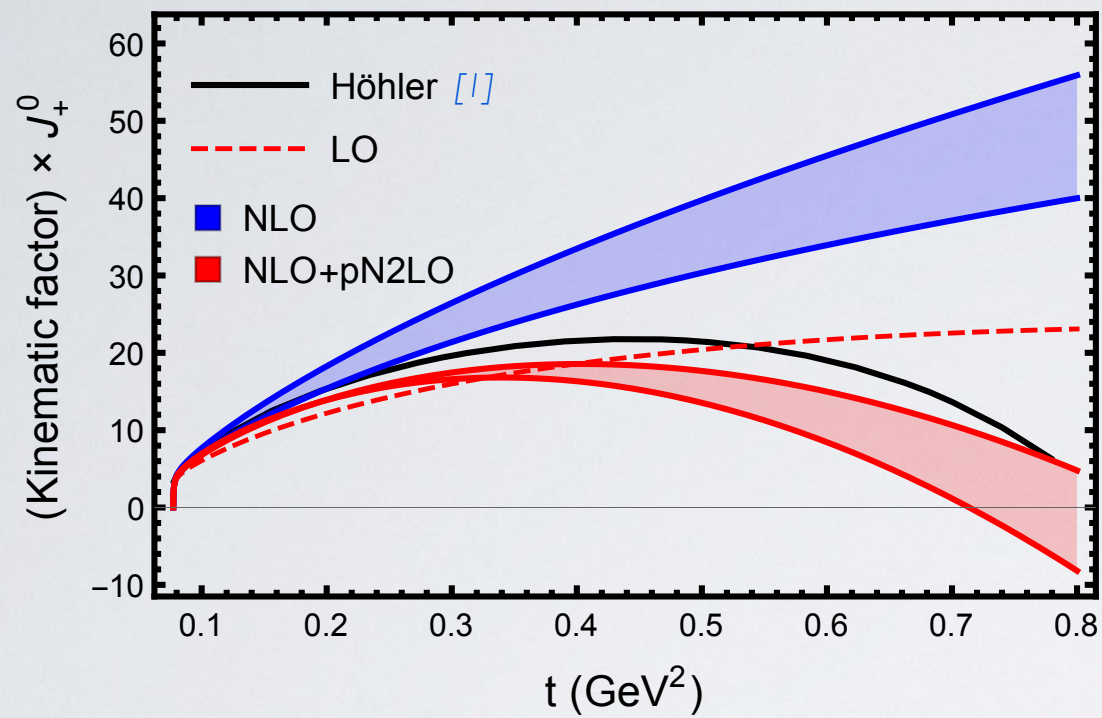
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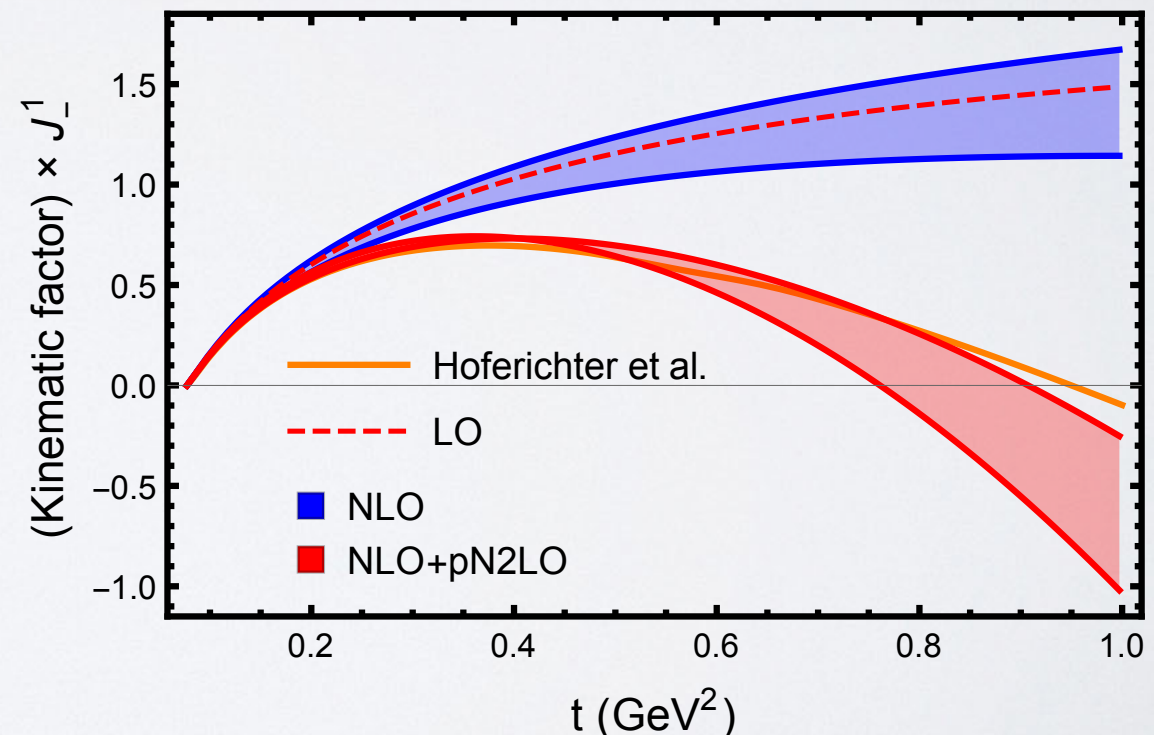
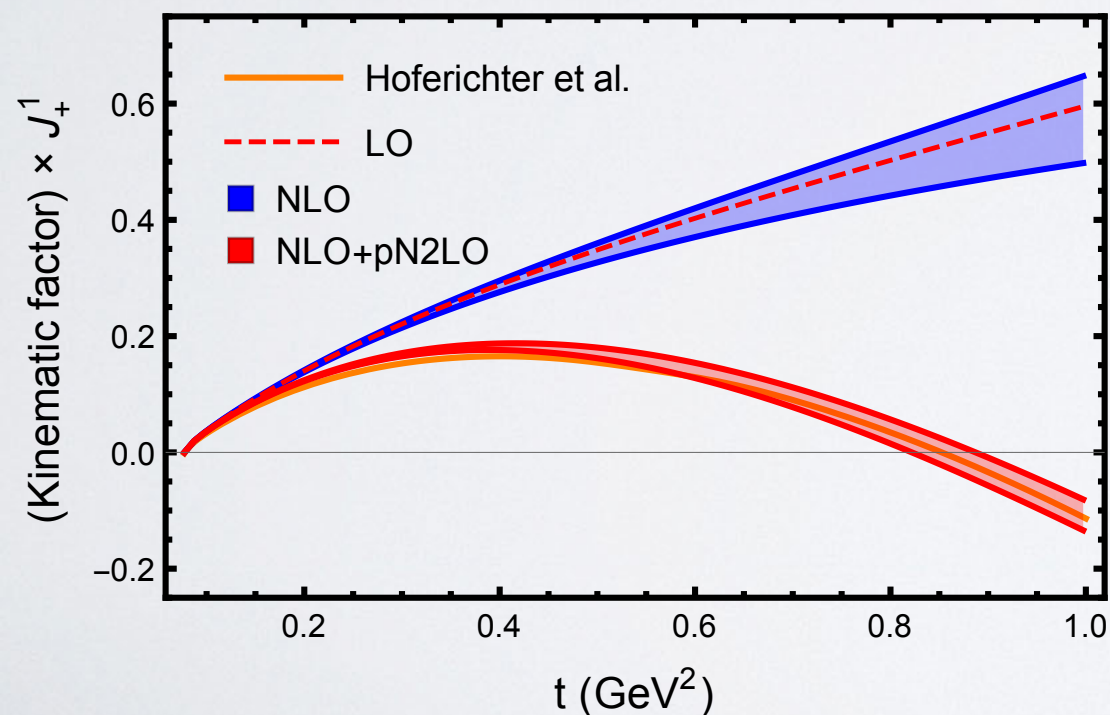
Form factors and their analytic structure

[J. M. Alarcón, C. Weiss, PRC 96 (2017)]



- Higher order corrections are important for $t > 0.2 \text{ GeV}^2$.
- Error bands shown correspond to the uncertainties in the LECs.
- Systematic errors are inferred from the difference between NLO and NLO+pN2LO.

[J. M. Alarcón, C. Weiss, 1710.06430; in preparation]



[1] Höhler, in Landolt-Börnstein, 9b2, ed. H. Schopper (Springer, Berlin, 1983)

Form factors and their analytic structure

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Form factors and their analytic structure

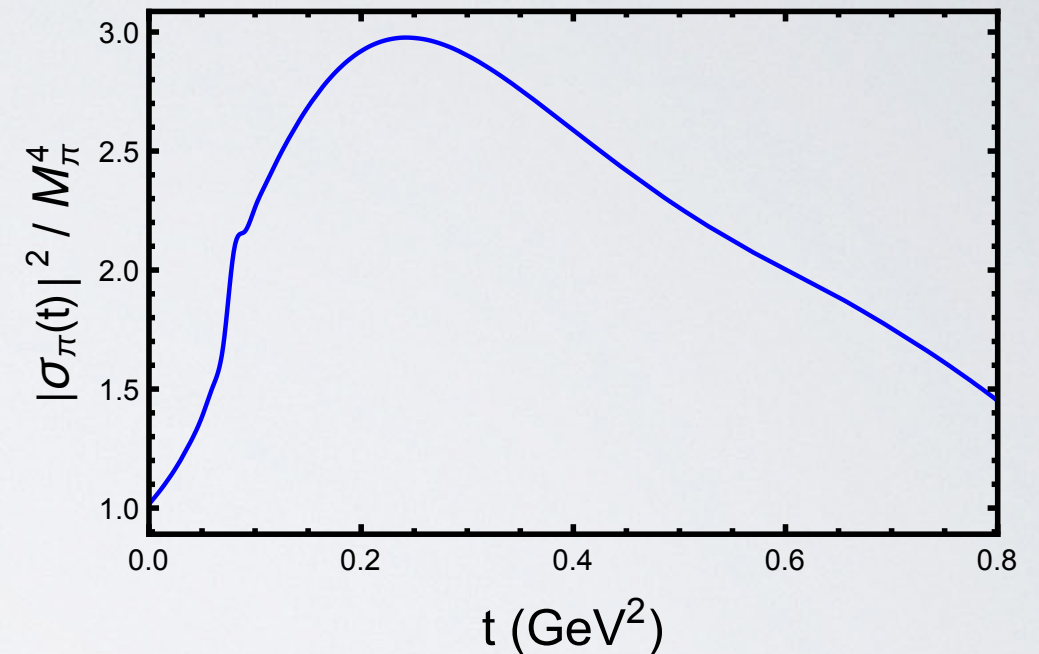
- Pion scalar FF
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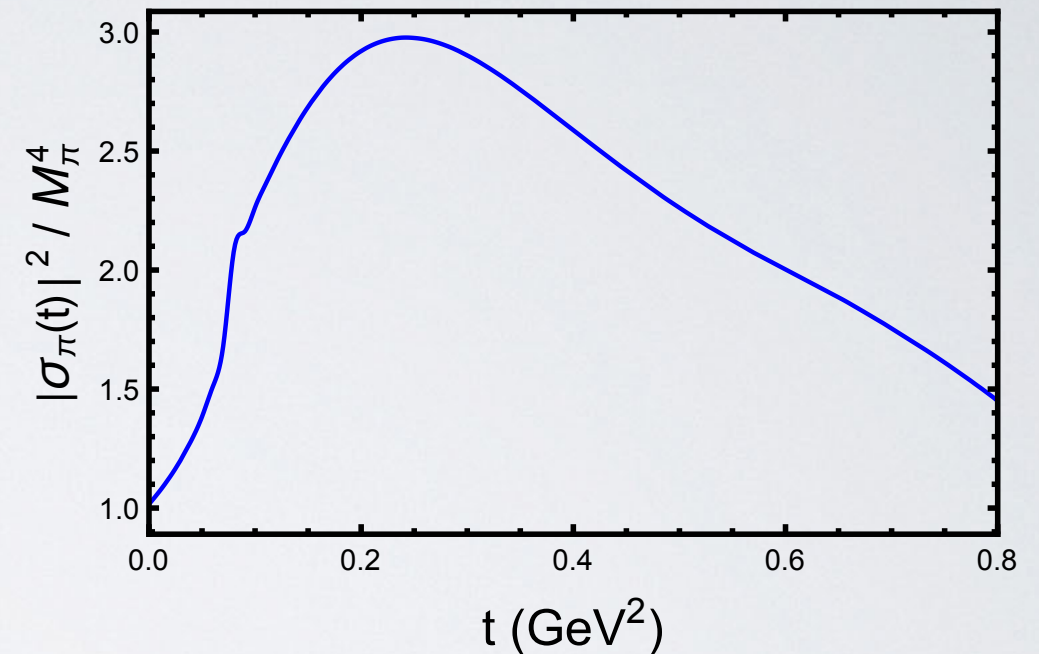


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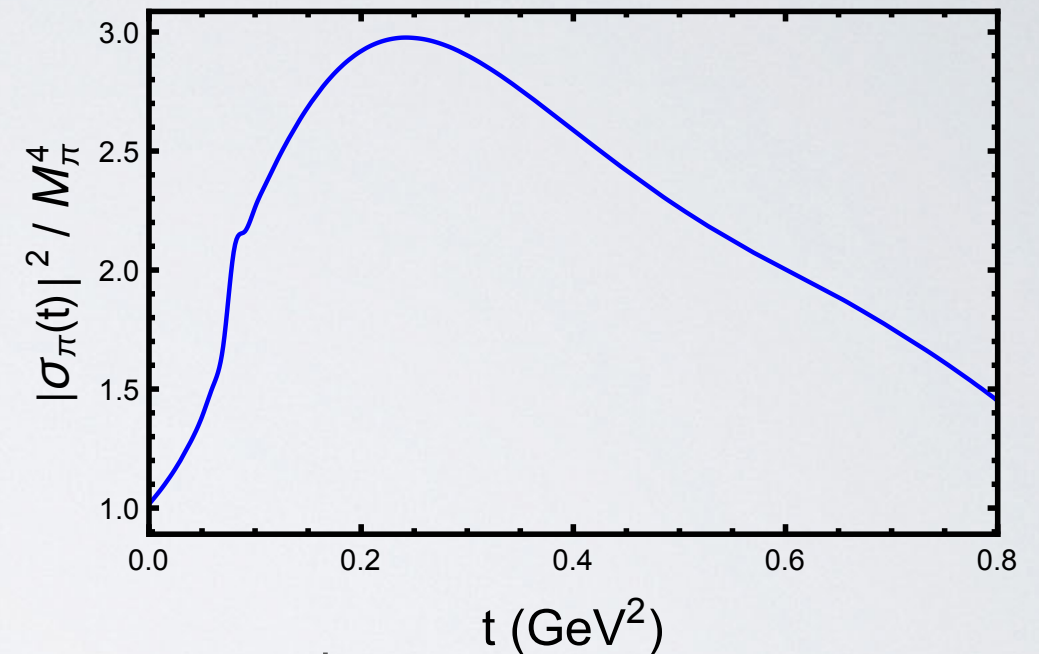
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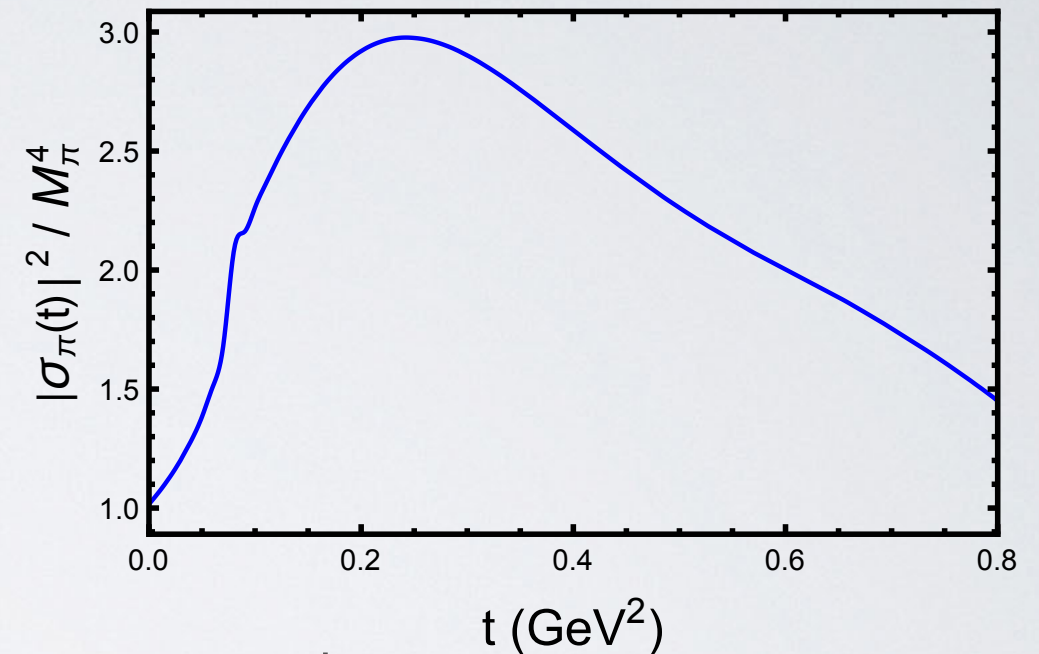
[Lorenz, Hammer, Meißner, EPJ A 48 (2012)]

