

Data output for extraction of SFs from DIS and SIDIS

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“Deep Process Working Group Meeting”

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- Inclusive pions and multiplicities
- First measurements of DIS and SIDIS
- MC-generators
- Comparing DIS generated input and output
- Radiative corrections
- Data output
- Summary

The role of MC simulations

- Understand detector performance, extract acceptance and efficiency.
- Optimize the output of data for further analysis using available extraction techniques

Need realistic MC, and maximum possible granularity (dictated by technical possibilities) in relevant bins for proper acceptance account

- 1) DIS, provides possibility to look (monitor) for electron efficiency in the accessible kinematics
- 2) SIDIS multiplicities, provides important info on fragmentation and also allow monitoring electrons and hadrons
- 3) Both should be used to test the extraction of underlying physics (several PAC proposals approved)

Candidate for first SIDIS publication: $e' \pi^0 X$

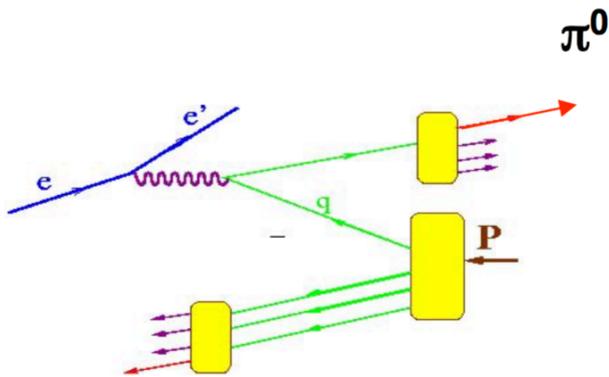
JLab Oct 5

1) $e'X$ -cross section: electron acceptance is relevant for all other measurements cons: we need the acceptance and the luminosity as well as contamination from pions under control.

2) $e' \pi^0 X / e'X$ ratio (ratio of semi-inclusive π^0 to inclusive electron)

For the ratio we just need the gamma acceptance, which could be defined using the KPP

Need: good control for neutral acceptance



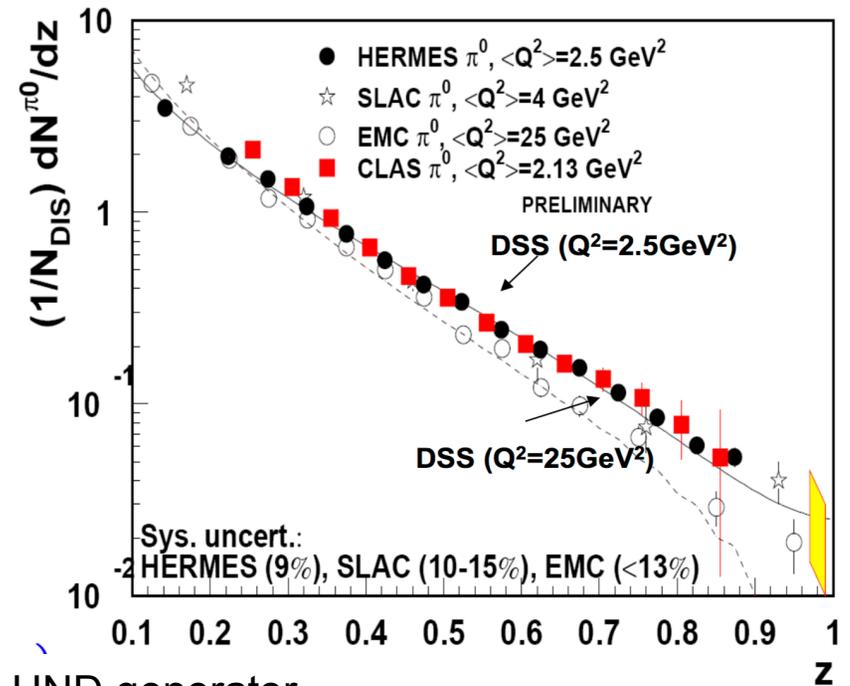
$$\sigma_p^{eX} \propto 4u + d + \dots$$

$$\sigma_p^{\pi^0} \propto 4uD^{u \rightarrow \pi^0} + dD^{d \rightarrow \pi^0} + \dots$$

$$D^{u \rightarrow \pi^0} \approx D^{d \rightarrow \pi^0}$$

clasDIS LUND generator

- 1) ratio should have weak dependence on x
- 2) Ratio should follow z -dependence of the fragmentation function



From SIDIS to DIS

$$\frac{d\sigma}{dx dQ^2 d\psi dz d\phi_h d|\mathbf{P}_{h\perp}|^2} = \frac{\alpha^2}{xQ^4} \frac{y^2}{2(1-\varepsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \varepsilon F_{UU,L} \right\}$$

3D SIDIS

$$F_{UU,T}(x, z, Q^2) = \int d^2 \vec{P}_{h,\perp} F_{UU,T}(x, z, P_{h,\perp}^2, Q^2)$$

$$\frac{d\sigma(lN \rightarrow lX)}{dx dQ^2 d\psi} = \frac{1}{\nu + M} \sum_h \int E_h dE_h \frac{d\sigma(lN \rightarrow lhX)}{dx dQ^2 d\psi dE_h} = \frac{\nu}{\nu + M} \sum_h \int z dz \frac{d\sigma(lN \rightarrow lhX)}{dx dQ^2 d\psi dz}$$

1D SIDIS

$$\frac{d\sigma}{dx dQ^2 d\psi} = \frac{2\alpha^2}{xQ^4} \frac{y^2}{2(1-\varepsilon)} \left\{ F_{UU,T}(x, Q^2) + \varepsilon F_{UU,L}(x, Q^2) \right\}$$

$$\frac{d\sigma}{dx dQ^2 d\psi} = \frac{2\alpha^2}{xQ^4} \frac{y^2}{2(1-\varepsilon)} \left\{ 2(1-\varepsilon)x F_1(x, Q^2) + \varepsilon(1+\gamma^2) F_2(x, Q^2) \right\}$$

DIS

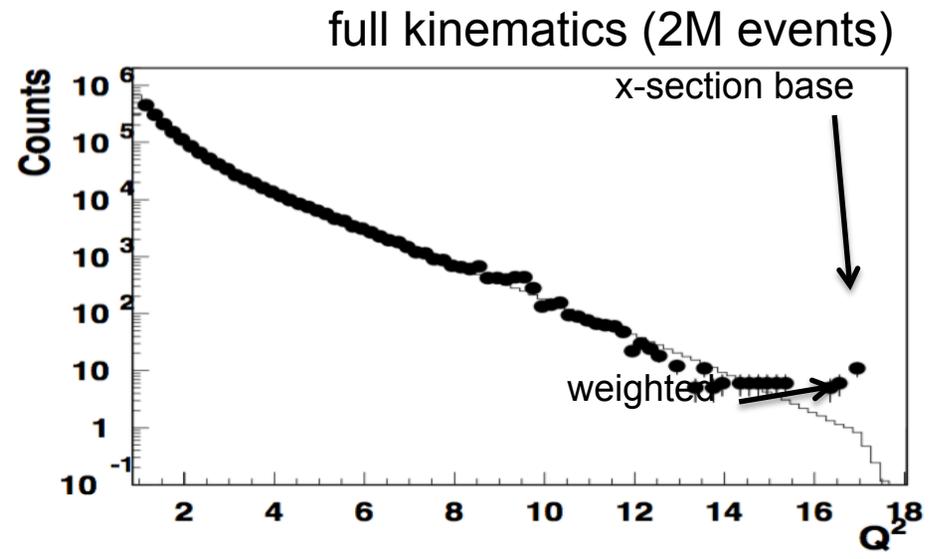
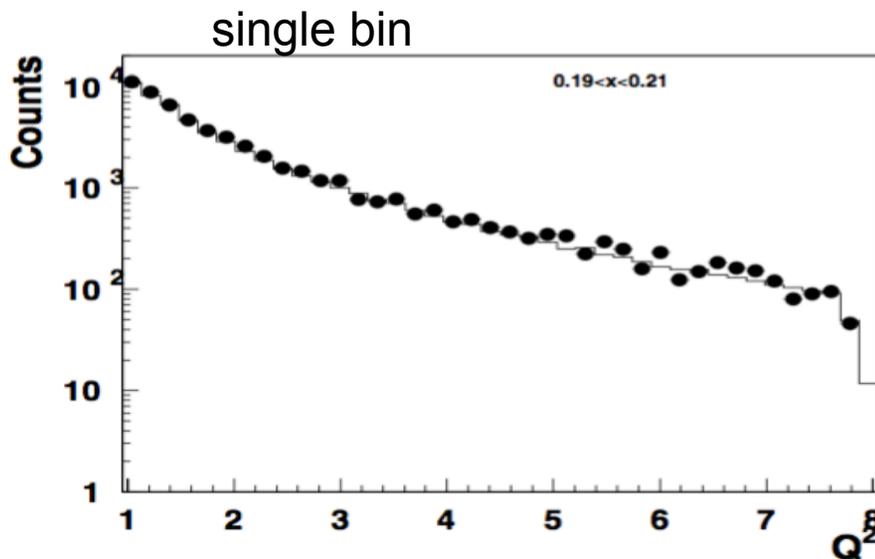
$$F_{UU,T}(x, Q^2) = F_T(x, Q^2) = 2x F_1(x, Q^2) = \sum_h \int z dz F_{UU,T}(x, z, Q^2)$$

$$F_{UU,L}(x, Q^2) = F_L(x, Q^2) = (1+\gamma^2) F_2(x, Q^2) - 2x F_1(x, Q^2) = \sum_h \int z dz F_{UU,L}(x, z, Q^2)$$

Generators: x-section vs weights

gemc-coatjava chain supports both x-section based and weighted generation

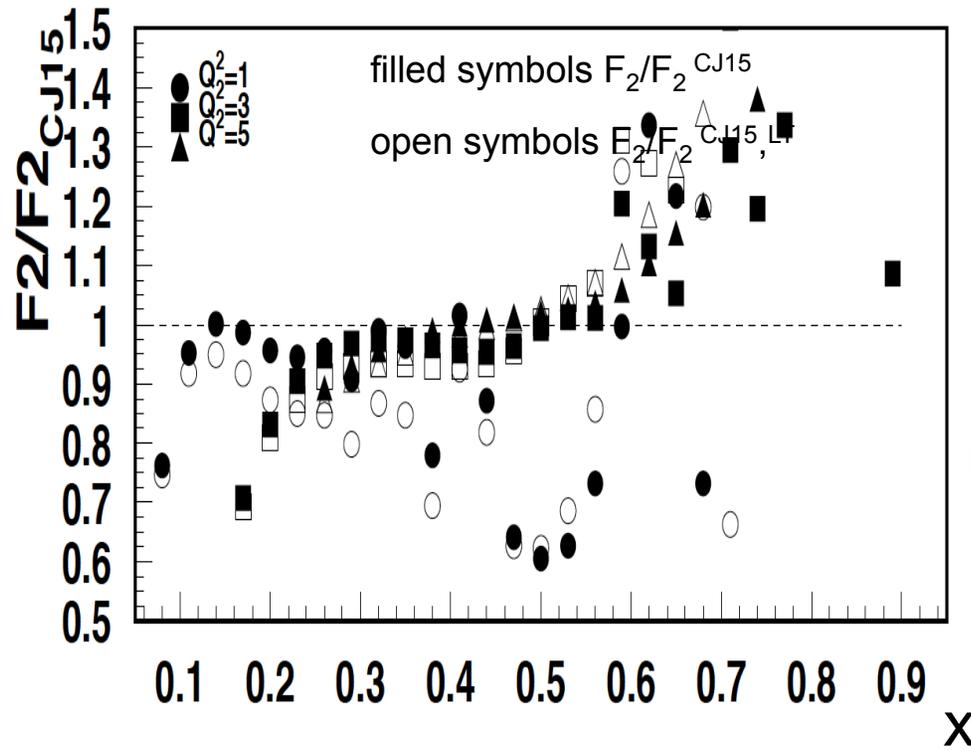
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1	-1.	1	11	0	0	-0.7583	-0.7440	3.9571	4.0972	0.0005	-0.0174	0.0305	1.3425
2	1.	1	211	0	0	0.8698	-0.6332	3.2529	3.4291	0.1396	-0.0174	0.0305	1.3425
	2	1	1	1.0	1.0	11	10.600	2212	1	0.4220764E-02			
1	-1.	1	11	0	0	-1.1716	0.9665	3.2259	3.5656	0.0005	0.0016	-0.0436	-1.5889
2	1.	1	211	0	0	0.1630	-0.4267	3.5986	3.6302	0.1396	0.0016	-0.0436	-1.5889



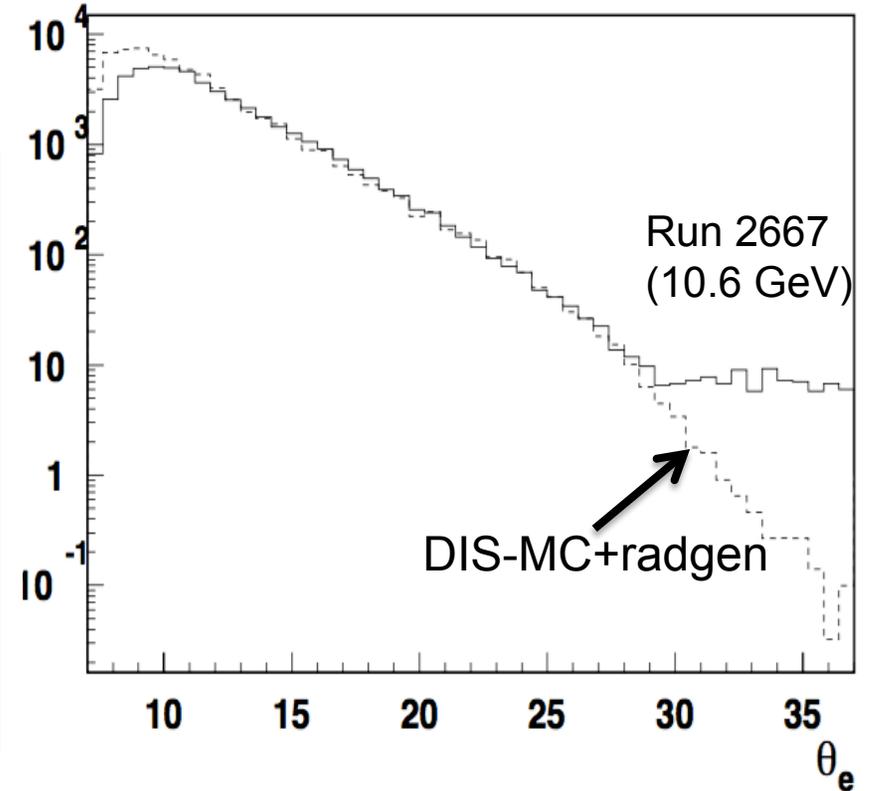
- Two approaches are fully compatible (2M events generated in both cases)
- Using weights for events makes the generation much faster, and most importantly provides statistics for acceptance studies in small bins.

