

Wide-angle photoproduction of pions

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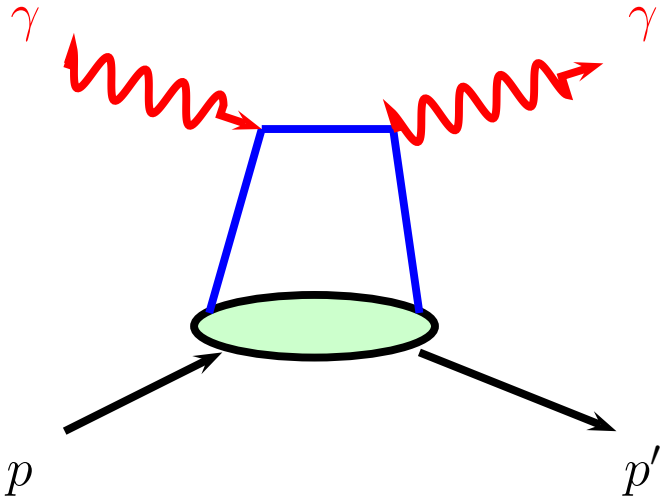
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Jefferson lab., June 2018

Outline:

- The Handbag factorization for wide-angle processes
- Wide-angle Compton scattering
- Wide-angle photoproduction of pions
- The twist-3 contribution to photoproduction
- Results
- The 2-particle twist-3 DAs
- Summary

The handbag factorization



factorization in a hard subprocess, e.g. $\gamma q \rightarrow \gamma q$, and a soft proton matrix element, parameterized as a

General Parton Distribution

$$\langle p' \lambda' | \bar{\Psi}_q(-\bar{z}/2) \Gamma \Psi_q(\bar{z}/2) | p \lambda \rangle_{z^+ = z_\perp = 0}$$

$$(\Gamma = \gamma^+, \gamma^+ \gamma_5, i\sigma^{+i}, A^+ = 0)$$

two classes of hard exclusive reactions:

DEEP VIRTUAL

e.g. DVCS or electroproduction of mesons

rigorous proof for factorization in **generalized Bjorken regime** of

$$\text{large } Q^2 \text{ and } W \text{ but fixed } x_B \text{ and } -t/Q^2 \ll 1$$

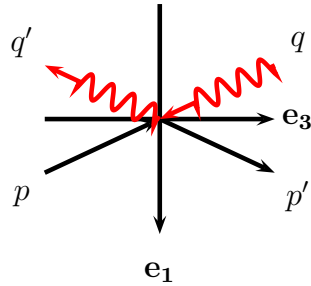
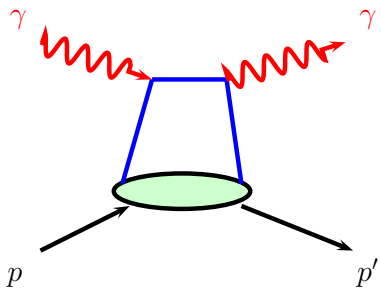
WIDE-ANGLE

e.g. RCS or photoproduction of mesons

arguments for factorization at large Mandelstam variables $s, -t, -u$

complementary: GPDs at small $-t$ in deep virtual and
GPDs at large $-t$ in wide-angle processes

The handbag contribution to WACS (and WAPP)



$$s, -t, -u \gg \Lambda^2$$

$$\Lambda \sim \mathcal{O}(1\text{GeV})$$

typical hadronic scale

- work in a symmetric frame: (otherwise additional contr.)

$$p^{(\prime)} = [p^+, \frac{m^2 - t/4}{2p^+}, \pm \Delta_{\perp}] \quad \xi = \frac{(p-p')^+}{(p+p')^+} = 0 \quad t = -\Delta_{\perp}^2$$

- assumption:

parton virtualities $k_i^2 < \Lambda^2$, intrinsic transverse momenta $k_{\perp i}^2/x_i < \Lambda^2$

- consequences propagators poles avoided

$$\hat{s} = (k_j + q)^2 \simeq (p + q)^2 = s \quad \text{active partons approximately on-shell}$$

$$\hat{u} = (k'_j - q)^2 \simeq (p' - q)^2 = u \quad \text{collinear with parent hadrons}$$

$$\text{and } x_j, x'_j \simeq 1$$

- physical situation: hard photon-parton scattering and soft emission and reabsorption of partons by hadrons

The Compton amplitudes

Radyushkin hep-ph/9803316; DFJK hep-ph/9811253; Huang-K.-Morii hep-ph/0110208

(light-cone helicities)

$$\mathcal{M}_{\mu'+, \mu+} = 2\pi\alpha_{\text{elm}} \left\{ \mathcal{H}_{\mu'+, \mu+}^{\gamma} [R_V^{\gamma} + R_A^{\gamma}] + \mathcal{H}_{\mu'-, \mu-}^{\gamma} [R_V^{\gamma} - R_A^{\gamma}] \right\}$$

$$\mathcal{M}_{\mu'-, \mu+} = \pi\alpha_{\text{elm}} \frac{\sqrt{-t}}{m} \left\{ \mathcal{H}_{\mu'+, \mu+}^{\gamma} + \mathcal{H}_{\mu'-, \mu-}^{\gamma} \right\} R_T^{\gamma}$$

form factors: $R_i^{\gamma}(t) = \sum_q e_q^2 R_i^q(t)$

$$R_V^q = \int_0^1 \frac{dx}{x} H^{qv}(x, \xi = 0, t) \quad E^{qv} \rightarrow R_T^q \quad \tilde{H}^{qv} \rightarrow R_A^q$$

\tilde{E} decouples at $\xi = 0$; $H^{qv} = H^q - H^{\bar{q}}$ (sea quarks neglected)

subprocess amplitudes: $\mathcal{H}_{++++} = 2\sqrt{-s/u}$
 $\mathcal{H}_{-+-+} = 2\sqrt{-u/s}$ (+ NLO)

Analysis of nucleon form factors

need for Compton ffs, i.e. need for GPDs at large $-t$
 deeply virtual processes provide GPDs only at small $-t$
 but large $-t$ GPDs from **nucleon ffs** through sum rules:

$$F_i^{p(n)} = e_u F_i^{u(d)} + e_d F_i^{d(u)}, \quad F_i^a = \int_0^1 dx K_v^a(x, \xi = 0, t)$$

Dirac (Pauli) ff: $K = H(E)$ (normalization from $\kappa_q = \int_0^1 dx E_v^q(x, \xi = t = 0)$)

axial form factor: \tilde{H} (κ anomalous magn. moment)

ansatz $K_i^a(x, \xi = 0, t) = k_i^a(x) \exp [t f_i^a(x)]$

profile fct: $f_i^a = (B_i^a + \alpha_i'^a \ln 1/x)(1-x)^3 + A_i^a x(1-x)^2$

forward limits $H : q(x) \quad \tilde{H} : \Delta q(x)$

$E: e_i = N_i x^{\alpha_i} (1-x)^{\beta_i}$ additional parameters

DFJK [hep-ph/0408173](#); update: Diehl-K, [1302.4604](#); (see also Guidal et al, [hep-ph/0410252](#))

fit to all data: $G_M^i, G_E^i / G_M^i$ ($i = p, n$) and

use of [ABM11](#), [DSSV09](#) parton densities

strong $x - t$ correlation

(see also de Teramond et al ([1801.09154](#)))