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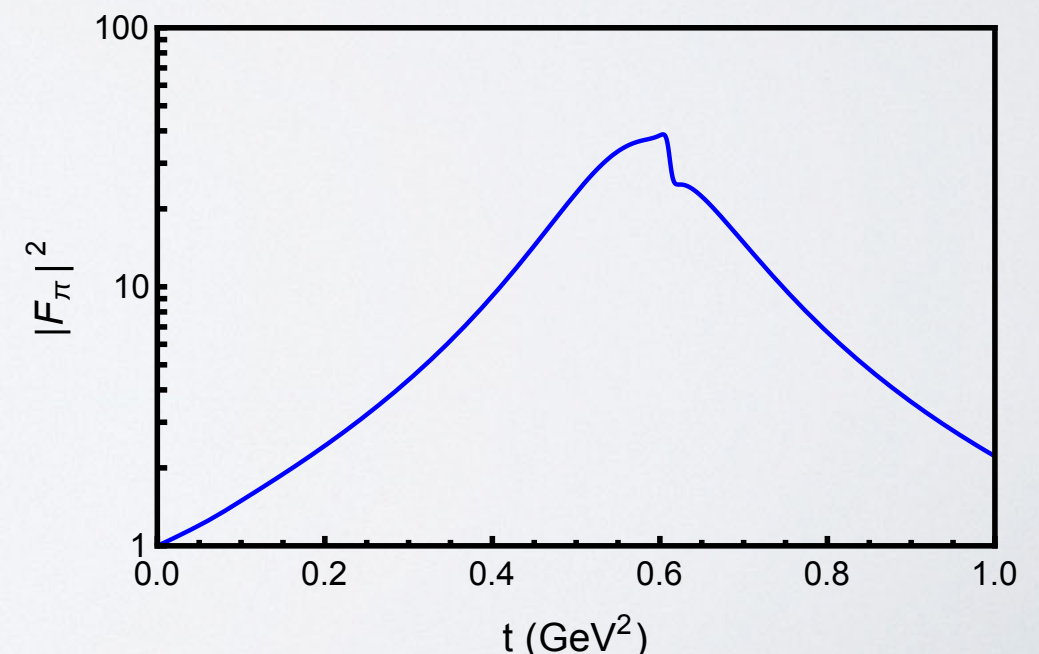
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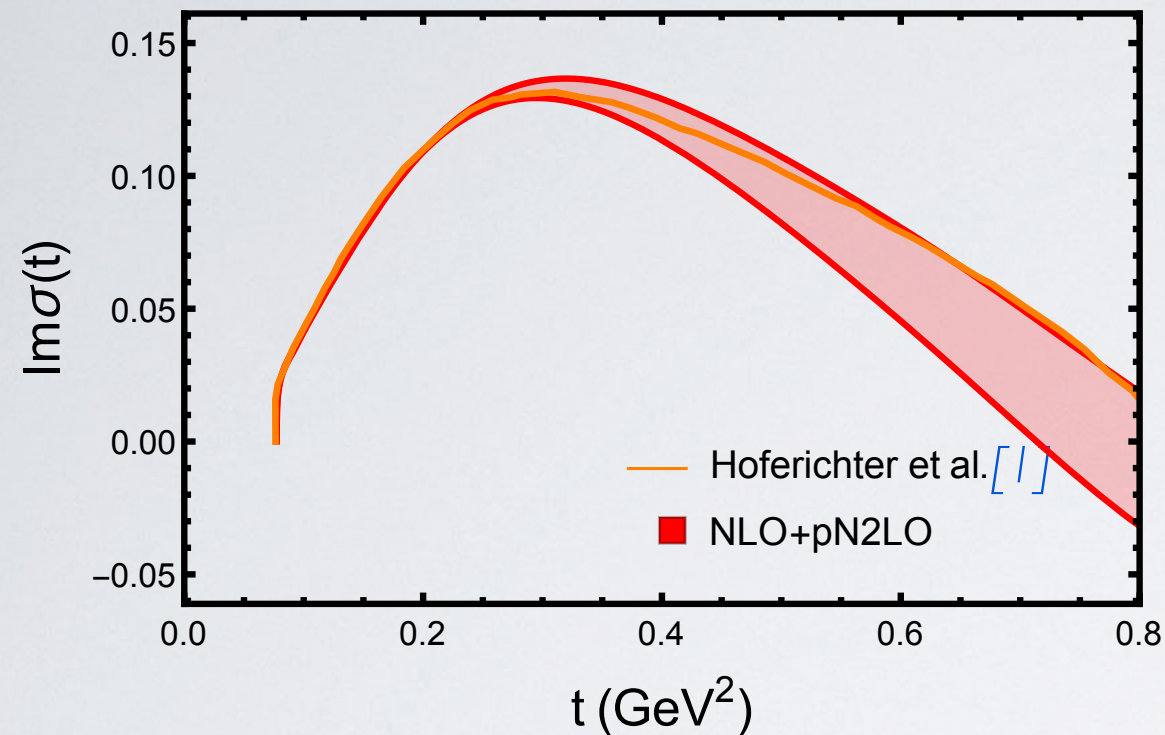
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Spectral Functions

[J. M. Alarcón, C. Weiss, PRC 96 (2017)]



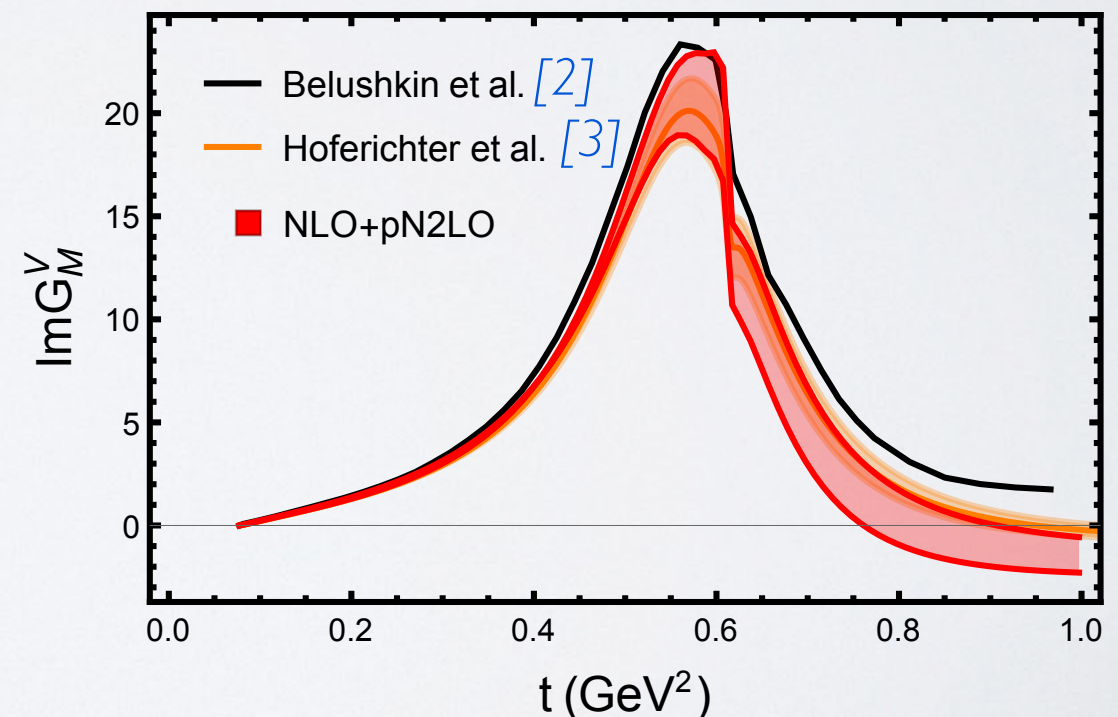
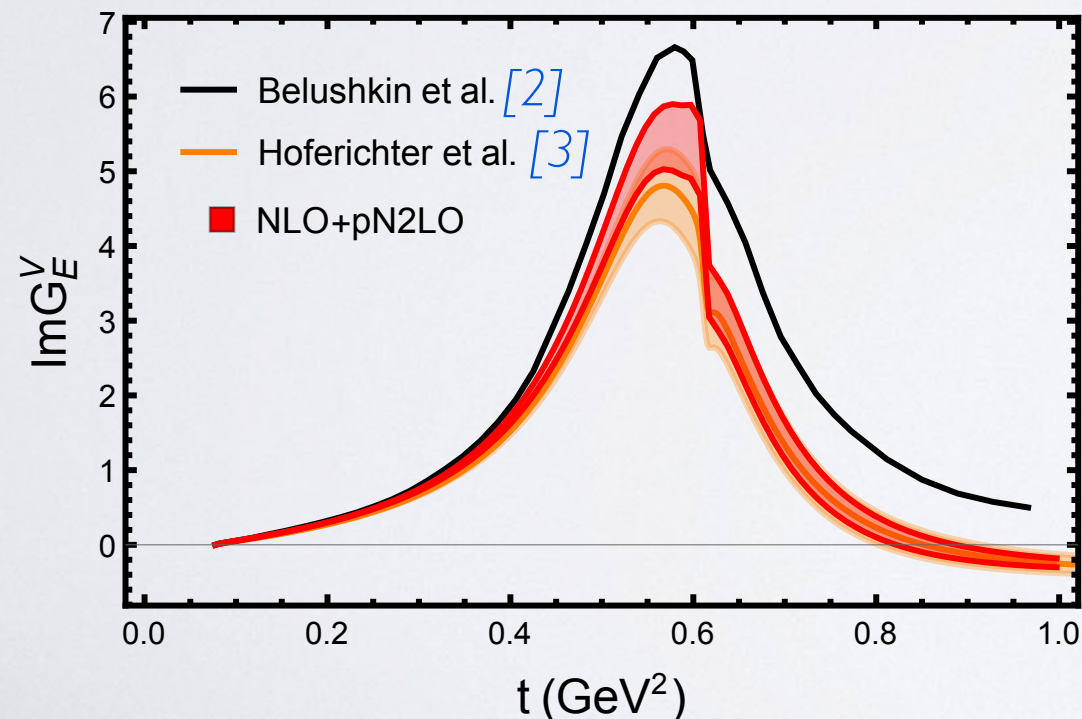
$$\text{Im}\sigma(t) = \frac{3k_{cm}}{4\sqrt{t}(m_N^2 - t/4)} |\Gamma_\pi(t)|^2 J_+^0(t)$$

$$\text{Im}G_{\{E,M\}}^V(t) = \frac{k_{cm}^3}{\{m_N, \sqrt{2}\}\sqrt{t}} |F_\pi(t)|^2 J_\pm^1(t)$$

[1] Hoferichter, Ditsche, Kubis, Meißner, JHEP 063 (2012)

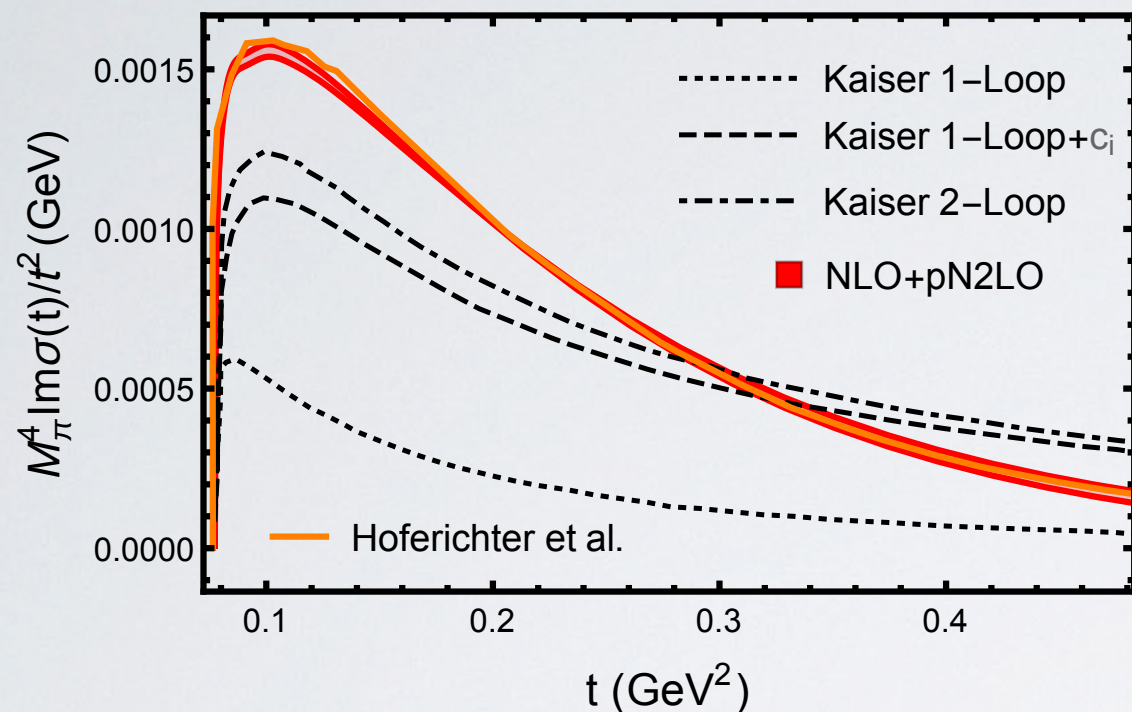
[2] Belushkin, Hammer and Meißner, PRC 75 (2007)

