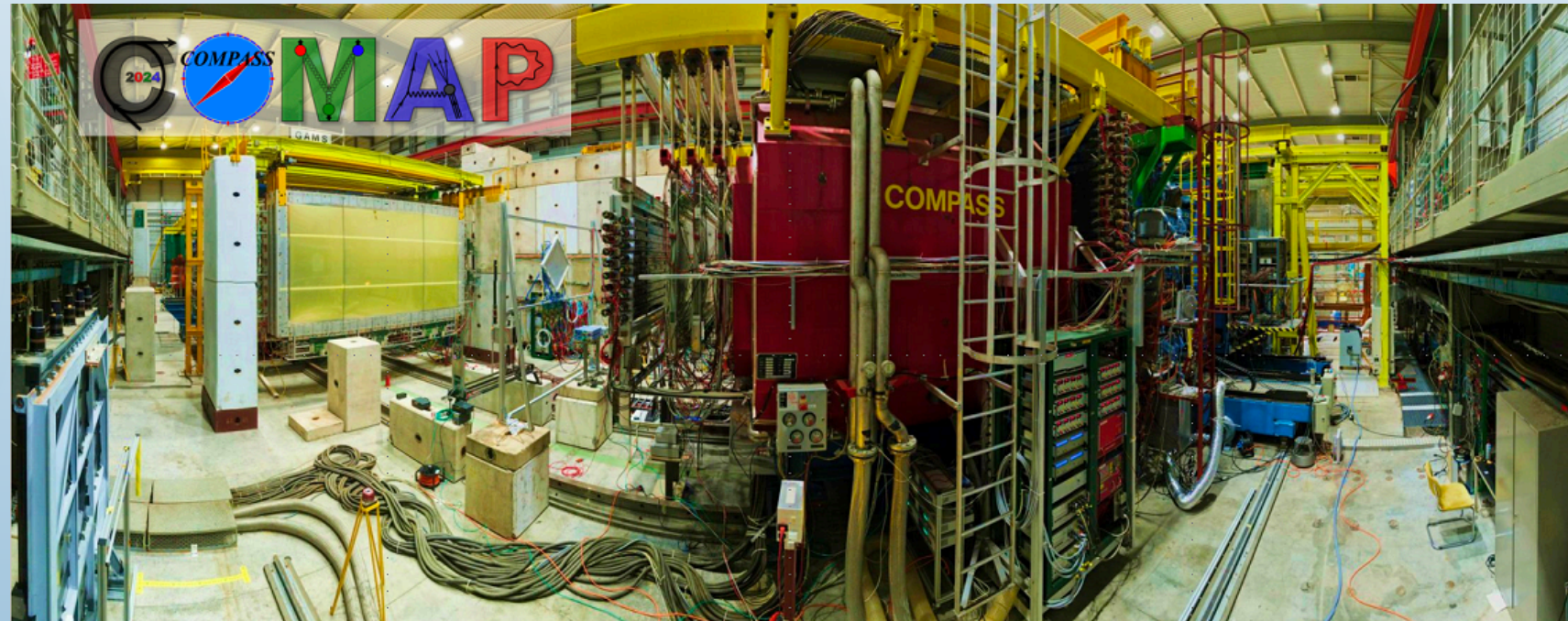


# Recent Updates from the JAM Collaboration on Helicity PDFs

Christopher Cocuzza



January 24, 2024

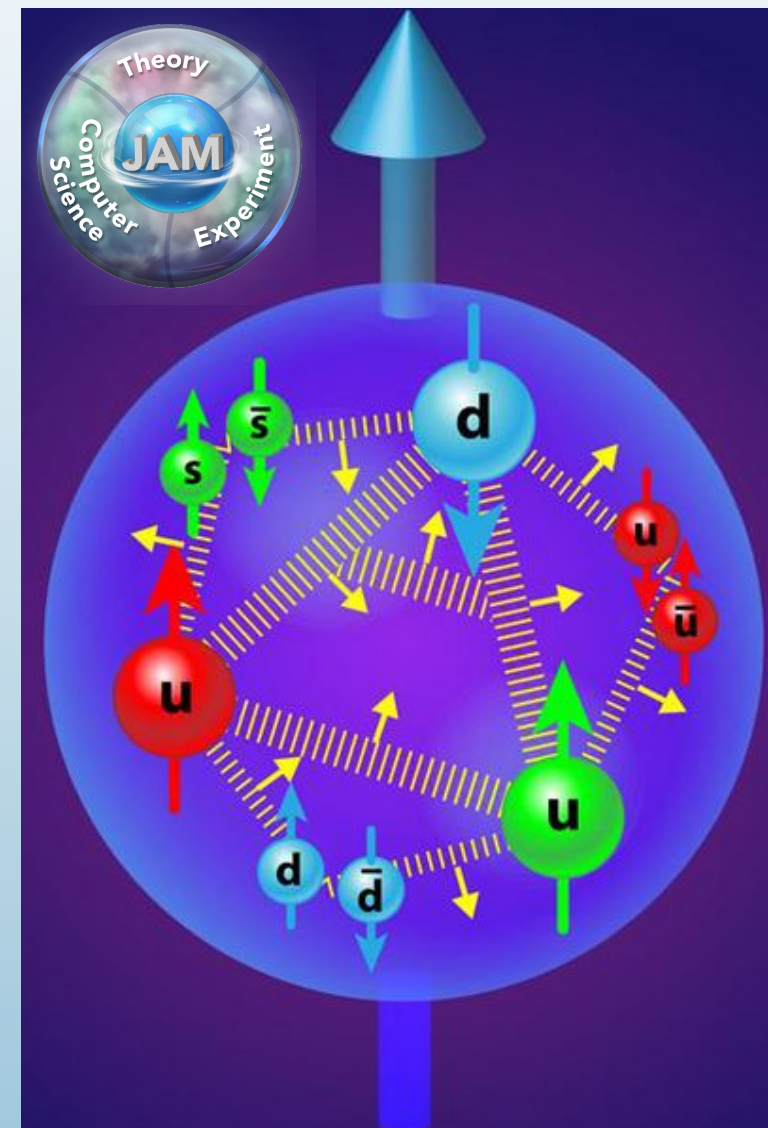


# JAM Collaboration

3-dimensional structure of nucleons:

- Parton distribution functions (PDFs)
- Fragmentation functions (FFs)
- Transverse momentum dependent distributions (TMDs)
- Generalized parton distributions (GPDs)

- Collinear factorization in perturbative QCD
- Simultaneous determinations of PDFs, FFs, etc.
