3D Spatial Imaging: from JLab 12 GeV to the EIC



Daria Sokhan

University of Glasgow, Scotland



Lecture course for the 33rd annual Hampton University Graduate Studies Programme (HUGS)

> 29th May - 15th June 2018 Jefferson Lab, Virginia, USA

General outline of lecture material:

- * Imaging at the sub-nucleon scale, Generalised Parton Distributions and how to access them
- Deeply Virtual Compton scattering
- Deeply Virtual Meson Production
- * Experimental measurements @ JLab
- ***** What we have learned pre JLab-12
- ***** Tomography with JLab-12 and the EIC

(5 lectures)

An abridged history of nucleon imaging

Before 1956: the nucleon is point-like and fundamental..





Robert Hofstadter 1915 - 1990 (Wikipedia)

ABORATORY ANGLE OF SCATTERING (IN DEGREES

1960s: the Ouark Model. Nucleons are composed of three valence quarks! Gell-Mann (Nobel Prize 1969), Zweig.

1968: Deep Inelastic scattering at SLAC: scaling observed. The proton consists of point-like charges: partons! Friedman, Kendall, Taylor: Nobel Prize 1990

1972: Theory of QCD developed.







1970s-1990s: Deep Inelastic Scattering reveals a

rich structure: quark-gluon sea, flavour distributions, puzzles of spin... what you see depends on how closely you look!

21st Century: High-precision imaging of quarks and gluons. 3D tomography of the nucleon: spatial and momentum distributions inside it across all scales.







Electron scattering: a reminder of terminology

Elastic scattering: initial and final state is the same, only momenta change.

Deep inelastic scattering (DIS):

state of the nucleon changed, new particles created.



e γ^* N

Measurements:

- \star Inclusive only the electron is detected
- ★ Semi-inclusive electron and typically one hadron detected
- \star Exclusive all final state particles detected



Complementary information on the nucleon's structure



Scales of resolution – an elephantine analogy

Lyuba, baby mamoth found in Siberia, imaged with visible light...

International Mammoth Committee



~ MeV²

 \mathbf{Q}^2



 $O^2 \sim MeV^2$

Scales of resolution – an elephantine analogy

Lyuba, baby mamoth found in Siberia, imaged with visible light... ... and X-rays.

International Mammoth Committee

> Equivalent wavelength of the probe:



What you see depends on what you use to look...

 e^{-}

 $O^2 >> GeV^2$

The 2D spatial image

Lepton (eg: electron, neutrino) scattering off a nucleon reveals different aspects of nucleon structure.

Elastic Scattering



Cross-section parameterised in terms of Form Factors (Pauli, Dirac, axial, pseudoscalar)



Transverse quark distributions: charge, magnetisation.

Charge density inside a nucleon

Proton

Neutron



C. Carlson, M. Vanderhaeghen PRL 100, 032004 (2008)



First experimental evidence of partons inside a nucleon

Cross-section parameterised in terms of polarised and unpolarised Structure Functions



Longitudinal momentum and helicity distributions of partons

Parton Distribution Functions

Momentum distributions of quarks and gluons within a nucleon.

x: longitudinal momentum of parton as a fraction of nucleon's momentum.



A full "knowledge" of the nucleon...



... is hard to come by



G. Renee Guzlas, artist.

What you see depends also on how you look...







Wigner function: • full phase space parton distribution of the nucleon

х

 δz_{\perp}

 $f(x,b_1)$

 \boldsymbol{b}_{\perp}



relate, in the infinite momentum frame, transverse position of partons (*b*_⊥) to longitudinal momentum (*x*).

 $\int d^2 k_T$

Deep exclusive reactions, e.g.: Deeply Virtual Compton Scattering, Deeply Virtual Meson production, ...

Wigner function: full phase space parton distribution of the nucleon



Generalised Parton Distributions (GPDs)



Fourier Transform of electric Form Factor: transverse charge density of a nucleon



proton

neutron

C. Carlson, M. Vanderhaeghen PRL 100, 032004 (2008)





Generalised Parton Distributions (GPDs) — proposed by Müller (1994), Radyushkin, Ji (1997).

* Directly related to the matrix element of the energymomentum tensor evaluated between hadron states.

In the infinite momentum frame, can be interpreted as relating transverse position of partons (impact parameter), b_{\perp} , to their longitudinal momentum fraction (*x*).

Tomography: 3D image of the nucleon.





* First studies at JLab and DESY (HERMES), currently at JLab and CERN (COMPASS). A crucial part of the JLab12 programme and, in the future, of the EIC.