[3] Hoferichter, Kubis, Ruiz de Elvira, Hammer, Meißner EPJA 52 (2016)



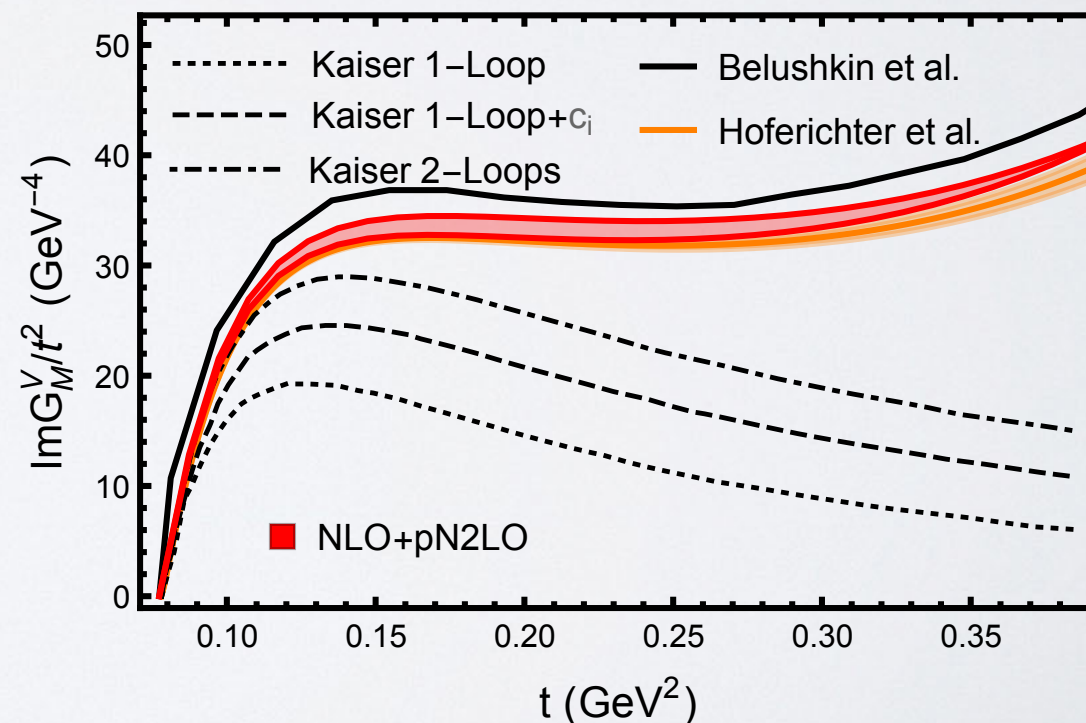
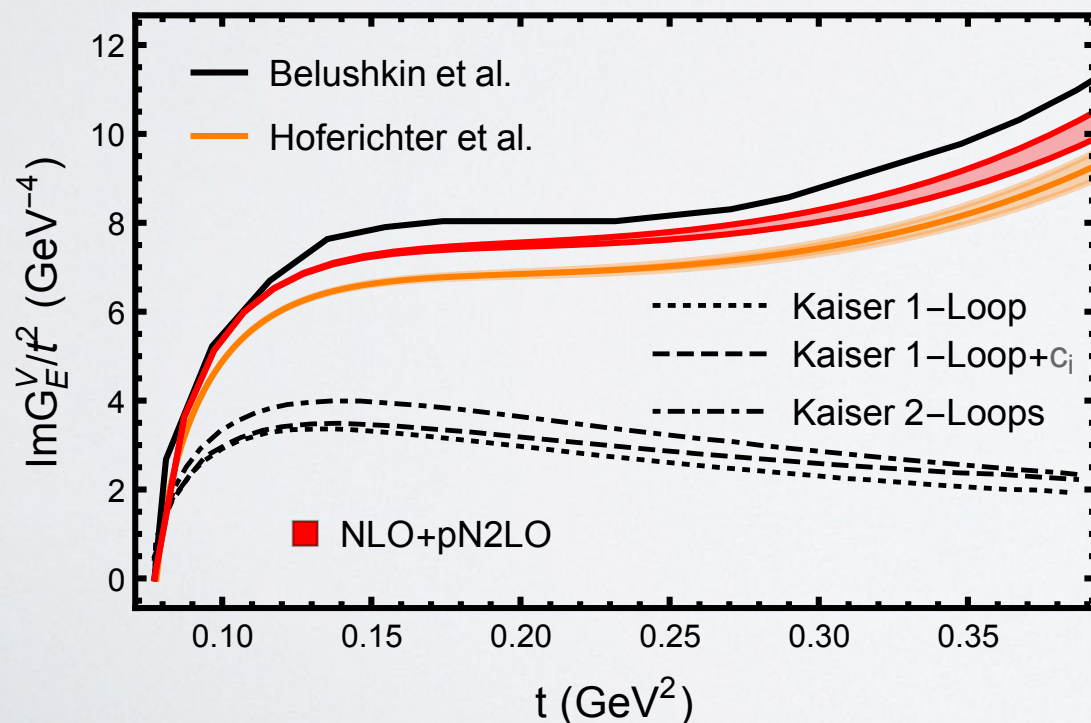
[J. M. Alarcón, C. Weiss, in preparation]

- Comparison with respect to the old results



- Conclusions:

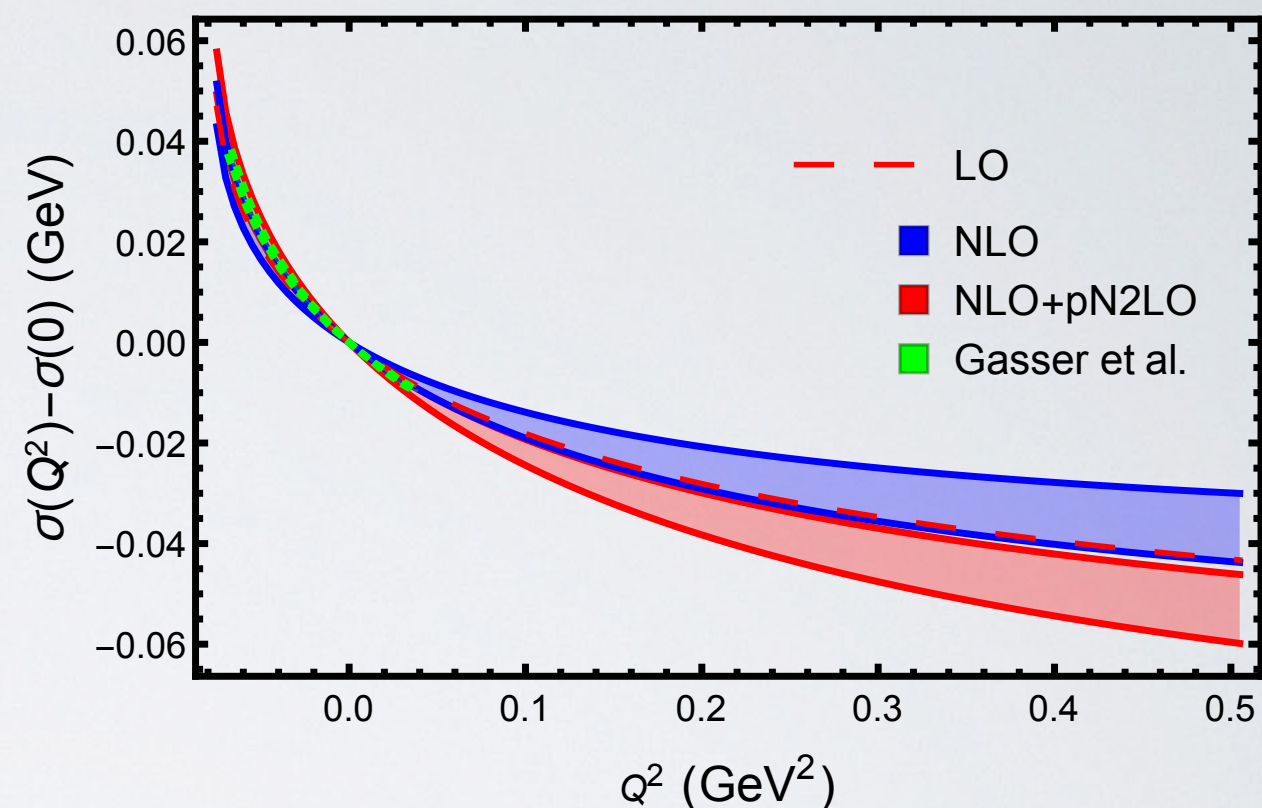
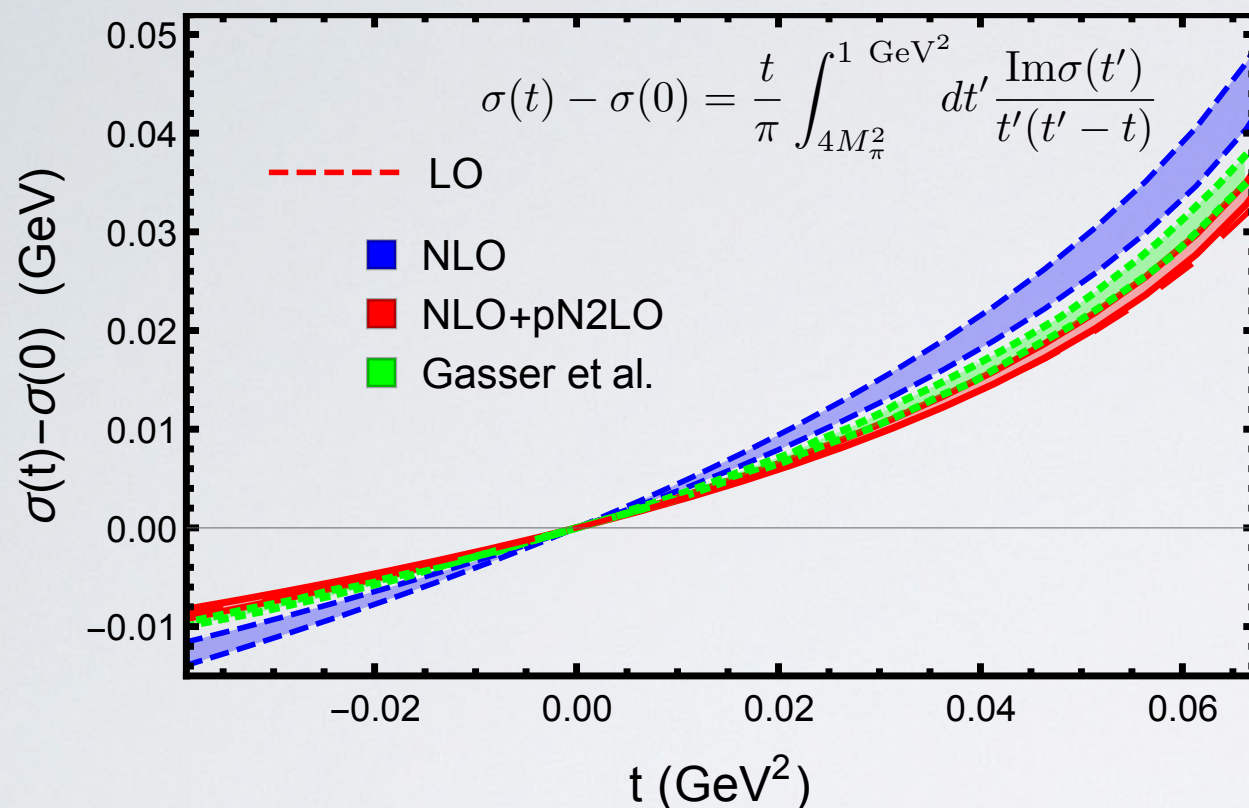
- Brute force calculations are hopeless.
- Non-perturbative effects are visible in the near-threshold region.
- Based on unitarity one achieves a factorization suitable for perturbative calculations.



Scalar Form Factor

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[J. M. Alarcón, C. Weiss, PRC 96 (2017)]



		LO	NLO	NLO+N2LO	GLS [1]	HKMS[2]
$\langle r^2 \rangle_S$ (fm ²)	$(\sigma(0) = 59 \text{ MeV})$	1.06	1.40–1.67	1.03–1.13	–	1.07(4)
	$(\sigma(0) = 45 \text{ MeV})$	1.38	1.83–2.19	1.34–1.49	1.6	–

	LO	NLO	NLO+N2LO	GLS [3]	HDKM [4]	ChPT $\mathcal{O}(p^3)$	ChPT $\mathcal{O}(p^4)$
Δ_σ (MeV)	13.3	17.4 - 20.6	13.3 - 14.5	15.2(4)	13.9(3)	4.6	$14.0 + 4M_\pi^4 \bar{e}_2$

[1] Gasser, Leutwyler, Sainio, PLB 253 260-264, [2] Hoferichter, Klos, Menéndez, Schwenk PRD 94 (2016)

[3] Gasser, Leutwyler, Sainio, PLB 253 252-259, [4] Hoferichter, Ditsche, Kubis, Meißner, JHEP 1206 (2012)