Estimate of proton radius

Approx: distance between active parton and cluster of spectators

work in hadron's center of momentum frame

$$\sum x_i \mathbf{b}_i = 0$$

Fourier transform of H

$$q(x, \mathbf{b}) = \frac{1}{4\pi} \frac{q(x)}{f_q(x)} \exp[-b^2 / (4f_q(x))]$$

$$d_q(x) = \frac{\sqrt{\langle b^2 \rangle_x^q}}{1-x} = \frac{2\sqrt{f_q(x)}}{1-x} \rightarrow 2\sqrt{A_q}$$

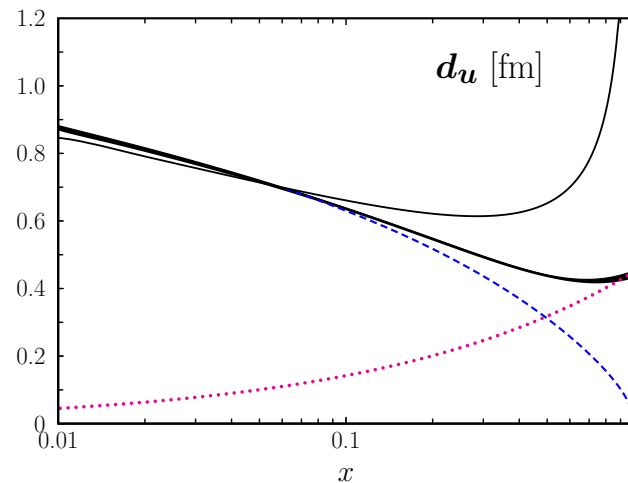
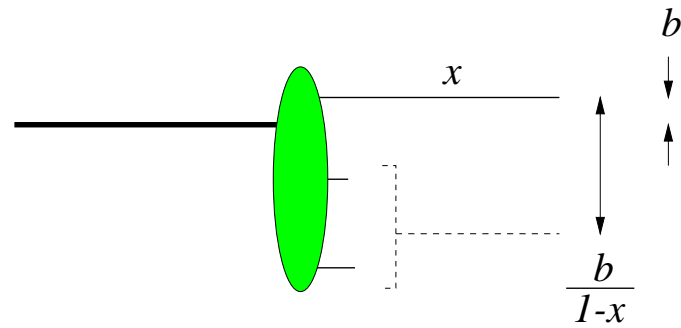
for $x \rightarrow 1$

Regge-type term, **A term**, full profile fct

Regge-like profile fct can (only) be used

at small x (small $-t$)

(Regge-like: $A = 0$ and $(1-x)^3 \rightarrow 1$)

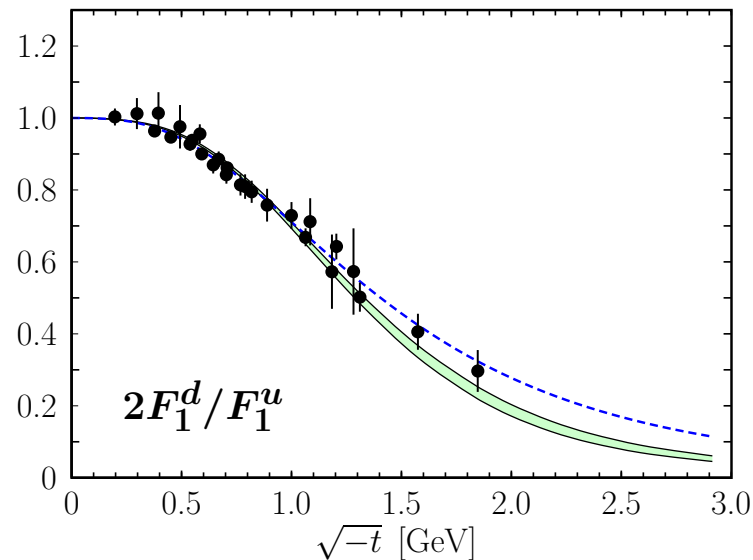


Large- t behavior of flavor form factors

at large t : dominance of narrow region of large x :

$$q_v \sim (1-x)^{\beta_q}, f_q \sim A_q(1-x)^2 \quad (\text{analogously for } F_2^q)$$

$$\text{Saddle point method provides } 1-x_s = \left(\frac{2}{\beta_q} A_q |t| \right)^{-1/2} \quad F_1^q \sim |t|^{-(1+\beta_q)/2}$$

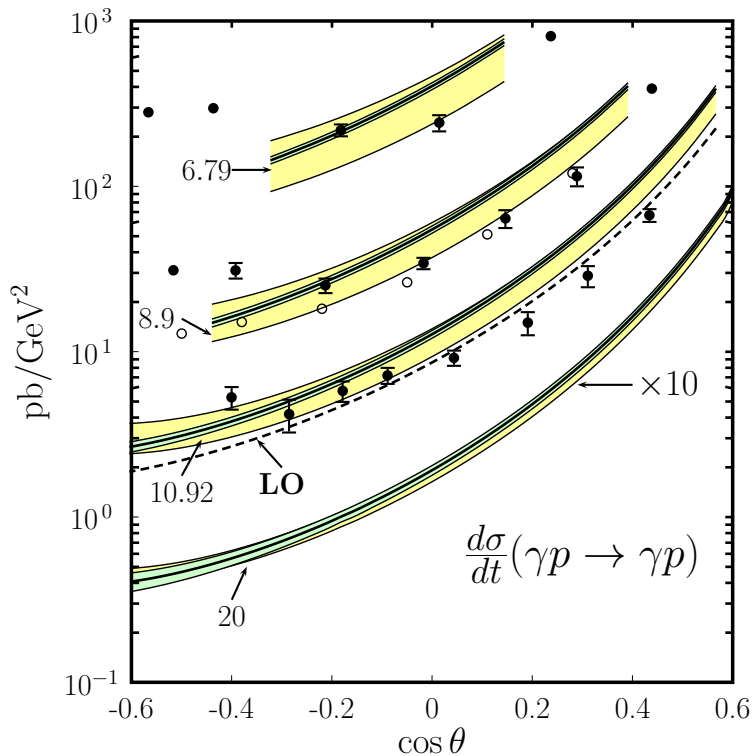


$$\text{ABM PDFs: } \beta_u \simeq 3.4, \beta_d \simeq 5,$$

power laws from wave fct overlaps: [Dagaonkar-Jain-Ralston \(14\)](#)

power laws are a necessary but not sufficient signal of perturbative physics

The Compton cross section



$$\frac{d\sigma}{dt} = \frac{d\hat{\sigma}}{dt} \left\{ \frac{1}{2} \frac{(s-u)^2}{s^2+u^2} \left[R_V^2(t) + \frac{-t}{4m^2} R_T^2(t) \right] + \frac{1}{2} \frac{t^2}{s^2+u^2} R_A^2(t) \right\} + \mathcal{O}(\alpha_s)$$

