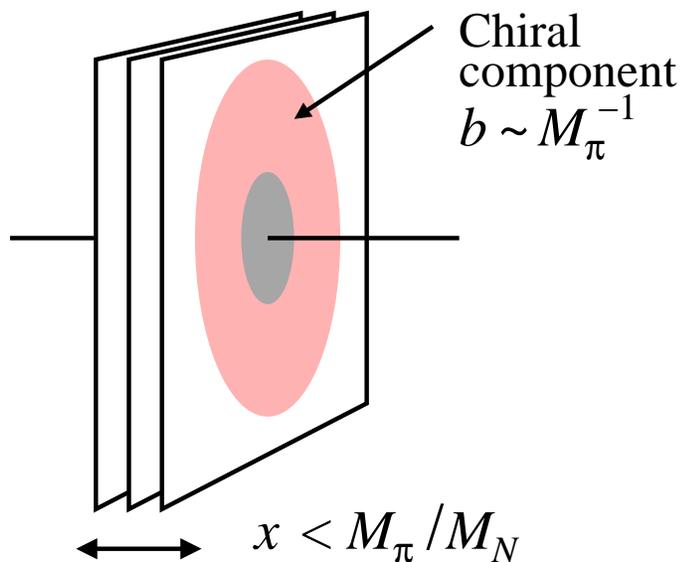


# Transverse hadron structure in QCD and chiral dynamics

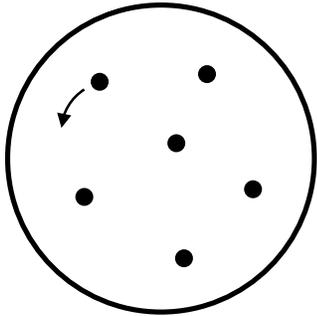
C. Weiss (JLab), Penn State Theory Seminar, 06-Dec-17

Jefferson Lab



- Spatial structure of nucleon
  - Light-front view
  - Transverse charge and current densities
  - Transverse quark and gluon distributions (GPDs)
- Chiral dynamics at large distances
  - Spontaneous symmetry breaking
  - Effective field theory
- Peripheral charge and current densities
  - Quantum-mechanical interpretation
  - $\rho$  meson in unitarity-based approach
- Peripheral quark/gluon distributions
  - Peripheral gluons and nucleon size
  - Peripheral high-energy processes in  $ep$  at EIC

# Spatial structure: Light-front view



- Non-relativistic quantum system

Particle number fixed, time absolute

$\psi(\mathbf{x}_1, \dots, \mathbf{x}_N; t)$  Schrödinger WF

$\rho(\mathbf{x}) = \sum \psi^\dagger(\dots; t)\psi(\dots; t)$  Densities

- Relativistic quantum system

Vacuum fluctuations: Particles appear/disappear

Time not absolute: How to synchronize clocks?

Light-front time  $x^+ = x^0 + x^3$

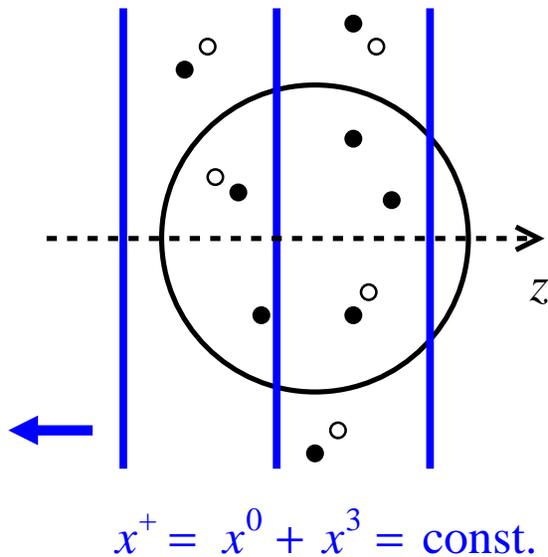
Wave function at fixed  $x^+$ : boost-invariant  
QCD: UV divergences, renormalization

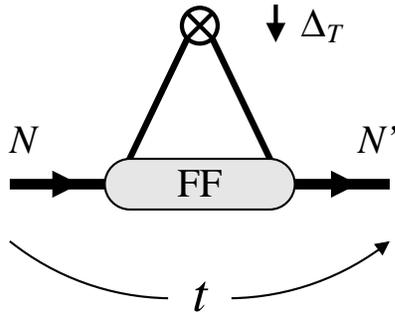
Densities at fixed  $x^+$ : boost-invariant

- Light-front view

Objective notion of spatial structure

Connection with high-energy scattering:  
Probes system at fixed LF time





- Current matrix element parametrized by invariant form factors

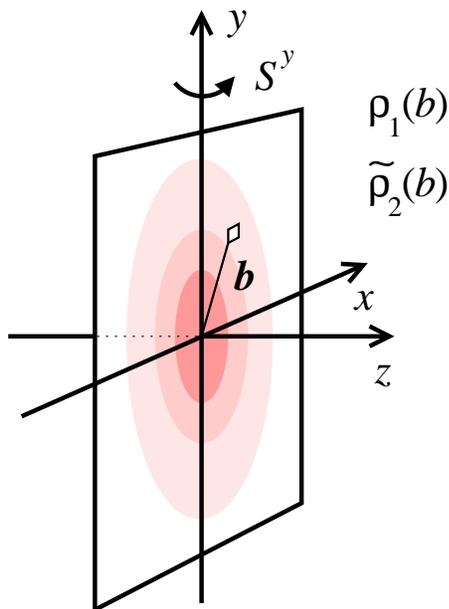
$$\langle N' | J_\mu | N \rangle \rightarrow F_1(t), F_2(t) \quad \text{Dirac, Pauli}$$

- Transverse charge/magnetization densities

$$\rho_{1,2}(b) = \int \frac{d^2 \Delta_T}{(2\pi)^2} e^{-i\Delta_T b} F_{1,2}(t = -\Delta_T^2)$$

$\mathbf{b}$  displacement from transverse center-of-mass

*Soper 76, Burkardt 00, Miller 07*



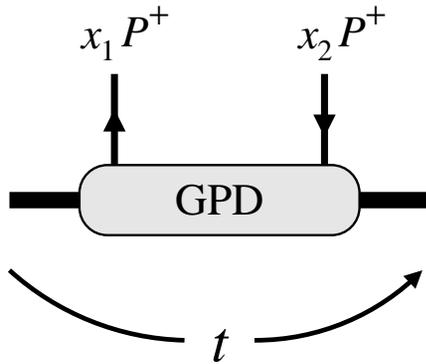
- Interpretation in polarized nucleon state

$$\langle J^+(\mathbf{b}) \rangle_{y\text{-pol}} = \rho_1(b) + (2S^y) \cos \phi \tilde{\rho}_2(b)$$

Spin-independent and -dependent current

$$\rho_1, \tilde{\rho}_2 = \langle J^+ \rangle_{\text{right}} \pm \langle J^+ \rangle_{\text{left}} \quad \text{left-right asymmetry}$$

