



# Quarkonium 2017

The 12<sup>th</sup> International Workshop on Heavy Quarkonium



November 6-10, 2017, PKU, Beijing, China  
Organized by the Quarkonium Working Group

## J/ψ Production and Polarization within a Jet

*Jianwei Qiu*

*Theory Center, Jefferson Lab*

*November 9, 2017*



# Heavy quarkonium

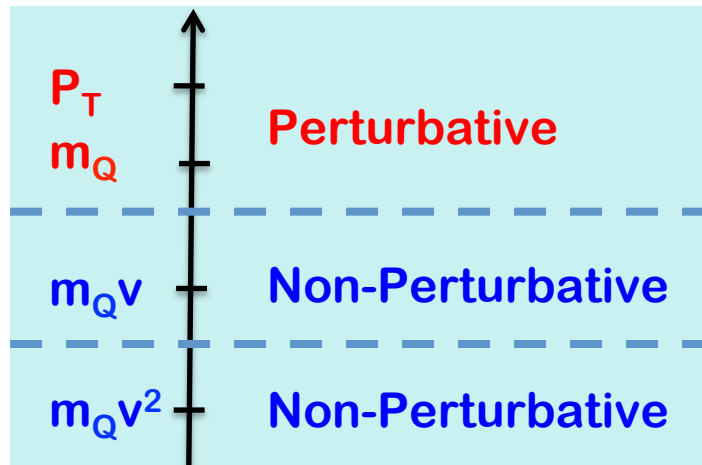
## □ One of the simplest QCD bound states:

Localized color charges (heavy mass), non-relativistic relative motion

Charmonium:  $v^2 \approx 0.3$

Bottomonium:  $v^2 \approx 0.1$

## □ Well-separated momentum scales – effective theory:



Hard — Production of  $Q\bar{Q}$  [pQCD]

Soft — Relative Momentum [NRQCD]

←  $\Lambda_{\text{QCD}}$

Ultrasoft — Binding Energy [pNRQCD]

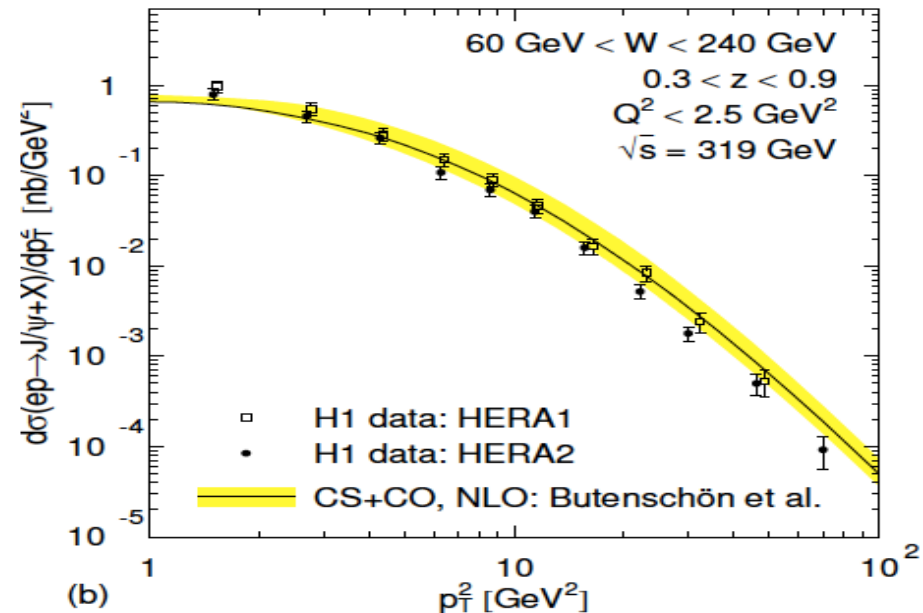
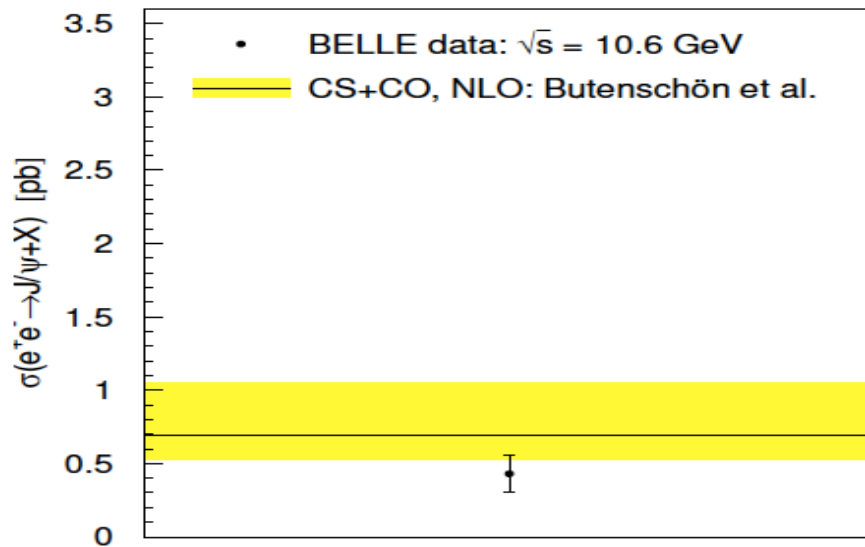
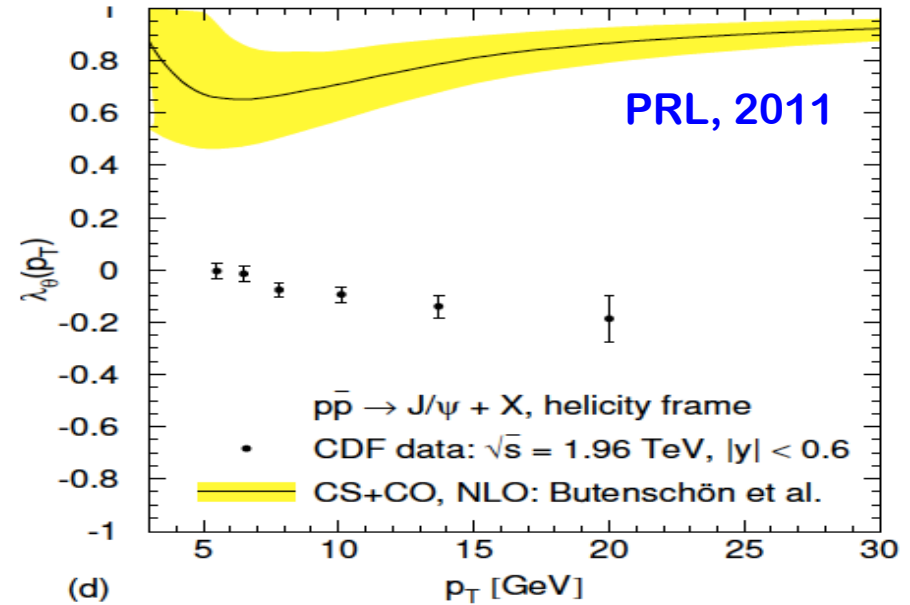
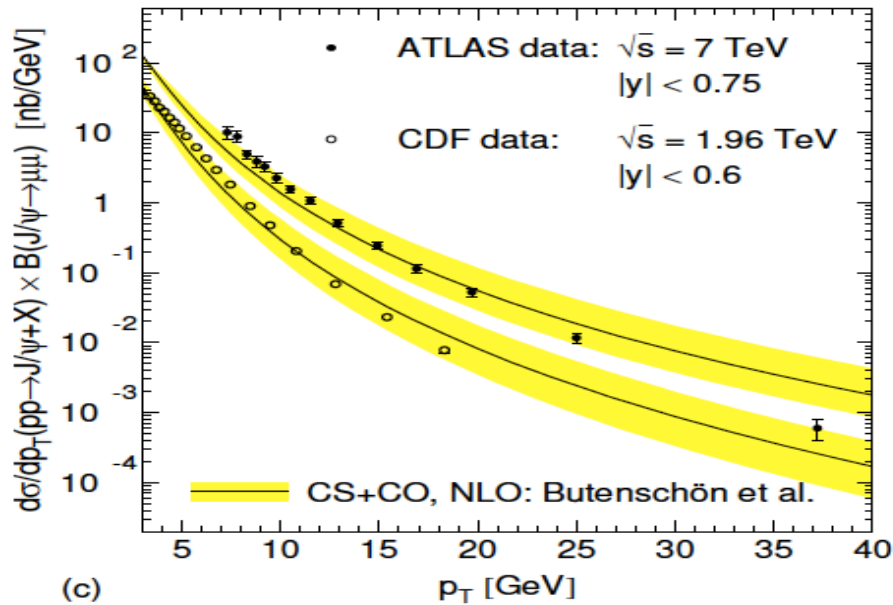
## □ Cross sections and observed mass scales:

$$\frac{d\sigma_{AB \rightarrow H(P)X}}{dy dP_T^2} \quad \sqrt{S}, \quad P_T, \quad M_H,$$

