



Introduction to Quantum Chromodynamics (QCD)

Jianwei Qiu Theory Center, Jefferson Lab May 29 – June 15, 2018

Lecture One



The plan for my four lectures

☐ The Goal:

To understand the strong interaction dynamics in terms of Quantum Chromo-dynamics (QCD), and to prepare you for upcoming lectures in this school

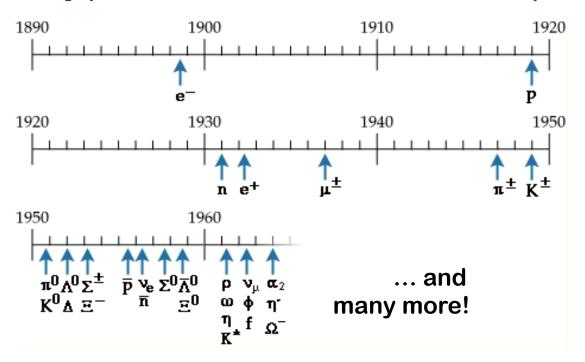
☐ The Plan (approximately):

From the discovery of hadrons to models, and to theory of QCD, Fundamentals of QCD,

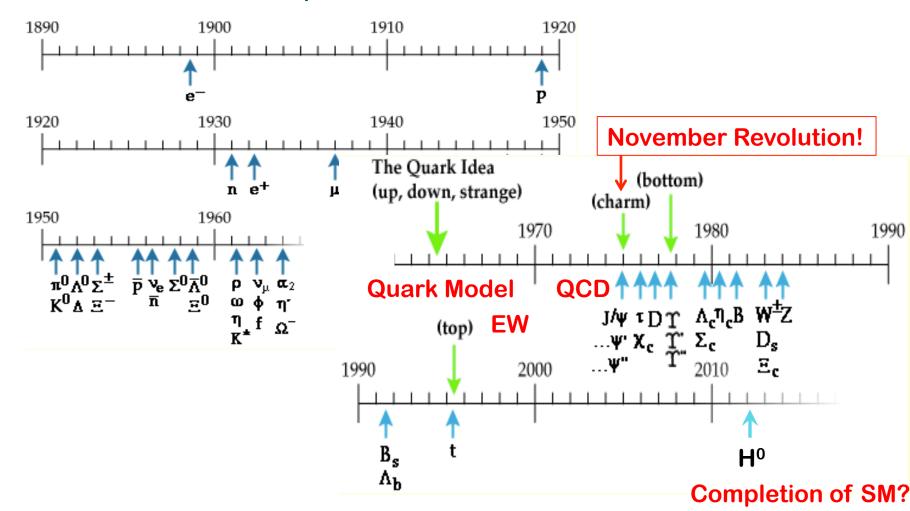
How to probe quarks/gluons without being able to see them? Factorization, Evolution, and Elementary hard processes

Hadron properties (mass, spin, ...) and structures in QCD
Uniqueness of lepton-hadron scattering
From JLab12 to the Electron-Ion Collider (EIC)

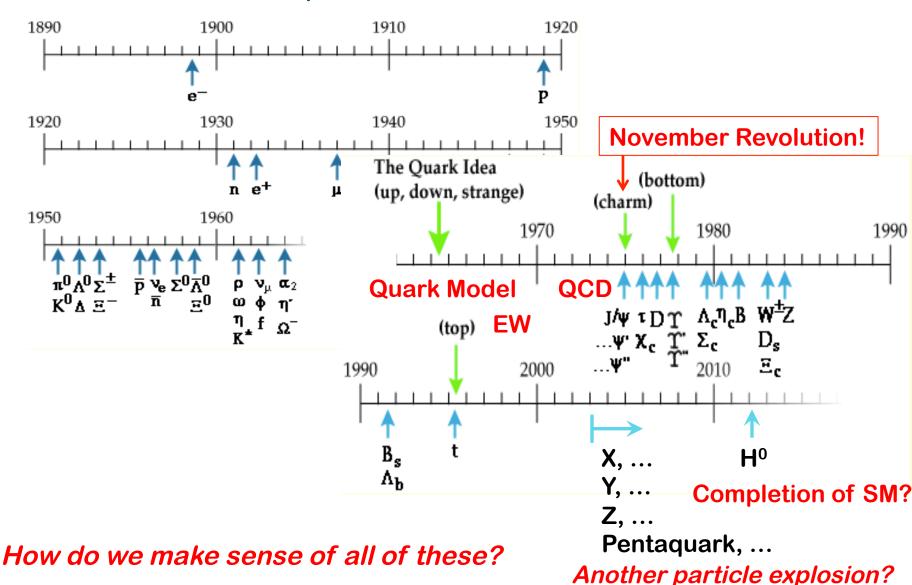
☐ Early proliferation of new hadrons – "particle explosion":