- Monte Carlo methods for Bayesian inference





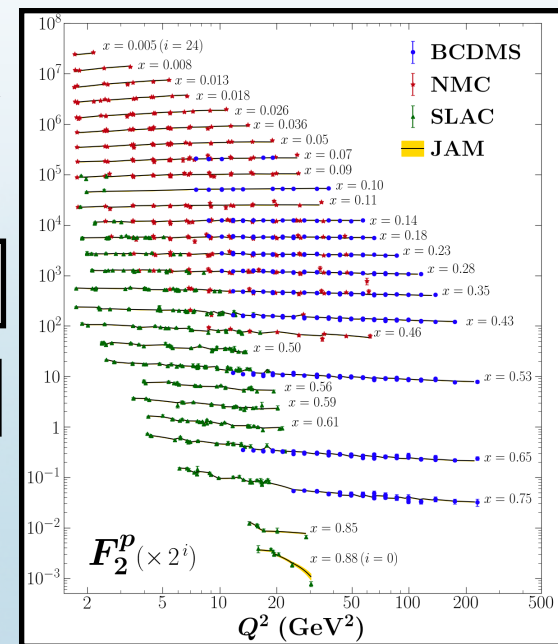


$$\chi^2(\mathbf{a}) = \sum_{i,e} \left( \frac{d_{i,e} - \sum_k r_e^k \beta_{i,e}^k - T_{i,e}(\mathbf{a})/N_e}{\alpha_{i,e}} \right)^2 + \sum_k (r_e^k)^2 + \left( \frac{1 - N_e}{\delta N_e} \right)^2$$

$\chi^2$  Minimization

$$\mathcal{L}(\mathbf{a}, \text{data}) = \exp \left( -\frac{1}{2} \chi^2(\mathbf{a}, \text{data}) \right)$$

$$\mathcal{P}(\mathbf{a}|\text{data}) \sim \mathcal{L}(\mathbf{a}, \text{data}) \pi(\mathbf{a})$$



