



# New parton distributions from large- $x$ , low- $Q^2$ data

*Wally Melnitchouk*

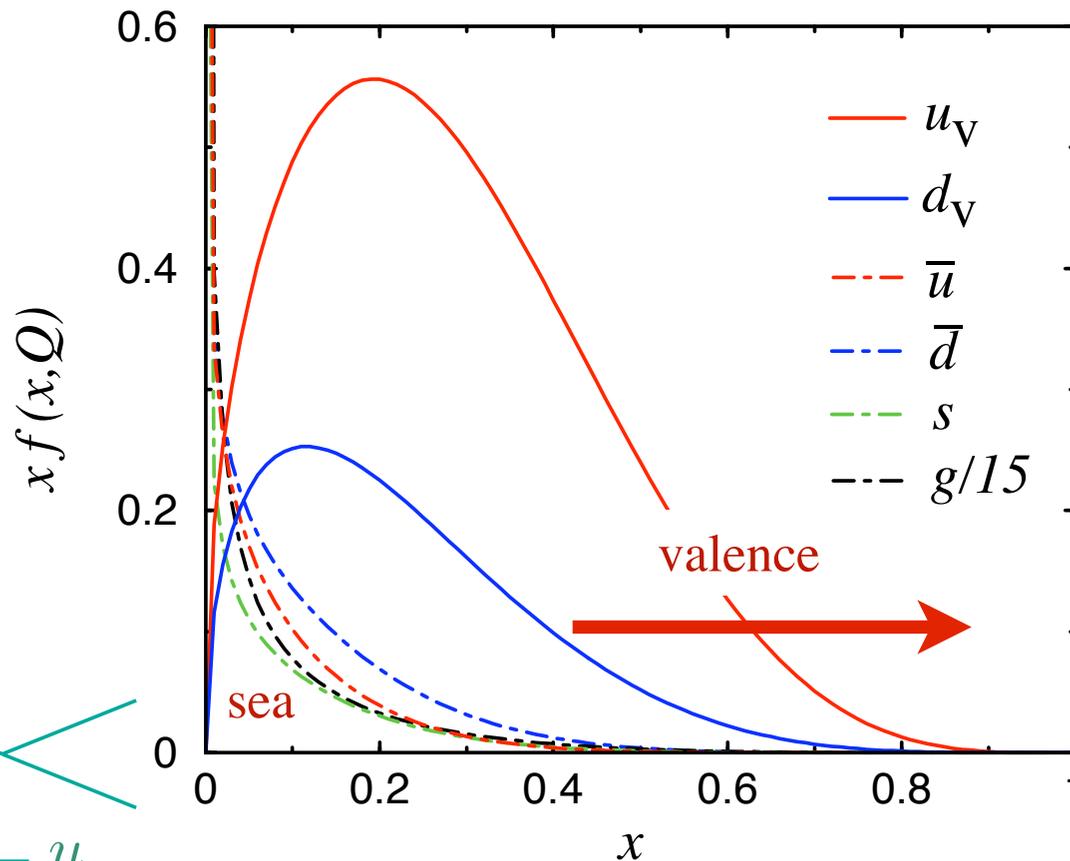


# Outline

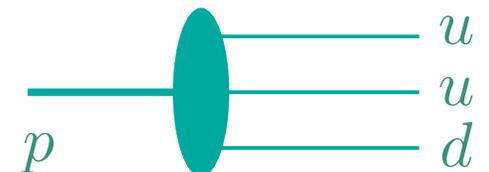
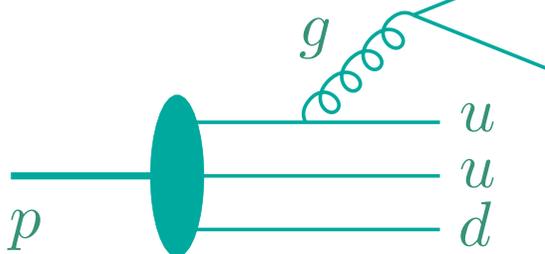
- Why are high-momentum (large  $x$ ) quarks in the nucleon important?
- Extraction of neutron structure from inclusive data
  - nuclear effects &  $d/u$  PDF ratio
  - $Q^2$  dependence
- New global “CJ” (CTEQ–Jefferson Lab) analysis
  - first foray into high- $x$ , low- $Q^2$  region
  - surprising new results for  $d$  quark
- Future plans

# Why are PDFs at large $x$ interesting?

- Most direct connection between quark distributions and nonperturbative structure of nucleon is via *valence* quarks  
→ most cleanly revealed at  $x > 0.4$



structure of *hadron*  
or structure of *probe*?



# Why are PDFs at large $x$ interesting?

- Most direct connection between quark distributions and nonperturbative structure of nucleon is via *valence* quarks
- Predictions for  $x \rightarrow 1$  behavior of *e.g.*  $d/u$  ratio
  - scalar diquark dominance:  $d/u = 0$  *Feynman (1972)*
  - hard gluon exchange:  $d/u = 1/5$  *Farrar, Jackson (1975)*
  - SU(6) symmetry:  $d/u = 1/2$
- Needed to understand backgrounds in searches for *new physics* beyond the Standard Model at LHC or in  $\nu$  oscillation experiments
  - DGLAP evolution feeds low  $x$ , high  $Q^2$  from high  $x$ , low  $Q^2$

- At large  $x$ , valence  $u$  and  $d$  distributions extracted from  $p$  and  $n$  structure functions, *e.g.* at LO

$$\frac{1}{x}F_2^p \approx \frac{4}{9}u_v + \frac{1}{9}d_v$$

$$\frac{1}{x}F_2^n \approx \frac{4}{9}d_v + \frac{1}{9}u_v$$

- $u$  quark distribution well determined from *proton*
- $d$  quark distribution requires *neutron* structure function

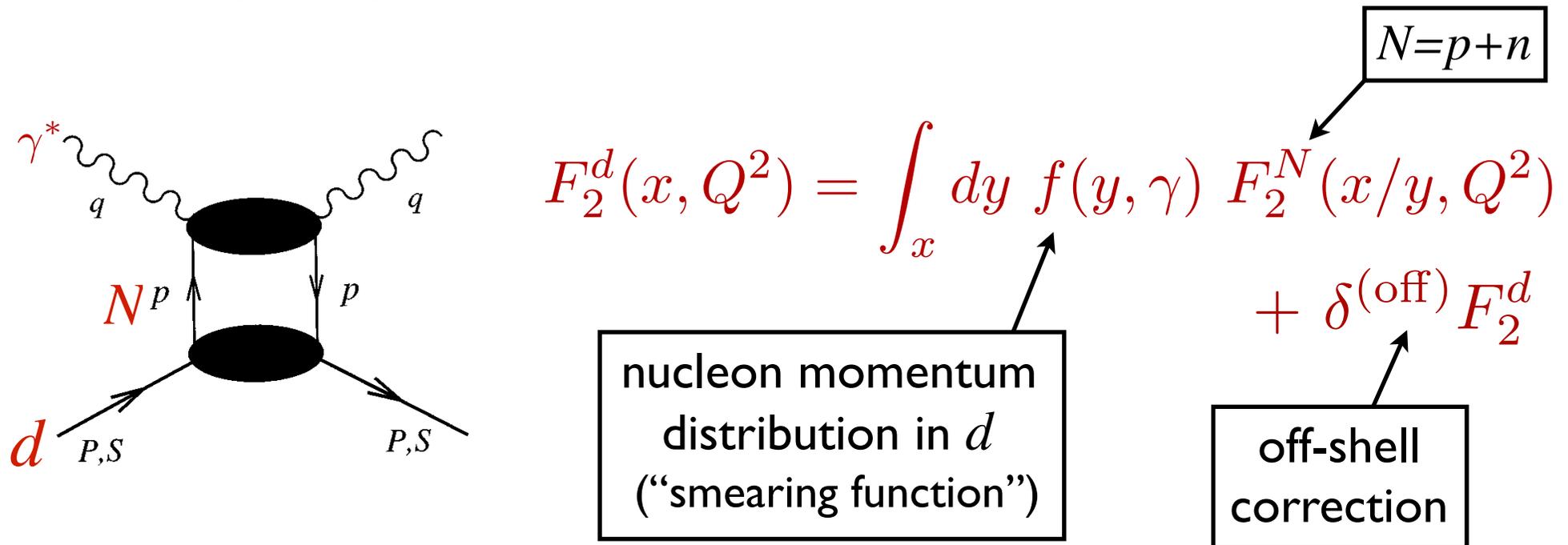
- No *free* neutron targets

- nuclear effects (nuclear binding, Fermi motion, shadowing)  
obscure neutron structure information

# Nuclear effects in the deuteron

## ■ Nuclear “impulse approximation”

→ incoherent scattering from individual nucleons in  $d$   
(good approx. at  $x \gg 0$ )



→  $y = p \cdot q / P \cdot q$  light-cone momentum fraction of  $d$  carried by  $N$

→ at finite  $Q^2$ , smearing function depends also on parameter

$$\gamma = |\mathbf{q}|/q_0 = \sqrt{1 + 4M^2 x^2 / Q^2}$$

# $N$ momentum distribution in $d$

$$f(y, \gamma) = \int \frac{d^3 p}{(2\pi)^3} |\psi_d(p)|^2 \delta\left(y - 1 - \frac{\varepsilon + \gamma p_z}{M}\right) \\ \times \frac{1}{\gamma^2} \left[ 1 + \frac{\gamma^2 - 1}{y^2} \left( 1 + \frac{2\varepsilon}{M} + \frac{\vec{p}^2}{2M^2} (1 - 3\hat{p}_z^2) \right) \right]$$

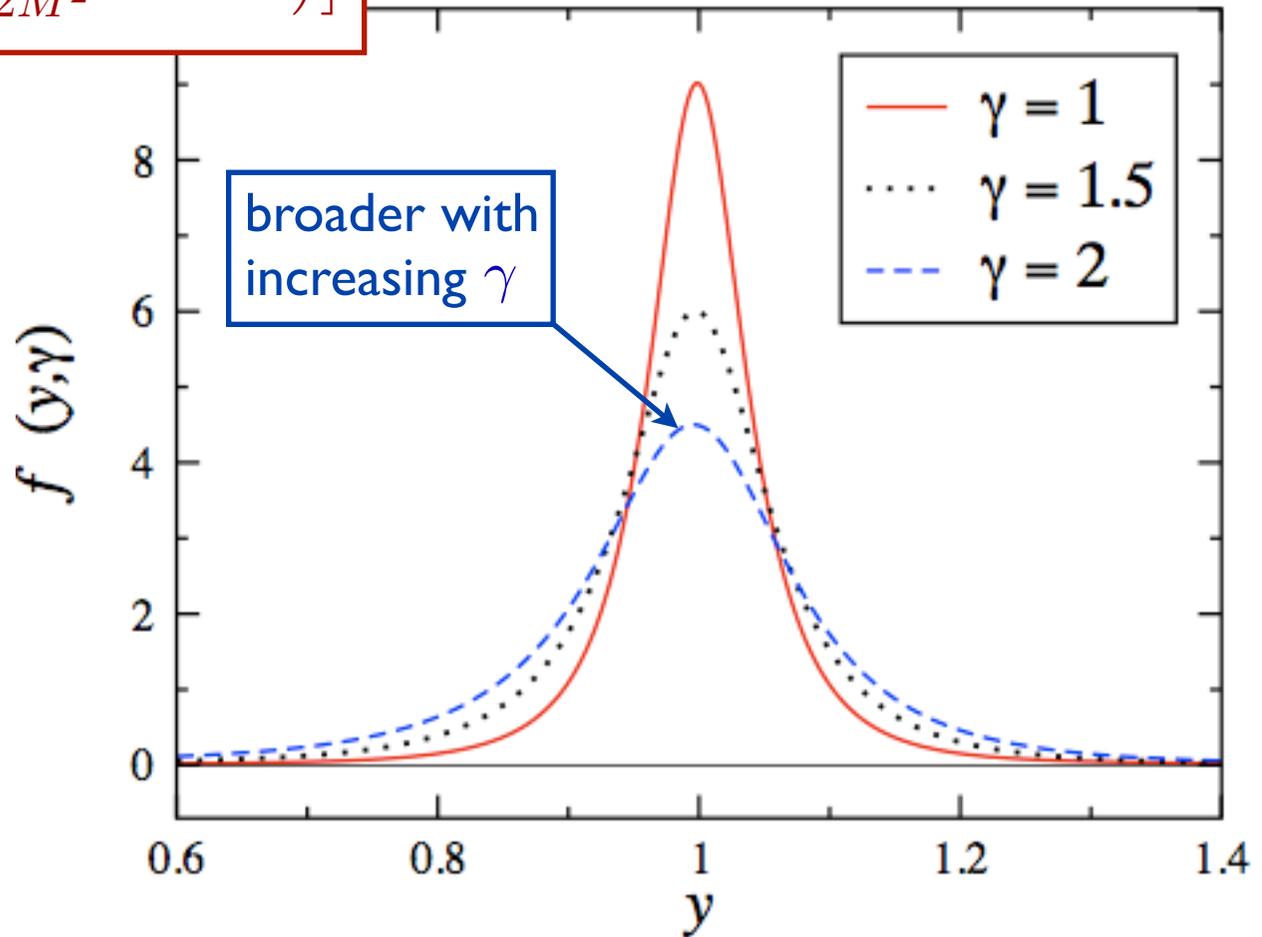
weak binding approximation (WBA):  
expand in powers of  $|\vec{p}|/M$

