

**2011 - 2014** — PhD in theoretical physics  
under supervision of Prof. Dr. Marc Vanderhaeghen  
at Johannes Gutenberg University Mainz.

Thesis title *“Light-by-light scattering and the muon’s anomalous magnetic moment”*

**2014 - 2015** — Postdoc at the Institute of Nuclear Physics in Mainz

Project: *Lepton universality test in the photoproduction of  $e^-e^+$  versus  $\mu^-\mu^+$  pairs on a proton target*

*JLab Director’s Theory Seminar, December 2, 2015*

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Lepton universality test  
in the photoproduction of  $e^-e^+$   
versus  $\mu^-\mu^+$  pairs on a proton target

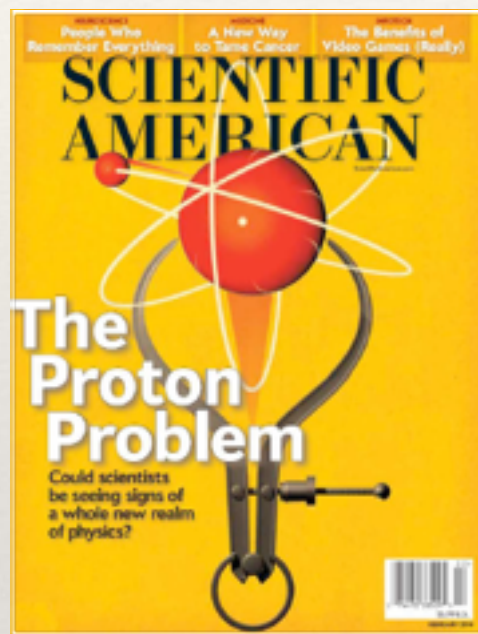
Vladislav Pauk  
Thomas Jefferson  
National Accelerator Facility  
Newport News, VA, USA



# Summary of research activity

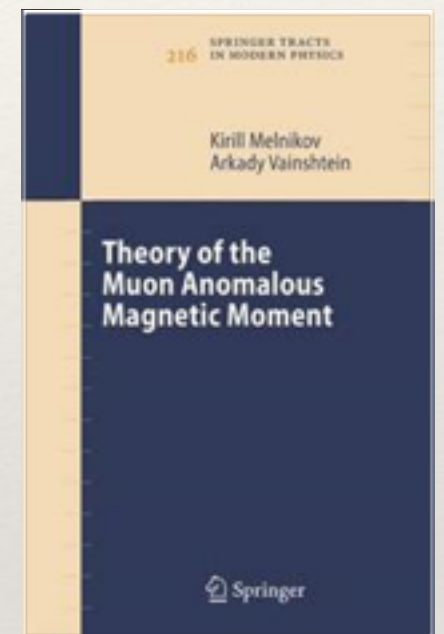
-01

Electromagnetic **properties of hadrons** and their role in **precision observables** and searches for **New Physics**.

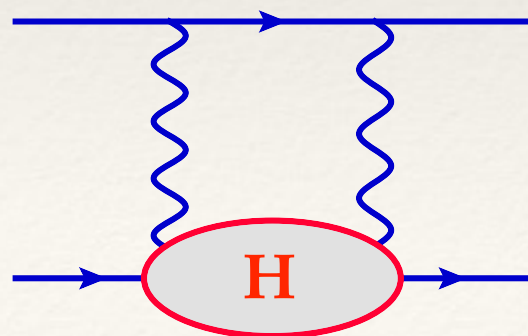


large discrepancy between theory and experiment

sign of New Physics!

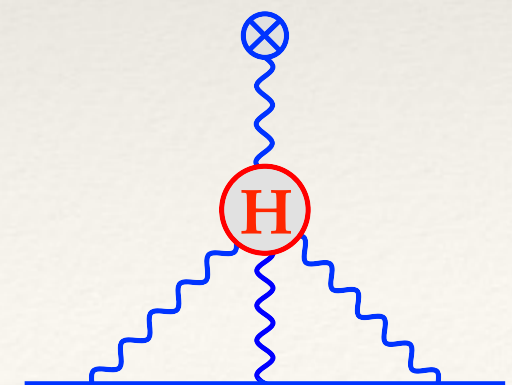


$\sim 7\sigma$  discrepancy



large uncertainties from unconstrained hadronic corrections

$\sim 3\sigma$  discrepancy

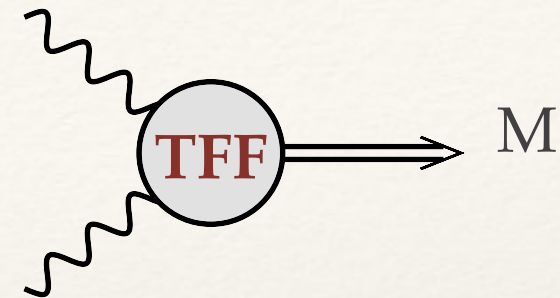




# Summary of research activity

-02

Two-photon production  
and meson transition form factors



analyticity

unitarity

gauge symmetry

Sum rules:

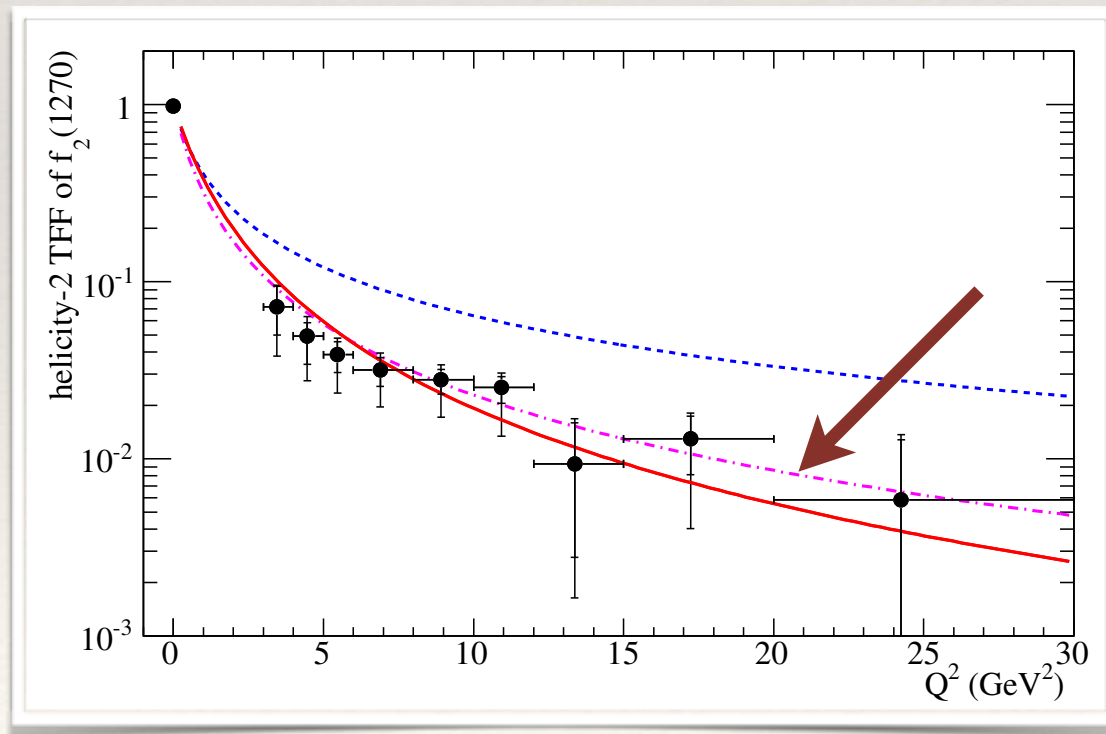
$$\int_{s_0}^{\infty} \frac{\sigma_0 - \sigma_2}{s + Q^2} = 0$$

Phys. Rev. D 85, 116001

Phys.Lett. B725, 504-509

predictions for the TFF for **f<sub>2</sub>(1270)**  
as a function of the photon virtuality

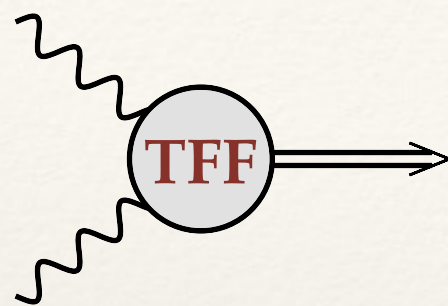
Next: update of the analysis using **new data**



Belle (2015)

# Summary of research activity

-03

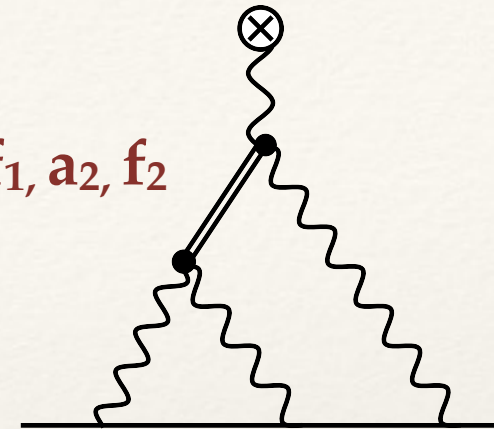


$(g-2)_\mu$



[Eur.Phys.J. C74 3008](#)

$a_0, f_0, f_1, a_2, f_2$



FNAL expected accuracy:

Total contribution of single meson exchanges beyond pseudo scalars:

$$\delta a_\mu \approx 16 \times 10^{-11}$$

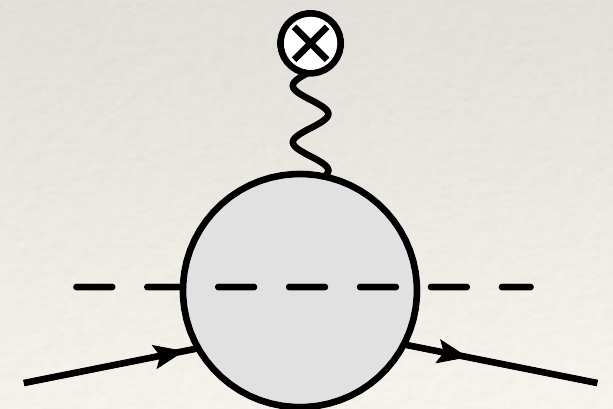
$$a_\mu(a_0, f_0, f_1, a_2, f_2) \approx 6 \times 10^{-11}$$

**model independent approach** needed for the **systematic account** of the hadronic uncertainties

**new dispersive framework**

[Phys.Rev. D90, 113012](#)

relate  $(g-2)_\mu$  to the absorptive part of the Pauli form factor in the **time-like region**