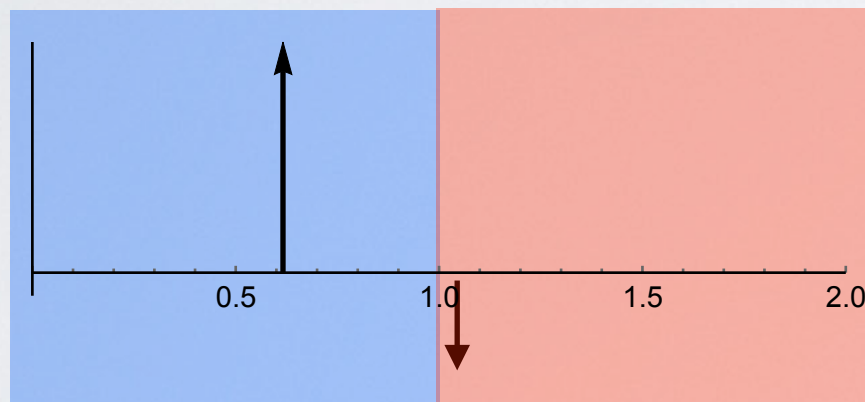
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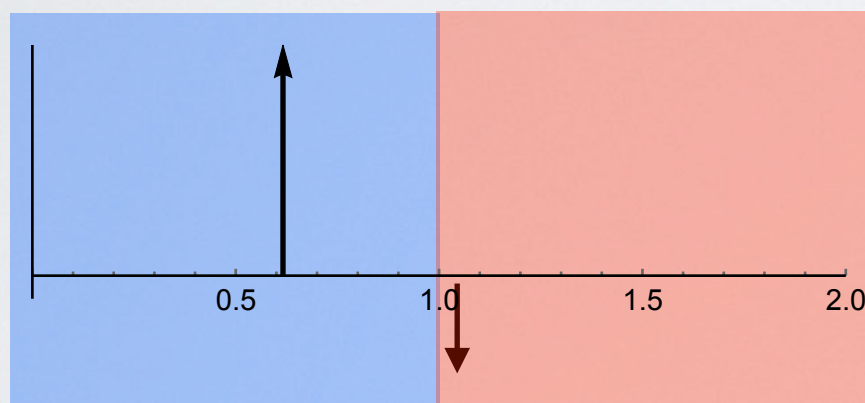
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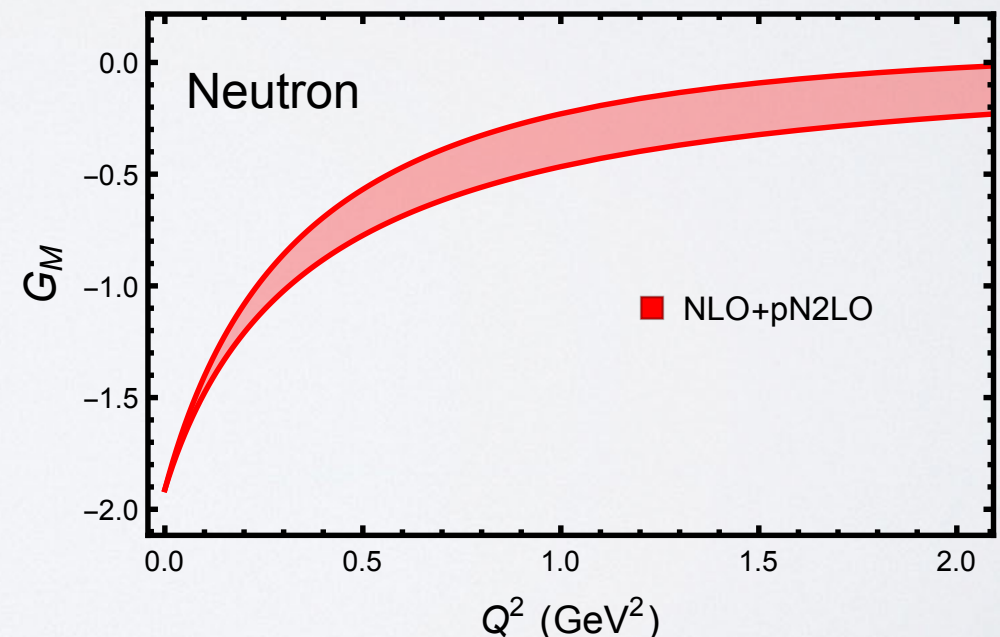
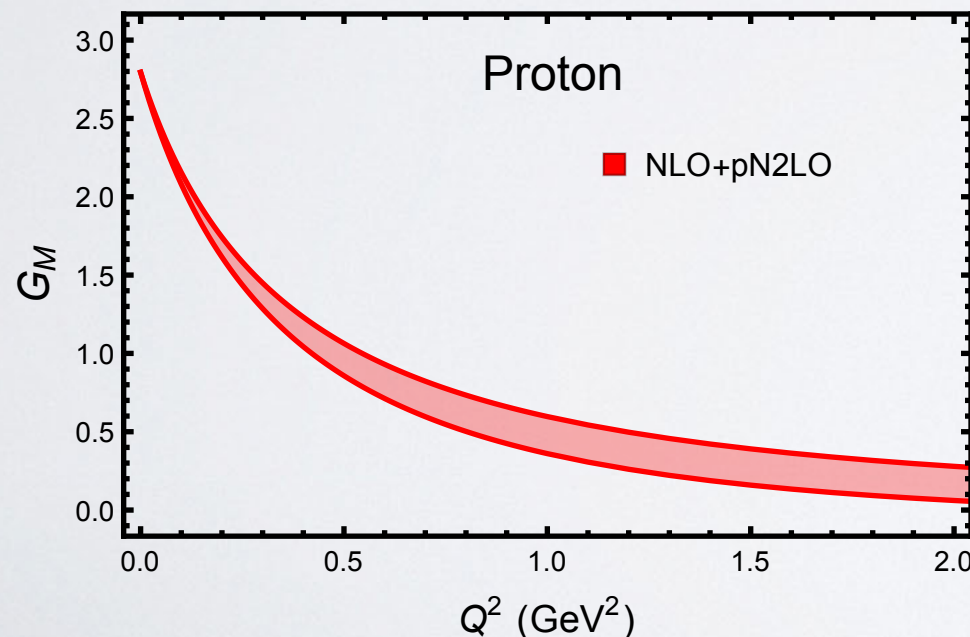
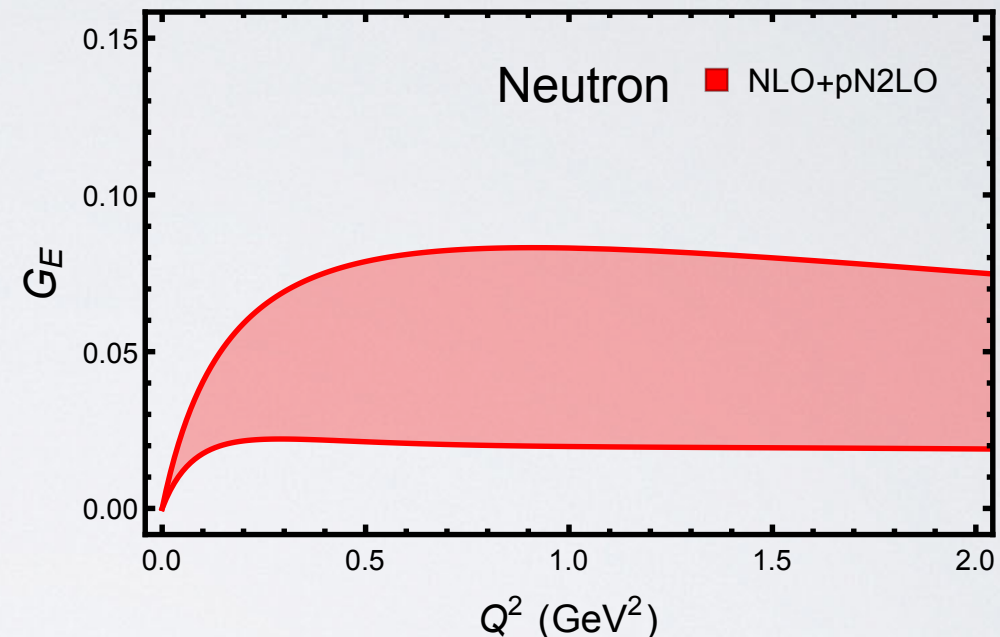
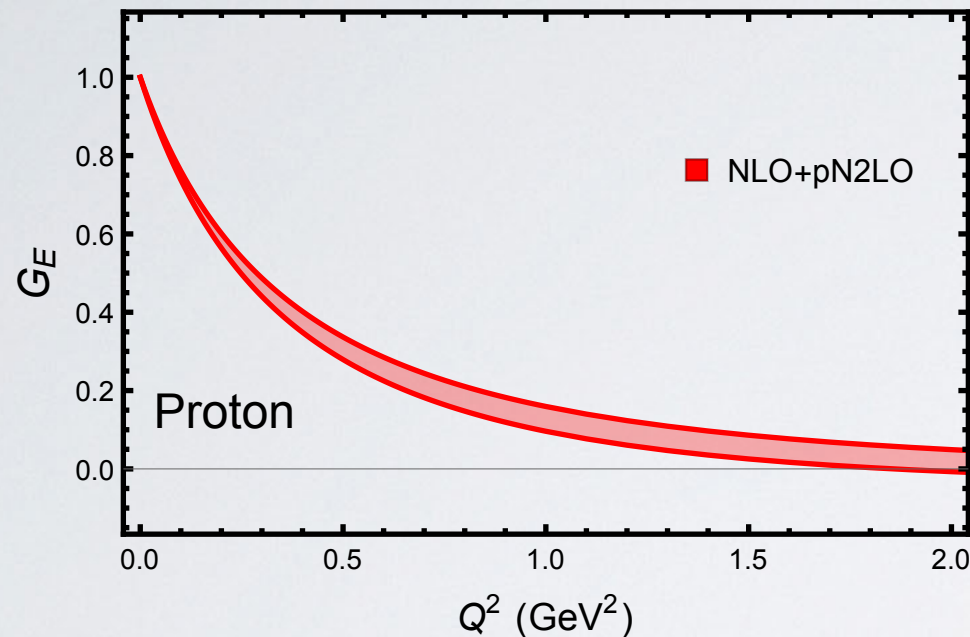
- We fix the couplings by imposing the charge and radii sum rules:

$$G_{E,M}^S(0) = \frac{1}{\pi} \int_{4M_\pi^2}^{\infty} dt' \frac{\text{Im}G_i^S(t')}{t'}$$

$$\langle r_{E,M}^2 \rangle^S = \frac{6}{\pi} \int_{4M_\pi^2}^{\infty} dt' \frac{\text{Im}G_{E,M}^S(t')}{t'^2}$$

- Reconstructing the form factors with $G_{E,M}^{p,n}(t) = \frac{1}{\pi} \int_{4M_\pi^2}^{\infty} dt' \frac{\text{Im} G_{E,M}^{p,n}(t')}{t' - t - i0^+}$

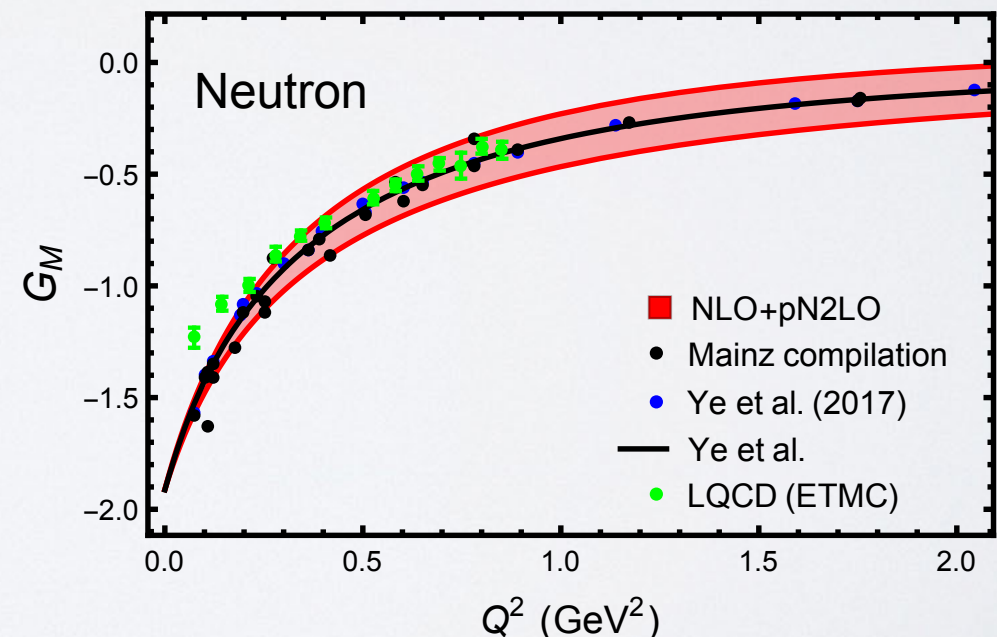
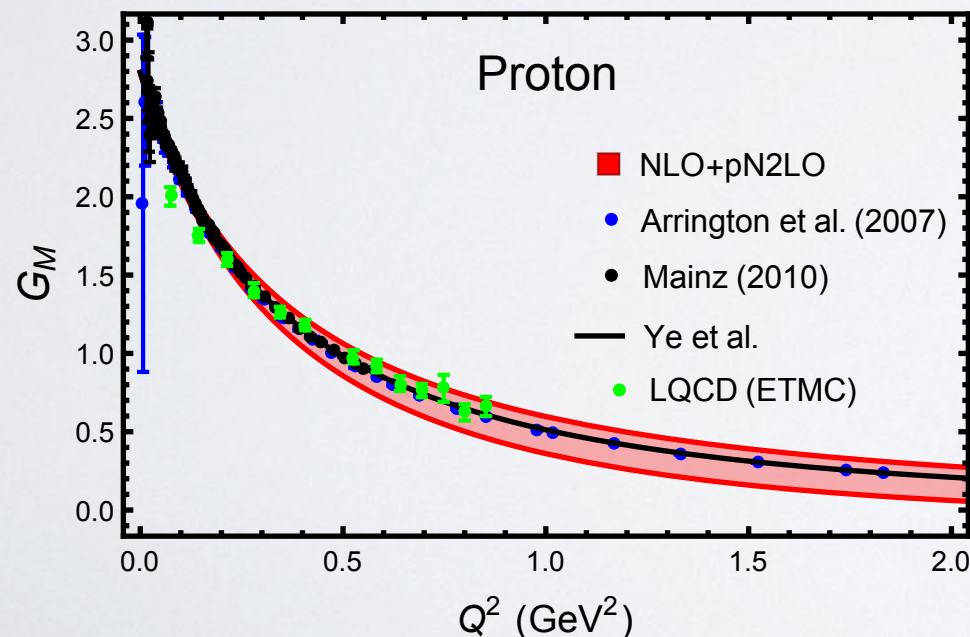
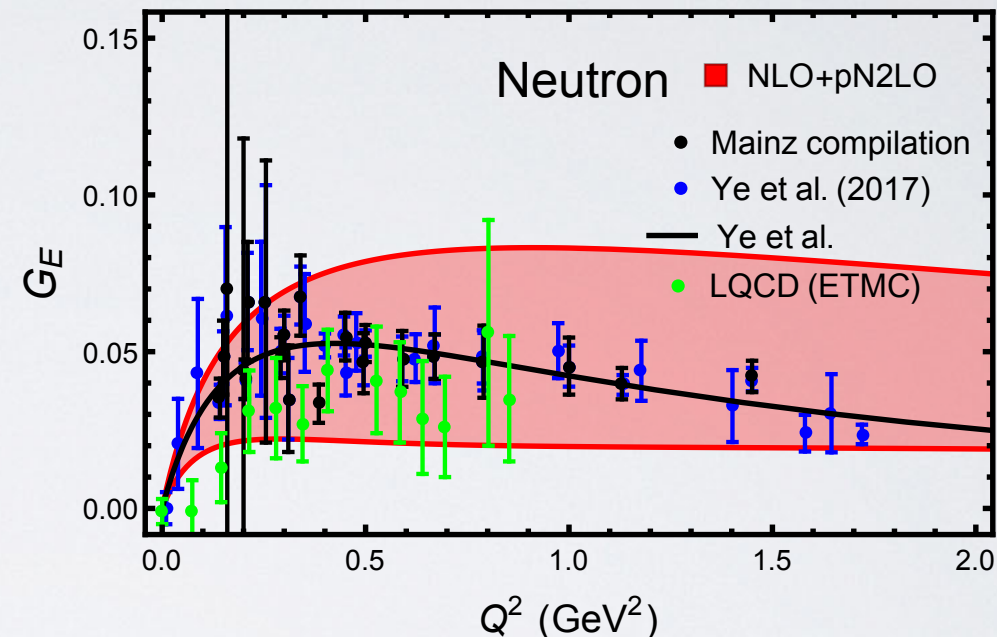
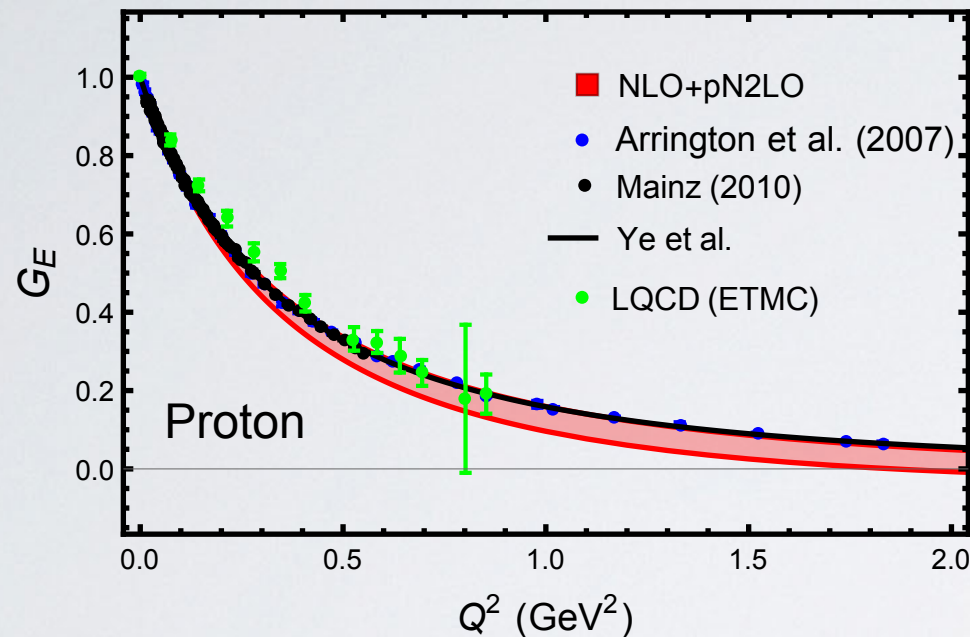
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[J. M. Alarcón, C. Weiss, in preparation]