→ deuteron wave function  $\psi_d(p)$

→ deuteron separation energy

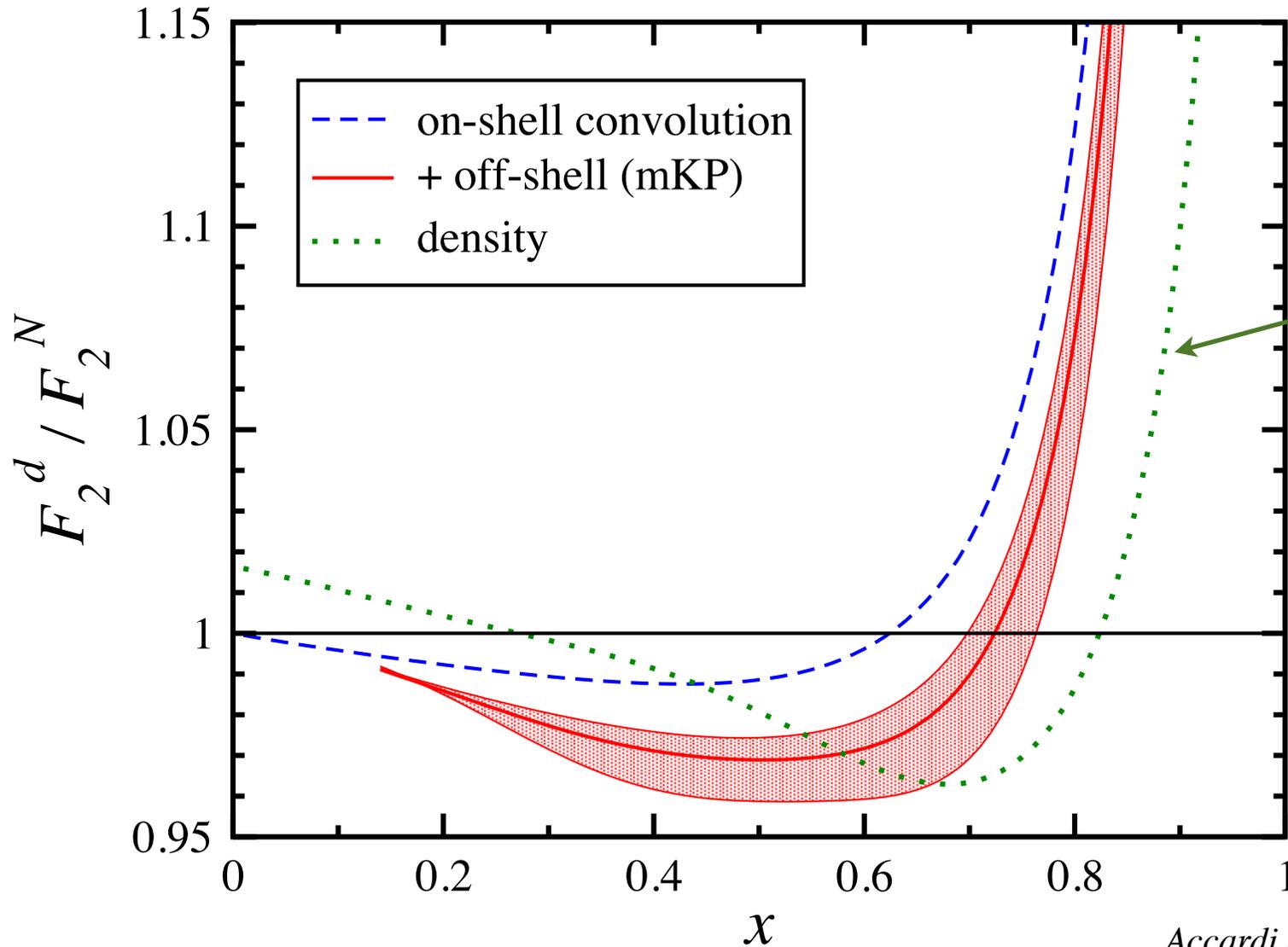
$$\varepsilon = \varepsilon_d - \frac{\vec{p}^2}{2M}$$

→ effectively more smearing for larger  $x$  or lower  $Q^2$



Kahn, WM, Kulagin, PRC 79, 035205 (2009)

# “EMC effect” in deuteron



nuclear density

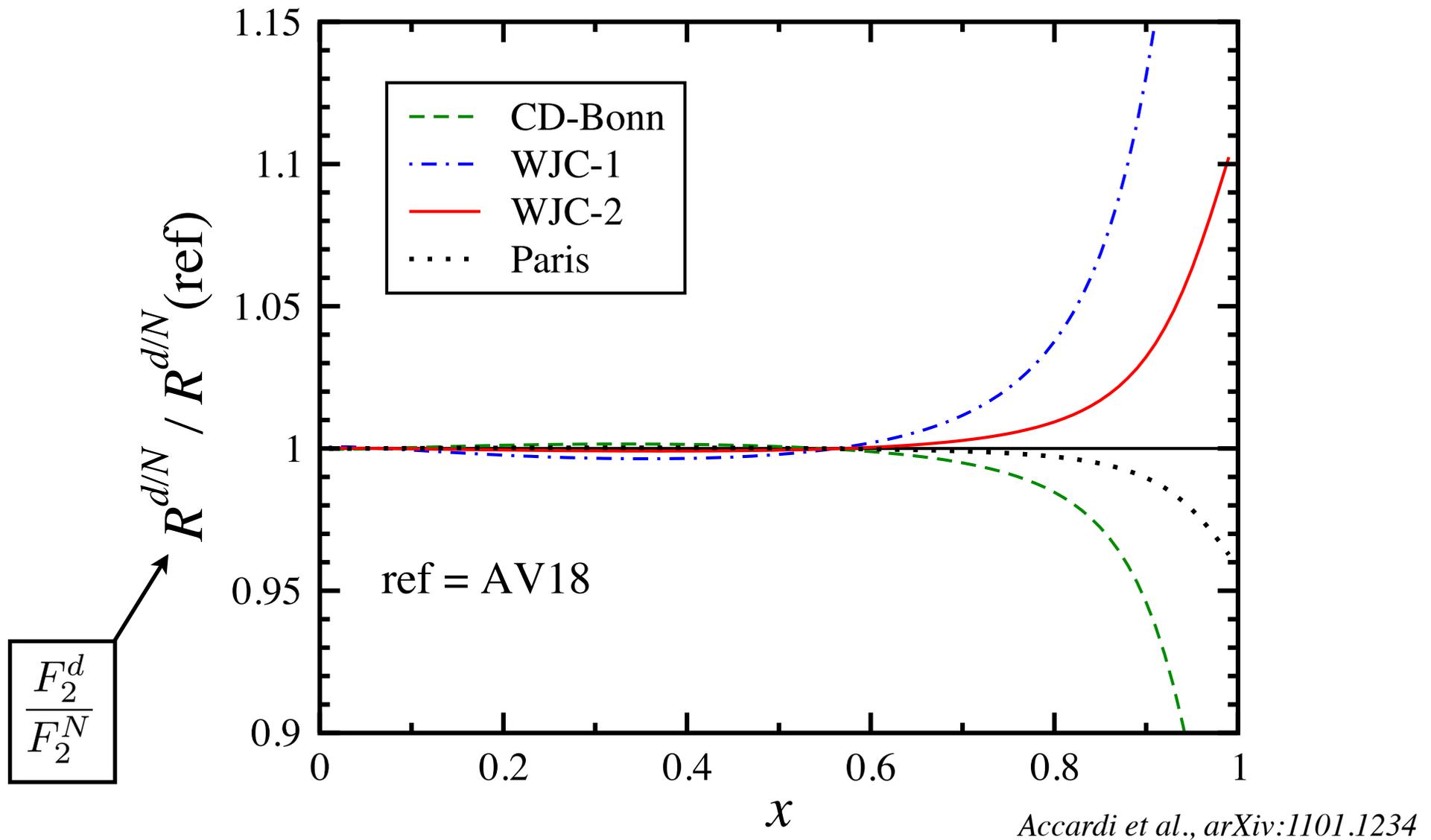
$$\frac{F_2^d}{F_2^N} - 1 \approx \frac{1}{4} \left( \frac{F_2^{\text{Fe}}}{F_2^d} - 1 \right)$$

assumes EMC effect scales with density; extrapolated from Fe  $\rightarrow$  deuterium

*Accardi et al., arXiv:1101.1234*

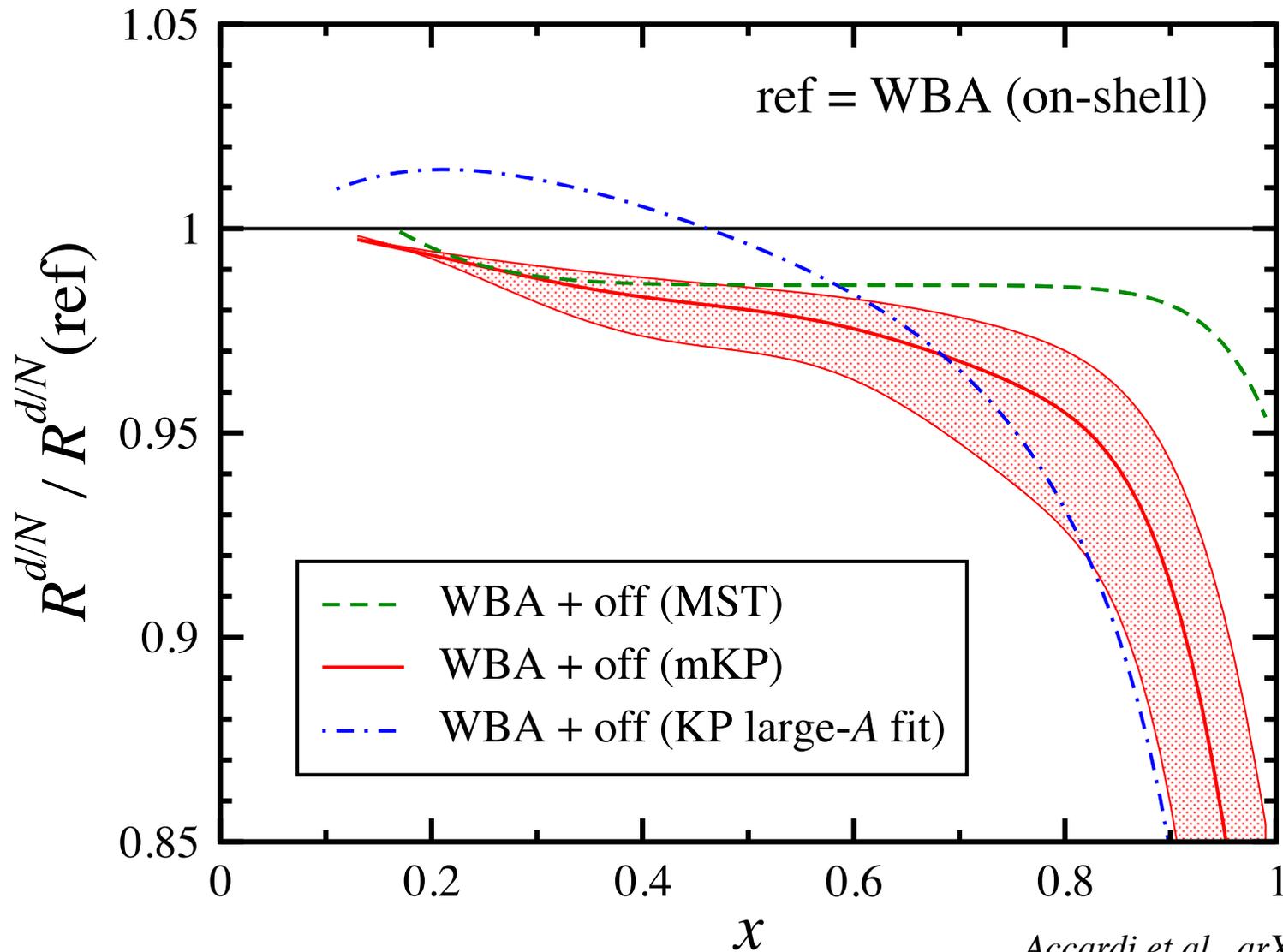
$\rightarrow \approx 2\text{--}4\%$  depletion at  $x \sim 0.4\text{--}0.6$ , depending on model