Comparing different DIS models

$$F_2(x, Q^2) = F_2^{LT}(x, Q^2) \left(1 + \frac{C_{HT}(x)}{Q^2} \right)$$



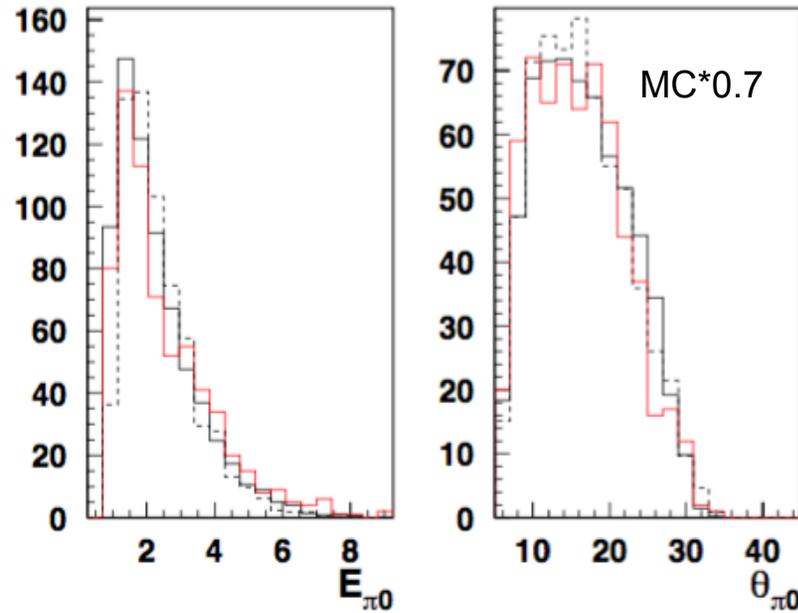
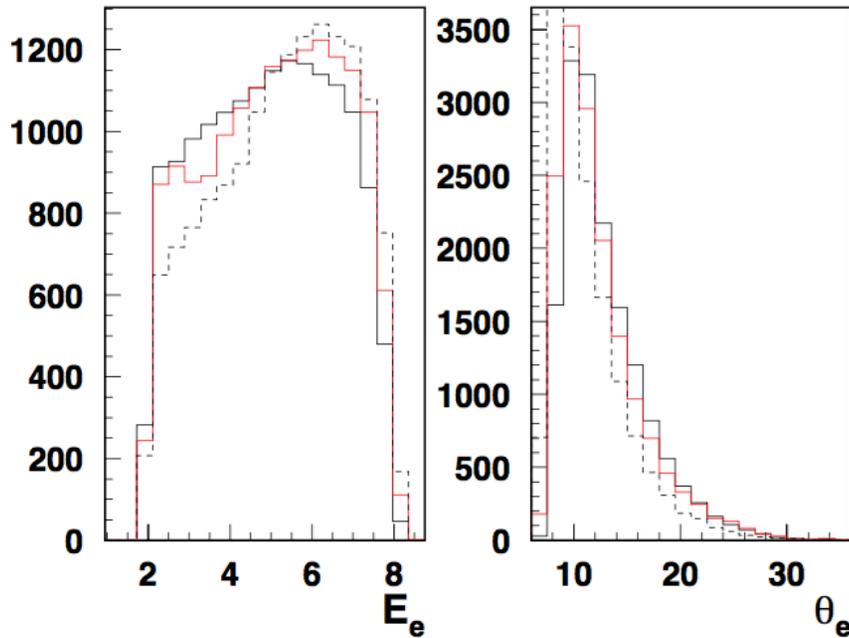
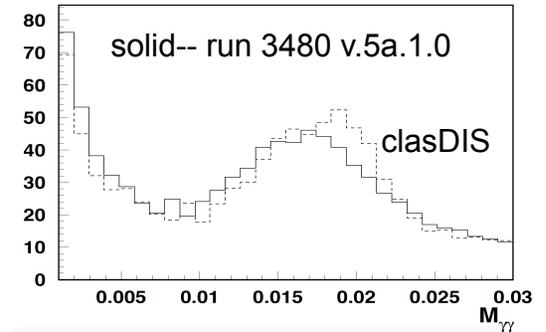
Available realistic SFs, consistent within 10%



reasonable agreement in most of the relevant kinematics

Pi0 efficiency in inbending: new vs old release

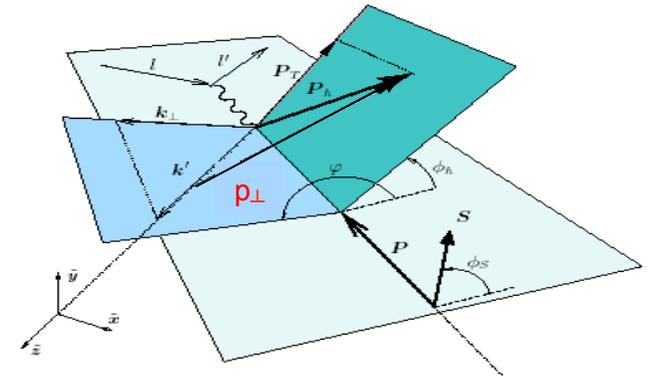
Comparing normalize by number of identified electrons from SIDIS-MC (dashed)
 Run 3480 (solid red lines-v.5a.1.0) and Run 2997
 (solid black v.5a.0.11?)



- Studies of SIDIS with pi-0 require reconstruction of electrons and photons (relatively stable in recent releases)
- Will require development of fiducial cuts for e- and photons for extraction of multiplicities

Reproduce DIS/SIDIS output with MC

SIDIS MC in 7D (10D)



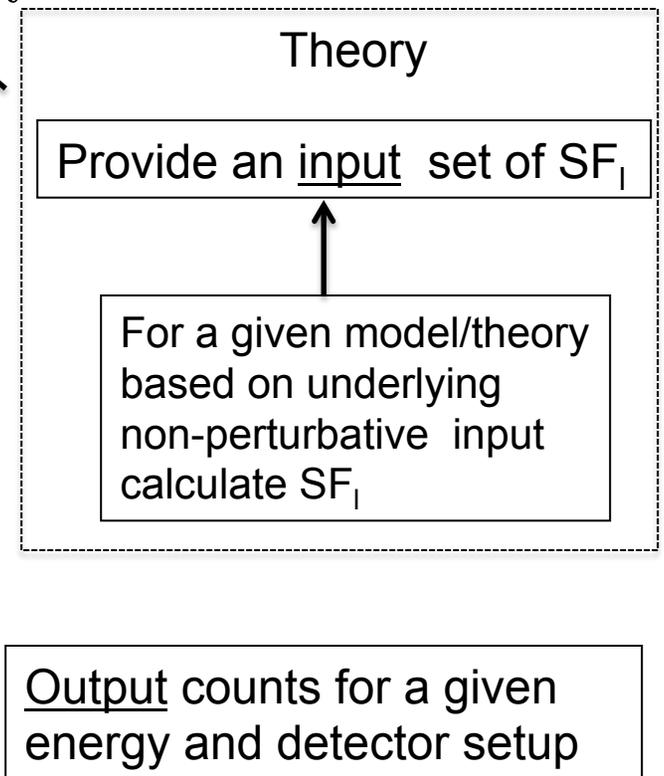
$$\frac{d\sigma_{\lambda\Lambda}^{eN \rightarrow e' h X}}{dx dQ^2 dz dP_{hT}^2 d\phi_h d\phi_l d\phi_s} = \sum_{l=1}^L SF_l$$

step-1 $x_i, Q_i^2, z_i, P_{hT}^{i2}, \phi_h^i, \phi_l^i, \phi_s^i$

step-2 (for a given $E_{\text{beam}}, \lambda, \Lambda$) P_i^{el}, P_i^h

step-3 (detected for a given Detector configuration)

$$x_j, Q_j^2, z_j, P_{hT,j}^2, \phi_h^j, \phi_l^j, \phi_s^j$$



Standard input for SFs

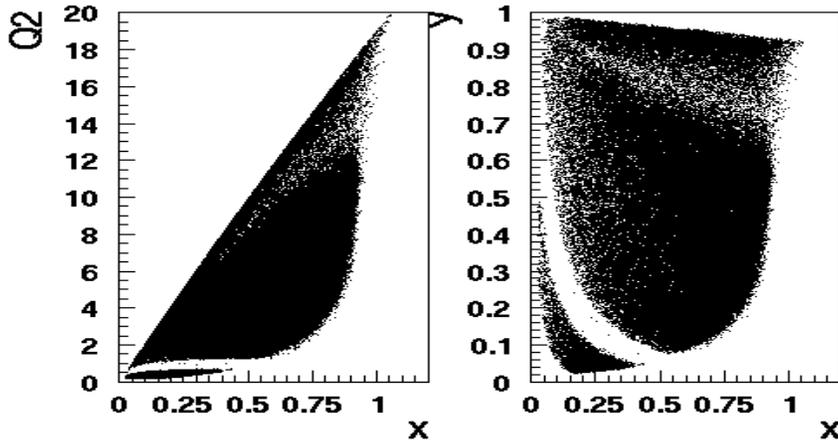
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}
```

(JavaScript Object Notation for a single hadron production $eN \rightarrow e'X$)

Table can be generated from any existing program for calculation of SFs for any given set of parameters, final state particles, target nucleon, polarization states in tiny bins.

ix	iy	x	y	Q2	F2	FL	F3	dsig/dxdy
0	191	5.2610e-02	9.5868e-01	1.0039e+00	3.0120e-01	6.0973e-02	5.4901e-04	1.6325e-03
0	192	5.2610e-02	9.6342e-01	1.0089e+00	3.0160e-01	6.0859e-02	5.5211e-04	1.6154e-03
0	193	5.2610e-02	9.6817e-01	1.0139e+00	3.0199e-01	6.0746e-02	5.5522e-04	1.5987e-03
0	194	5.2610e-02	9.7291e-01	1.0188e+00	3.0239e-01	6.0633e-02	5.5832e-04	1.5823e-03
0	195	5.2610e-02	9.7765e-01	1.0238e+00	3.0278e-01	6.0522e-02	5.6142e-04	1.5662e-03
0	196	5.2610e-02	9.8240e-01	1.0288e+00	3.0317e-01	6.0411e-02	5.6453e-04	1.5503e-03
0	197	5.2610e-02	9.8714e-01	1.0337e+00	3.0355e-01	6.0301e-02	5.6763e-04	1.5348e-03
0	198	5.2610e-02	9.9188e-01	1.0387e+00	3.0394e-01	6.0192e-02	5.7074e-04	1.5196e-03

Binning in DIS



With small bins x,y-binning will be much better for extraction of SFs

- 1) scale variable
- 2) fixed range
- 3) smaller change in resolution