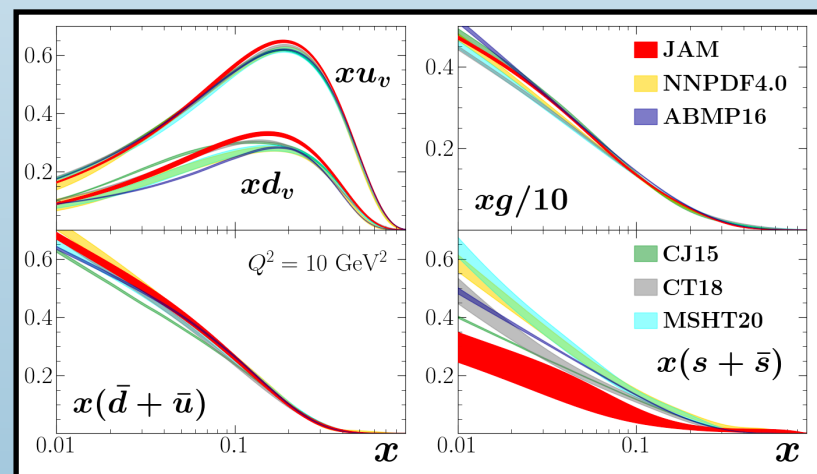
Hadron  
Structure

$$\frac{d}{d \ln(\mu^2)} f_i(x, \mu) = \sum_j \int_x^1 \frac{dz}{z} P_{ij}(z, \mu) f_j\left(\frac{x}{z}, \mu\right)$$