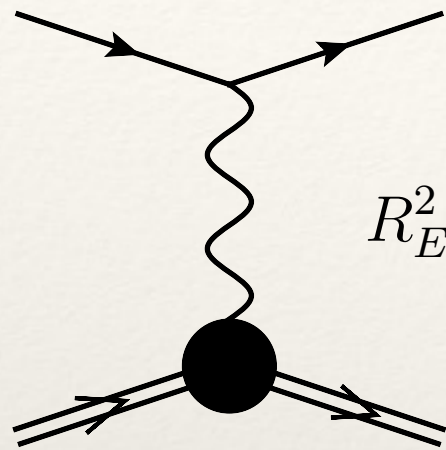


**Next:** realistic estimate of the contributions of the **single-** and **two-pion** thresholds



# The proton radius

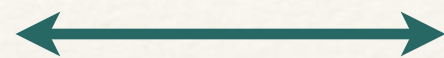
-04



$$R_E^2 \stackrel{def}{=} -6 \left. \frac{dG_E}{dQ^2} \right|_{Q^2=0}$$

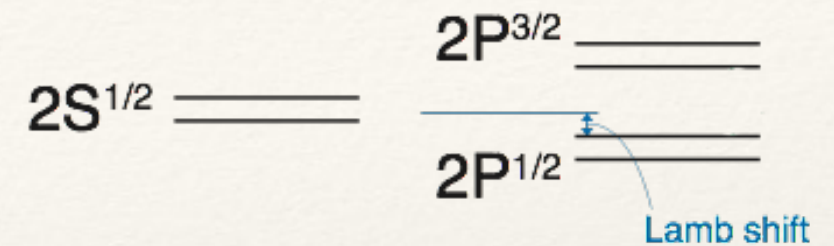
elastic scattering

proton radius  
extraction



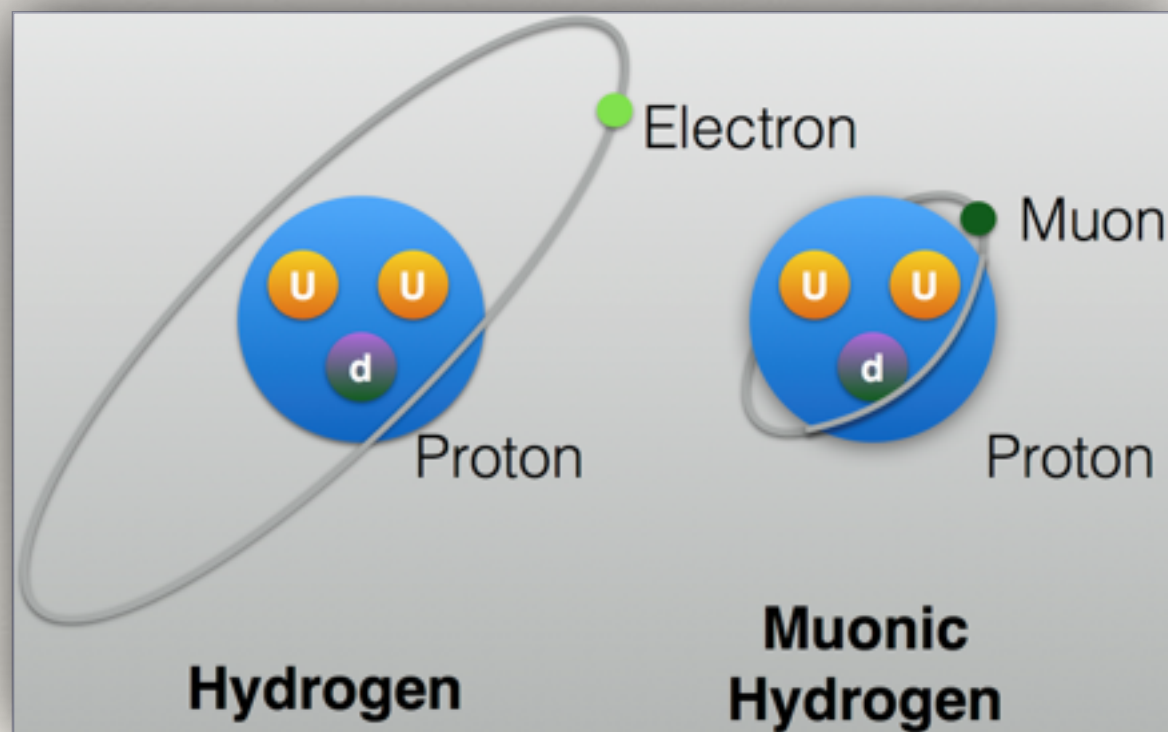
agree for the electron

(uncertainty ~0.6%)