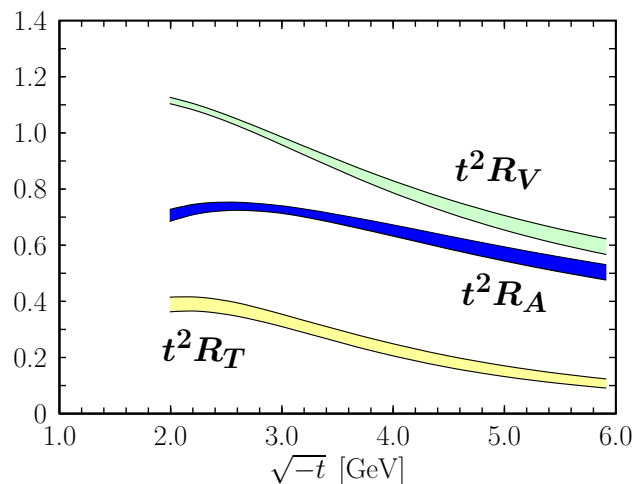
$$\frac{d\hat{\sigma}}{dt} = 2\pi \frac{\alpha_{\text{elm}}^2}{s^2} \left[-\frac{u}{s} - \frac{s}{u} \right]$$

Klein-Nishina cross section

$$-t, -u > 2.5 \text{ GeV}^2$$

data: [JLab E99-114](#)

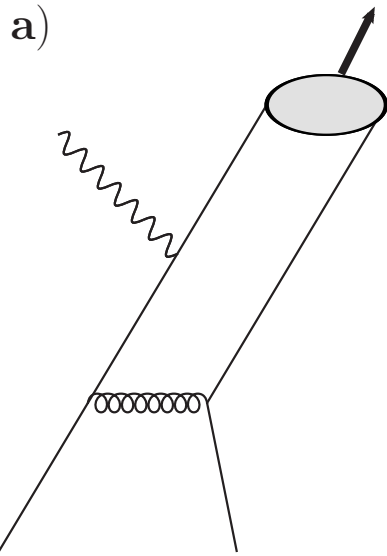
form factors from $\xi = 0$ analysis



Photoproduction of pions

arguments for handbag factorization as for WACS

$$s, -t, -u \ll \Lambda^2$$



leading-twist contribution

$$\mathcal{M}_{0+\mu+}^{\pi} = \frac{e_0}{2} \sum_{\lambda} \mathcal{H}_{0\lambda\mu\lambda}^{\pi} [R_V^{\pi} + 2\lambda R_A^{\pi}]$$

$$\mathcal{M}_{0-\mu+}^{\pi} = \frac{e_0}{2} \sum_{\lambda} \frac{\sqrt{-t'}}{2m} \mathcal{H}_{0+\mu+}^{\pi} R_T^{\pi}$$

$$R_i^{\pi^0} = \frac{1}{\sqrt{2}} [e_u R_i^u - e_d R_i^d]$$

$$R_i^{\pi^+} = R_i^{\pi^-} = R_i^u - R_i^d$$

same flavor form factors as for WACS

twist-2 subprocess amplitude

known, universality

$$(\langle 1/\tau \rangle_{\pi} = \int d\tau / \tau \Phi_{\pi}(\tau))$$

$$\mathcal{H}_{0\lambda\mu\lambda}^{\pi^0} = 2\pi\alpha_s f_{\pi} \frac{C_F}{N_C} \langle 1/\tau \rangle_{\pi} \sqrt{-t/2} \frac{(1+\mu)s - (1-\mu)u}{su}$$

cross section too small by factor 50 - 100

Huang-K., hep-ph/0005318

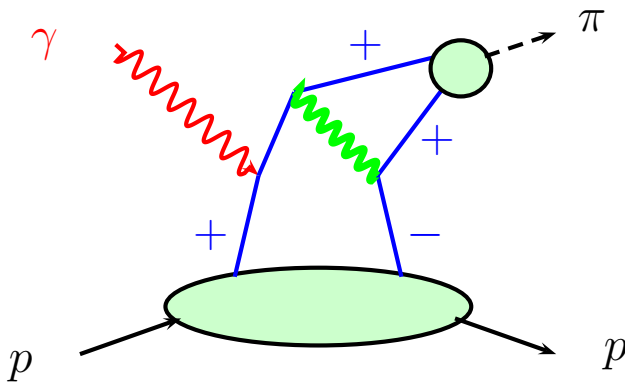
Photoproduction: Transversity GPDs?

Huang-Jakob-K-Passek-Kumericki, hep-ph/0309071

$H_T, E_T, \tilde{H}_T, \tilde{E}_T$

transversity GPDs go along with
twist-3 pion wave functions

fed subprocess ampl. $\mathcal{H}_{0-\mu+}$ and $\mathcal{H}_{0+\mu-}$



projector $q\bar{q} \rightarrow \pi$ (3-part. $q\bar{q}g$ contr. neglected)

Beneke-Feldmann (01)

$$\sim q' \cdot \gamma \gamma_5 \Phi + \mu_\pi \gamma_5 \left[\Phi_P - i\sigma_{\mu\nu} \left(\frac{q'^\mu k'^\nu}{q' \cdot k'} \frac{\Phi'_\sigma}{6} + q'^\mu \frac{\Phi_\sigma}{6} \frac{\partial}{\partial \mathbf{k}_{\perp\nu}} \right) \right]$$

definition: $\langle \pi^+(q') | \bar{d}(x) \gamma_5 u(-x) | 0 \rangle = i f_\pi \mu_\pi \int d\tau e^{iq'x\tau} \Phi_P(\tau)$

local limit $x \rightarrow 0$ related to divergency of axial vector current

$$\implies \mu_\pi = m_\pi^2 / (m_u + m_d) \simeq 2 \text{ GeV at scale } 2 \text{ GeV} \quad \left(\int d\tau \Phi_P(\tau) = 1 \right)$$