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[J. M. Alarcón, C. Weiss, in preparation]

- Moments

$$G_E(Q^2) = 1 - \frac{\langle r_E^2 \rangle}{3!} Q^2 + \frac{\langle r_E^4 \rangle}{5!} Q^4 - \frac{\langle r_E^6 \rangle}{7!} Q^6 + \frac{\langle r_E^8 \rangle}{9!} Q^8 + \dots$$
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[J. M. Alarcón, C. Weiss, 1710.06430]

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	G_E^p	G_E^n	G_M^p	G_M^n
$\langle r^2 \rangle \text{ (fm}^2\text{)}$	(0.70059, 0.767638)	(-0.079362, -0.14641)	(0.688927, 0.764926)	(0.740108, 0.775516)
$\langle r^4 \rangle \text{ (fm}^4\text{)}$	(1.47274, 1.6019)	(-0.635304, -0.506146)	(1.67591, 1.78208)	(2.04528, 2.04238)
$\langle r^6 \rangle \text{ (fm}^6\text{)}$	(8.51876, 8.96183)	(-6.10983, -5.66675)	(11.525, 11.5793)	(15.2307, 15.6446)
$\langle r^8 \rangle \text{ (} 10^2 \text{ fm}^8\text{)}$	(1.26893, 1.29627)	(-1.1587 , -1.13137)	(1.83446, 1.8822)	(2.59672, 2.69128)
$\langle r^{10} \rangle \text{ (} 10^3 \text{ fm}^{10}\text{)}$	(3.93325, 3.96482)	(-3.86593, -3.83435)	(5.70736, 5.90496)	(8.27382, 8.58060)
$\langle r^{12} \rangle \text{ (} 10^5 \text{ fm}^{12}\text{)}$	(2.04126, 2.04851)	(-2.03856, -2.03131)	(2.90303, 3.00426)	(4.23250, 4.38216)
$\langle r^{14} \rangle \text{ (} 10^7 \text{ fm}^{14}\text{)}$	(1.55741, 1.56055)	(-1.55921, -1.55608)	(2.15788, 2.2296)	(3.14973, 3.2547)
$\langle r^{16} \rangle \text{ (} 10^9 \text{ fm}^{16}\text{)}$	(1.62407, 1.62627)	(-1.62604, -1.62384)	(2.19083, 2.25977)	(3.19849, 3.2992)
$\langle r^{18} \rangle \text{ (} 10^{11} \text{ fm}^{18}\text{)}$	(2.20993, 2.21213)	(-2.21208, -2.20988)	(2.90451, 2.99138)	(4.24059, 4.36742)
$\langle r^{20} \rangle \text{ (} 10^{13} \text{ fm}^{20}\text{)}$	(3.79638, 3.79932)	(-3.79931, -3.79637)	(4.86668, 5.00572)	(7.1054, 7.30839)

[J. M. Alarcón, C. Weiss, 1710.06430]

- Moments

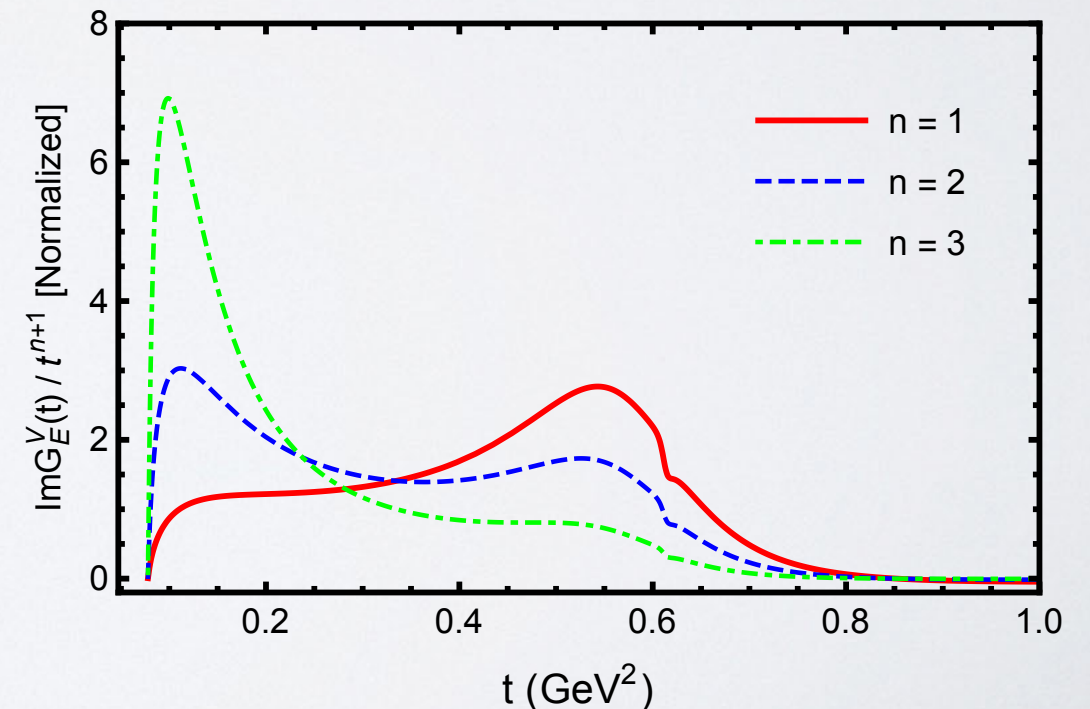
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$\langle r^{14} \rangle$ (10 ⁷ fm ¹⁴)	(1.55741, 1.56055)	(-1.55921, -1.55608)	(2.15788, 2.2296)	(3.14973, 3.2547)
$\langle r^{16} \rangle$ (10 ⁹ fm ¹⁶)	(1.62407, 1.62627)	(-1.62604, -1.62384)	(2.19083, 2.25977)	(3.19849, 3.2992)
$\langle r^{18} \rangle$ (10 ¹¹ fm ¹⁸)	(2.20993, 2.21213)	(-2.21208, -2.20988)	(2.90451, 2.99138)	(4.24059, 4.36742)
$\langle r^{20} \rangle$ (10 ¹³ fm ²⁰)	(3.79638, 3.79932)	(-3.79931, -3.79637)	(4.86668, 5.00572)	(7.1054, 7.30839)

- Higher order moments governed by the near-threshold region

$$\langle r^{2n} \rangle = \frac{(2n+1)!}{\pi} \int_{4M_\pi^2}^{\infty} dt' \frac{\text{Im}G(t')}{t'^{n+1}}$$



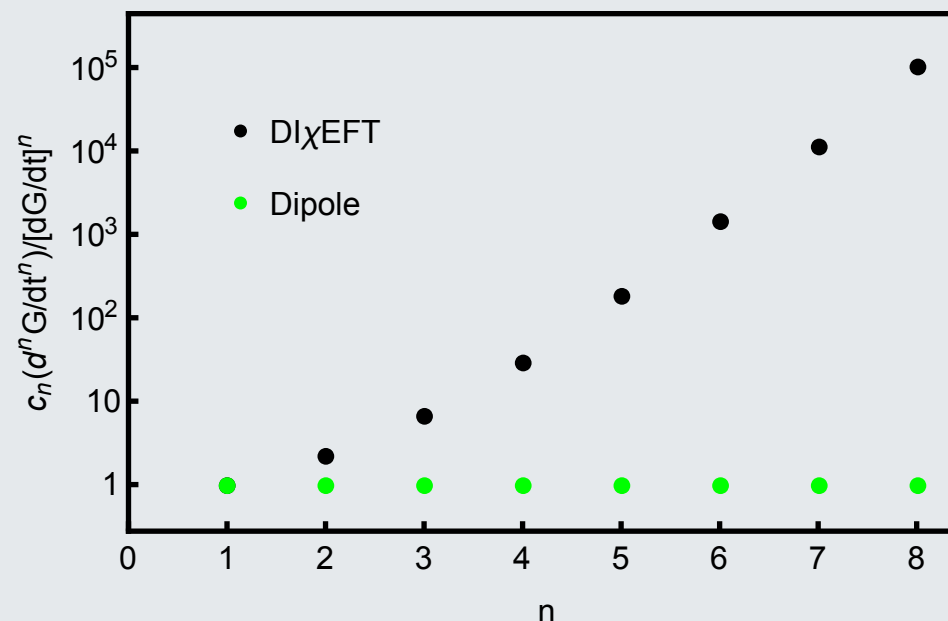
[J. M. Alarcón, C. Weiss, 1710.06430]

- Moments

$$G_E(Q^2) = 1 - \frac{\langle r_E^2 \rangle}{3!} Q^2 + \frac{\langle r_E^4 \rangle}{5!} Q^4 - \frac{\langle r_E^6 \rangle}{7!} Q^6 + \frac{\langle r_E^8 \rangle}{9!} Q^8 + \dots$$

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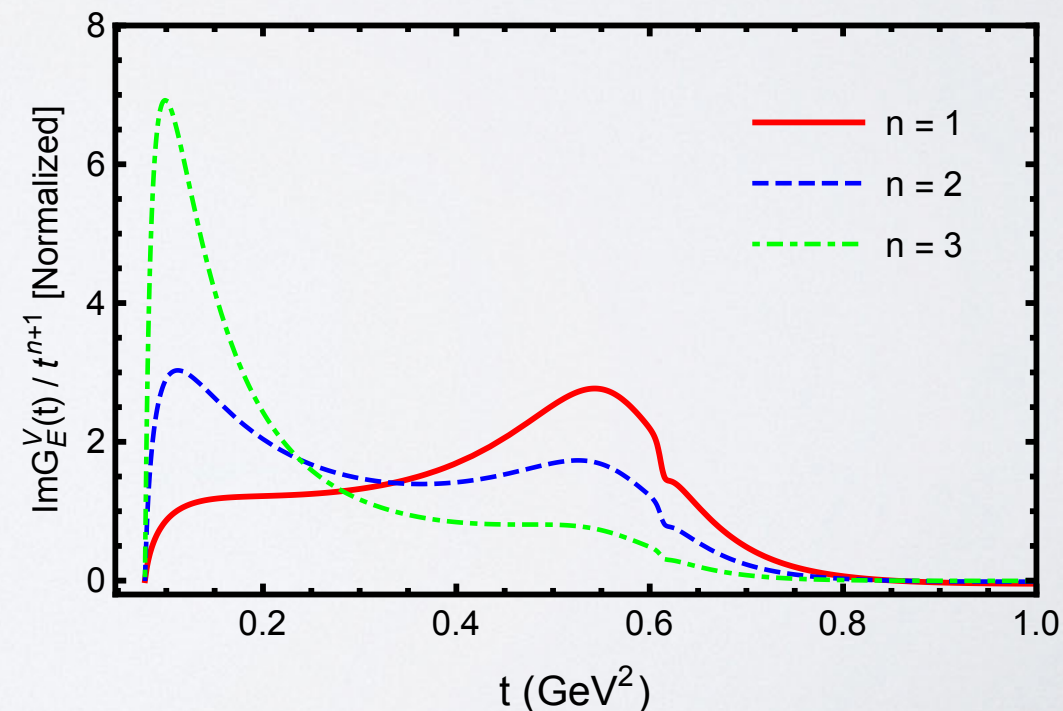
	G_E^p
$\langle r^2 \rangle$ (fm ²)	(0.70059, 0.767638)
$\langle r^4 \rangle$ (fm ⁴)	(1.47274, 1.6019)
$\langle r^6 \rangle$ (fm ⁶)	(8.51876, 8.96183)
$\langle r^8 \rangle$ (10 ² fm ⁸)	(1.26893, 1.29627)
$\langle r^{10} \rangle$ (10 ³ fm ¹⁰)	(3.93325, 3.96482)
$\langle r^{12} \rangle$ (10 ⁵ fm ¹²)	(2.04126, 2.04851)
$\langle r^{14} \rangle$ (10 ⁷ fm ¹⁴)	(1.55741, 1.56055)
$\langle r^{16} \rangle$ (10 ⁹ fm ¹⁶)	(1.62407, 1.62627)
$\langle r^{18} \rangle$ (10 ¹¹ fm ¹⁸)	(2.20993, 2.21213)
$\langle r^{20} \rangle$ (10 ¹³ fm ²⁰)	(3.79638, 3.79932)



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[J. M. Alarcón, C. Weiss, 1710.06430]



Nucleon Densities

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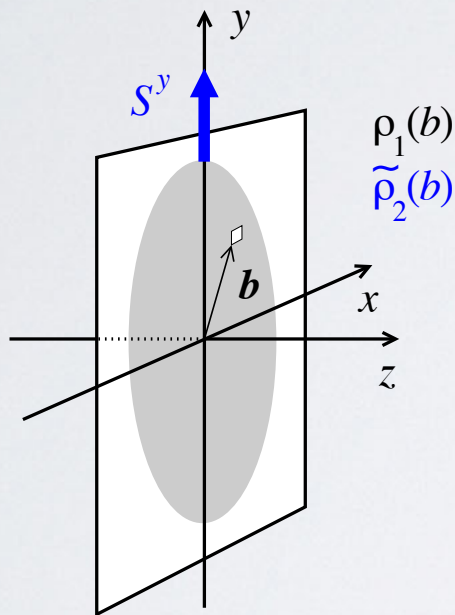
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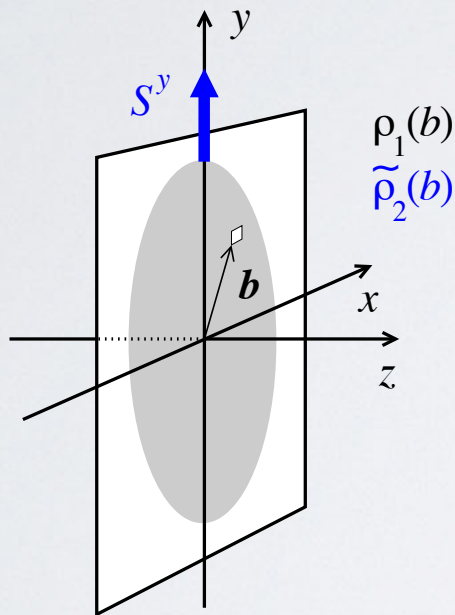
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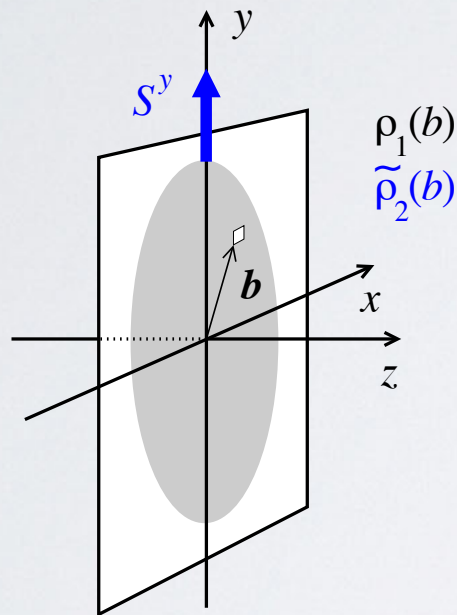
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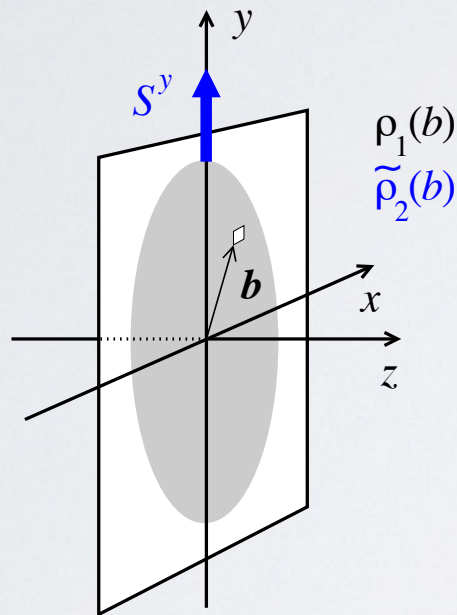
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$$\rho_1(b) = \int_0^\infty d\Delta_T \frac{\Delta_T J_0(\Delta_T b)}{2\pi} F_1^B(t = -\Delta_T^2) = \int_{t_{\text{thr}}}^\infty dt \frac{K_0(\sqrt{t}b)}{2\pi} \frac{\text{Im} F_1^B(t)}{\pi}$$

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- The input necessary to compute the densities can be taken from experimental data (parametrizations) or theory.