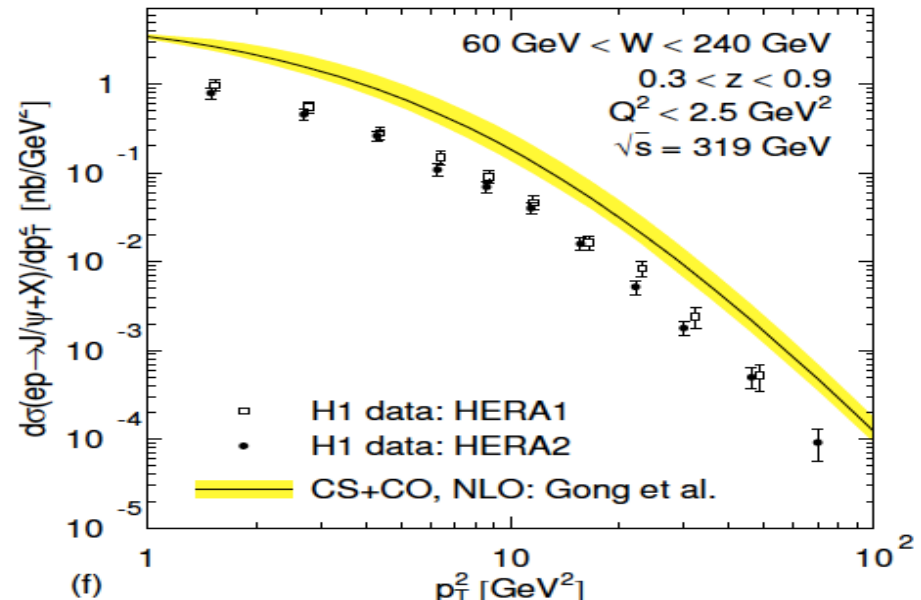
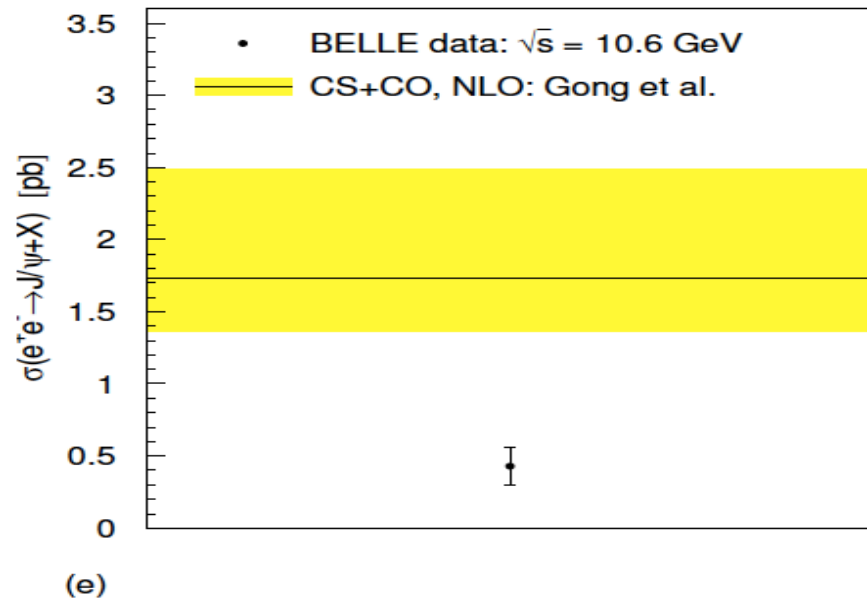
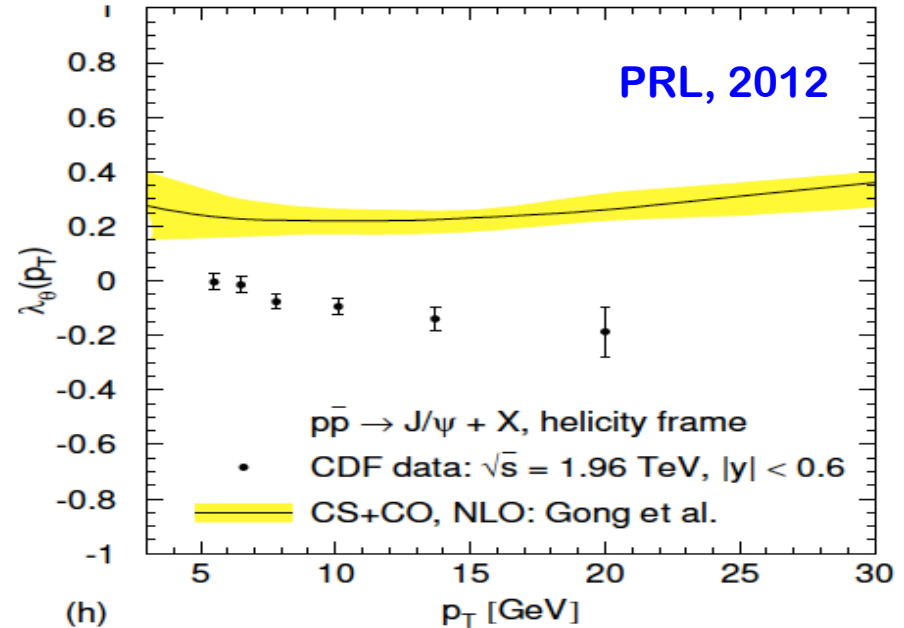
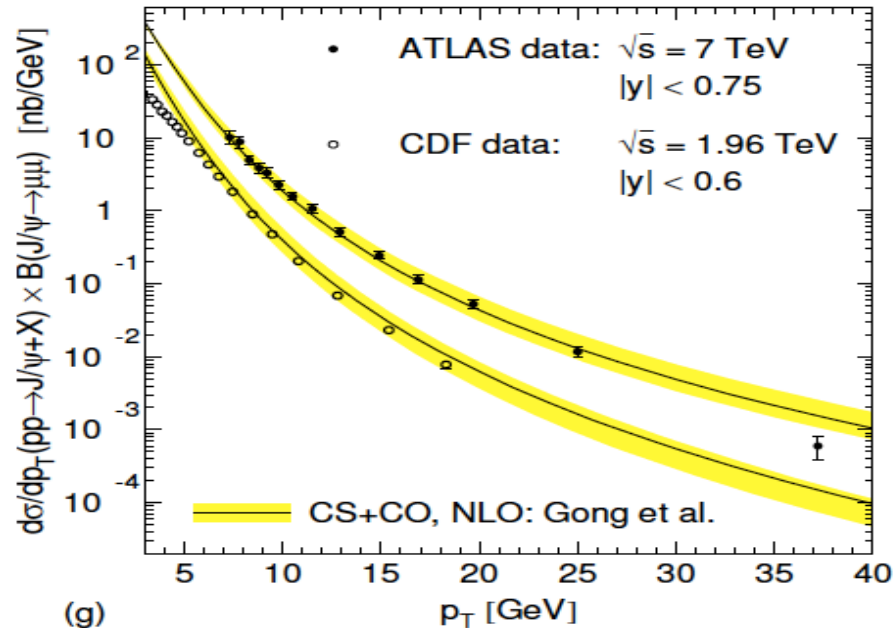
PQCD is “expected” to work for the production of heavy quarks