Deeply Virtual Compton scattering



*
$$Q^2 = -q^2 = -(p_e - p_e')^2$$

q: four-momentum transfer to the struck quark

*
$$t = (\mathbf{p}_n - \mathbf{p}'_n)^2$$
 $\mathbf{v} = E_e - E'_e$

t: quantifies change in fourmomentum of the nucleon

* Bjorken variable $x_B = \frac{Q^2}{2\mathbf{p}_n \cdot \mathbf{q}}$

In the Bjorken limit (high Q^2 , high v), low t and infinitenucleon-momentum frame:

Skewness:

$$\boldsymbol{\xi} \cong \frac{\boldsymbol{x}_B}{2 - \boldsymbol{x}_B}$$

* $x+\xi$ and $x-\xi$:

initial and final longitudinal momentum of struck quark, as a fraction of nucleon momentum

* Factorisation: allows to separate the "hard"-scattering of electron off a quark from the "soft" part of the interaction inside the nucleon.



*At sufficiently high Q², can extract GPD information from cross-sections and asymmetries in DVCS and related processes.

Definitions: Order and Twist

* Twist: powers of $\frac{1}{\sqrt{Q^2}}$ in the DVCS amplitude. Leading-twist (LT) is twist-2.

* Order: introduces powers of $\, lpha_{s} \,$



* LO requires $Q^2 >> M^2$ (*M*: target mass)

A closer look at GPDs



Independent of quark helicity, unpolarised GPDs

 $\left. \begin{array}{c} \widetilde{H}(x,\boldsymbol{\xi},t) \\ \\ \widetilde{E}(x,\boldsymbol{\xi},t) \end{array} \right\}$

Helicity-dependent, polarised GPDs

If no longitudinal momentum transfer to quark ($\xi=0$) and no net momentum transfer to nucleon (t=0):

$$H(x,0,0) = q(x)$$
$$\widetilde{H}(x,0,0) = \Delta q(x)$$



Two of the GPDs reduce to PDFs

A closer look at GPDs

* The first Mellin moments of the GPDs reduce to Form Factors:

$$\int_{-1}^{1} dx \ H(x,\xi,t) = F_{1}(t) \qquad \int_{-1}^{1} dx \ \widetilde{H}(x,\xi,t) = G_{A}(t)$$

$$\int_{-1}^{1} dx \ E(x,\xi,t) = F_{2}(t) \qquad \int_{-1}^{1} dx \ \widetilde{E}(x,\xi,t) = G_{P}(t)$$
istinct regions:

* Two distinct regions:

 $\begin{aligned} |x| > |\xi| & \text{The DGLAP region: scattering from} \\ & \text{quarks or anti-quarks} \end{aligned}$

 $|x| < |\xi|$ The ERBL region: scattering results in a $q\overline{q}$ pair.

* Fourier Transform of GPD w.r.t. Δ gives the transverse spatial distribution at each given *x*. Small changes in transverse momentum carry sensitivity to transverse structure at large distances within the nucleon.

The Nucleon Spin Puzzle

* What contributes to nucleon spin?

accessed, in Ji's decomposition, via **GPDs**, which

contain information on total angular momentum, J_{q} .

* 1980's: European Muon Collaboration (EMC) measures contribution of valence quarks to proton spin to be ~ 30 %. Subsequent deep inelastic scattering (DIS) experiments confirm.



In Ji's decomposition of nucleon spin, the gluon spin and OAM terms cannot be separated.

GPDs and nucleon spin

$$J_{N} = \frac{1}{2} = \frac{1}{2}\Sigma_{q} + L_{q} + J_{g}$$

* Ji's relation:
$$J^q = \frac{1}{2} - J^g = \frac{1}{2} \int_{-1}^{1} x dx \left\{ H^q(x,\xi,0) + E^q(x,\xi,0) \right\}$$

Second Mellin moments of the GPDs contain information on the total angular momentum carried by quarks.

