

Θ^+ production in photon-nucleon and meson-nucleon reactions

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hep-ph/0310019 (PRD in press),
hep-ph/0310117, hep-ph/0311054

Searching for Pentaquarks

- Light pentaquarks ($qqq\bar{q}s^-$ $q=u,d$)

quark models, $Y=2$ exotics (1960's)

1970-1980's: KN scattering for Z^* (Golowich, PDG 86, ...)

Soliton models: Diakonov, Petrov, Polyakov, Chemtob, Praszalowicz etc

2003: LEPS of Spring-8, first *discovery* of pentaquark, $\Theta^+(1540)$ (PRL 91, 012002)

Confirmed by CLAS, DIANA, SAPHIR, HERMES, etc.

NA49: $\Xi^{*-}(1862)$ – another exotic state

- Heavy pentaquarks ($qqq\bar{q}\bar{Q}$ $q=u,d,s$)

1987: quark models (Lipkin, Gignoux, Silvestre-Brac, Richard, ...)

$$P_{\bar{Q}s} \quad P_{\bar{Q}}$$

1990's: soliton model (Helsinki, Seoul, Syracuse, ...)

Stable against strong decays? (mass < DN , D_sN threshold)

1998: E791 of Fermilab, search for $P_{cs}(2750-2860)$ by weak decays into $\phi\pi p$, K^*Kp (PRL 81, 44):
no evidence

Many works on N^* for crypto-exotic pentaquark states (meson-nucleon quasi-bound states)

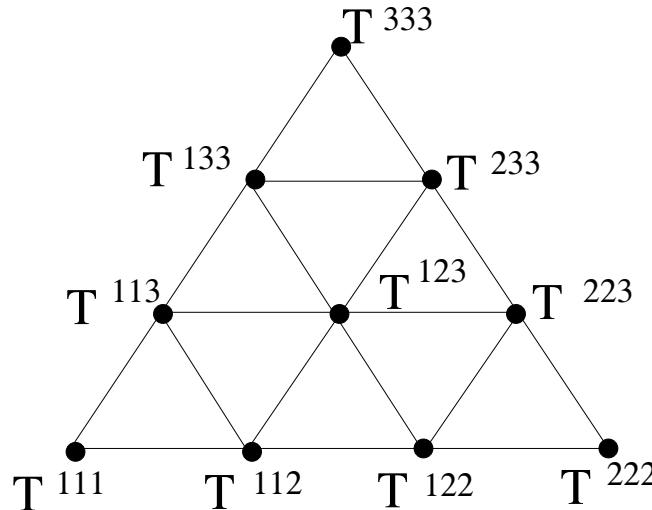
Many calculations in various models

Pentaquark states ($q^4\bar{q}$) in SU(3)

| | Multip. | # | |
|--|--|-----------|--|
| $\square \otimes \square \otimes \square \otimes \square \otimes \begin{array}{ c }\hline \square \\ \hline \square \\ \hline \end{array} =$ | $\begin{array}{ c c c c c }\hline & & & & \\ \hline \end{array}$ | 35 | 1 $I = 2$ Θ and $I = 5/2, 3/2 N^*$ ($J=5/2?$) |
| $\oplus \begin{array}{ c c c c }\hline & & & \\ \hline \end{array}$ | $\begin{array}{ c c c c }\hline & & & \\ \hline \end{array}$ | 27 | 3 $I = 1$ Θ and $I = 3/2, 1/2 N^*$ ($J=3/2?$) |
| $\oplus \begin{array}{ c c c c }\hline & & & \\ \hline \end{array}$ | $\begin{array}{ c c c c }\hline & & & \\ \hline \end{array}$ | 10 | 4 |
| $\oplus \begin{array}{ c c c }\hline & & \\ \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array}$ | $\begin{array}{ c c c }\hline & & \\ \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array}$ | 10 | 2 $I = 0$ Θ and $I = 1/2 N^*$ ($J=1/2?$) |
| $\oplus \begin{array}{ c c c }\hline & & \\ \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array}$ | $\begin{array}{ c c c }\hline & & \\ \hline & & \\ \hline & & \\ \hline & & \\ \hline \end{array}$ | 8 | 8 |
| $\oplus \begin{array}{ c c }\hline & \\ \hline & \\ \hline & \\ \hline & \\ \hline \end{array}$ | $\begin{array}{ c c }\hline & \\ \hline & \\ \hline & \\ \hline & \\ \hline \end{array}$ | 1 | 3 |
| | | | Cf. Θ has $Y=2$, N^* has $Y=1$ |

