
Study of nucleon resonances at EBAC@JLab

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**in collaboration with
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Outline

- ✓ **Excited Baryon Analysis Center (EBAC)
at Jefferson Lab**

- ✓ **Dynamical origin of P11 nucleon resonances**

PDG *s and N*'s origin

Particle	$L_{2I,2J}$ status	$N\pi$	$N\eta$	ΔK					
$N(939)$	P_{11}	****							
$N(1440)$	P_{11}	****	****	*					
$N(1520)$	D_{13}	****	****	***					
$N(1535)$	S_{11}	****	****	****					
$N(1650)$	S_{11}	****	****	*	***				
$N(1675)$	D_{15}	****	****	*	*				
$N(1680)$	F_{15}	****	****	*		****	***		
$N(1700)$	D_{13}	***	***	*	**	*	**		
$N(1710)$	P_{11}	***	***	**	**	*	**		****
$N(1720)$	P_{13}	****	****	*	**	*	*	**	**
$N(1900)$	P_{13}	**	**	*			*		
$N(1990)$	F_{17}	**	**	*	*				*
$\Delta(1232)$	P_{33}	****	****	F					****
$\Delta(1600)$	P_{33}	***	***	o	?		***	*	**
$\Delta(1620)$	S_{31}	****	****	r			****	****	***
$\Delta(1700)$	D_{33}	****	****	b		*	***	**	***
$\Delta(1750)$	P_{31}	*	*	?					
$\Delta(1900)$	S_{31}	**	**	d		*	*	**	*
$\Delta(1905)$	F_{35}	****	****	d		*	**	**	****
$\Delta(1910)$	P_{31}	****	****	e		*	*	*	*
$\Delta(1920)$	P_{33}	***	***	n	?	*	**		*
$\Delta(1930)$	D_{35}	***	***			*			**
$\Delta(1940)$	D_{33}	*	*	F					
$\Delta(1950)$	F_{37}	****	****	o		*	****	*	****

All of these studies essentially agree on the existence and (most) properties of the 4-star states. For the 3-star and lower states, however, even a statement of existence is problematic.

— Arndt, Briscoe, Strakovsky, Workman PRC 74 045205 (2006)

PDG *s and N*'s origin

✓ Most of their properties were extracted from

$$\pi N \rightarrow \pi N$$

$$\gamma N \rightarrow \pi N$$

Need consistent analysis of πN and $\pi\pi N$ channels

Particle	$L_{2I,2J}$ status	$N\pi$	$N\eta$	ΔK	ΣK	$\Delta\pi$	$N\rho$	$N\gamma$
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$N(1680)$	F_{15}	****	**** *			**** ****	****	****
$N(1700)$	D_{13}	***	*** * ?	** *	*	** *	*	**
$N(1710)$	P_{11}	***	*** ** ?	** *	*	** *	*	****
$N(1720)$	P_{13}	****	**** * ?	** *	*	* **	**	**
$N(1900)$	P_{13}	**	** * ?				*	
$N(1990)$	F_{17}	**	** * ?	*	*			*
$\Delta(1232)$	P_{33}	****	**** F					****
$\Delta(1600)$	P_{33}	***	*** o ?			*** *	*	**
$\Delta(1620)$	S_{31}	****	**** r			**** ****	****	****
$\Delta(1700)$	D_{33}	****	**** b		*	*** **	**	****
$\Delta(1750)$	P_{31}	*	* ?					
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$\Delta(1905)$	F_{35}	****	**** d		*	** **	**	****
$\Delta(1910)$	P_{31}	****	**** e		*	* *	*	*
$\Delta(1920)$	P_{33}	***	*** n ?		*	**		*
$\Delta(1930)$	D_{35}	***	*** ?		*			**
$\Delta(1940)$	D_{33}	*	* F					
$\Delta(1950)$	F_{37}	****	**** o		*	**** *	*	****

PDG *s and N*'s origin

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$\Delta(1910)$	P_{31}	****	**** e	*	*	* *	*	*
$\Delta(1920)$	P_{33}	***	*** n	*	*	** **	**	*
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$\Delta(1940)$	D_{33}	*	* F					
$\Delta(1950)$	F_{37}	****	**** o	*	*	**** *	*	****

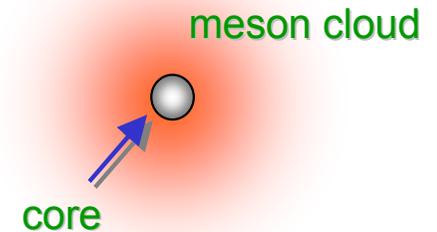
✓ Most of their properties were extracted from

$$\pi N \rightarrow \pi N$$

$$\gamma N \rightarrow \pi N$$

✓ Are they all genuine quark/gluon excitations (with meson cloud) ?

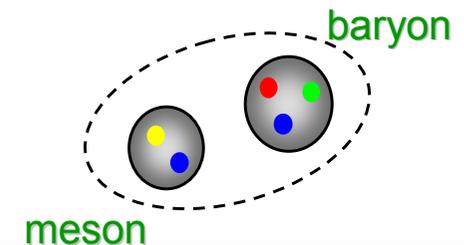
$$|N^*\rangle = |qqq\rangle + |\text{m.c.}\rangle$$



✓ Is their origin dynamical ?