Eq. of motion: $\tau \Phi_P = \Phi_\sigma / N_c - \tau \Phi'_\sigma / (2N_c)$

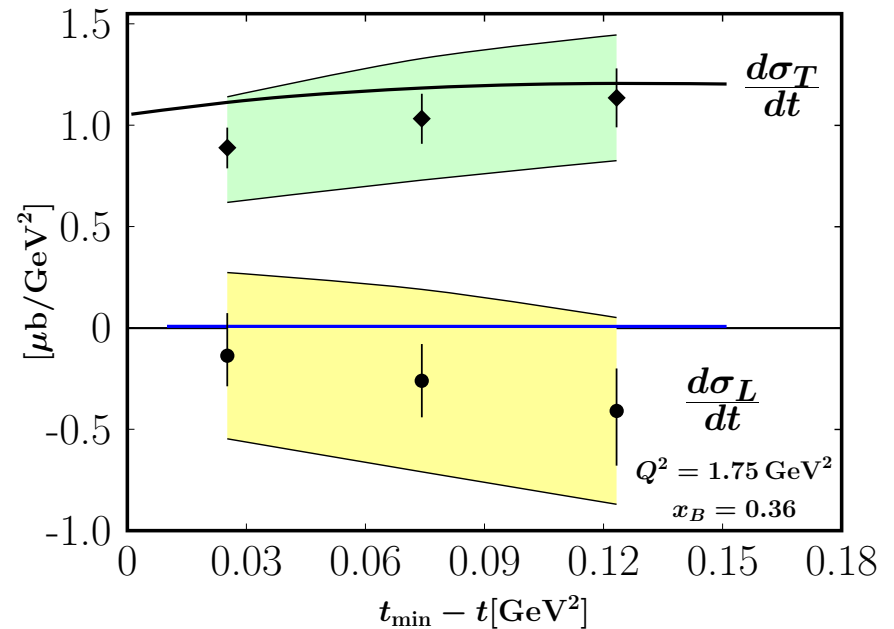
solution: $\Phi_P = 1, \quad \Phi_\sigma = \Phi_{AS} = 6\tau(1 - \tau)$ Braun-Filyanov (90)

(WW approx.)

$$\implies \mathcal{H}_{0-\mu+} = \mathcal{H}_{0+\mu-} = 0$$

to be contrasted with electroproduction of pions:

- the subprocess amplitudes in WW appr. are non-zero
- contribute to transversely polarized photons
- dominate the cross section for π^0 production
- in agreement with experiment



Defurne et al (1608.01003)

π^0 production off protons

curves: Goloskokov-K (1106.4897)

$Q^2 \rightarrow \infty : d\sigma_L \gg d\sigma_T$

Pion photoproduction again

K.-Passek-Kumericki, (1802.06597)

In view of situation in electroproduction:

include **full twist-3** contribution ($q\bar{q} + q\bar{q}g$ Fock components of the pion)

both are needed in order to achieve gauge invariance

they are related by eq. of motion (with light-cone gauge $A^+ = 0$):

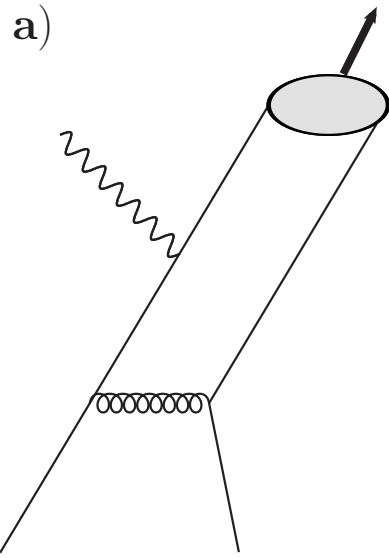
$$\bar{\tau}\Phi_p - \frac{1}{6}\bar{\tau}\Phi'_\sigma - \frac{1}{3}\Phi_\sigma = 2\frac{f_{3\pi}}{f_\pi\mu_\pi} \int_0^\tau \frac{d\tau_g}{\tau_g} \Phi_{3\pi}(\tau - \tau_g, \bar{\tau}, \tau_g) = \Phi_1^{EOM}(\tau)$$

$$\tau\Phi_p + \frac{1}{6}\tau\Phi'_\sigma - \frac{1}{3}\Phi_\sigma = 2\frac{f_{3\pi}}{f_\pi\mu_\pi} \int_0^{\bar{\tau}} \frac{d\tau_g}{\tau_g} \Phi_{3\pi}(\tau, \bar{\tau} - \tau_g, \tau_g) = \Phi_2^{EOM}(\tau)$$

for pions: $\Phi_1^{EOM}(\tau) = \Phi_2^{EOM}(\bar{\tau})$

$$f_{3\pi} = f_{3\pi}(\mu_R^2) \quad \mu_\pi = \mu_\pi(\mu_R^2)$$

The 2-particle twist-3 contribution



amplitude for $\gamma q \rightarrow \pi^0 q$

$$\begin{aligned} \mathcal{H}_{0-\lambda, \mu\lambda}^{twist-3, 2-particle} &= 4\pi\alpha_s f_\pi \mu_\pi \frac{C_F}{N_C} \\ &\times \frac{\sqrt{-us}}{\sqrt{2s^2u^2}} \int_0^1 d\tau \phi_2^{EOM}(\tau) \left[\mu \frac{ts}{\tau(1-\tau)} \right. \\ &\left. + \left(\frac{2\lambda - \mu}{2(1-\tau)^2} + \frac{2\lambda + \mu}{2\tau(1-\tau)} \right) (s^2 + u^2) \right] \end{aligned}$$

Huang-Jakob-K-Passek-Kumericki, hep-ph/0309071

(Φ_P and Φ_σ always appear in combinations Φ_i^{EOM})

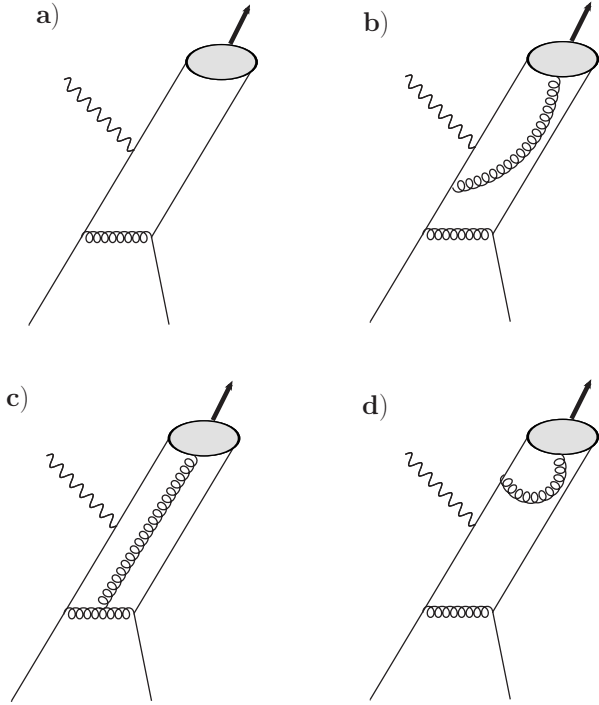
gauge invariant in QCD but **not** in QED

violates $s - u$ crossing symmetry

(Chew-Goldberger-Low-Nambu (57))

need also 3-particle twist-3 contribution

The 3-particle twist-3 contribution



$$\begin{aligned}
 \mathcal{H}_{0-\lambda, \mu\lambda}^{twist-3, 3-particle} &= 4\pi\alpha_s f_{3\pi} \frac{C_F}{N_C} \frac{\sqrt{-us}}{\sqrt{2s^2u^2}} \\
 &\times \int_0^1 d\tau \int_0^{1-\tau} \frac{d\tau_g}{\tau_g} \Phi_{3\pi}(\tau, 1-\tau-\tau_g, \tau_g) \\
 &\times \left\{ (2\lambda - \mu) \left[\left(\frac{1}{1-\tau} - \frac{1}{1-\tau-\tau_g} \right) \frac{s^2 + u^2}{\tau_g} \right. \right. \\
 &\quad \left. \left. + \left(1 - \frac{1}{2} \frac{C_A}{C_F} \right) \left(\frac{1}{\tau} + \frac{1}{1-\tau-\tau_g} \right) \frac{t^2}{\tau_g} \right] \right. \\
 &\quad \left. - \frac{2\lambda + \mu}{\tau(1-\tau)} (s^2 + u^2) - 2\mu \frac{st}{\tau(1-\tau)} \right\}
 \end{aligned}$$