➡ *Emergence of a quarkonium from a heavy quark pair?*

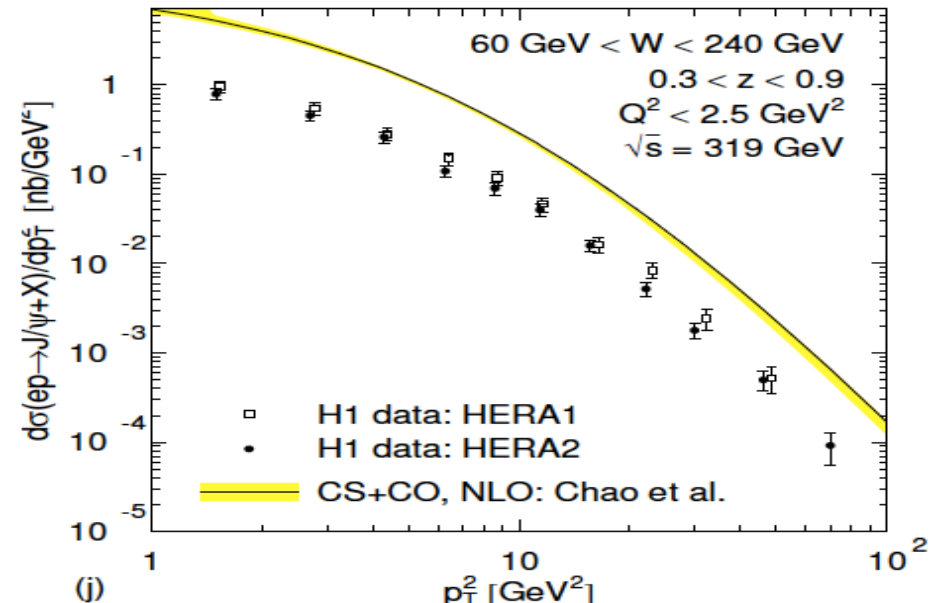
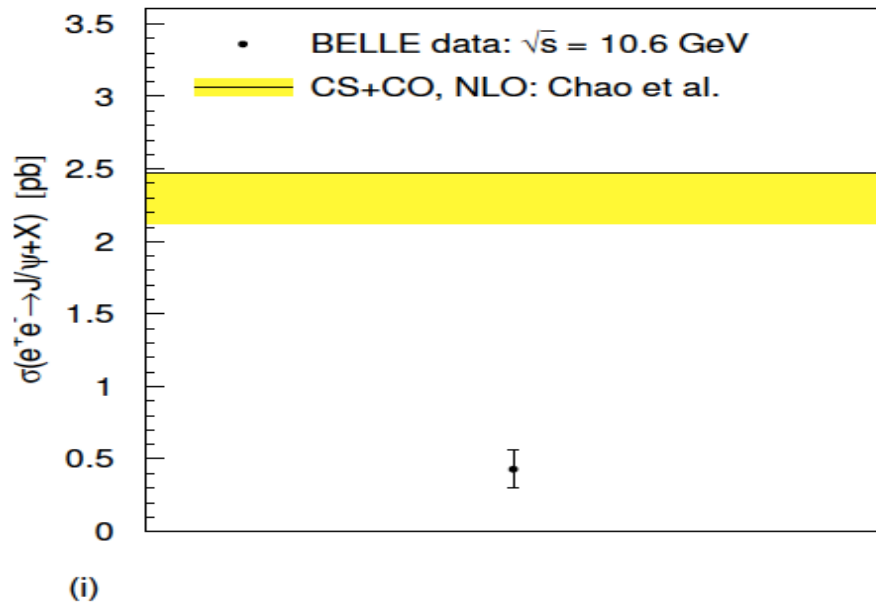
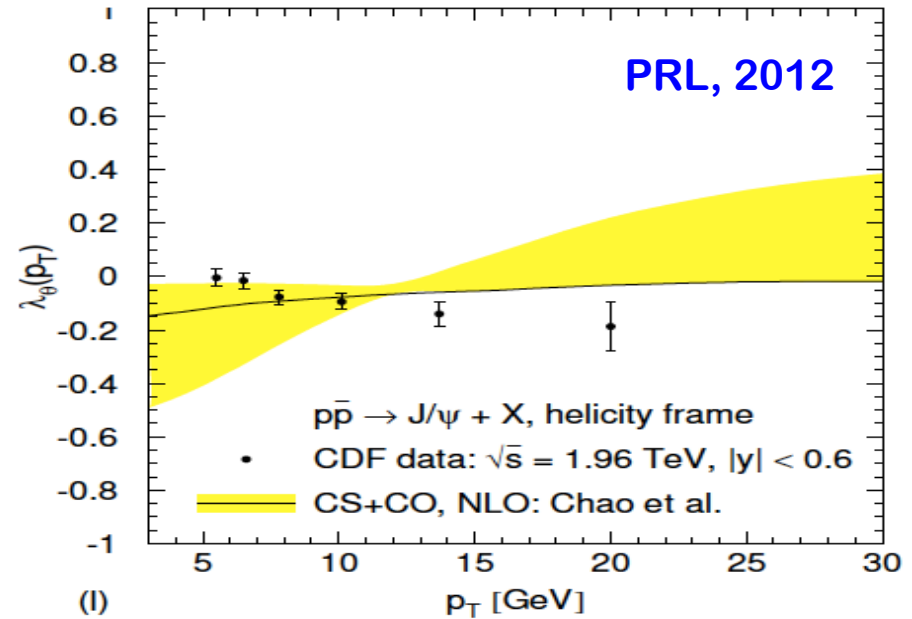
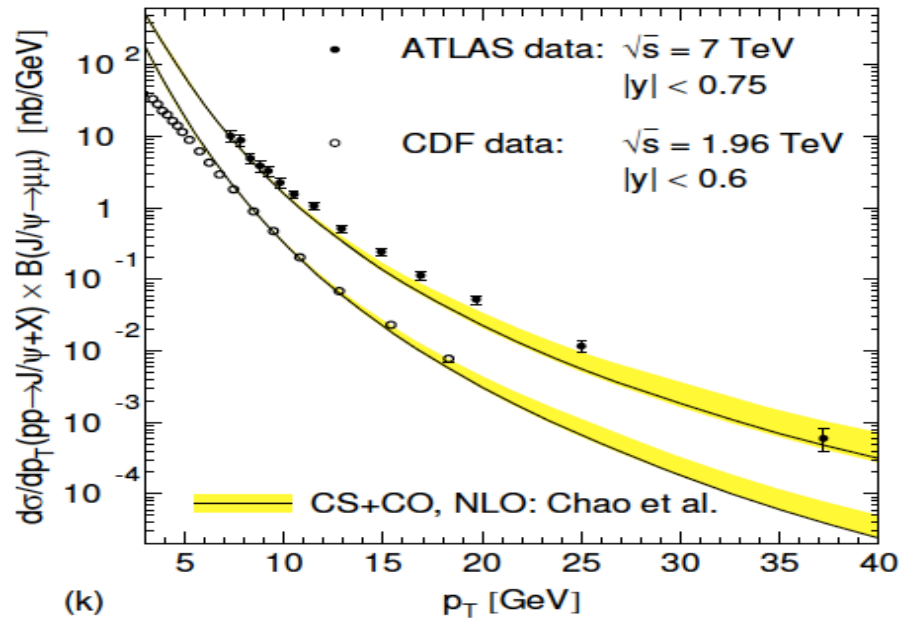
# NLO theory fits – Butenschön et al.



# NLO theory fits – Gong et al.



# NLO theory fits – Chao et al.



# Production at collider energies

G.T. Bodwin, et al., PRD 1995

## □ NRQCD factorization:

$$d\sigma_{A+B \rightarrow H+X}(p_T) = \sum_n d\hat{\sigma}_{A+B \rightarrow [Q\bar{Q}(n)]+X}(p_T) \langle \mathcal{O}_n^H \rangle$$

Expansion in powers of both  $\alpha_s$  and  $v$ !

Hadronization

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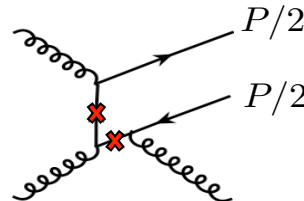
Hadronization

## Re-organization is needed when $p_T \gg m_Q$ :

Z.B. Kang, et al., PRL 2011

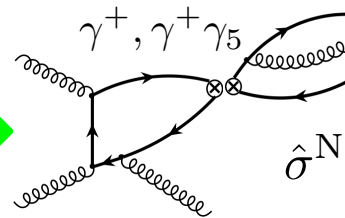
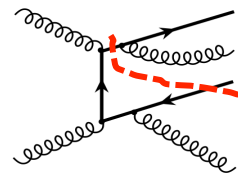
CS channel as a case study

LO in  $\alpha_s$ :



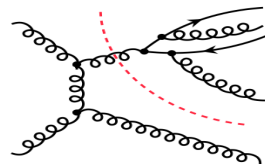
$$\hat{\sigma}^{\text{LO}} \propto \frac{\alpha_s^3(p_T)}{p_T^8}$$

NLO in  $\alpha_s$ :



$$\hat{\sigma}^{\text{NLO}} \rightarrow \frac{\alpha_s^3(p_T)}{p_T^6} \otimes \alpha_s(\mu) \log(\mu^2/\mu_0^2)$$

NNLO in  $\alpha_s$ :



$$\hat{\sigma}^{\text{NNLP}} \rightarrow \frac{\alpha_s^2(p_T)}{p_T^4} \otimes \alpha_s^3(\mu) \log^m(\mu^2/\mu_0^2)$$

$P_T$  Power!

$$\mu_0 \gtrsim 2m_Q$$



✧ When  $p_T \gg m_Q$ , the expansion in powers of  $\alpha_s$  is not reliable!