→ some could be understood as arising from meson-baryon dynamics

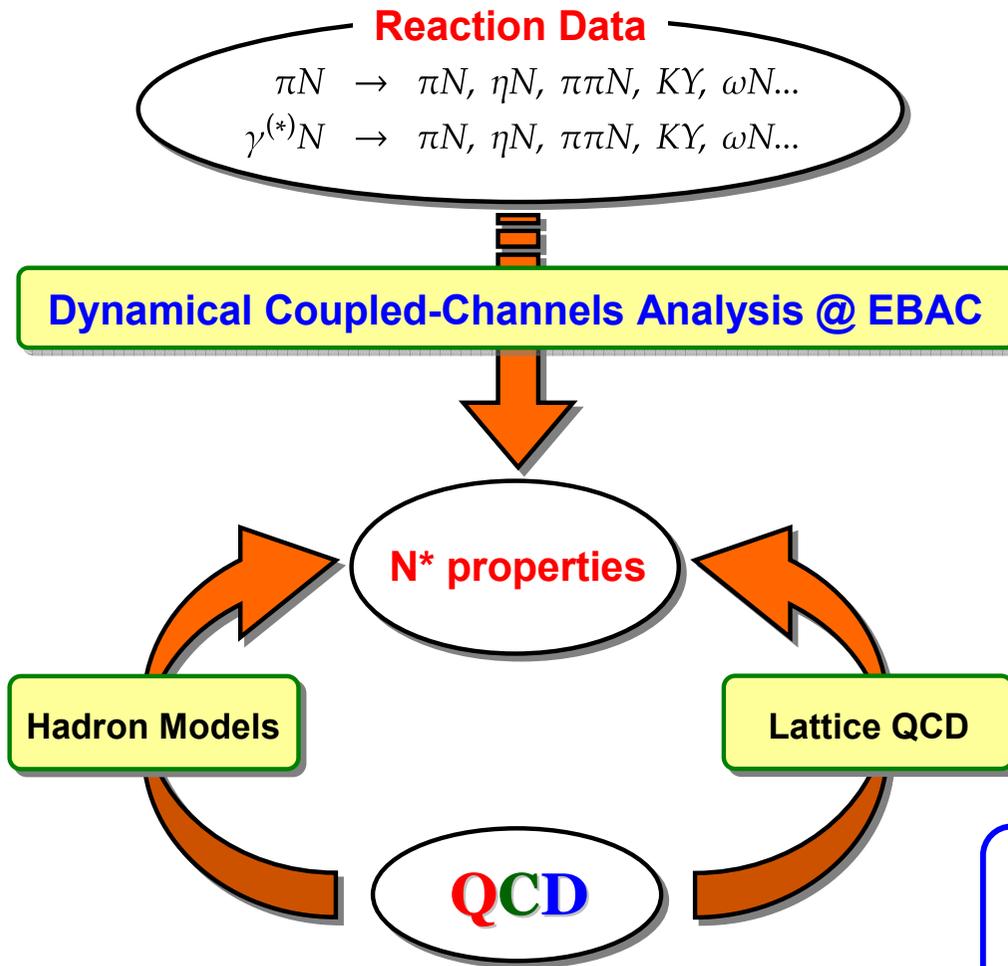
$$|N^*\rangle = |MB\rangle$$



Excited Baryon Analysis Center (EBAC) at Jefferson Lab

Founded in January 2006

<http://ebac-theory.jlab.org/>



Objectives and goals:

Through the **comprehensive analysis** of world data of πN , γN , $N(e,e')$ reactions,

- ✓ Determine N^* spectrum (masses, widths)
- ✓ Extract N^* form factors, in particular the **N - N^* e.m. transition form factors**
- ✓ Provide **reaction mechanism information** for interpreting the N^* properties

Theory support for
Excited Baryon Program by **CLAS@JLab**
(arXiv:0907.1901)

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Reaction Data

$\pi N \rightarrow \pi N, \eta N, \pi\pi N, KY, \omega N...$

Objectives and goals:

Through the comprehensive analysis

Careful treatment of **couplings** between **multi-reaction channels** is necessary !!



“Dynamical coupled-channels model of meson production reactions”

A. Matsuyama, T. Sato, T.-S.H. Lee Phys. Rep. 439 (2007) 193

Hadron Models

Lattice QCD

QCD



Theory support for
Excited Baryon Program by **CLAS@JLab**
(arXiv:0907.1901)

Dynamical coupled-channels model @ EBAC

For details see Matsuyama, Sato, Lee, Phys. Rep. 439,193 (2007)

✓ Partial wave (LSJ) amplitude of $a \rightarrow b$ reaction:

$$T_{a,b}^{(LSJ)}(p_a, p_b; E) = V_{a,b}^{(LSJ)}(p_a, p_b) + \sum_c \int_0^\infty q^2 dq V_{a,c}^{(LSJ)}(p_a, q) G_c(q; E) T_{c,b}^{(LSJ)}(q, p_b; E)$$

coupled-channels effect

✓ Reaction channels:

$$a, b, c = (\gamma^{(*)}N, \pi N, \eta N, \pi\Delta, \sigma N, \rho N, K\Lambda, K\Sigma, \omega N)$$

$\pi\pi N$

✓ Potential:

$$V_{a,b} = v_{a,b} + \sum_{N^*} \frac{\Gamma_{N^*,a}^\dagger \Gamma_{N^*,b}}{E - M_{N^*}}$$

ground
meson-baryon
exchange

bare N^* state

Current status of the EBAC-DCC analysis

Hadronic part

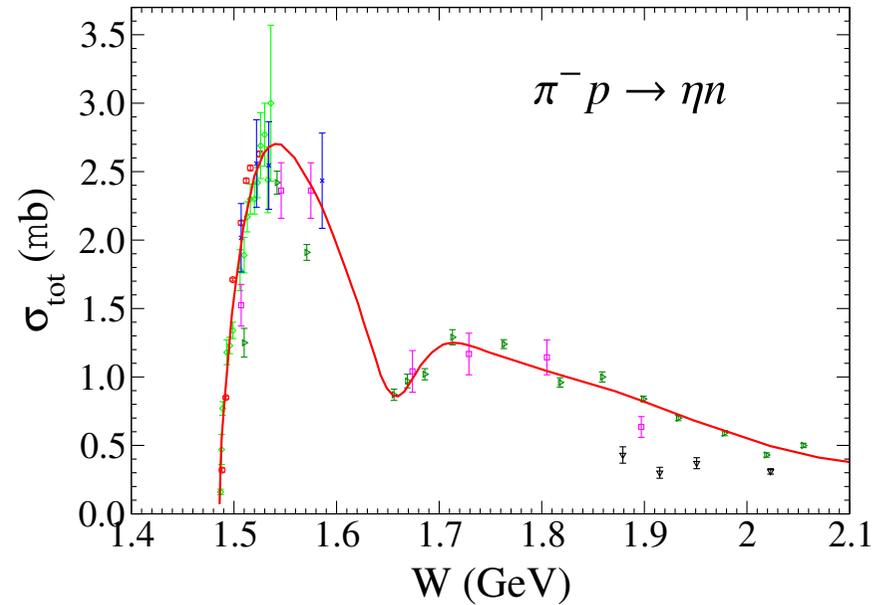
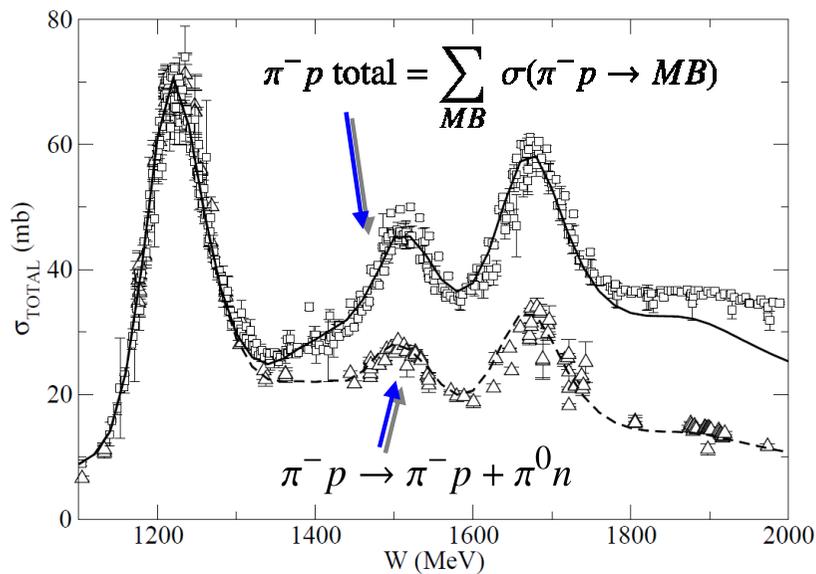
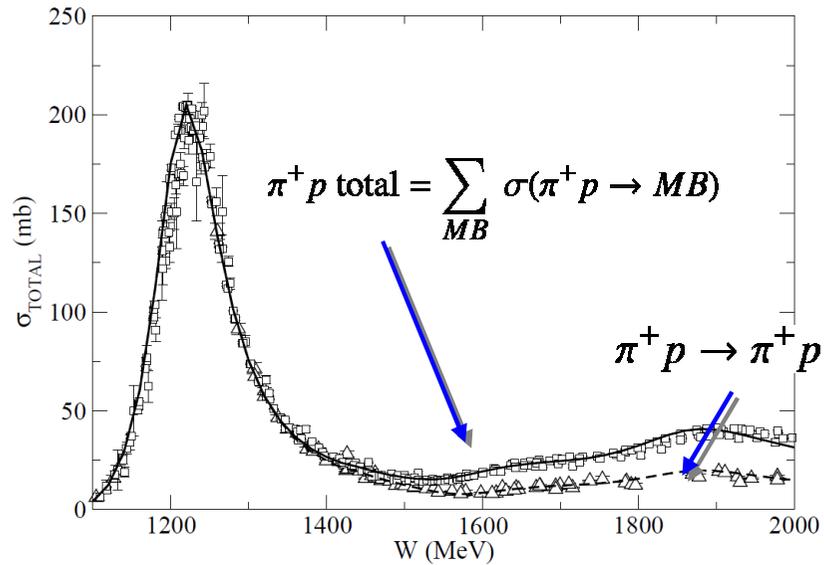
- ✓ $\pi N \rightarrow \pi N$: model constructed up to $W = 2$ GeV.
Julia-Diaz, Lee, Matsuyama, Sato, PRC76 065201 (2007)
- ✓ $\pi N \rightarrow \pi \pi N$: cross sections calculated with the πN model; fit is ongoing.
Kamano, Julia-Diaz, Lee, Matsuyama, Sato, PRC79 025206 (2009)
- ✓ $\pi N \rightarrow \eta N$: model constructed up to $W = 2$ GeV
Durand, Julia-Diaz, Lee, Saghai, Sato, PRC78 025204 (2008)