```

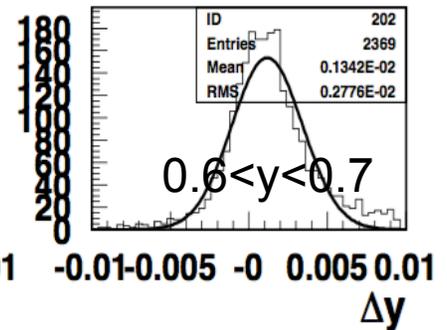
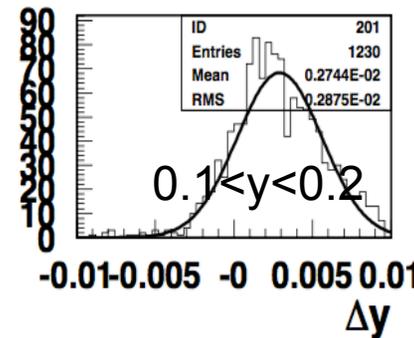
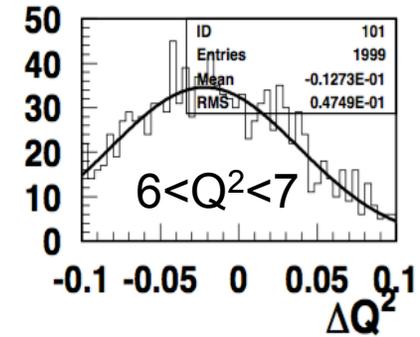
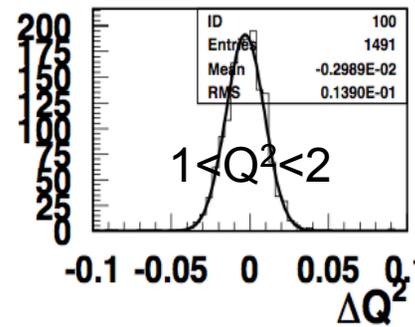
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}

```

More traditional binning in x
 Q^2 used so far

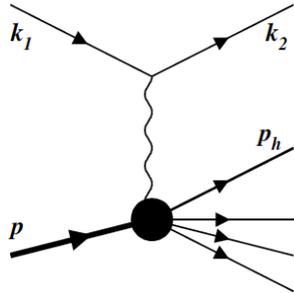
0	0	0.26510E+01	0.65582E-01	0.2844	0.0567	0.9068	1.0230
0	1	0.45973E+00	0.26153E-01	0.1292	0.0583	0.9387	1.0889
1	0	0.50249E+01	0.93813E-01	0.4135	0.0633	0.8204	1.0316
1	1	0.74271E+01	0.10466E+00	0.4572	0.0640	0.8863	1.1270
1	2	0.16775E+01	0.45997E-01	0.2508	0.0664	0.9288	1.2271
2	0	0.42042E+01	0.90587E-01	0.3478	0.0726	0.7160	1.0321
2	1	0.68917E+01	0.10499E+00	0.4300	0.0725	0.7861	1.1326
2	2	0.67994E+01	0.93186E-01	0.5257	0.0726	0.8699	1.2546
2	3	0.32602E+01	0.59573E-01	0.3875	0.0745	0.9191	1.3624
2	4	0.10215E+00	0.99691E-02	0.0751	0.0768	0.9474	1.4476
3	0	0.34061E+01	0.85340E-01	0.2959	0.0818	0.6358	1.0339
3	1	0.56184E+01	0.99012E-01	0.3585	0.0817	0.6982	1.1334
3	2	0.54527E+01	0.86880E-01	0.4473	0.0817	0.7737	1.2556
3	3	0.55007E+01	0.78669E-01	0.5458	0.0816	0.8494	1.3780
3	4	0.42467E+01	0.63689E-01	0.5134	0.0825	0.9090	1.4907
3	5	0.67098E+00	0.23812E-01	0.2186	0.0851	0.9380	1.5869

x=0.4



Radiative SIDIS

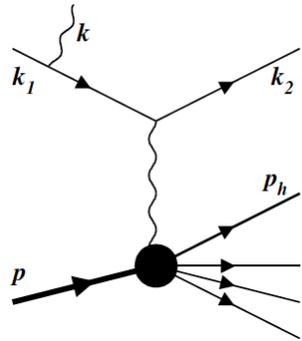
Akushevich&Ilyichev in progress



$$e(k_1, \xi) + n(p, \eta) \longrightarrow e(k_2) + h(p_h) + x(p_x)$$

$$\frac{d\sigma^B}{dx dy dz dp_t^2 d\phi_h d\phi}$$

$$d\sigma^B = \frac{\alpha^2}{\sqrt{\lambda_S} Q^4} W_{\mu\nu} L^{\mu\nu} \frac{d^3 k_2}{k_{20}} \frac{d^3 p_h}{p_{h0}}$$



$$e(k_1, \xi) + n(p, \eta) \rightarrow e(k_2) + h(p_h) + x(\tilde{p}_x) + \gamma(k)$$

$$d\sigma_R = \frac{\alpha^3}{4\pi^2 \tilde{Q}^4 \sqrt{\lambda_S}} W^{\mu\nu}(q - k, p, p_h) L_{\mu\nu}^R \frac{d^3 k}{k_0} \frac{d^3 k_2}{k_{20}} \frac{d^3 p_h}{p_{h0}}$$

+..... additional photon can be described by three additional variables:

$$R = 2kp, \quad \tau = \frac{kq}{kp}, \quad \phi_k$$

$$S_x = 2p(k_1 - k_2)$$

The phase space of the real photon: $\frac{d^3 k}{k_0} = \frac{R dR d\tau d\phi_k}{2\sqrt{\lambda_Y}}$

$$\lambda_Y = S_x^2 - 4M^2 Q^2$$

ϕ_k is an angle between $(\mathbf{k}_1, \mathbf{k}_2)$ and (\mathbf{k}, \mathbf{q}) planes.

$$e(k_1, \xi) + n(p, \eta) \rightarrow e(k_2) + h(p_h) + u(p_u) + \gamma(k), \quad \delta^4(k_1 + p - k_2 - p_h - p_u - k)$$

Radiative DIS

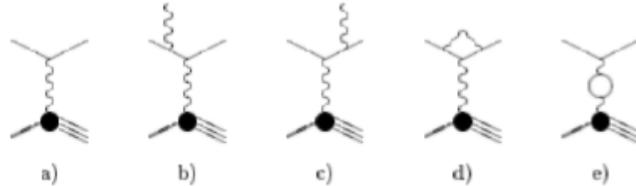
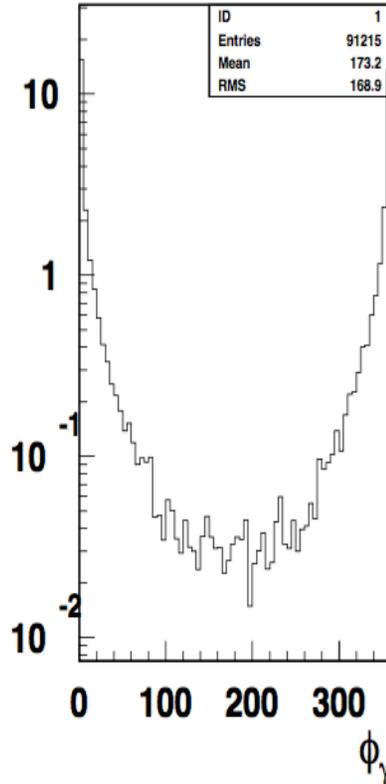
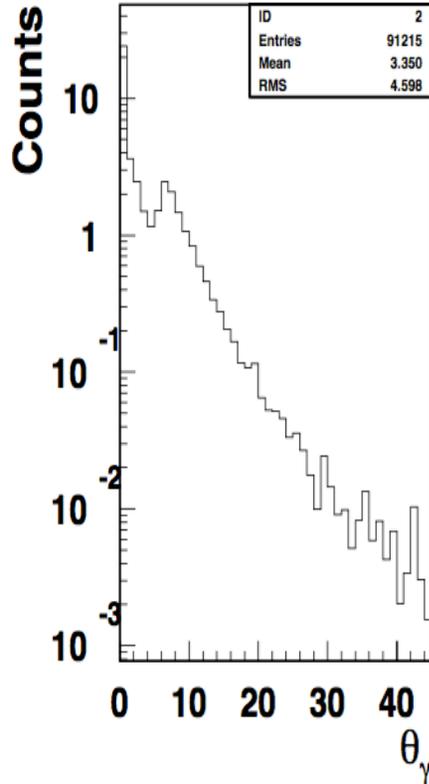


Figure 1: Feynman diagrams contributing to the Born and the radiative correction cross sections in lepton-nucleus scattering.

Akushevich et al. <http://www.jlab.org/RC/radgen/>
[/group/gpd/sidis/inclusive-dis-rad/generate-dis](http://www.jlab.org/RC/radgen/group/gpd/sidis/inclusive-dis-rad/generate-dis)

--xgrid -> use xsec grid
 --sfgrid -> use F_1, F_2, F_L grids
 --writegrid .FALSE. dump the grid
 --rad 0 no radiation, 1-grid, 2-calc



```

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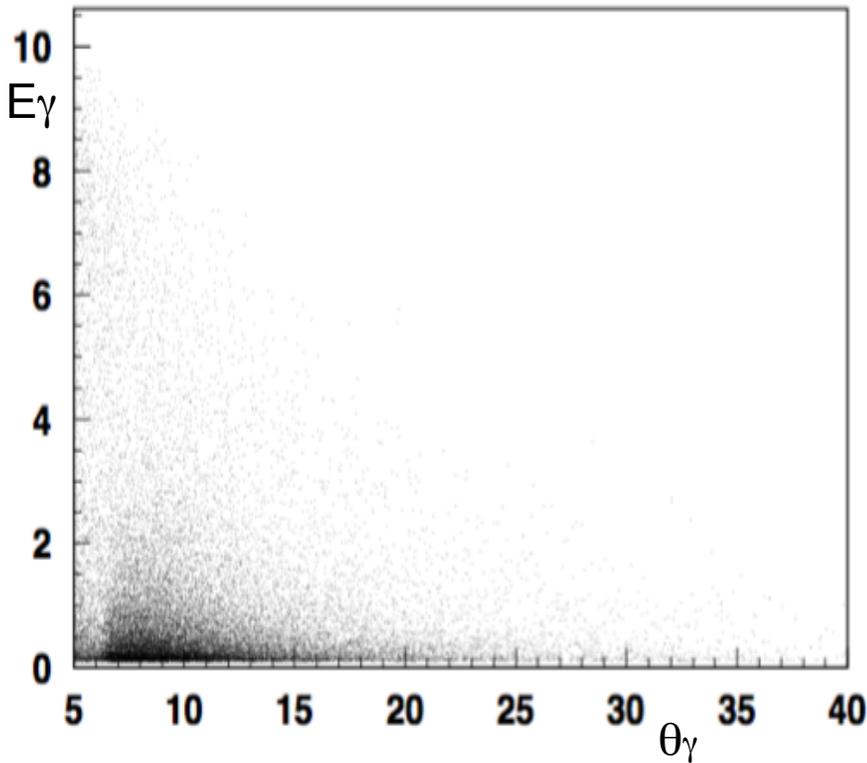
DIS input (N. Sato)

ix	iy	x	y	Q2	F2	FL	F3	dsig/dxdy
0	191	5.2610e-02	9.5868e-01	1.0039e+00	3.0120e-01	6.0973e-02	5.4901e-04	1.6325e-03
0	192	5.2610e-02	9.6342e-01	1.0089e+00	3.0160e-01	6.0859e-02	5.5211e-04	1.6154e-03
0	193	5.2610e-02	9.6817e-01	1.0139e+00	3.0199e-01	6.0746e-02	5.5522e-04	1.5987e-03
0	194	5.2610e-02	9.7291e-01	1.0188e+00	3.0239e-01	6.0633e-02	5.5832e-04	1.5823e-03
0	195	5.2610e-02	9.7765e-01	1.0238e+00	3.0278e-01	6.0522e-02	5.6142e-04	1.5662e-03
0	196	5.2610e-02	9.8240e-01	1.0288e+00	3.0317e-01	6.0411e-02	5.6453e-04	1.5503e-03

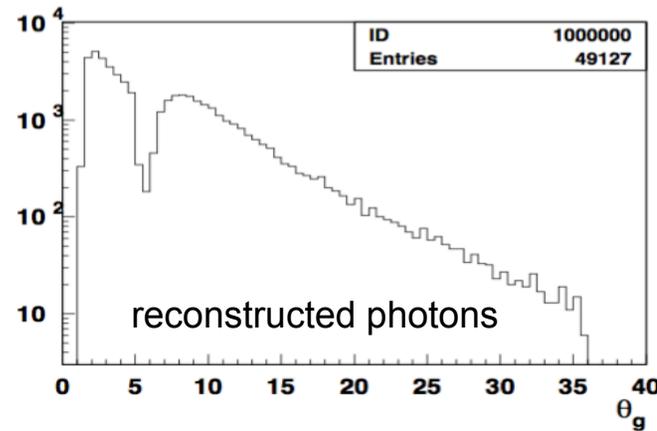
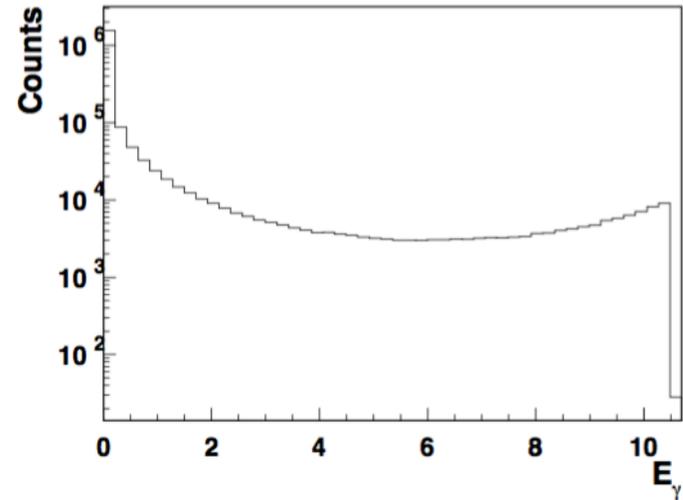
Radiative DIS

Dedicated DIS generator with radgen (gemc input)

	2	1	1	0.12	1.04	11	10.600	2212	1	0.6882683E-05	0.1235496E+00	11.55	8.13
1	-1.	1	11	0	0	-1.2610	-0.0968	1.5722	2.0177	0.0005	-0.0185	0.0768	-0.4312
2	0.	1	22	1	0	0.2821	-0.0185	0.3528	0.4521	0.0000	-0.0185	0.0768	-0.4312



Significant fraction of DIS radiative photons may be reconstructed



Radiative DIS

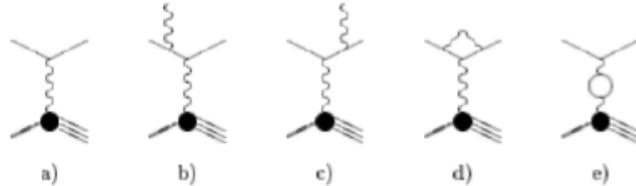
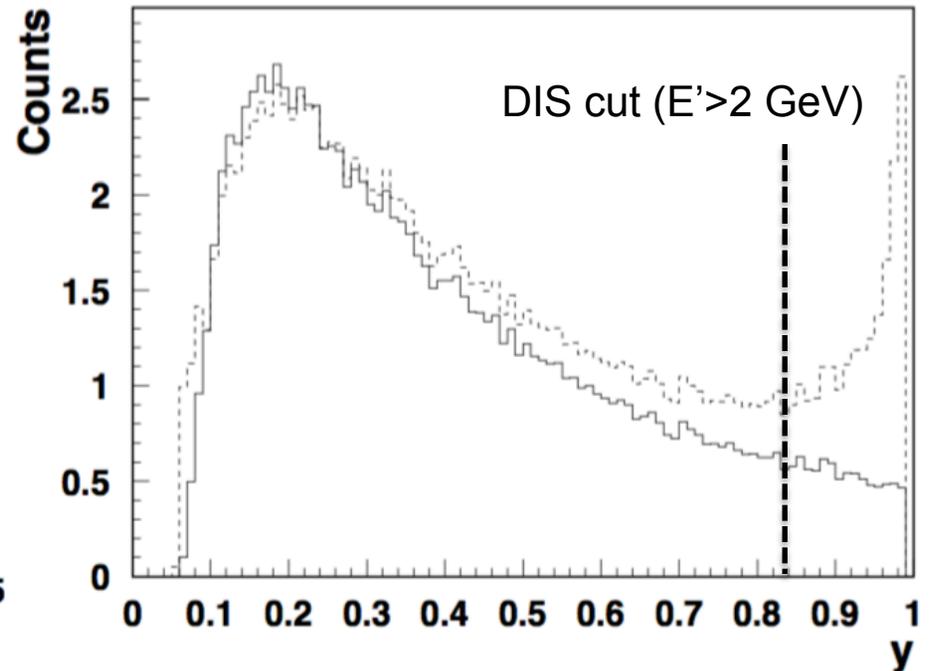
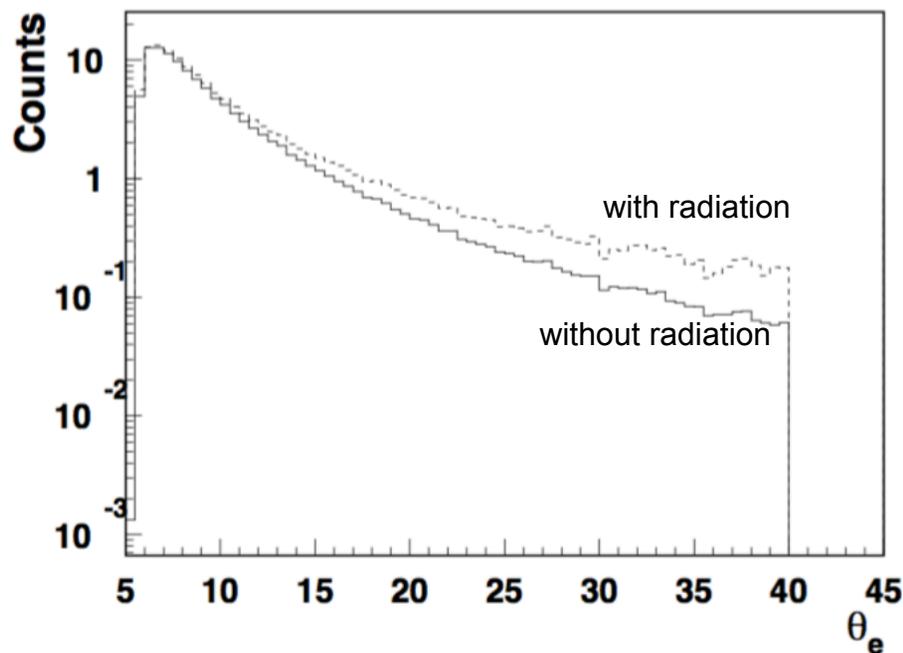


Figure 1: Feynman diagrams contributing to the Born and the radiative correction cross sections in lepton-nucleus scattering.