Param. + Evolve + Factorization

$$\sigma = \sum_{i,j} H_{ij} \otimes f_i \otimes f_j$$

Global  
QCD  
Analysis



Data  
Resampling

$$\tilde{\sigma} = \sigma + N(0,1) \alpha$$

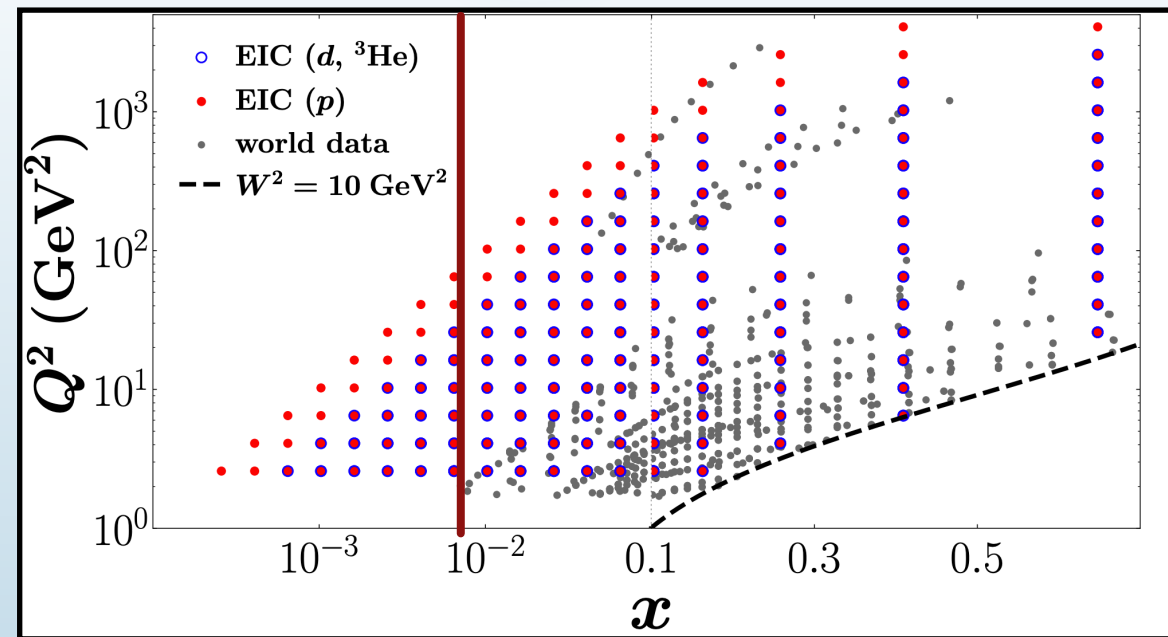
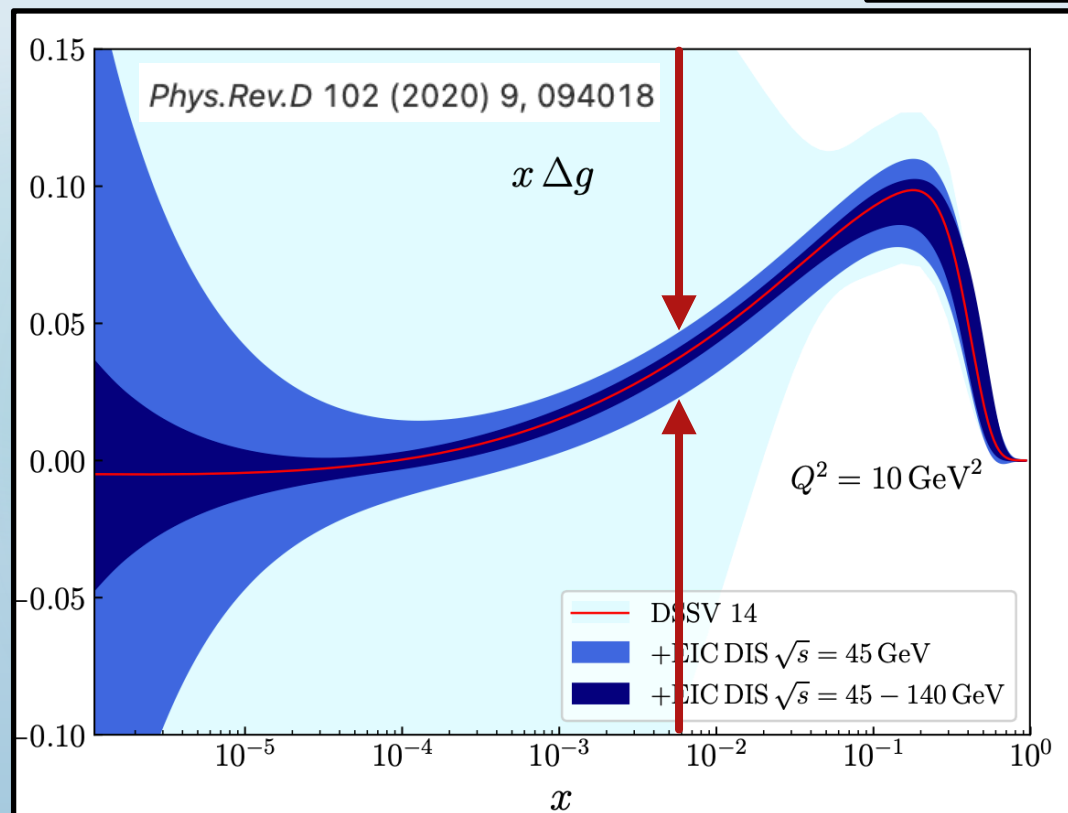
# Current State of Helicity PDFs

Proton spin puzzle:

$$\frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_q + L_g$$

$$\Delta\Sigma = \int_0^1 dx \sum_q \Delta q^+$$

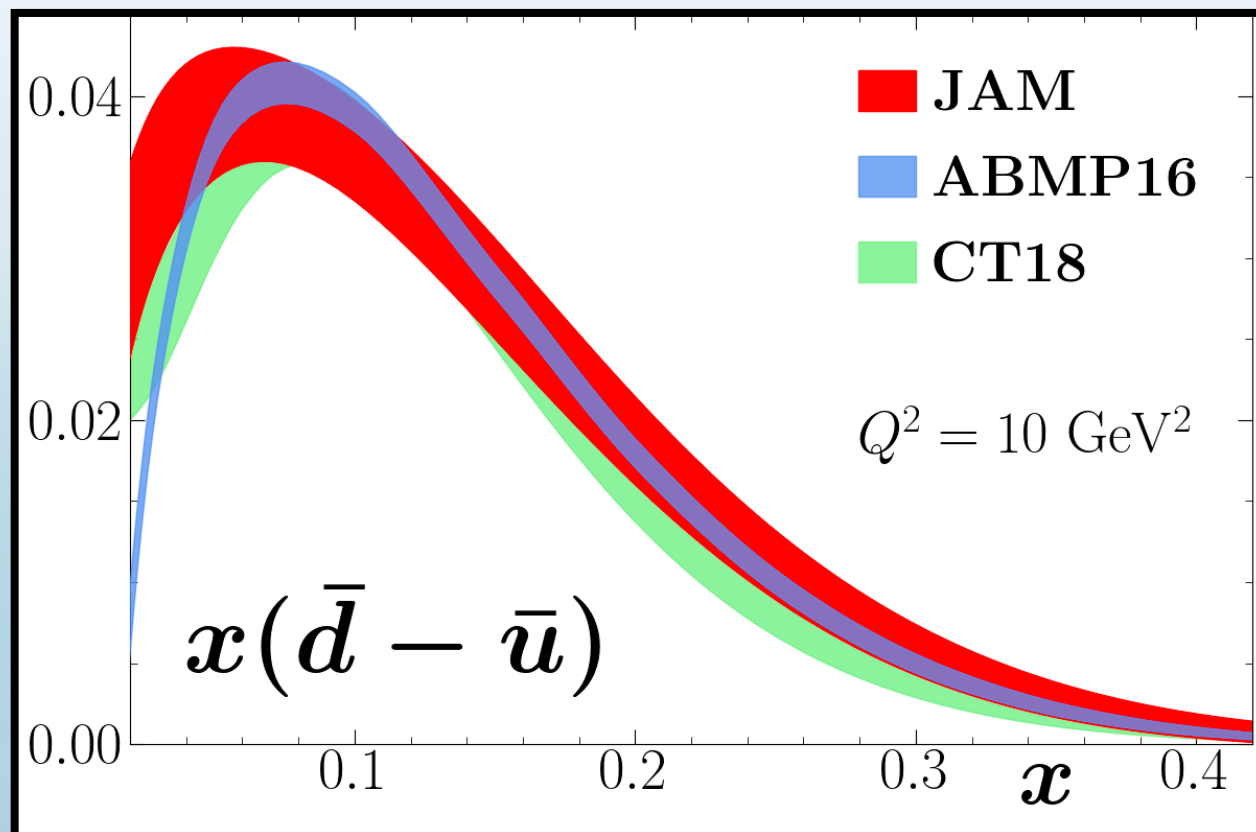
$$\Delta G = \int_0^1 dx \Delta g$$



Still a lot to learn about  
helicity PDFs!  
(antiquarks and gluon)