Electromagnetic part

- ✓ $\gamma^{(*)} N \rightarrow \pi N$: model constructed up to $W = 1.6$ GeV (& up to $Q^2 = 1.5$ GeV²)
(photoproduction) Julia-Diaz, Lee, Matsuyama, Sato, Smith, PRC77 045205 (2008)
(electroproduction) Julia-Diaz, Kamano, Lee, Matsuyama, Sato, Suzuki, PRC80 025207 (2009)
- ✓ $\gamma N \rightarrow \pi \pi N$: cross sections calculated with the γN & πN model; fit is ongoing.
Kamano, Julia-Diaz, Lee, Matsuyama, Sato, arXiv:0909.1129 [nucl-th]
- ✓ $\gamma^{(*)} N \rightarrow \eta N$: *in progress*
- ✓ $\gamma N \rightarrow KY, \omega N$: *in progress*

Analysis of $\pi N \rightarrow \pi N$ & ηN reactions

Julia-Diaz, Lee, Matsuyama, Sato, PRC76 065201 (2007)
Durand, Julia-Diaz, Lee, Saghai, Sato, PRC78 025204 (2008)

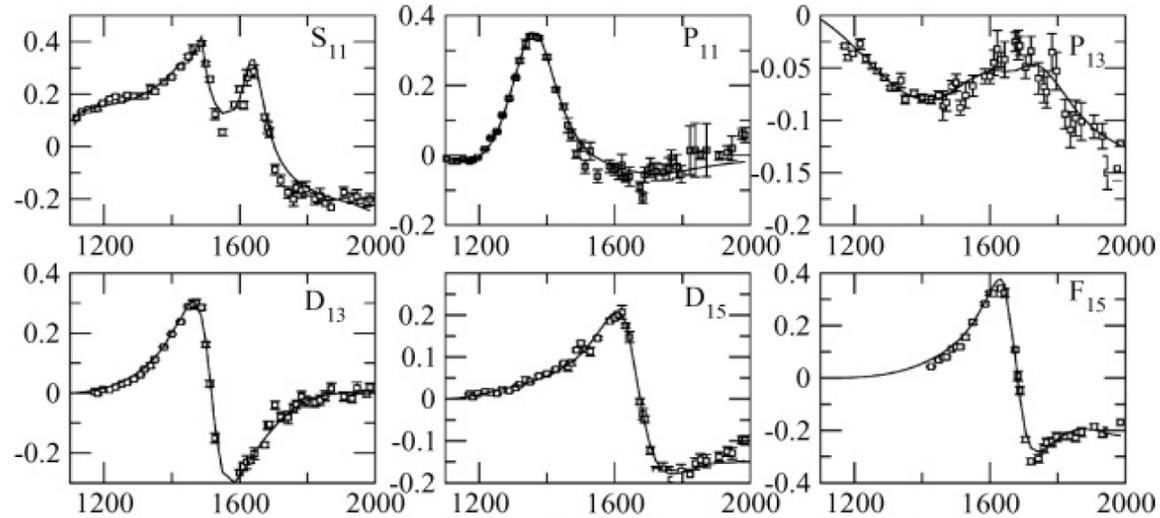


Constructed pi N partial wave amplitudes

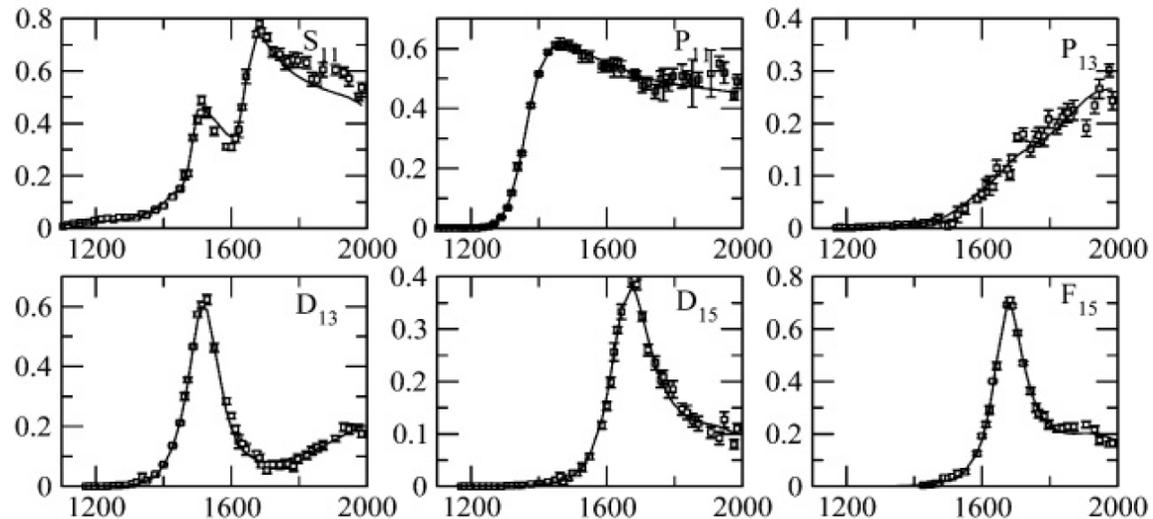
Julia-Diaz, Lee, Matsuyama, Sato, PRC76 065201 (2007)

Isospin = 1/2

Real part



Imaginary part



— EBAC
⊕ SAID06

W (MeV)

How can we extract N^* information?