Akushevich et al. <http://www.jlab.org/RC/radgen/group/gpd/sidis/inclusive-dis-rad/generate-dis>

--rad 1 (table input, generated on flight)



Radiative correction become very significant for low energy scattered electron

Extraction of DIS x-section and acceptance

```

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Radiative corrections may be significant

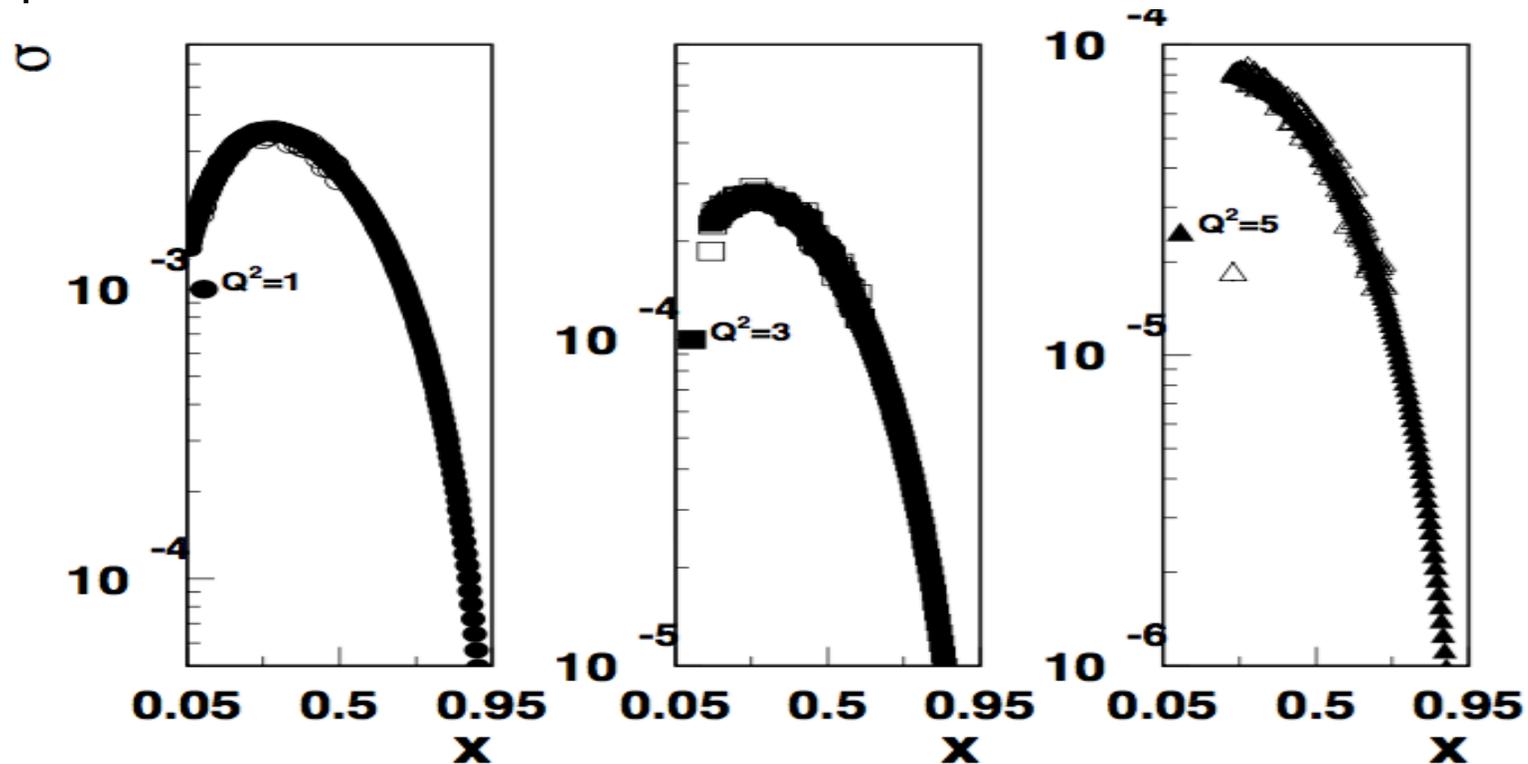


0	0	0.81900E+03	0.33103E+07	0.11567E+06	0.18094E+00	2.5475	0.0566	0.9099	1.0248
0	1	0.17300E+03	0.79404E+06	0.60369E+05	0.83559E-01	3.1196	0.0583	0.9392	1.0883
1	0	0.14940E+04	0.45989E+07	0.11898E+06	0.43024E+00	1.7770	0.0631	0.8246	1.0334
1	1	0.24200E+04	0.78833E+07	0.16025E+06	0.38679E+00	2.2943	0.0637	0.8924	1.1298
1	2	0.74100E+03	0.25279E+07	0.92865E+05	0.18311E+00	2.7515	0.0664	0.9300	1.2276
2	0	0.10610E+04	0.29902E+07	0.91799E+05	0.34089E+00	1.4475	0.0725	0.7176	1.0332
2	1	0.21560E+04	0.54615E+07	0.11762E+06	0.44019E+00	1.5917	0.0723	0.7891	1.1339
2	2	0.26110E+04	0.66272E+07	0.12970E+06	0.51925E+00	2.0516	0.0722	0.8767	1.2579
2	3	0.15350E+04	0.41679E+07	0.10638E+06	0.29366E+00	2.5589	0.0744	0.9235	1.3654
2	4	0.48000E+02	0.14361E+06	0.20728E+05	0.41388E-01	3.0801	0.0768	0.9478	1.4485
3	0	0.82900E+03	0.23725E+07	0.82399E+05	0.30402E+00	1.3423	0.0816	0.6379	1.0341
3	1	0.15660E+04	0.38319E+07	0.96832E+05	0.35124E+00	1.4013	0.0816	0.6993	1.1334
3	2	0.20270E+04	0.42636E+07	0.94699E+05	0.44952E+00	1.5274	0.0814	0.7773	1.2578
3	3	0.24600E+04	0.49319E+07	0.99437E+05	0.54600E+00	1.8039	0.0814	0.8531	1.3798
3	4	0.22240E+04	0.48486E+07	0.10281E+06	0.43699E+00	2.3514	0.0822	0.9135	1.4934
3	5	0.44000E+03	0.10058E+07	0.47048E+05	0.15150E+00	2.7774	0.0850	0.9385	1.5850

- Acceptance can be used to correct distributions for monitoring
- DIS output can be generated using input F_1, F_2 or F_2, F_L or directly x-sections

Recovering generated input from generated set

Step-I



- Reasonable agreement with generated input (filled symbols \rightarrow N. Sato)
- Extract the EBC-bins from actual data using acceptance from MC

Suggested standard input for SFs:SIDIS Example

```

#!{
#!  "model": "VGD_Fuu_01",
#!  "description": "Cahn contribution to cos",
#!  "reference": "M. Boglione, S. Melis & A. Prokudin Phys. Rev. D 84, 034033 2011",
#!  "web-source": "http://aaa.html",
#!  "formula": "$sf1=-2*d/b*a*a*(1-a)^p0*c^p1*(1-c)^p2*c*p3/p4*exp(-d*d/(p4+c*c*p3)/p4$",
#!  "moment": "$A_{uu}\\cos\\phi$",
#!  "lepton-polarization": "0",
#!  "nucleon-polarization": "0",
#!  "particle": "pi+",
#!  "variables": ["AuuCos2","AuuCos2-Err"],
#!  "axis": [
#!    {"name": "a", "bins": 40, "min": 0.025, "max": 0.995, "scale":"arb", "description":"Bjorken x"}
#!    {"name": "b", "bins": 40, "min": 20.00, "max": 4.70, "scale":"arb", "description":"Q^2"},
#!    {"name": "c", "bins": 40, "min": 0.025, "max": 0.995, "scale":"lin", "description":"z,hadron frac. energy"},
#!    {"name": "d", "bins": 40, "min": 0.00, "max": 2.00, "scale":"lin", "description":"P_T, transverse momentum"}
#!  ],
#!  "parameters": [
#!    {"name":"p0", "value": 1.0},
#!    {"name":"p1", "value": 0.2},
#!    {"name":"p2", "value": 0.1},
#!    {"name":"p3", "value": 0.33, "description":"average k_T2"},
#!    {"name":"p4", "value": 0.16, "description":"average pt_T2"}
#!  ]
#! }

```

(JavaScript Object Notation for a single hadron production eN->e' hX)

2 more variables

Multiple files for all relevant combinations of involved parameters

0	0	0	0	-0.01285	0.00200
0	0	0	1	-0.03736	0.00200
0	0	0	2	-0.05850	0.00200
0	0	0	3	-0.07459	0.00200
0	0	0	4	-0.08467	0.00200

- Table can be generated from any existing program for calculation of SFs for any given set of parameters, final state particles, target nucleon, polarization states.

Standard output for data

```
{
  "model": "Nobuo_Fuu_01"
  "description": "F_uu,T"
  "reference": "N. Sato et al"
  "multiplicity": "Counts"
  "Beam Energy": 10.600
  "lepton-polarization": "0"
  "nucleon-polarization": "0"
  "particle": "pi+"
  "variables": ["Counts", "acc", "xav", "qav", "zav", "ptav", "yav", "phav", "pt/zav", "eta"
  "axis": [
    {"name": "a", "bins": 10, "min": 0.05, "max": 0.55, "scale": "lin", "description": "x_bj"}
    {"name": "b", "bins": 7, "min": 1.00, "max": 8.0, "scale": "lin", "description": "Q^2"}
    {"name": "c", "bins": 7, "min": 0.20, "max": 0.9, "scale": "lin", "description": "z"}
    {"name": "d", "bins": 15, "min": 0.00, "max": 1.5, "scale": "lin", "description": "PT"}
    {"name": "e", "bins": 36, "min": 0.0, "max": 360.0, "scale": "lin", "description": "PHI"}
  ],
  "parameters": [
  ]
}
11 1 1 4 0.999900E+02 0.0141 0.0994 1.0424 0.2636 0.0708 0.5271 0.5492 0.2686 -0.5311
1 1 1 1 5 0.110602E+03 0.0191 0.0937 1.0067 0.2710 0.0818 0.5404 0.8707 0.3000 -0.5052
.....
1 1 1 1 35 0.655700E+02 0.0090 0.0969 1.1218 0.2447 0.0310 0.5820 5.9564 0.1266 -0.5818
1 1 1 1 36 0.619600E+01 0.0012 0.0913 1.0703 0.2268 0.0029 0.5896 6.1982 0.0136 -0.5068
1 1 1 2 4 0.604000E+03 0.0311 0.0985 1.0670 0.2055 0.1918 0.5446 0.6019 0.9336 0.1294
1 1 1 2 7 0.911300E+03 0.0385 0.0927 1.2218 0.2506 0.1408 0.6631 1.1898 0.5642 -0.3208
```

keep bins in phi

- Table may contain generated (for given beam energy) or reconstructed (for given detector configuration) event counts
- Some bins miss due to phase space limitations and detector acceptance

Summary

- Inclusive electron cross sections well known, can be extracted and compared with world data and existing parameterizations
 - π^0 -multiplicities can be extracted and used in studies of fragmentation functions
 - Developed DIS generator has flexible input (x-sections, structure functions, grids, functional forms) can generate events in (x,y) and (x,Q²) space both in weighting and x-section modes, as well as with and without radiative effects.
 - EBC files created from generated/reconstructed DIS events
Tables files (/work/clas12/avakian/eva/) produced from simulation can be used to correct for acceptance and radiative corrections.
 - Extraction procedures based on DIS input tested.
-
- Need realistic MC, and maximum possible granularity (dictated by technical possibilities) in relevant bins for proper acceptance account
 - Understand detector performance and define fiducial region
 - Optimize the output of data for further analysis using available extraction techniques

Support slides...

Implementation

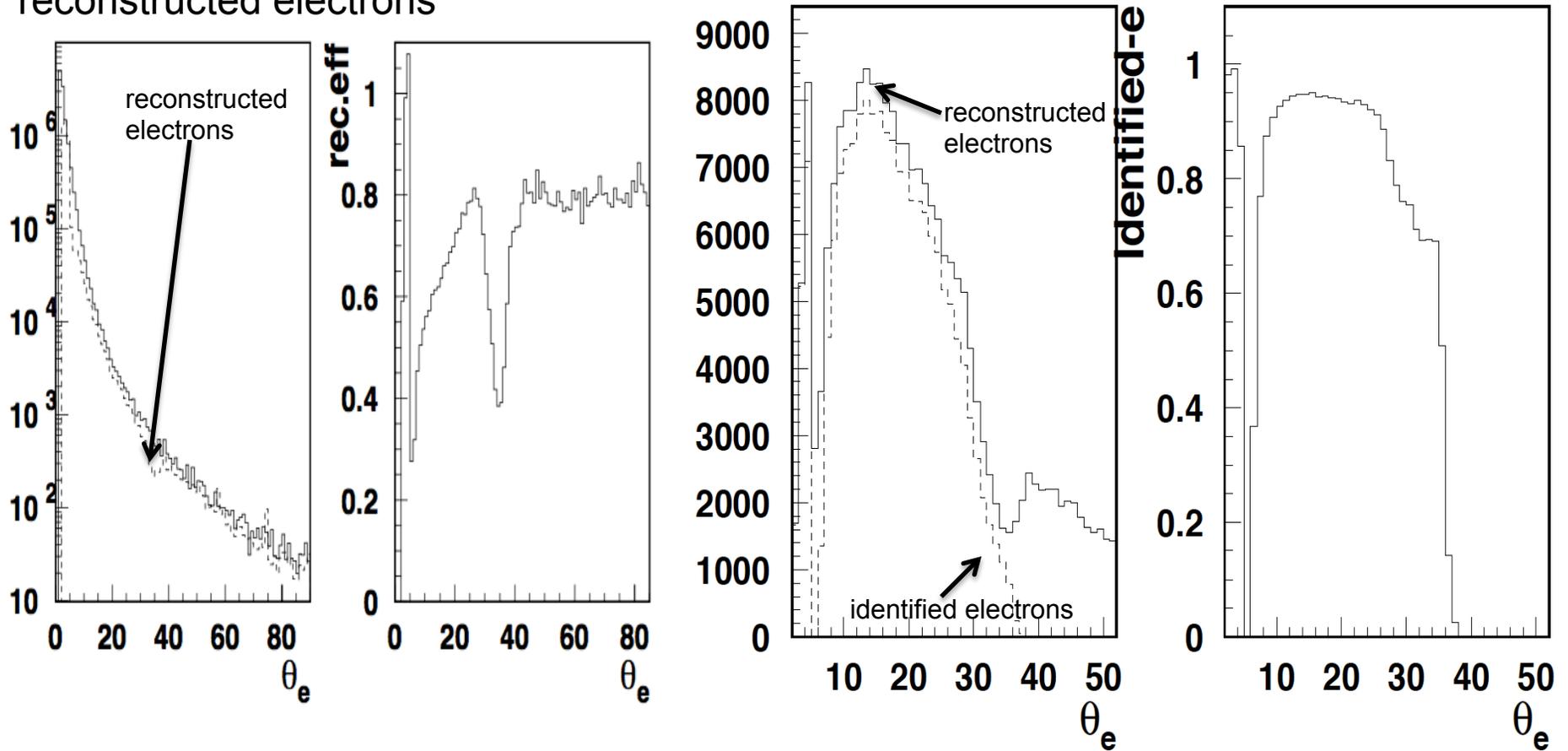
- “Solid” : one program controlling the flow starting from SF calculations up to extraction of TMDs
 - advantages
 - self consistent, flexible, simpler to validate internally
 - takes number of parameters and variables and processes the full chain
 - disadvantages
 - Complex, hard to link different contributors, hard to check, add new SFs
- “Modular” : many programs (may be in different languages) communicating through JSON input/output files.
 - advantages
 - easier to write, different people can contribute at different stages
 - disadvantages
 - harder to run the full chain in consistent way, validation is not trivial

In both cases we need a collaboration of theorists, experimentalists and software experts to run the full chain

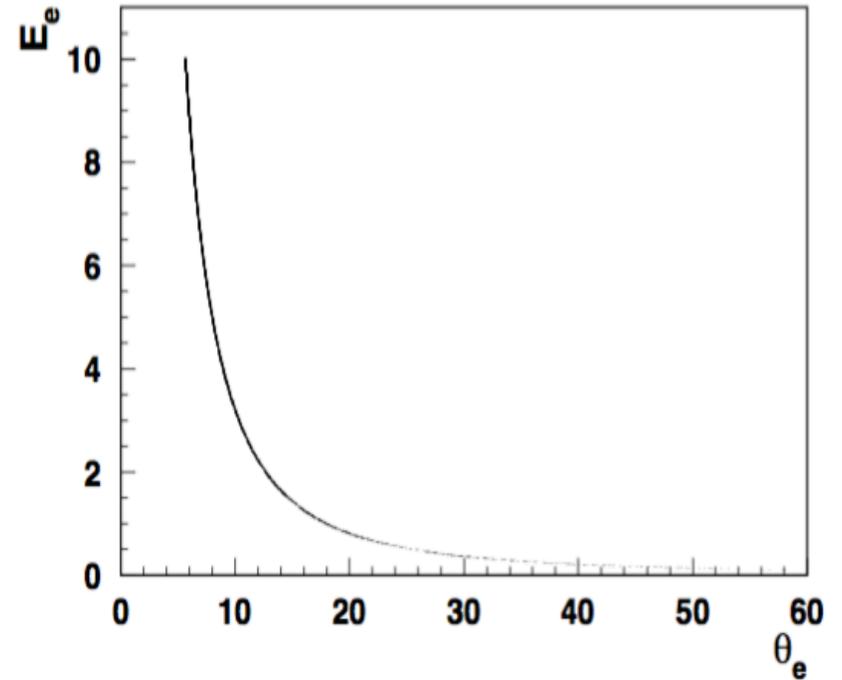
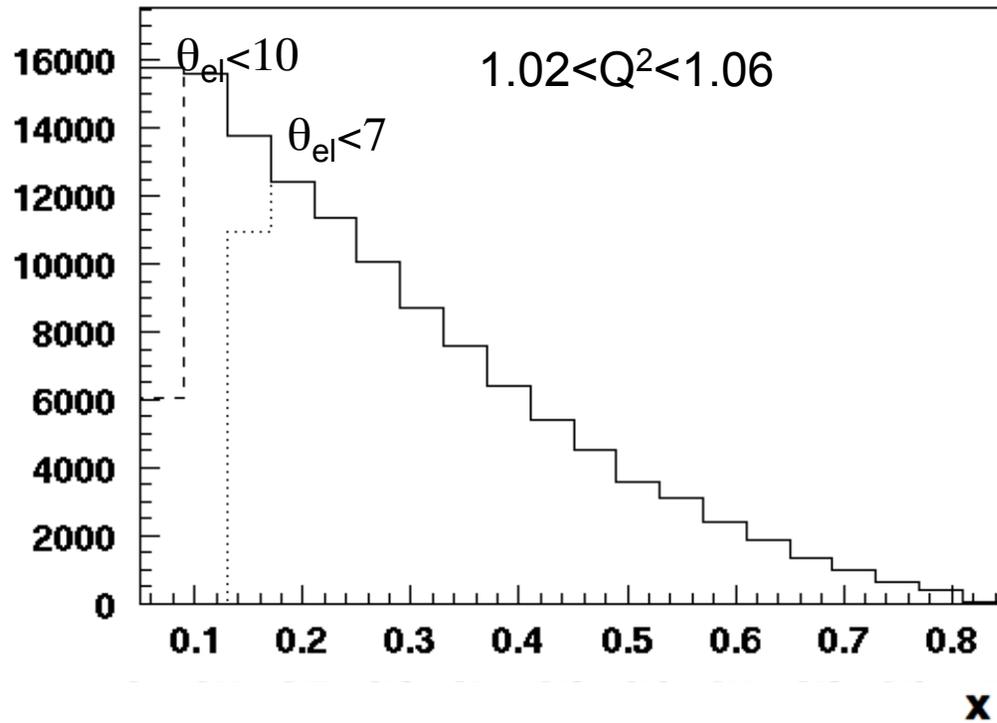
Reconstruction using clas12

Using DIS generator+gemc 4a.2.2 +coatjava v. 4a.8.4

reconstructed electrons



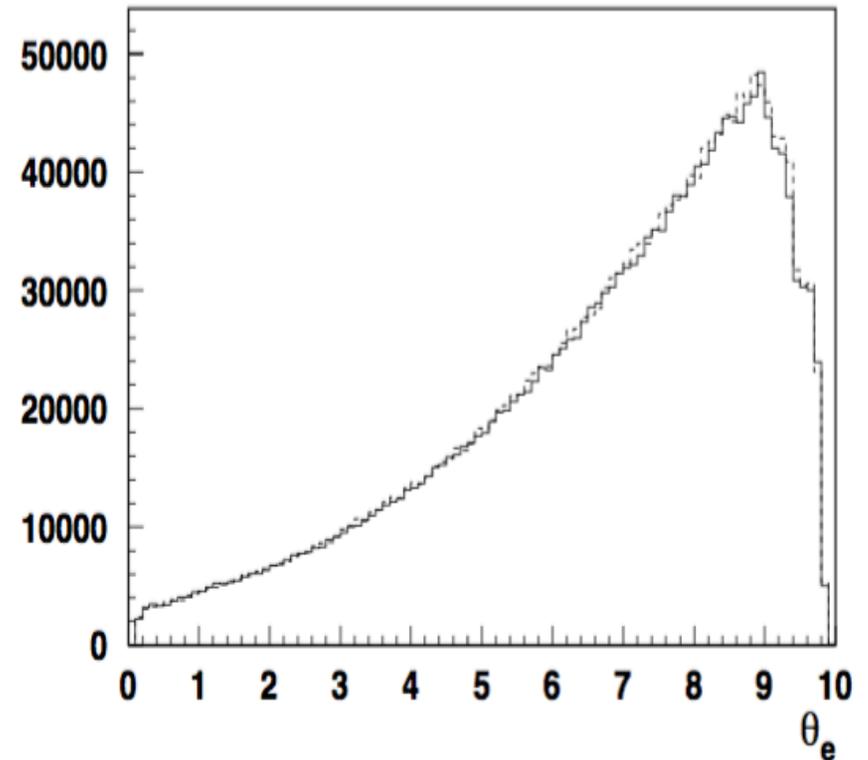
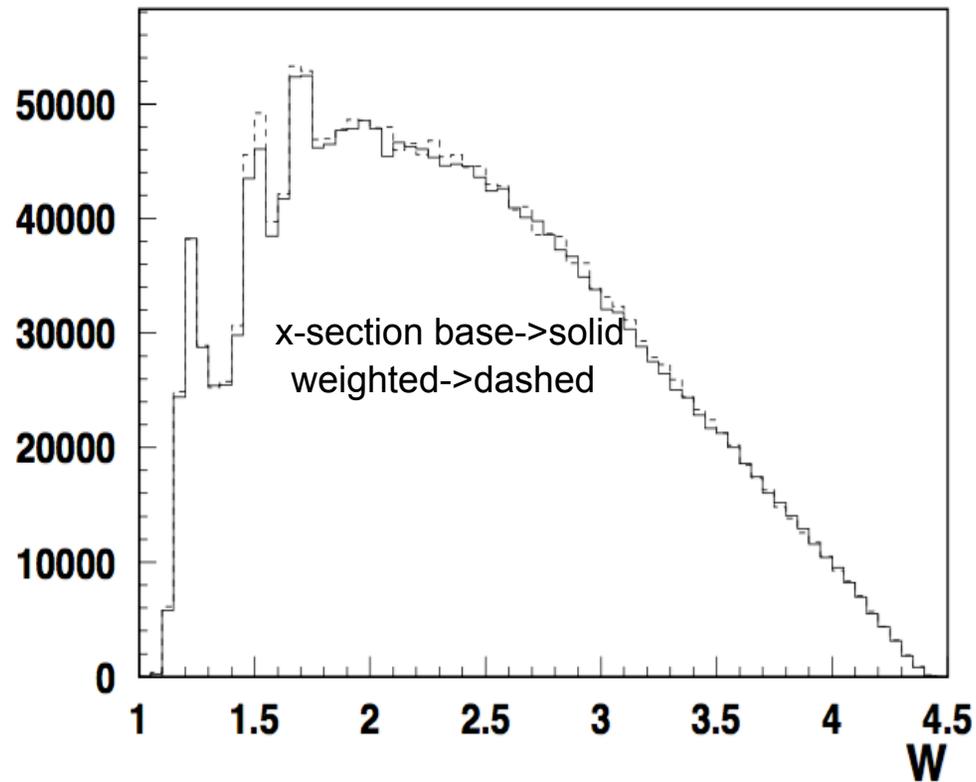
Phase space and acceptance



Limitations in energy and angle deform the phase space

Generators: x-section vs weights

full kinematics (2M events)



- Two approaches are fully compatible (2M events generated in both cases)

Estimating systematics

Steps for Extraction and Validation procedure

- 1) make sure we can recover the underlying 3D PDFs (TMD/GPD...) PDF from generated for a given beam energy sample
- 2) make sure we can recover the underlying 3D PDFs (TMD/GPD...) from reconstructed for a given detector configuration sample

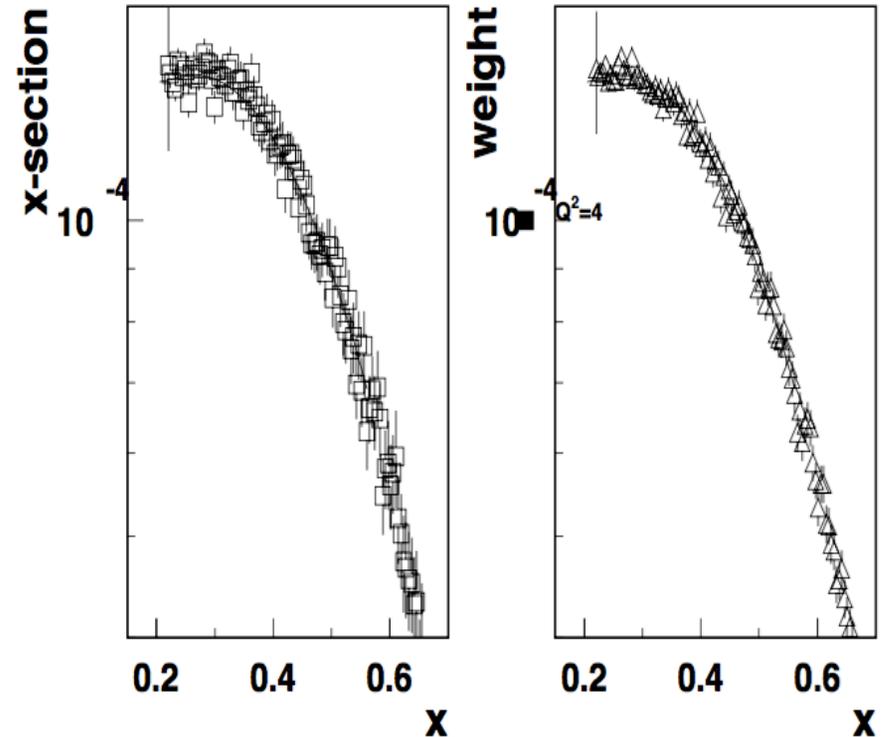
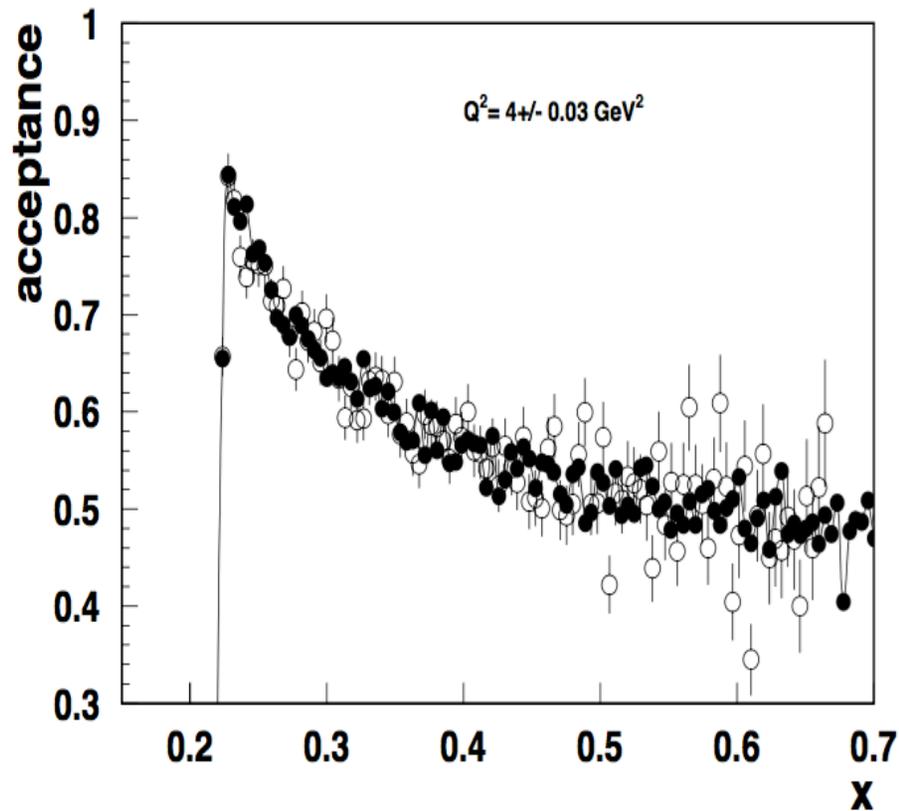
- 1) add radiative effects
 - 2) add other SFs to see the effect of Cahn on extraction of the $F_{UU,T}$ and check the extraction of \cos and \cos^2 moments
 - 3) add/eliminate evolution effects with HT effects and see if we can indeed separate them
 - 4) add $F_{UU,L}$ part (HERMES is using R in their multiplicities) and see the effect of disregarding it in the extraction.
- big list of systematic checks....

Recovering generated input from reconstructed set

Step-II

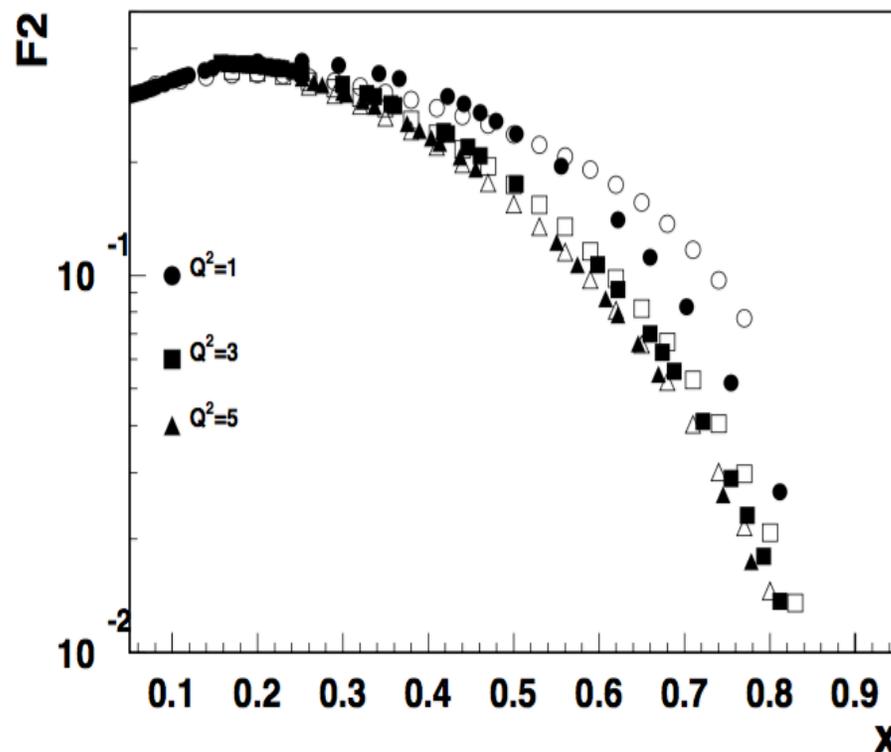
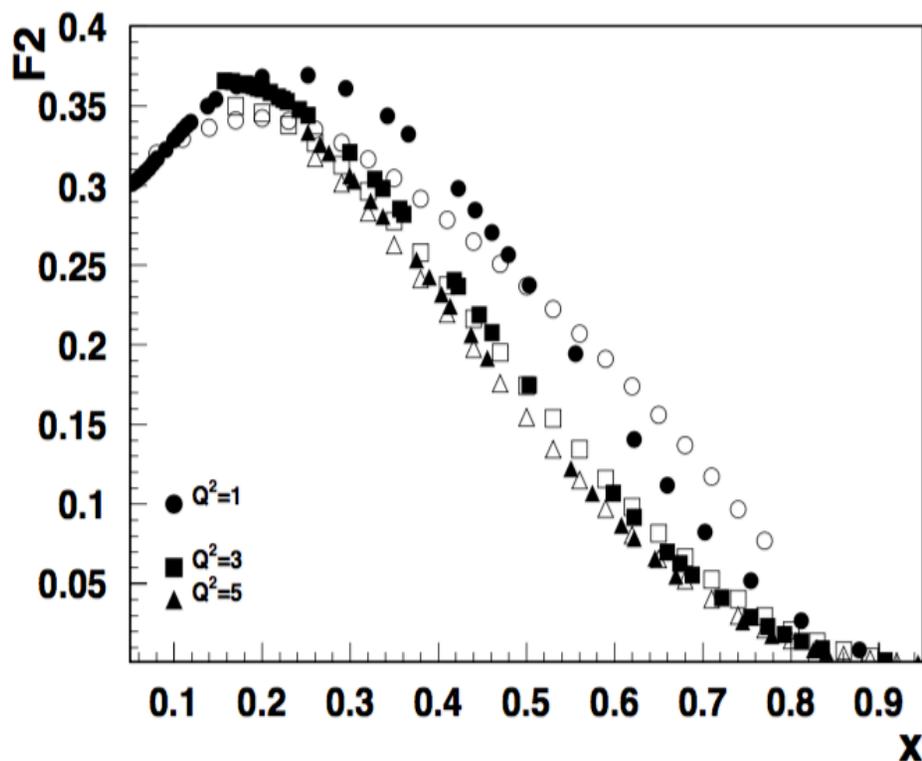
40Mil generated events (200x200 bins)

line N. Sato



- Acceptance can be defined using the weighted generator set
- Both MCs after reconstruction recover the generated input in most of the kinematics.)

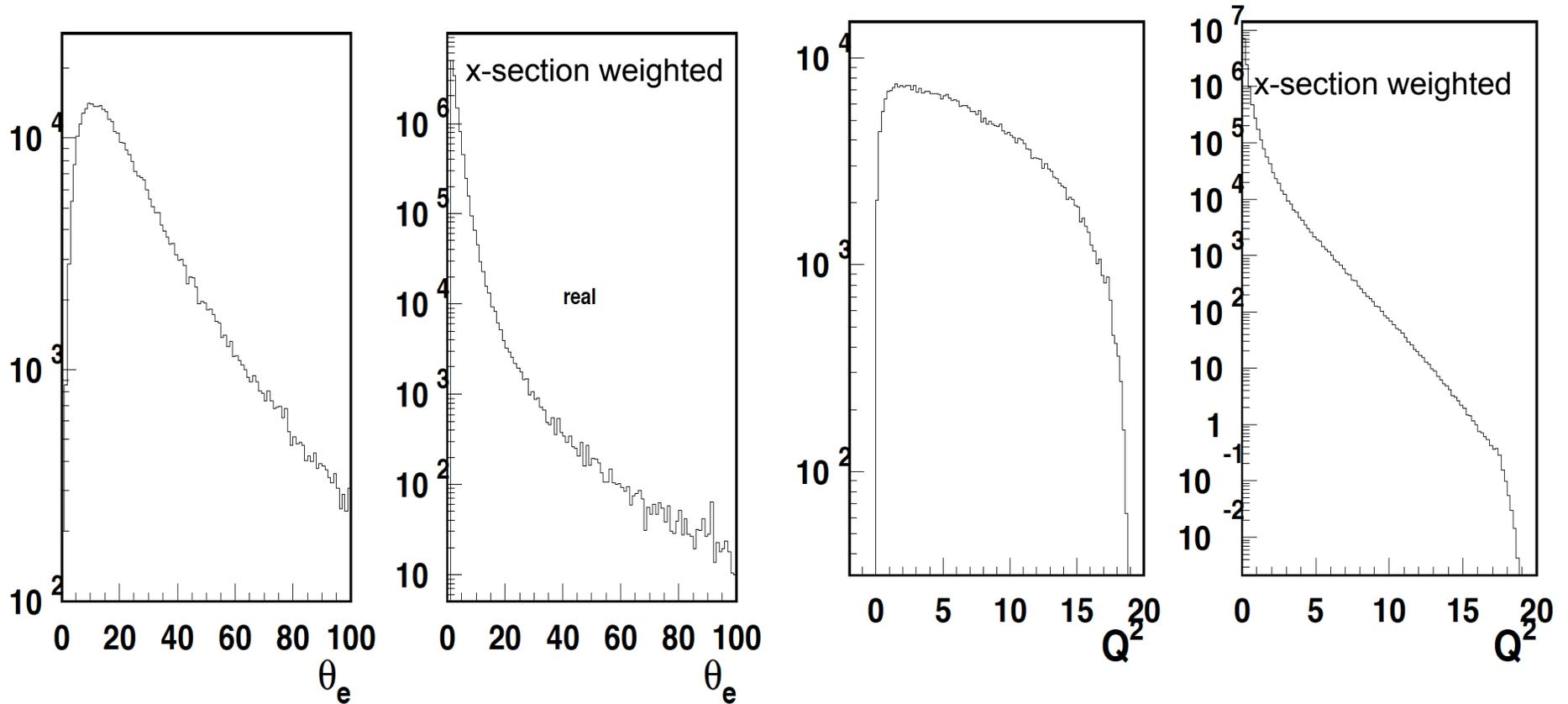
F2 Nobuo vs CJ15



Difference more significant at small Q^2

Reconstruction using clas12

Using DIS generator+gemc 4a.2.2 +coatjava v. 4a.8.4



Generators for MC simulations

- Full event generators (PYTHIA, PEPSI, LEPTO)
- Dedicated event generators ($e^+ X, e^+ hX, e^+ hhx, \dots$)

Types of event generators:

- 1) Providing events with cross section
 - 1) pros: easier defined systematics, can be directly compared with data
 - 2) cons: require huge statistics to provide acceptance functions for kinematic edges with reasonable error bars.
- 2) Phase space with realistic x-sections provided as weight factors.
 - 1) pros: acceptance for all acceptable kinematics can be provided with small error bars, much faster, easy to incorporate different models
 - 2) cons: more efforts to define systematics, need weighting

Generating DIS and SIDIS

Full event generator (PEPSI)

	N_tracks	A	N	I-pol	N-pol	I-ID	E_beam	T	T-ID	process-ID	x-section		
	13	1	1	0.0	1.0	11	10.600	2212	1	0.8052759E+05			
1	-1.	21	11	0	0	0.0000	0.0000	10.6000	10.6000	0.0005	0.0000	0.0000	0.0000
2	1.	21	2212	0	0	0.0000	0.0000	0.0000	0.9383	0.9383	0.0000	0.0000	0.0000
3	0.	21	22	1	0	-0.9974	-0.7292	3.5178	3.4109	-1.5059	0.0000	0.0000	0.0000
4	-1.	1	11	1	0	0.9974	0.7292	7.0822	7.1891	0.0005	0.0000	0.0000	0.0000
5	1.	13	2	0	6	-1.0092	-0.9040	3.2382	3.5102	0.0056	0.0000	0.0000	0.0000
6	0.	13	2103	2	0	0.0117	0.1747	0.2796	0.8389	0.7713	0.0000	0.0000	0.0000
7	1.	12	2	5	9	-1.0092	-0.9040	3.2382	3.5102	0.0056	0.0000	0.0000	0.0000
8	0.	11	2103	6	9	0.0117	0.1747	0.2796	0.8389	0.7713	0.0000	0.0000	0.0000
9	0.	11	92	7	10	-0.9974	-0.7292	3.5178	4.3492	2.2391	0.0000	0.0000	0.0000
10	2.	11	2224	9	12	-0.7729	-1.0806	3.4710	3.9069	1.2047	0.0000	0.0000	0.0000
11	-1.	1	-211	9	0	-0.2245	0.3514	0.0468	0.4422	0.1396	0.0000	0.0000	0.0000
12	1.	1	2212	10	0	-0.5843	-0.9049	2.3668	2.7645	0.9383	0.0000	0.0000	0.0000
13	1.	1	211	10	0	-0.1886	-0.1757	1.1042	1.1425	0.1396	0.0000	0.0000	0.0000

0 (twist-4)

$$\frac{d\sigma}{dx dQ^2 d\psi dz d\phi_h d|P_{h\perp}|^2} = \frac{\alpha^2}{xQ^4} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x}\right) \left\{ F_{UU,T} + \epsilon F_{UU,L} \right\}$$

Dedicated (inclusive pion generator)

	2	1	1	1.0	1.0	11	10.600	2212	1	0.1108596E-01			
1	-1.	1	11	0	0	-0.7583	-0.7440	3.9571	4.0972	0.0005	-0.0174	0.0305	1.3425
2	1.	1	211	0	0	0.8698	-0.6332	3.2529	3.4291	0.1396	-0.0174	0.0305	1.3425
	2	1	1	1.0	1.0	11	10.600	2212	1	0.4220764E-02			
1	-1.	1	11	0	0	-1.1716	0.9665	3.2259	3.5656	0.0005	0.0016	-0.0436	-1.5889
2	1.	1	211	0	0	0.1630	-0.4267	3.5986	3.6302	0.1396	0.0016	-0.0436	-1.5889

$$\frac{d\sigma}{dx dQ^2 d\psi} = \frac{2\alpha^2}{xQ^4} \frac{y^2}{2(1-\epsilon)} \left\{ 2(1-\epsilon)x F_1(x, Q^2) + \epsilon(1+\gamma^2) F_2(x, Q^2) \right\}$$

Dedicated DIS generator

	2	1	1	0.12	1.04	11	10.600	2212	1	0.6882683E-05	0.1235496E+00	11.55	8.13
1	-1.	1	11	0	0	-1.2610	-0.0968	1.5722	2.0177	0.0005	-0.0185	0.0768	-0.4312
2	0.	1	22	1	0	0.2821	-0.0185	0.3528	0.4521	0.0000	-0.0185	0.0768	-0.4312

Generating DIS and SIDIS

Dedicated SIDIS generator

```

      2      1      1      1.0      1.0      11      10.600      2212      1      0.1108596E-01
1 -1.      1      11      0      0      -0.7583      -0.7440      3.9571      4.0972      0.0005      -0.0174      0.0305      1.3425
2 1.      1      211      0      0      0.8698      -0.6332      3.2529      3.4291      0.1396      -0.0174      0.0305      1.3425
      2      1      1      1.0      1.0      11      10.600      2212      1      0.4220764E-02
1 -1.      1      11      0      0      -1.1716      0.9665      3.2259      3.5656      0.0005      0.0016      -0.0436      -1.5889
2 1.      1      211      0      0      0.1630      -0.4267      3.5986      3.6302      0.1396      0.0016      -0.0436      -1.5889
    
```

Dedicated DIS generator (Bosted)

```

      1      1      1      1.0      1.0      11      10.600      2212      1      0.6224668E+00
1 -1.      1      11      0      0      -0.6109      1.3411      8.1241      8.2567      0.0005      -0.1465      0.0724      -0.0298
    
```

COATJAVA 4a.8.4

```

"bank": "MC::Event",
"group": 41,
"info": "Lund header bank for the generated event",
"items": [
  {"name": "npart", "id":1, "type":"int16", "info":"number of particles in the event"},
  {"name": "atarget", "id":2, "type":"int16", "info":"Mass number of the target"},
  {"name": "ztarget", "id":3, "type":"int16", "info":"Atomic number of the target"},
  {"name": "ptarget", "id":4, "type":"float", "info":"Target polarization"},
  {"name": "pbeam", "id":5, "type":"float", "info":"Beam polarization"},
  {"name": "btype", "id":6, "type":"int16", "info":"Beam type, electron=11, photon=22"},
  {"name": "ebeam", "id":7, "type":"float", "info":"Beam energy (GeV)"},
  {"name": "targetid", "id":8, "type":"int16", "info":"Interacted nucleon ID (proton=2212, neutron=2112)"},
  {"name": "processid", "id":9, "type":"int16", "info":"Process ID"},
  {"name": "weight", "id":10, "type":"float", "info":"Event weight"}
]
    