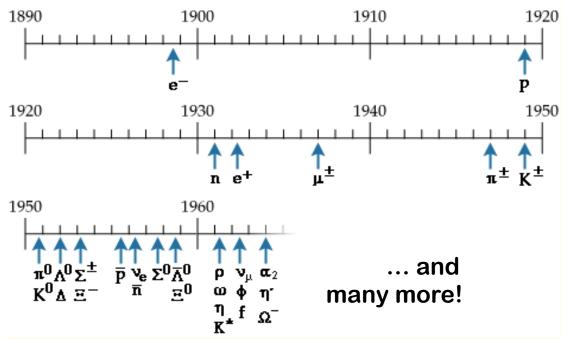
□ Proliferation of new particles – "November Revolution":



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□ Early proliferation of new hadrons – "particle explosion":



Nucleons has internal structure!

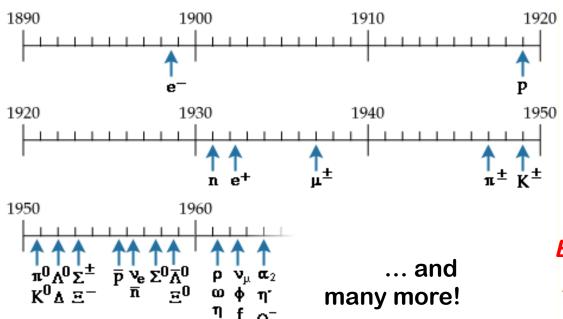
1933: Proton's magnetic moment



Otto Stern
Nobel Prize 1943

$$\mu_p = g_p \left(\frac{e\hbar}{2m_p}\right)$$
 $g_p = 2.792847356(23) \neq 2!$
 $\mu_n = -1.913 \left(\frac{e\hbar}{2m_p}\right) \neq 0!$

☐ Early proliferation of new hadrons – "particle explosion":

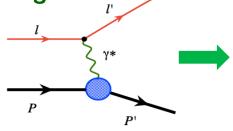


☐ Nucleons has internal structure!

1960: Elastic e-p scattering

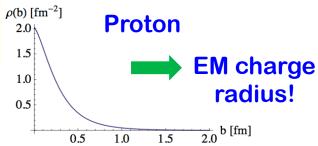


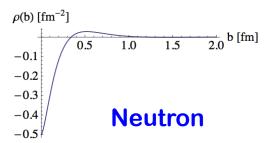
Robert Hofstadter
Nobel Prize 1961



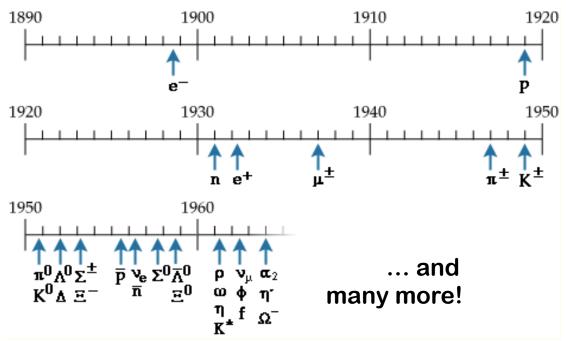
Form factors

Electric charge distribution





☐ Early proliferation of new particles – "particle explosion":

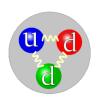


■ Nucleons are made of quarks!

Proton



Neutron





Quark Model





Murray Gell-Mann Nobel Prize, 1969

The naïve Quark Model

☐ Flavor SU(3) – assumption:

Physical states for u, d, s, neglecting any mass difference, are represented by 3-eigenstates of the fund'l rep'n of flavor SU(3)

 \Box Generators for the fund'l rep'n of SU(3) – 3x3 matrices:

$$J_i = \frac{\lambda_i}{2}$$
 with $\lambda_i, i = 1, 2, ..., 8$ Gell-Mann matrices

Good quantum numbers to label the states:

$$J_3 = \frac{1}{2} \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 0 \end{pmatrix} \quad J_8 = \frac{1}{2\sqrt{3}} \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -2 \end{pmatrix} \qquad \begin{array}{c} \text{simultaneously} \\ \text{diagonalized} \end{array}$$

Isospin: $\hat{I}_3 \equiv J_3$, Hypercharge: $\hat{Y} \equiv \frac{2}{\sqrt{2}}J_8$

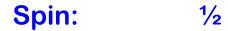
Basis vectors – Eigenstates: $|I_3, Y\rangle$

$$v^{1} \equiv \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix} \Longrightarrow u = \left| \frac{1}{2}, \frac{1}{3} \right\rangle \qquad v^{2} \equiv \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} \Longrightarrow d = \left| -\frac{1}{2}, \frac{1}{3} \right\rangle \quad v^{3} \equiv \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \Longrightarrow s = \left| 0, -\frac{2}{3} \right\rangle$$