Note that the contribution from GPD H is given by the quark momentum, already known from PDFs:

$$2J^{q} = \int_{0}^{1} \mathrm{d}x \, x[q(x) + \bar{q}(x)] + \int_{-1}^{+1} \mathrm{d}x \, xE^{q}(x, 0, 0)$$

Experimental paths to GPDs

Accessible in *exclusive* reactions, where all final state particles are detected.



cliparts.co

Trodden paths, or ones starting to be explored:

Deeply Virtual Compton Scattering (DVCS)
Deeply Virtual Meson Production (DVMP)
Time-like Compton Scattering (TCS)
Double DVCS



TCS

Virtual photon time-like



DDVCS One time-like, one space-like virtual photon



υνΜΡ



DVCS Virtual photon space-like

Measuring DVCS

* Process measured in experiment:



Compton Form Factors in DVCS

Experimentally, DVCS amplitude is proportional to Compton Form Factors (CFFs) — sums of GPD integrals over *x*:

$$\int_{-1}^{1} dx F(\mp x, \xi, t) \left[\frac{1}{x - \xi + i\epsilon} \pm \frac{1}{x + \xi - i\epsilon} \right]$$

$$GPD$$

$$Plus sign for unpolarised GPDs, minus for polarised.$$

Can be decomposed into real and imaginary parts:

Cauchy's principal value integral

$$\Re \mathbf{e}\mathcal{F} = \mathcal{P} \int_{-1}^{1} dx \left[\frac{1}{x-\xi} \mp \frac{1}{x+\xi} \right] F(x,\xi,t)$$

 $\Im m \mathcal{F}(\xi, t) = -\pi [F(\xi, \xi, t) \mp F(-\xi, \xi, t)]$

Both parts are accessible in different experimental observables

Compton Form Factors in DVCS

At leading twist, leading order:



of CFFs in DVCS.



$$A = \frac{d\vec{\sigma} - d\vec{\sigma}}{d\vec{\sigma} + d\vec{\sigma}} = \frac{\Delta\sigma}{d\vec{\sigma} + d\vec{\sigma}}$$

***** Beam-charge asymmetry, from a probe with two opposite charges (e^+/e^-)

* Beam-spin asymmetry, from different electron helicities

* Target-spin asymmetry, from different target polarisation orientations

***** Double-spin asymmetries, from combining beam and target polarisations

Which DVCS experiment?



Other reactions to get at GPDs

* **Time-like Compton scattering**: virtual photon is time-like. At leading order, access same integrals of GPDs. At higher orders, they differ.





* Double Deeply Virtual Compton scattering: two virtual photons: the second vertex provides a second variable Q'^2 . This allows direct access to *x*, but cross-sections are suppressed by another factor of Ω .

Deeply Virtual Meson Production: the meson vertex provides flavour information. Amplitude now depends on GPDs and the meson Distribution Amplitudes. In light mesons, more sensitive to higher order and higher twist.

In vector mesons, gluon GPDs appear at lowest order!



Deeply Virtual Meson Production



Plus, DVMP enables flavour decomposition of quark GPDs!

Transversity GPDs

* Transversity GPDs appear in the scattering amplitude when the virtual photon has a transverse polarisation.

Not accessible at leading twist in DVCS, but appearing in DVMP!

 \hat{F}_T can be related to the transverse anomalous magnetic moment:

$$\kappa_T = \int_{-1}^{+1} \tilde{E}_T(x,\xi,t=0) \, dx$$

* and H_T to the transversity distribution: $H_T(x,0,0) = h_1(x)$

which describes distribution of transverse partons in a transverse nucleon

$$h_1 = -$$

***** The combination
$$\bar{E}_T = 2\tilde{H}_T + E_T$$

is related to spatial density of transversely polarised quarks in an unpolarised nucleon.

DVMP Cross-section



where
$$\epsilon = \frac{1 - y - \frac{Q^2}{4E^2}}{1 - y + \frac{y^2}{2} + \frac{Q^2}{4E^2}}$$

is the ratio of the fluxes of longitudinally (L) and transversely (T) polarised virtual photons and

$$y = pq/qk = \nu/E$$
DVMP Cross-sections

***** Unpolarised cross-section for meson-production:

$$\frac{d^2\sigma}{dtd\phi_{\pi}} = \frac{1}{2\pi} \left[\left(\frac{d\sigma_T}{dt} + \epsilon \frac{d\sigma_L}{dt} \right) + \epsilon \cos 2\phi_{\pi} \frac{d\sigma_{TT}}{dt} + \sqrt{2\epsilon(1+\epsilon)} \cos \phi_{\pi} \frac{d\sigma_{LT}}{dt} \right]$$