Skyrmion picture: Walliser +, hep-ph/0304058

Pentaquarks as anti-decuplet



Θ
 N_{10}
 Σ_{10}
 Ξ_{10}

| T^{333} | $Y=2$ | $I=0$ | Θ |
|---|--------|---------|---------------|
| T^{133}, T^{233} | $Y=1$ | $I=1/2$ | N_{10} |
| $T^{113}, T^{123},$ T^{223} | $Y=0$ | $I=1$ | Σ_{10} |
| $T^{111}, T^{112},$ T^{122}, T^{222} | $Y=-1$ | $I=3/2$ | Ξ_{10} |

$\Theta^+(1540)$: observed by LEPS, CLAS, SAPHIR, DIANA, etc

$\Xi_{3/2}^- (1862)$ observed by NA49 and ??

Equal-spacing rule in anti-decuplet from GMO mass formula

mixing with pentaquark octet? N(1440) and N(1710) (?) Jaffe-Wilczek

Cf: N(1440) $\sim \sigma N$ quasi-bound state: Juelich Group in πN scattering,

PRC57,1464 (1998); PRC62,025207 (2000)

SU(3) symmetric Lagrangian

1.Baryon anti-decuplet – meson octet – baryon octet

$$\mathcal{L} = -ig \overline{T^{jkl}} \gamma_5 P_m^j B_n^k \epsilon^{lmn} + \text{h.c.}$$

T : baryon anti-decuplet
P : meson octet
B : baryon octet

2.Baryon anti-decuplet – meson octet – baryon anti-decuplet

$$\mathcal{L} = g' \overline{T^{jkl}} P_m^j T^{mkl}$$

3.Baryon anti-decuplet – meson octet – baryon decuplet

Not allowed since $8 \otimes 10 = 35 \oplus 27 \oplus 10 \oplus 8$. Thus the N_{10} cannot decay into $\pi\Delta$

$$\text{BR}[N(1710) \rightarrow \Delta\pi] = 15\text{-}40\% \text{ (PDG)}$$

U-spin conservation \mapsto the N_{10} can be produced by γn but not by γp



Quantum numbers of the $\Theta^+(1540)$:

- ① $I=0$ if $\Theta(1540)$ belongs to anti-decuplet
- ② Spin? - most models predict $1/2$
- ③ Parity?
 - lattice, QCD sum rules \mapsto odd parity
 - quark models with orbital motion, soliton models
 \mapsto even parity

Soliton models for heavy pentaquark gives

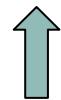
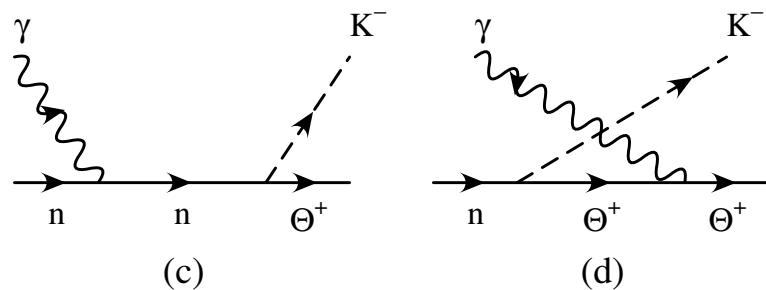
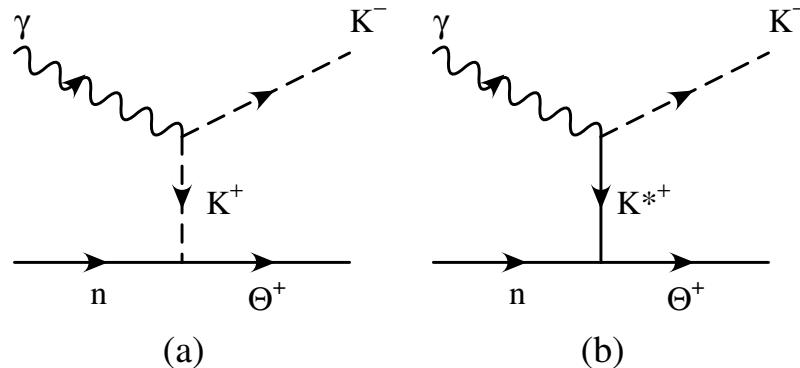
$1/2^+$: ground state