d) soft, part of DA

gauge invariant in QCD but **not** in QED

$s - u$ crossing symmetry violated

twist-3 3-particle projector ($q\bar{q}g \rightarrow \pi$)

$$\mathcal{P}_{3,fg}^{\beta,c} = \frac{i}{g} \frac{f_{3\pi}}{2\sqrt{2}N_C} \frac{(t^c)_{fg}}{C_F\sqrt{N_C}} \frac{\gamma_5}{\sqrt{2}} \sigma_{\mu\nu} q'^{\mu} g_{\perp}^{\nu\beta} \frac{\Phi_{3\pi}(\tau_a, \tau_b, \tau_g)}{\tau_g} \quad g_{\perp}^{\nu\beta} = g^{\nu\beta} - \frac{k'_j{}^{\nu} q'^{\beta} + q'^{\nu} k'_j{}^{\beta}}{k'_j \cdot q'}$$

π^0 subprocess amplitudes

$$\begin{aligned}
 \mathcal{H}_{0-\lambda,\mu\lambda}^{twist-3} &= \mathcal{H}^{twist-3,2-particle} + \mathcal{H}^{twist-3,3-particle} \\
 &= 4\pi\alpha_s f_{3\pi} \frac{C_F}{N_C} \frac{2\lambda - \mu}{2} \frac{\sqrt{-us}}{s^2 u^2} \int_0^1 d\tau \int_0^{\bar{\tau}} \frac{d\tau_g}{\tau_g} \Phi_{3\pi}(\tau, \bar{\tau} - \tau_g, \tau_g) \\
 &\times \left[\left(\frac{1}{\bar{\tau}^2} - \frac{1}{\bar{\tau}(\bar{\tau} - \tau_g)} \right) (s^2 + u^2) + \left(1 - \frac{1}{2} \frac{C_A}{C_F} \right) \left(\frac{1}{\tau} + \frac{1}{\bar{\tau} - \tau_g} \right) \frac{t^2}{\tau_g} \right]
 \end{aligned}$$

$\mathcal{H}^{twist-3} = 0$ if $\Phi_{3\pi} = 0$ (WW appr.)

sum is gauge invariant (QCD and QED) and $s \leftrightarrow u$ crossing symmetric

generalization to other pseudoscalar mesons straightforward

The photoproduction amplitudes

$$\mathcal{M}_{0+\mu+}^{\pi} = \frac{e_0}{2} \sum_{\lambda} \left\{ \mathcal{H}_{0\lambda\mu\lambda}^{\pi} [R_V^{\pi} + 2\lambda R_A^{\pi}] - 2\lambda \frac{\sqrt{-t}}{2m} \mathcal{H}_{0-\lambda\mu\lambda}^{\pi} \bar{S}_T^{\pi} \right\}$$

$$\mathcal{M}_{0-\mu+}^{\pi} = \frac{e_0}{2} \sum_{\lambda} \left\{ \frac{\sqrt{-t}}{2m} \mathcal{H}_{0\lambda\mu\lambda}^{\pi} R_T^{\pi} - 2\lambda \frac{t}{2m^2} \mathcal{H}_{0-\lambda\mu\lambda}^{\pi} S_S^{\pi} \right\} + e_0 \mathcal{H}_{0-, \mu+}^{\pi} S_T^{\pi}$$

form factors S_i are $1/x$ moments of transversity GPDs

light-cone helicities, transform to ordinary helicities

Diehl(01)

$$\Phi_{0\nu', \mu\nu} = \mathcal{M}_{0\nu', \mu\nu} + \frac{1}{2} \kappa \left[(-1)^{1/2-\nu'} \mathcal{M}_{0-\nu', \mu\nu} + (-1)^{1/2+\nu} \mathcal{M}_{0\nu', \mu-\nu} \right] + \mathcal{O}(m^2/s)$$

$$\kappa = \frac{2m}{\sqrt{s}} \frac{\sqrt{-t}}{\sqrt{s+\sqrt{-u}}}$$

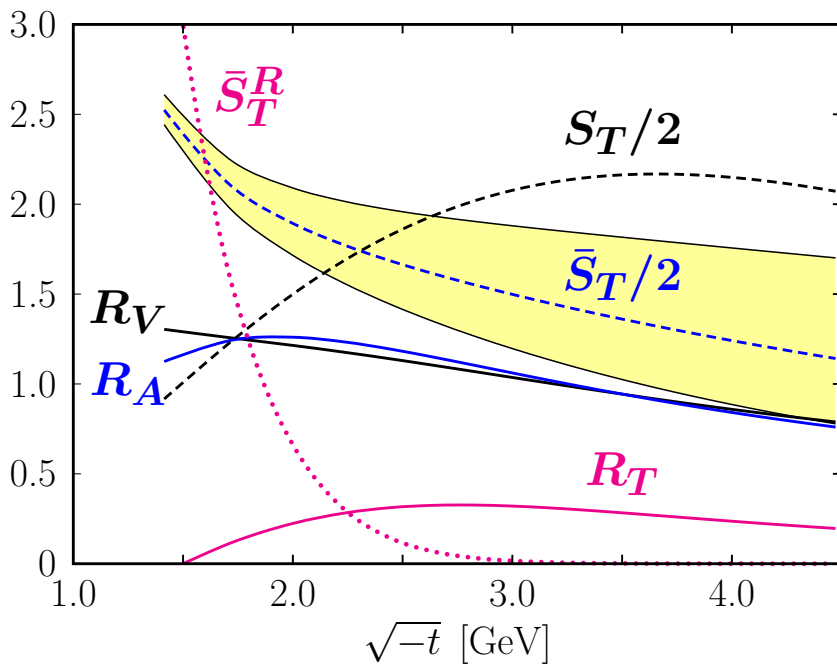
relevant for spin effects

Form factors

in addition to R_V, R_A, R_T :

transversity FFs (skewness = 0)

$$S_T^a(t) = \int_{-1}^1 \frac{dx}{x} \text{sign}(x) H_T^a(x, t), \quad \bar{S}_T^a(t) \rightarrow \bar{E}_T^a(x, t), \quad S_S^a(t) \rightarrow \tilde{H}_T^a(x, t),$$



$$\bar{E}_T = 2\tilde{H}_T + E_T$$

only valence quarks contribute
(charge conjugation symmetry)

$$F_i^{\pi^0} = (e_u F_i^a - e_d F_i^d) / \sqrt{2}$$

from electroproduction:

H_T, \bar{E}_T known at small $-t$

\tilde{H}_T unknown, suppressed by $-t/(4m^2)$

extrapolation to large $-t$:

by term $Ax(1-x)^2$ in profile fct.

with $A \simeq 0.5 \text{ GeV}^{-2}$ and $S_S^{\pi^0} \simeq \bar{S}_T^{\pi^0} / 2$

Large $-t$ behavior of form factors

the power law behavior of the elm. FF also holds for the $1/x$ moments

$$F_i \sim 1/(-t)^{d_i}$$

d_i determined by the powers β_i in $K_i(x, t = 0) \rightarrow (1 - x)^{\beta_i}$ for $x \rightarrow 1$

$$d_i = (1 + \beta_i)/2$$

	R_V	R_A	R_T	S_T	\bar{S}_T
u	2.25	2.22	2.83	2.5	2.5
d	3.0	2.61	3.12	3.5	3.0

The 3-particle twist-3 pion DA

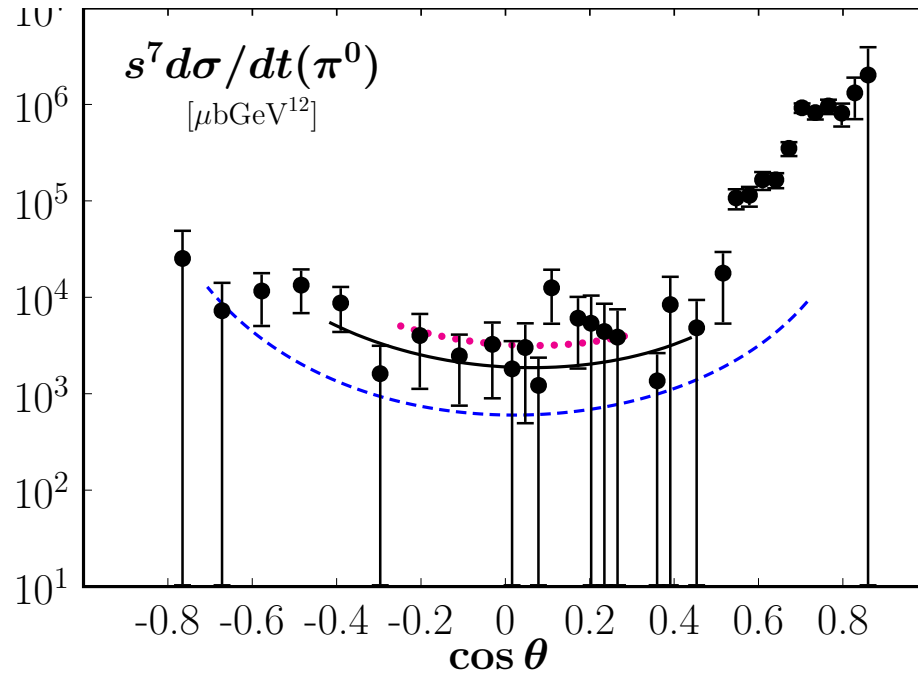
$$\begin{aligned} \Phi_{3\pi} = & 360\tau_a\tau_b\tau_g^2 \left[1 + \omega_{10}(\mu_R^2)(7\tau_g - 3)/2 \right. \\ & \left. + \omega_{20}(\mu_R^2)(2 - 4\tau_a\tau_b - 8\tau_g + 8\tau_g^2) + \omega_{11}(\mu_R^2)(3\tau_a\tau_b - 2\tau_g + 3\tau_g^2) + \dots \right] \end{aligned}$$

(expansion in a series of Jacobi polynomials; coeff. evolve with scale)

Braun-Filyanov (90), Chernyak-Zhitnitsky(84)

choice: $\mu_R^2 = \mu_F^2 = tu/s$

Results on π^0 cross section



data: CLAS (17) at $s = 11.06 \text{ GeV}^2$

$s = 11.06(9, 20) \text{ GeV}^2$

solid(dotted, dashed)

$-t, -u \geq 2.5 \text{ GeV}^2$

dominance of twist-3

large parametric uncertainty (about 70%)

energy dependence: $s^{-7} \frac{\mu_\pi^2}{s} \times$ logs from evolution $\times t$ dependence of form factors

parameters of $\Phi_{3\pi}$ at $\mu_0 = 2 \text{ GeV}$:

$f_{3\pi} = 0.004 \text{ GeV}^2$ $\omega_{10} = -2.55$

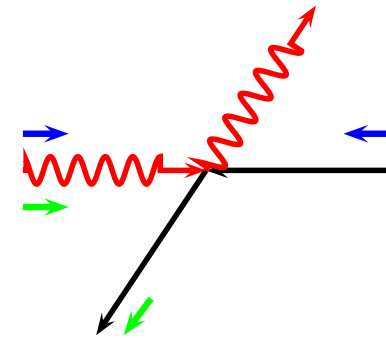
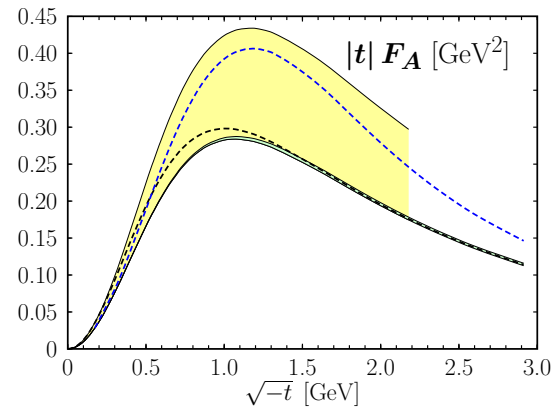
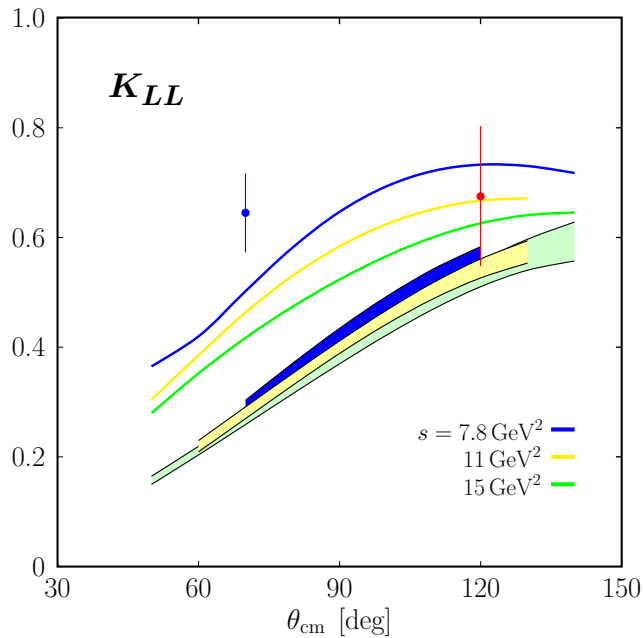
from Ball (98)

fit to data: $\omega_{20} = 8.0$ $\omega_{11} = 0$

close to values quoted in

Braun-Filyanov (90), Chernyak-Zhit.(84)