$$\Delta E_L = \frac{2\pi\alpha}{3} |\phi(0)|^2 R_E^2$$

atomic spectroscopy



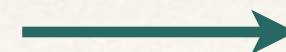
muon vs electron

$$m_\mu \sim 200 m_e$$

$$a_0 = \frac{\hbar^2}{m_e e^2}$$

Bohr radius

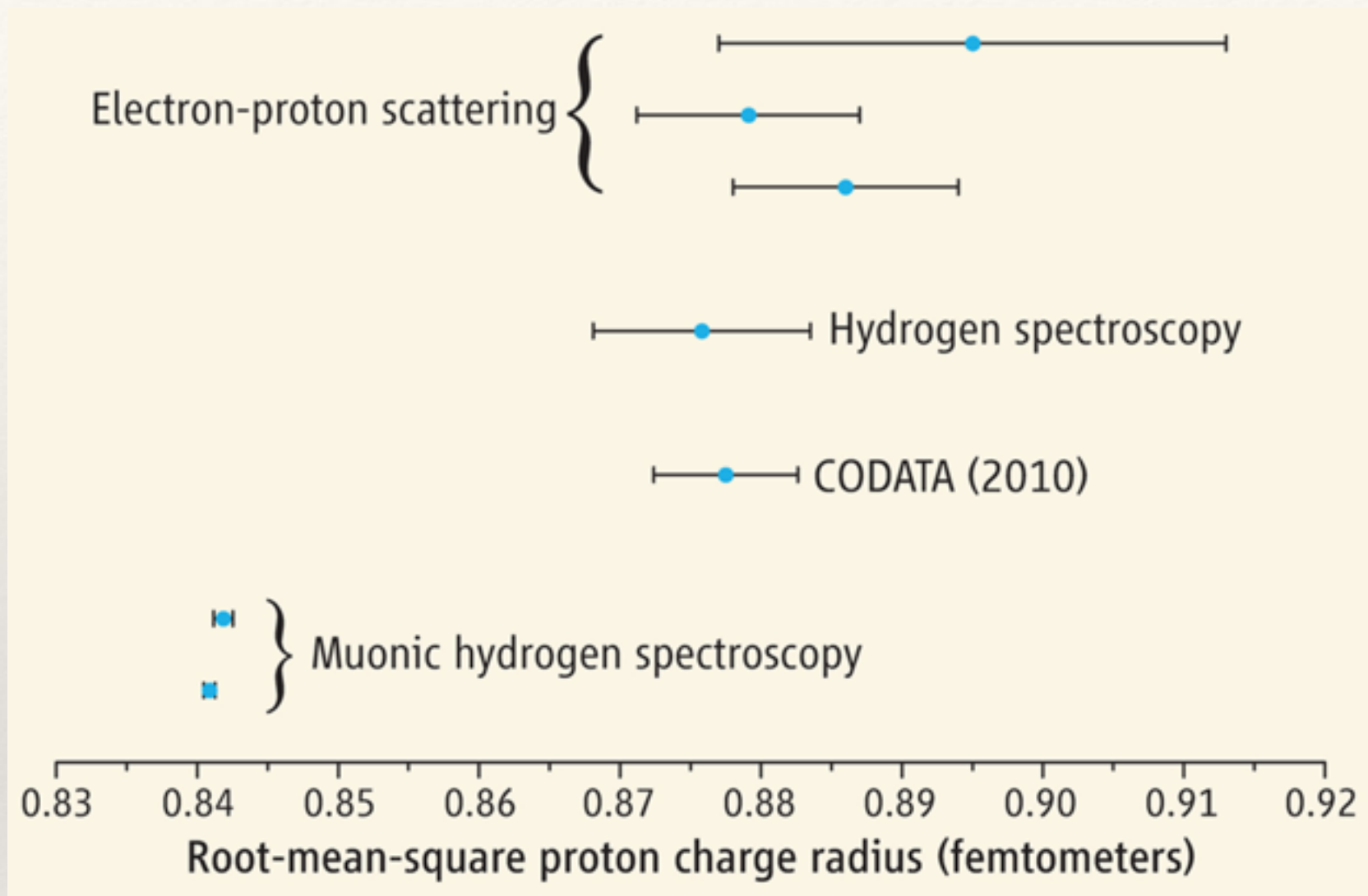
stronger effect  
from the proton size



10x better  
precision

# The puzzle

-05



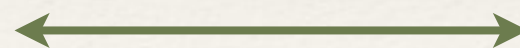
## $\mu$ H data:

$$R_E = 0.8409 \pm 0.0004 \text{ fm}$$

Antognini et al.(2013)

Pohl et al.(2010)

7  $\sigma$  difference !?



## ep/eH data:

$$R_E = 0.8775 \pm 0.0051 \text{ fm}$$

CODATA(2012)

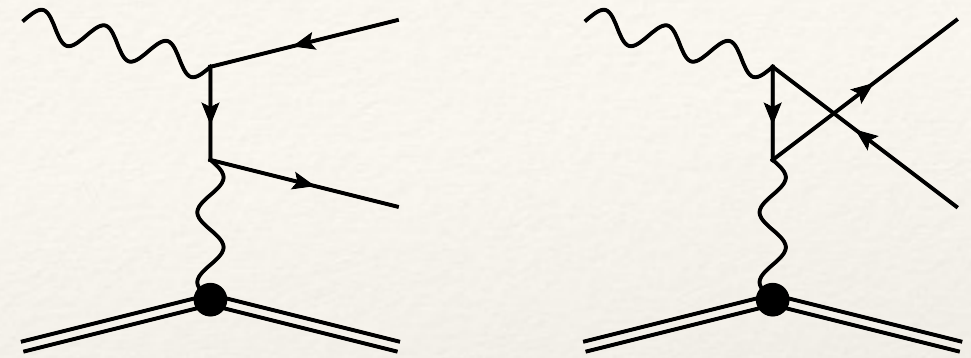


# Lepton pair production on a proton target -06

Measure the ratio of the e vs  $\mu$  cross sections

$$R_{\mu/e} \equiv \frac{d\sigma(\mu^- \mu^+ + e^- e^+)}{d\sigma(e^- e^+)} - 1$$

Phys. Rev. Lett. 115, 221804



**Bethe-Heitler process**

Two-fold differential cross section of the **Bethe-Heitler** production to leading order

$$\frac{d\sigma^{BH}}{dt dM_{ll}^2} = \frac{\alpha^3}{(s - M^2)^2} \cdot \frac{4\beta}{t^2 (M_{ll}^2 - t)^4} \cdot \frac{1}{1 + \tau} \left\{ C_E G_{Ep}^2 + C_M \tau G_{Mp}^2 \right\}$$

at **small t** the ratio  **$R_{\mu/e}$**  gives direct access to the ratio of the proton electric form factor in the  **$\mu p$  versus  $e p$**  scattering

the deviation from the unity will be a sign of violation of the lepton universality

# Lepton pair production on a proton target -07

Bethe-Heitler is **highly peaked**  
in the lepton **forward region**

Detect the proton  
integrate over the lepton phase space

increase the count rates  
the same systematics

no lepton acceptance corrections needed  
large cancellation of radiative corrections