The naïve Quark Model

■ Quark states:

$$u = |\frac{1}{2}, \frac{1}{3}\rangle$$
 $d = |-\frac{1}{2}, \frac{1}{3}\rangle$ $s = |0, -\frac{2}{3}\rangle$



Baryon #: $B = \frac{1}{3}$

Strangeness: S = Y - B Electric charge: $Q \equiv I_3 + \frac{Y}{2}$

$$u \begin{cases} Q = 2/3 e \\ s = 1/2 \\ I_3 = 1 \\ Y = 1/3 \\ B = 1/3 \\ S = 0 \end{cases}$$

$$u \begin{cases} Q = 2/3 e \\ s = 1/2 \\ I_3 = 1 \\ Y = 1/3 \\ B = 1/3 \\ S = 0 \end{cases} \qquad d \begin{cases} Q = -1/3 e \\ s = 1/2 \\ I_3 = -1 \\ Y = 1/3 \\ B = 1/3 \\ S = 0 \end{cases} \qquad s \begin{cases} Q = -1/3 e \\ s = 1/2 \\ I_3 = 0 \\ Y = -2/3 \\ B = 1/3 \\ S = -1 \end{cases}$$

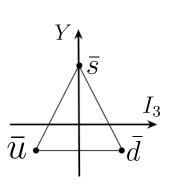
$$\begin{cases}
Q = -1/3 \\
s = 1/2 \\
I_3 = 0 \\
Y = -2/3 \\
B = 1/3 \\
S = -1
\end{cases}$$

\Box Antiquark states: $v_i \equiv \epsilon_{ijk} v^j v^k$

$$\hat{I}_{3}v_{1} = \epsilon_{123}[(\hat{I}_{3}v^{2})v^{3} + v^{2}(\hat{I}_{3}v^{3})] + \epsilon_{132}[(\hat{I}_{3}v^{3})v^{2} + v^{3}(\hat{I}_{3}v^{2})] = -\frac{1}{2}v_{1}$$

$$\hat{Y}v_{1} = \epsilon_{123}[(\hat{Y}v^{2})v^{3} + v^{2}(\hat{Y}v^{3})] + \epsilon_{132}[(\hat{Y}v^{3})v^{2} + v^{3}(\hat{Y}v^{2})] = -\frac{1}{3}v_{1}$$

$$u \longrightarrow \bar{u} = \left|-\frac{1}{2}, -\frac{1}{3}\right\rangle$$



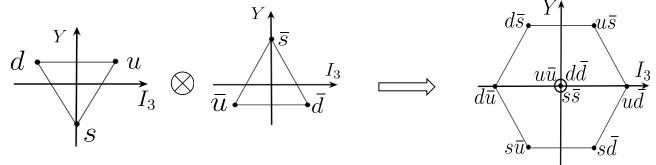
Mesons

Quark-antiquark $q\bar{q}$ flavor states: B=0

☐ Group theory says:

$$q(u,d,s) = \mathbf{3}, \quad \bar{q}(\bar{u},\bar{d},\bar{s}) = \mathbf{\bar{3}}, \quad \text{of flavor SU(3)}$$

$$3\otimes ar{3}=8\oplus 1$$
 \Longrightarrow 1 flavor singlet + 8 flavor octet states



There are three states with $I_3=0, Y=0$: $u\bar{u}, d\bar{d}, s\bar{s}$

☐ Physical meson states (L=0, S=0):

Quantum Numbers

■ Meson states:

$$J^{PC}$$

$$\diamond$$
 Spin of $q \bar{q}$ pair:

$$\vec{S} = \vec{s}_q + \vec{s}_{\bar{q}} \rightarrow S = 0, 1$$

$$J = S + L$$

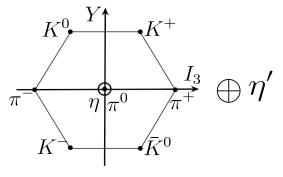
$$P = -(-1)^L$$

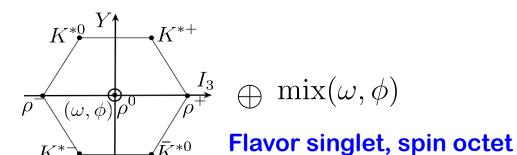
$$C = (-1)^{L+S}$$

☐ L=0 states:

$$J^{PC} = 0^{-+} : (Y=S)$$

$$J^{PC} = 1^{--}$$
: (Y=S)





☐ Color:

Flavor octet, spin octet

No color was introduced!