Helicity correlation A_{LL} and K_{LL} in WACS



Klein-Nishina result

$$\hat{A}_{LL} = \hat{K}_{LL} = \frac{s^2 - u^2}{s^2 + u^2}$$

$$A_{LL} = K_{LL} \simeq \hat{A}_{LL} \frac{R_A}{R_V}$$

JLab E99-114 ($s = 6.9 \text{ GeV}^2$ $u = -1.04 \text{ GeV}^2$)

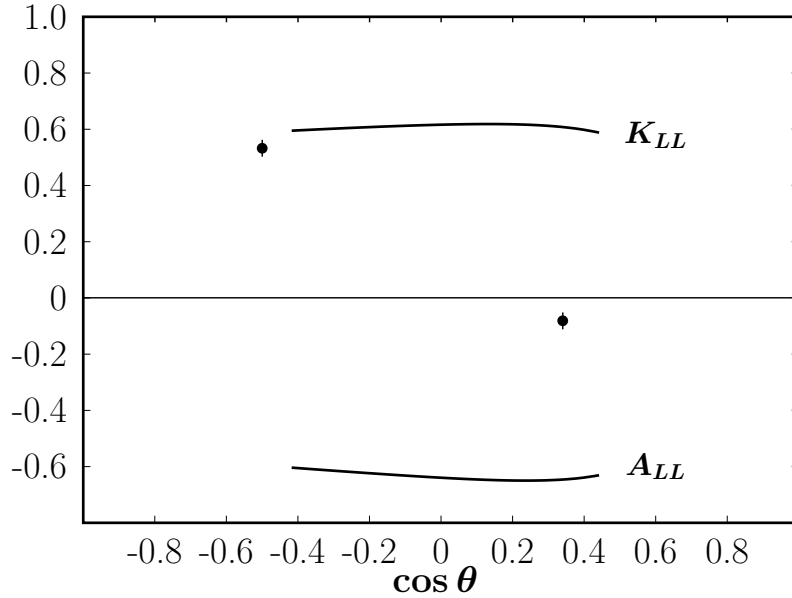
JLab E07-002 ($s = 7.8 \text{ GeV}^2$ $t = -2.1 \text{ GeV}^2$)

application of handbag mechanism is at the limits

R_A badly known since F_A badly known, old data for $-t \lesssim 2 \text{ GeV}^2$ Kitagaki (83)

MINERvA? or K_{LL} from Jlab?

Helicity correlation in photoproduction



$$s = 11.06 \text{ GeV}^2$$

$$A_{LL}^{twist-2} = K_{LL}^{twist-2} \text{ as for WACS}$$

$$A_{LL}^{twist-3} = -K_{LL}^{twist-3}$$

characteristic signature for dominance
of twist-3

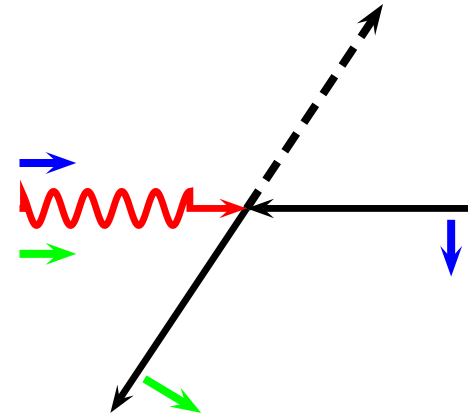
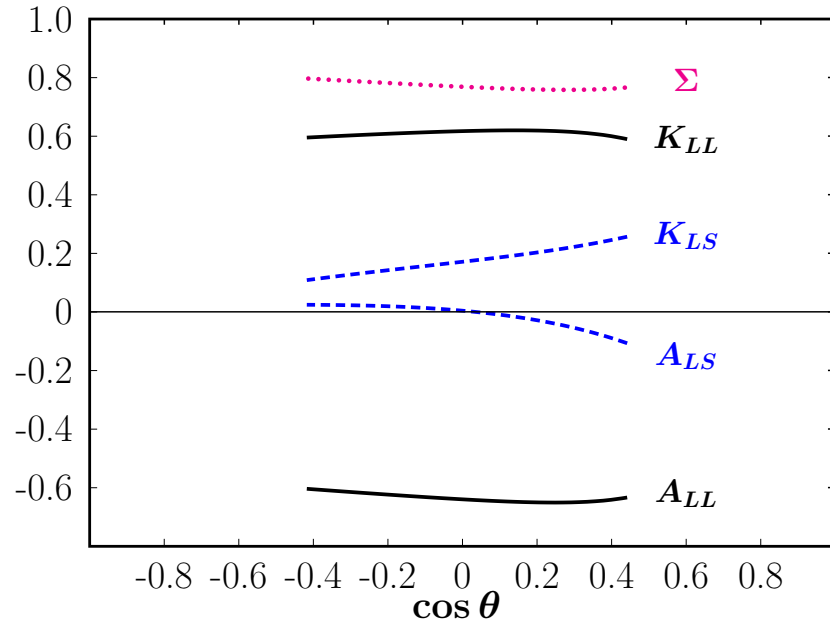
like $\sigma_T \gg \sigma_L$ in pion electroprod.

$$A_{LL}^{twist-3} = -K_{LL}^{twist-3} = -4 \frac{S_T^{\pi^0}}{F^{\pi^0}} \left[S_T^{\pi^0} - \frac{t}{2m^2} S_S^{\pi^0} + \kappa \frac{\sqrt{-t}}{2m} \bar{S}_T^{\pi^0} \right]$$

$$F^{\pi^0} = \frac{-t}{2m^2} \left[(\bar{S}_T^{\pi^0})^2 - \frac{t}{m^2} (S_S^{\pi^0})^2 + 4S_S^{\pi^0} S_T^{\pi^0} - 8 \frac{m^2}{t} (S_T^{\pi^0})^2 \right]$$

K_{LL} data: Fanelli(15)(Hall A(05)) $s = 7.8(6.9) \text{ GeV}^2$, $t = -2.1(u = -1.04) \text{ GeV}^2$

Other observables



$$A_{LS}^{twist-3} = -K_{LS}^{twist-3}$$

$$= -2 \frac{S_T^{\pi^0}}{F^{\pi^0}} \left[\frac{\sqrt{-t}}{m} \bar{S}_T^{\pi^0} - 2\kappa \left(S_T^{\pi^0} - \frac{t}{4m^2} S_S^{\pi^0} \right) \right]$$