$1/2^-$: first excited state

$I=1,2$: higher states

we first assume $I = 0$ and $J^P = 1/2^+$ for $\Theta^+(1540)$.

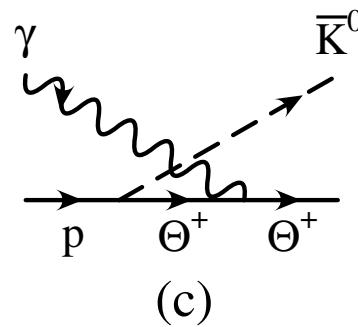
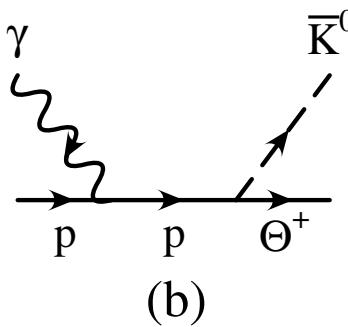
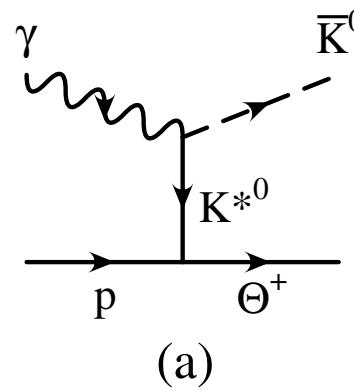
$$\gamma n \mapsto K\Theta$$



$I=0 \& I=1 \Theta^+$

Other resonances: Δ (no), N_{10} (yes), others....

$\gamma p \mapsto K\Theta$



Other resonance: $\Delta(\text{no}), N_{10}(\text{no}), \text{others...}$

Lagrangian

SU(3) Lagrangian for $\bar{10} - 8 - 8$
gives

$$\mathcal{L}_{KN\Theta} = -ig \bar{\Theta} \gamma_5 K^+ n - \bar{\Theta} \gamma_5 K^0 p) + \text{h.c.}$$

$$\mathcal{L}_{K^*N\Theta} = -g_{K^*N\Theta} (\bar{\Theta} \gamma_\mu K^{*+\mu} n - \bar{\Theta} \gamma_\mu K^{*0\mu} p) + \text{h.c.} + (\text{tensor coup.})$$

Other Lagrangian

$$\mathcal{L}_{\gamma KK}, \quad \mathcal{L}_{\gamma NN}, \quad \mathcal{L}_{K^*K\gamma}, \quad \mathcal{L}_{\gamma\Theta\Theta} = -e \bar{\Theta} \left(A_\mu \gamma^\mu - \frac{\kappa_\Theta}{2M_\Theta} \sigma_{\mu\nu} \partial^\nu A^\mu \right) \Theta,$$

$$\mathcal{L}_{\pi NN} = \frac{g_{\pi NN}}{2M_N} \bar{N} \gamma^\mu \gamma_5 \partial_\mu \pi N,$$

$$\mathcal{L}_{K^*K\pi} = -ig_{K^*K\pi} (\bar{K} \partial^\mu \pi K_\mu^* - \partial^\mu \bar{K} \pi K_\mu^*) + \text{h.c.}$$