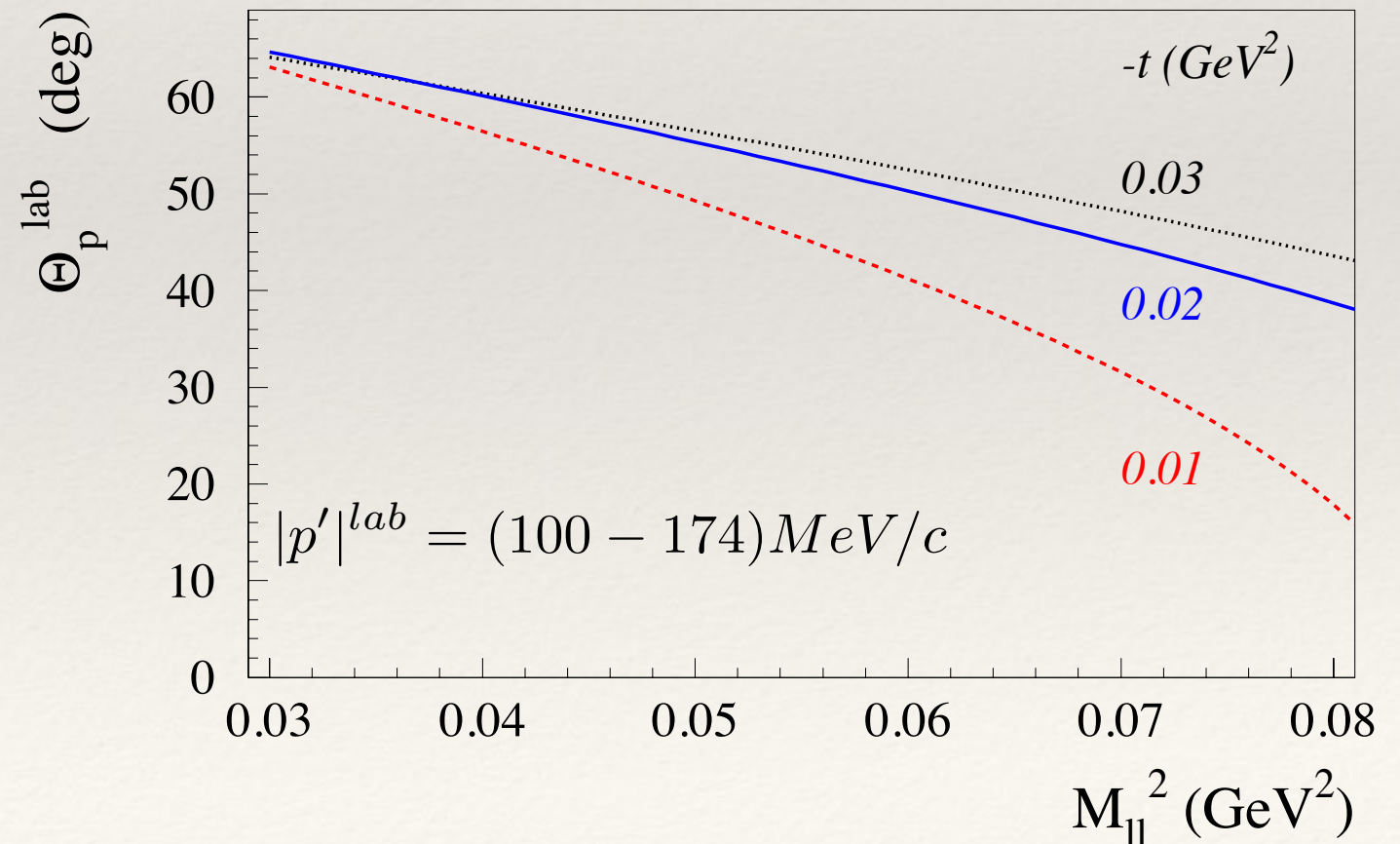
recoil proton Lab angle

$$\cos \Theta_p^{lab} = \frac{M_{ll}^2 + 2(s + M^2)\tau}{2(s - M^2)\sqrt{\tau(1 + \tau)}}$$

proton Lab momentum

$$|\vec{p}'|^{lab} = 2M\sqrt{\tau(1 + \tau)}$$

$$\tau = -t/(4M)^2$$

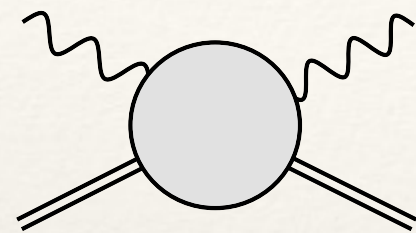




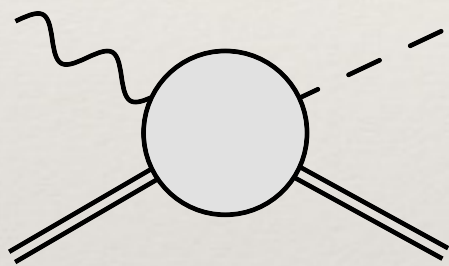
# Experimental feasibility

-08

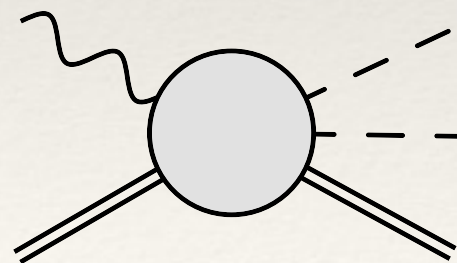
$\gamma p \rightarrow \mu^- \mu^+ p$  : 200 000 events produced



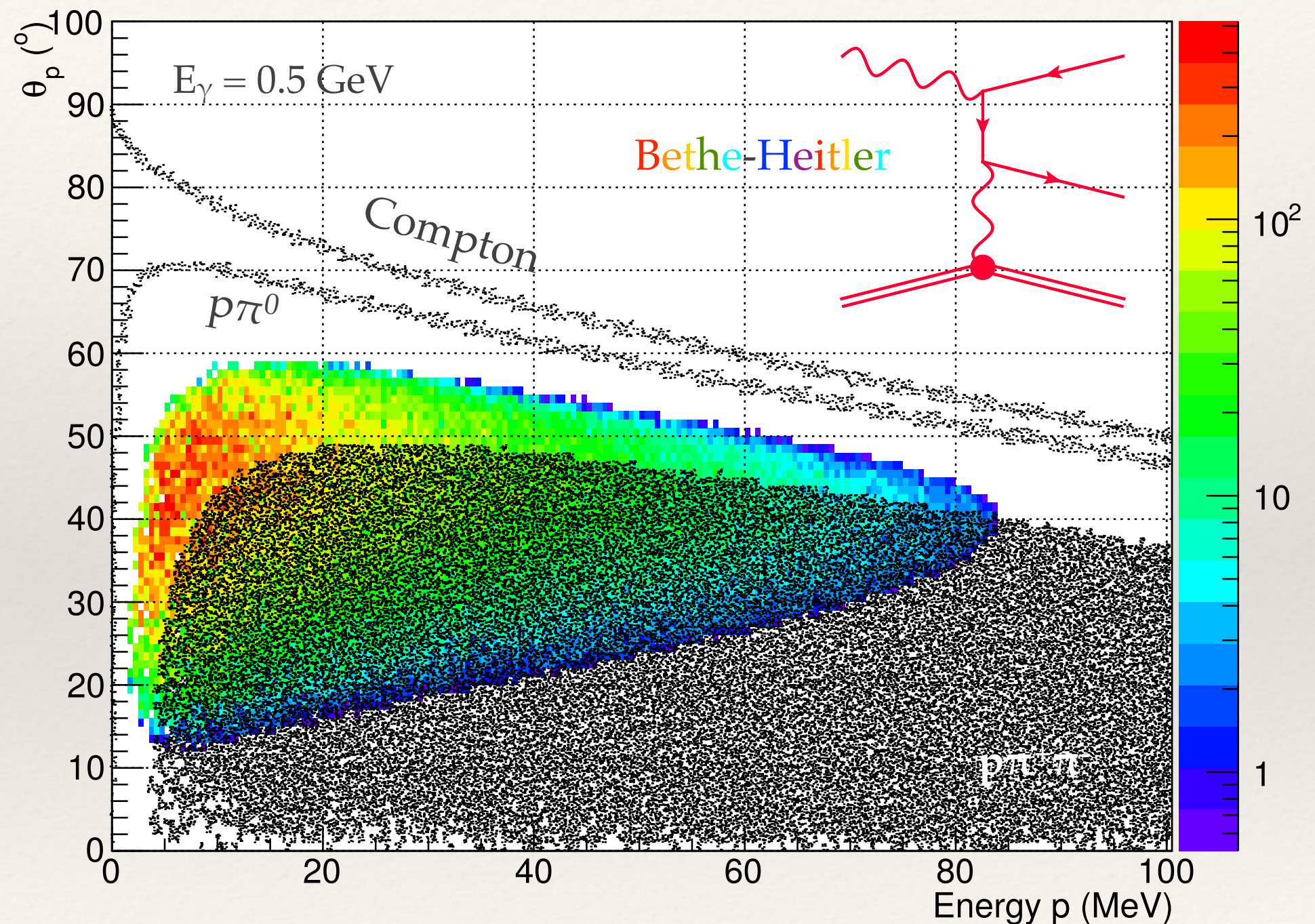
Compton



$p\pi^0$



$p\pi^+\pi^-$



Adlarson (2015)

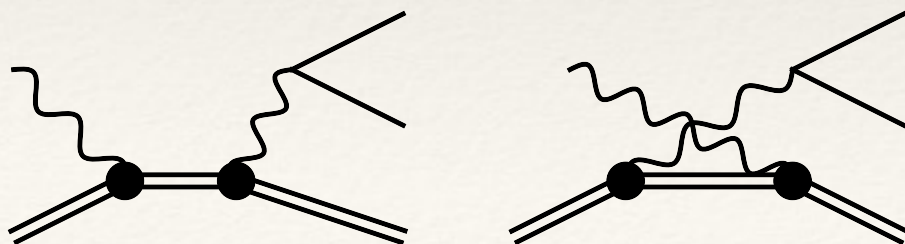
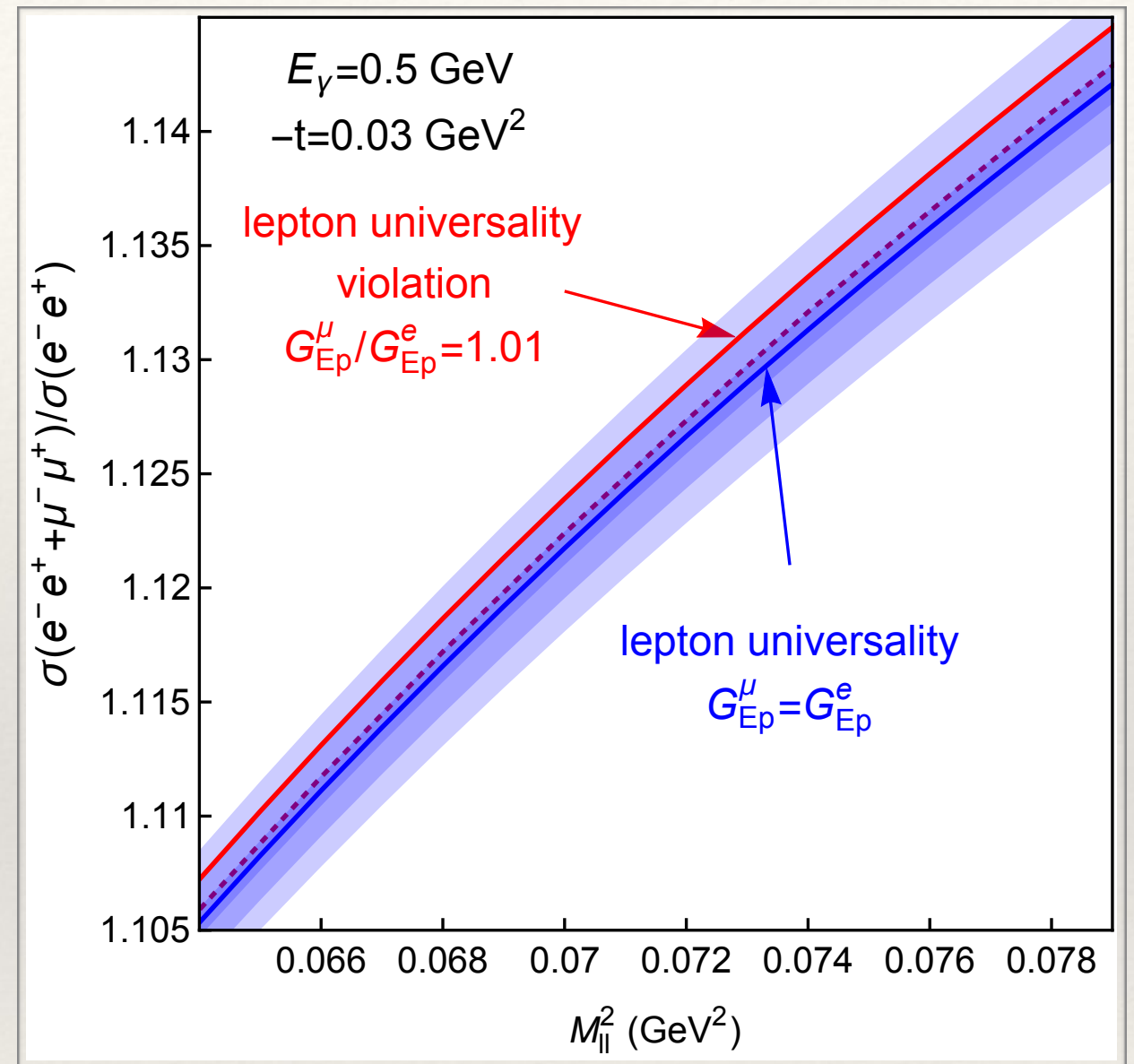
# Lepton universality test

-09

## The cross section ratio

$$R_{\mu/e} \equiv \frac{d\sigma(\mu^- \mu^+ + e^- e^+)}{d\sigma(e^- e^+)} - 1$$

1% difference in measured proton charge FF in electron vs muon observables leads to a 0.2% absolute effect for  $R_{\mu/e}$



the contribution of the TVCS **~5x smaller** than the effect due to the 1% variation in the value of  $G_{\text{Ep}}^\mu$



Double-Regge exchange model for

$$\pi^- p \rightarrow \pi^- \eta' p$$

at COMPASS

and explanation of  $J^{PG}=1^{-+}$  exotics

JPAC



Study the **double-Regge** limit of the  $2 \rightarrow 3$  process and connect to to the **resonance region** by the finite energy sum rules

JLab

Dilepton production  
by detecting electrons and muons

Forward-backward asymmetries  
and study of the TVCS

access the proton form factor from the Bethe-Heitler process by analyzing **angular distributions of the lepton pairs**

direct measurement of the **interference between TVCS and BH** to extract the information on the TVCS (polarizabilities, high-energy behavior)