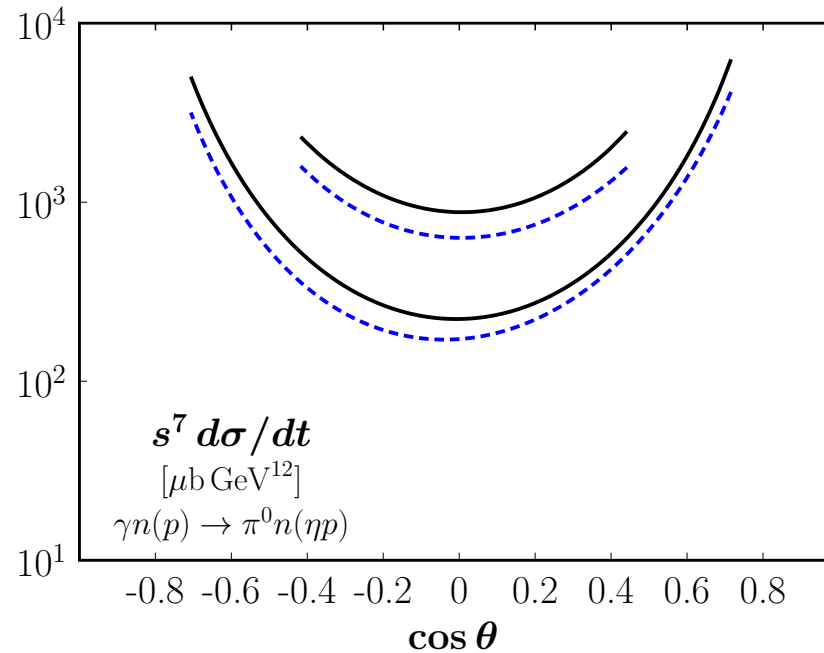
$$A_{LS}^{twist-2} = K_{LS}^{twist-2}$$

$$\Sigma^{twist-3} = 1 - 4 \frac{(S_T^{\pi^0})^2}{F^{\pi^0}} \quad \text{asymmetry for linearly polarized photons}$$

data: Fanelli(15)(Hall A(05)) $s = 7.8(6.9) \text{ GeV}^2$, $t = -2.1(u = -1.04) \text{ GeV}^2$

$$K_{LS} = -0.296 \pm 0.007(0.480 \pm 0.007)$$

π^0 production off neutrons and η production



$$F_{in}^{\pi^0} = \frac{1}{\sqrt{2}} [e_u F_i^d - e_d F_i^u]$$

$$F_i^{(8)} \simeq F_i^{(1)} \simeq \frac{1}{\sqrt{6}} [e_u F_i^u + e_d F_i^d]$$

$$\mathcal{M}_i^\eta = \cos \theta_8 \mathcal{M}_i^{(8)} - \sin \theta_1 \mathcal{M}_i^{(1)}$$

solid: neutron

dashed: η

$$s = 11.06 \text{ GeV}^2$$

The 2-particle twist-3 DAs

a combination of EOM is linear first order diff. equation for Φ_σ solution:

$$\Phi_\sigma = 6\tau\bar{\tau} \left(\int d\tau \frac{\bar{\tau}\Phi_1^{EOM} - \tau\Phi_2^{EOM}}{2\tau^2\bar{\tau}^2} + C \right)$$

$$\Phi_P = \frac{\Phi_\sigma}{6\tau\bar{\tau}} + \frac{\Phi_1^{EOM}}{2\tau} + \frac{\Phi_2^{EOM}}{2\bar{\tau}}$$

local limit: $\langle \pi^+(q') | \bar{d}(0)\gamma_5 u(0) | 0 \rangle = if_\pi\mu_\pi \quad \left(\int_0^1 d\tau \Phi_P(\tau) = 1 \right)$

\implies fixes constant of integration:

$$C = 1 + \eta_3(7\omega_{1,0} - 2\omega_{2,0} - \omega_{1,1}) \quad (\eta_3 = f_{3\pi}/(f_\pi\mu_\pi))$$

$$\Phi_P = 1 + \sum_{n=2,4,\dots} a_n^P C_n^{(1/2)}(2\tau - 1) \quad a_2^P = -\frac{10}{3}a_4^P = \frac{10}{7}\eta_3(7\omega_{1,0} - 2\omega_{2,0} - \omega_{1,1})$$

$$\Phi_\sigma = \eta_\sigma \tilde{\Phi}_\sigma \quad \tilde{\Phi}_\sigma = 6\tau\bar{\tau} \left[1 + \sum_{n=2,4,\dots} a_n^\sigma C_n^{(3/2)}(2\tau - 1) \right]$$

$$a_2^\sigma = \frac{1}{6} \frac{\eta_3}{\eta_\sigma} (12 + 3\omega_{1,0} - 4\omega_{2,0}) \quad a_4^\sigma = \frac{1}{105} \frac{\eta_3}{\eta_\sigma} (22\omega_{2,0} - 3\omega_{1,1})$$

$$\eta_\sigma = 1 - \eta_3(12 - 4\omega_{1,0} + \frac{8}{7}\omega_{2,0} + \frac{4}{7}\omega_{1,1}) \quad \text{may be absorbed in } \mu_\pi$$

for $\eta_3 \rightarrow 0$: $\Phi_P \rightarrow 1$, $\Phi_\sigma \rightarrow 2\tau\bar{\tau}$ **WW approx.**

The Gegenbauer coefficients

at scale $\mu_0 = 2 \text{ GeV}$:

$$\begin{aligned} a_2^P &= -0.56, & a_4^P &= 0.17, \\ a_2^\sigma &= -0.084, & a_4^\sigma &= 0.031, & \eta_\sigma &= 0.64. \end{aligned}$$

$$a_n^P = a_n^\sigma = 0 \text{ for } n \geq 6$$

values of $a_2^{P,\sigma}$ compatible with other results

values of $a_4^{P,\sigma}$ have opposite sign

Dyson-Schwinger approach	Shi et al (15)
light-cone quark model	Choi-Ji (17)
chiral quark model	Nam-Kim (06)

An alternative

Braun-Filyanov (90), Ball (98)

instead of $A^+ = 0$ the contour (Fock-Schwinger) gauge $x^\mu A_\mu(x) = 0$ is used

EOM more complicated but a [recursion formula](#) for the moments of the twist-3 DAs has been derived, allows also to calculate Φ_P and Φ_σ for given $\Phi_{3\pi}$

they differ from our ones for the same $\Phi_{3\pi}$

With these DAs the result for the subprocess amplitude is **not** gauge invariant

Reason: the Wilson lines ($\neq 1$) in the vacuum-pion matrix elements affect the calculation of the amplitudes

At least for electroproduction of ρ_T the equivalence of the two methods has been shown [Anikin et al \(10\)](#)

Summary

handbag factorization applied to wide-angle photoproduction of pions

- In contrast to WACS, the leading-twist analysis (with helicity non-flip GPDs) fails by order of magnitude
- we calculated the full (2- and 3-particle) twist-3 contribution; in contrast to electroproduction the subprocess amplitude is regular in collinear approximation
- together with the transversity form factors ($1/x$ moments of transversity GPDs) which are known from pion electroproduction at small $-t$ and are extrapolated to large $-t$ and a 3-particle twist-3 DA taken (partially) from literature we are able to fit the CLAS data at $s = 11.06 \text{ GeV}^2$
- there are interesting spin effects, e.g. $A_{LL}^{twist-3} = -K_{LL}^{twist-3}$ but $A_{LL}^{twist-2} = K_{LL}^{twist-2}$ as for WACS