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- Densities are more sensitive to near-threshold contributions for

$b > 1 \text{ fm}$:

$$K_{0,1}(\sqrt{tb}) \sim \frac{e^{-\sqrt{tb}}}{(\sqrt{tb})^{1/2}} \quad (\sqrt{tb} \gg 1)$$

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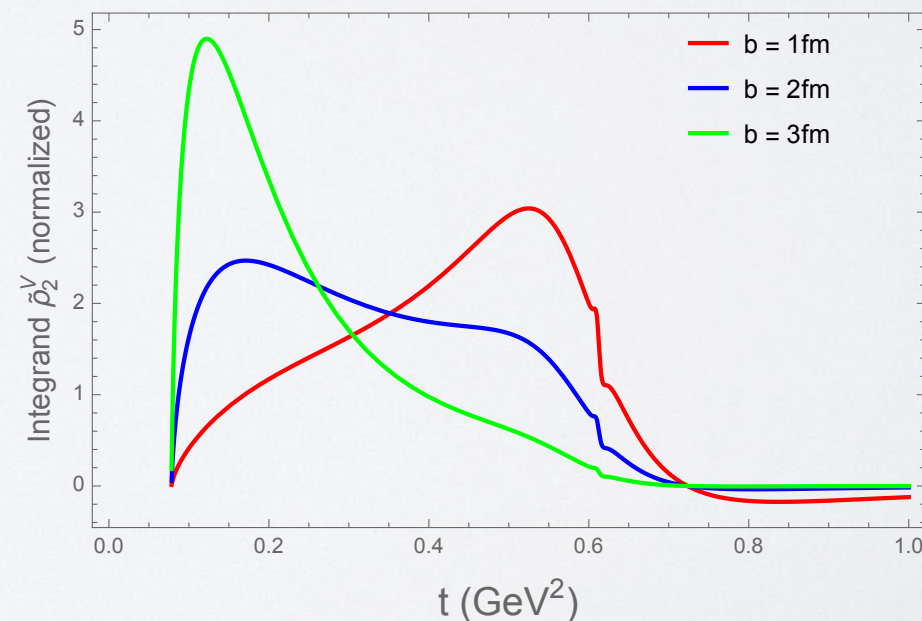
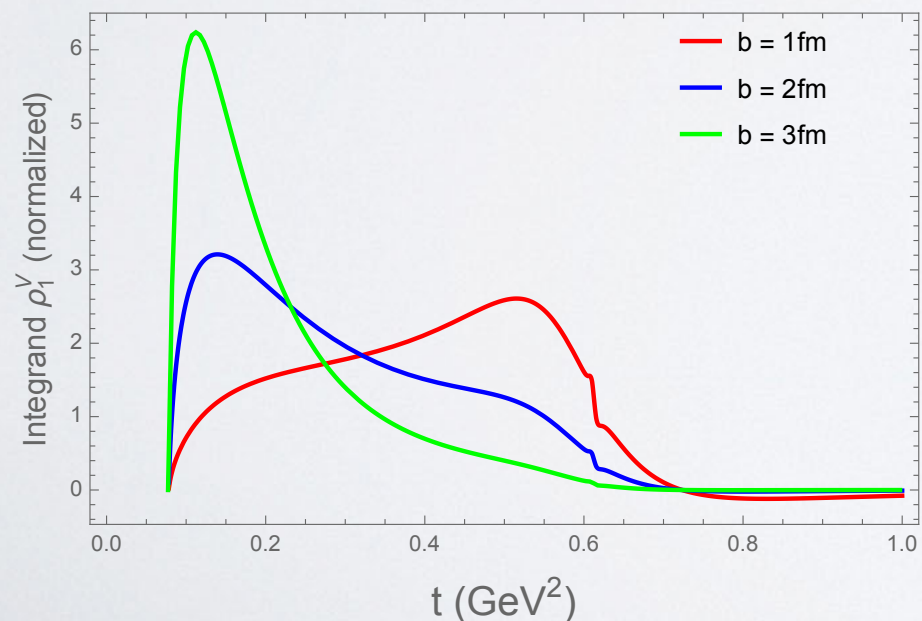
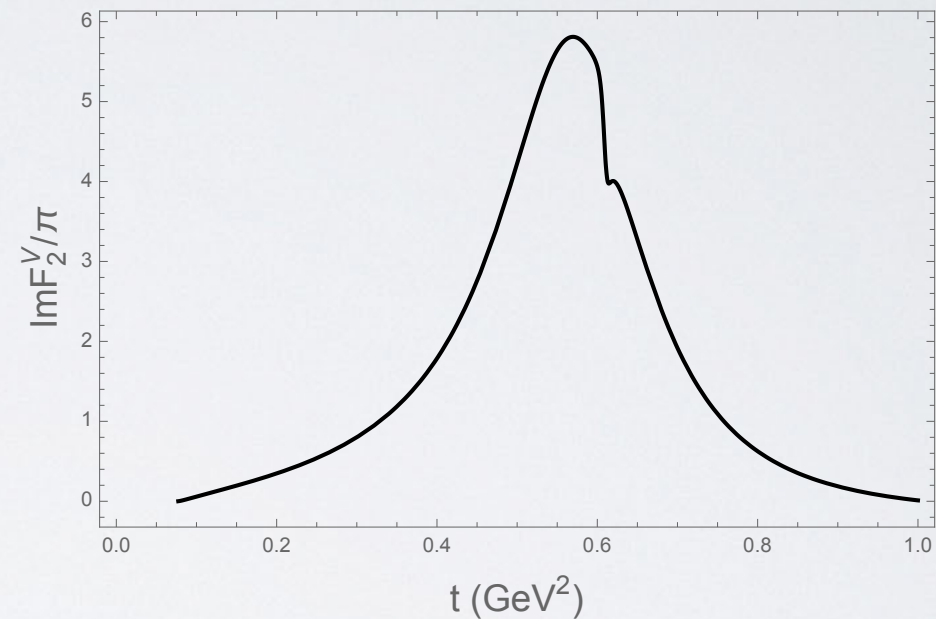
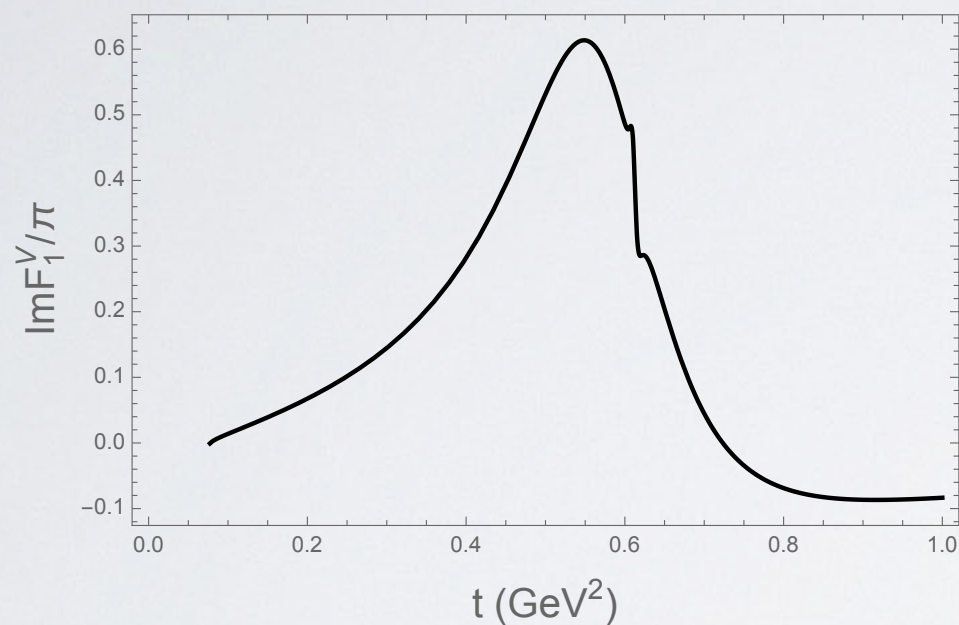
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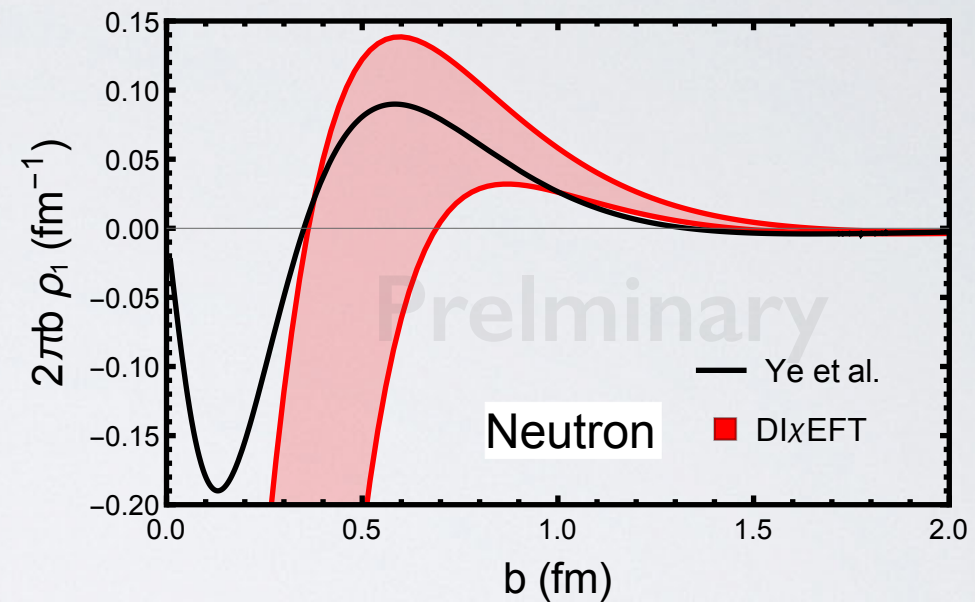
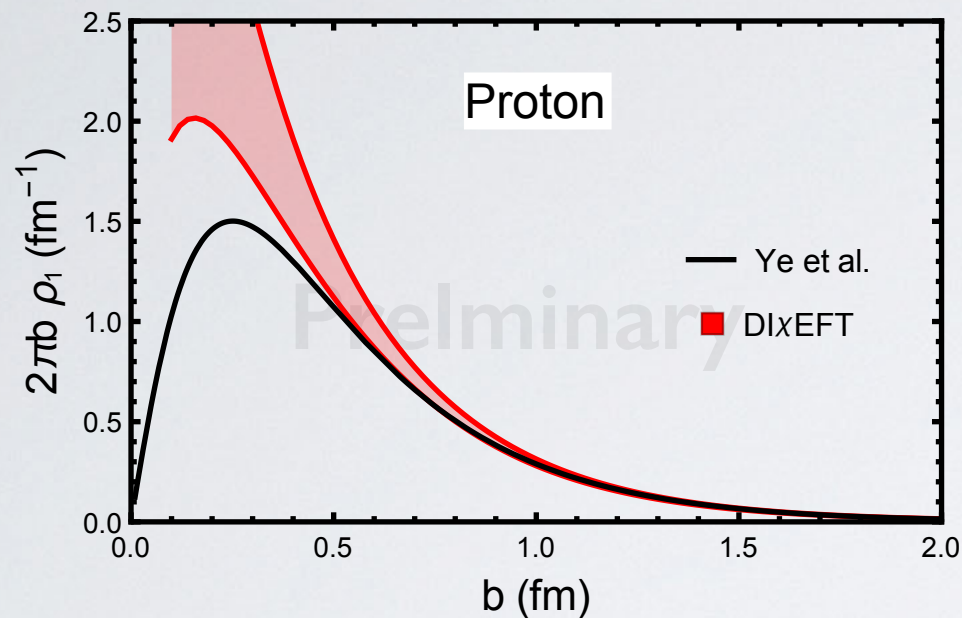
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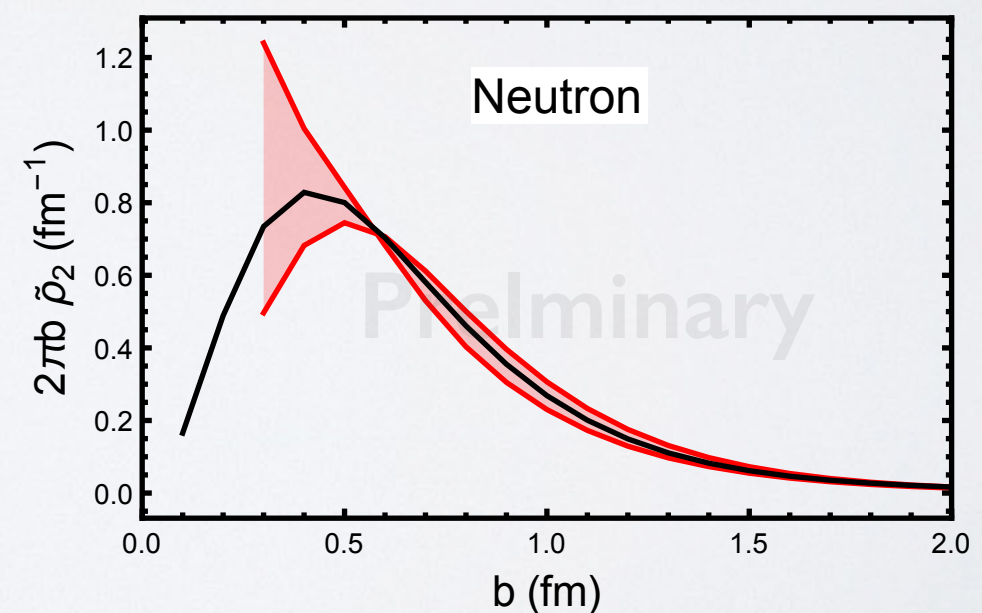
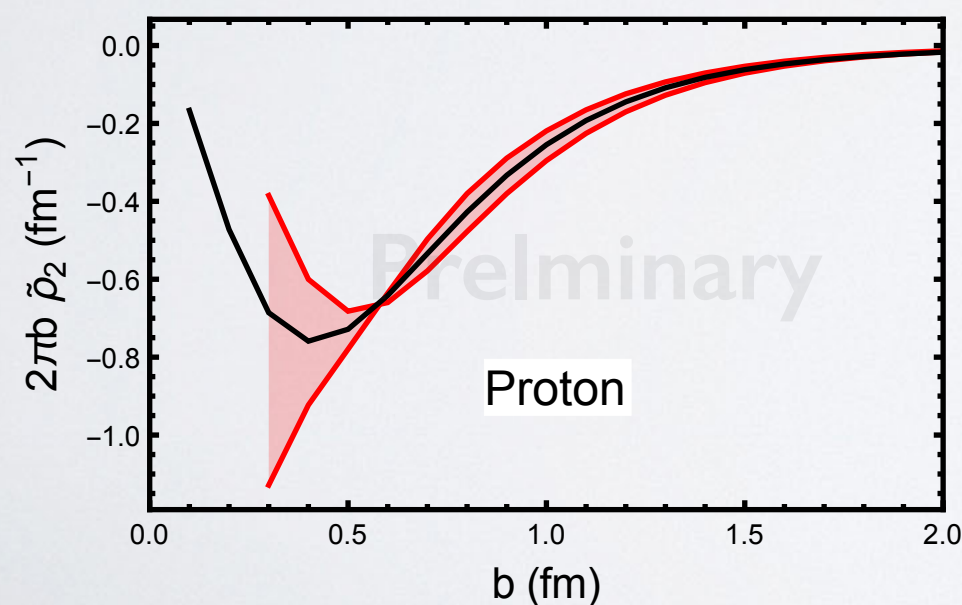