# Introduction to Sea Asymmetry



Unpolarized

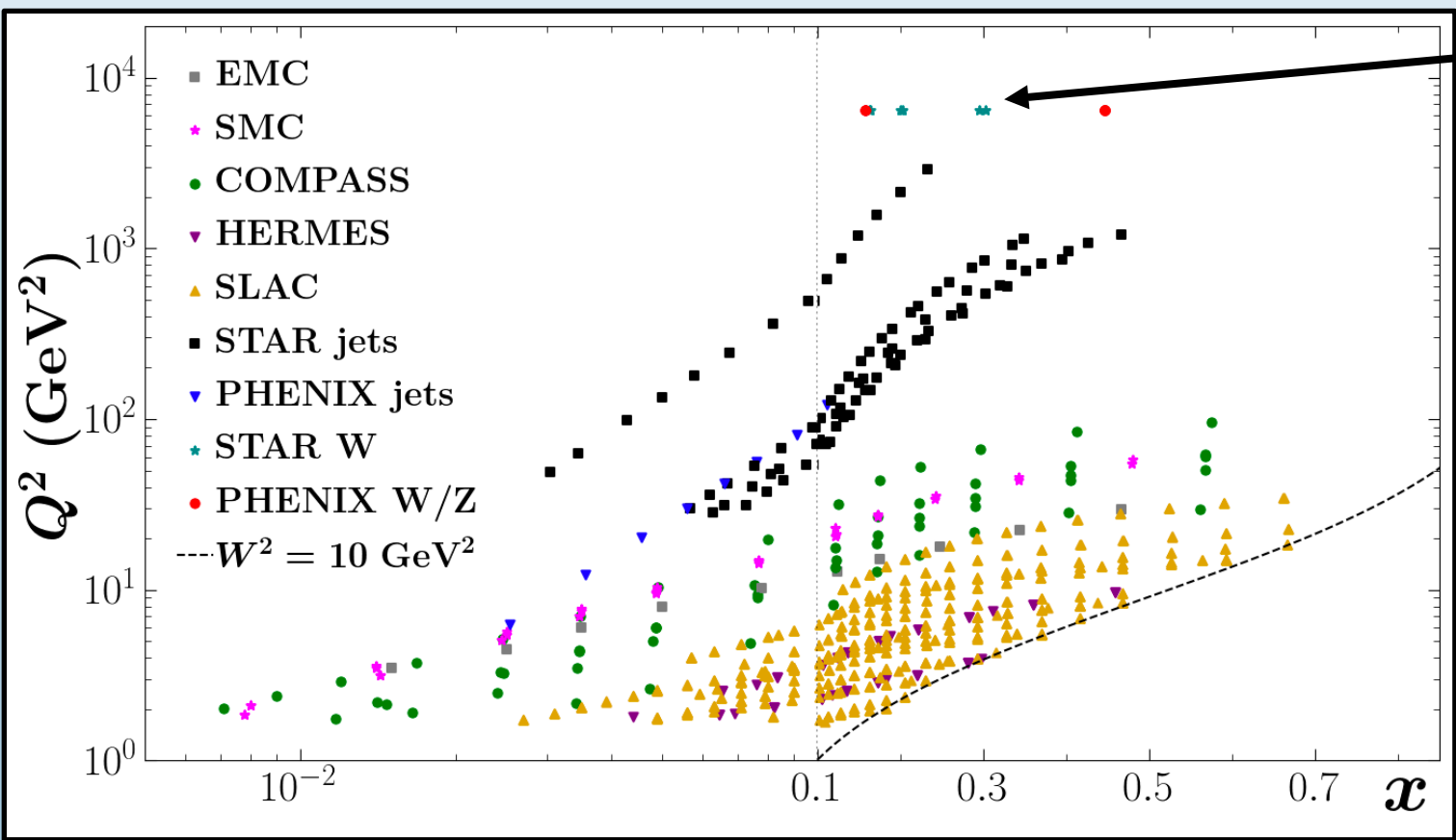
Cannot be explained from gluons  
splitting into quark-antiquark pairs

Meson Cloud Models  
Chiral Soliton Models  
Statistical Models

Still questions for helicity  
asymmetry

# Kinematic Coverage (Helicity)

Deep Inelastic Scattering	COMPASS, EMC, HERMES, SLAC, SMC	365 points
Semi-Inclusive DIS	COMPASS, HERMES, SMC	231 points
W/Z Boson Production	STAR, PHENIX	18 points
Jets	STAR, PHENIX	61 points



STAR + PHENIX  
W/Z Production

process	$N_{\text{dat}}$	$\chi^2/N_{\text{dat}}$
<b>polarized</b>		
inclusive DIS	365	0.95
SIDIS ( $\pi^+, \pi^-$ )	64	1.05
SIDIS ( $K^+, K^-$ )	57	0.42
SIDIS ( $h^+, h^-$ )	110	0.95
inclusive jets	83	0.84
STAR $W^\pm$	12	0.65
PHENIX $W^\pm/Z$	6	0.50
<b>total</b>	<b>697</b>	<b>0.89</b>
<b>unpolarized</b>		
inclusive DIS	3908	1.17
SIDIS ( $\pi^+, \pi^-$ )	498	0.94
SIDIS ( $K^+, K^-$ )	494	1.31
SIDIS ( $h^+, h^-$ )	498	0.71
inclusive jets	198	1.28
Drell-Yan	205	1.21
W/Z production	153	1.01
<b>total</b>	<b>5954</b>	<b>1.12</b>
SIA ( $\pi^\pm$ )	231	0.91
SIA ( $K^\pm$ )	213	0.70
SIA ( $h^\pm$ )	120	1.07
<b>total</b>	<b>7215</b>	<b>1.08</b>