✧ Leading order in  $\alpha_s$ -expansion  $\neq$  leading power in  $1/p_T$ -expansion!



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## □ PQCD factorization:

G.T. Nayak, et al., PRD2005  
Z.B. Kang, et al., PRD2014

$$d\sigma_{A+B \rightarrow H+X}(p_T) = \sum_i d\tilde{\sigma}_{A+B \rightarrow i+X}(p_T/z, \mu) \otimes D_{H/i}(z, \mu) \quad \leftarrow \text{LP}$$

$$\text{NLP} \rightarrow + \sum_n d\tilde{\sigma}_{A+B \rightarrow [Q\bar{Q}(n)]+X}(p_T/z, \zeta_1, \zeta_2, \mu) \otimes \mathcal{D}_{H/[Q\bar{Q}(n)]}(z, \zeta_1, \zeta_2, \mu)$$



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G.T. Bodwin, et al., PRD 1995

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**Model:** Using NRQCD factorization for the INPUT fragmentation functions

Y.Q. Ma, et al., PRD2014

$$D_{H/i}(z, \mu_0) = \sum_n d_{i \rightarrow [Q\bar{Q}(n)]}(z, \mu_0) \langle \mathcal{O}_n^H \rangle$$

$$\mathcal{D}_{H/[Q\bar{Q}(m)]}(z, \zeta_1, \zeta_2, \mu_0) = \sum_n d_{[Q\bar{Q}(m)] \rightarrow [Q\bar{Q}(n)]}(z, \zeta_1, \zeta_2, \mu_0) \langle \mathcal{O}_n^H \rangle$$

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$$\mathcal{D}_{H/[Q\bar{Q}(m)]}(z, \zeta_1, \zeta_2, \mu_0) = \sum_n d_{[Q\bar{Q}(m)] \rightarrow [Q\bar{Q}(n)]}(z, \zeta_1, \zeta_2, \mu_0) \langle \mathcal{O}_n^H \rangle$$

## □ PQCD improved NRQCD factorization:

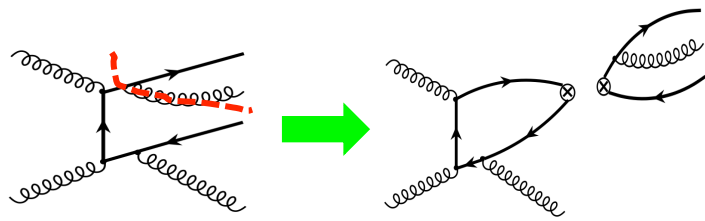
Evolution  
= resummation

$$d\hat{\sigma}_{A+B \rightarrow [Q\bar{Q}(n)]+X}(p_T) = \sum_i d\tilde{\sigma}_{A+B \rightarrow i+X}(p_T/z) \otimes d_{i \rightarrow [Q\bar{Q}(n)]}(z)$$

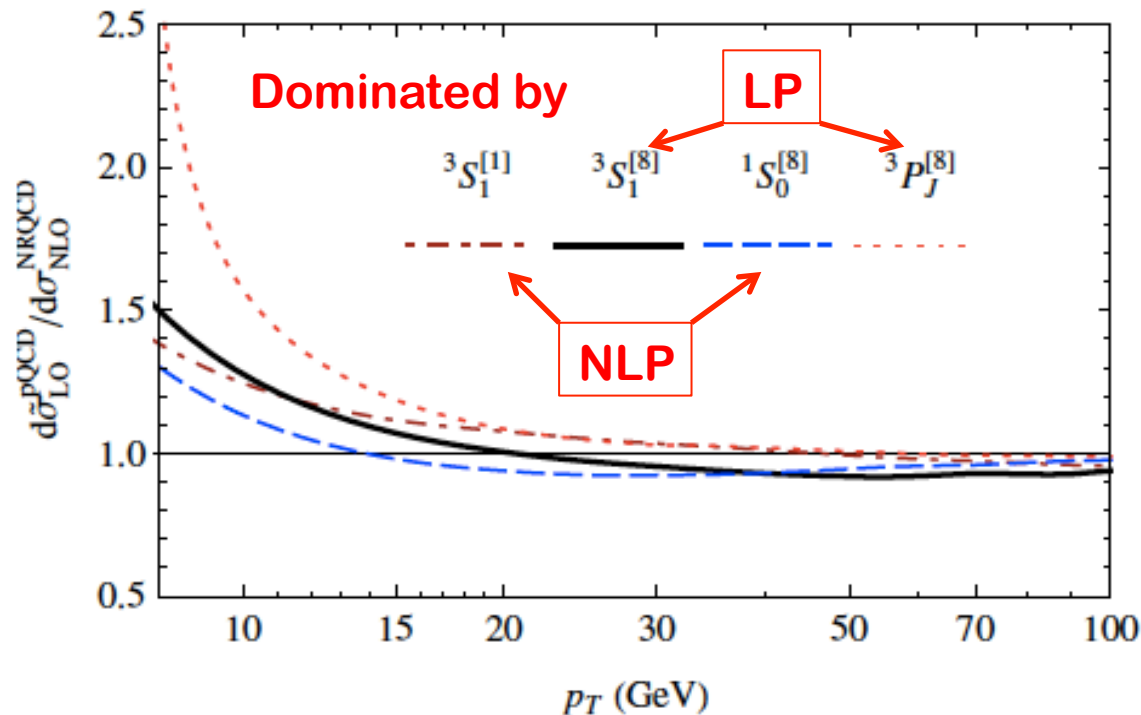
$$+ \sum_m d\tilde{\sigma}_{A+B \rightarrow [Q\bar{Q}(m)]+X}(p_T/z, \zeta_1, \zeta_2) \otimes d_{[Q\bar{Q}(m)] \rightarrow [Q\bar{Q}(n)]}(z, \zeta_1, \zeta_2)$$

# Channel-by-channel comparison

## NRQCD vs. PQCD improved NRQCD:



$$\sigma_{\text{NRQCD}}^{(\text{NLO})} \propto \left[ d\hat{\sigma}_{ab \rightarrow [Q\bar{Q}(v8)]}^{A(\text{LO})} \otimes \mathcal{D}_{[Q\bar{Q}(v8)] \rightarrow J/\psi}^{(\text{LO})} + d\hat{\sigma}_{ab \rightarrow [Q\bar{Q}(a8)]}^{S(\text{LO})} \otimes \mathcal{D}_{[Q\bar{Q}(a8)] \rightarrow J/\psi}^{(\text{LO})} \right]$$

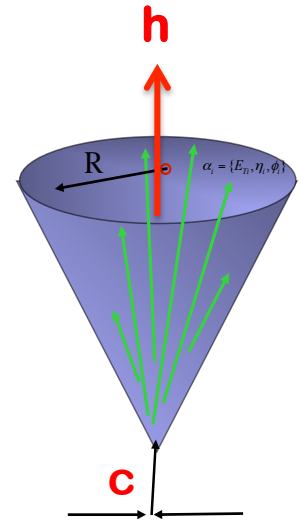
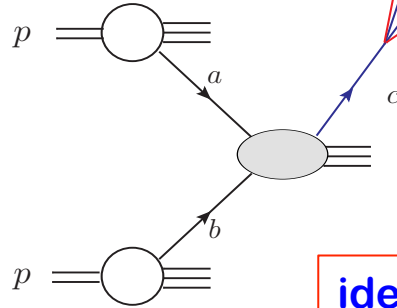
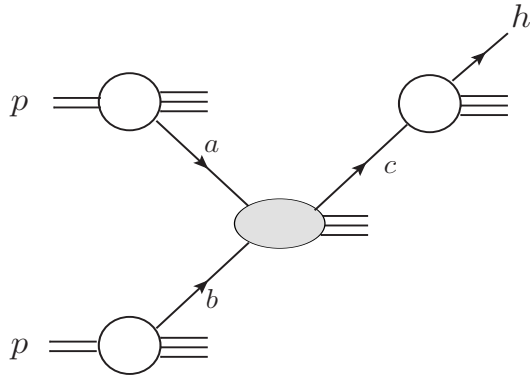