Coupling constants

Coupling constants

$g_{KN\Theta}$: can be determined from $\Gamma(\Theta)$

expt. upper bound: **9-25 MeV**

chiral soliton model: **5-15 MeV** (Polyakov +, Diakonov +)

KN scattering analyses: a few (~ 5) MeV or even less (Nussinov, Arndt +, ...)

we do not try to fix this coupling and set $g_{KN\Theta} = 1$ ($\Gamma(\Theta) \sim 1$ MeV)

leaving its determination to near future expt.

$g_{K^*N\Theta}$: unknown and cannot be inferred from $\Gamma(\Theta)$

some estimate based on several assumptions (not suppressed)

we give the results by varying $g_{K^*N\Theta}/g_{KN\Theta}$

κ_Θ : anomalous magnetic moment of the Θ

depends on the model for the pentaquark structure **-0.9~+0.3 (?)**

we take $\kappa_\Theta=0$ (the results are *not so much dependent* on κ_Θ in the above range)

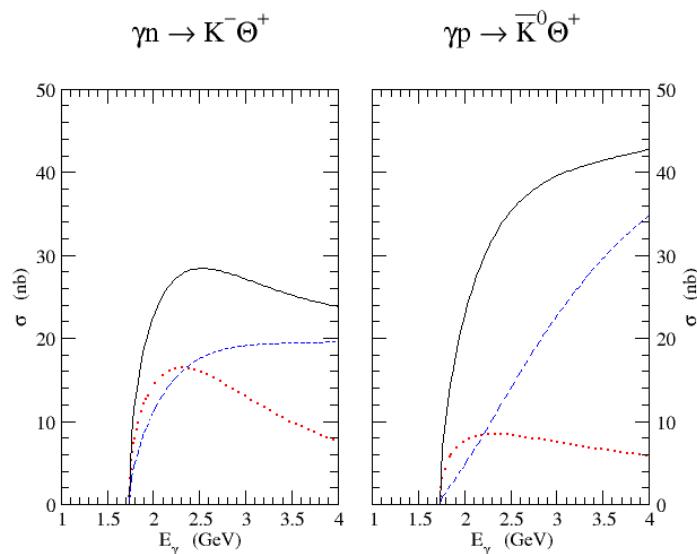
Form factors

$$F(r, M_{\text{ex}}) = \frac{\Lambda^4}{\Lambda^4 + (r - M_{\text{ex}}^2)^2}$$

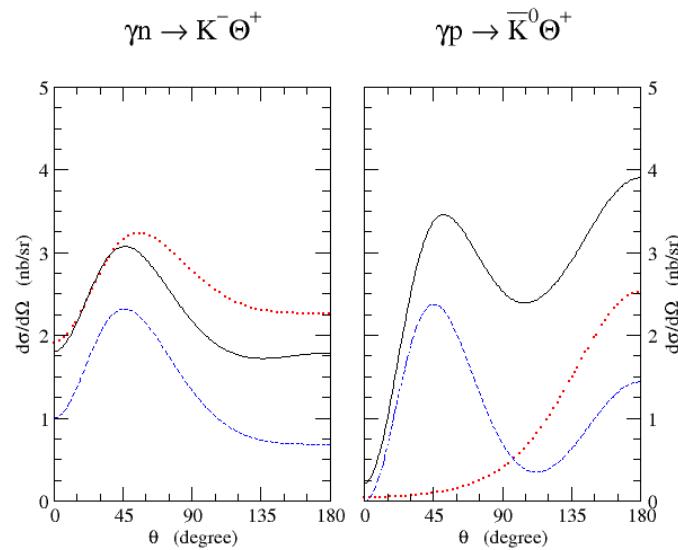
$\Lambda = 1.8$ GeV from kaon photonproduction
1.2 GeV from πN scattering
(Janssen et al., Giessen group)

$\gamma N \rightarrow K\Theta$ (results)