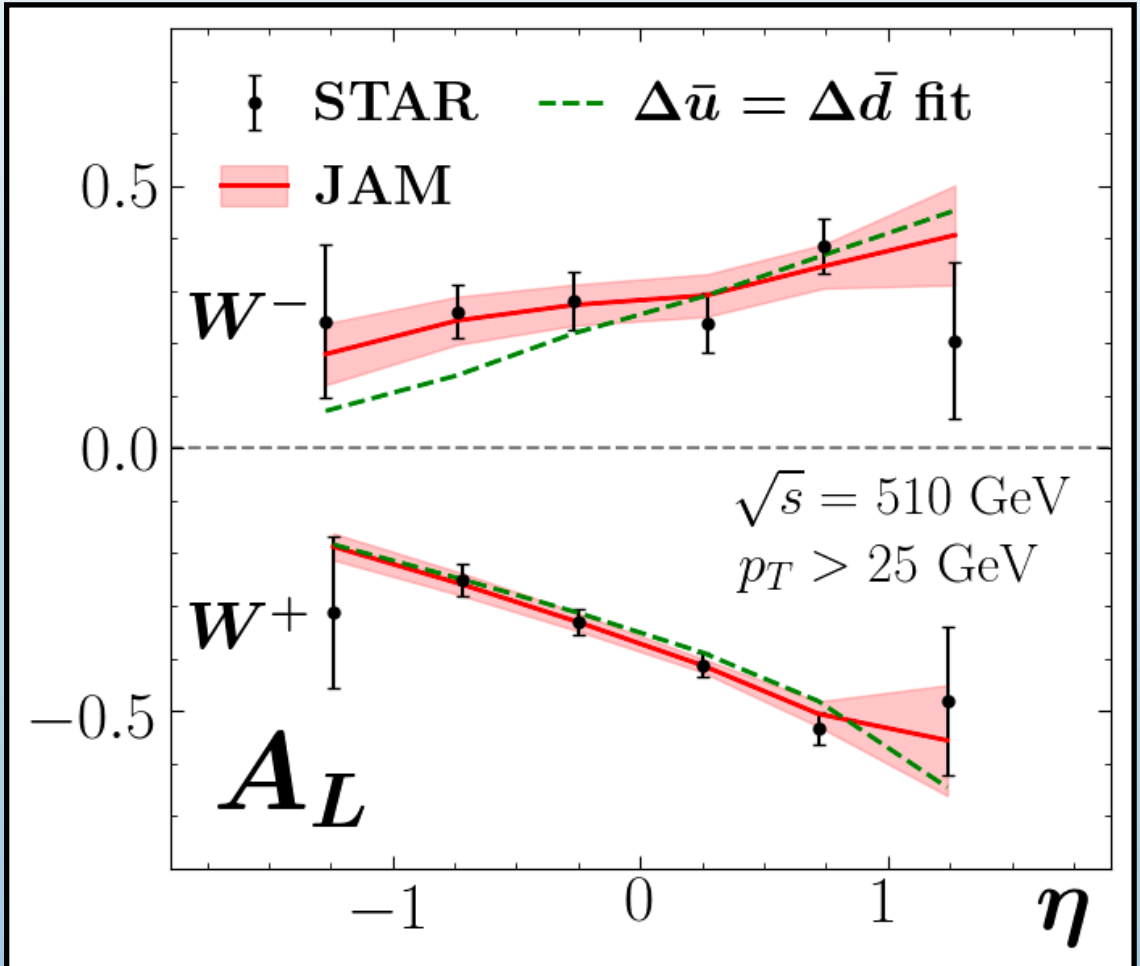


# STAR Quality of Fit

Polarized antimatter in the proton from a global QCD analysis

Jefferson Lab Angular Momentum (JAM) Collaboration • C. Cocuzza (Temple U.) [Show All\(4\)](#)