Baryons

3 quark qqq states: B=1

☐ Group theory says:

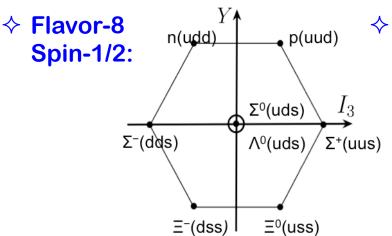
$$\diamond$$
 Flavor: $\mathbf{3} \otimes \mathbf{3} \otimes \mathbf{3} = \mathbf{10}_S \oplus \mathbf{8}_{M_S} \oplus \mathbf{8}_{M_A} \oplus \mathbf{1}_A$

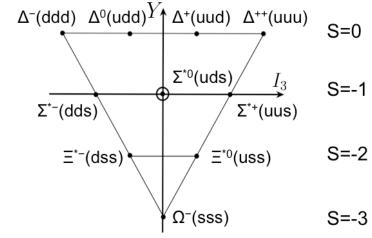
S: symmetric in all 3 q, M_S : symmetric in 1 and 2,

 M_A : antisymmetric in 1 and 2, A: antisymmetric in all 3

$$riangle$$
 Spin: $\mathbf{2}\otimes\mathbf{2}\otimes\mathbf{2}=\mathbf{4}_S\oplus\mathbf{2}_{M_s}\oplus\mathbf{2}_{M_A}\ \Longrightarrow\ S= frac{3}{2}, frac{1}{2}, frac{1}{2}$

☐ Physical baryon states:





Proton



Neutron



∆ ++(uuu), ...

Violation of Pauli exclusive principle



Need another quantum number - color!

Color

- Minimum requirements:
 - Quark needs to carry at least 3 different colors
 - ♦ Color part of the 3-quarks' wave function needs to antisymmetric
- □ SU(3) color:

$$\mathbf{3} \otimes \mathbf{3} \otimes \mathbf{3} = \mathbf{10}_S \oplus \mathbf{8}_{M_S} \oplus \mathbf{8}_{M_A} \oplus \mathbf{1}_A$$

Antisymmetric color singlet state:

$$\implies c(\text{Red, Green, Blue})$$

$$\psi_{\text{Color}}(c_1, c_2, c_3) = \frac{1}{\sqrt{6}} [\text{RGB-GRB+RBG-BRG+GBR-BGR}]$$

□ Baryon wave function:

$$\Psi(q_1, q_2, q_3) = \psi_{\text{Space}}(x_1, x_2, x_3) \otimes \psi_{\text{Flavor}}(f_1, f_2, f_3) \otimes \psi_{\text{Spin}}(s_1, s_2, s_3) \otimes \psi_{\text{Color}}(c_1, c_2, c_3)$$

Antisymmetric Symmetric Symmetric Symmetric Antisymmetric

A complete example: Proton

■ Wave function – the state:

$$|p\uparrow\rangle = \frac{1}{\sqrt{18}} \left[uud(\uparrow\downarrow\uparrow + \downarrow\uparrow\uparrow -2\uparrow\uparrow\downarrow) + udu(\uparrow\uparrow\downarrow + \downarrow\uparrow\uparrow -2\uparrow\downarrow\uparrow) + duu(\uparrow\downarrow\uparrow + \uparrow\uparrow\downarrow -2\downarrow\uparrow\uparrow) \right]$$

■ Normalization:

$$\langle p \uparrow | p \uparrow \rangle = \frac{1}{18} [(1+1+(-2)^2) + (1+1+(-2)^2) + (1+1+(-2)^2)] = 1$$

$$\hat{Q} = \sum_{i=1}^{3} \hat{Q}_i$$

$$\langle p \uparrow | \hat{Q} | p \uparrow \rangle = \frac{1}{18} \left[\left(\frac{2}{3} + \frac{2}{3} - \frac{1}{3} \right) (1 + 1 + (-2)^2) + \left(\frac{2}{3} - \frac{1}{3} + \frac{2}{3} \right) (1 + 1 + (-2)^2) + \left(\frac{1}{3} + \frac{2}{3} + \frac{2}{3} \right) (1 + 1 + (-2)^2) \right] = 1$$

☐ Spin:

Spin:
$$\hat{S} = \sum_{i=1}^{3} \hat{s}_{i}$$

$$\langle p \uparrow | \hat{S} | p \uparrow \rangle = \frac{1}{18} \{ \left[\left(\frac{1}{2} - \frac{1}{2} + \frac{1}{2} \right) + \left(-\frac{1}{2} + \frac{1}{2} + \frac{1}{2} \right) + 4 \left(\frac{1}{2} + \frac{1}{2} - \frac{1}{2} \right) \right]$$

$$+\left[\frac{1}{2} + \frac{1}{2} + 4\frac{1}{2}\right] + \left[\frac{1}{2} + \frac{1}{2} + 4\frac{1}{2}\right] = \frac{1}{2}$$

☐ Magnetic moment:

$$\mu_p = \langle p \uparrow | \sum_{i=1}^{3} \hat{\mu}_i(\hat{\sigma}_3)_i | p \uparrow \rangle = \frac{1}{3} [4\mu_u - \mu_d]$$