LO analytical  
results  
reproduce  
NLO NRQCD  
calculations  
(numerical)

***$P_T$  – distribution is not sufficient for fixing all NRQCD matrix elements  
Need more physical observables!***

# Hadron distributions at high $P_T$

## Factorization formulas:



$$\frac{d\sigma^{pp \rightarrow hX}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes D_c^h$$

$$\frac{d\sigma^{pp \rightarrow \text{jet}X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes J_c(\mu \sim p_T R)$$

$$\frac{d\sigma^h}{dy dp_T dz_h} \propto \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes \mathcal{G}_c^h(z, z_h, R, \mu)$$

identified

Not identified

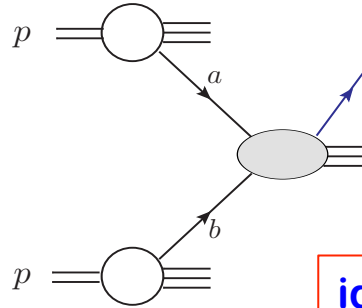
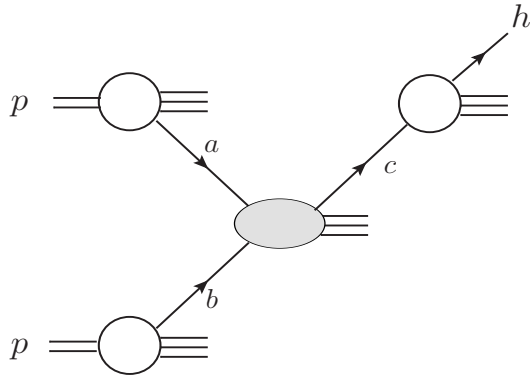
Identified within a jet

$$z = p_T / p_T^c$$

$$z_h = p_T^h / p_T$$

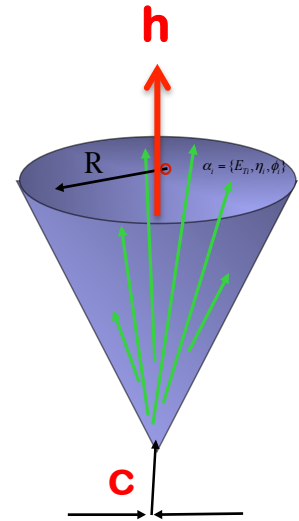
# Hadron distributions at high $P_T$

## Factorization formulas:



identified

Not identified



$$z = p_T / p_T^c$$

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Identified within a jet

Calculable!

$$\frac{d\sigma^{pp \rightarrow hX}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab \rightarrow c} \otimes D_c^h$$

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## Scale dependence – ( $R \ll 1$ ):

$$\mu \frac{\partial}{\partial \mu} \left\{ \begin{matrix} D_c^h \\ J_c \\ \mathcal{G}_c^h \end{matrix} \right\} = \mathcal{P}_{c/d}^{\text{DGLAP}} \otimes \left\{ \begin{matrix} D_d^h \\ J_d \\ \mathcal{G}_d^h \end{matrix} \right\}$$

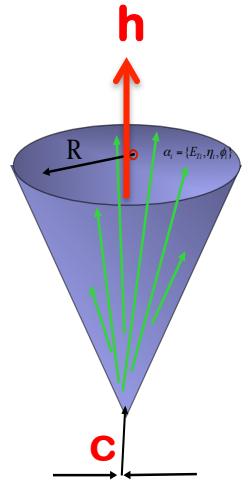
$$\mathcal{G}_c^h(z, z_h, R, \mu) = \sum_d \mathcal{J}_{cd}(z, z_h, R, z', \mu) D_d^h\left(\frac{z}{z'}, \mu\right) \times \left[ 1 + \mathcal{O}\left(\frac{\max(\Lambda_{\text{QCD}}^2, m_h^2)}{(E_{\text{jet}} R)^2}\right) \right]$$

# Jet fragmentation function

□ Ratio of two physical observables:

$$F(z_h, p_T) = \frac{d\sigma^h}{dy dp_T dz_h} \bigg/ \frac{d\sigma}{dy dp_T} \quad \begin{aligned} z_h &= p_T^h / p_T \\ z &= p_T / p_T^c \end{aligned}$$

*First produce a jet, and then look further for a hadron inside the jet!*



➡ ***Favor the contribution initiated by a single energetic parton!***

$$F_{A+B \rightarrow H+X}(z_h, p_T) \propto \sum_n \tilde{\mathcal{F}}_{A+B \rightarrow [Q\bar{Q}(n)]+X}(z_h, p_T) \langle \mathcal{O}_n^H \rangle$$

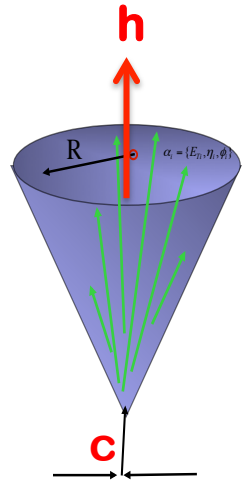
**Different relative size of the coefficients,  
and different weights of the matrix elements**

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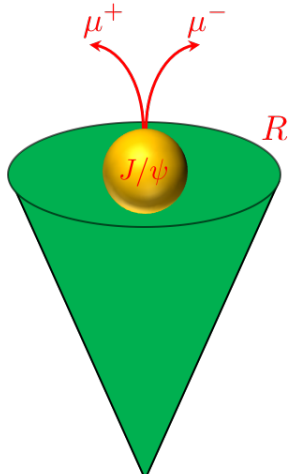


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## □ Polarization:

Different relative size of the coefficients, and different weights of the matrix elements



In the helicity frame:

Kang, Qiu, Ringer, Xing, Zhang, PRL 2017

$$\frac{d\sigma^{J/\psi(\rightarrow \ell^+ \ell^-)}}{d \cos \theta} \propto 1 + \lambda_F \cos^2 \theta$$

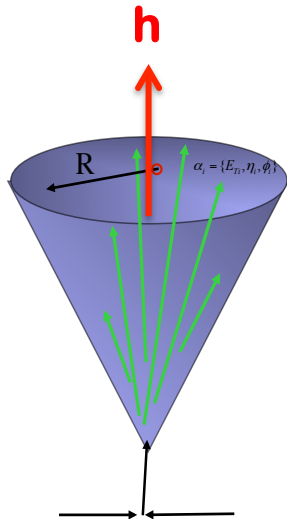
with

$$\lambda_F(z_h, p_T) = \frac{F_T^{J/\psi} - F_L^{J/\psi}}{F_T^{J/\psi} + F_L^{J/\psi}} = \begin{cases} +1, & \text{Transverse} \\ -1, & \text{Longitudinal} \end{cases}$$