# Spatial structure: Transverse parton distributions 4



- Generalized parton distribution

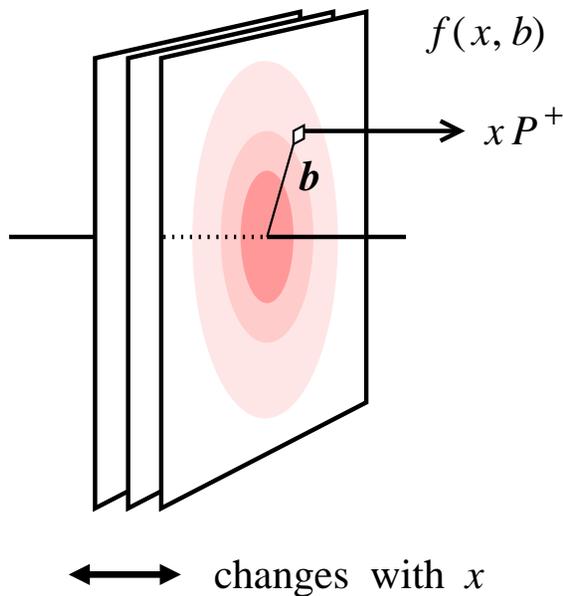
$$\langle N' | \underbrace{\bar{\psi}(0) \dots \psi(z)}_{\text{QCD light-ray operator, } z^2 = 0, \text{ scale } \mu^2} | N \rangle \rightarrow H(x_1, x_2; t), E(\dots), \dots$$

- Transverse distribution of partons

$$H(x, x; t) = \int d^2b e^{i\Delta_T b} f(x, b) \quad x_1 = x_2 = x$$

Transverse spatial distribution of partons with LC momentum  $xP^+$ : “Tomography”

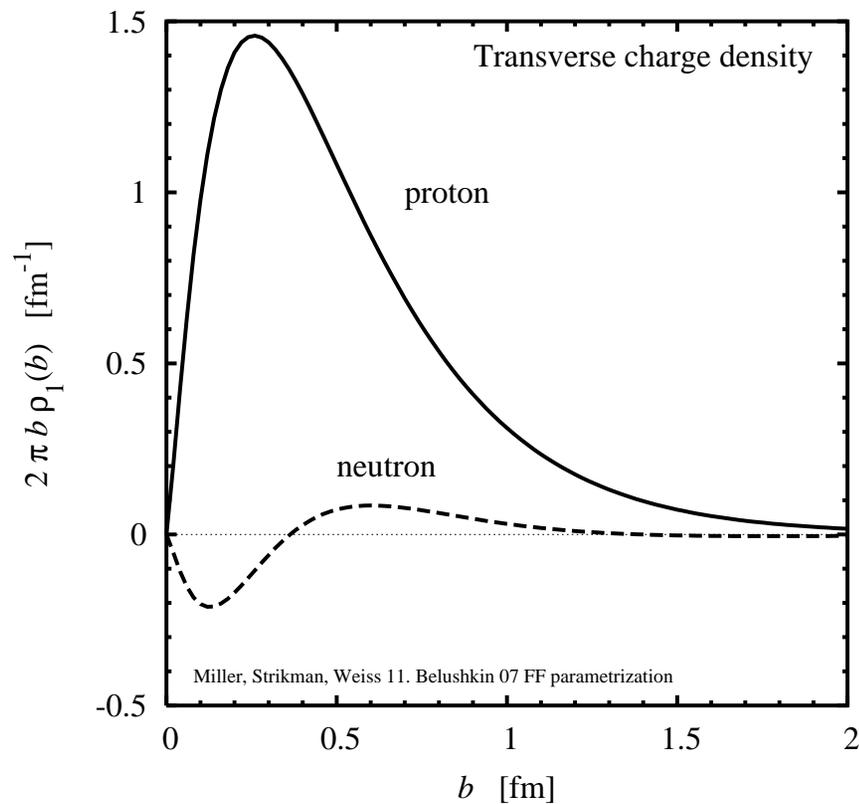
Burkardt 00



- Transverse charge density as reduction

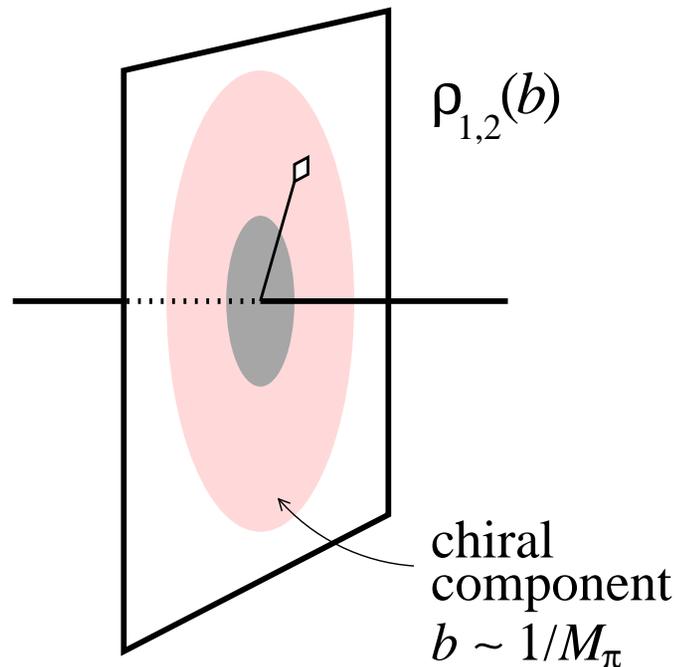
$$\rho_1(b) = \sum_q e_q \int_0^1 dx [f_q(x, b) - f_{\bar{q}}(x, b)] \quad \text{etc.}$$

Dual role of transverse densities:  
Accessible through low-energy elastic FFs,  
interpretable in context of QCD partons



- Empirical transverse densities
  - Experimental and incompleteness errors  
Venkat, Arrington, Miller, Zhan 10
  - Recent low- and high- $|t|$  FF data  
MAMI Mainz, JLab Hall A
- Many interesting questions
  - Neutron charge density
  - Flavor/isospin decomposition
  - Charge vs. magnetization densities

# Spatial structure: Peripheral distances



- Peripheral distances  $b = O(M_\pi^{-1})$

Densities governed by chiral dynamics

Calculable from first principles

- Theoretical interest

Use distance  $b \gg R_{\text{had}}$  as parameter

Study space-time picture of EFT dynamics

Quantify chiral and non-chiral contributions

- Practical interest

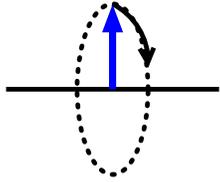
Connection with low- $|t|$  form factors,  
proton charge radius

Atomic physics and electron scattering measurements; much activity

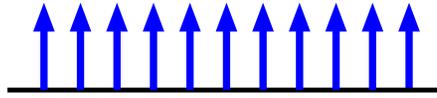
Peripheral quark/gluon structure  
in high-energy processes

# Chiral dynamics: Spontaneous symmetry breaking 7

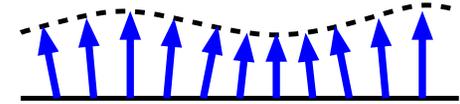
- Rotational symmetry in spin system



Rotational  
invariance  $O(3)$



$M = \langle \sum \mathbf{S} \rangle \neq 0$   
order parameter



spin wave  
massless excitation

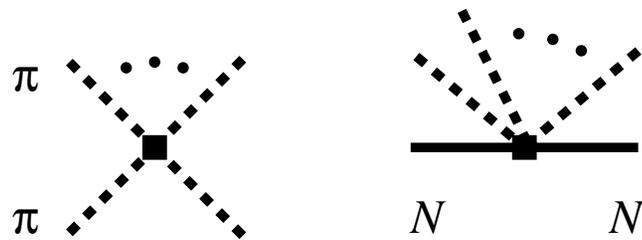
- Chiral symmetry in QCD

$L, R$  independent  
flavor rotations  
 $SU(2)_L \times SU(2)_R$

$\langle \bar{\psi}_L \psi_R \rangle \neq 0$   
chiral condensate

$\langle \dots \rangle \sim e^{i\tau\pi(x)}$   
pion wave

- Determines large-distance, low-energy behavior



- Effective dynamics

Valid at momenta  $p_\pi \sim M_\pi \ll \Lambda_\chi \sim 1 \text{ GeV}$

Structure determined by chiral invariance

Couplings parametrize short-distance dynamics

Pions couple weakly  $\propto p_\pi^\mu$

Nucleon as external source

- Constructed and solved using EFT methods

Parametric expansion in  $p_\pi/\Lambda_\chi$

Controlled accuracy, uncertainty estimates

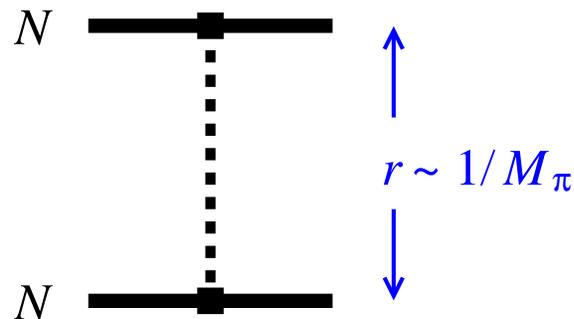
*Gasser, Leutwyler 83; Weinberg 90. Extensive work*