Nucleon Densities

- Charge Densities




- Magnetization Densities



[J. M. Alarcón, C. Weiss, in preparation]

Summary and Conclusions

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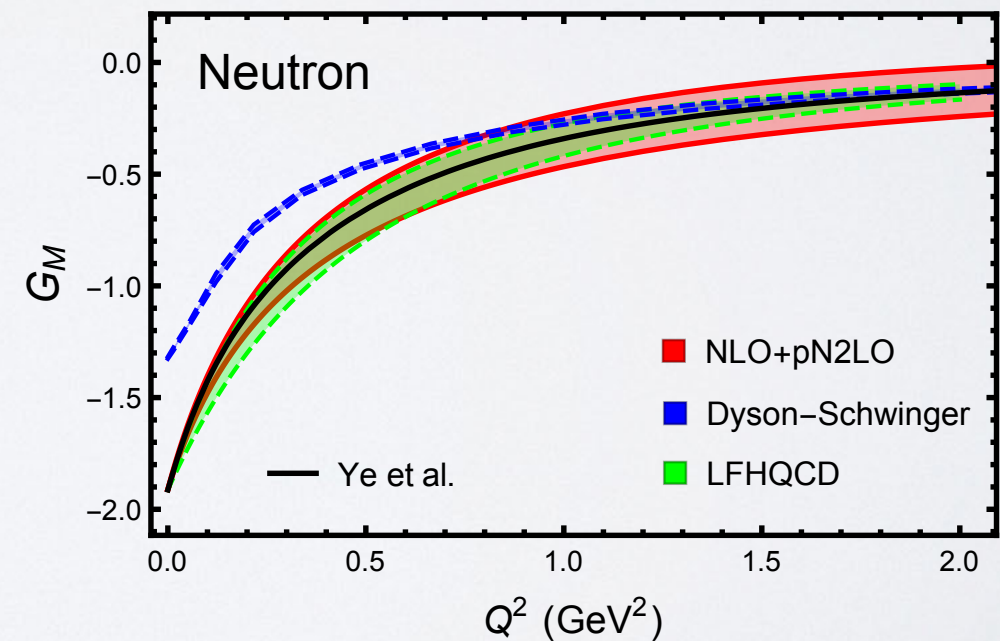
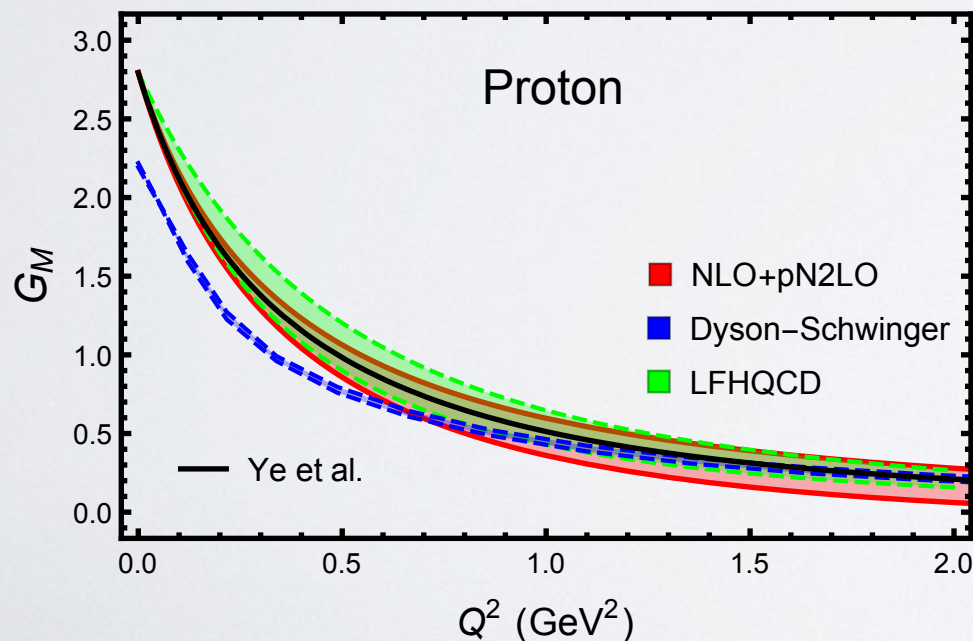
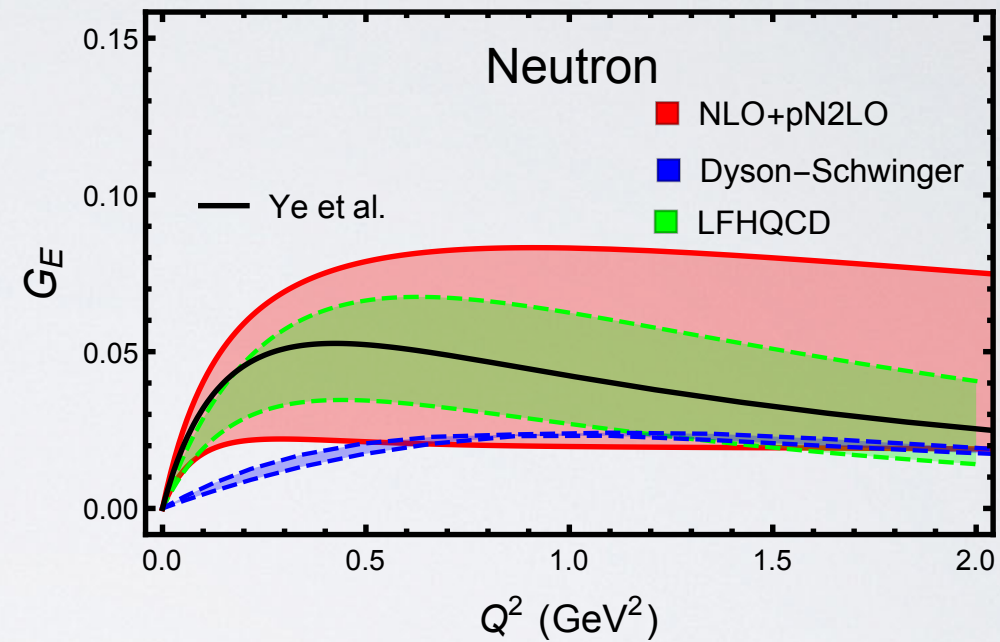
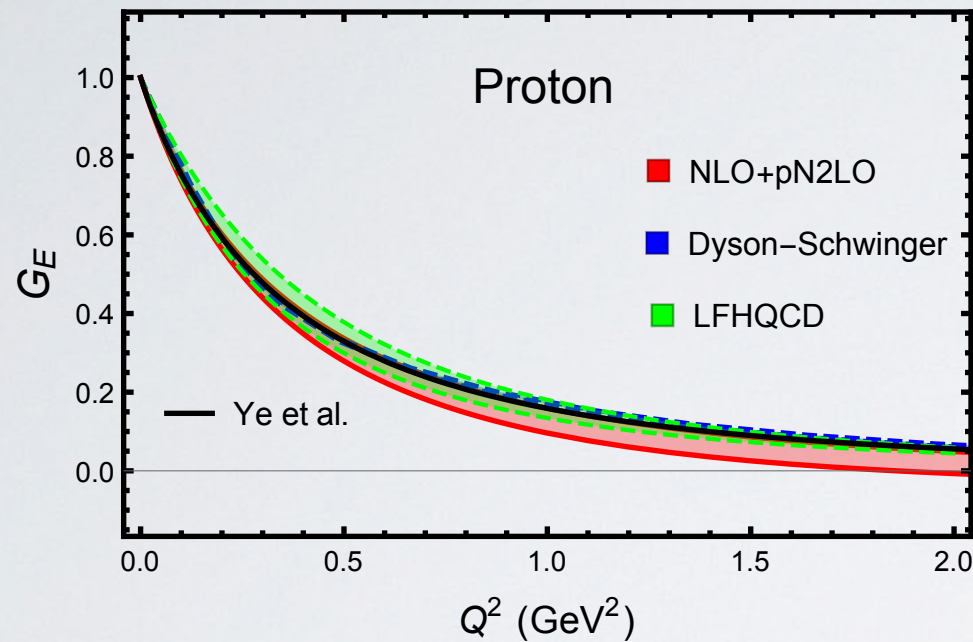
- Through unitarity, it is possible to find a representation suited for ChEFT  **Predictions** of the Nucleon Form factors.
- The results improve previous ChEFT calculations and are competitive with dispersion theory calculations.
- EM FFs have a much complex structure than what it seems.
- D χ EFT implements the constraints that allow to reconstruct the FFs with its full complexity:
 - Analyses of FF data.
 - Two photon exchange corrections to $e-p$ scattering.
- Results used to understand “Proton Radius Puzzle” (PRad).
- Learn about the partonic structure of the nucleon.
- New promising method to compute nucleon matrix elements from first principles (EM tensor, D-term, extension to G-parity odd, ...).

FIN

Spares

DIχEFT

- Reconstructing the form factors with $G_{E,M}^{p,n}(t) = \frac{1}{\pi} \int_{4M_\pi^2}^{\infty} dt' \frac{\text{Im} G_{E,M}^{p,n}(t')}{t' - t - i0^+}$