* Structure functions which parametrise the cross-section are related to scattering amplitudes in the interaction thus:

$$\frac{d\sigma_i}{dt} = \frac{1}{16\pi} \frac{x_B^2}{1 - x_B} \frac{1}{Q^4} \frac{1}{\sqrt{1 + 4x_B^2 m^2/Q^2}} \sum_{\text{spins}} \left| \mathcal{A}(\gamma_i^* p \to M p) \right|^2$$

i = T, L

DVMP Cross-sections and GPDs

Relation between structure functions in DVMP and GPDs:

$$\begin{split} \frac{d\sigma_L}{dt} &= \frac{4\pi\alpha}{k'} \frac{1}{Q^6} \bigg\{ (1-\xi^2) |\langle \tilde{H} \rangle|^2 - 2\xi^2 \operatorname{Re}[\langle \tilde{H} \rangle^* \langle \tilde{E} \rangle] - \frac{t'}{4m^2} \xi^2 |\langle \tilde{E} \rangle|^2 \bigg\} \\ &\frac{d\sigma_T}{dt} &= \frac{4\pi\alpha}{2k'} \frac{\mu_\pi^2}{Q^8} \bigg[(1-\xi^2) |\langle H_T \rangle|^2 - \frac{t'}{8m^2} |\langle \bar{E}_T \rangle|^2 \bigg] \\ &\frac{d\sigma_{LT}}{dt} &= \frac{4\pi\alpha}{\sqrt{2}k'} \frac{\mu_\pi}{Q^7} \xi \sqrt{1-\xi^2} \frac{\sqrt{-t'}}{2m} \operatorname{Re}[\langle H_T \rangle^* \langle \tilde{E} \rangle] \\ &\frac{d\sigma_{TT}}{dt} &= \frac{4\pi\alpha}{k'} \frac{\mu_\pi^2}{Q^8} \frac{t'}{16m^2} |\langle \bar{E}_T \rangle|^2 \\ &\text{where} \quad \langle F \rangle \equiv \sum_{\lambda} \int_{-1}^{1} dx \mathcal{H}_{\mu'\lambda'\mu\lambda} F \\ &\frac{Hard-scattering \, \text{kernel}}{\text{for quark} \, (\lambda, \lambda'), \text{photon } (\mu) \text{ and meson}} \end{split}$$

Nucleon Tomography from GPDs

* At a fixed Q^2 , x_B , slope of GPD with *t* is related, via a Fourier Transform, to the transverse spatial spread.





Formally, the radial separation, **b**, between the struck parton and the centre of momentum of the remaining spectators.

* Experimentally, fit the *t*-dependence of structure functions or CFFs with an exponential. $eg: \frac{d\sigma_U}{dt} = Ae^{Bt}$

Nucleon Tomography from GPDs

* Flavour separation is possible in DVCS using different targets (proton and neutron), and in DVMP with different mesons.

For example, compare measurements of π^0 and η DVMP:

$$H_{T}^{\pi^{0}} = \left(e_{u}H_{T}^{u} - e_{d}H_{T}^{d}\right)/\sqrt{2}, \qquad H_{T}^{\eta} = \left(e_{u}H_{T}^{u} + e_{d}H_{T}^{d}\right)/\sqrt{6},$$

$$\bar{E}_{T}^{\pi^{0}} = \left(e_{u}\bar{E}_{T}^{u} - e_{d}\bar{E}_{T}^{d}\right)/\sqrt{2}, \qquad \bar{E}_{T}^{\eta} = \left(e_{u}\bar{E}_{T}^{u} + e_{d}\bar{E}_{T}^{d}\right)/\sqrt{6}.$$

Up-quark charge (Goloskokov-Kroll model)

Different GPDs represent different aspects of the parton distributions: EM charge, axial charge, transversity, etc....

* Sensitivity to gluon distributions through gluon GPDs. Particularly cleanly accessible for heavier $q:J/\Psi$

Measuring DVCS/DVMP

* Need an exclusive reconstruction of the reaction, eg. DVCS:



***** HERMES @ DESY: electron / positron scattering on fixed gas target

* COMPASS @ CERN: muon scattering on fixed targets

*** JLab (6 and 11 GeV):** electron (positron?) scattering on fixed targets

* EIC: electron / positron - proton / ion collisions



Jefferson Lab today

CEBAF: Continuous Electron Beam Accelerator Facility.

- * Energy up to 11 GeV (Halls A, B, C), 12 GeV Hall D
- ***** Energy spread $\delta E/E_e \sim 10^{-4}$
- Electron polarisation up to >80%, measured to 3%
- Beam size at target < 0.4 mm</p>





Jefferson Lab: 6 GeV era

CEBAF: Continuous Electron Beam Accelerator Facility.

- **★** Energy up to ∼6 GeV
- * Energy resolution $\delta E/E_e \sim 10^{-5}$

***** Longitudinal electron polarisation up to ~85%



Hall A:



* High resolution($\delta p/p = 10^{-4}$) spectrometers, very high luminosity.

Hall B: CLAS



 Very large acceptance, detector array for multiparticle final states.