- Large-distance behavior of strong interactions

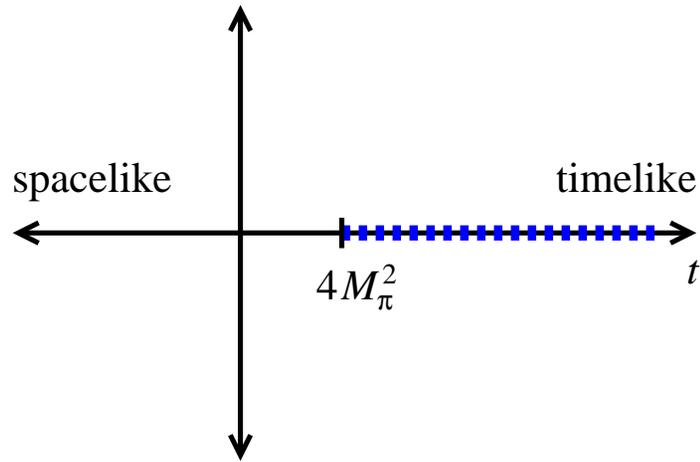
$\pi\pi$  scattering

$NN$  interaction at distances  $\sim 1/M_\pi$

$\pi N$  scattering, EM processes near threshold



# Peripheral densities: Dispersive representation



- Dispersive representation of form factor

$$F(t) = \int_{4M_\pi^2}^{\infty} \frac{dt'}{t' - t - i0} \frac{\text{Im } F(t')}{\pi}$$

Process: Current  $\rightarrow$  hadronic states  $\rightarrow N\bar{N}$

Unphysical region:  $\text{Im } F(t')$  from theory  
 Frazer, Fulco 60; Höhler et al 74

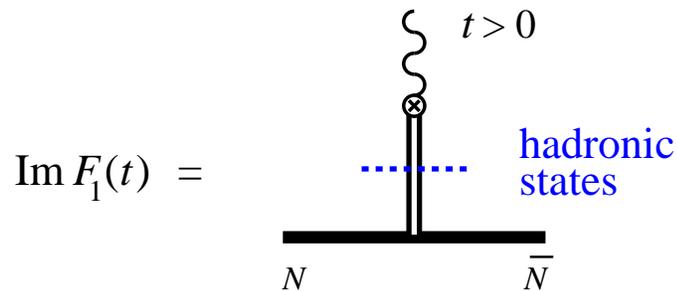
- Transverse densities

$$\rho(b) = \int_{4M_\pi^2}^{\infty} \frac{dt}{2\pi} K_0(\sqrt{t}b) \frac{\text{Im } F(t)}{\pi}$$

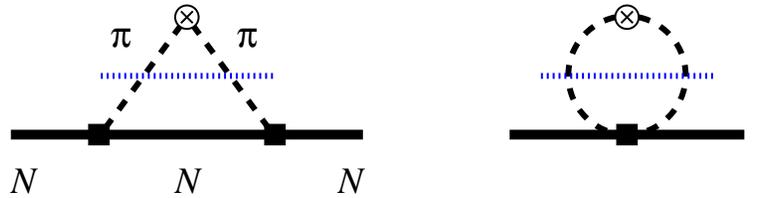
Exponential suppression of large  $t$

Distance  $b$  selects masses  $\sqrt{t} \lesssim 1/b$

Peripheral densities  $\longleftrightarrow$  low-mass states  
 Strikman, CW 10; Miller, Strikman, CW 11



Isovector:  $\pi\pi$  (incl.  $\rho$ ),  $4\pi, \dots$   
 Isoscalar:  $3\pi$  (incl.  $\omega$ ),  $K\bar{K}$  (incl.  $\phi$ ),  $\dots$

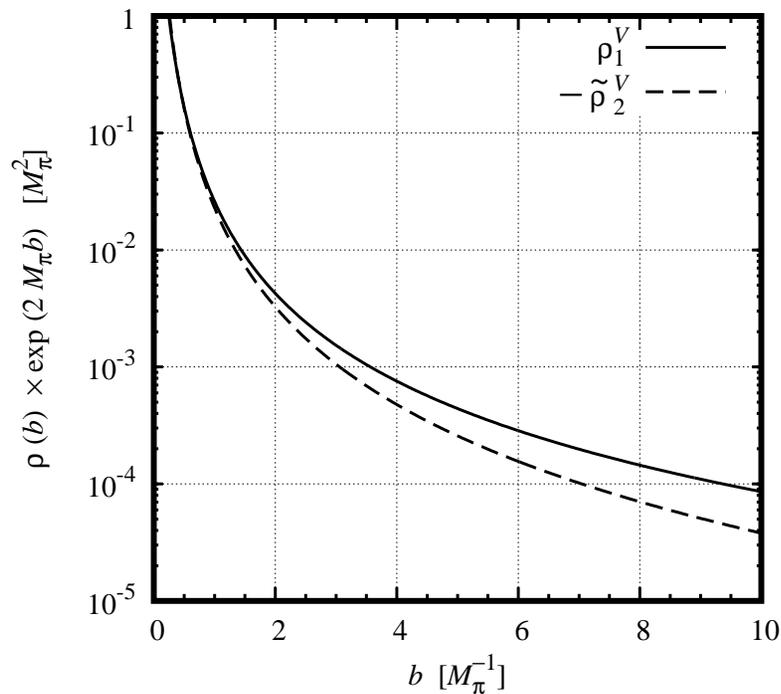


- Spectral functions from  $\chi$ EFT

$\pi\pi$  exchange, isovector channel

LO results; higher-order corrections

Gasser et al. 87; Bernard et al. 96, Kubis, Meissner 00, Kaiser 03



- Chiral component of isovector densities

$$\rho_1^V, \tilde{\rho}_2^V(b) = e^{-2M_\pi b} \times \text{fun}(M_N, M_\pi; b)$$

Yukawa tail with range  $2M_\pi$ , rich structure

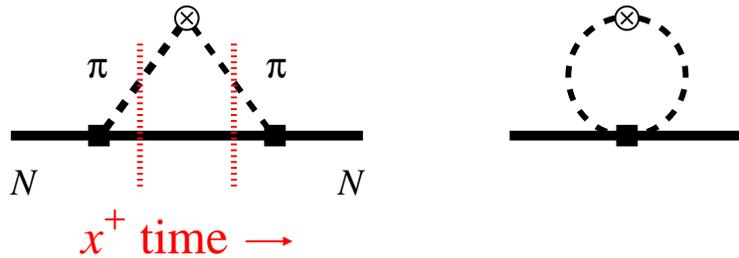
$\rho_1^V, \tilde{\rho}_2^V$  of same order in  $M_\pi/M_N$

Inequality  $\tilde{\rho}_2^V(b) \leq \rho_1^V(b)$  — explain?

Strikman, CW 10; Granados CW 13

# Peripheral densities: Time-ordered formulation

11



- Evolution in LF time  $x^+ = x^0 + x^3$
- Wave function of chiral  $\pi N$  system

Describes transition  $N \rightarrow N\pi$  in  $\chi$ EFT, calculable from chiral Lagrangian

Universal, frame-independent  
Also in high-energy processes,  $\bar{u} - \bar{d}$ , etc.

Pion momentum fraction  $y \sim M_\pi/M_N$ ,  
transverse distance  $r_T \sim M_\pi^{-1}$

Orbital angular momentum  $L_z = 0, 1$

- Densities as wave function overlap

Explains inequality  $|\rho_2^V| < \rho_1^V$  Granados, CW 13

Contact terms  $\delta(y)$  represent high-mass interm. states. Coefficient  $(1 - g_A^2)$

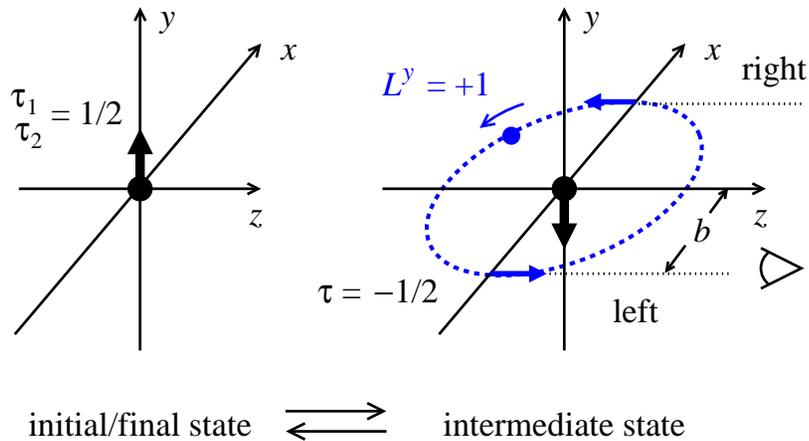
Equivalent to invariant formulation  
Granados, CW 13. See also Ji, Melnitchouk et al. 09+

$$\psi_{L=0,1}^{\pi N}(y, \mathbf{r}_T) = \frac{\langle \pi N | \mathcal{L}_\chi | N \rangle}{\underbrace{p_\pi^- + p_{N'}^- - p_N^-}_{\text{energy denominator}}}$$

$$\rho_1^V(b) = \int_0^1 dy \left[ |\psi_0|^2 + |\psi_1|^2 \right]_{r_T=b/\bar{y}}$$

+ contact term

$$\tilde{\rho}_2^V(b) = \dots \quad \psi_0^* \psi_1 + \psi_1^* \psi_0$$

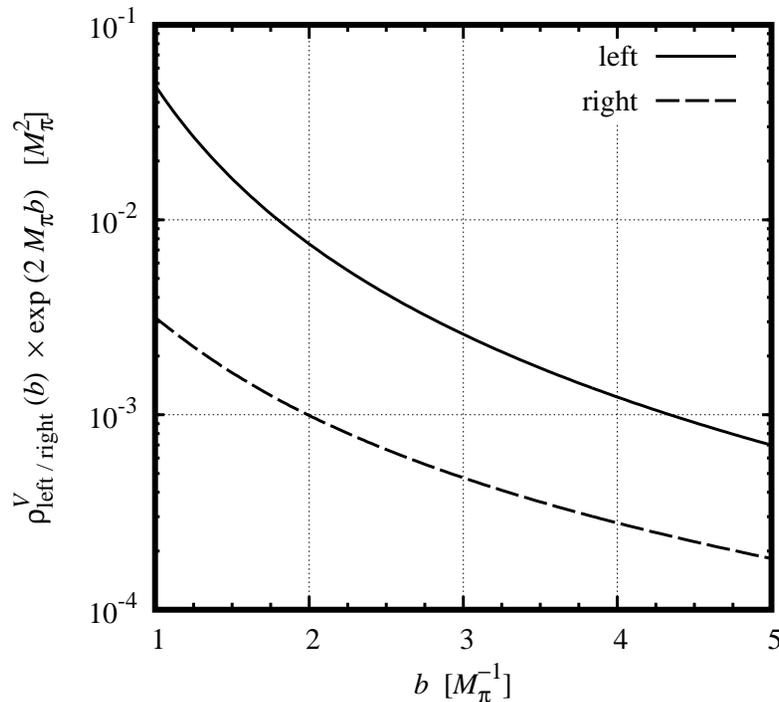


- $\chi$ EFT process as time sequence

Rest frame, nucleon polarized in  $y$ -direction

Bare  $N$  fluctuates into  $\pi N$  system via  $\chi$ EFT interaction

Peripheral densities result from  $J^+$  current carried by orbiting pion



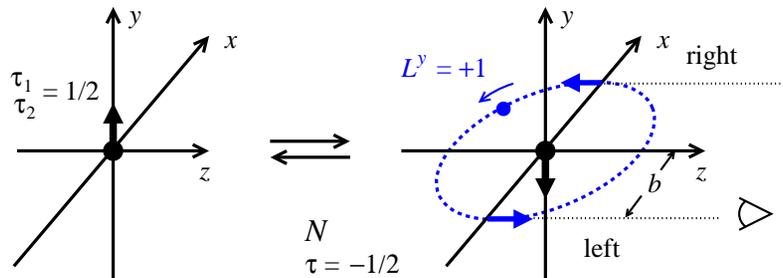
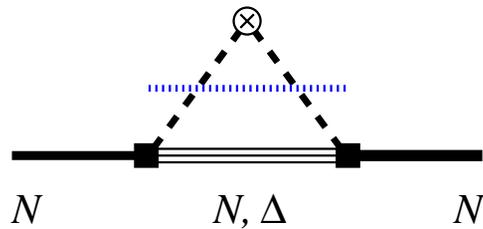
- Explains peripheral densities

$$\rho_1, \tilde{\rho}_2 = \langle J^+ \rangle_{\text{right}} \pm \langle J^+ \rangle_{\text{left}}$$

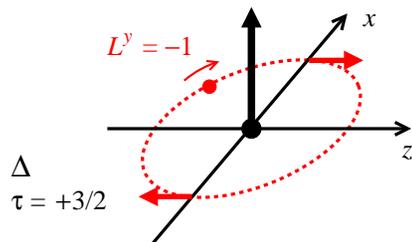
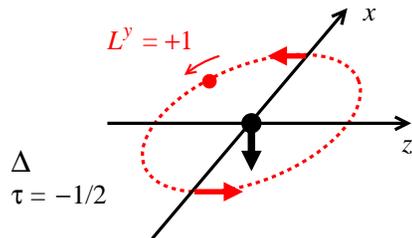
$$\langle J^+ \rangle_{\text{left}} \gg \langle J^+ \rangle_{\text{right}} \quad \text{large asymmetry}$$

Pion motion relativistic  $k_\pi \sim M_\pi$

- Quantitative picture based on  $\chi$ EFT



initial/final state



intermediate state

- Intermediate  $\Delta$  isobar

Large coupling to  $\pi N$ , low mass

Included in relativistic  $\chi$ EFT  
Rarita-Schwinger formalism, small-scale expansion

Contributes to peripheral transverse densities  
Strikman, CW 10, Granados, CW 13

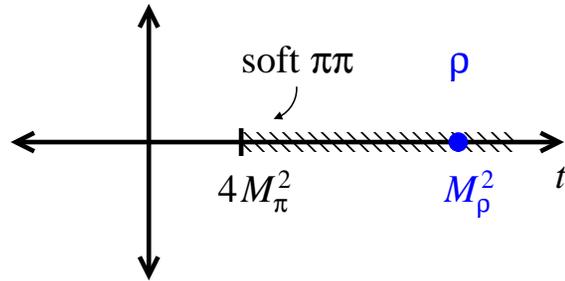
- Mechanical picture with  $\Delta$

More spin-isospin states, reverse pion motion

- Large- $N_c$  limit of QCD

$N, \Delta$  degenerate,  $M_\Delta - M_N = O(N_c^{-1})$

$N + \Delta$   $\chi$ EFT densities have correct  $N_c$ -scaling  
Granados, CW 13; see also Cohen, Broniowski 92; Cohen 96



- Region of applicability of  $\chi$ EFT?

Corrections?

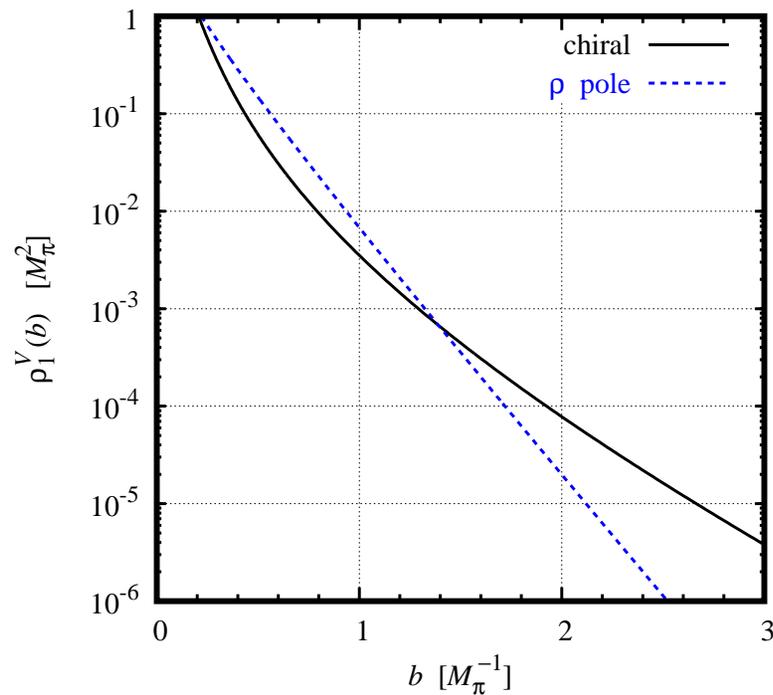
- Dispersive representation

Density  $\rho(b) \leftrightarrow$  spectral function  $\text{Im}F(t)$

Soft  $\pi\pi$  exchange near threshold  $t \sim 4 M_\pi^2$

$\rho$  resonance at  $t \sim 30 M_\pi^2$

$\rho$  dominates peripheral densities  
up to distances  $b \sim 1.5 M_\pi^{-1} \sim 2 \text{ fm}$

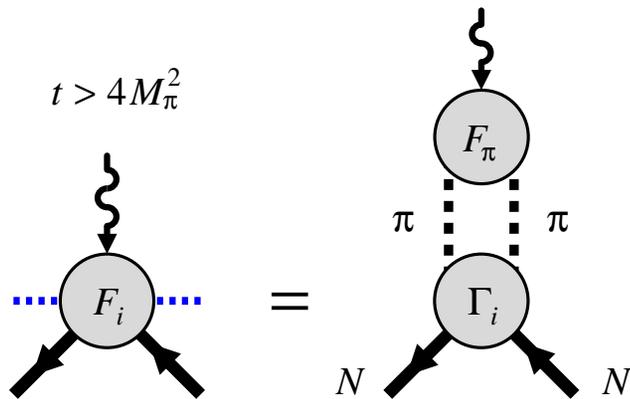


- Include  $\rho$  in systematic fashion

New unitarity-based approach

Alarcon, Blin, Vicente Vacas, Weiss, NPA 964 18 (2017)

NLO: Alarcon, Weiss, arXiv:1710.06430; in progress.



$$\begin{aligned} \text{Im}F_i(t) &= \frac{k_{\text{cm}}^3}{\sqrt{t}} \Gamma_i(t) F_\pi^*(t) \\ &= \underbrace{\frac{k_{\text{cm}}^3}{\sqrt{t}} \frac{\Gamma_i(t)}{F_\pi(t)}}_{\chi\text{EFT}} \underbrace{|F_\pi(t)|^2}_{\text{Data}} \end{aligned}$$

- Elastic unitarity relation

Timelike pion FF  $F_\pi(t)$ ,  $\pi\pi \rightarrow N\bar{N}$  partial-wave amplitude  $\Gamma_i$

Functions have same phase — Watson's theorem

Includes  $\rho$  as  $\pi\pi$  resonance

- Combine unitarity and  $\chi$ EFT

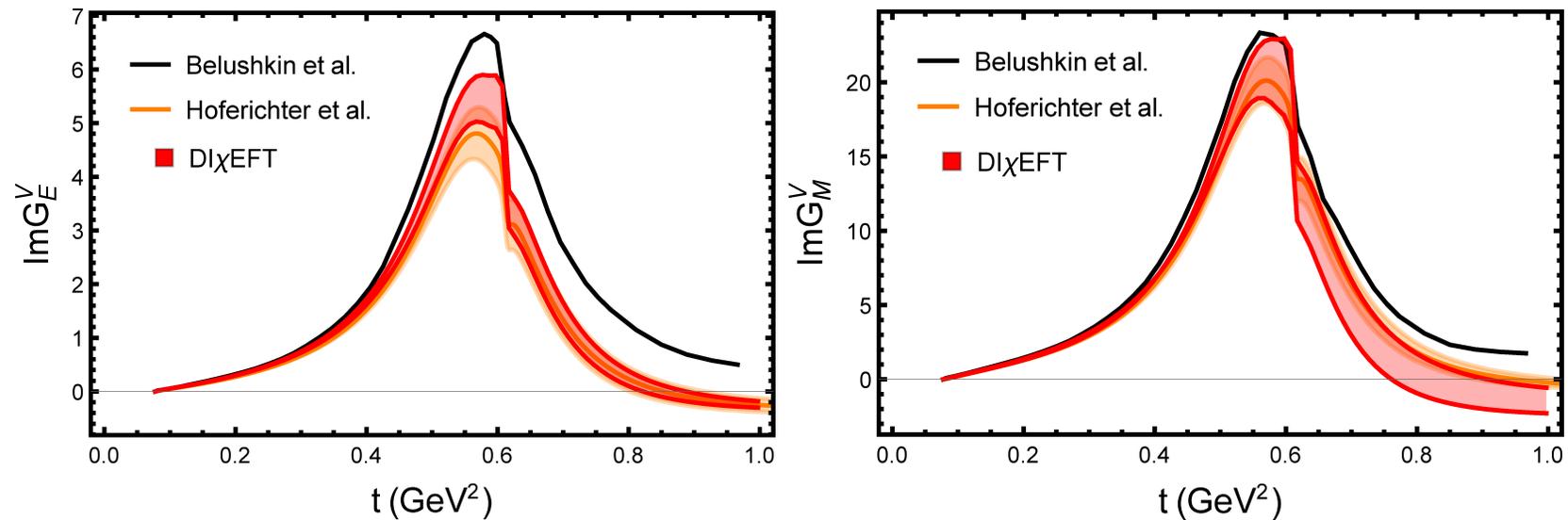
Calculate  $\Gamma_i/F_\pi$  in  $\chi$ EFT — free of  $\pi\pi$  rescattering, well convergent

Multiply with  $|F_\pi|^2$  from  $e^+e^-$  data — includes  $\pi\pi$  rescattering,  $\rho$  resonance

*N/D* method. Frazer, Fulco 60; Höhler et al 74. Many theoretical advantages. Predictive!

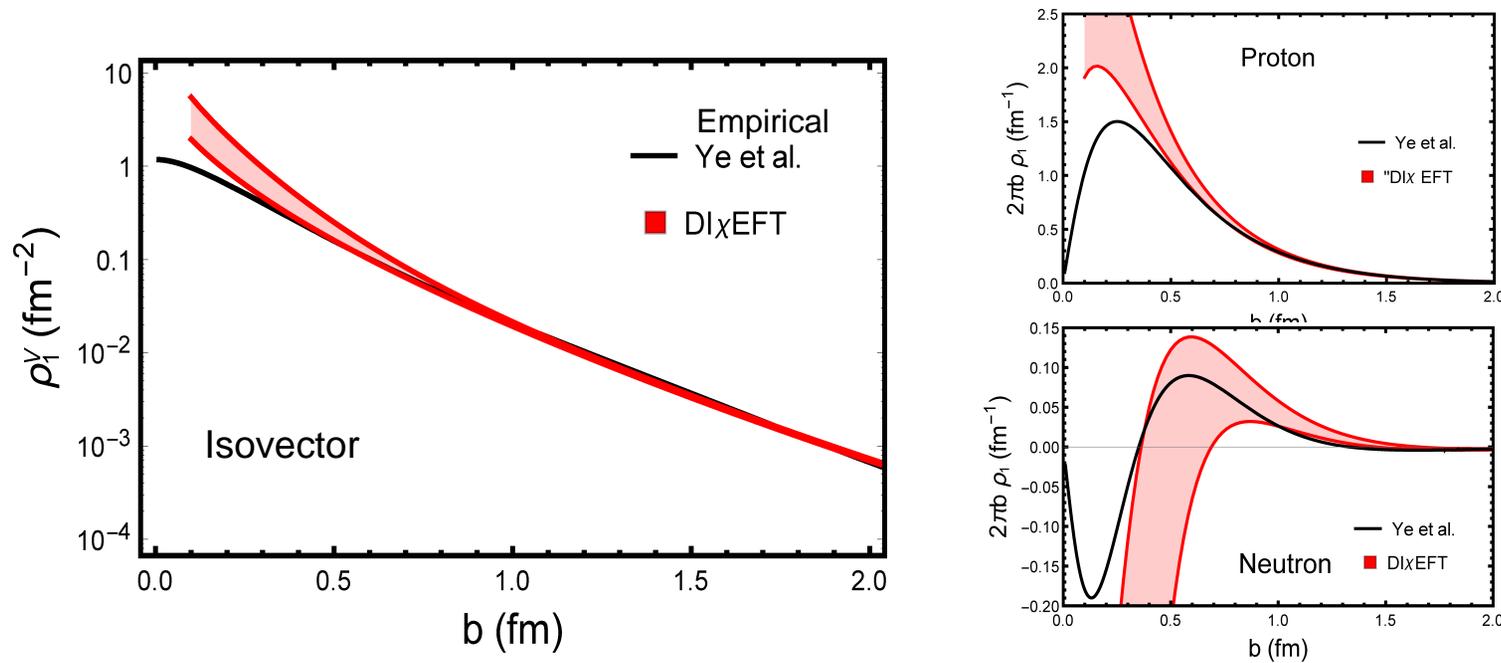
Alarcon, Hiller Blin, Vicente Vacas, Weiss, NPA 964, 18 (2017); Alarcon, Weiss, arXiv:1707.07682; arXiv:1710.06430.

# Peripheral densities: Improved spectral functions 16



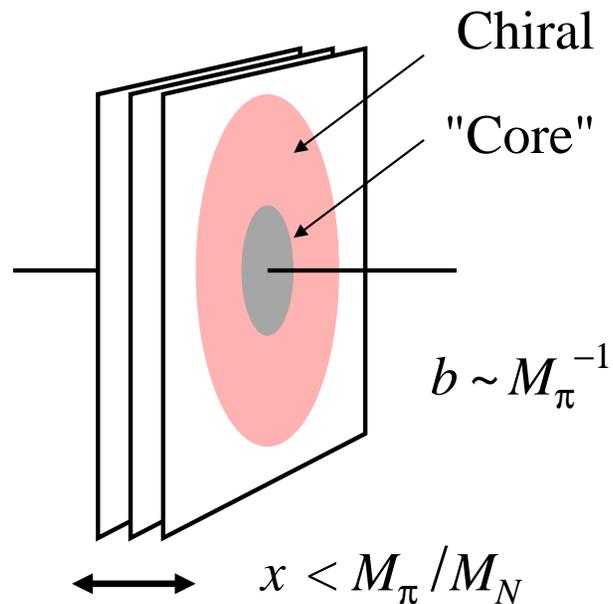
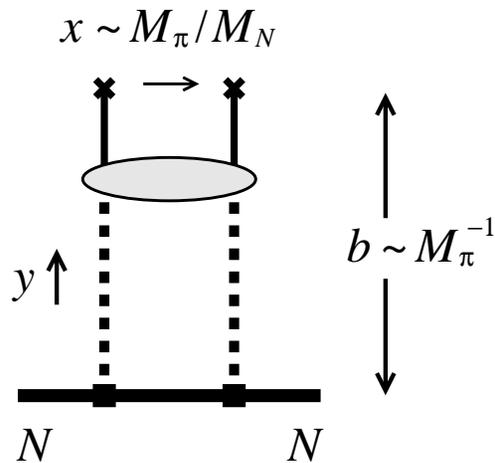
LO Alarcon, Blin, Vicente Vacas, Weiss, NPA 964 18 (2017). NLO: Alarcon, Weiss, arXiv:1710.06430; in progress.

- Spectral functions computed in  $\text{DI}\chi\text{EFT}$
- Method includes  $\pi\pi$  rescattering,  $\rho$  resonance, applicable up to  $\sim 1 \text{ GeV}^2$
- Dramatic improvement over conventional  $\chi\text{EFT}$  calculations
- Good convergence in higher orders (NLO, partial N2LO), uncertainty estimates



NLO + partial N2LO: Alarcon, Weiss, arXiv:1710.06430; in progress.

- Use DI $\chi$ EFT spectral functions to calculate peripheral transverse densities
- Peripheral isovector densities predicted down to  $b < 1$  fm with controlled accuracy  
Isoscalar densities from empirical parametrization with  $\omega, \phi$
- Peripheral transverse nucleon structure can be computed from first principles!



- Transverse spatial distribution (GPD)

$f(x, b)$  longitudinal momentum  
transverse position

- Chiral component

$b \sim M_\pi^{-1}$  transverse distance

$y \sim M_\pi / M_N$  momentum fraction  
of soft pion

$x < y$  quark/gluon in pion

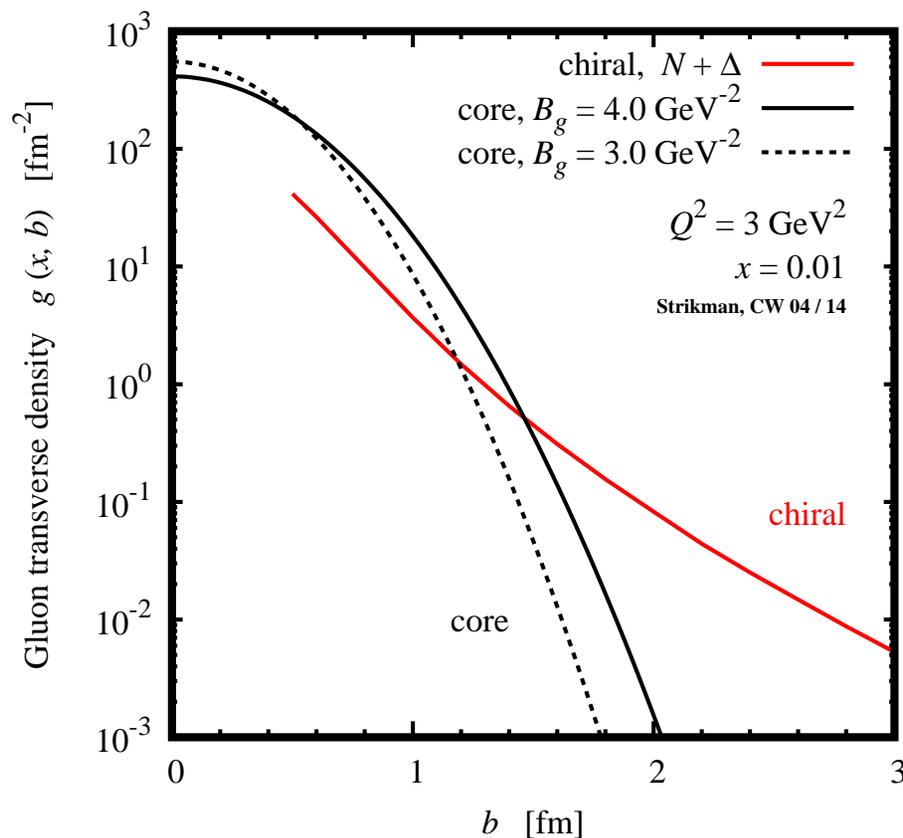
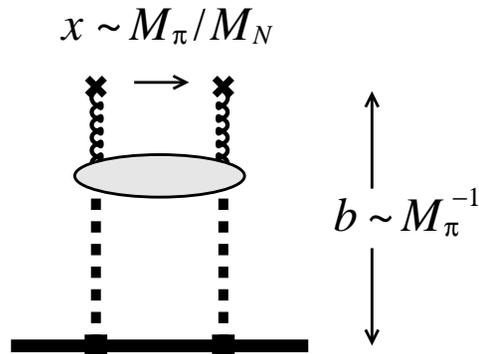
Peripheral, slow partons

- Calculable model-independently

Pion distribution in nucleon  
from chiral dynamics

Parton distribution in pion  
from independent measurements

Strikman, CW, PRD 69, 054012 (2004); PRD 80, 114029 (2009)



- Gluon transverse density

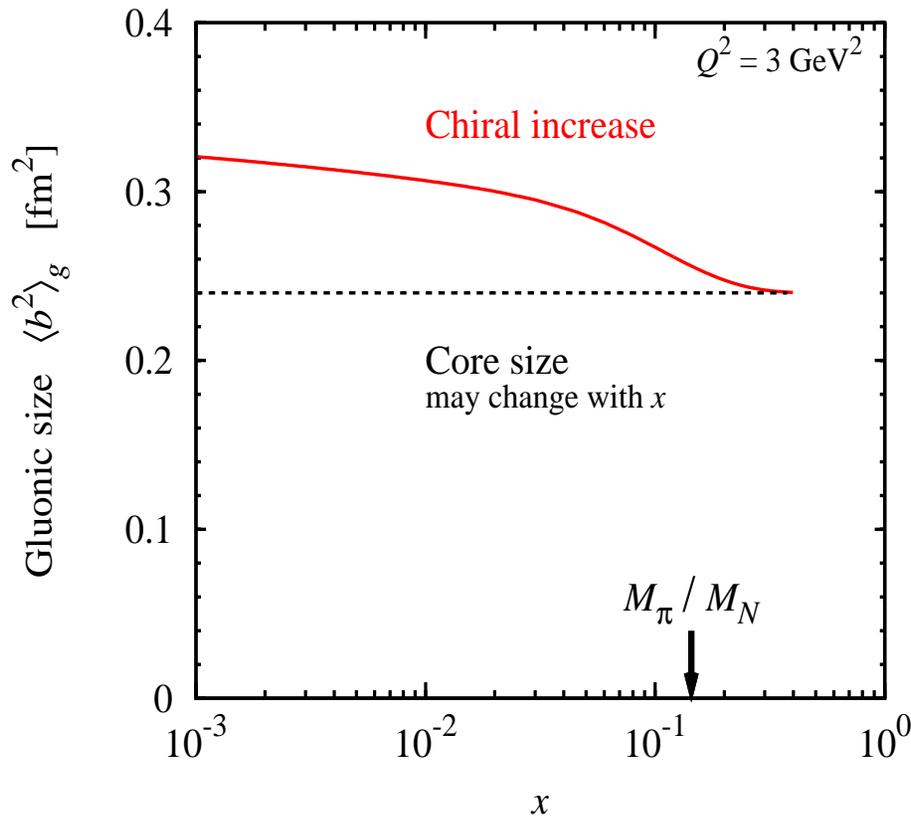
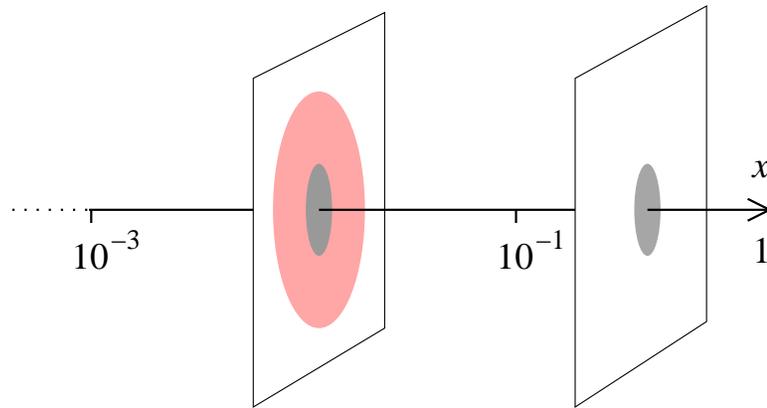
Chiral component calculated  
Strikman, CW 04

Nonchiral core modeled  
empirically using  $J/\psi$  data  
HERA, FNAL

- Chiral component is distinct only at distances  $b \gtrsim 2 \text{ fm}$

- $O(1\%)$  contribution to overall gluon density in nucleon

Model-independent feature!



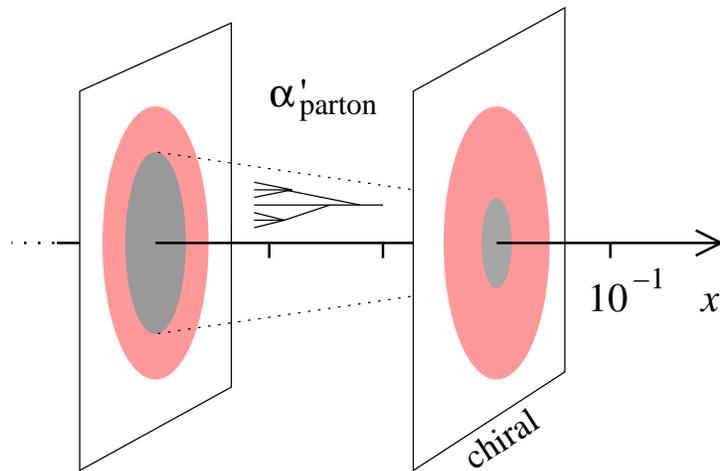
- Average transverse size

$$\langle b^2 \rangle_f(x) = \frac{\int d^2b b^2 f(x, b)}{\int d^2b f(x, b)}$$

cf. EM charge radius

Changes with  $x$  and  $Q^2$  (DGLAP)

- Chiral component causes increase below  $x \sim M_\pi / M_N$   
Strikman, CW 04 / 09
- Faster increase for quarks than for gluons  $\langle b^2 \rangle_{q+\bar{q}} > \langle b^2 \rangle_g$
- Size changes also due to non-chiral effects,  $\langle b^2 \rangle$  cannot discriminate



- Non-chiral core size grows due to Gribov diffusion

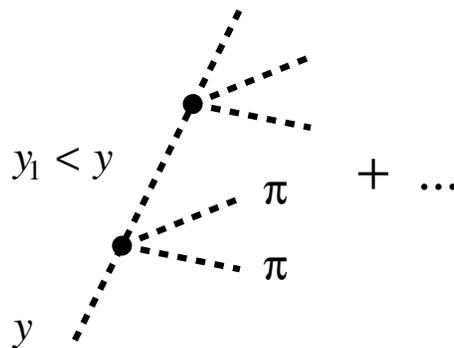
Slow because  $\alpha'_{\text{gluon}}(Q^2) \ll \alpha'_{\text{soft}}$   
if  $Q^2 \sim \text{few GeV}^2$

- Pion size can grow due to higher-order chiral effects

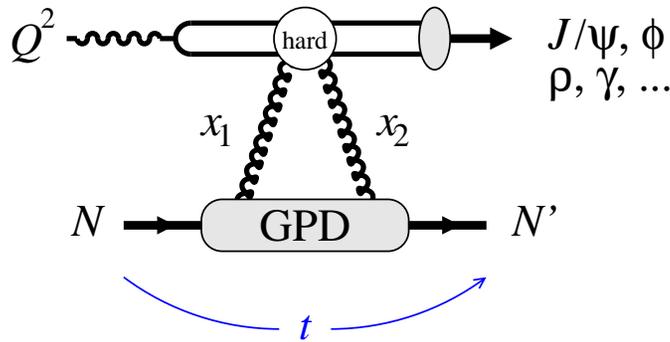
Logarithmic terms resummed using functional methods

*Polyakov, Kivel 08; PK + Vladimirov 09; Perevalova et al 11*

Could become important at  $x \ll 10^{-2}$



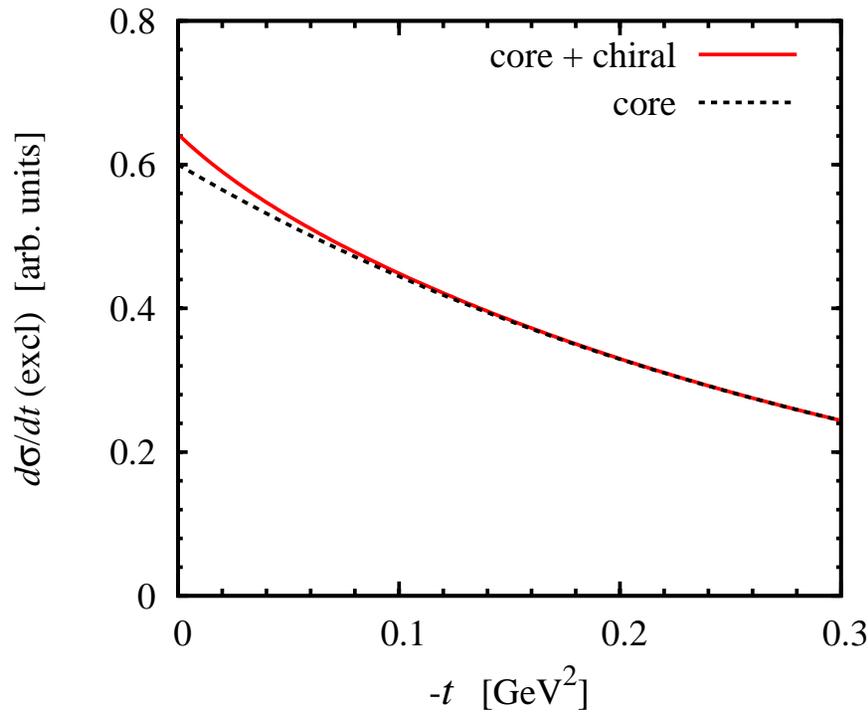
- “Single-step” chiral component should be safe for  $x > 10^{-3}$



- Hard exclusive processes:  
Transverse imaging of nucleon

$$\frac{d\sigma}{dt} \xrightarrow{x_1 = x_2 \text{ Fourier}} H_f(x_1, x_2, t) \longrightarrow f(x, b)$$

$$\langle b^2 \rangle_f = 4 \left. \frac{\partial}{\partial t} \frac{H_f(x, x, t)}{H_f(x, 0)} \right|_{t=0}$$



- Effect of chiral component

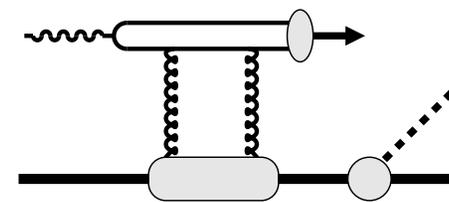
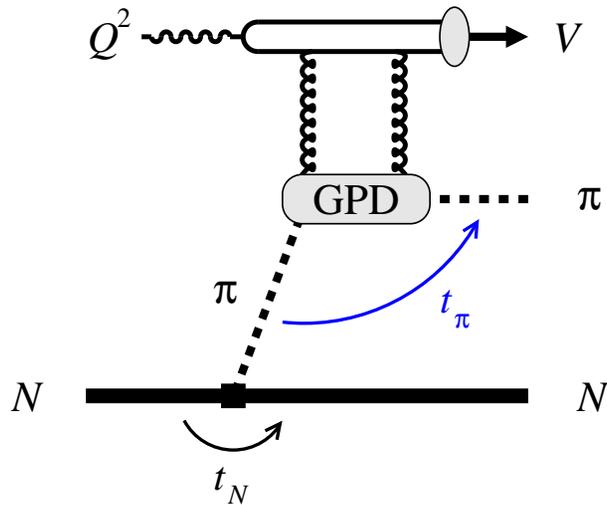
Numerically small

Visible at  $-t < 0.1 \text{ GeV}^2$

Simple model estimate,  
needs detailed simulation!

- Caution when extracting  $\langle b^2 \rangle$   
from measurements at finite  $-t$

Very challenging!



suppressed!

- Hard exclusive process on soft pion

$$k_\pi^2 = O(M_\pi^2) \text{ pion soft}$$

Requires  $x \ll M_\pi/M_N \sim 0.1$

- Kinematics with  $p_T(\pi) \gg p_T(N)$  suppresses production on nucleon

$$F_{\pi NN}(t) \text{ softer than } GPD_\pi(t)$$

- Probe pion GPD at  $|t_\pi| \sim 1 \text{ GeV}^2$

Fundamental interest

Moments calculable in LQCD

- Detection requirements

Forward nucleon  $p_T \sim 100 \text{ MeV}$

Forward pion  $p_T \lesssim 1 \text{ GeV}$

Direct probe of chiral component!

Needs detailed simulation...

Strikman, CW PRD69, 054012 (2004)

- Light–front view provides spatial representation of relativistic system
  - Elastic FFs reveal transverse densities
  - Independent of dynamics — can be applied to QCD,  $\chi$ EFT, ...
- Peripheral transverse densities from  $\chi$ EFT
  - Chiral expansion justified by  $b = O(M_\pi^{-1})$  — new parameter
  - Quantum-mechanical picture of low–energy chiral nucleon structure
  - New unitarity-based approach includes  $\pi\pi$  rescattering, predicts densities at  $b \gtrsim 1$  fm
  - Many applications and extensions: Form factors of energy-momentum tensor  $2\pi$ , isoscalar vector current  $3\pi$ , axial current  $3\pi$
- Peripheral partons in nucleon
  - Chiral dynamics expressed in partonic structure
  - Could be probed in pion knockout processes at EIC