Magnetic moment:
$$\mu_{p} = \langle p \uparrow | \sum_{i=1}^{3} \hat{\mu}_{i}(\hat{\sigma}_{3})_{i} | p \uparrow \rangle = \frac{1}{3} [4\mu_{u} - \mu_{d}]$$

$$\mu_{n} = \frac{1}{3} [4\mu_{d} - \mu_{u}]$$

$$\frac{\mu_{u}}{\mu_{d}} \approx \frac{2/3}{-1/3} = -2$$

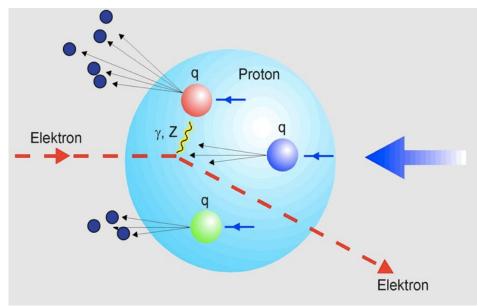
$$\left(\frac{\mu_{n}}{\mu_{p}}\right)_{\text{QM}} = -\frac{2}{3}$$

$$\left(\frac{\mu_{n}}{\mu_{p}}\right)_{\text{Exp}} = -0.68497945(58)$$

How to "see" substructure of a nucleon?

■ Modern Rutherford experiment – Deep Inelastic Scattering:

SLAC 1968:
$$e(p) + h(P) \rightarrow e'(p') + X$$



♦ Localized probe:

$$Q^{2} = -(p - p')^{2} \gg 1 \text{ fm}^{-2}$$

$$\frac{1}{Q} \ll 1 \text{ fm}$$

♦ Two variables:

$$Q^{2} = 4EE' \sin^{2}(\theta/2)$$

$$x_{B} = \frac{Q^{2}}{2m_{N}\nu}$$

$$\nu = E - E'$$

Discovery of spin ½ quarks, and partonic structure!

What holds the quarks together?









Nobel Prize, 1990

– Quark Model + Yang-Mill gauge theory

Quantum Chromo-dynamics (QCD)

= A quantum field theory of quarks and gluons =

☐ Fields:

 $\psi_i^f(x)$ Color triplet: $i=1,2,3=N_c$

f = u, d, s, c, b, tFlavor:

$$A_{\mu,a}(x)$$
 Gluon fields: spin-1 vector field (like photon)

Color octet: $a = 1, 2, ..., 8 = N_c^2 - 1$

QCD Lagrangian density:

$$\mathcal{L}_{QCD}(\psi, A) = \sum_{f} \overline{\psi}_{i}^{f} \left[(i\partial_{\mu}\delta_{ij} - gA_{\mu,a}(t_{a})_{ij})\gamma^{\mu} - m_{f}\delta_{ij} \right] \psi_{j}^{f}$$

$$-\frac{1}{4} \left[\partial_{\mu}A_{\nu,a} - \partial_{\nu}A_{\mu,a} - gC_{abc}A_{\mu,b}A_{\nu,c} \right]^{2}$$
+ gauge fixing + ghost terms

QED – force to hold atoms together:

$$\mathcal{L}_{QED}(\phi, A) = \sum_{f} \overline{\psi}^{f} \left[(i\partial_{\mu} - eA_{\mu})\gamma^{\mu} - m_{f} \right] \psi^{f} - \frac{1}{4} \left[\partial_{\mu} A_{\nu} - \partial_{\nu} A_{\mu} \right]^{2}$$

QCD is much richer in dynamics than QED

Gluons are dark, but, interact with themselves, NO free quarks and gluons

Gauge property of QCD

☐ Gauge Invariance:

$$\psi_i(x) \to \psi'_j(x) = U(x)_{ji} \, \psi_i(x)$$

$$A_{\mu}(x) \to A'_{\mu}(x) = U(x) \, A_{\mu}(x) \, U^{-1}(x) + \frac{i}{g} \left[\partial_{\mu} U(x) \right] U^{-1}(x)$$

where
$$A_{\mu}(x)_{ij} \equiv A_{\mu,a}(x)(t_a)_{ij}$$

$$U(x)_{ij} = \left[e^{i\alpha_a(x)t_a}\right]_{ij}$$
 Unitary [det=1, SU(3)]

□ Color matrices:

$$[t_a, t_b] = i C_{abc} t_c$$

Generators for the fundamental representation of SU3 color

☐ Gauge Fixing:

$$\mathcal{L}_{gauge} = -\frac{\lambda}{2} (\partial_{\mu} A_{a}^{\mu}) (\partial_{\nu} A_{a}^{\nu})$$