Total cross sections

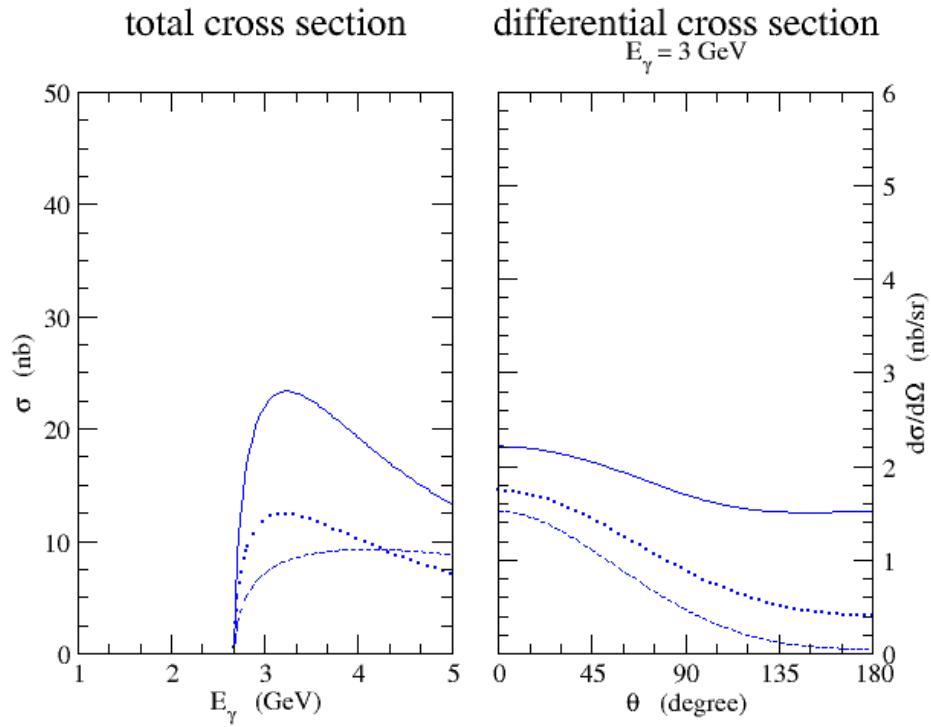
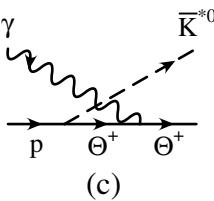
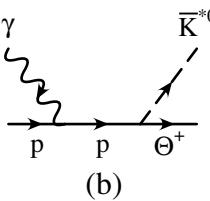
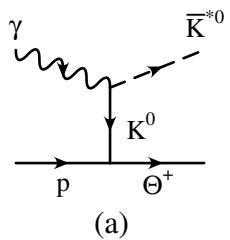


Diff. cross sections at $E_\gamma = 2.5$ GeV



- $g_{K^*N\Theta} = 0$
- $g_{K^*N\Theta}/g_{KN\Theta} = 0.7$
- - - $g_{K^*N\Theta}/g_{KN\Theta} = -0.7$

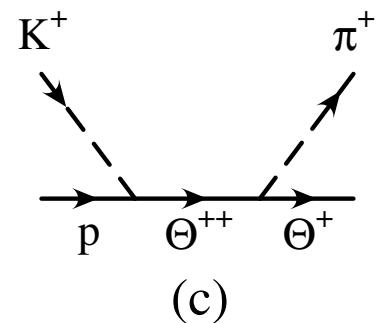
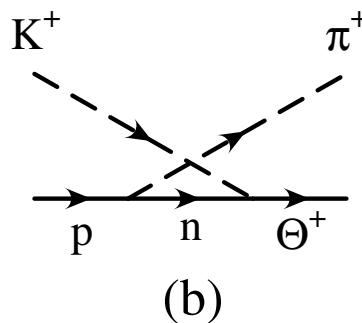
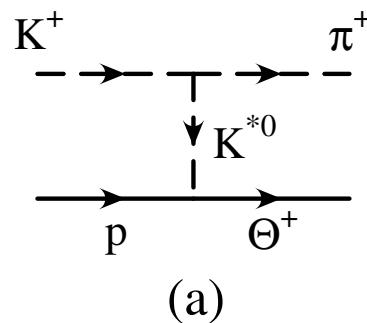
$\gamma N \mapsto K^* \Theta$