PROPER definition of

- ✓ N^* mass and width → **Pole position** of the amplitudes
- ✓ $N^* \rightarrow MB, \gamma N$ decay vertices → **Residue** of the pole

$$\langle p_a | \hat{T}(E) | p_b \rangle \Big|_{E \rightarrow E_0} \rightarrow \frac{\bar{\Gamma}(E_0, p_a) \bar{\Gamma}(E_0, p_b)}{E - E_0} + (\text{regular terms})$$

$N^* \rightarrow b$
decay vertex

N^* pole position
($\text{Im}(E_0) < 0$)

How can we extract N^* information?

PROPER definition of

- ✓ N^* mass and width → **Pole position** of the amplitudes
- ✓ $N^* \rightarrow MB, \gamma N$ decay vertices → **Residue** of the pole

Need **analytic continuation** of the amplitudes !!

→ Suzuki, Sato, Lee, PRC79 025205 (2009); arXiv:0910.1742

N^* pole position
($\text{Im}(E_0) < 0$)

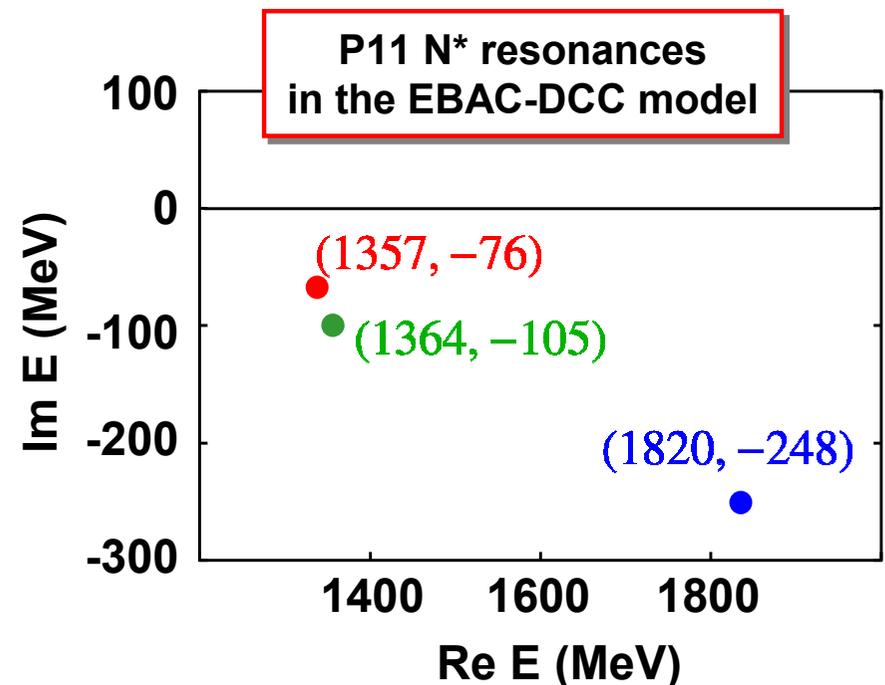
Dynamical origin of P11 nucleon resonances

Suzuki, Julia-Diaz, Kamano, Lee, Matsuyama, Sato arXiv:0909.1356

Findings:

1. **Two almost degenerate poles** in the Roper resonance region.
2. **All three poles** below 2 GeV evolve from a *same, single* bare state.

Analysis	P11 poles (MeV)	
EBAC (2009)	(1357, -76)	(1364, -105)
CMB (1990)	(1370, -114)	(1360, -120)
GWU/VPI (2006)	(1359, -82)	(1388, -83)
Jülich (2009)	(1387, -74)	(1387, -71)



Dynamical origin of P11 nucleon resonances

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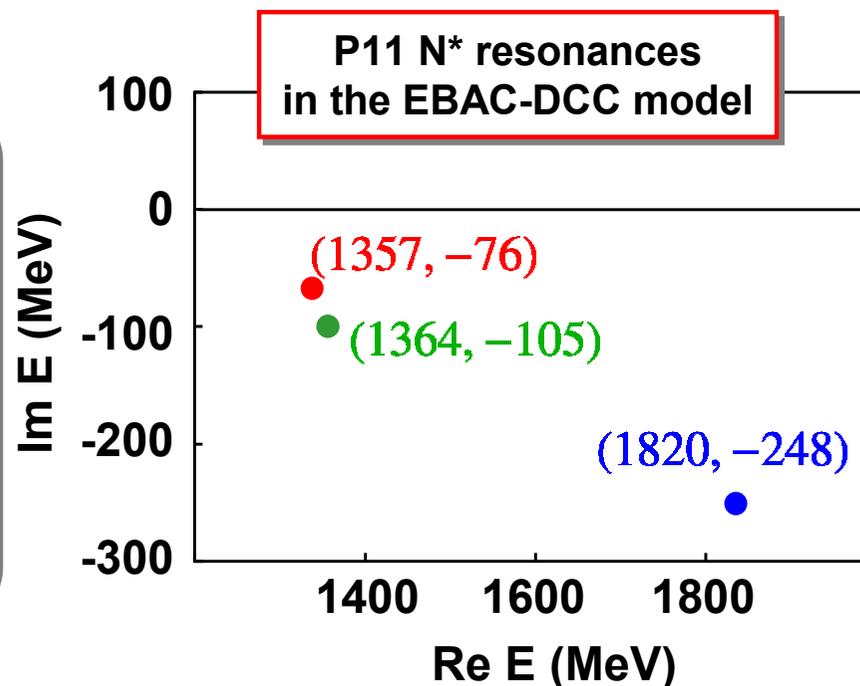
1. **Two almost degenerate poles** in the Roper resonance region.
2. **All three poles** below 2 GeV evolve from a *same, single* bare state.

Multi-channels reactions can generate **many** resonance poles from a **single** bare state!!

Eden, Taylor, Phys. Rev. 133 B1575 (1964)

e.g.)