Allow us to define the gauge field propagator: $v, b \xrightarrow{k} \mu, a$

$$G_{\mu\nu}(k)_{ab} = \frac{\delta_{ab}}{k^2} \left[-g_{\mu\nu} + \frac{k_{\mu}k_{\nu}}{k^2} \left(1 - \frac{1}{\lambda} \right) \right]$$

with $\lambda = 1$ the Feynman gauge

Ghost in QCD

☐ Ghost:

$$\mathcal{L}_{ghost} = (\partial_{\mu} \bar{\eta}_a(x))(\partial^{\mu} \eta_a(x) - g \, C_{abc} \, A_b^{\mu}(x) \, \eta_c(x)$$

so that the optical theorem (hence the unitarity) can be respected

$$2 \text{ Im} \left(\begin{array}{c} + \\ + \\ + \\ \end{array} \right) + \cdots + \left(\begin{array}{c} + \\ + \\ \end{array} \right)$$

$$= \sum_{\text{Sum over all physical polarizations}} \left| \begin{array}{c} 2 \\ \\ \end{array} \right|$$
Fail without the ghost loop

Feynman rules in QCD

□ Propagators:

Quark:

$$j \longrightarrow k$$

$$\frac{i}{\gamma \cdot k - m} \, \delta_{ij}$$

Gluon:

$$\nu, b \sim \mu, a$$

$$\frac{i\delta_{ab}}{k^2} \left[-g_{\mu\nu} + \frac{k_{\mu}k_{\nu}}{k^2} \left(1 - \frac{1}{\lambda} \right) \right]$$

for a covariant gauge

$$\frac{i\delta_{ab}}{k^2} \left[-g_{\mu\nu} + \frac{k_{\mu}n_{\nu} + n_{\mu}k_{\nu}}{k \cdot n} \right]$$

for a light-cone gauge

$$n \cdot A(x) = 0$$
 with $n^2 = 0$

$$\nu, b = - - \mu, a$$

$$\frac{i\delta_{ab}}{k^2}$$

Feynman rules in QCD

■ Interactions:

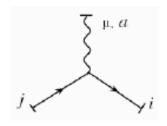
$$-g\bar{\psi}\gamma^{\mu}A_{\mu,a}t_a\psi$$

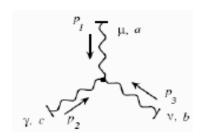
$$rac{1}{2}gC_{abc}(\partial_{\mu}A_{
u,a}\ -\partial_{
u}A_{\mu,a})A^{\mu}_{b}A^{
u}_{c}$$

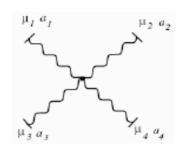
$$-\frac{g^2}{4}C_{abc}C_{ab'c'}$$

$$* A_b^{\mu}A_c^{\nu}A_{\mu,b'}A_{\nu,c'}$$

$$\partial_{\mu}\bar{\eta}_{a}\left(gC_{abc}A_{b}^{\mu}\right)\eta_{c}$$







$$\begin{array}{c}
 & \downarrow \\
 & \downarrow \\$$

$$-ig(t_a)_{ij}\gamma_{\mu}$$

$$-gC_{abc} [g_{\mu\nu}(p_1 - p_2)_{\gamma} + g_{\nu\gamma}(p_2 - p_3)_{\mu} + g_{\gamma\mu}(p_3 - p_1)_{\nu}]$$

$$-ig^{2} [C_{ea_{1}a_{2}}C_{ea_{3}a_{4}}$$

$$* (g_{\mu_{1}\mu_{3}}g_{\mu_{2}\mu_{4}}$$

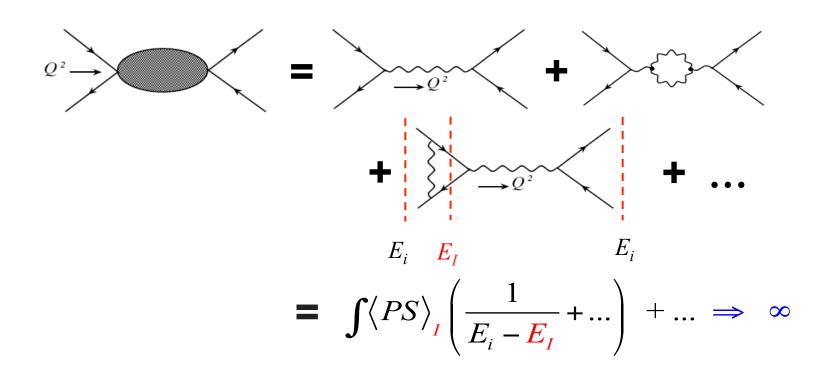
$$- g_{\mu_{1}\mu_{4}}g_{\mu_{2}\mu_{3}})$$

$$+ ...]$$

$$gC_{abc}k_{\mu}$$

Renormalization, why need?