Hall C:



* Two movable spectrometer arms, well-defined acceptance, high luminosity

CLAS in Hall B: 6 GeV era

- Drift chambers
 Toroidal magnetic field
 Cerenkov Counters
 Scintillator Time of Flight
- Electromagnetic Calorimeters

+ a forward-angle Inner Calorimeter:





Charged particle ID in CLAS

- * Charge: direction of track curvature through drift chambers in toroidal magnetic field
- *** Momentum**: radius of curvature
- * Time of flight: from beam bunch timing and thin scintillator paddles beyond the drift chambers - combine with track length to give β

$$m^2 = \frac{p^2(1-\boldsymbol{\beta}^2)}{\boldsymbol{\beta}^2}$$



* Works well to ID heavy species. Need more tricks for light ones!

Electrons and π^{\perp} in CLAS

* Electrons leave a signal in Cerenkov Counters: pions will not.

* Energy deposit in the Electromagnetic Calorimeter (EC).



Neutrals: photons, neutrons, π^0

* Energy deposit in the calorimeters + lack of charged track.

* Photons in the EC and IC (very forward angles), neutrons only in EC.

* Can reconstruct π^0 through invariant mass.



Targets for CLAS

***** Unpolarised protons: Liquid H₂

* Longitudinally polarised protons: Frozen ammonia beads (NH₃)

- Unpolarised neutrons: Liquid D₂
 Longitudinally polarised neutrons: Frozen deuterated ammonia beads (ND₃)
- Dynamic Nuclear Polarisation (DNP): polarise butanol or ammonia in a high magnetic field (5T) at low temp (1K), use microwaves to transfer electron polarisation to protons/deuterons.



Eg1-dvcs target

* Transverse target polarisation possible, but very challenging...

In the CLAS era: FROST, HD-ice (but only for photon beams)

Reconstructing the DVCS reaction

* A series of experiment-dependent "exclusivity cuts" to ID reaction. Example from eg1-dvcs (CLAS):



Lines: before exclusivity cuts (dashed: *NH*₃, solid: *C*) Filled: after (grey: signal, black: background), arrows indicate cut. S. Pisano *et al* (CLAS), **PRD 91** (2015) 052014

DVCS asymmetries *a* **CLAS**

The "eg1-dvcs" experiment.

- ***** Feb. Sept. 2009
- * 5.87 and 5.95 GeV polarised electron beam
- Longitudinally polarised (via DNP) ¹⁴NH₃ target, 1.45 cm long, 1.5cm diam.
- CLAS + Inner Calorimeter detectors
- ***** Exclusive reconstruction:

 $ep \rightarrow e'p'\gamma$



Eg1-dvcs target

Extracting asymmetries



The DVCS/BH amplitude

$$\mathcal{T}^2 = |\mathcal{T}_{\rm BH}|^2 + |\mathcal{T}_{\rm DVCS}|^2 + \mathcal{I} \longleftarrow \frac{\text{Interference term}}{\text{for DVCS/BH}}$$
$$|\mathcal{T}_{\rm BH}|^2 = \frac{e^6}{x_B^2 y^2 (1+\epsilon^2)^2 t \mathcal{P}_1(\phi) \mathcal{P}_2(\phi)} [c_0^{\rm BH} + \sum_{n=1}^2 c_n^{\rm BH} \cos n\phi + s_1^{\rm BH} \sin \phi]$$

$$|\mathcal{T}_{\rm DVCS}|^2 = \frac{e^6}{y^2 \mathcal{Q}^2} \{ c_0^{\rm DVCS} + \sum_{n=1}^2 [c_n^{\rm DVCS} \cos n\phi \, + \, s_n^{\rm DVCS} \sin n\phi] \}$$



Intermediate lepton propagators

From asymmetries to CFFs

At leading twist, beam-spin asymmetry (BSA) can be expressed as:

$$A_{\rm LU}(\phi) \sim \frac{s_{1,\rm unp}^{\mathcal{I}} \sin \phi}{c_{0,\rm unp}^{\rm BH} + (c_{1,\rm unp}^{\rm BH} + c_{1,\rm unp}^{\mathcal{I}} + \dots) \cos \phi \dots} \quad higher-twist \ terms\dots$$

The leading coefficient is related to the imaginary part of the Compton Form Factors:

$$s_{1,\text{unp}}^{\mathcal{I}} \propto \Im[F_1\mathcal{H} + \xi(F_1 + F_2)\widetilde{\mathcal{H}} - \frac{t}{4M^2}F_2\mathcal{E}]$$