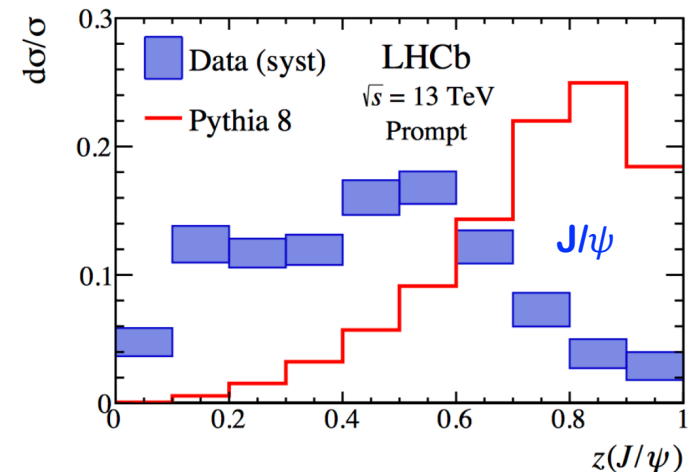
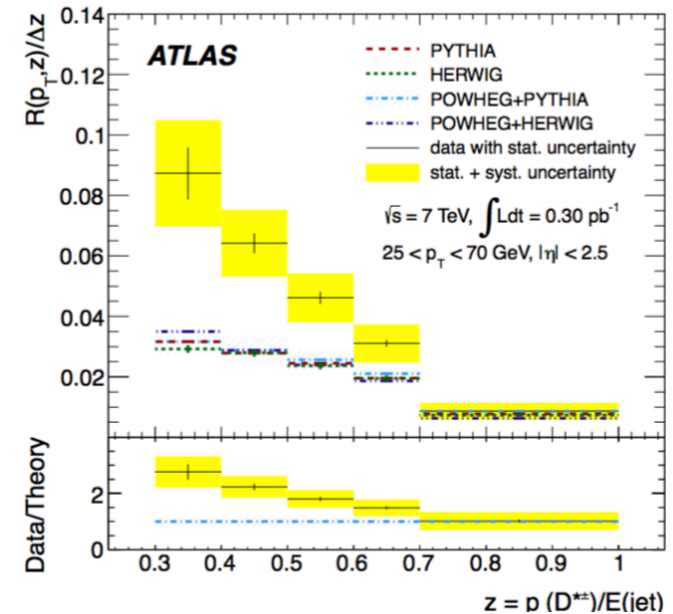
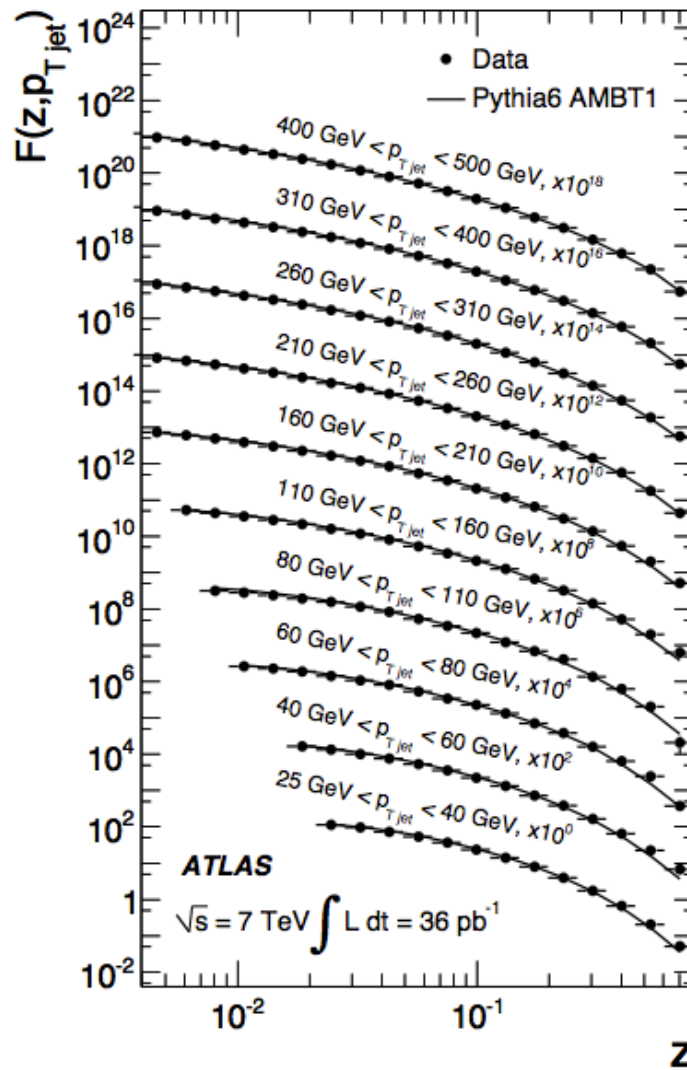


# Jet fragmentation function at the LHC

□ A puzzle (or opportunity) for heavy flavor?

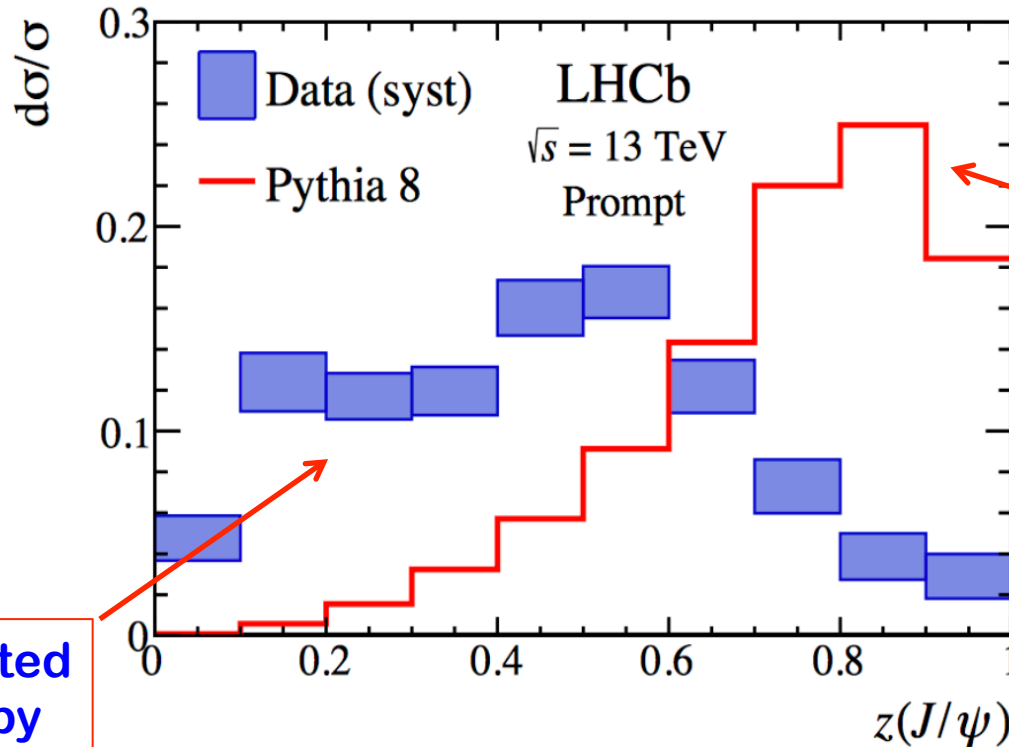


$$z_h = \frac{E_h}{E_{\text{jet}}}$$



# Quarkonium production inside a jet

## □ $J/\psi$ -in-jet measurement from LHCb:



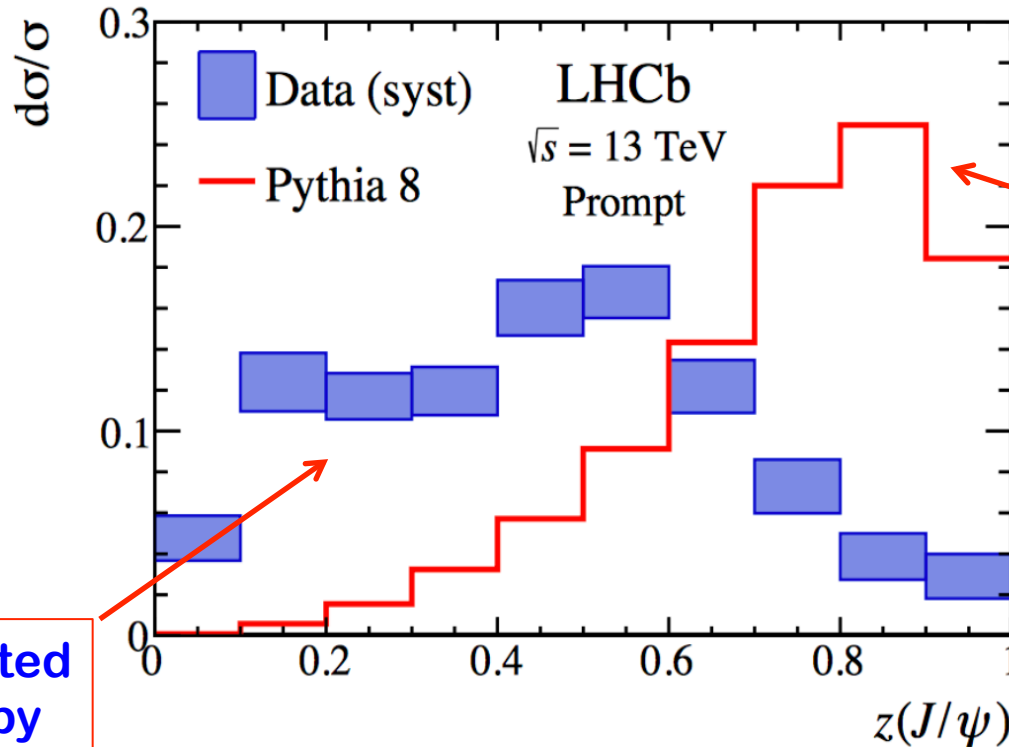
Jet was initiated  
more likely by  
a produced  
SINGLE parton

Leading power contribution dominated!

Jet was initiated  
likely by  
a produced  
heavy quark pair

# Quarkonium production inside a jet

## □ $J/\psi$ -in-jet measurement from LHCb:



Jet was initiated more likely by a produced SINGLE parton

Jet was initiated likely by a produced heavy quark pair

Leading power contribution dominated!