```

GEMC

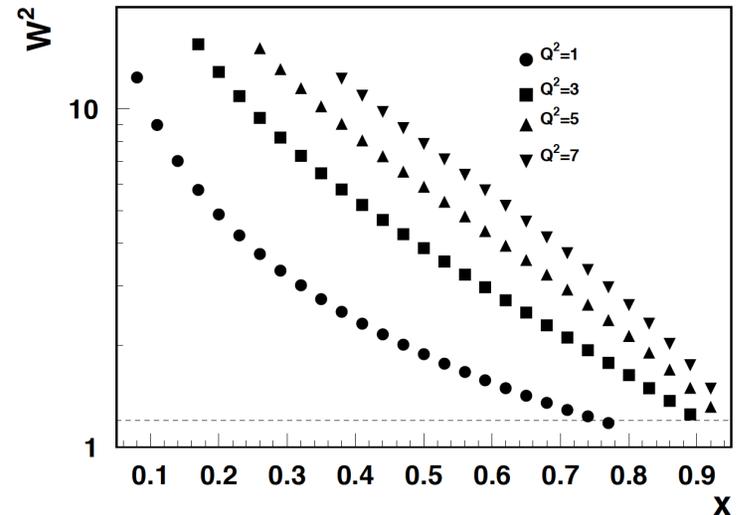
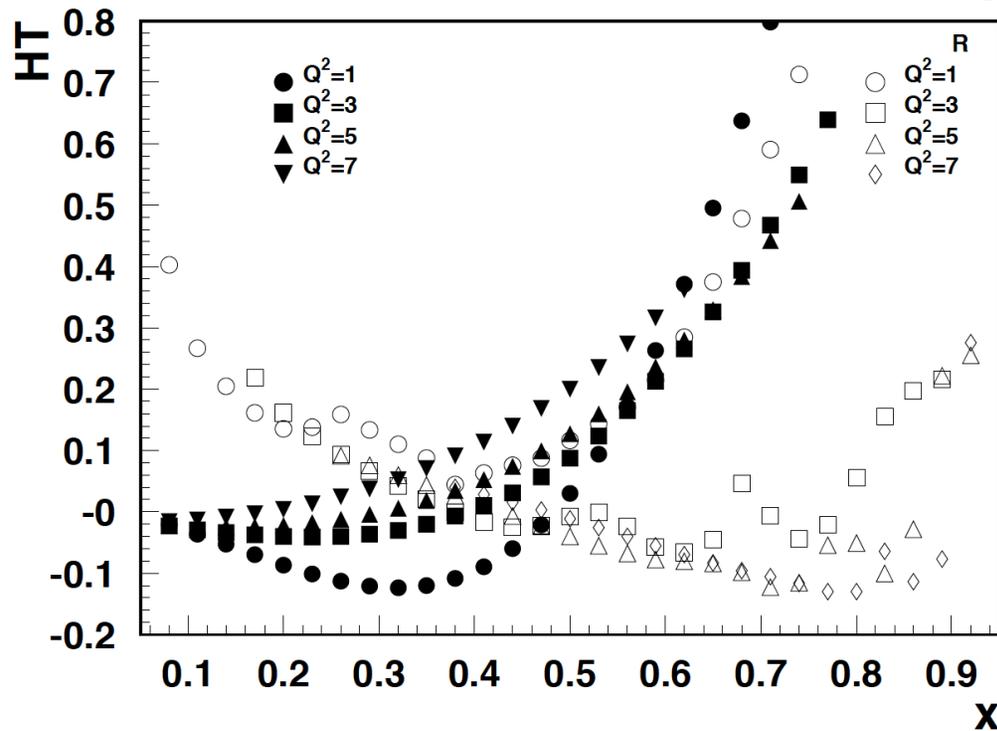
LUND Header		LUND Particles	
column	quantity	column	quantity
1	Number of particles	1	index
2	Number of target nucleons	2	lifetime
3	Number of target protons	3	type (1 is active)
4	Target Polarization	4	particle ID
5	Beam Polarization	5	parent index
6	beam PID (electron=11, photon=22)	6	index of the first daughter
7	beam energy	7	momentum x [GeV]
8	target nucleon ID	8	momentum y [GeV]
9	process ID	9	momentum z [GeV]
10	event weight/cross section	10	E
		11	mass
		12	vertex x [cm]
		13	vertex y [cm]
		14	vertex z [cm]

DIS input from theory and phenomenology

Study the effect of $F_{UU,L}$ (accounted in DIS and ignored in SIDIS)

$$F_2(x, Q^2) = F_2^{LT}(x, Q^2) \left(1 + \frac{C_{HT}(x)}{Q^2} \right)$$

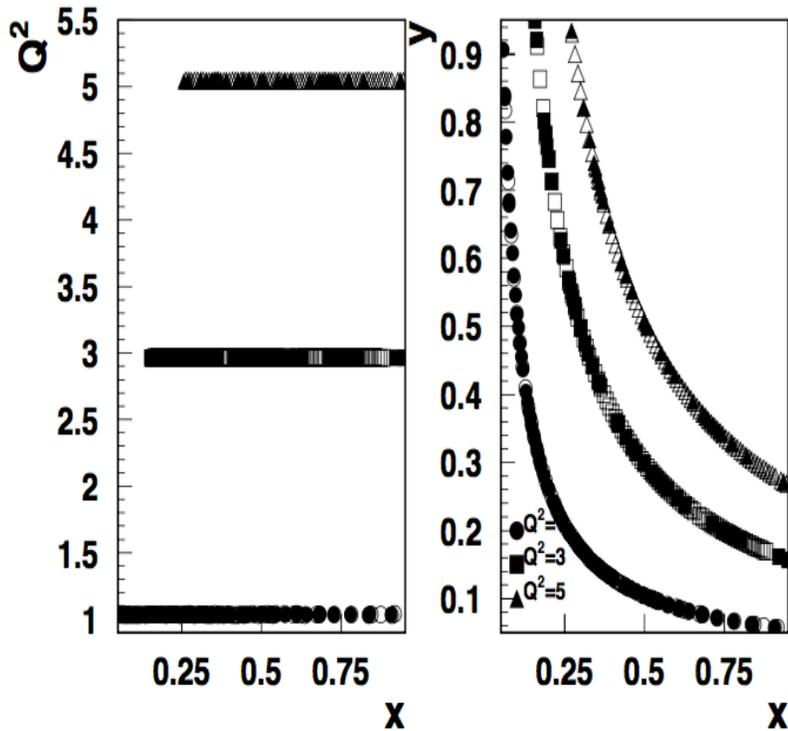
$$1 + R = \frac{(1 + \gamma^2) F_2}{2x F_1}$$



Consistent in kinematics,
where HT are not significant

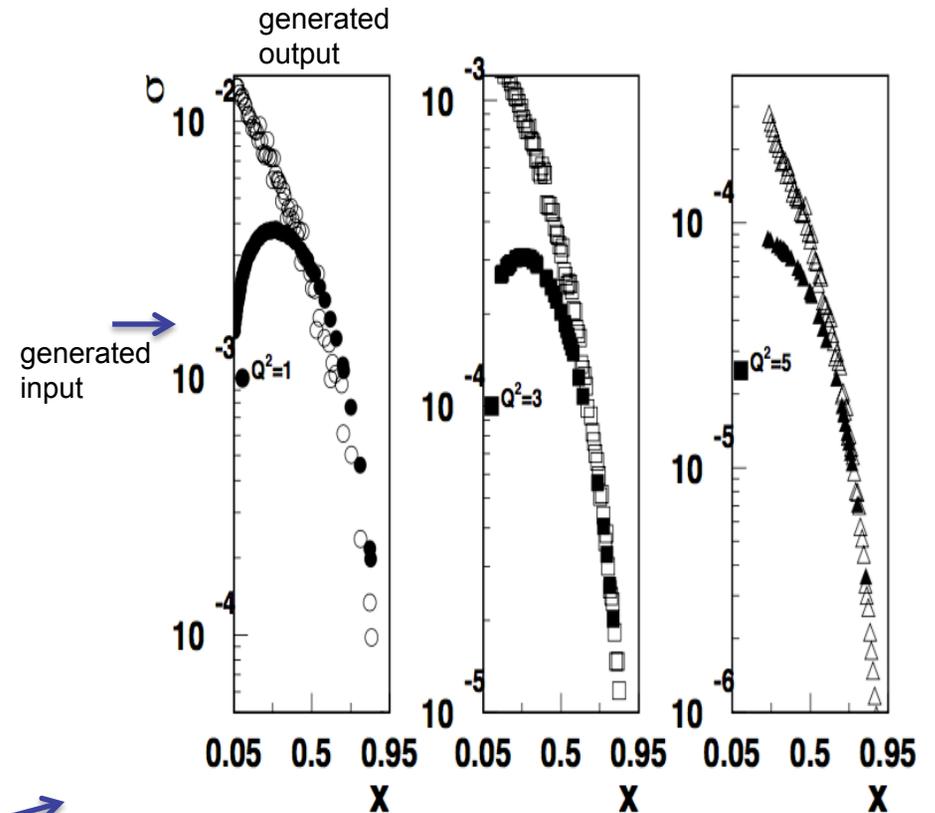
- Different Q^2 -dependent factors contribute.
- Separation is important for DIS, but will be critical for SIDIS

Comparing generated output with input



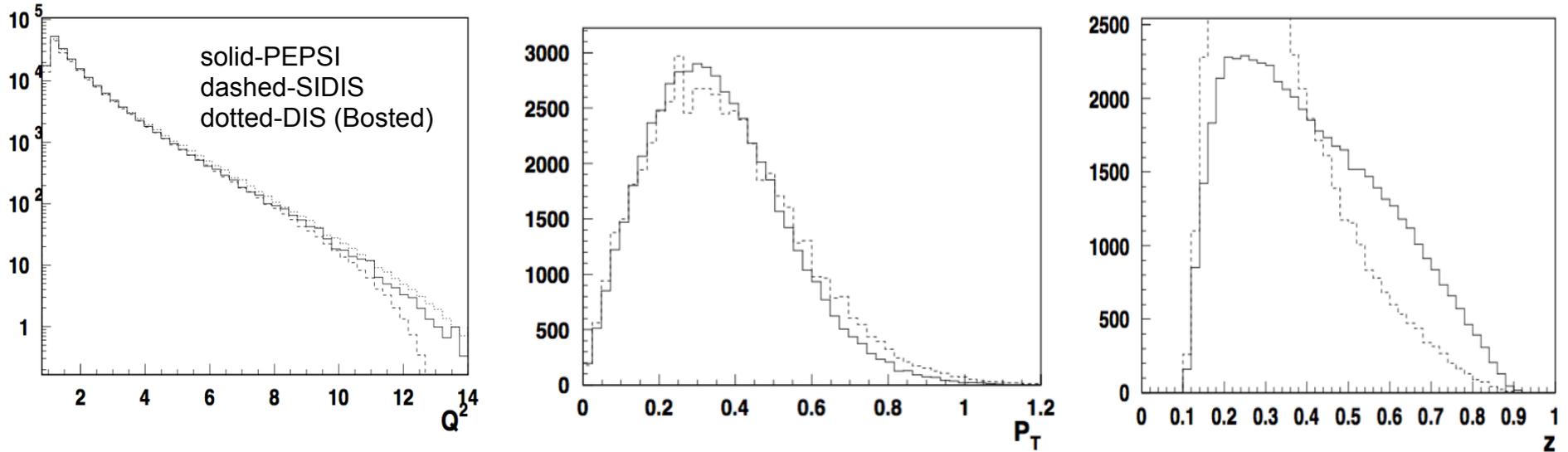
compare 3 bins in Q^2
average values agree

using x-section generator in x/y



Even with uniform distribution in x , the generated distribution is not uniform and depends on initial cuts on electron angle and energy

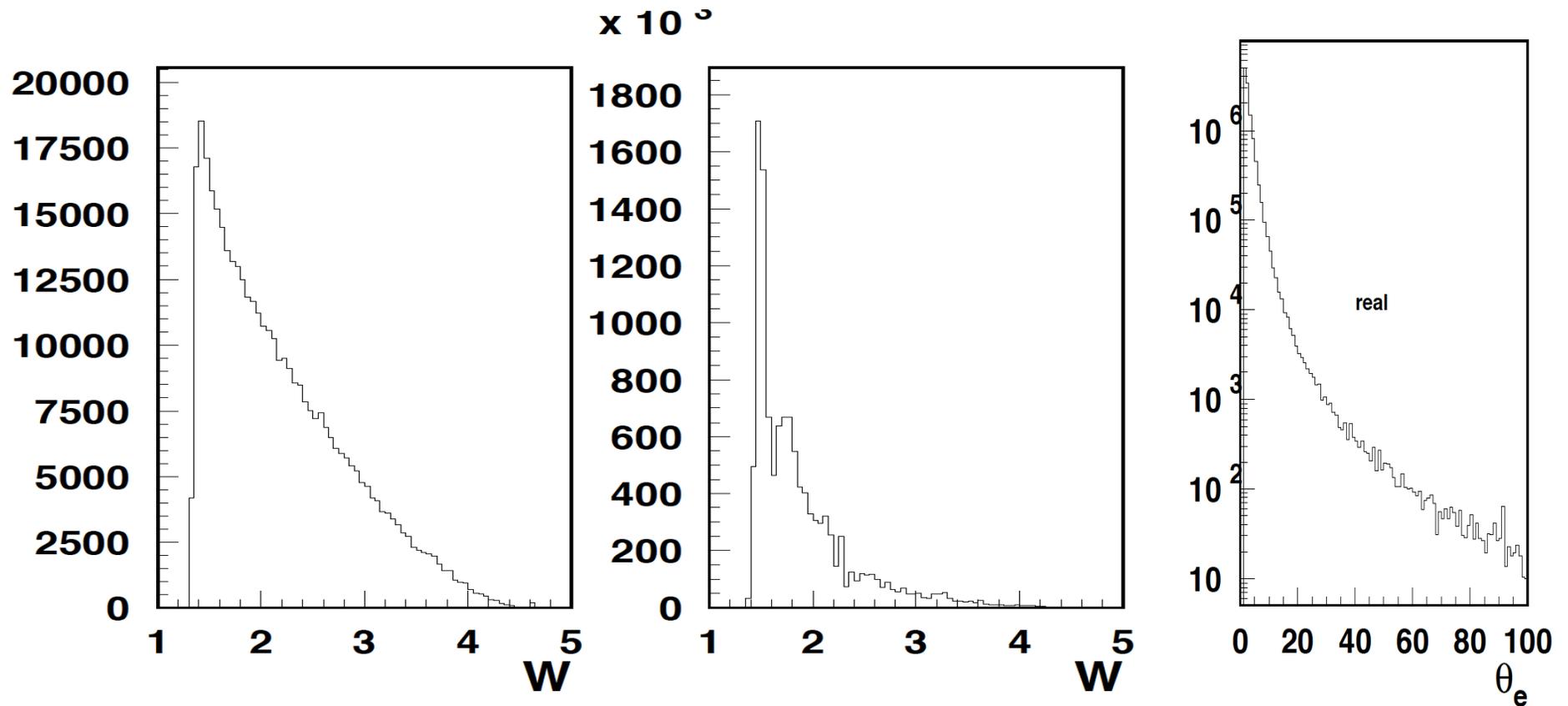
Kinematic distributions



$e\pi X$ evnts compared with $e\pi X$ events from PYTHIA tuned to data

Simple event generator should be “reasonable”

DIS generator



CLAS12-MC vs theory: defining variables

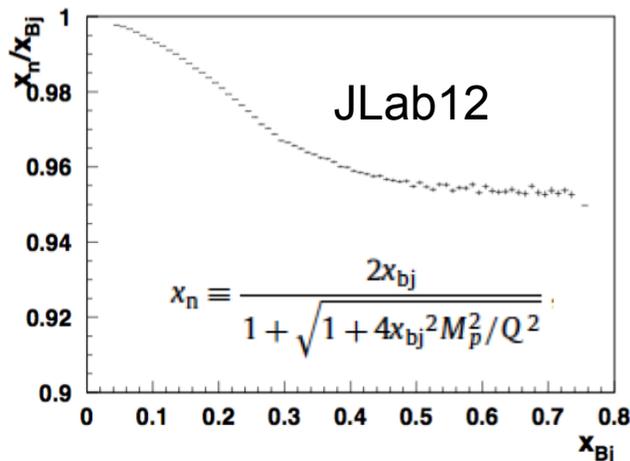
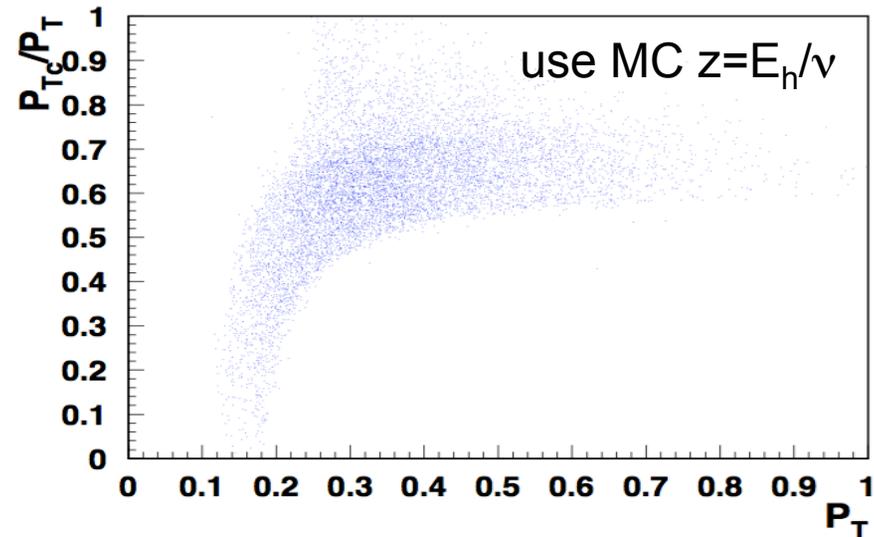
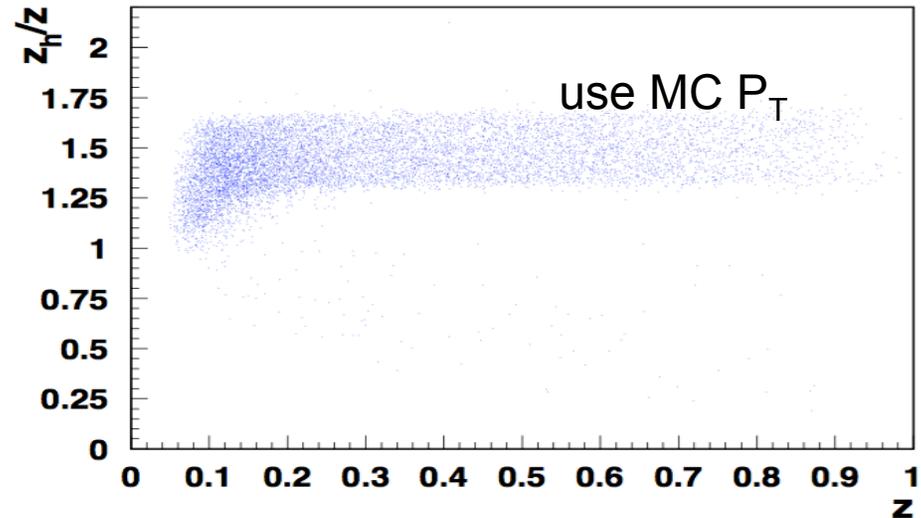
Boglione et al. $M_{hT} \equiv \sqrt{P_{hT}^2 + M_h^2}$

$$z_h = \frac{M_{hT}}{Q} \left(1 - x_n^2 \frac{M_p^2}{Q^2} \right)^{-1} \left(e^{-y_h} + x_n^2 \frac{M_p^2}{Q^2} e^{y_h} \right)$$

$$P_{Tc} = Q \sqrt{\frac{z_h^2 e^{2y_h} (1 - x_n^2 M_p^2 / Q^2)^2}{(1 + e^{2y_h} x_n^2 M_p^2 / Q^2)^2} - \frac{M_h^2}{Q^2}}$$

$$z = (P_h P) / (q P) = E_h / \nu$$

$$x = Q^2 / 2(q P)$$



Consistency check for z and P_T

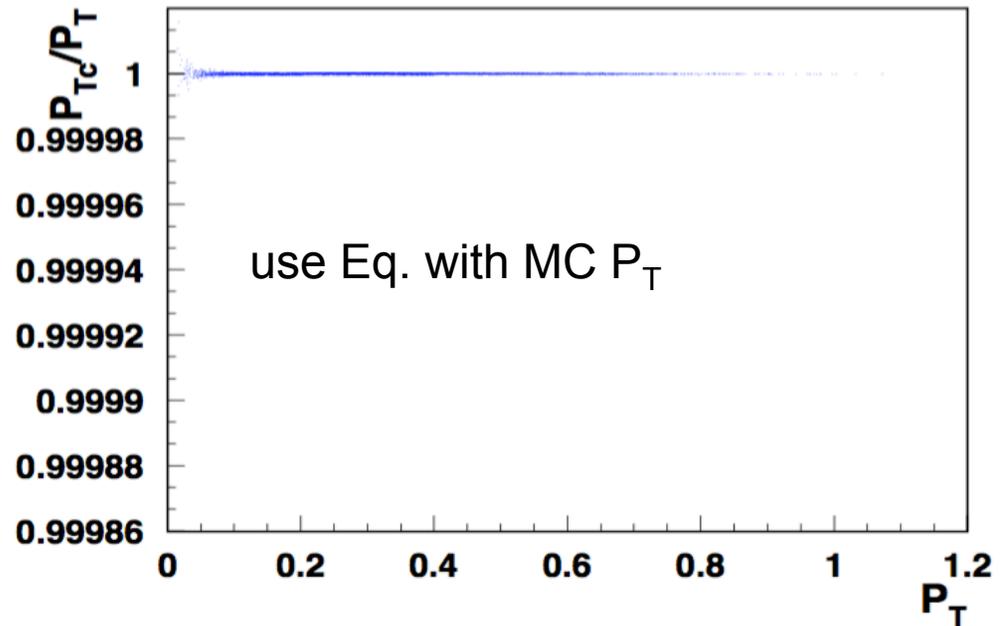
Boglione et al. $M_{hT} \equiv \sqrt{P_{hT}^2 + M_h^2}$.

$$z_h = \frac{M_{hT}}{Q} \left(1 - x_n^2 \frac{M_p^2}{Q^2} \right)^{-1} \left(e^{-y_h} + x_n^2 \frac{M_p^2}{Q^2} e^{y_h} \right)$$

$$P_T = Q \sqrt{\frac{z_h^2 e^{2y_h} \left(1 - x_n^2 \frac{M_p^2}{Q^2} \right)^2}{\left(1 + e^{2y_h} x_n^2 \frac{M_p^2}{Q^2} \right)^2} - \frac{M_h^2}{Q^2}}$$

$$x = Q^2 / 2(qP)$$

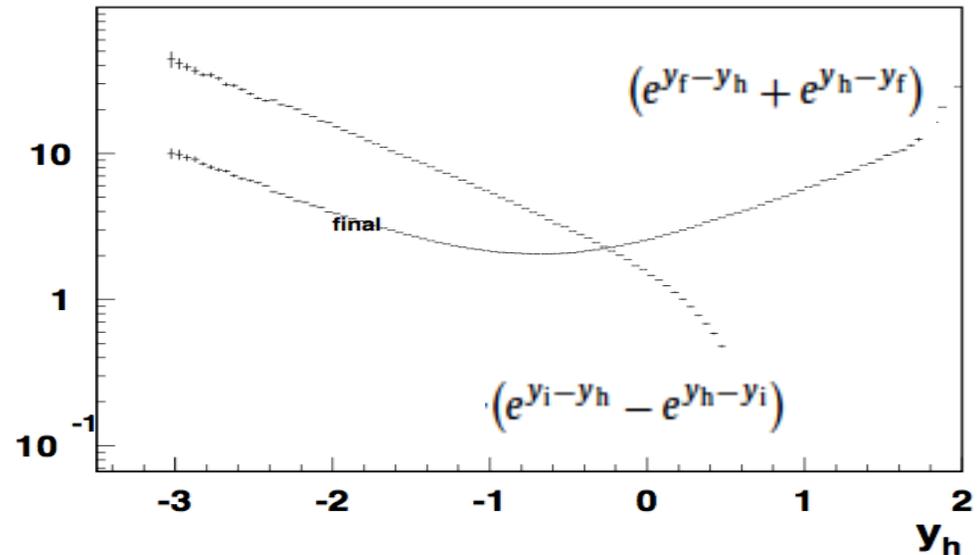
$$z = (P_h P) / (qP) = E_h / \nu$$



$$P_h \cdot k_f = \frac{1}{2} M_{hT} M_{fT} (e^{y_f - y_h} + e^{y_h - y_f})$$

and

$$P_h \cdot k_i = \frac{1}{2} M_{hT} M_{iT} (e^{y_i - y_h} - e^{y_h - y_i}).$$



$$R(y_h, z_h, x_{bj}, Q) \equiv \frac{P_h \cdot k_f}{P_h \cdot k_i},$$

for which we identify

$R(y_h, z_h, x_{bj}, Q) \ll 1$: collinear to outgoing quark,

$R(y_h, z_h, x_{bj}, Q)^{-1} \ll 1$: collinear to incoming quark.