At CLAS kinematics, this dominates F_1, F_2 : Dirac,
Pauli form factors

Likewise, for the target-spin asymmetry (TSA):

$$\begin{aligned} A_{\rm UL}(\phi) &\sim \frac{s_{1,\rm LP}^{\mathcal{I}} \sin \phi}{c_{0,\rm unp}^{\rm BH} + (c_{1,\rm unp}^{\rm BH} + c_{1,\rm unp}^{\mathcal{I}} + ...) \cos \phi + ...} \\ s_{1,\rm LP} &\propto \Im [F_1 \widehat{\mathcal{H}} + \xi (F_1 + F_2) \widehat{\mathcal{H}} + \frac{x_B}{2} \mathcal{E}) - \xi (\frac{x_B}{2} F_1 + \frac{t}{4M^2} F_2) \widetilde{\mathcal{E}}] \\ At CLAS kinematics, these CFFs dominate \end{aligned}$$

* Obtain coefficients from fitting the phidependence of the asymmetry:

$$A_i = \frac{\alpha_i \sin \phi}{1 + \beta_i \cos \phi}$$



Follows first CLAS measurement: S. Chen *et al* (CLAS), *PRL* 97 (2006) 072002

A_{UL} from fit to asymmetry:

$$A_i = \frac{\alpha_i \sin \phi}{1 + \beta_i \cos \phi}$$

A_{UL} characterised by imaginary parts of CFFs via: $x_B = \xi t$

$$F_1 \tilde{\boldsymbol{H}} + \xi G_M (\boldsymbol{H} + \frac{x_B}{2} \boldsymbol{E}) - \frac{\zeta \iota}{4M^2} F_2 \tilde{\boldsymbol{E}} + \dots$$

High statistics, large kinematic coverage, strong constraints on fits, simultaneous fit with BSA and DSA from the same dataset.

E. Seder *et al* (CLAS), *PRL* 114 (2015) 032001S. Pisano *et al* (CLAS), *PRD* 91 (2015) 052014



Beam- and target-spin asymmetries



Double-spin asymmetry

At leading twist, double-spin asymmetry (DSA) can be expressed as:

$$A_{\rm LL}(\phi) \sim \frac{c_{0,\rm LP}^{\rm BH} + c_{0,\rm LP}^{\mathcal{I}} + (c_{1,\rm LP}^{\rm BH} + c_{1,\rm LP}^{\mathcal{I}})\cos\phi}{c_{0,\rm unp}^{\rm BH} + (c_{1,\rm unp}^{\rm BH} + c_{1,\rm unp}^{\mathcal{I}} + ...)\cos\phi...}$$

$$c_{0,\mathrm{LP}}^{\mathcal{I}}, c_{1,\mathrm{LP}}^{\mathcal{I}} \propto \Re \left[F_1 \widehat{\mathcal{H}} + \xi (F_1 + F_2) (\mathcal{H} + \frac{x_B}{2} \mathcal{E}) - \xi (\frac{x_B}{2} F_1 + \frac{t}{4M^2} F_2) \widetilde{\mathcal{E}}\right]$$

At CLAS kinematics, leading-twist dominance of these CFFs

***** Fit function for the phi-dependence of the asymmetry:

 $\frac{\kappa_{\rm LL} + \lambda_{\rm LL}\cos\phi}{1 + \beta\cos\phi}$

Shares denominator with BSA and TSA! If measurements at same kinematics, can do a simultaneous fit.

Double-spin Asymmetry (A_{LL})





A_{LL} from fit to asymmetry: $\frac{\kappa_{LL} + \lambda_{LL} \cos \phi}{1 + \beta \cos \phi}$

A_{LL} characterised by real parts of CFFs via:

 $F_1 \tilde{\boldsymbol{H}} + \xi G_M (\boldsymbol{H} + \frac{x_B}{2} \boldsymbol{E}) + \dots$

- * Fit parameters extracted from a simultaneous fit to BSA, TSA and DSA.
- Constant term dominates and is almost entirely BH.

E. Seder *et al* (CLAS), *PRL* 114 (2015) 032001
S. Pisano *et al* (CLAS), *PRD* 91 (2015) 052014

CFF extraction from three spin asymmetries at common kinematics.



What can we learn from the asymmetries?

Answers hinge on a global analysis of all available data.

*Information on relative distributions of quark momenta (PDFs) and quark helicity, $\Delta q(x)$.