☐ Scattering amplitude:



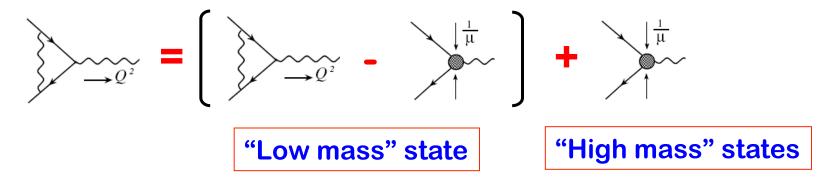
UV divergence: result of a "sum" over states of high masses

Uncertainty principle: High mass states = "Local" interactions

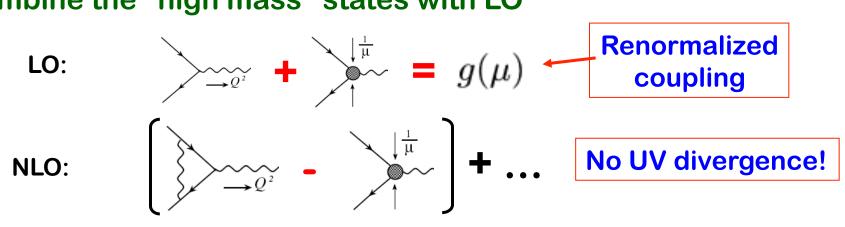
No experiment has an infinite resolution!

Physics of renormalization

□ UV divergence due to "high mass" states, not observed



☐ Combine the "high mass" states with LO



□ Renormalization = re-parameterization of the expansion parameter in perturbation theory

Renormalization Group

□ Physical quantity should not depend on renormalization scale μ renormalization group equation:

$$\mu^2 \frac{d}{d\mu^2} \, \sigma_{\text{Phy}} \left(\frac{Q^2}{\mu^2}, g(\mu), \mu \right) = 0 \quad \Longrightarrow \quad \sigma_{\text{Phy}}(Q^2) = \sum_n \hat{\sigma}^{(n)}(Q^2, \mu^2) \left(\frac{\alpha_s(\mu)}{2\pi} \right)^n$$

☐ Running coupling constant:

$$\mu \frac{\partial g(\mu)}{\partial \mu} = \beta(g) \qquad \alpha_s(\mu) = \frac{g^2(\mu)}{4\pi}$$

 \square QCD β function:

$$\beta(g) = \mu \frac{\partial g(\mu)}{\partial \mu} = +g^3 \frac{\beta_1}{16\pi^2} + \mathcal{O}(g^5) \qquad \beta_1 = -\frac{11}{3} N_c + \frac{4}{3} \frac{n_f}{2} < 0 \quad \text{for } n_f \le 6$$

□ QCD running coupling constant:

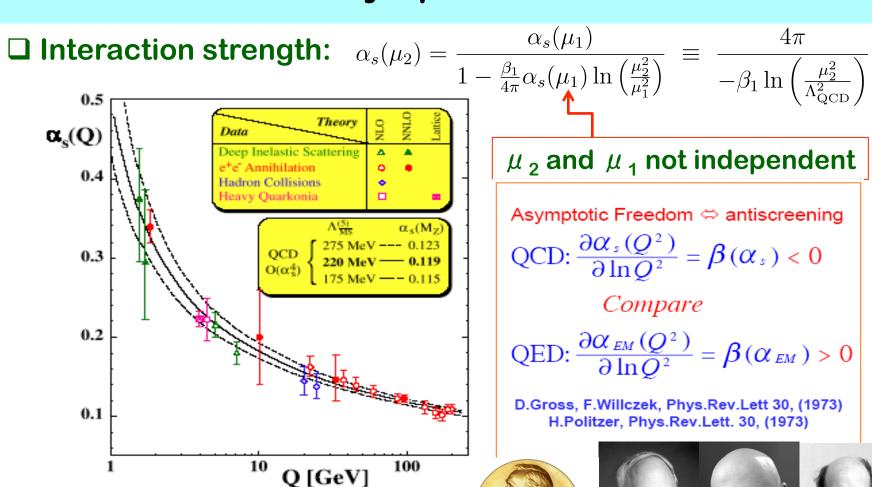
$$\alpha_s(\mu_2) = \frac{\alpha_s(\mu_1)}{1 - \frac{\beta_1}{4\pi}\alpha_s(\mu_1)\ln\left(\frac{\mu_2^2}{\mu_1^2}\right)} \Rightarrow 0 \quad \text{as } \mu_2 \to \infty \quad \text{for } \beta_1 < 0$$
Asymptotic freedom!