**Recall:**

A delicate **cancelation** was required between  $^3S_1^{[8]}$  and  $^3P_J^{[8]}$  channels was required for fitting the high  $p_T$ -distribution!



*Incomplete cancelation could lead to a “negative”  $d\sigma$  or  $F$ , ...*

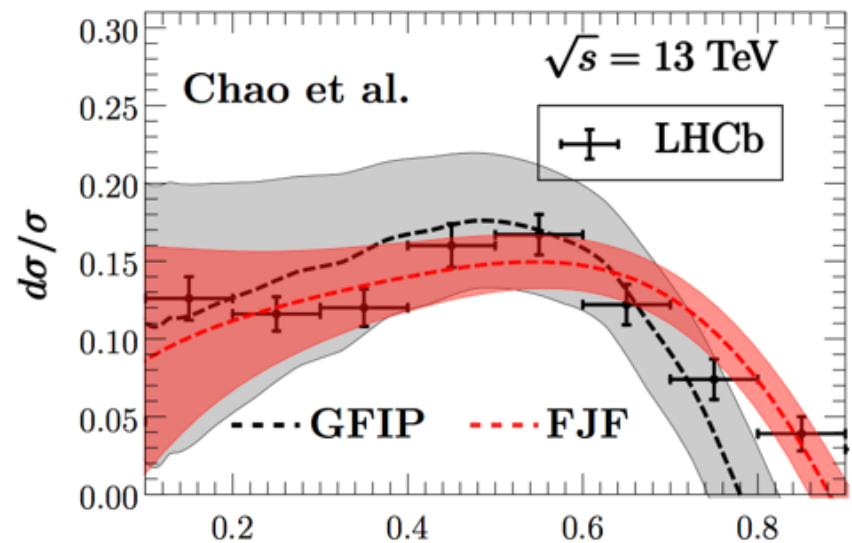
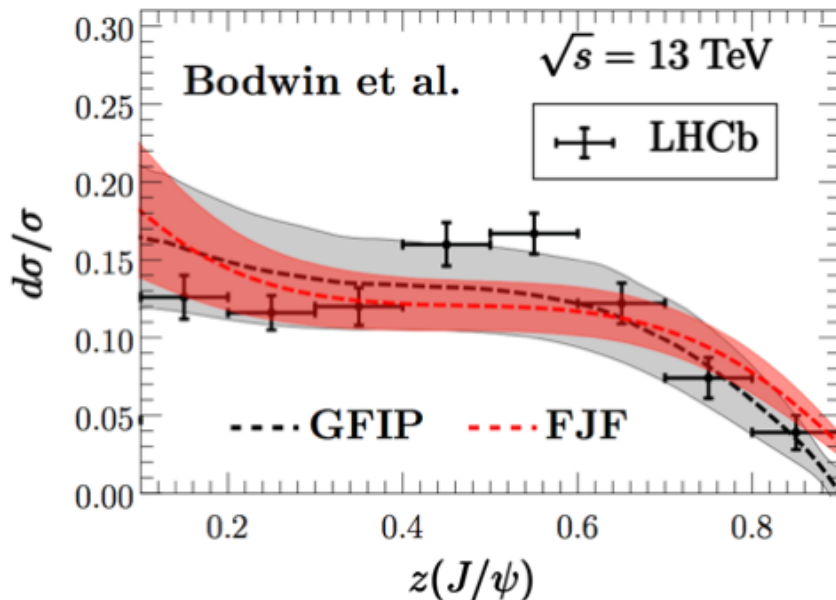
# $J/\psi$ production in jets

## □ Fitted NRQCD matrix elements:

Baumgart et al., JHEP14

Bain et al. PRL17

	$\langle \mathcal{O}^{J/\psi}(^3S_1^{[1]}) \rangle$ $\times \text{GeV}^3$	$\langle \mathcal{O}^{J/\psi}(^3S_1^{[8]}) \rangle$ $\times 10^{-2} \text{GeV}^3$	$\langle \mathcal{O}^{J/\psi}(^1S_0^{[8]}) \rangle$ $\times 10^{-2} \text{GeV}^3$	$\langle \mathcal{O}^{J/\psi}(^3P_0^{[8]}) \rangle / m_c^2$ $\times 10^{-2} \text{GeV}^3$
B & K [5, 6]	$1.32 \pm 0.20$	$0.224 \pm 0.59$	$4.97 \pm 0.44$	$-0.72 \pm 0.88$
Chao, et al. [12]	$1.16 \pm 0.20$	$0.30 \pm 0.12$	$8.9 \pm 0.98$	$0.56 \pm 0.21$
Bodwin et al. [13]	$1.32 \pm 0.20$	$1.1 \pm 1.0$	$9.9 \pm 2.2$	$0.49 \pm 0.44$



FJFs: fragmentation jet functions

GFIP: gluon fragmentation improved PYTHIA

Two are consistent

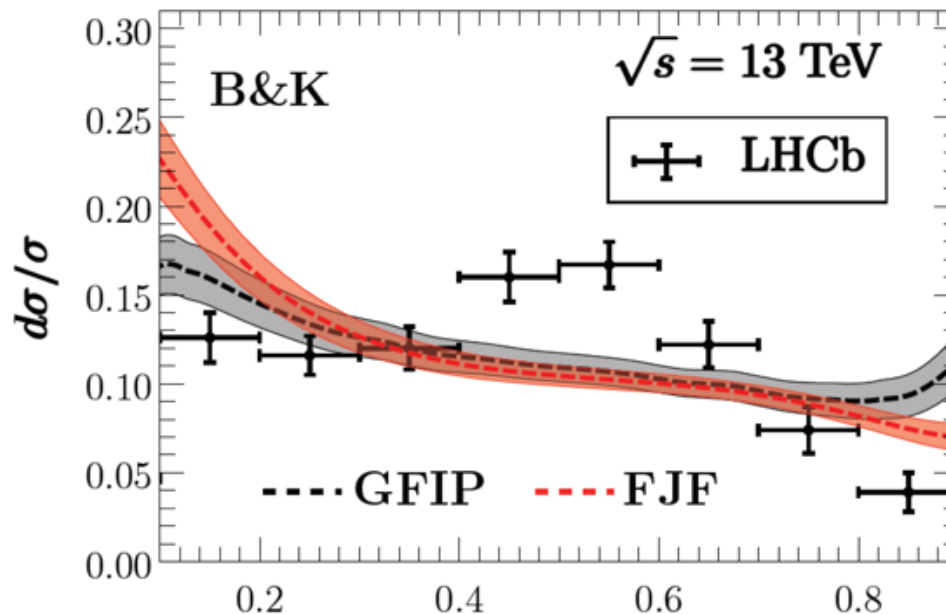
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FJFs: fragmentation jet functions