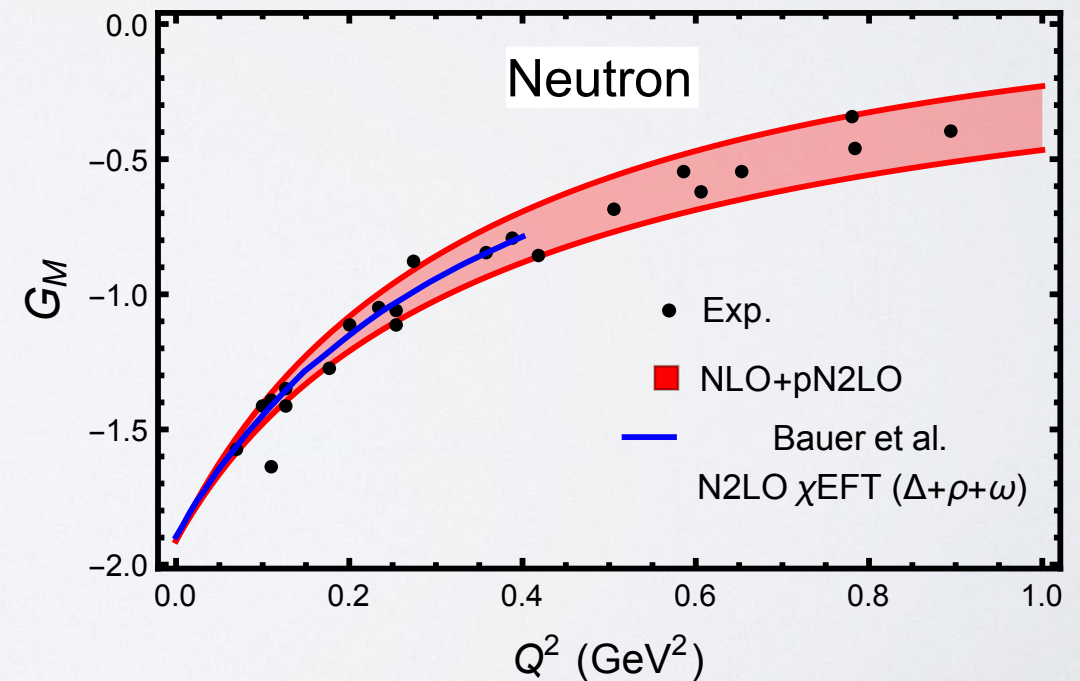
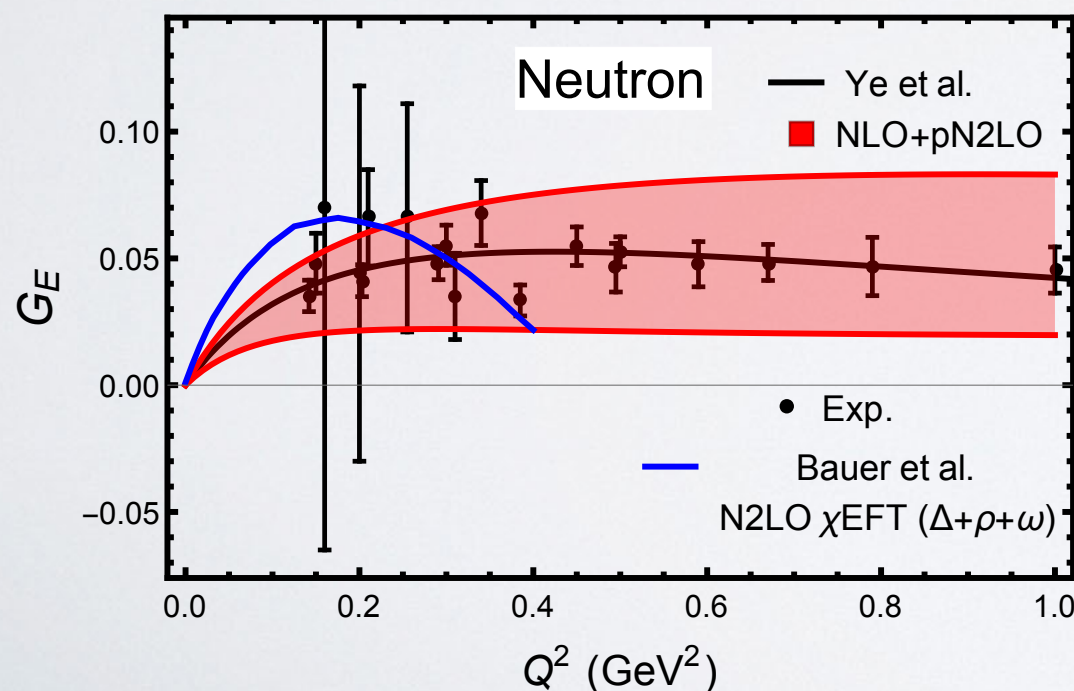
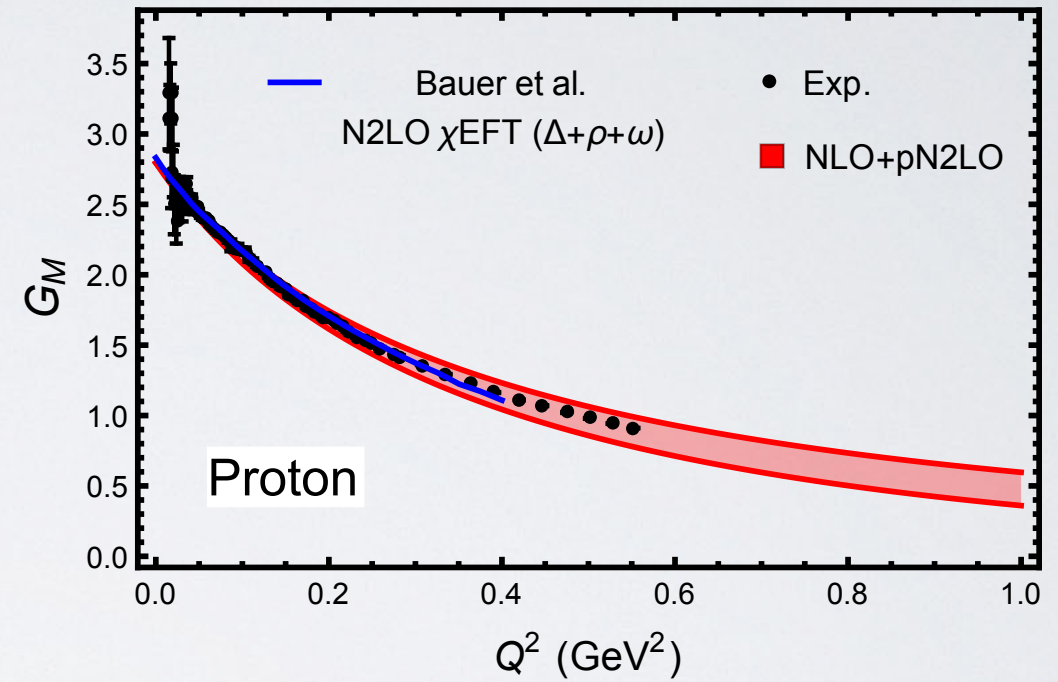
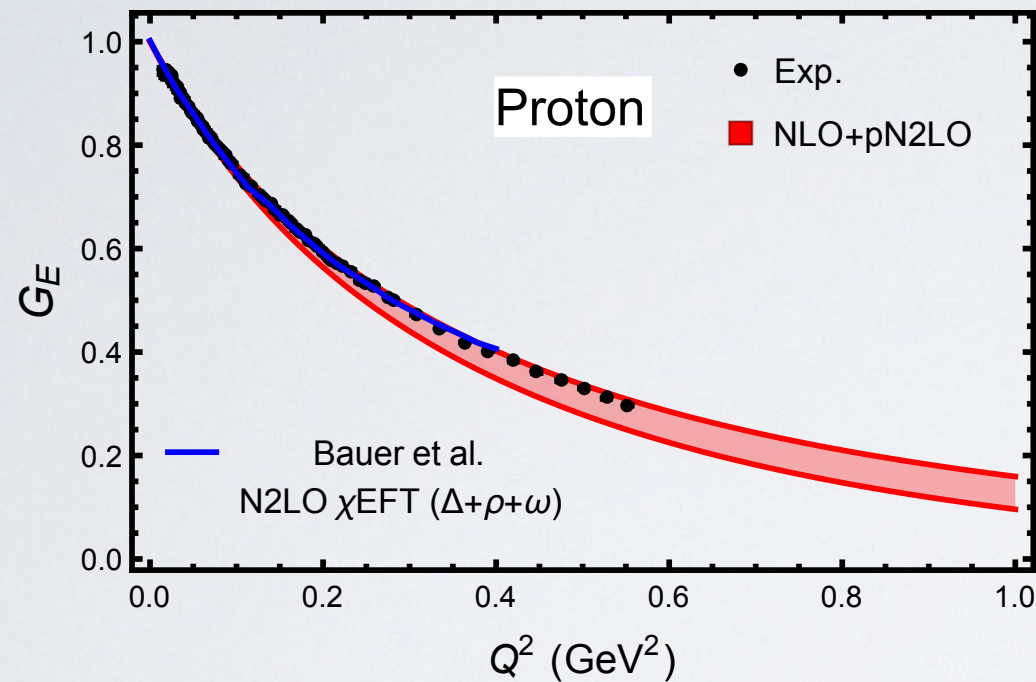


[J. M. Alarcón, C. Weiss, in preparation]

DI χ EFT

- Comparison with respect to the old results

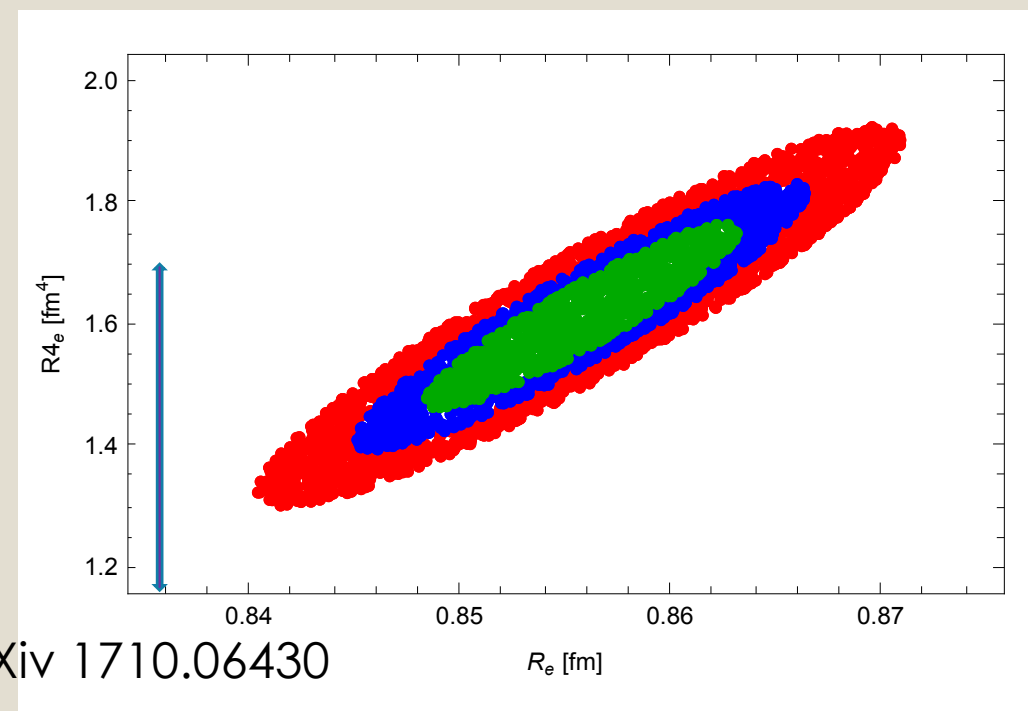
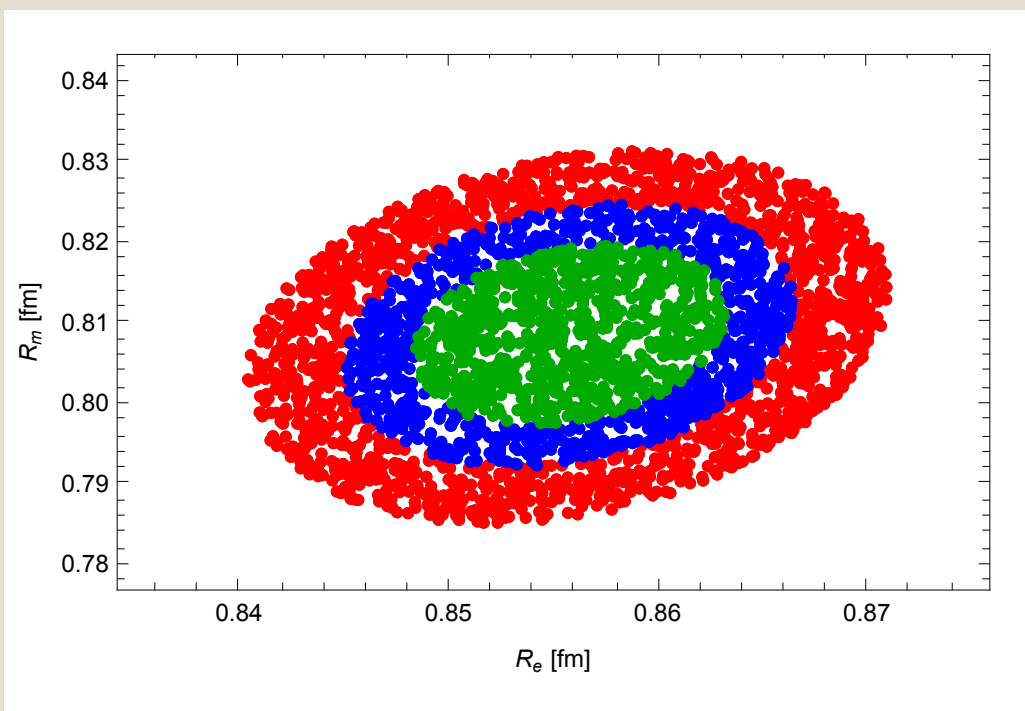
[T. Bauer, J. Bernauer, S. Scherer, PRC 86 (2012)]



D χ EFT

Talk by Marko Horbatsch (JLab, 12/8/2017)

$(Q_{\text{max}}^2 = 0.2 \text{ GeV}^2) \chi_{\text{red}}^2$: green < 1.08, blue < 1.10, red < 1.14



J.A & C.W arXiv 1710.06430

Is lowest reduced chi-squared χ_{red}^2 the answer?

If not, why not?

Are there systematic problems with the MAMI data?

Clearly: P&P prediction 0.6(3) = No Go

I. Sick & D. Trautmann: 2.01(5) PRC 2017

M. Distler: 2.6 fm⁴

Note the R_e vs $\langle r^4 \rangle_e$ correlation !!

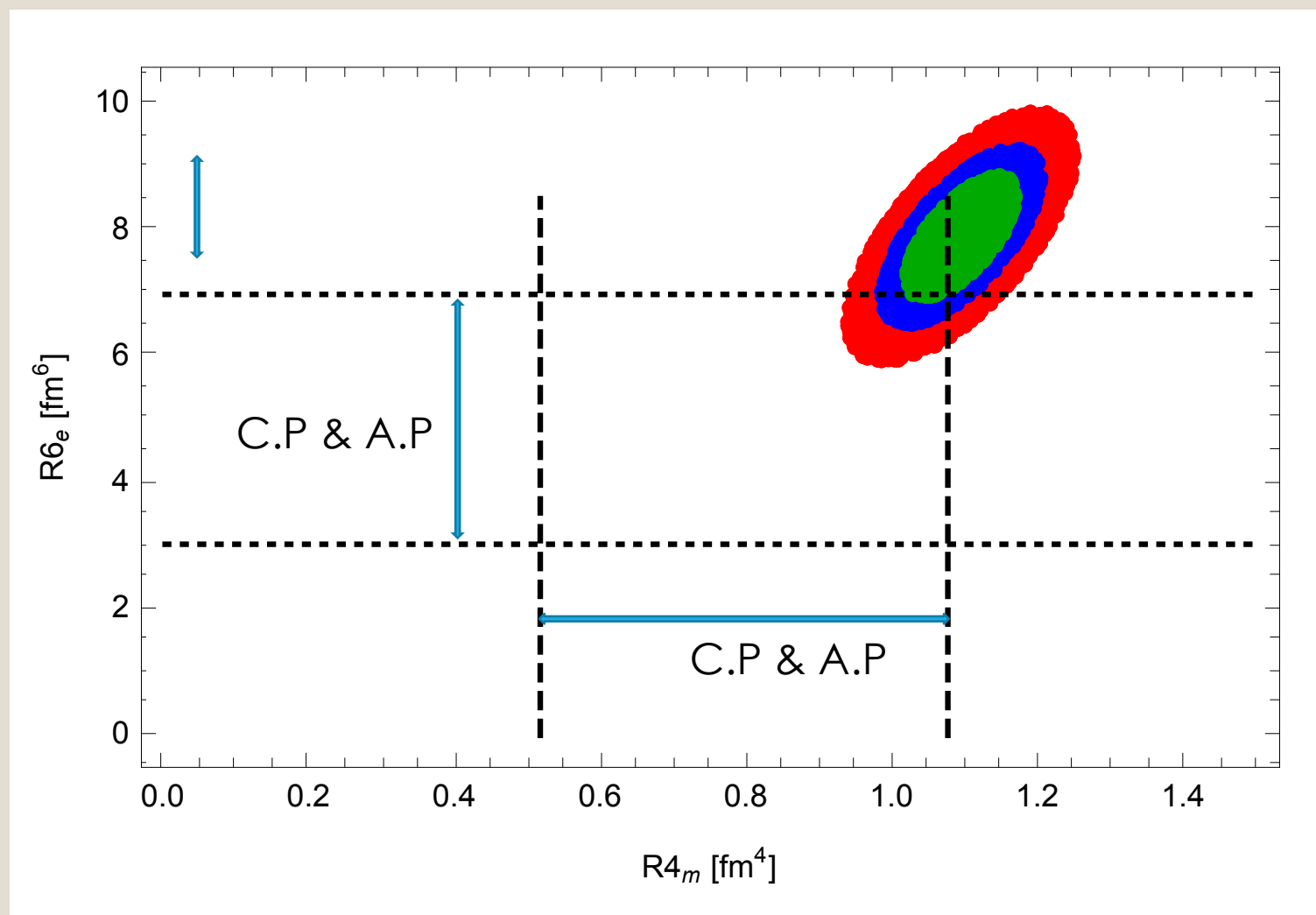
(Courtesy of Marko Horbatsch)

D χ EFT

Talk by Marko Horbatsch (JLab, 12/8/2017)

Is it consistent for the higher moments ?

J.A & C.W arXiv 1710.06430



(Courtesy of Marko Horbatsch)

DI χ EFT

- We study the naturalness of the isovector moments by defining:

$$a_n = \frac{\langle r^{2n} \rangle^V}{(2n+1)!} = \frac{1}{\pi} \int_{4M_\pi^2}^{\infty} dt' \frac{\text{Im} G^V(t')}{t'^{n+1}}$$

- If the integral were dominated by a certain region t' , the ratio $\frac{a_{n+1}}{a_n}$ would be given by the average of $1/t'$ over this region.