 $H(x,0,0)=q(x) \quad \tilde{H}(x,0,0)=\Delta q(x)$

Indications that axial charge is more concentrated than electromagnetic charge.

$$\int_{-1}^{+1} H dx = F_1$$
$$\int_{-1}^{+1} \tilde{H} dx = G_A$$

E. Seder *et al* (CLAS), *PRL* **114** (2015) 032001 S. Pisano *et al* (CLAS), *PRD* **91** (2015) 052014

DVCS cross-sections (a) **CLAS**

***** Three months in 2005

 \$ 5.79 GeV polarised electron beam (79.4% polarisation)

***** 2.5cm long liquid H₂ target

- * CLAS + IC detectors
- * Luminosity = $2 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$
- ***** Exclusive reconstruction:



H.-S. Jo et al (CLAS), PRL 115 (2015) 212003

DVCS cross-sections *@* **CLAS**



Towards nucleon tomography



- * CFFs extracted in a VGG fit.
- * Imaginary part of CFF: $F_{Im}(\xi, t) = F(\xi, \xi, t) \mp F(-\xi, \xi, t)$



Towards nucleon tomography

Quasi model-independent extraction of CFFs based on a local fit:

- * Set 8 CFFs as free parameters to fit, at each (x_B, t) point, the available observables.
- Limits imposed within +/- 5 times the VGG model predictions (Vanderhaeghen-Guichon-Guidal).
- * Relies on knowledge of BH and leading-twist DVCS amplitude parametrisation.

The best constraints in fits to CLAS data were obtained on H_{IM} .



Towards nucleon tomography

Further, can relate the impact parameter to helicity-averaged transverse charge distribution: a 19 A

$$\rho^{q}(x, \mathbf{b}_{\perp}) = \int \frac{d^{2} \boldsymbol{\Delta}_{\perp}}{(2\pi)^{2}} e^{-i\mathbf{b}_{\perp} \cdot \boldsymbol{\Delta}_{\perp}} H^{q}_{-}(x, 0, -\boldsymbol{\Delta}_{\perp}^{2})$$

$$Transverse four-network transfer to nucleo$$

$$H^{q}_{-}(x, 0, t) \equiv H^{q}(x, 0, t) + H^{q}(-x, 0, t)$$

nomentum n

Assuming leading-twist and exponential dependence of GPD on *t*, using models to extrapolate to the zero skewness point $\xi = 0$ and assuming similar behaviour for u and dquarks there:

$$\langle b_{\perp}^2 \rangle^q(x) = -4 \frac{\partial}{\partial \Delta_{\perp}^2} \ln H_-^q(x, 0, -\Delta_{\perp}^2) \bigg|_{\mathbf{A}}$$

0.8 *Charge radius* 0.7 at different 0.6 momentum fractions *x* (fm²) 0.5 (x) (x) 0.2 0.1 $\Delta_{\perp}=0$ 0.1 X



Not enough information yet for a conclusive picture, but tentative hints of 3D distributions are emerging!

R. Dupré *et al.*, arXiv:1704.07330 [hep-ph]

DVCS cross-sections in Hall A



*** E00-110 experiment** (2004):
 5.75 GeV polarised electron beam



*** E07-004 experiment** (2010):

Energy scan for fixed x_B , Q^2 :

Q^2 (GeV ²)	Х _В	E ^{beam} (GeV)	−t (GeV²)
1.50	0.36	3.355 5.55	0.18, 0.24, 0.30
1.75	0.36	4.455 5.55	0.18, 0.24, 0.30, 0.36
2.00	0.36	4.455 5.55	0.18, 0.24, 0.30, 0.36

M. Defurne et al, PRC 92 (2015) 055202.

Can we assume leading twist?

* Twist: powers of $\frac{1}{\sqrt{Q^2}}$ in the DVCS amplitude. Leading-twist (LT) is twist-2.

- ***** Order: introduces powers of α_s
- LO requires Q² >> M² (M: target mass)
 Bold assumption for JLab 6 GeV kinematics!
- CFFs can be classified according to real and virtual photon helicity:
- \mathcal{F}_{++-} helicity of virtual incoming photon
 - \odot Helicity-conserved CFFs \mathcal{F}_{++}
 - Helicity-flip (transverse) \mathcal{F}_{-+}
 - \odot Longitudinal to transverse flip \mathcal{F}_{0+}



- ***** CFFs contributing to the scattering amplitude:
 - \odot LT in LO: only \mathcal{F}_{++}
 - LT in NLO: both \mathcal{F}_{++} and \mathcal{F}_{-+} • Twist-3: \mathcal{F}_{0+}

Can we assume leading twist?