Two poles for $J^\pi = 3/2^+$ resonance in He^5
Hale, Brown, Jarmie, PRL59 763 (1987)

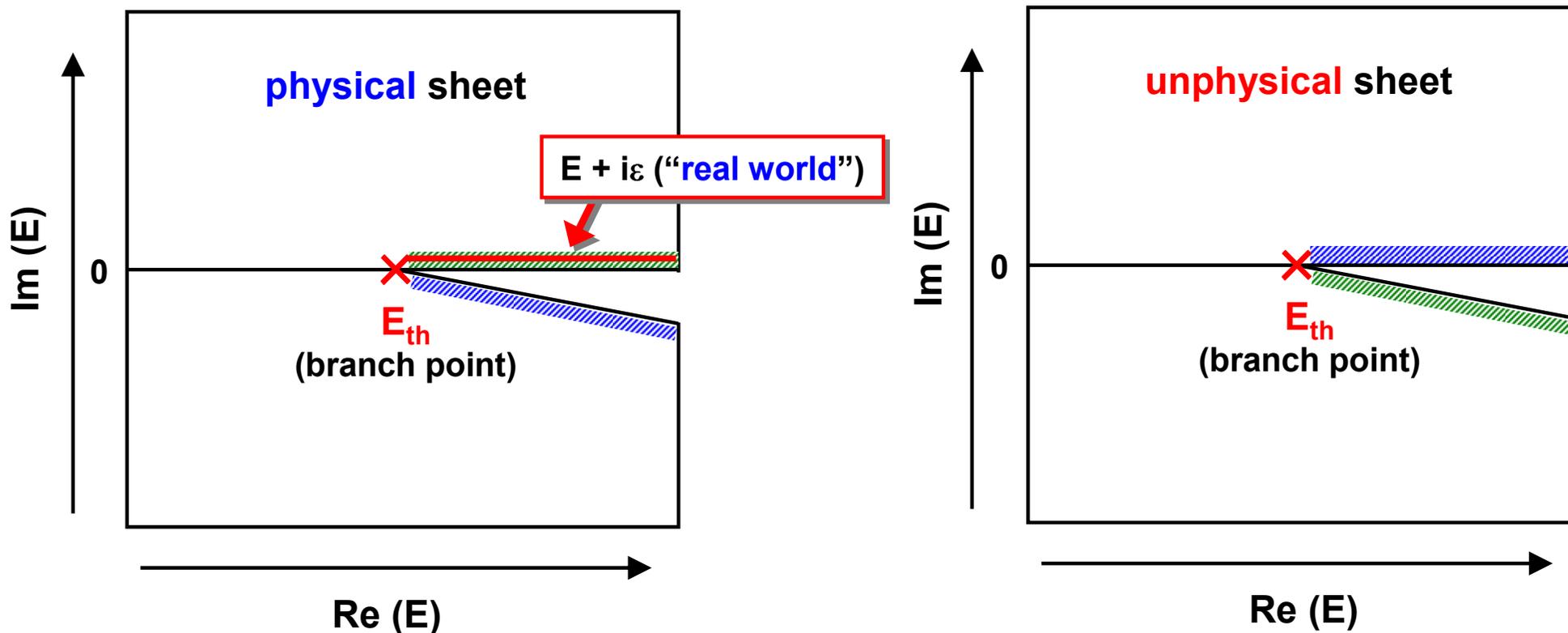


Analytic structure of the scattering amplitudes

e.g.) single-channel meson-baryon scattering

$$T(p, p'; E) = V(p, p') + \int q^2 dq V(p, q) G(q; E) T(q, p'; E)$$

Scattering amplitude is
a **double-valued function of E !!**



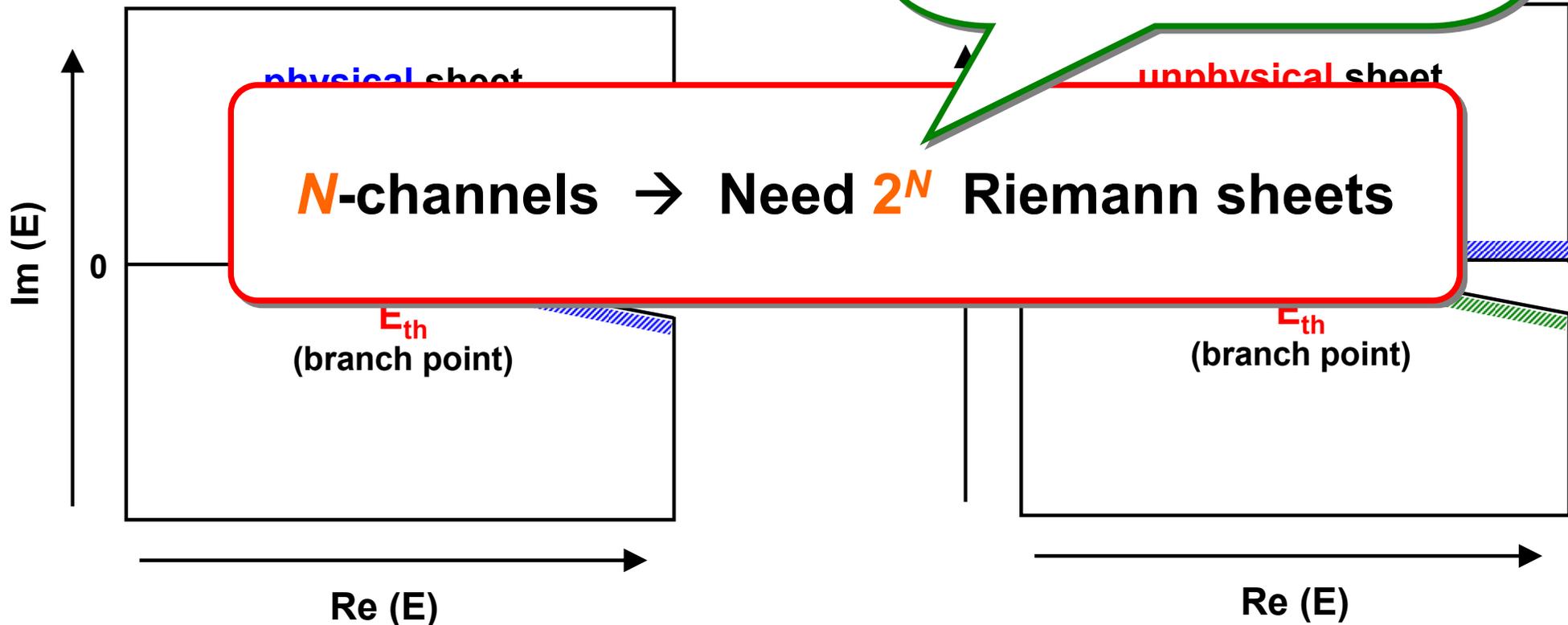
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Scattering amplitude is a **double-valued function of E !!**

2-channel case (4 sheets):
 (channel 1, channel 2) =
 (p, p), (u, p), (p, u), (u, u)
 p = physical sheet
 u = unphysical sheet

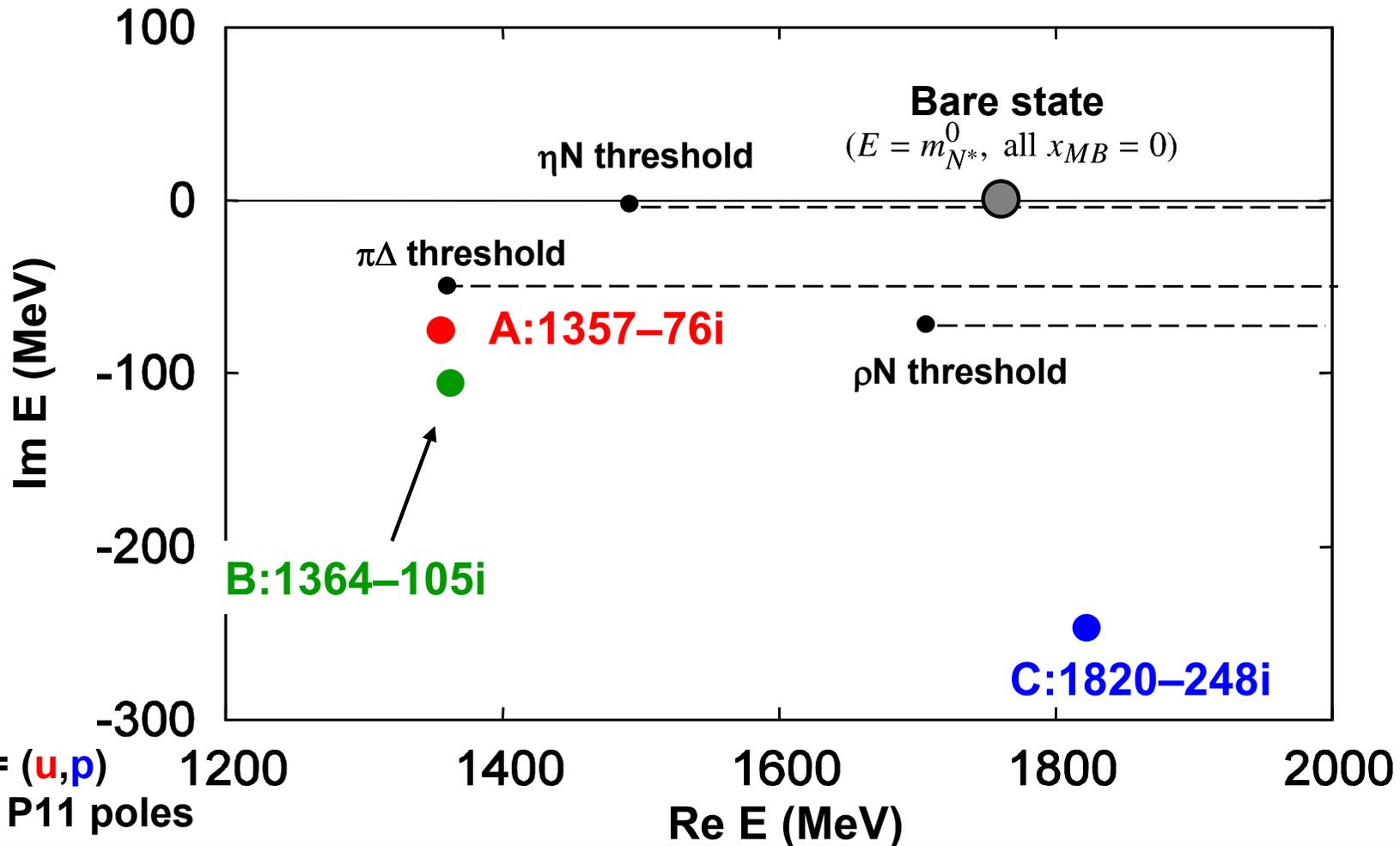


Dynamical origin of P11 resonances

Suzuki, Julia-Diaz, Kamano, Lee, Matsuyama, Sato, PRL104 042302 (2010)

Pole trajectory
of N^* propagator

$$\frac{1}{E - m_{N^*}^0 - \sigma(E)} \rightarrow \frac{1}{E - m_{N^*}^0 - \sum_{MB} x_{MB} \sigma_{MB}(E)} \quad x_{MB} : 0 \rightarrow 1$$

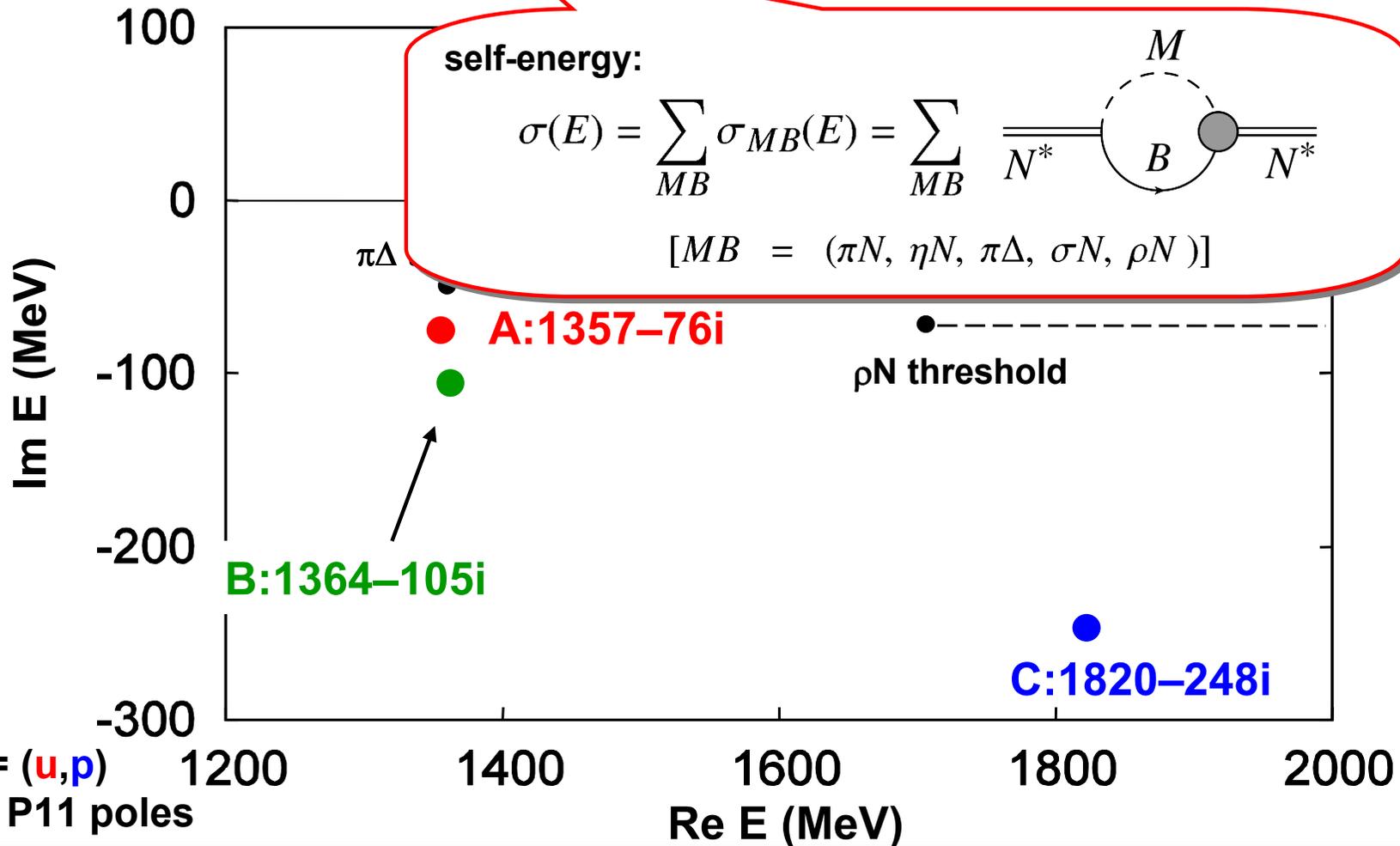


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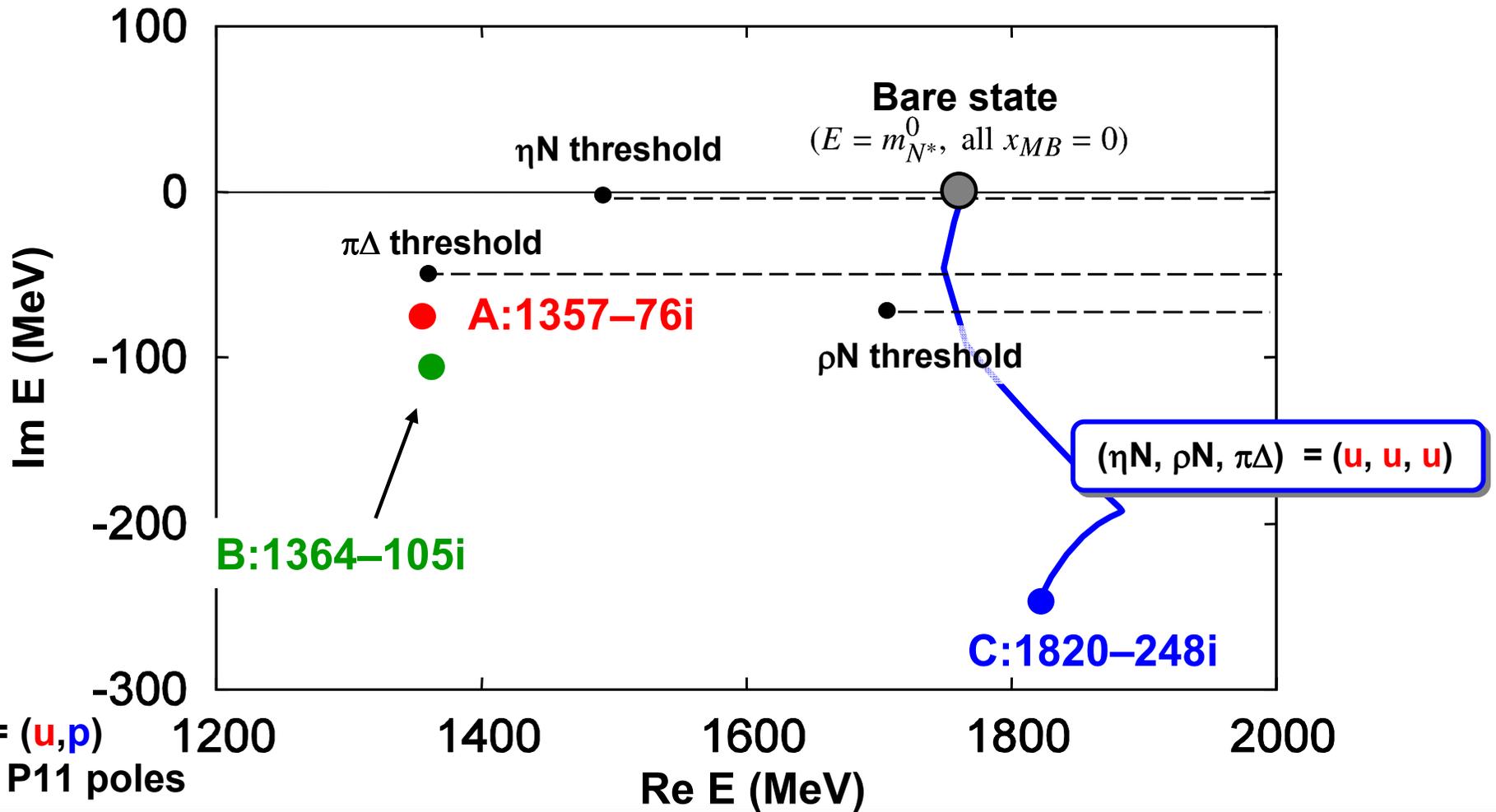


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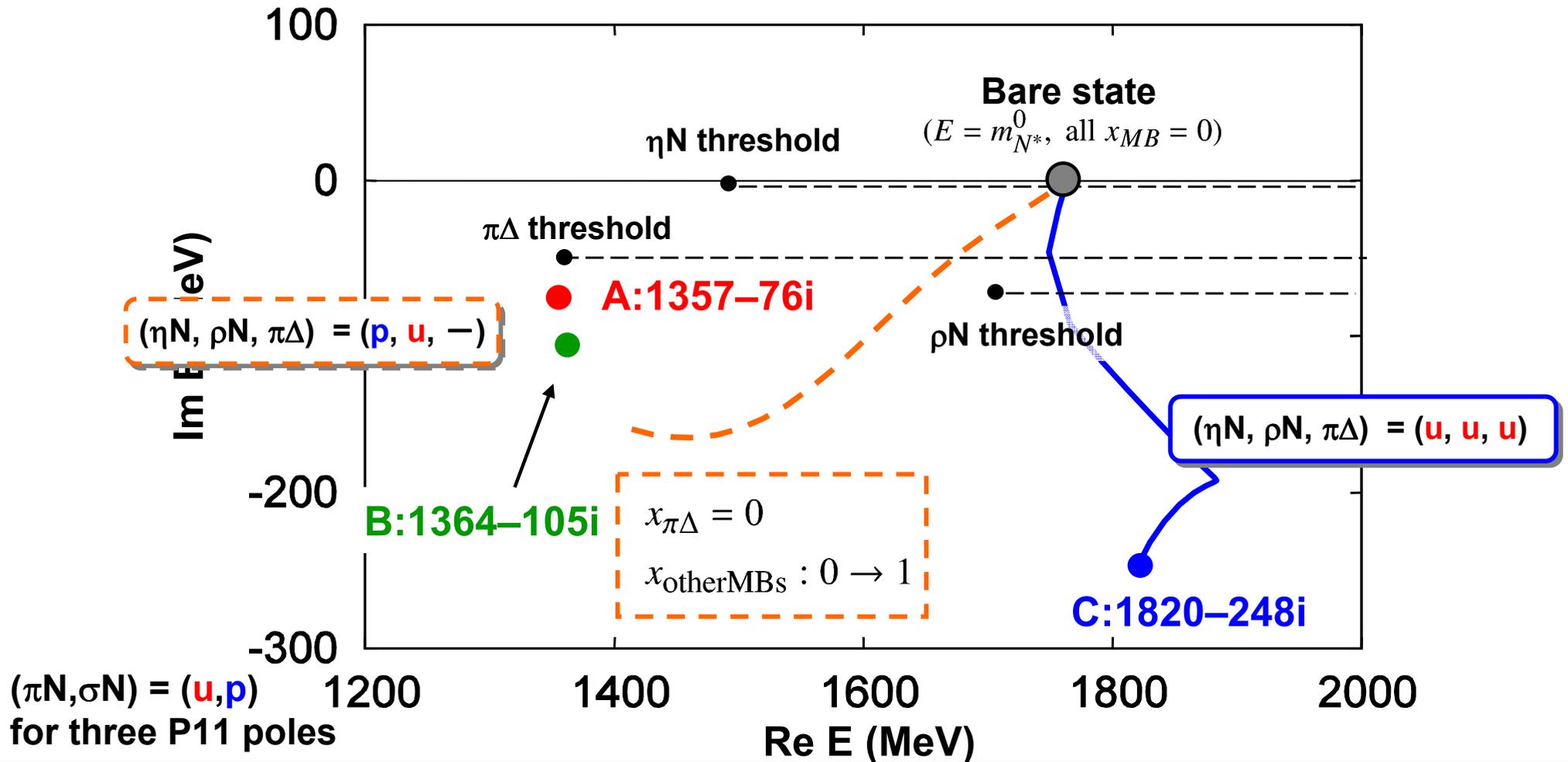


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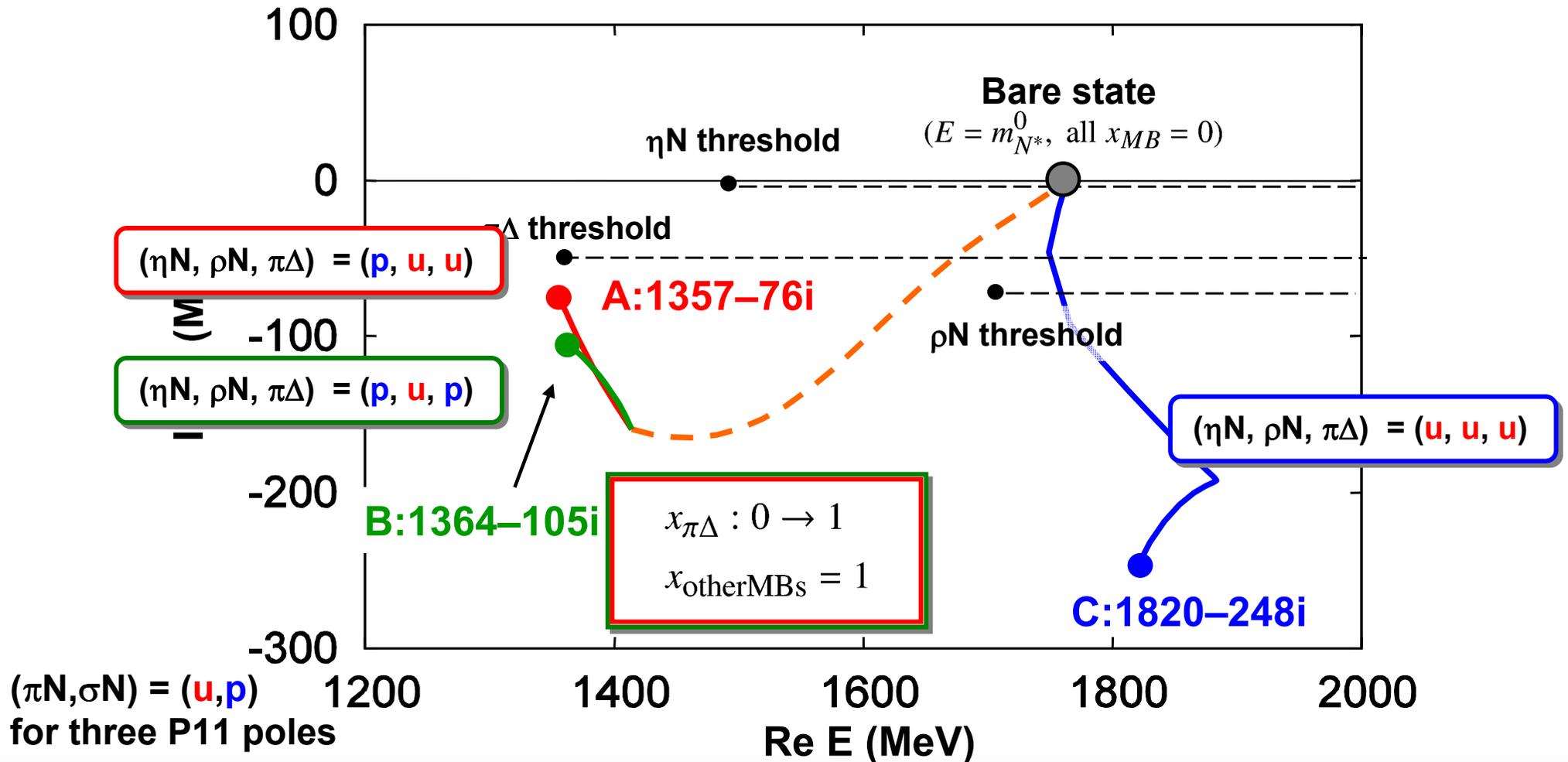


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Summary

- ✓ Continuous effort for exploring the N^* states in Excited Baryon Analysis Center (**EBAC**) at Jefferson Lab.
- ✓ Scattering amplitudes are successfully constructed by **dynamical coupled-channels analysis** of meson production reactions.
- ✓ **Dynamical origin** of the **P11** nucleon resonances:
 - **Two resonance poles** are found in the Roper energy region.
 - (Two) Roper and $N^*(1710)$ originate from a **same, single** bare state.

Treatment of **multi-reaction channels** is key to understanding the **N^* spectrum** !!