■ Model dependence:  $NN$  interaction at short distances

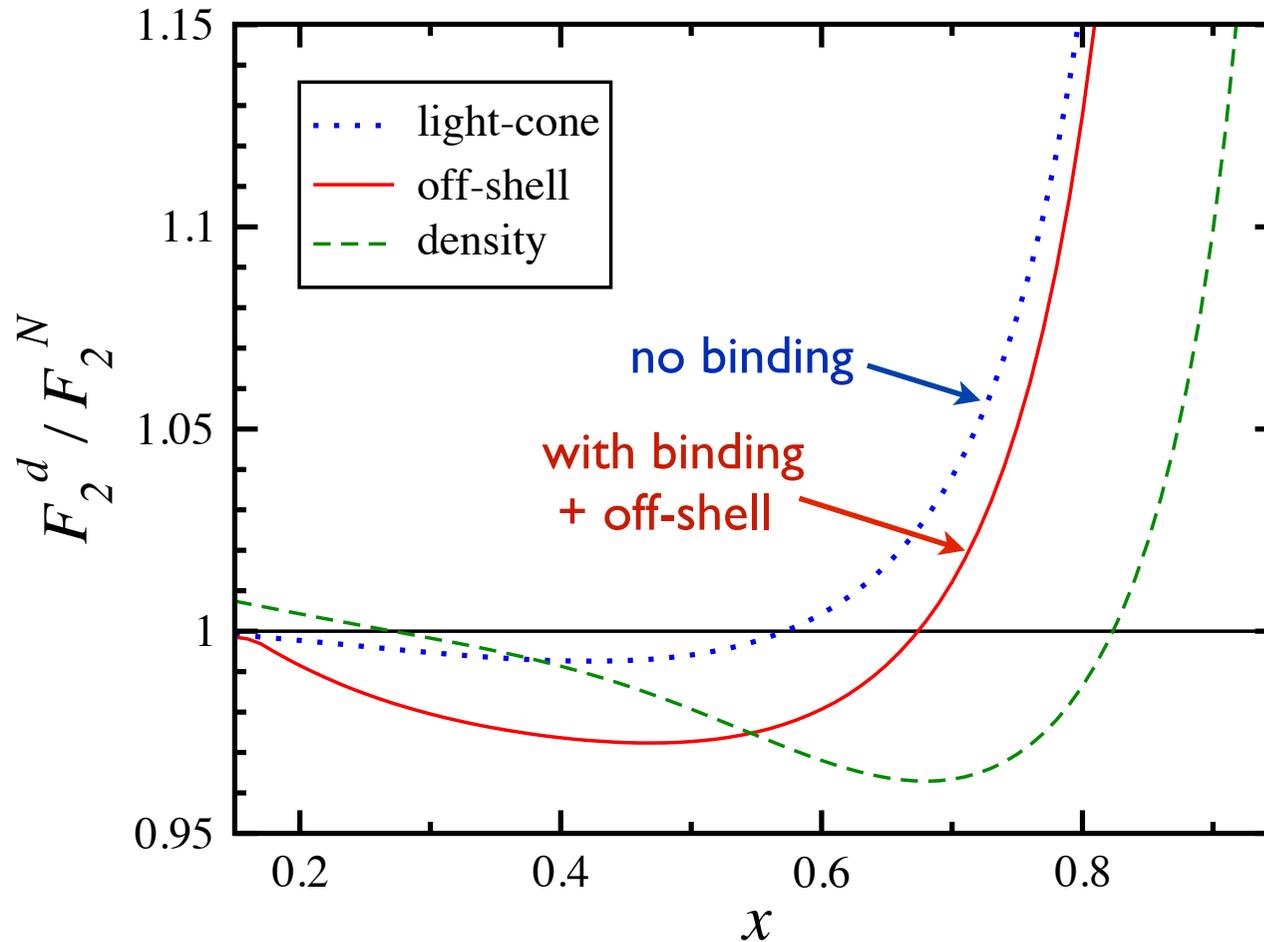


→ high  $x$  probes large- $y$  tail of momentum distribution

## ■ Model dependence: nucleon off-shell corrections

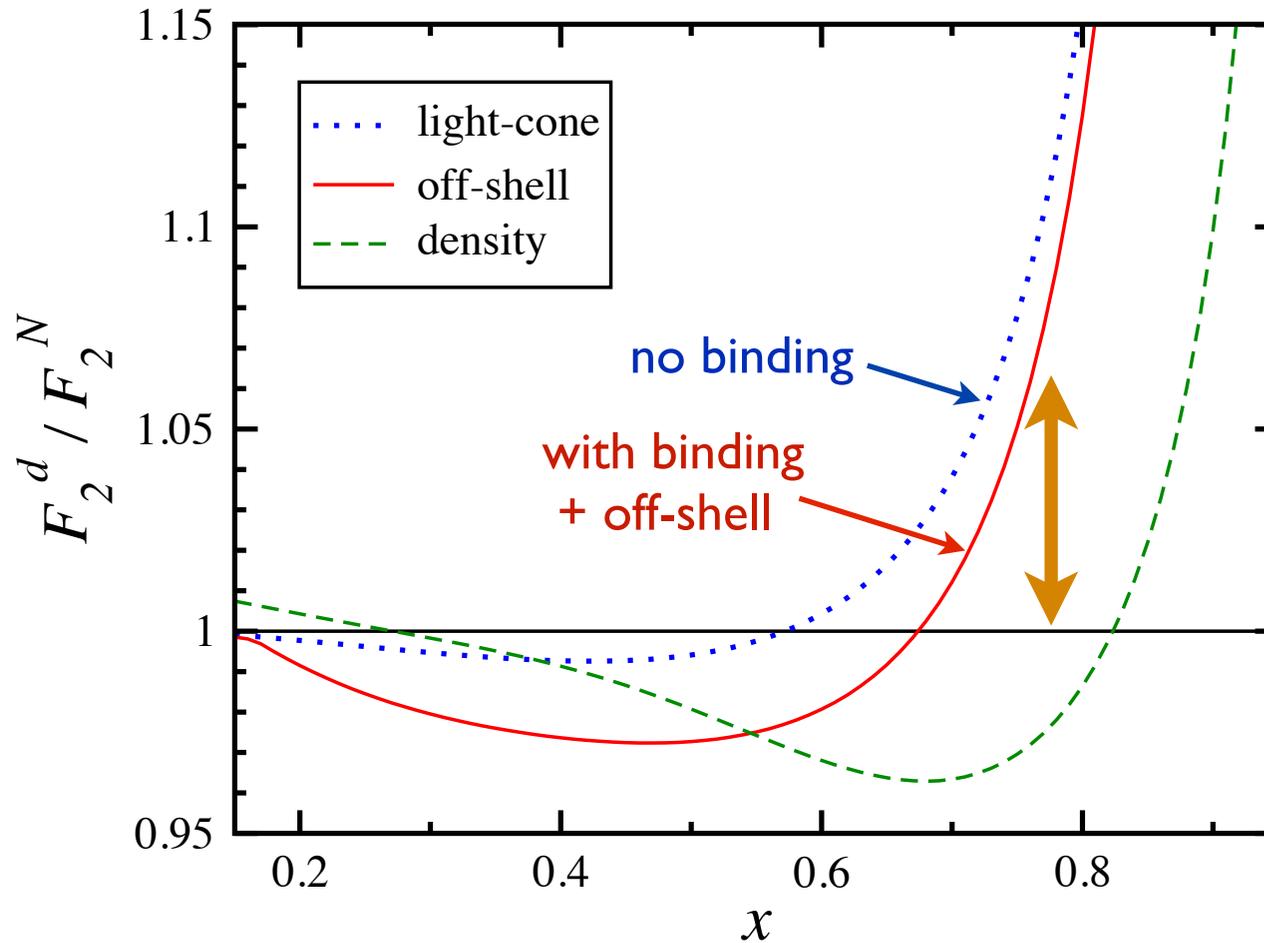


→ additional few % suppression at large  $x$



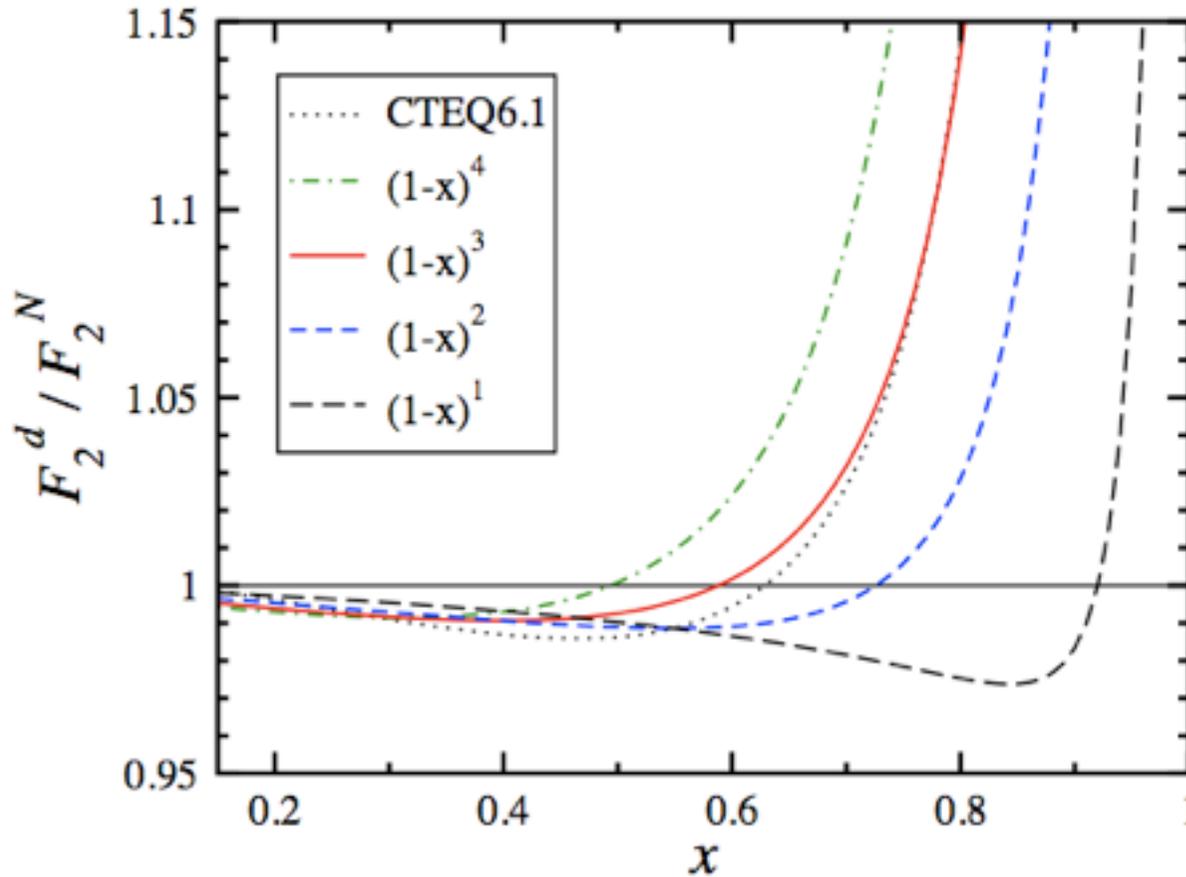
→  $\sim 2-3\%$  reduction of  $F_2^d / F_2^N$  at  $x \sim 0.5-0.6$   
with steep rise for  $x > 0.6-0.7$

→ larger EMC effect at  $x \sim 0.5-0.6$  with  
binding + off-shell corrections *cf.* light-cone



- using off-shell model, will get *larger* neutron *cf. light-cone* model
- but will get *smaller* neutron *cf. no nuclear effects* or *density* model

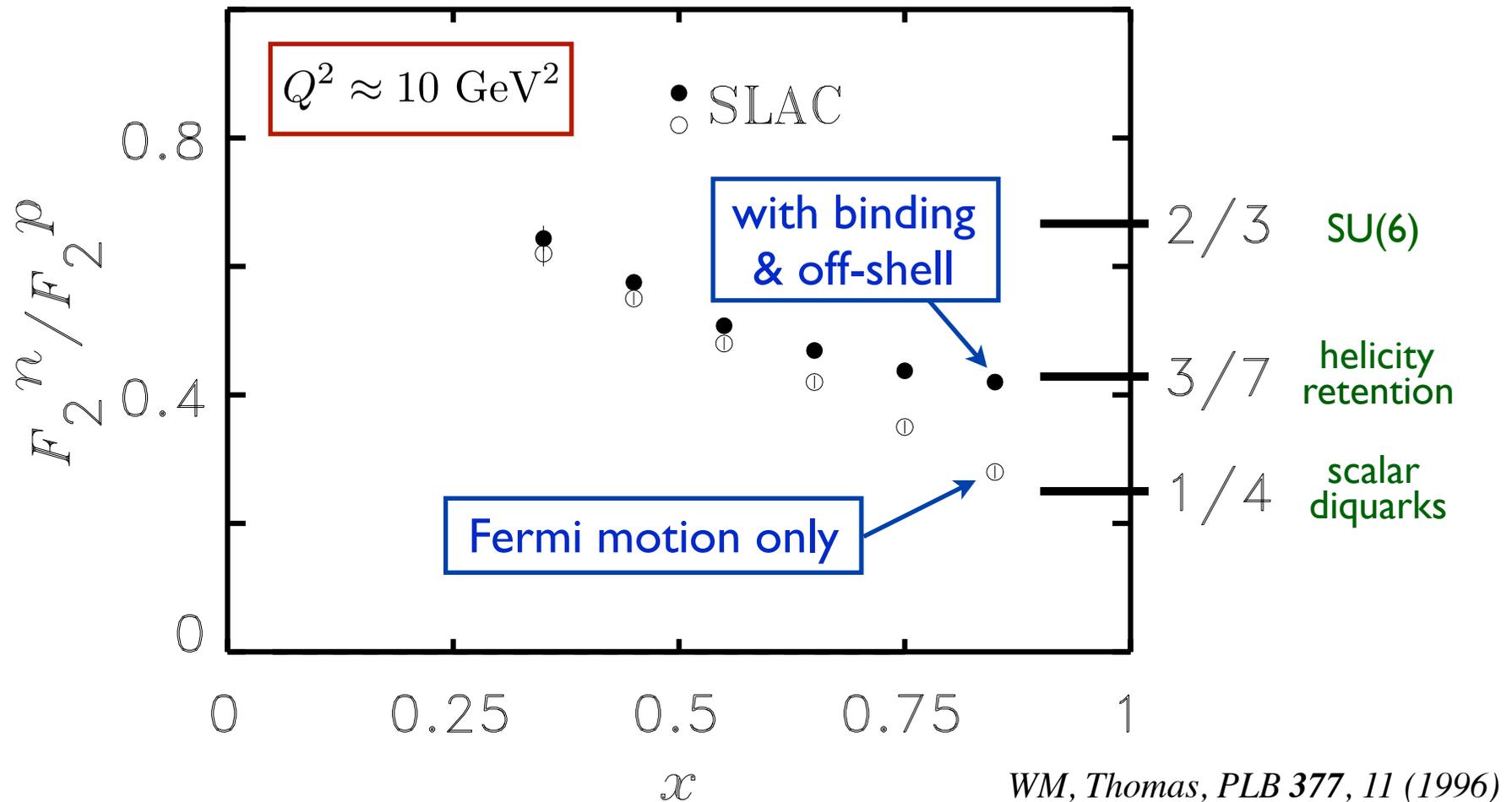
# ⚠ WARNING ⚠



→ EMC ratio depends also on *input nucleon SFs*;  
need to iterate when extracting  $F_2^n$