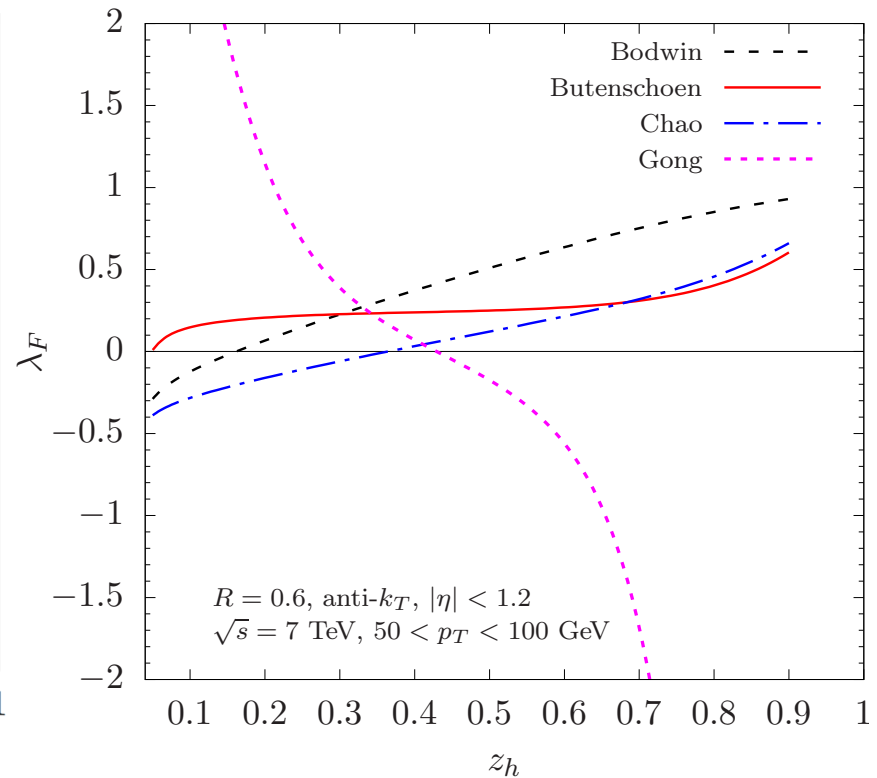
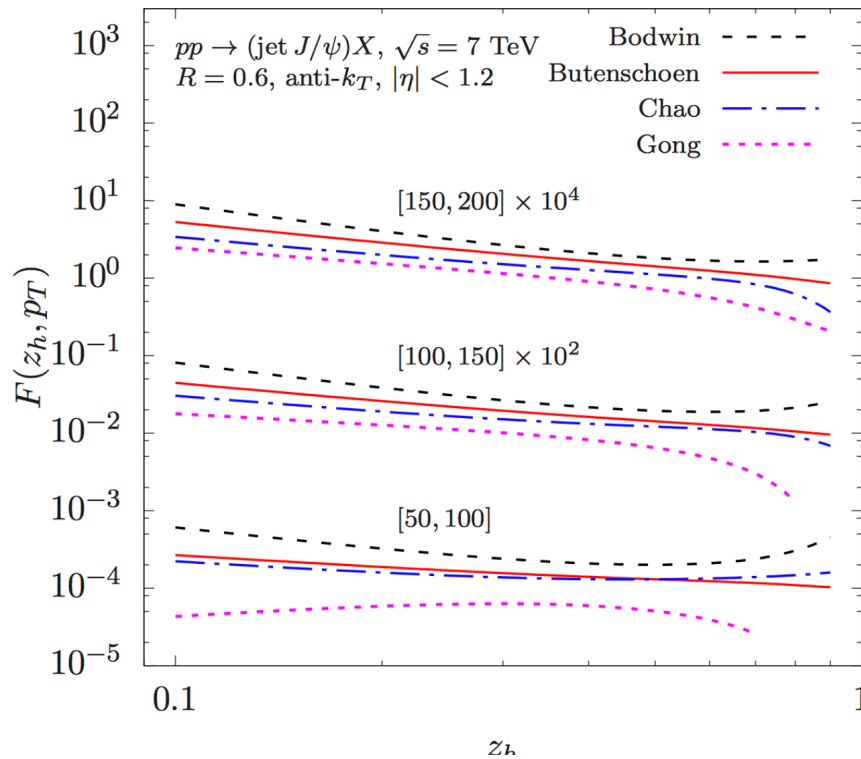
GFIP: gluon fragmentation improved PYTHIA

This fit has a poor agreement with jet data

# $J/\psi$ production and polarization in jets

## □ Polarization:

Kang, Qiu, Ringer, Xing, Zhang, PRL 2017  
See also Bain, et al, PRL 2017



**NOTE:**  $\lambda_F(z_h, p_T) = \frac{F_T^{J/\psi} - F_L^{J/\psi}}{F_T^{J/\psi} + F_L^{J/\psi}}$   
 $|\lambda_F| \leq 1!$

If  $|\lambda_F| > 1$ , the  $F_T$  or  $F_L$  is effectively negative!



**More differential than inclusive  $J/\psi$   $p_T$  spectrum, and can better discriminate different NRQCD parameterizations!**

# Summary and outlook

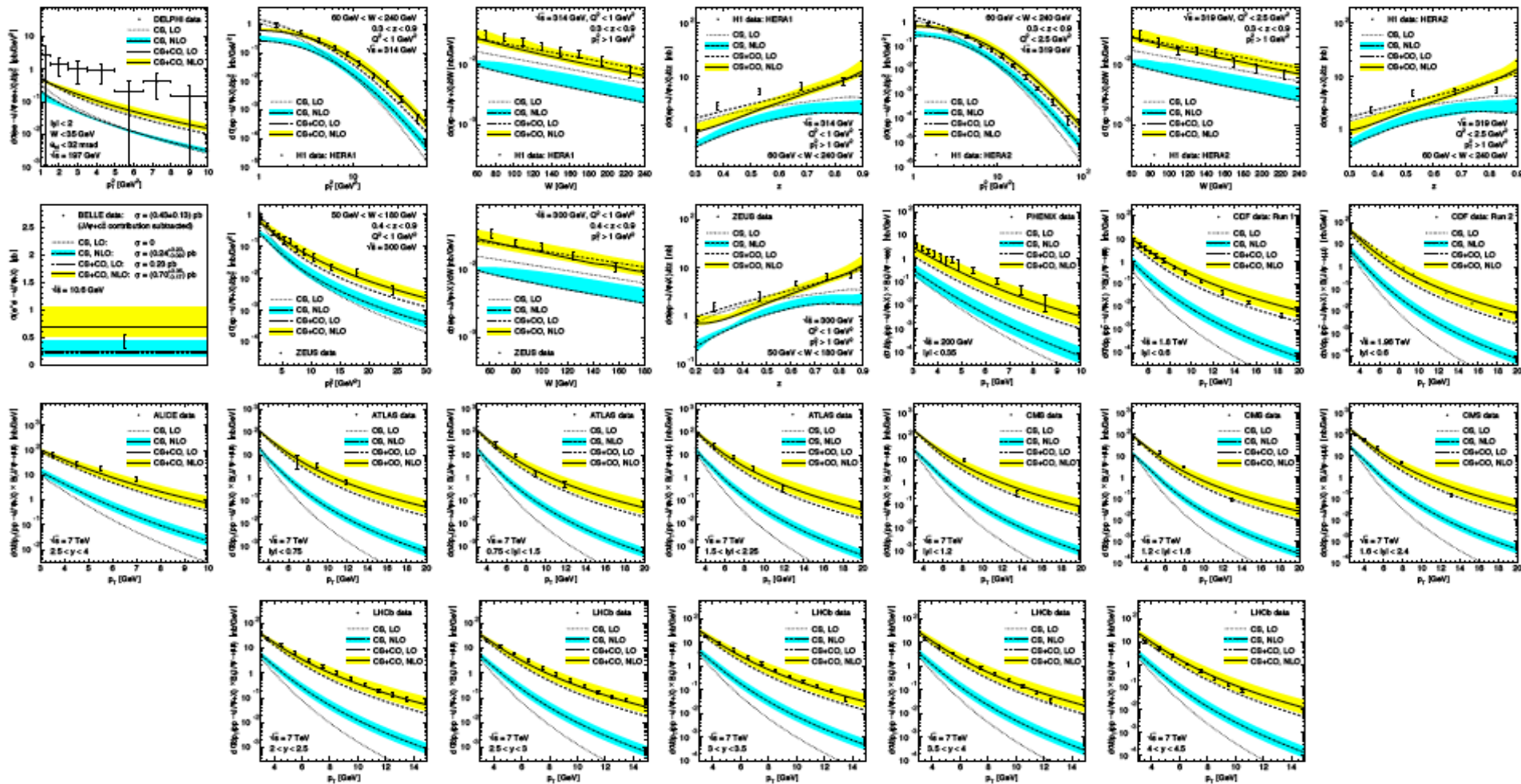
- ❑ It has been over 40 years since the discovery of  $J/\psi$ , we still have a lot of questions about their production mechanism
- ❑ When  $p_T(E) \gg m_Q$  at collider energies, earlier model calculations for the production of heavy quarkonia are not perturbatively stable  
LO in  $\alpha_s$ -expansion may not be the LP term in  $m_Q/p_T(E)$ -expansion
- ❑ QCD factorization works for both LP and NLP ( $\alpha_s$  for each power)  
Sub-leading power is very important for the  $p_T$ -shape and polarization  
*There are still a lot of unanswered questions related to quarkonium!*
- ❑ Quarkonium production and polarization in the jet could be very good observables to help pin down the production mechanism

Thank you!



**Backup slides**

# Global analysis of heavy quarkonium production



194 data points from 10 experiments, fix singlet  $\langle O[{}^3S_1[{}^1]] \rangle = 1.32 \text{ GeV}^3$

$$\langle O[{}^1S_0[{}^8]] \rangle = (4.97 \pm 0.44) \cdot 10^{-2} \text{ GeV}^3$$

$$\langle O[{}^3S_1[{}^8]] \rangle = (2.24 \pm 0.59) \cdot 10^{-3} \text{ GeV}^3$$

$$\langle O[{}^3P_0[{}^8]] \rangle = (-1.61 \pm 0.20) \cdot 10^{-2} \text{ GeV}^5$$

$$\chi^2/d.o.f. = 857/194 = 4.42$$