- * At finite Q^2 and non-zero *t* there's ambiguity in defining the light-cone axis for the GPDs:
 - Traditional GPD phenomenology uses the Belitsky convention, in plane of q and P:
 A. Belitsky *et al*, *Nucl. Phys. B878* (2014), 214
 - New, Braun definition using q and q': more natural.
 V. Braun *et al*, *Phys. Rev. D89* (2014), 074022

Reformulating CFFs in the Braun frame:

$$\mathcal{F}_{++} = \mathbb{F}_{++} + \frac{\chi}{2} \left[\mathbb{F}_{++} + \mathbb{F}_{-+} \right] - \chi_0 \mathbb{F}_{0+}$$
$$\mathcal{F}_{-+} = \mathbb{F}_{-+} + \frac{\chi}{2} \left[\mathbb{F}_{++} + \mathbb{F}_{-+} \right] - \chi_0 \mathbb{F}_{0+}$$
$$\mathcal{F}_{0+} = -(1+\chi) \mathbb{F}_{0+} + \chi_0 \left[\mathbb{F}_{++} + \mathbb{F}_{-+} \right]$$
$$\overset{\bullet}{\mathsf{Braun CFFs}}$$
Belitsky CFFs



Assuming LO and LT in the Braun frame leaves higher-twist, higher-order contributions in the Belitsky frame, scaled by kinematic factors χ and χ_0 .

Non-negligible at the Q^2 and x_B of the Hall A crosssection measurements in JLab @ 6 GeV era!

M. Defurne et al, Nature Communications 8 (2017) 1408.

Hints of higher twist or higher orders



E07-007: Hall A experiment to measure helicity-dependent and -independent crosssections at two beam energies and constant x_B and t.



Simultaneous fit to cross-sections at both energies and three values of Q² using only leading twist and leading order (LT/LO) do not describe the cross-sections fully: higher twist/order effects?

Using Braun's decomposition, \mathbb{H}_{-+} and \mathbb{H}_{0+} can't be neglected.

Hints of higher twist or higher orders



* Including either higher order or higher twist effects (HT) improves the match with data:



Higher-order and / or higher-twist terms are important! A glimpse of gluons.

Wider range of beam energy needed to identify the dominant effect — JLab at 11 GeV.

M. Defurne et al, Nature Communications 8 (2017) 1408.

Rosenbluth separation of DVCS² and BH-DVCS terms



* Generalised Rosenbluth separation of the DVCS² and the BH-DVCS interference terms in the cross-section is possible but NLO and/or higher-twist required.



- Significant differences
 between pure DVCS and
 interference contributions.
- Helicity-dependent crosssection has a sizeable DVCS² contribution in the higher-twist scenario.
- Separation of HT and NLO effects requires scans across wider ranges of Q² and beam energy: JLab12!

M. Defurne et al, Nature Communications 8 (2017) 1408.

JLab @ 12 GeV



High resolution($\delta p/p = 10^{-4}$) spectrometers, very high luminosity, large installation experiments.



9 GeV tagged polarised photons, full acceptance



Hall B: CLAS12



Hall C



Two movable high momentum spectrometers, welldefined acceptance, very high luminosity.

Very large acceptance, high luminosity.

CLAS12 Design luminosity

 $L \sim 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$

High luminosity & large acceptance: Concurrent measurement of exclusive, semi-inclusive, and inclusive processes

Acceptance for photons and electrons: • $2.5^{\circ} < \theta < 125^{\circ}$

Acceptance for all charged particles: • $5^{\circ} < \theta < 125^{\circ}$

Acceptance for neutrons: • $5^{\circ} < \theta < 120^{\circ}$



CLAS12 assembled


DVCS in CLAS12: detection

*** Electrons** detected and identified in the Forward Detector using similar techniques to CLAS: signal in Cerenkov detector, energy deposit in calorimeters and tracking through drift chambers in a toroidal magnetic field.

*** Protons**: tracking in a magnetic field, time of flight from scintillator paddles.



* **Neutrons** in the Central Detector: on the basis of time of flight and energy deposit in the Central Neutron Detector scintillator barrel.

DVCS in CLAS12: detection

*** Photons** in the Forward Detector: energy deposit in the Calorimeters — EC and the Forward Tagger.



DVCS in Hall A @ 11 GeV



Detect photon in PbF₂ calorimeter: < 3% energy resolution



Reconstruct recoiling proton through missing mass.

DVCS in Hall C @ 11 GeV

Detect electron with (Super) High Momentum Spectrometer, (S)HMS.

Detect photon in PbWO₄ calorimeter.

Sweeping magnet to reduce backgrounds in calorimeter.

Reconstruct recoiling proton through missing mass.