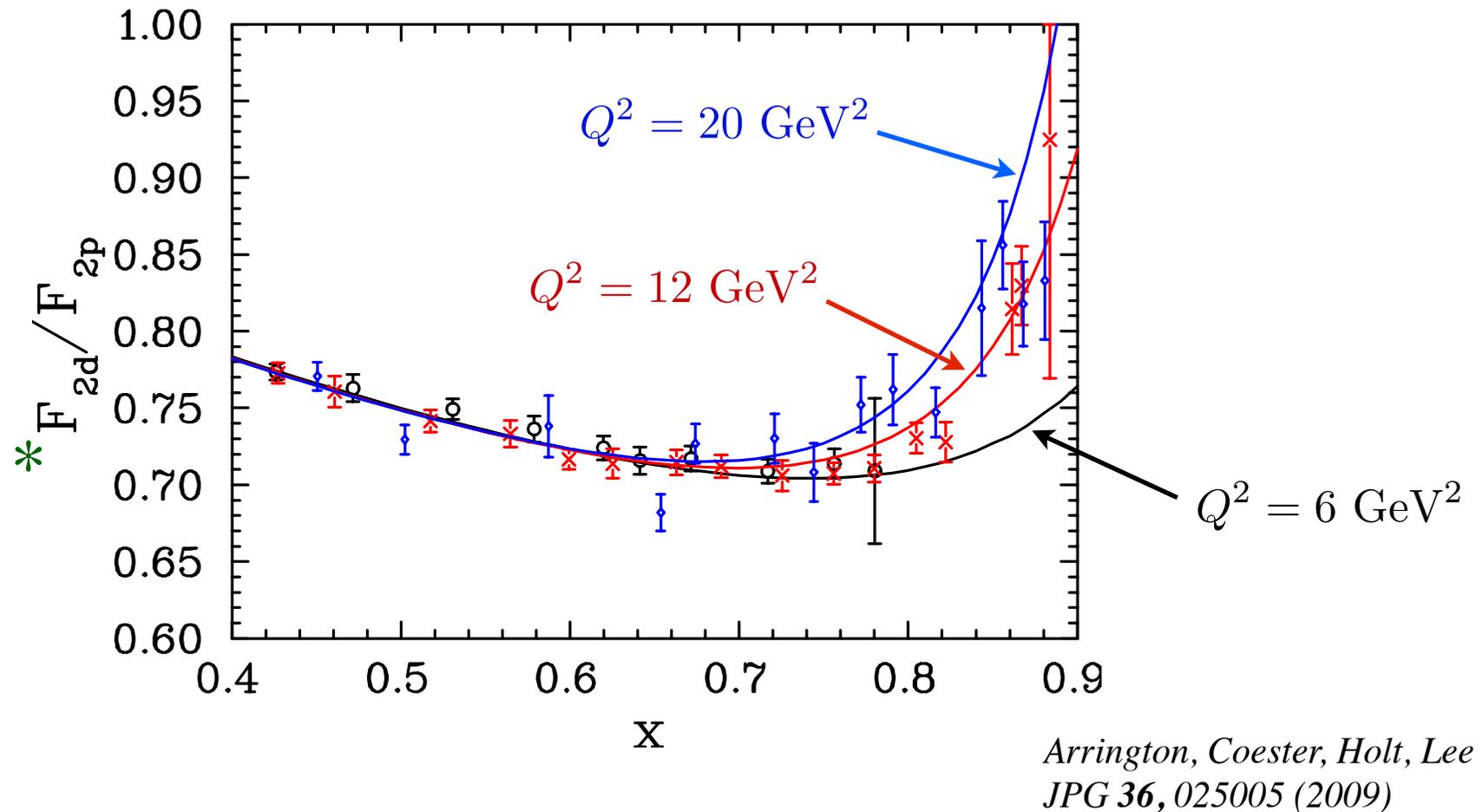
# Extraction of neutron SF from inclusive data

■ Impact of nucleon off-shell corrections (+ iteration)



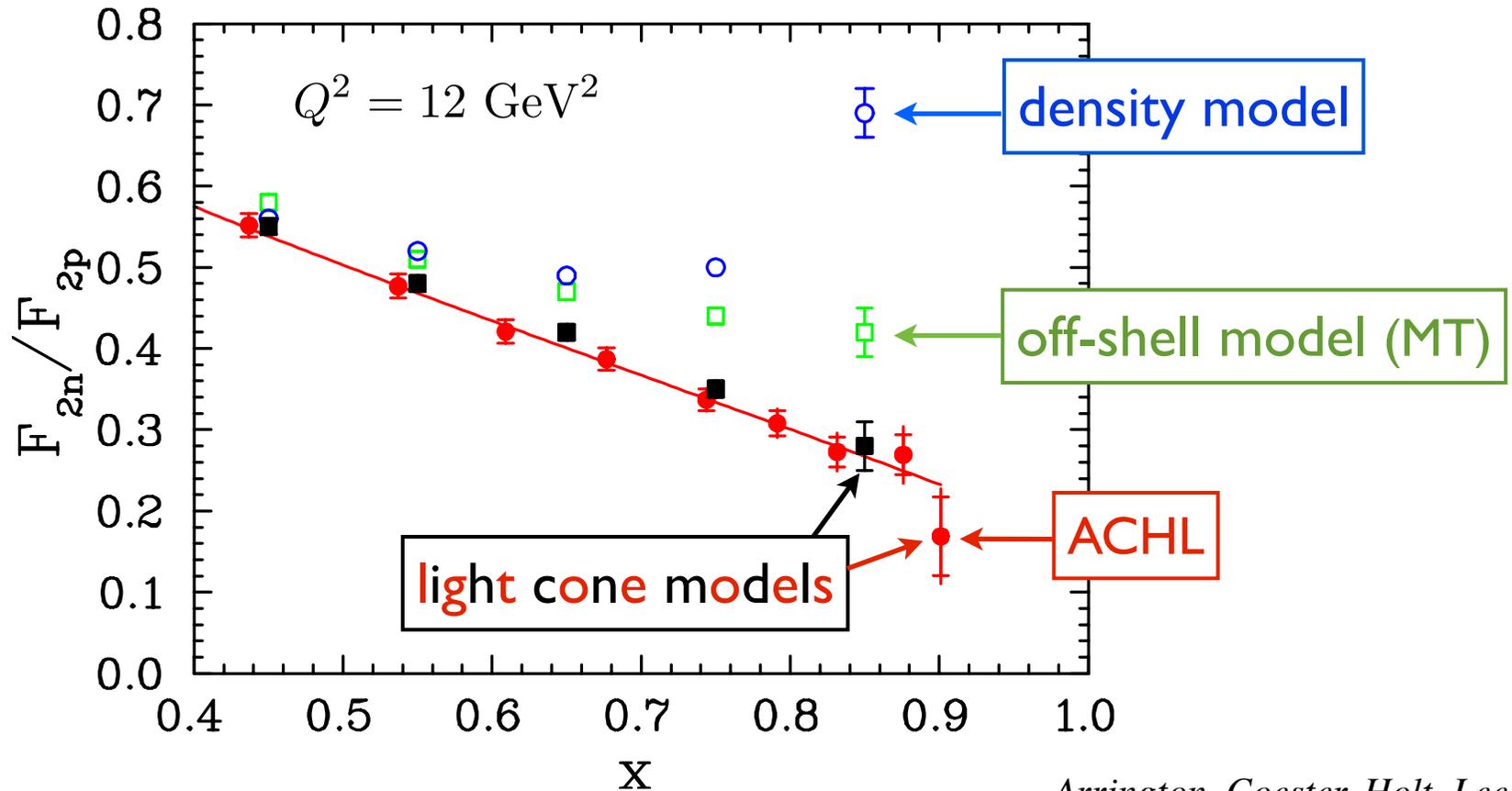
→ without EMC effect in  $d$ ,  $F_2^n$  underestimated at large  $x$

- Important to account for  $Q^2$  dependence of data at large  $x$



- \*  $F_2^d$  computed using smearing ratios  $S_N = F_2^{N/d} / F_2^N$   
in light-cone model

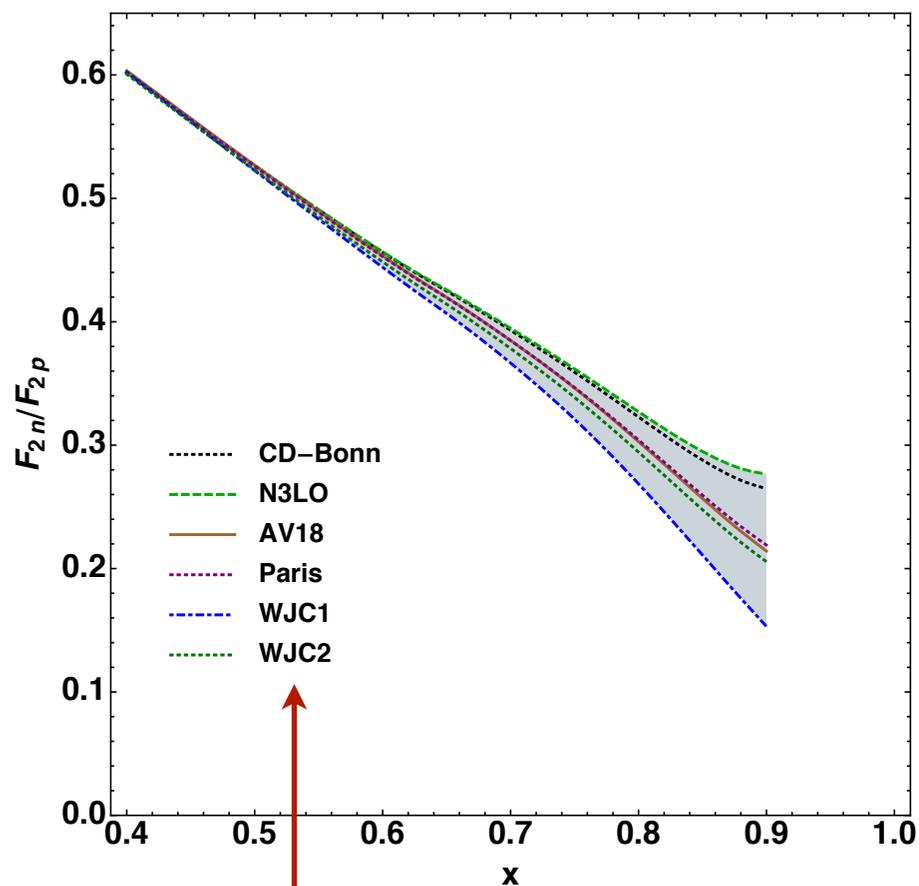
- Important to account for  $Q^2$  dependence of data at large  $x$



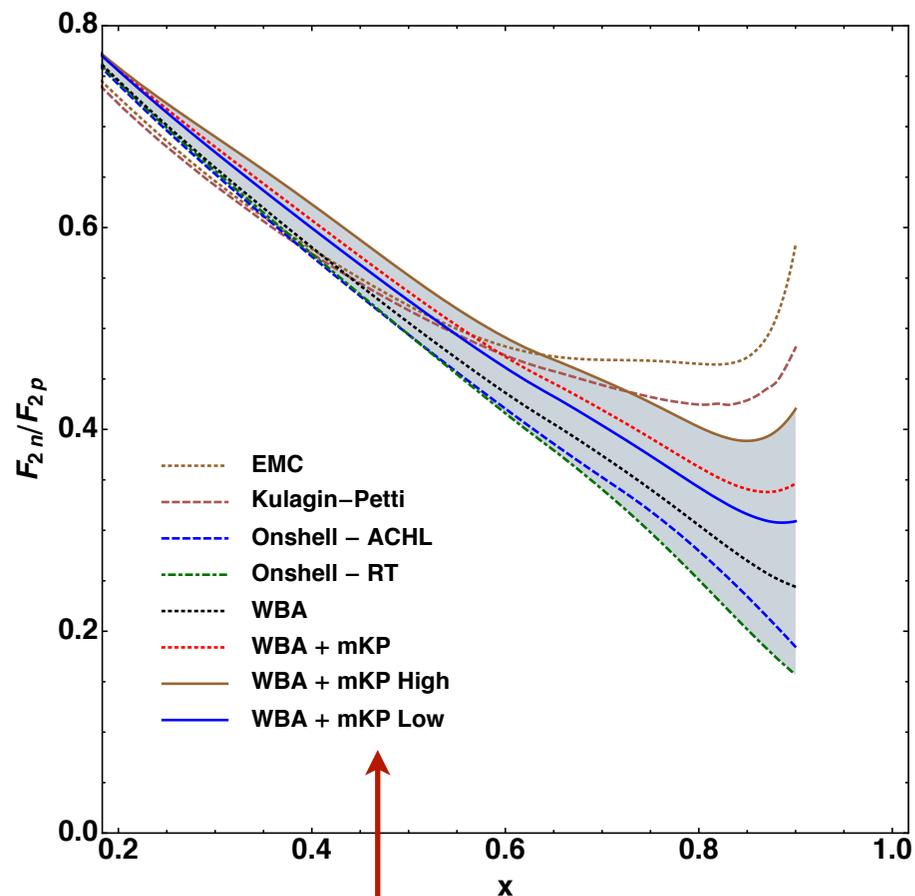
Arrington, Coester, Holt, Lee  
*JPG 36, 025005 (2009)*

- nuclear model dependence consistent with earlier findings  
 (NB:  $F_2^n / F_2^p$  ratio here *not* constrained by 1/4 PDF-positivity bound)

# Deuteron model dependence explored in subsequent analysis



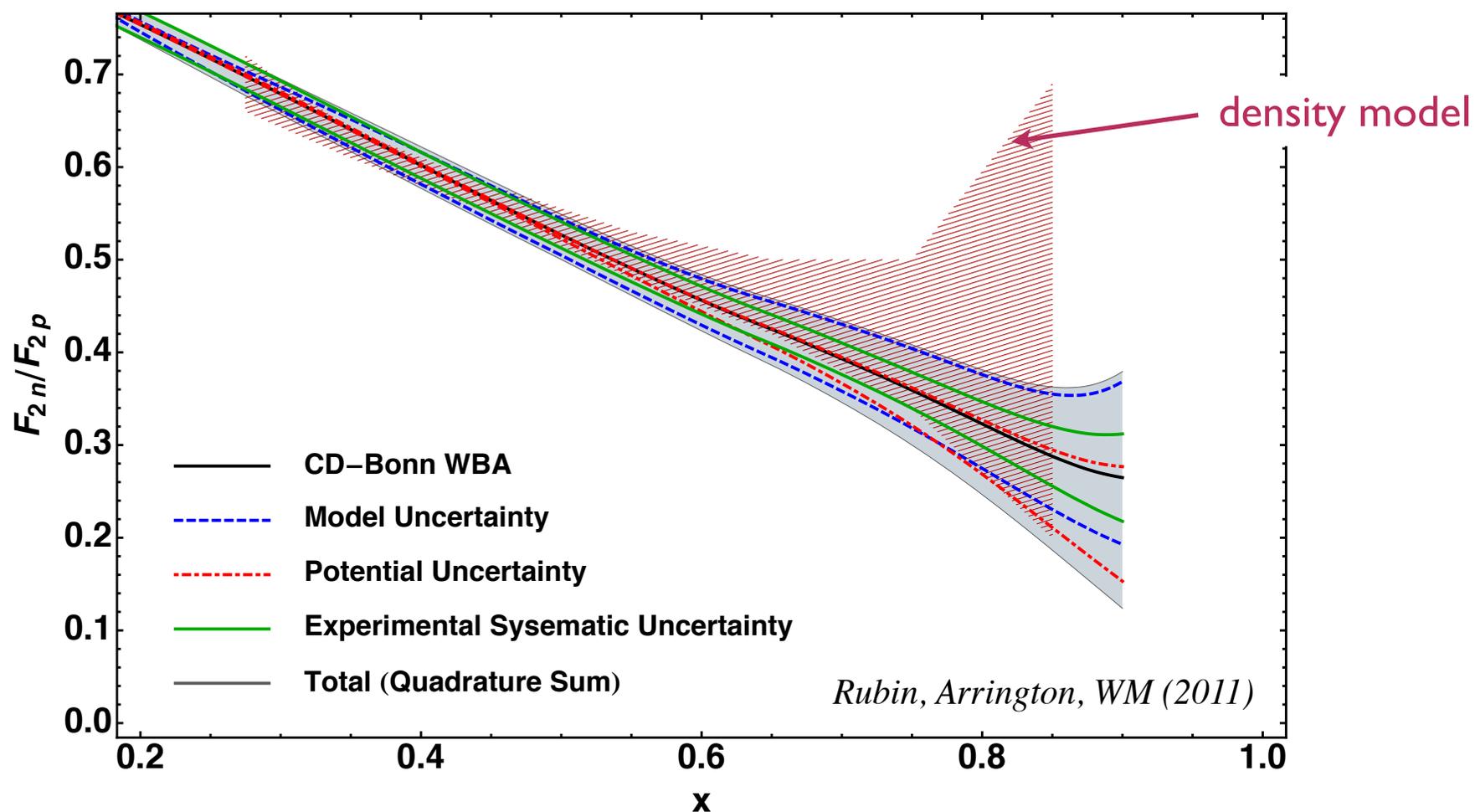
deuteron wave function dependence



nucleon on-shell / off-shell model dependence

*Rubin, Arrington, WM (2011)*

## ■ Deuteron model dependence explored in subsequent analysis



- total uncertainty band smaller than “full” range of models (including *e.g.* density model)
- significant *cf.* usual assumptions made in global PDF analyses

# New global analysis: “CJ” (CTEQ-JLab) collaboration

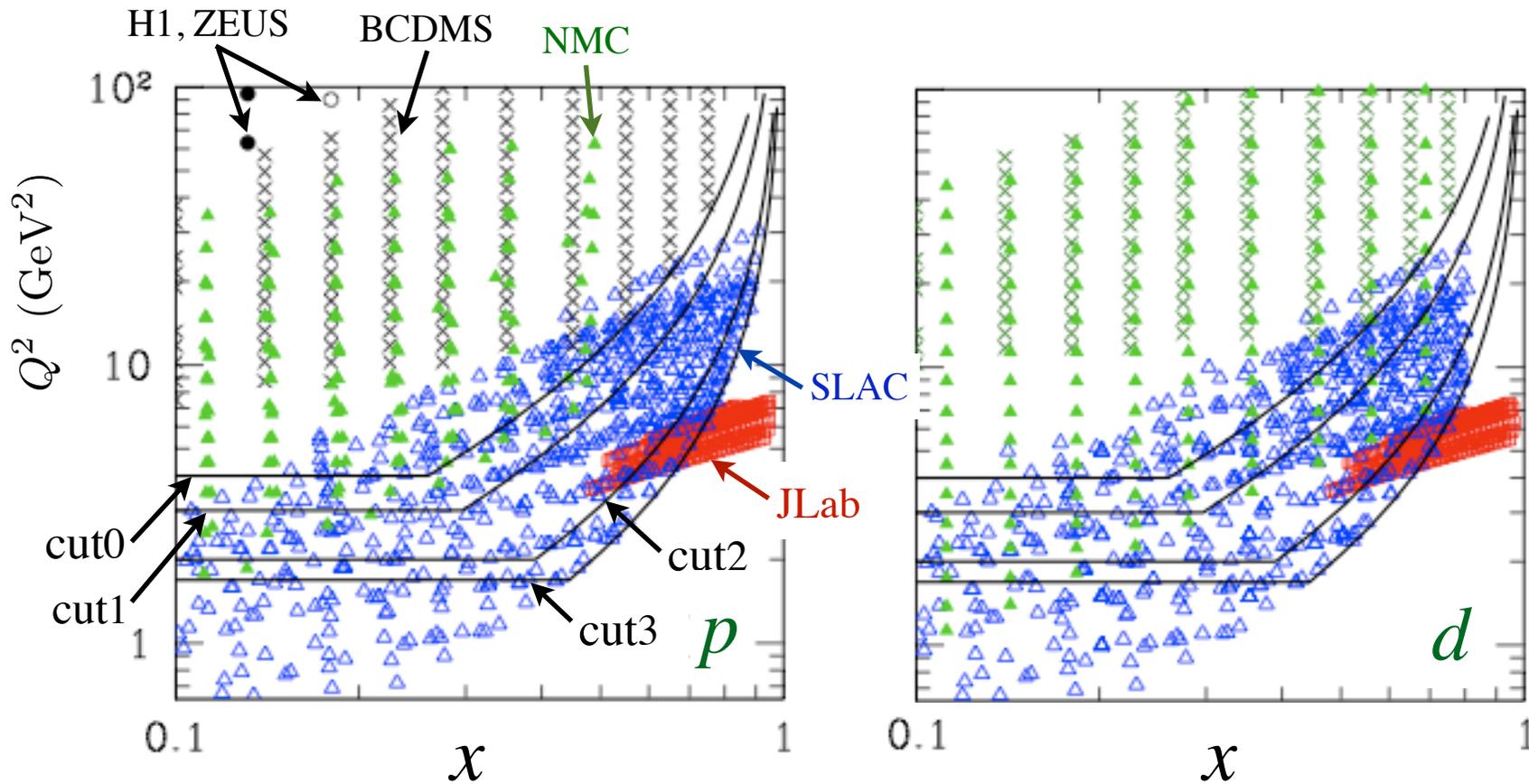
A. Accardi, E. Christy, C. Keppel, S. Malace,  
W. Melnitchouk, P. Monaghan, J. Morfin, J. Owens, L. Zhu

*Accardi et al., Phys. Rev. D 81, 034016 (2010)*

*Accardi et al., arXiv:1101.1234, to appear in PRD*

- Next-to-leading order (NLO) analysis of expanded set of *proton* and *deuterium* data, including large- $x$ , low- $Q^2$  region
  - also include new CDF & D0  $W$ -asymmetry, and E866 DY data
- Systematically study effects of  $Q^2$  &  $W$  cuts
  - as low as  $Q \sim m_c$  and  $W \sim 1.7$  GeV
- Include subleading  $1/Q^2$  corrections
  - target mass corrections & dynamical higher twists
- Correct for *nuclear* effects in the deuteron (binding + off-shell)
  - most global analyses assume *free* nucleons; some use density model, a few assume Fermi motion only

# Kinematic cuts



cut0:  $Q^2 > 4 \text{ GeV}^2, W^2 > 12.25 \text{ GeV}^2$

cut1:  $Q^2 > 3 \text{ GeV}^2, W^2 > 8 \text{ GeV}^2$

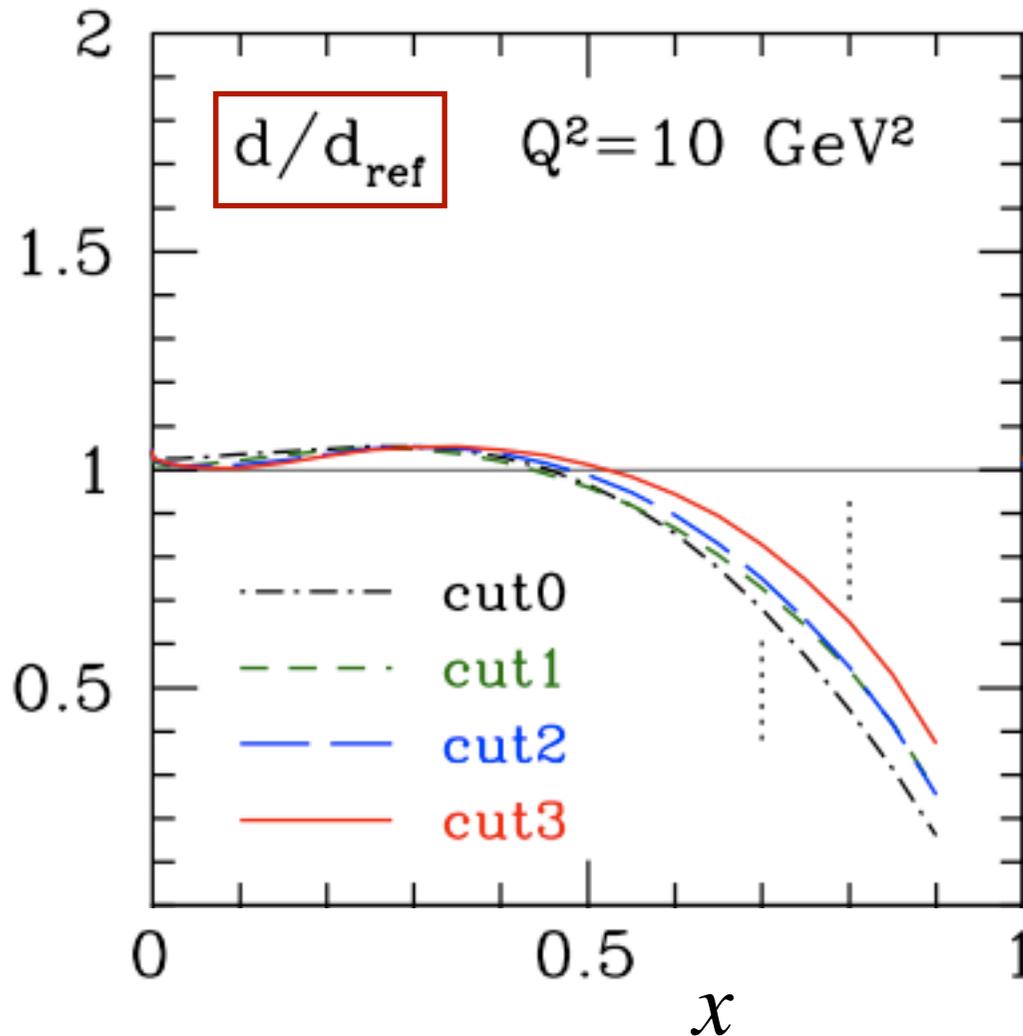
cut2:  $Q^2 > 2 \text{ GeV}^2, W^2 > 4 \text{ GeV}^2$

cut3:  $Q^2 > m_c^2, W^2 > 3 \text{ GeV}^2$

factor 2 increase  
in DIS data from  
cut0  $\rightarrow$  cut3

## Effect of $Q^2$ & $W$ cuts

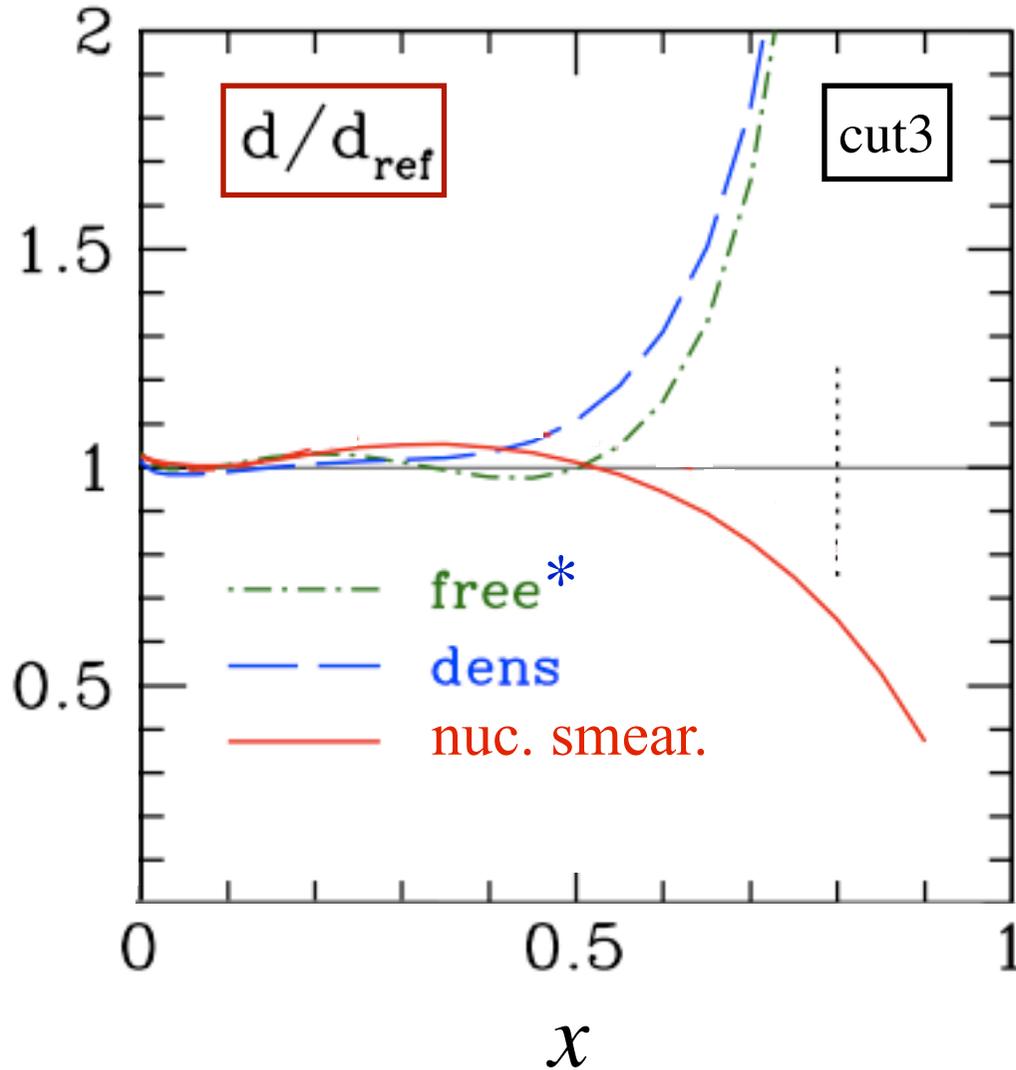
- Systematically reduce  $Q^2$  and  $W$  cuts
- Fit includes TMCs, HT term, nuclear corrections



→ *stable* with respect to cut reduction

→ *d* quark suppressed by  $\sim 50\%$  for  $x > 0.5$  (driven by nuclear corrections)

# Nuclear corrections



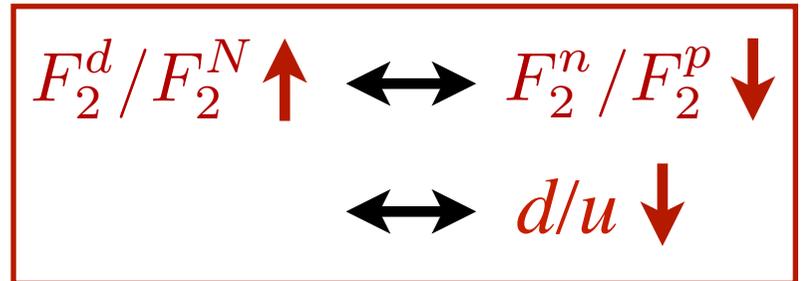
\* assumes  $F_2^d = F_2^p + F_2^n$  as in CTEQ6.1 and most other global fits

→ increased  $d$  quark for no nuclear effects  
(compensates for nuclear smearing in deuteron → increased  $F_2^d$ )

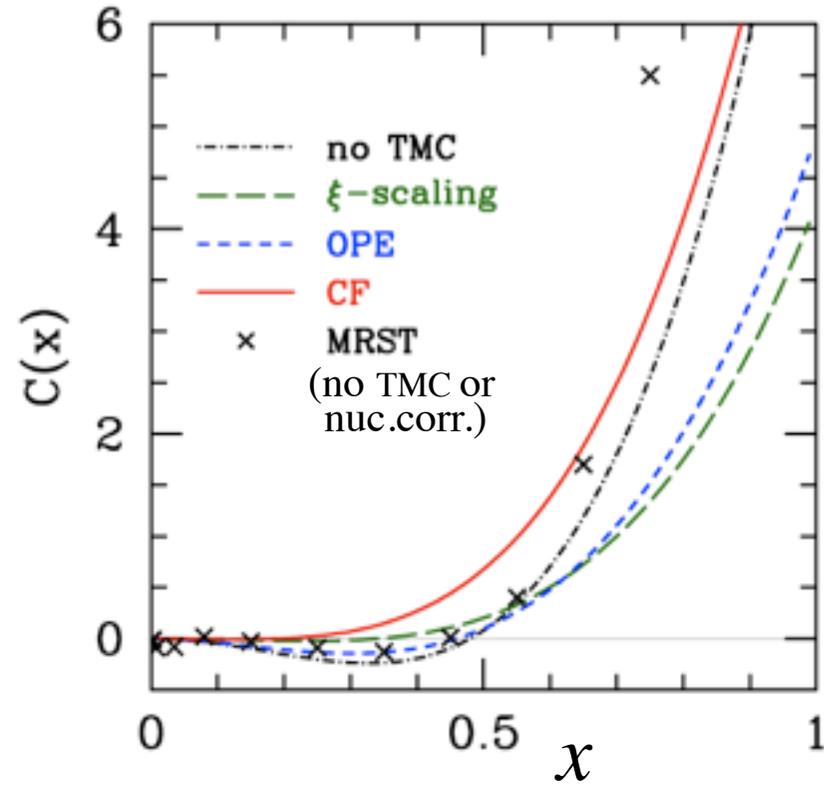
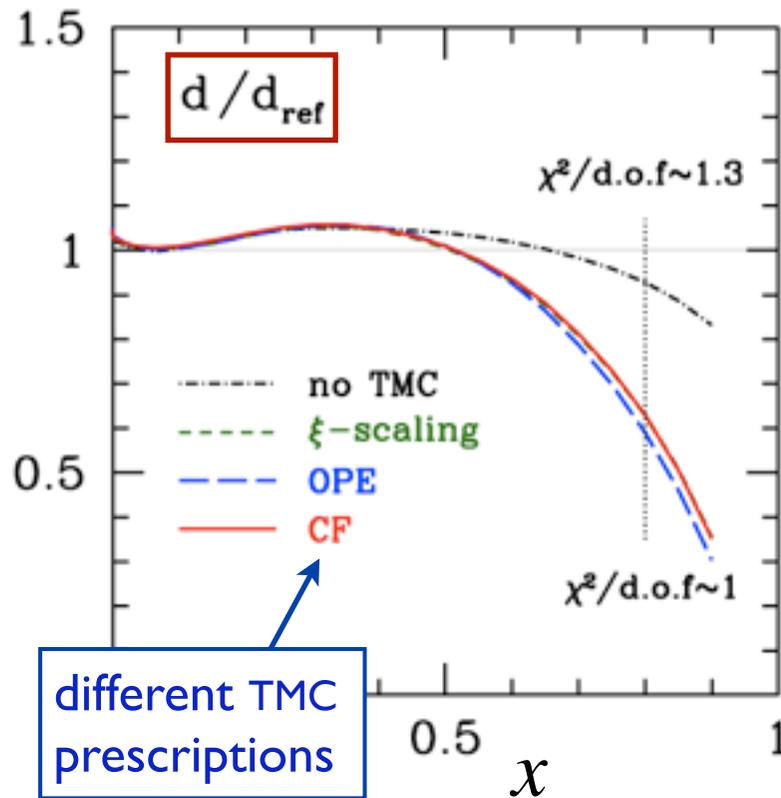
→ decreased  $d$  quark for nuclear smearing models



$F_2^d / F_2^N > 1$  for  $x \sim 0.6-0.8$   
while  $F_2^d / F_2^N < 1$  for “free” and “density” models

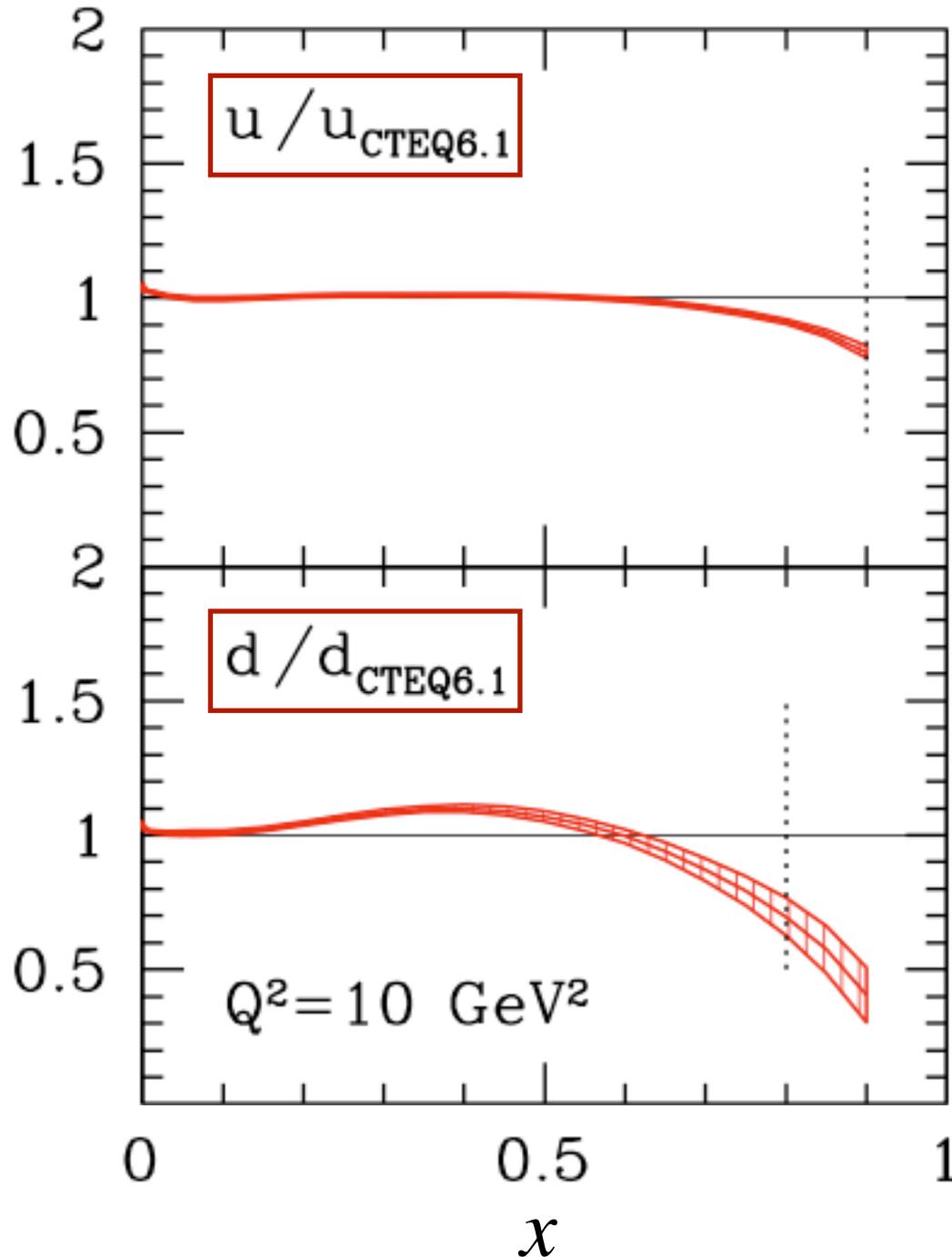


# Effect of $1/Q^2$ corrections



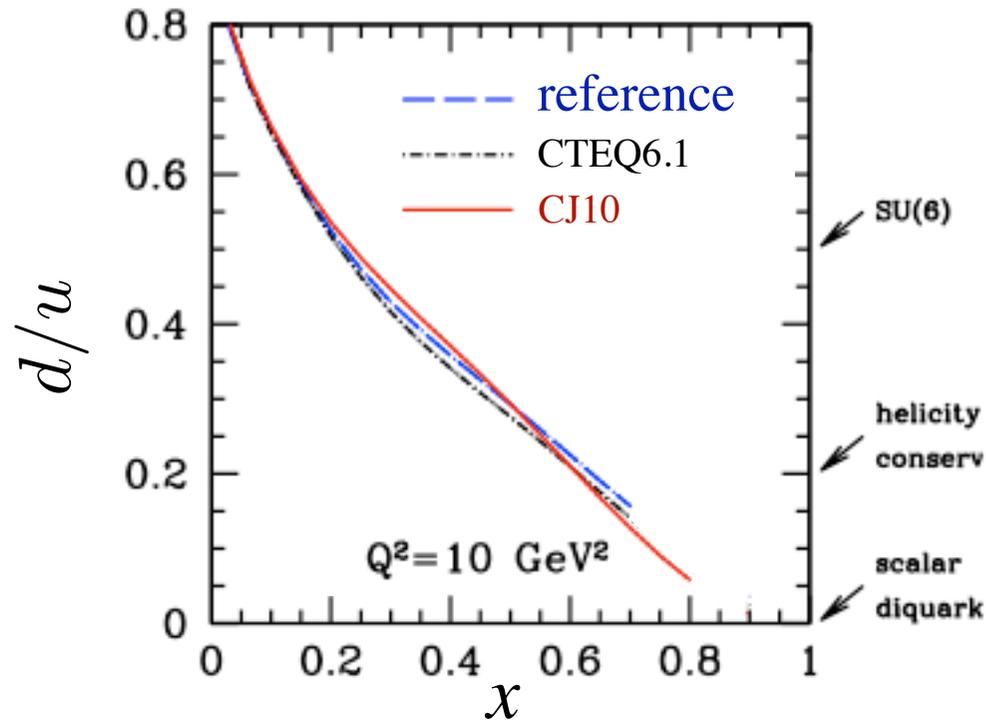
- $1/Q^2$  correction  $F_2 = F_2^{\text{LT}} \left( 1 + \frac{C(x)}{Q^2} \right)$ ,  $C(x) = c_1 x^{c_2} (1 + c_3 x)$
- important interplay between TMCs and higher twist: HT alone *cannot* accommodate full  $Q^2$  dependence
- stable leading twist when both TMCs and HTs included

# CJ10 PDF results



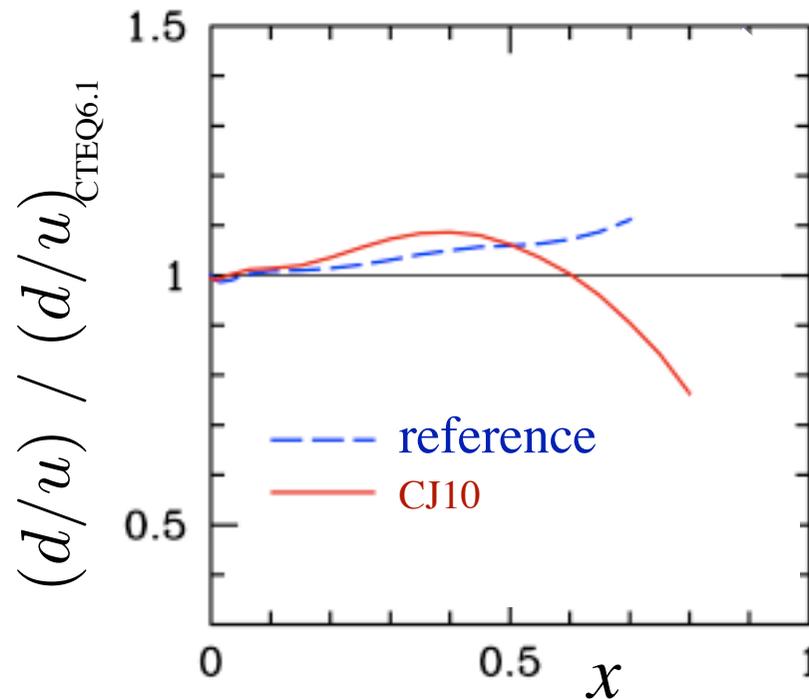
→ full fits favors smaller  $d/u$  ratio

# CJ10 PDF results

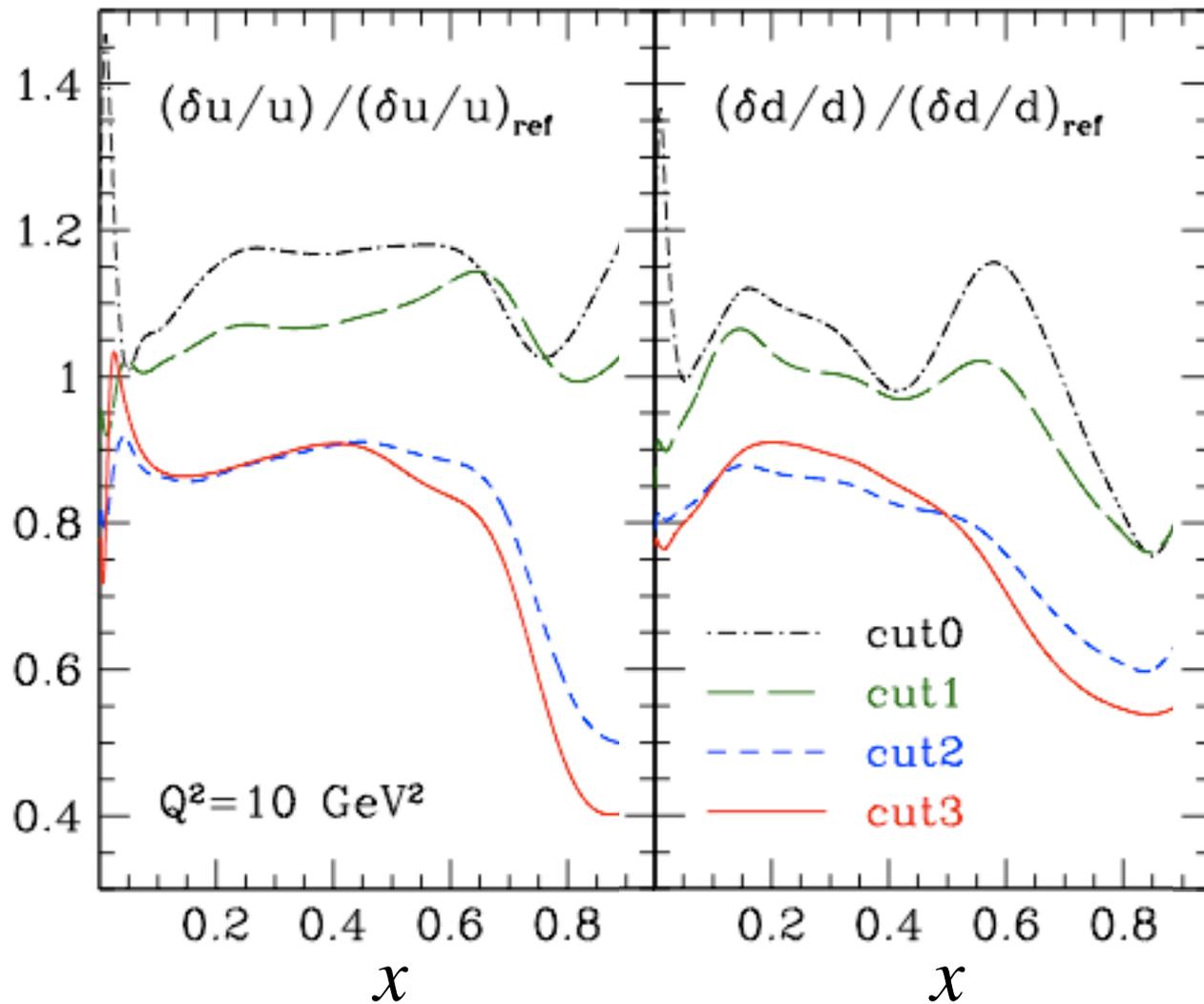


→ full fits favors smaller  $d/u$  ratio

→ dominance of non-pQCD physics (cf. hard  $g$  exchange)



# CJ10 PDF results



→ full fits favors smaller  $d/u$  ratio

→ dominance of non-pQCD physics (*cf.* hard  $g$  exchange)

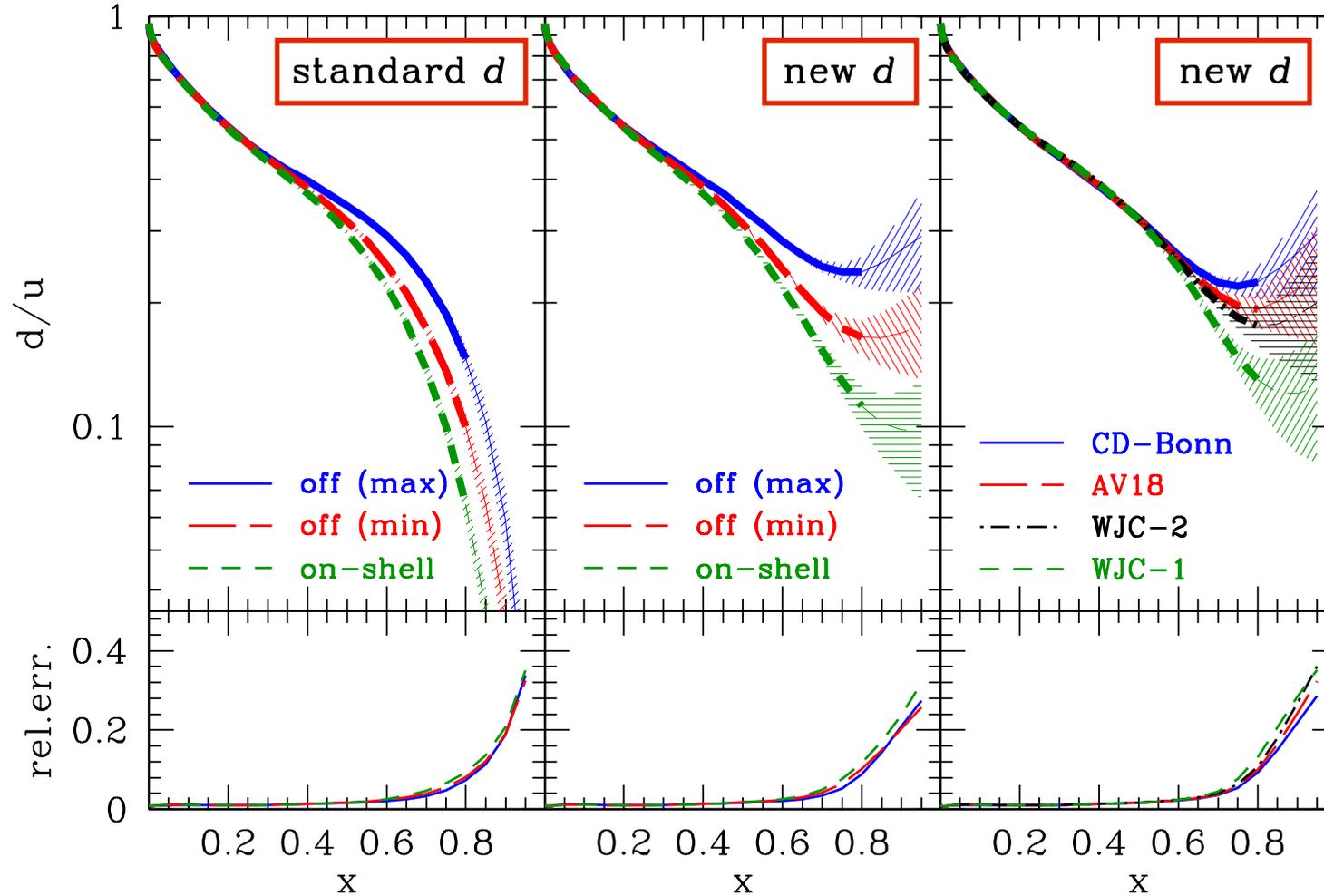
→ significantly reduced errors with weaker cuts

# New CJ11 PDF analysis

- Explore dependence of PDF fits on deuteron wave functions and nucleon off-shell corrections
  - use only “high-precision” wave functions (AV18, CD-Bonn, WJC-1, WJC-2)
  - off-shell model bounds given by upper & lower limits of “mKP” model parameters
- Dependence of  $d/u$  ratio on  $d$  quark parametrization
  - allow for finite, nonzero ratio in  $x = 1$  limit

$$d(x, Q^2) \rightarrow d(x, Q^2) + a x^b u(x, Q^2)$$

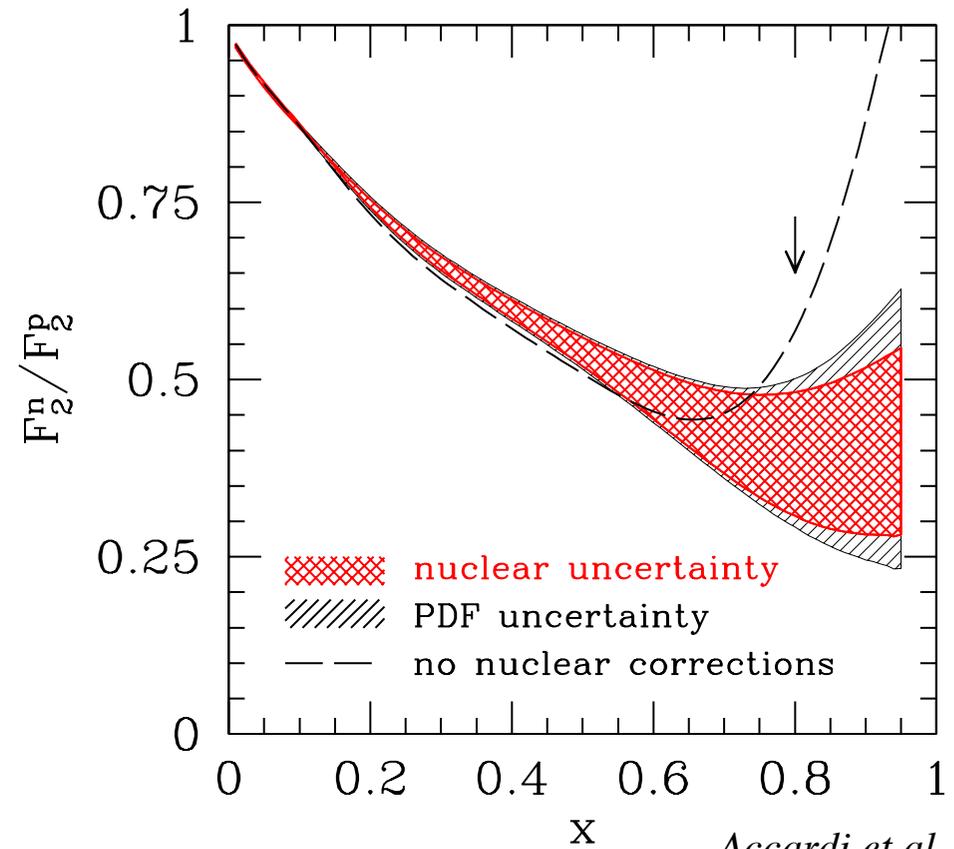
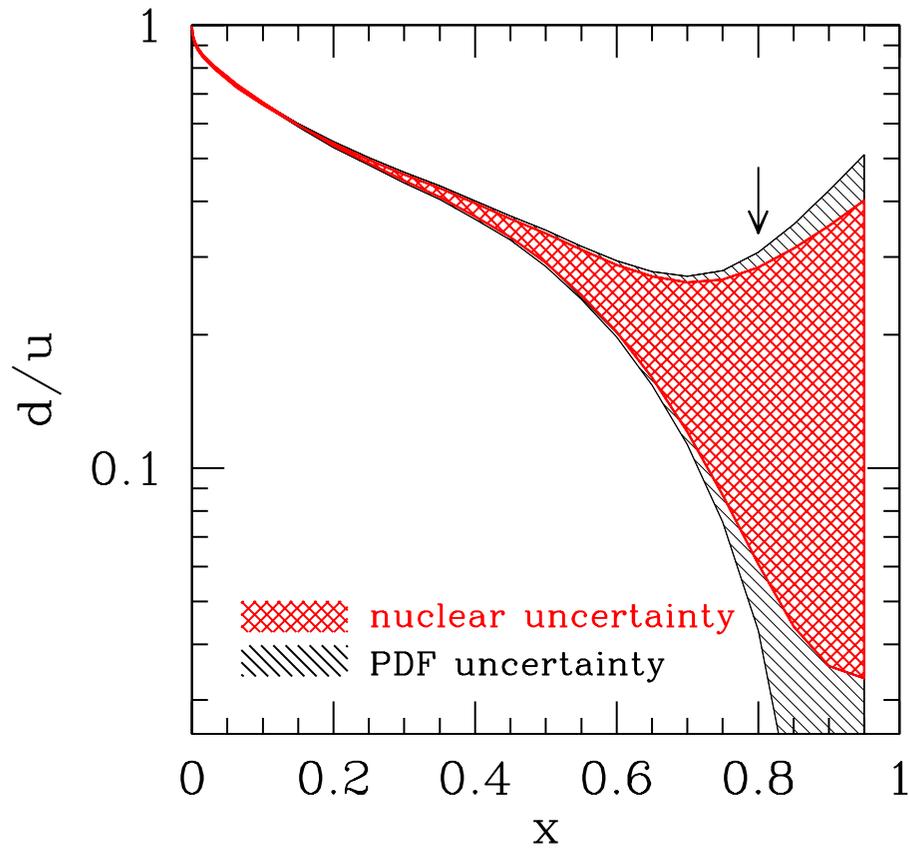
# New CJ11 PDF analysis



Accardi et al.  
arXiv:1101.1234

→ dramatic increase in  $d$  PDF in  $x \rightarrow 1$  limit  
with more flexible parametrization

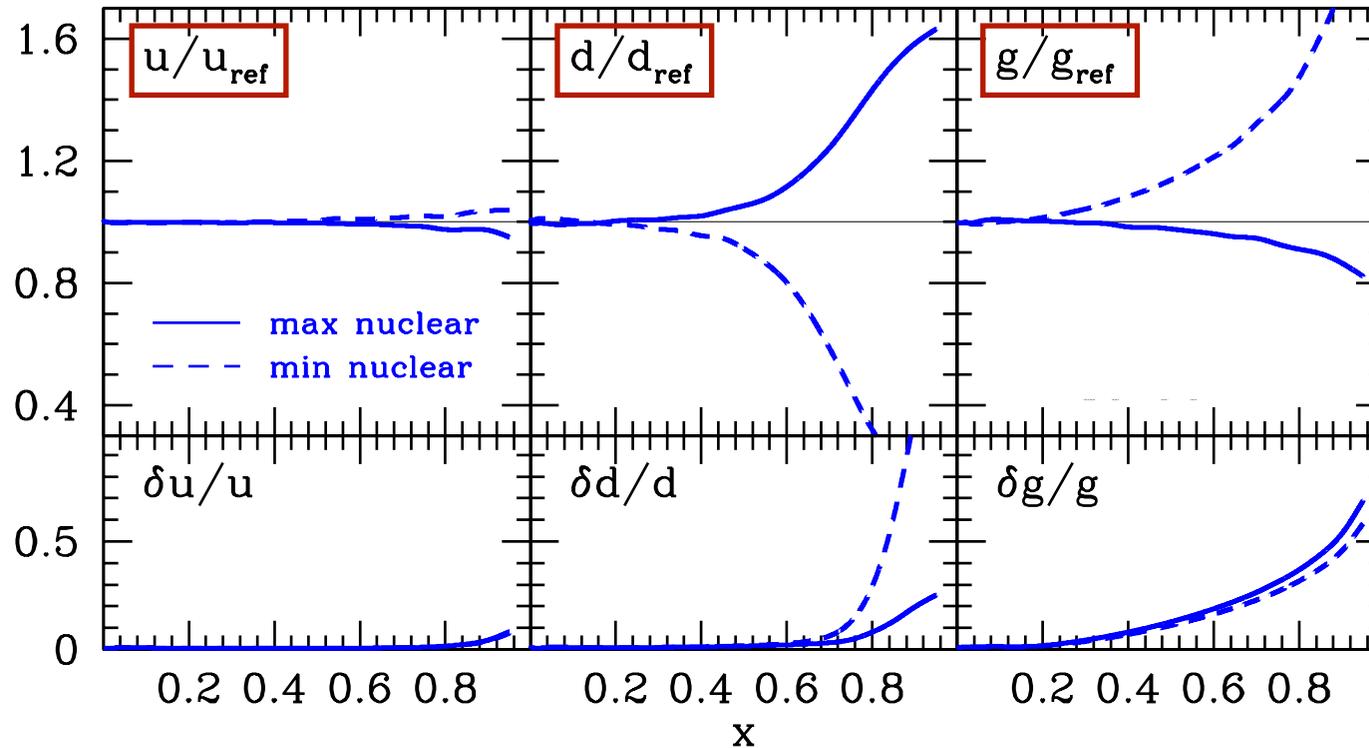
# New CJ11 PDF analysis



Accardi et al.  
arXiv:1101.1234

- combined nuclear correction uncertainties sizable at  $x > 0.5$
- $x \rightarrow 1$  limiting value depends critically on deuteron model
- $n/p$  ratio smaller at large  $x$  *cf.* no nuclear corrections fit

# New CJ11 PDF analysis



Accardi et al.  
arXiv:1101.1234

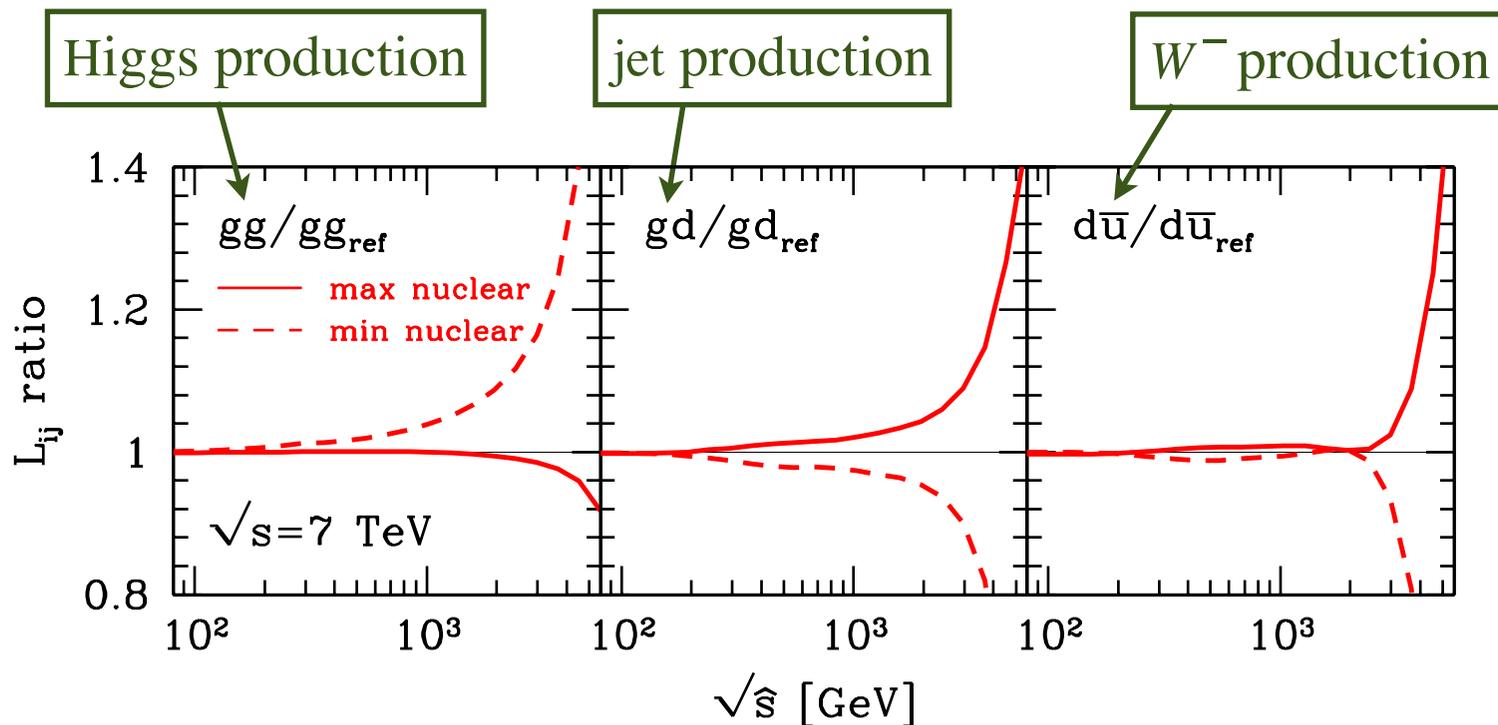
- **very little effect on  $u$  quark PDF**  
(tightly constrained by DIS & DY proton data)
- **gluon PDF anticorrelated with  $d$  quark**  
( $g$  compensates for smaller  $d$  quark contribution in jet data)
- **uncertainty in  $d$  feeds into larger uncertainty in  $g$  at high  $x$**

# New CJ11 PDF analysis

## Impact on parton “luminosities” at colliders

$$L_{ij} = \frac{1}{s(1 + \delta_{ij})} \int_{\hat{s}/s}^1 \frac{dx}{x} f_i(x, \hat{s}) f_j(\hat{s}/xs, \hat{s}) + (i \leftrightarrow j)$$

$s(\hat{s}) = \text{hadronic (partonic) c.m. energy squared}$



Accardi et al.  
arXiv:1101.1234

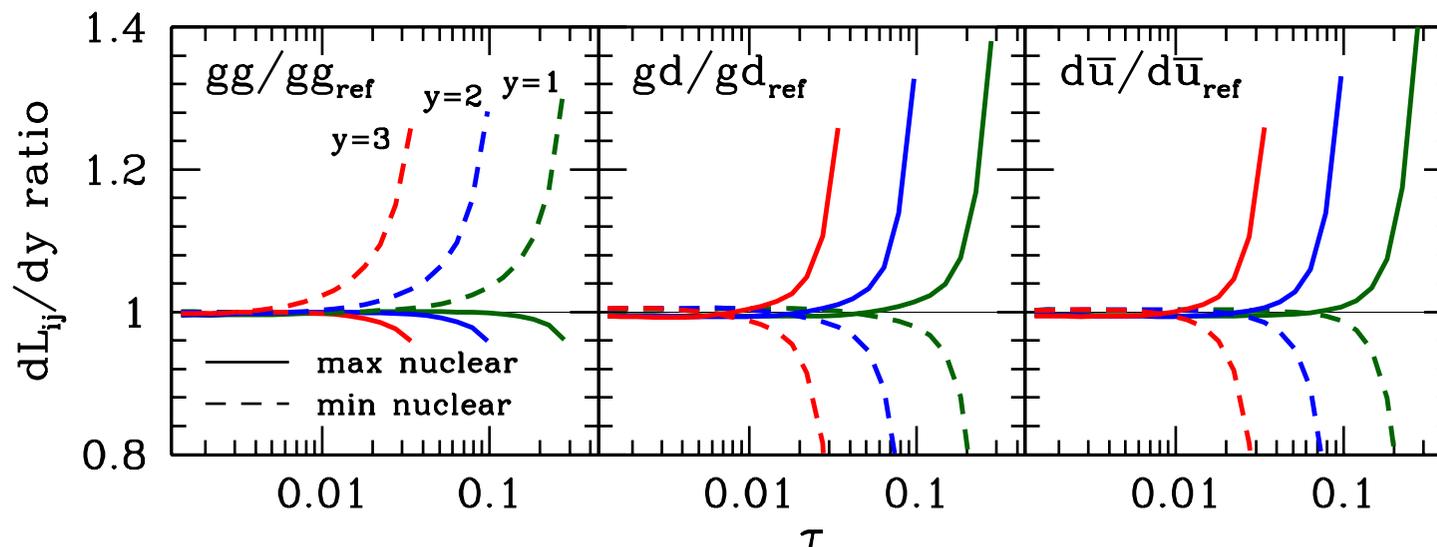
→ nuclear uncertainties important for  $\sqrt{\hat{s}} \gtrsim 1$  TeV mass range

# New CJ11 PDF analysis

## ■ Impact on differential parton luminosities

$$\frac{dL_{ij}}{dy} = \frac{1}{s(1 + \delta_{ij})} f_i(x_1, \hat{s}) f_j(x_2, \hat{s}) + (i \leftrightarrow j)$$

$$x_{1,2} = \tau e^{\pm y}, \quad \tau = \sqrt{\hat{s}/s} \text{ for rapidity } y$$



Accardi et al.  
arXiv:1101.1234

→ greater sensitivity to high- $x$  region at larger rapidities

# Future methods of determining $d/u$

■  $e d \rightarrow e p_{\text{spec}} X^*$

“BoNuS”

semi-inclusive DIS from  $d$

→ tag “spectator” protons

(see talk session 9, 18:05)

■  $e {}^3\text{He}({}^3\text{H}) \rightarrow e X^*$

“MARATHON”

${}^3\text{He}$ -tritium mirror nuclei

■  $e p \rightarrow e \pi^\pm X^*$

semi-inclusive DIS as flavor tag

■  $e^\mp p \rightarrow \nu(\bar{\nu}) X$

$\nu(\bar{\nu}) p \rightarrow l^\mp X$

$p p(\bar{p}) \rightarrow W^\pm X, Z^0 X$

$\vec{e}_L(\vec{e}_R) p \rightarrow e X^*$

“PVDIS / SOLID”

} weak current  
as flavor probe

\* planned for JLab at 12 GeV

# Summary & outlook

- New frontiers explored at large momentum fractions  $x$ 
  - dedicated global PDF analysis (CJ collaboration)
- Stable leading twist PDFs obtained for  $W^2 > 3 \text{ GeV}^2$  and  $Q^2 \gtrsim 1.5 \text{ GeV}^2$  including nuclear and  $1/Q^2$  corrections
  - new set of “CJ11” PDFs & structure functions released soon
  - include lower- $W^2$  data
  - explore consequences for colliders (*e.g.* LHC)
- Further constraints will require new experiments uniquely sensitive to  $d$  quark PDF (see *BoNuS* talk – session 9, 18:05)
- Extend methodology to *spin-dependent* global PDF analysis
  - dedicated JLab (theory/experiment) postdoc from Jan. 2012 (Pedro Jimenez-Delgado)

The End