Dotted: $g_{K^*N\Theta} = 0$, Solid: $g_{K^*N\Theta}/g_{KN\Theta} = 0.7$,
Dashed: $g_{K^*N\Theta}/g_{KN\Theta} = -0.7$

$$KN \mapsto \pi\Theta$$

$$K^+ p \rightarrow \pi^+ \Theta^+$$

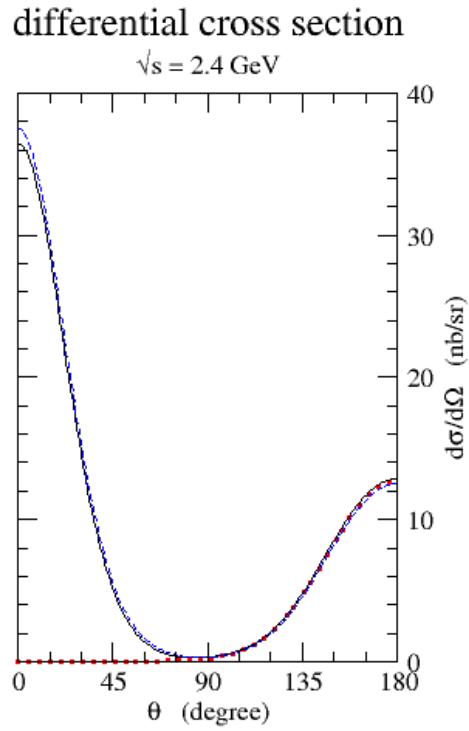
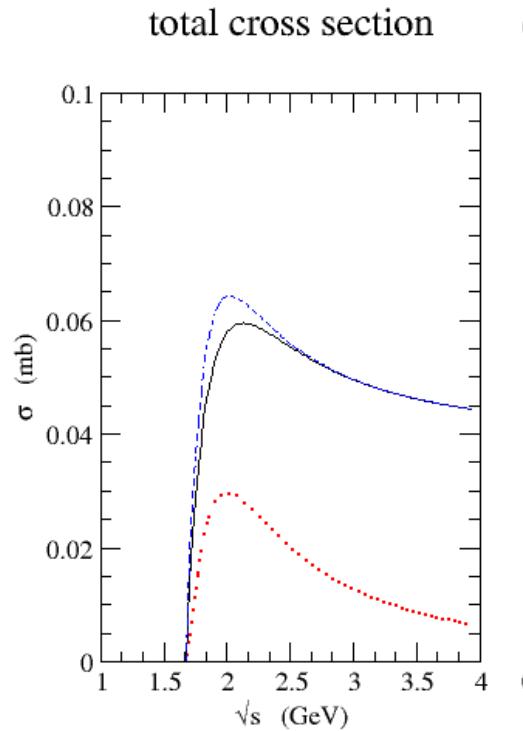


Isospin relation

$$\mathcal{M}_{K^+ p} = -\mathcal{M}_{K^0 n} = -\sqrt{2}\mathcal{M}_{K^0 p} = -\sqrt{2}\mathcal{M}_{K^+ n}$$

Δ (no)

I=1 Θ (yes)
I=2 Θ (no)

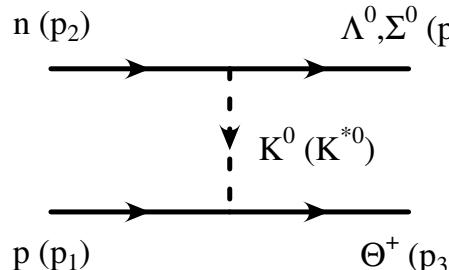


red: $g_{K^*N\Theta} = 0$

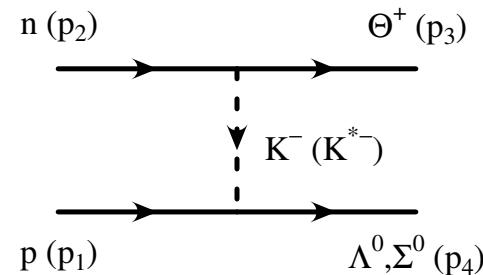
black: $g_{K^*N\Theta}/g_{KN\Theta} = 0.7$

blue: $g_{K^*N\Theta}/g_{KN\Theta} = -0.7$

$NN \mapsto \Lambda\Theta \Sigma\Theta$



(a)



(b)

Isospin relation for $NN \mapsto \Sigma\Theta$

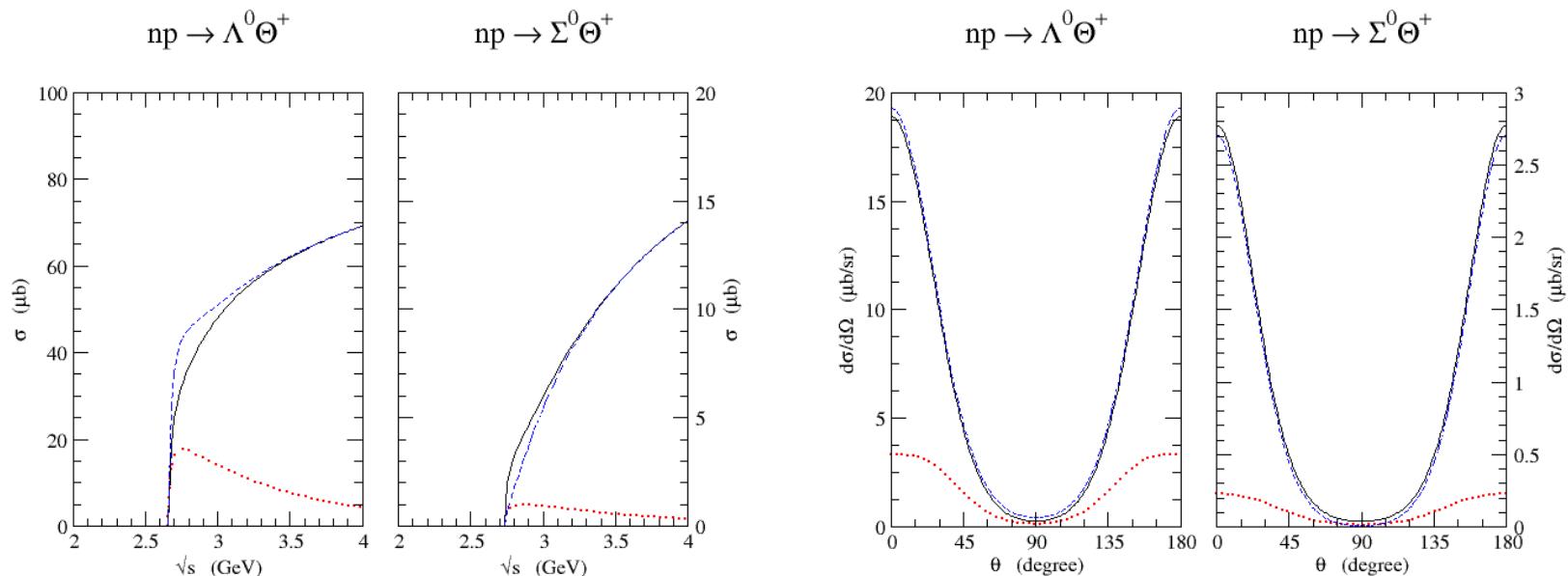
$$\mathcal{M}_{pp} = -\mathcal{M}_{nn} = -\sqrt{2}\mathcal{M}_{np}$$