QCD Asymptotic Freedom

$$\alpha_s(\mu_2) = -$$

$$\frac{1 - \frac{\beta_1}{4\pi} \alpha_s(\mu_1) \ln\left(\frac{\mu_2^2}{\mu_2^2}\right)}{1 - \frac{\beta_1}{4\pi} \alpha_s(\mu_1) \ln\left(\frac{\mu_2^2}{\mu_2^2}\right)}$$

$$\equiv \frac{4\pi}{-\beta_1 \ln\left(\frac{\mu}{\Lambda_2^2}\right)}$$



μ_2 and μ_1 not independent

Asymptotic Freedom \Leftrightarrow antiscreening

QCD:
$$\frac{\partial \alpha_s(Q^2)}{\partial \ln Q^2} = \beta(\alpha_s) < 0$$

Compare

QED:
$$\frac{\partial \alpha_{\scriptscriptstyle EM}(Q^2)}{\partial \ln Q^2} = \beta(\alpha_{\scriptscriptstyle EM}) > 0$$

D.Gross, F.Willczek, Phys.Rev.Lett 30, (1973) H.Politzer, Phys.Rev.Lett. 30, (1973)





Controllable perturbative QCD calculations



Nobel Prize, 2004

Effective Quark Mass

Ru2nning quark mass:

$$m(\mu_2) = m(\mu_1) \exp \left[-\int_{\mu_1}^{\mu_2} \frac{d\lambda}{\lambda} [1 + \gamma_m(g(\lambda))] \right]$$

Quark mass depend on the renormalization scale!

□ QCD running quark mass:

$$m(\mu_2) \Rightarrow 0$$

as
$$\mu_2 \to \infty$$

$$m(\mu_2) \Rightarrow 0$$
 as $\mu_2 \to \infty$ since $\gamma_m(g(\lambda)) > 0$

Choice of renormalization scale:

$$\mu \sim Q$$

 $\mu \sim Q$ for small logarithms in the perturbative coefficients

$$m_f(\mu) \ll \Lambda_{\rm QCD}$$

$$\Box$$
 Light quark mass: $m_f(\mu) \ll \Lambda_{\rm QCD}$ for $f = u, d$, even s

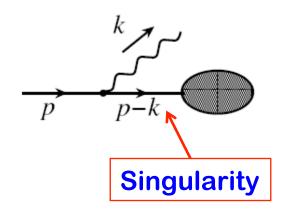
QCD perturbation theory (Q>> \land _{QCD}) is effectively a massless theory

Infrared and collinear divergences

☐ Consider a general diagram:

$$p^2=0, \quad k^2=0 \quad \text{for a massless theory}$$

Infrared (IR) divergence



Collinear (CO) divergence

IR and CO divergences are generic problems of a massless perturbation theory

Infrared Safety

☐ Infrared safety:

$$\sigma_{\text{Phy}}\left(\frac{Q^2}{\mu^2}, \alpha_s(\mu^2), \frac{m^2(\mu^2)}{\mu^2}\right) \Rightarrow \hat{\sigma}\left(\frac{Q^2}{\mu^2}, \alpha_s(\mu^2)\right) + \mathcal{O}\left[\left(\frac{m^2(\mu^2)}{\mu^2}\right)^{\kappa}\right]$$

Infrared safe = $\kappa > 0$

Asymptotic freedom is useful only for quantities that are infrared safe

Foundation of QCD perturbation theory

- □ Renormalization
 - QCD is renormalizable

Nobel Prize, 1999 't Hooft, Veltman

- **☐** Asymptotic freedom
 - weaker interaction at a shorter distance

Nobel Prize, 2004 Gross, Politzer, Welczek

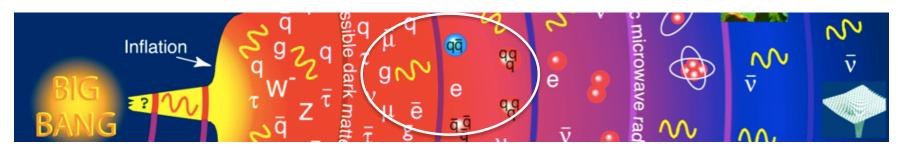
- ☐ Infrared safety and factorization
 - calculable short distance dynamics
 - pQCD factorization connect the partons to physical cross sections

J. J. Sakurai Prize, 2003 Mueller, Sterman

Look for infrared safe and factorizable observables!

QCD is everywhere in our universe

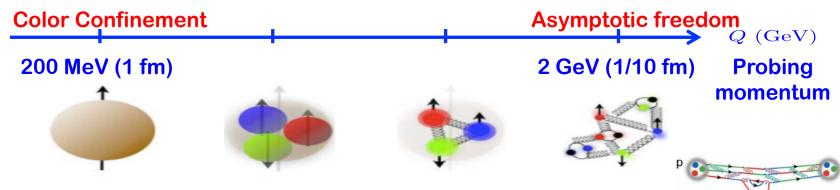
■ What is the role of QCD in the evolution of the universe?



- □ How hadrons are emerged from quarks and gluons?
- ☐ How does QCD make up the properties of hadrons?

Their mass, spin, magnetic moment, ...

■ What is the QCD landscape of nucleon and nuclei?



- ☐ How do the nuclear force arise from QCD?

Backup slides

From Lagrangian to Physical Observables

- ☐ Theorists: Lagrangian = "complete" theory
- ☐ Experimentalists: Cross Section → Observables
- □ A road map from Lagrangian to Cross Section:

