

Spatial imaging of the nucleon

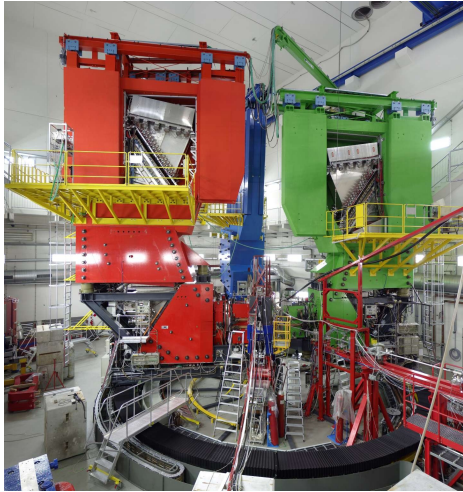
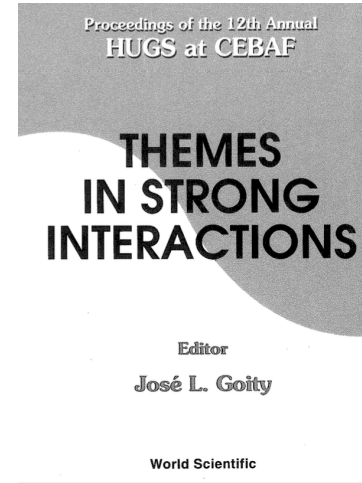
J. Roche (Ohio University)

- Hard exclusive reactions allow the study of the 2+1 D structure of nucleon through the measure of Generalized Parton Distributions that goes beyond what can be achieved with elastic scattering.
- Dedicated experiments are conducted world-wide.
- The growing set of existing results is helping refine our approach to extracting the GPDs from the data and within limits some preliminary results.
- DVCS experiments are an essential part of the comprehensive GPD program with the 12 GeV CEBAF beam and the EIC.

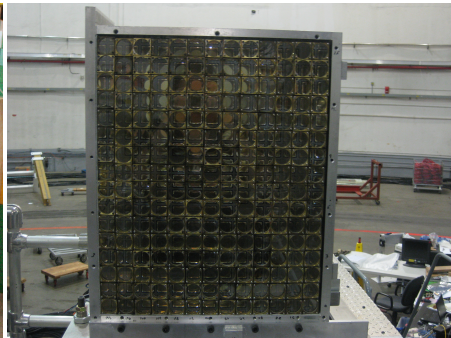
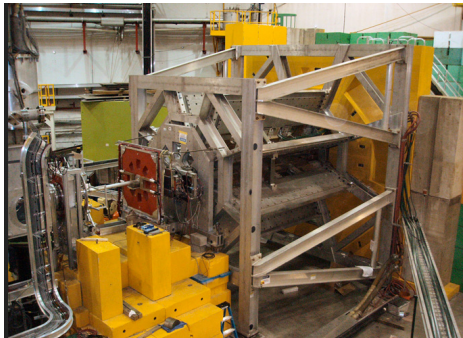


Introduction

- '97 HUGS participant
- '98 PhD from France
- Postdoc at JLab ('99-06)
- Associate professor at Ohio U (NSF funded)



Polarizabilities of the nucleon: VCS@MAMI- Germany
Strange form factor the nucleon: GO@JLab
Physics beyond the Standard Model: QWEAK@Jlab
GPDs: DVCS-Hall A @Jlab

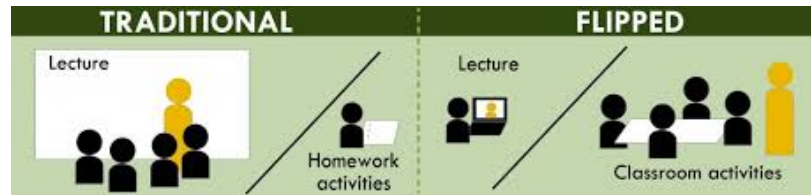


Absolute cross-sections measurements
Parity violation in Electron Scattering

Six hours together

Three 2-hours sessions:

- 30 minutes introduction by me
- Two rounds of questions I will ask you to think about
 - 30 minutes of your researching questions
 - 15 minutes of you presenting your finding to the class



The outline and some slides are inspired by a recent paper by N. d'Hose (CEA Saclay) [10.1051/epjconf/20158501004](https://doi.org/10.1051/epjconf/20158501004)

Spatial imaging of the nucleon

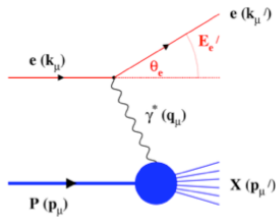
J. Roche (Ohio University)

- Hard exclusive reactions allow the study of the 2+1 D structure of nucleon through the measure of Generalized Parton Distributions that goes beyond what can be achieved with elastic scattering.
- Dedicated experiments are conducted world-wide.
- The growing set of existing results is helping refine our approach to extracting the GPDs from the data and within limits some preliminary results.
- DVCS experiments are an essential part of the comprehensive GPD program with the 12 GeV CEBAF beam and the EIC.



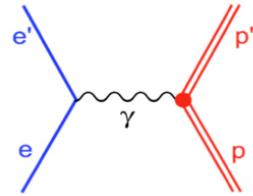
3D picture of the nucleon

DIS Parton Distribution Functions

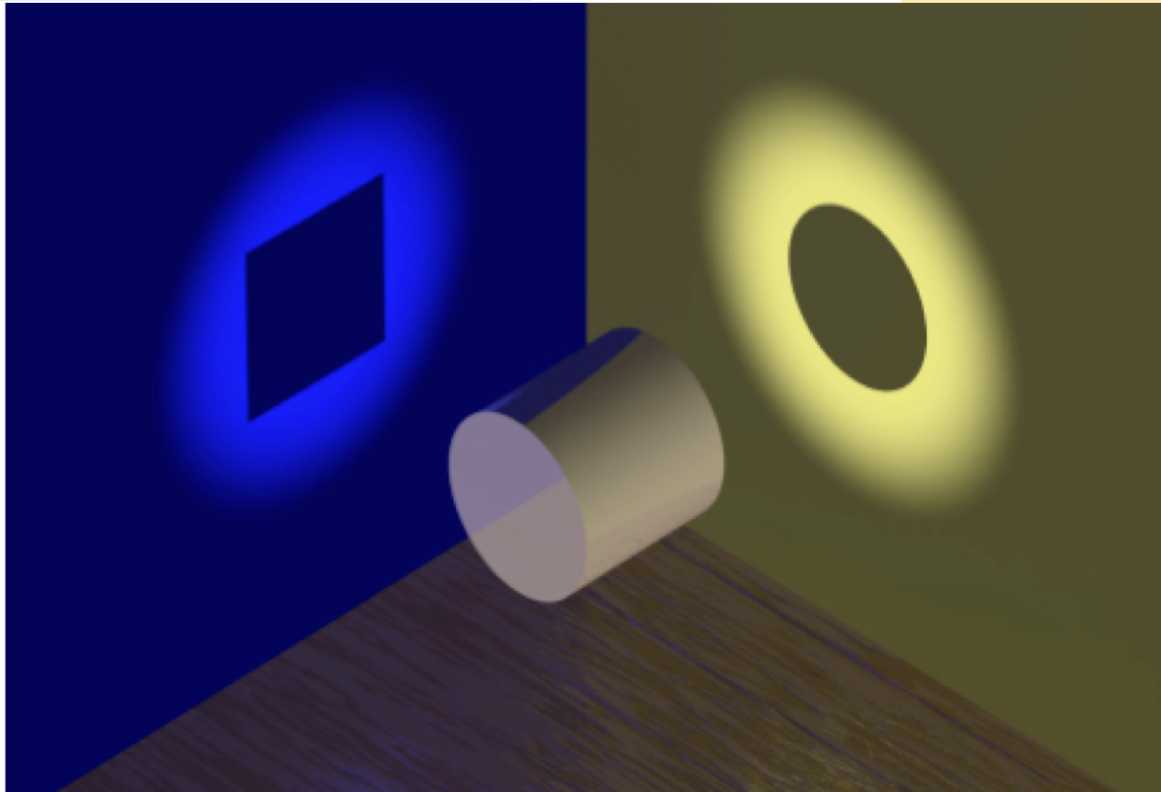


No information on the spatial location of the constituents

Elastic Form Factors



No information about the underlying dynamics of the system



Generalized Parton Distribution Function :

3-D imaging of the nucleon with access to **correlations** between **transverse spatial distribution and longitudinal momentum distributions**.

From PDFs to TMDs and GPDs

PDFs: 1-D structure

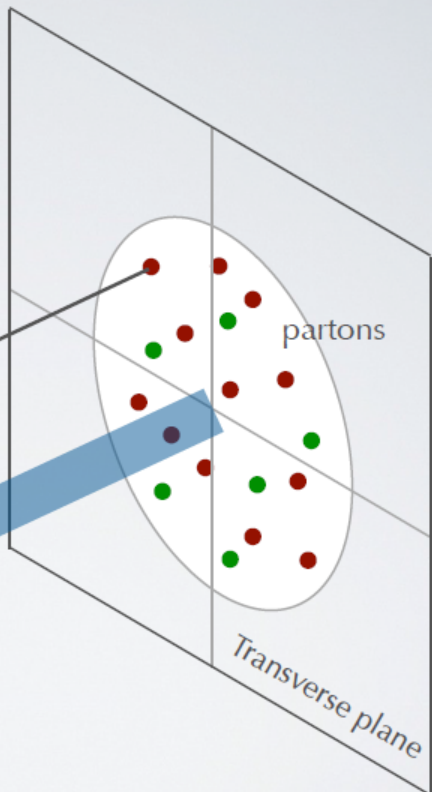
PDF (x)

Longitudinal momentum

$$k^+ = xP^+$$

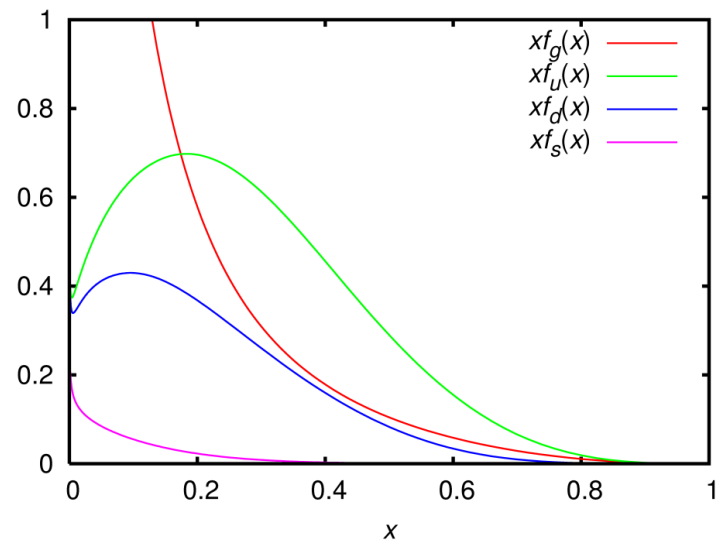


(x_B, Q^2)



A. Bacchetta

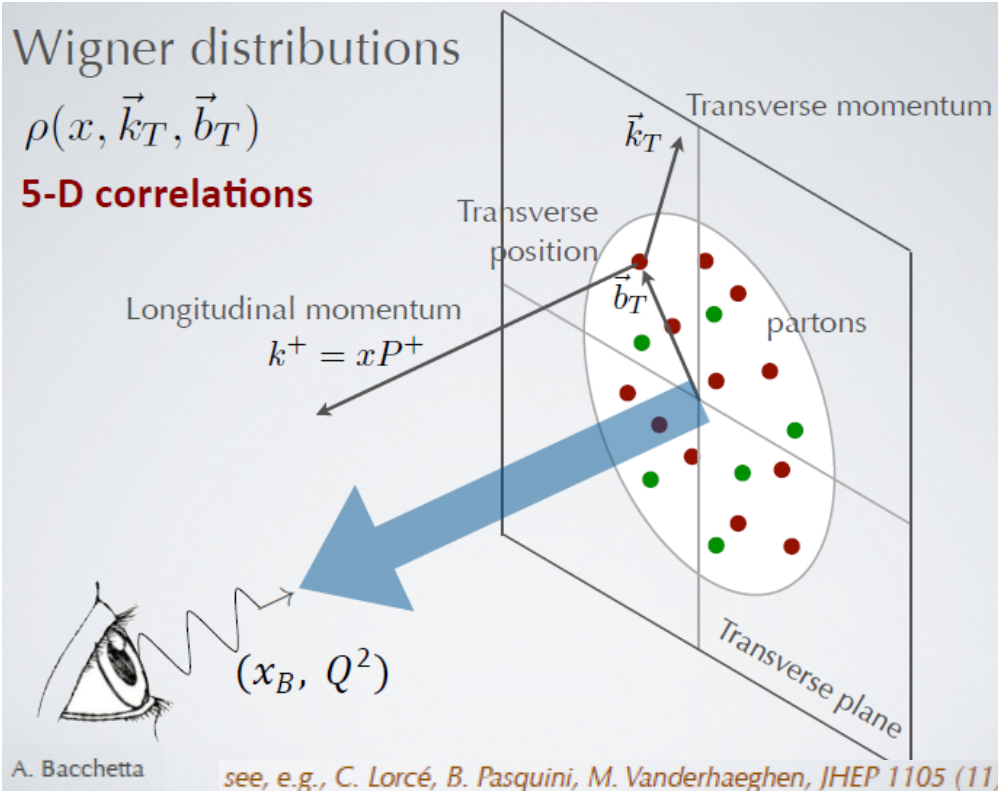
PDFs from CTEQ6



PDF measured in Deep Inelastic Scattering

$$lp \rightarrow l'X$$

From PDFs to TMDs and GPDs



3-dimensional nucleon structure
in momentum and configuration space:

GPD ($\mathbf{x}, \mathbf{b}_\perp$) :

Generalised Parton Distribution
(position in the transverse plane)

TMD ($\mathbf{x}, \mathbf{k}_\perp$) :

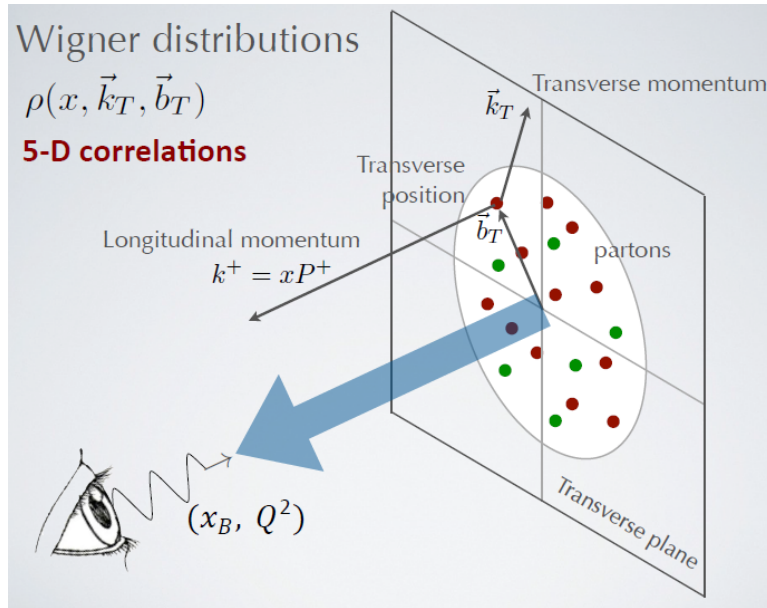
Transverse Momentum Distribution
(momentum in the transv. Plane)

TMD accessible in **SIDIS** and **DY**

GPD in **Exclusive reactions**
DVCS and **HEMP**



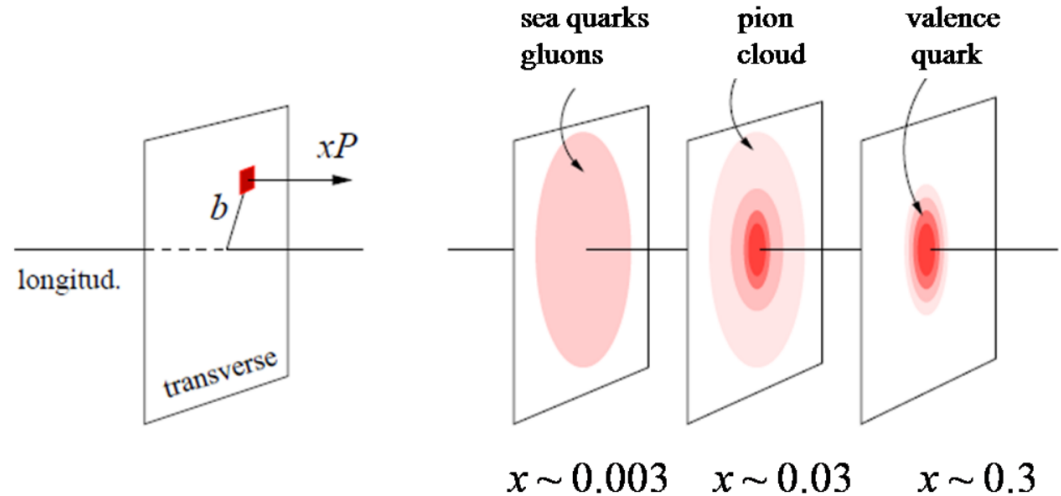
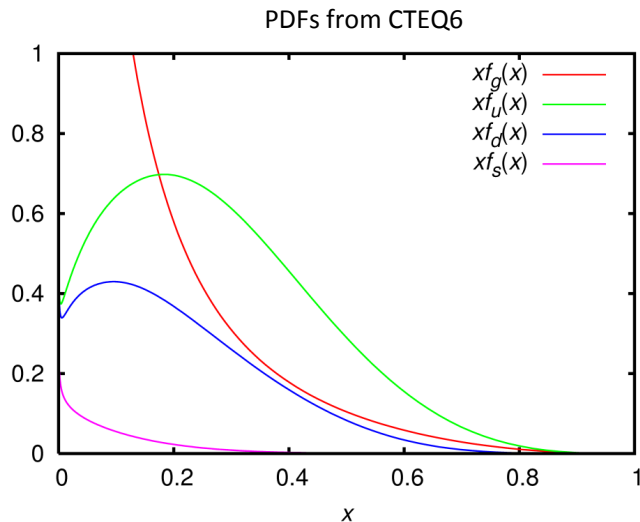
From PDFs to TMDs and GPDs



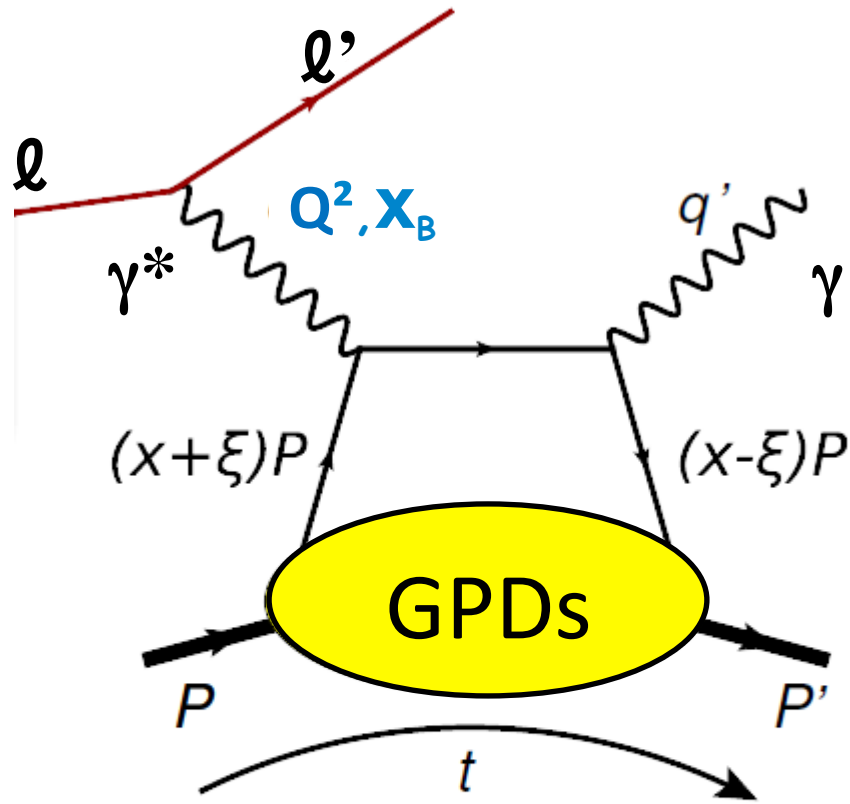
3-dimensional nucleon structure
 in momentum and configuration space:

GPD (x, \mathbf{b}_\perp) :

Generalised Parton Distribution
 (position in the transverse plane)



Exclusive reactions



DVCS: $l p \rightarrow l' p' \gamma$ (golden channel)

HEMP: $l p \rightarrow l' p' \rho$ or ϕ or $J/\psi, \dots$

γ or $\rho, \phi, J/\psi, \dots$

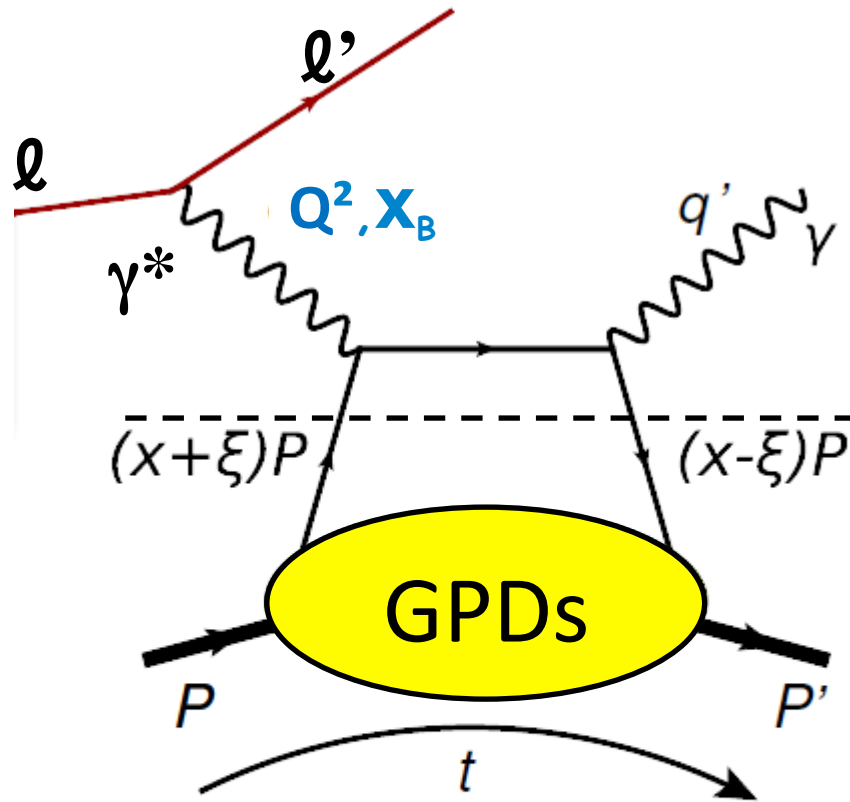
Definition of variables:

x : average long. momentum - NOT ACCESSIBLE

ξ : long. mom. difference $\approx x_B / (2 - x_B)$

t : four-momentum transfer
related to b_{\perp} via Fourier transform

GPDs and factorization



D. Mueller *et al*, Fortsch. Phys. 42 (1994)

X.D. Ji, PRL 78 (1997), PRD 55 (1997)

A. V. Radyushkin, PLB 385 (1996), PRD 56 (1997)

Hard process

Soft process

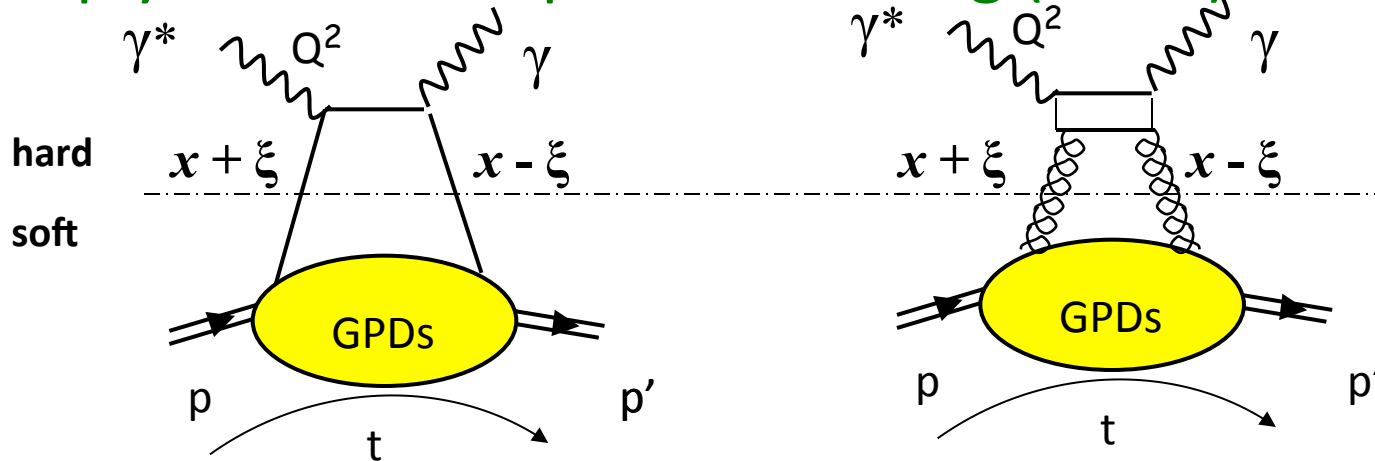
Non perturbative QCD
described by GPDs

The minimal Q^2 at which the factorization holds **must be tested** and established by **experiments**

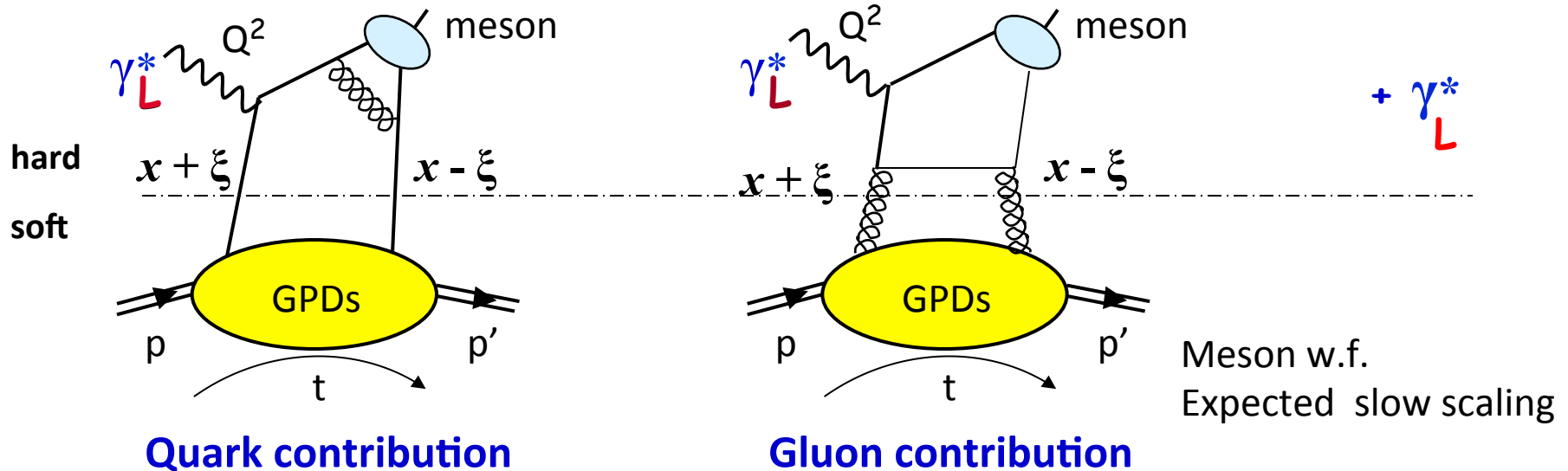
Exclusive reactions

Deeply Virtual Compton Scattering (DVCS):

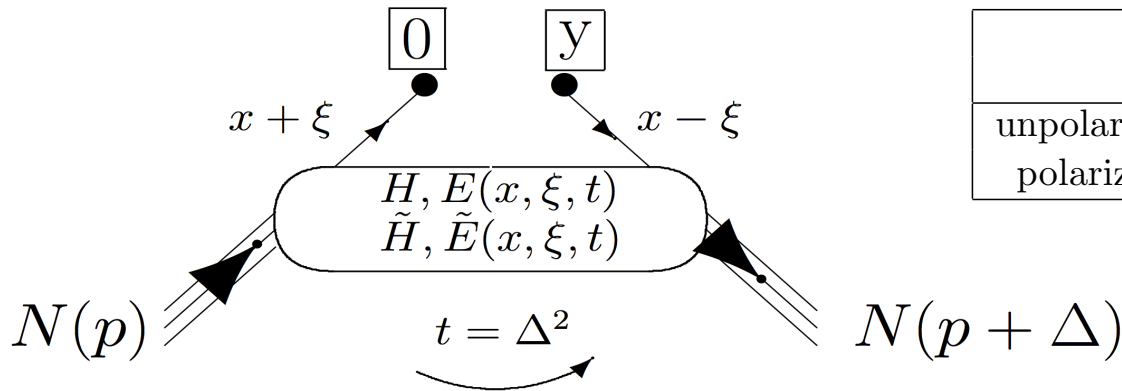
Factorisation:
Collins *et al.*



Hard Exclusive Meson Production (HEMP):



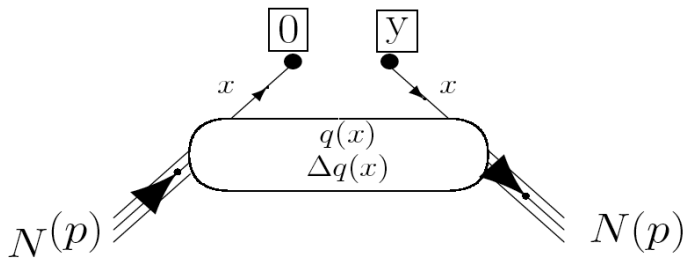
Generalized Parton Distributions



	Nucleon Helicity	
	conserving	non-conserving
unpolarized GPD	H	E
polarized GPD	H-tilde	E-tilde

$$\lim_{t \rightarrow 0} (GPD) \rightarrow PDF$$

DIS



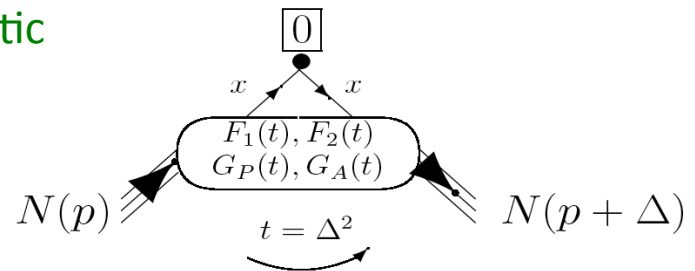
$$H^q(x, 0, 0) = q(x), -\bar{q}(-x)$$

$$\tilde{H}^q(x, 0, 0) = \Delta q(x), \Delta \bar{q}(-x)$$

No relation for E(x, 0, 0)

GPD first moments \rightarrow Form Factors

Elastic



$$\int_{-1}^{+1} dx H^q(x, \xi, t) = F_1^q(t) \quad \int_{-1}^{+1} dx \tilde{H}^q(x, \xi, t) = g_A^q(t)$$

$$\int_{-1}^{+1} dx E^q(x, \xi, t) = F_2^q(t) \quad \int_{-1}^{+1} dx \tilde{E}^q(x, \xi, t) = h_A^q(t)$$

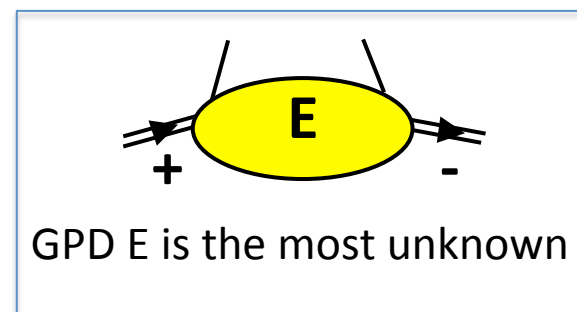
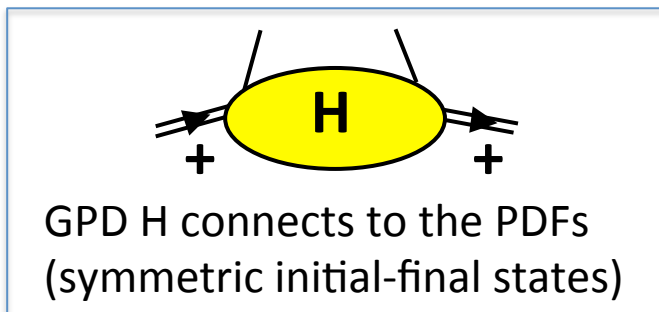
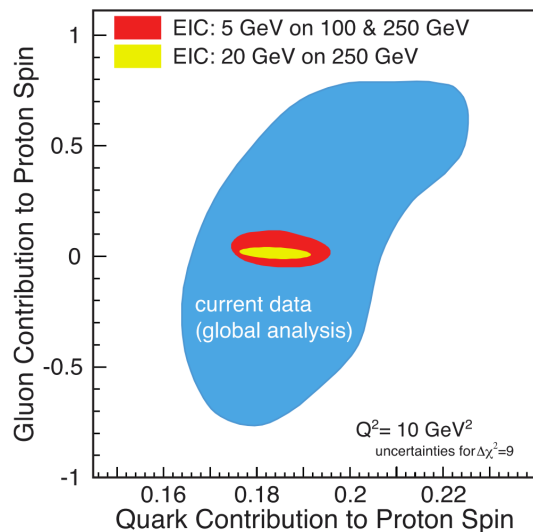
The “Holy grail” of GPDs (and TMDs) physics

$$\frac{1}{2} = \text{Spin of all Quarks} + \text{Spin of Gluons} + \text{Angular Momentum of all Quarks} + \text{Angular Momentum of Gluons}$$

Contribution of the **angular momentum of quarks** to proton spin:

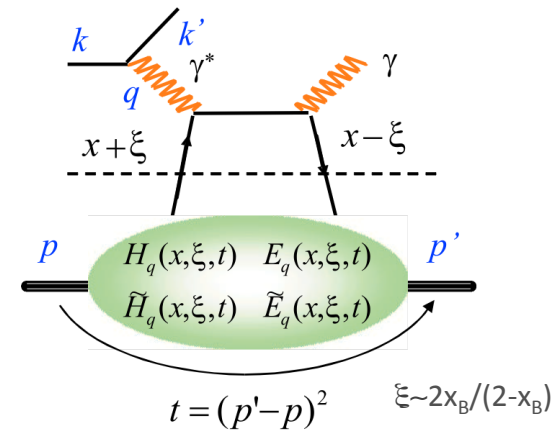
$$\frac{1}{2} = \underbrace{\frac{1}{2} \Delta\Sigma}_{J_q} + L_q + J_g \quad \Rightarrow \quad J_q = \frac{1}{2} \int_{-1}^1 dx x [H^q(x, \xi, 0) + E^q(x, \xi, 0)]$$

Ji's sum rule



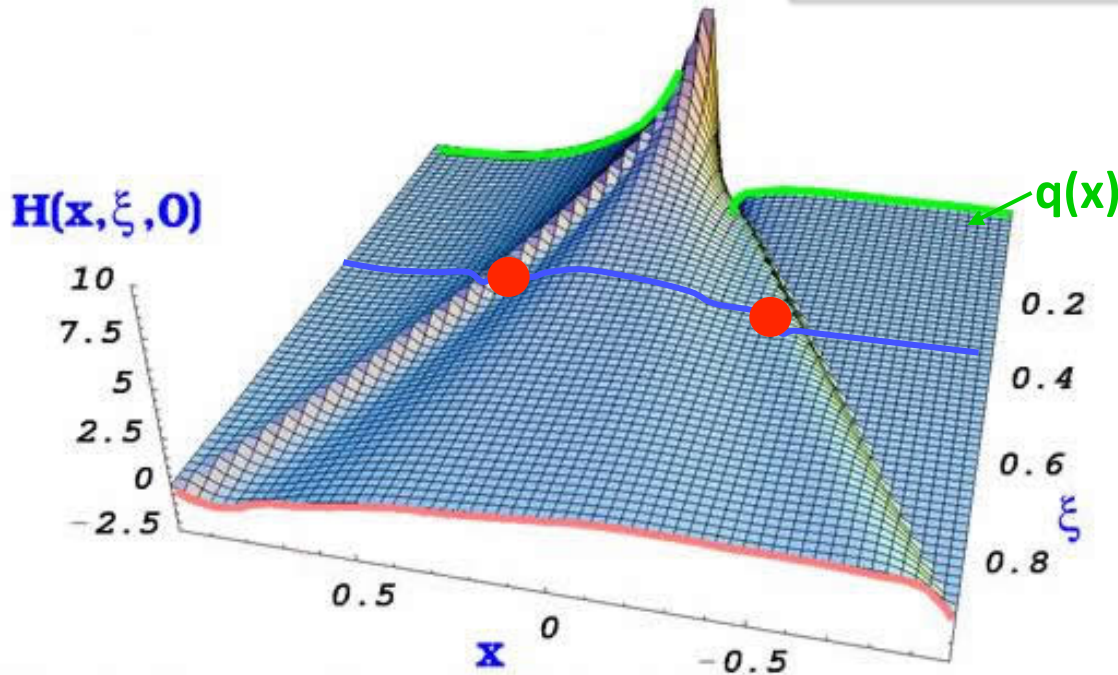
Experimentally, producing enough data to support the integration over the whole x range is a challenge.

GPDs and Compton Form Factors



CFF \downarrow GPD \downarrow

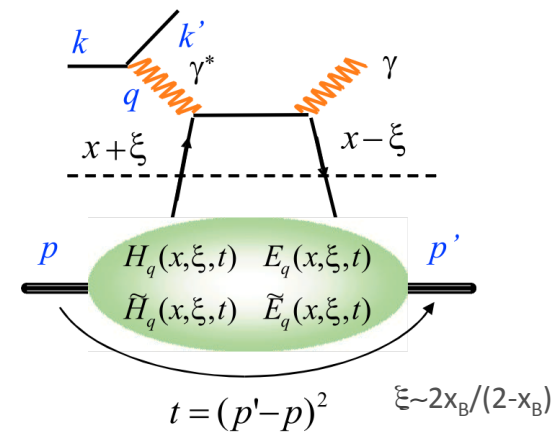
$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i\pi H(x = \xi, \xi, t)$$



Im part measured in
Beam Spin
 or **Target Spin**
 cross section difference

Real part measured in
Beam Charge
 cross section difference or
Total cross section

GPDs and Compton Form Factors



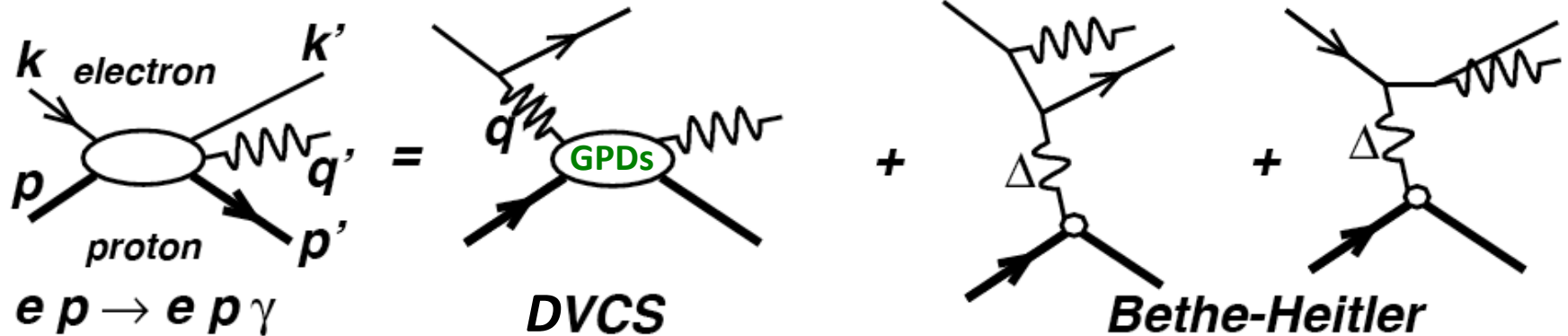
$$\mathcal{H} = \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi + i\epsilon} = \mathcal{P} \int_{-1}^{+1} dx \frac{H(x, \xi, t)}{x - \xi} - i \pi H(x = \xi, \xi, t)$$

$$\text{Re } \mathcal{H}(\xi, t) = \mathcal{P} \int dx \frac{\text{Im } \mathcal{H}(x, t)}{x - \xi} + \mathcal{D}(t)$$

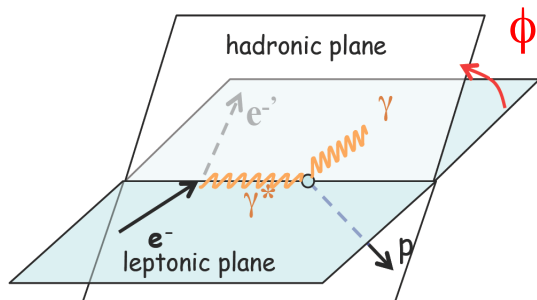
\mathcal{D} term related to the Energy-Momentum Tensor : Polyakov, PLB 555 (2003) 57-62

The Imaginary part and the Real part are not trivially related:
both need to be measured.

Measuring DVCS to access GPDs information

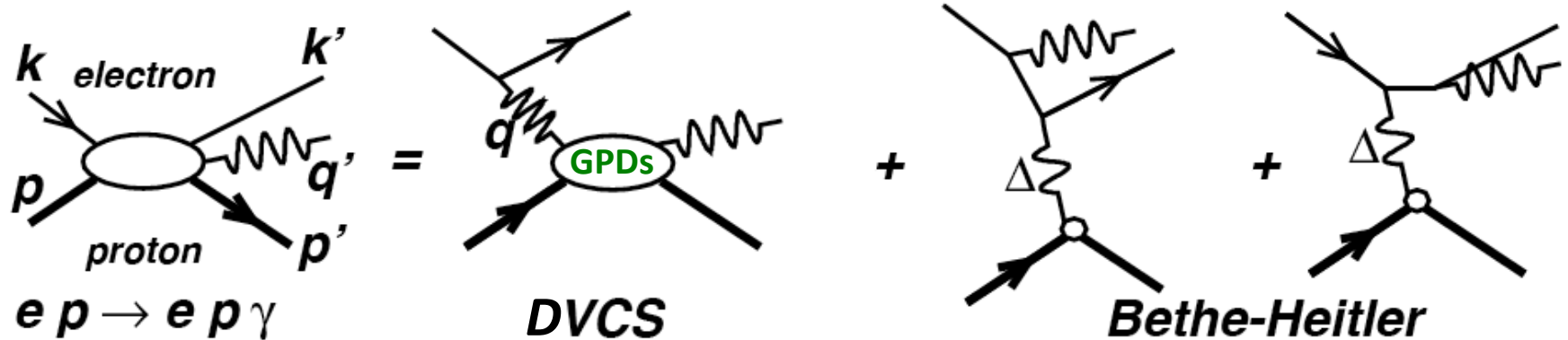


$$\frac{d^4\sigma(lp \rightarrow lp\gamma)}{dx_B dQ^2 d|t| d\phi} = d\sigma^{\text{BH}} + d\sigma_{\text{unpol}}^{\text{DVCS}} + \mathbf{P}_1 d\sigma_{\text{pol}}^{\text{DVCS}} + e_1 (\text{Re}(\mathbf{I}) + \mathbf{P}_1 \text{Im}(\mathbf{I}))$$



\mathbf{P}_1 : polarization target or beam
 e_1 : charge of the lepton beam

Measuring DVCS to access GPDs information



When only considering the handbag diagram (at leading twist)

$$d^5 \vec{\sigma} - d^5 \overleftarrow{\sigma} = \Im (T^{BH} \cdot T^{DVCS})$$

$$d^5 \vec{\sigma} + d^5 \overleftarrow{\sigma} = |BH|^2 + \Re (T^{BH} \cdot T^{DVCS}) + |DVCS|^2$$

↓
↓
↓

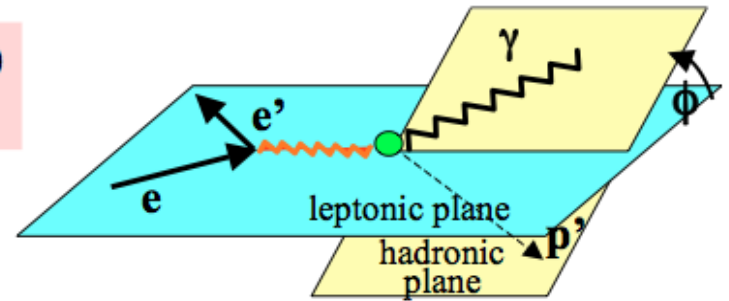
Known to 1%
 Linear combinations of GPDs
Bilinear combinations of GPDs

DVCS sensitivities to GPDs

$$\Delta\sigma = d^5\vec{\sigma} - d^5\overleftarrow{\sigma}$$

$$\xi = x_B/(2-x_B)$$

$$k = -t/4M^2$$



Polarized **beam**, unpolarized **proton** target:

$$\Delta\sigma_{LU} \sim \sin\phi \operatorname{Im} \{ F_1 H + \xi(F_1 + F_2) \tilde{H} + kF_2 E \} d\phi$$

Kinematically suppressed

$$\rightarrow H_p, \tilde{H}_p, E_p$$

Unpolarized beam, **longitudinal proton** target:

$$\Delta\sigma_{UL} \sim \sin\phi \operatorname{Im} \{ F_1 \tilde{H} + \xi(F_1 + F_2)(H + \dots) \} d\phi$$

$$\rightarrow H_p, \tilde{H}_p$$

Unpolarized beam, **transverse proton** target:

$$\Delta\sigma_{UT} \sim \sin\phi \operatorname{Im} \{ k(F_2 H - F_1 E) + \dots \} d\phi$$

$$\rightarrow H_p, E_p$$

Polarized **beam**, unpolarized **neutron** target:

$$\Delta\sigma_{LU} \sim \sin\phi \operatorname{Im} \{ F_1 H + \xi(F_1 + F_2) \tilde{H} - kF_2 E \} d\phi$$

$$\rightarrow H_n, \tilde{H}_n, E_n$$

To “extract the GPDs”, one can:

- Compare data to models of the GPDs (Double-distribution models, dual models, Mellin-Barnes models)
- Fit the CFFs from data:
 - world-wide data fitted at once (8 quantities varying with x_B and t),
 - fit data points versus ϕ at one kinematic point choosing a limited set of GPDs.

Multipole expansion of the amplitude

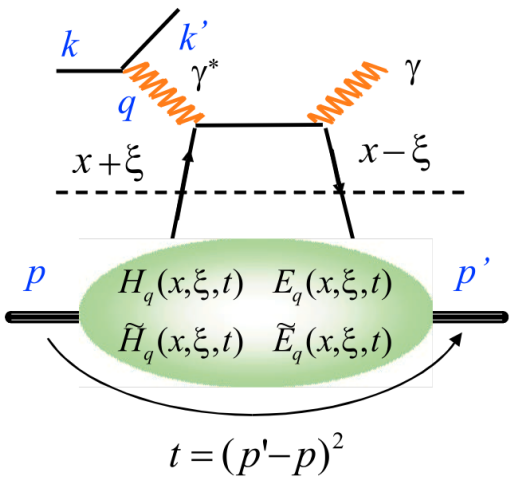
The full DVCS amplitude (ep->epγ) is

$$T_{\text{VCS}}(e^\pm) = \bar{u}(k', \lambda) \gamma_\mu u(k, \lambda) \frac{(\pm e)}{q^2} H^{\mu\nu} \epsilon_\nu^\dagger$$

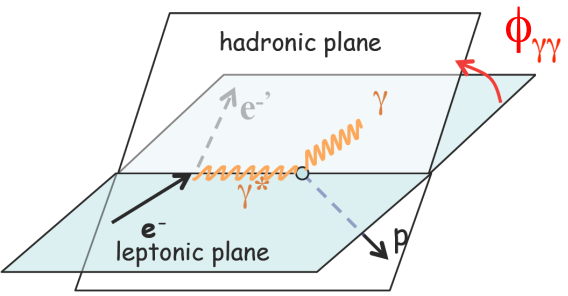
The hadronic tensor is

$$H_{\text{LO, twist 2}}^{\mu\nu} = \frac{1}{2} (-g^{\mu\nu})_\perp \bar{U}(p') \left[(n \cdot \gamma) \mathcal{H}(\xi, t) + \frac{i}{2M} n_\kappa \sigma^{\kappa\lambda} \Delta_\lambda \mathcal{E}(\xi, t) \right] U(p) - (\epsilon^{\mu\nu})_\perp \bar{U}(p') \left[(n \cdot \gamma \gamma_5) \tilde{\mathcal{H}}(\xi, t) + (\gamma_5 n \cdot \Delta) \tilde{\mathcal{E}}(\xi, t) \right] U(p),$$

CFFs



In practice, one exploits the azimuthal modulation of the DVCS (and its interference)



$$|T_{\text{DVCS}}|^2 = \frac{e^6 (s_e - M^2)^2}{x_{Bj}^2 Q^6} \left\{ \sum_{n=0}^2 c_n^{\text{DVCS}} \cos(n\phi_{\gamma\gamma}) + \sum_{n=1}^2 s_n^{\text{DVCS}} \sin(n\phi_{\gamma\gamma}) \right\}$$

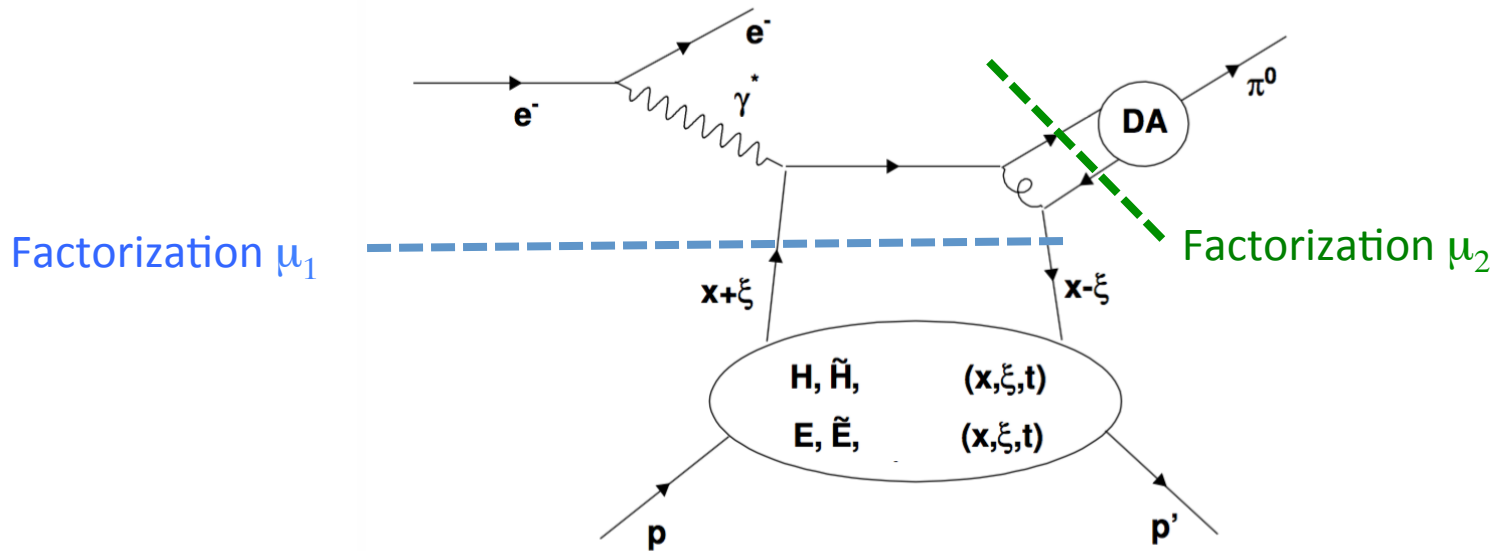
$$c_0^{\text{DVCS}} = f(\text{kine}) \left\{ 4(1 - x_{Bj}) \mathcal{H} \mathcal{H}^* + 4 \left(1 - x_{Bj} + \frac{2Q^2 + t}{Q^2 + x_{Bj}t} \frac{\epsilon^2}{4} \right) \tilde{\mathcal{H}} \tilde{\mathcal{H}}^* + \dots \right\}$$

Harmonic coefficients

CFFs

$$c_{\text{unp}}^I = g(\text{kine}) \left\{ F_1 \mathcal{H} - \frac{t}{4M^2} F_2 \mathcal{E} + \frac{x_{Bj}}{2 - x_{Bj} + x_{Bj} \frac{t}{Q^2}} (F_1 + F_2) \tilde{\mathcal{H}} + \dots \right\}$$

HEMP \rightarrow (MFF)² \rightarrow filter of GPDs and flavors



Vector meson production ($\rho, \omega, \phi, J/\psi \dots$) \Rightarrow H & E

Pseudo-scalar production ($\pi, \eta \dots$) \Rightarrow \tilde{H} & \tilde{E}

But also contribution from
 - gluons and
 - different quark flavor

$$H\rho^0 = 1/\sqrt{2} (2/3 H^u + 1/3 H^d + 3/8 H^g)$$

$$H\omega = 1/\sqrt{2} (2/3 H^u - 1/3 H^d + 1/8 H^g)$$

$$H\phi = -1/3 H^s - 1/8 H^g$$

1 question: 30 m reading + 15 min discussions

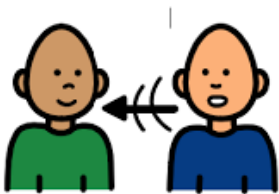
ACTIVE LEARNING

What I hear, I forget

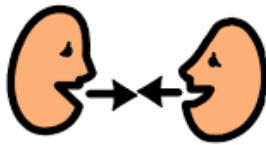
What I see, I remember

What I do, I understand

Talking At Someone



Talking With Someone



Group 1

Meriem*, Shokhna, Kieran, Carlos Y.

Group 5

Nabil*, Brandon C., Fillipo

Group 2

Frederic*, Shujie, Shivangi, Ryan

Group 6

Brandon K.*, Alexa, Bailing, Gavin

Group 3

Waverly*, Sandra, Bijit, Arkadiusz

Group 7

Holly, Larissa, David AQ, Giovanni

Group 4

Hamza, Scott, Marco, Dexu

Group 8

Luca*, Elias, David R.

Group 9

Abel, Tao, Rajesh, Manuel

*: familiar with GPDs/DVCS

Factorization, scaling and twist

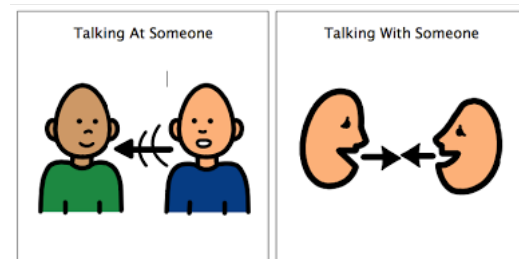
- How do the scaling violations observed in the DIS/PDF case express themselves in the DVCS/GPD case?
- How do they affect the parametrization of the DVCS cross-section in term of GPDs?

Paper of reference:

M. Defurne, 2016, Thesis document, Université Paris-Sud.

Photon and π^0 electroproduction at Jefferson Laboratory- Hall A

Section 1.2 and 1.4



GPDs and Fitting procedures for DVCS

When trying to extract GPDs from DVCS data one often talks about the *curse of dimensionality*. What is this? What are the ways the authors list to deal with it?

Paper of reference:

GPDs and Fitting Procedures for DVCS,

Kumericki and Mueller, 2016, DOI 10.1142/S2010019.