SU(3) symmetry for KNY couplings

$$g_{KN\Lambda}/\sqrt{4\pi} \sim -3.7, \quad g_{KN\Sigma}/\sqrt{4\pi} \sim 1.0$$

Nijmegen potential (1999) for K^*NY couplings

$$np \mapsto \Lambda^0 \Theta^+, \Sigma^0 \Theta^+$$



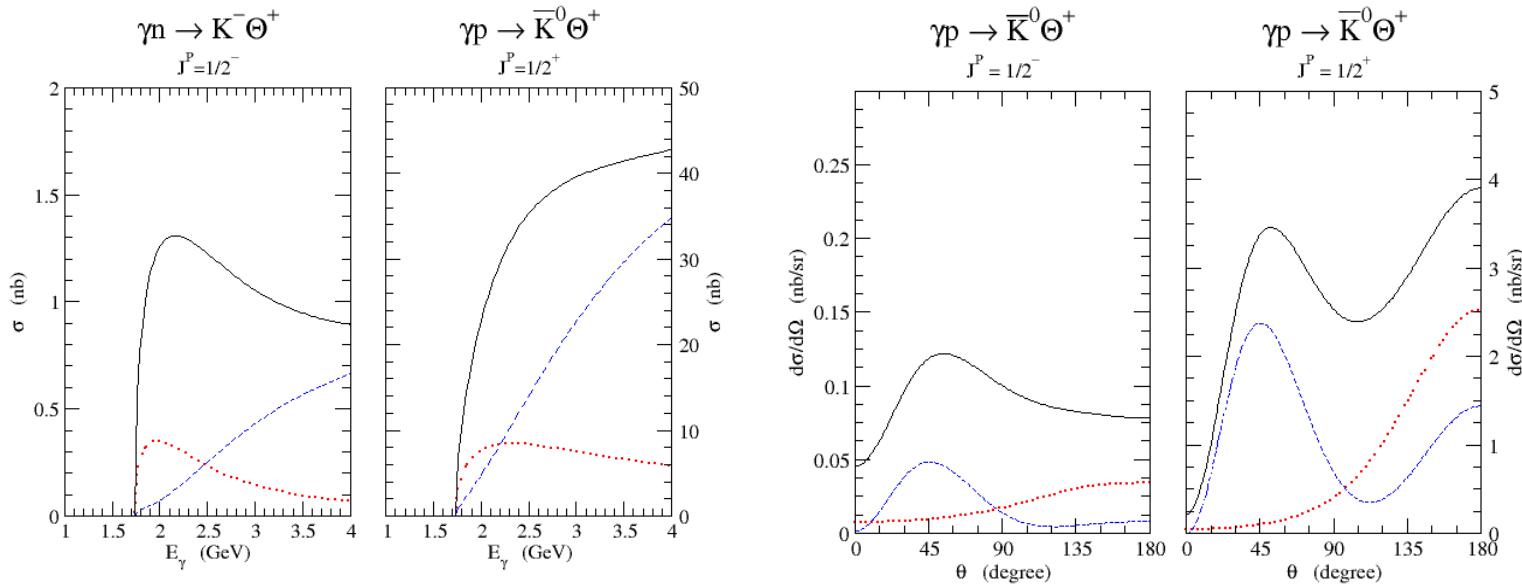
red: $g_{K^*N\Theta} = 0$

black: $g_{K^*N\Theta}/g_{KN\Theta} = 0.7$

blue: $g_{K^*N\Theta}/g_{KN\Theta} = -0.7$

Summary

- Exploratory study on $\Theta^+(1540)$ production in γN , KN (πN), and NN reactions
- N^* contribution? Spin asymmetries?
- Other reactions with other final states? [Liu & Ko, PRC68, nucl-th/0309023,0310087](#)
- Other Θ particles? Quantum numbers?
- Total and diff. cross sections at $E_\gamma = 2.5$ GeV for odd-parity $\Theta^+(1540)$



red: $g_{K^*N\Theta} = 0$

black: $g_{K^*N\Theta}/g_{KN\Theta} = 0.7$

blue: $g_{K^*N\Theta}/g_{KN\Theta} = -0.7$