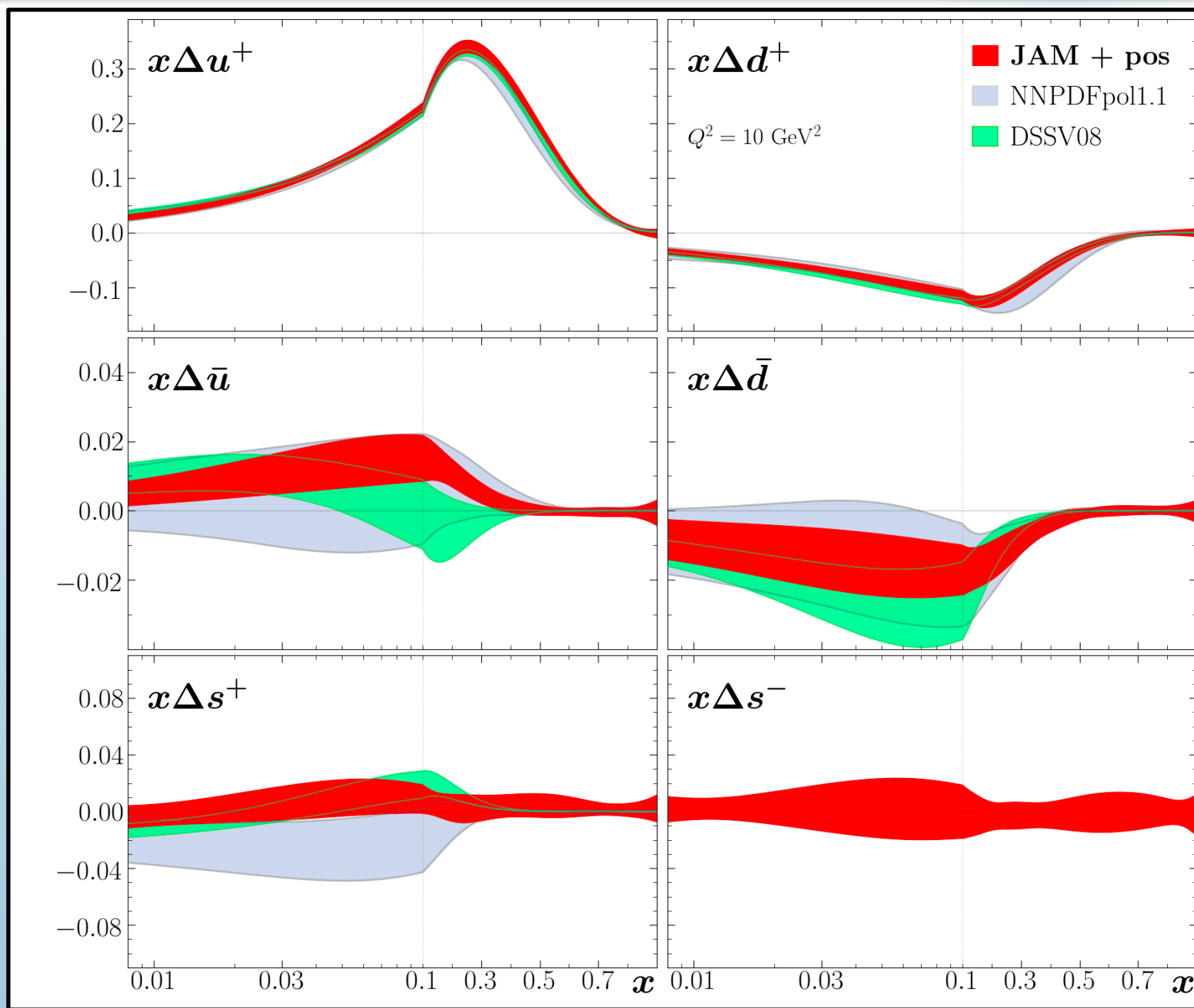
Feb 7, 2022



process	$N_{\text{dat}}$	JAM	$\chi^2/N_{\text{dat}}$ +Pos.	$\Delta\bar{u} = \Delta\bar{d}$
STAR $W^\pm$	12	0.45	0.61	1.53
PHENIX $W^\pm/Z$	6	0.47	0.46	0.48
pol. DIS	365	0.93	0.93	0.93
pol. jet	61	1.00	1.03	1.00
<b>total</b>	<b>444</b>	<b>0.92</b>	<b>0.94</b>	<b>0.95</b>

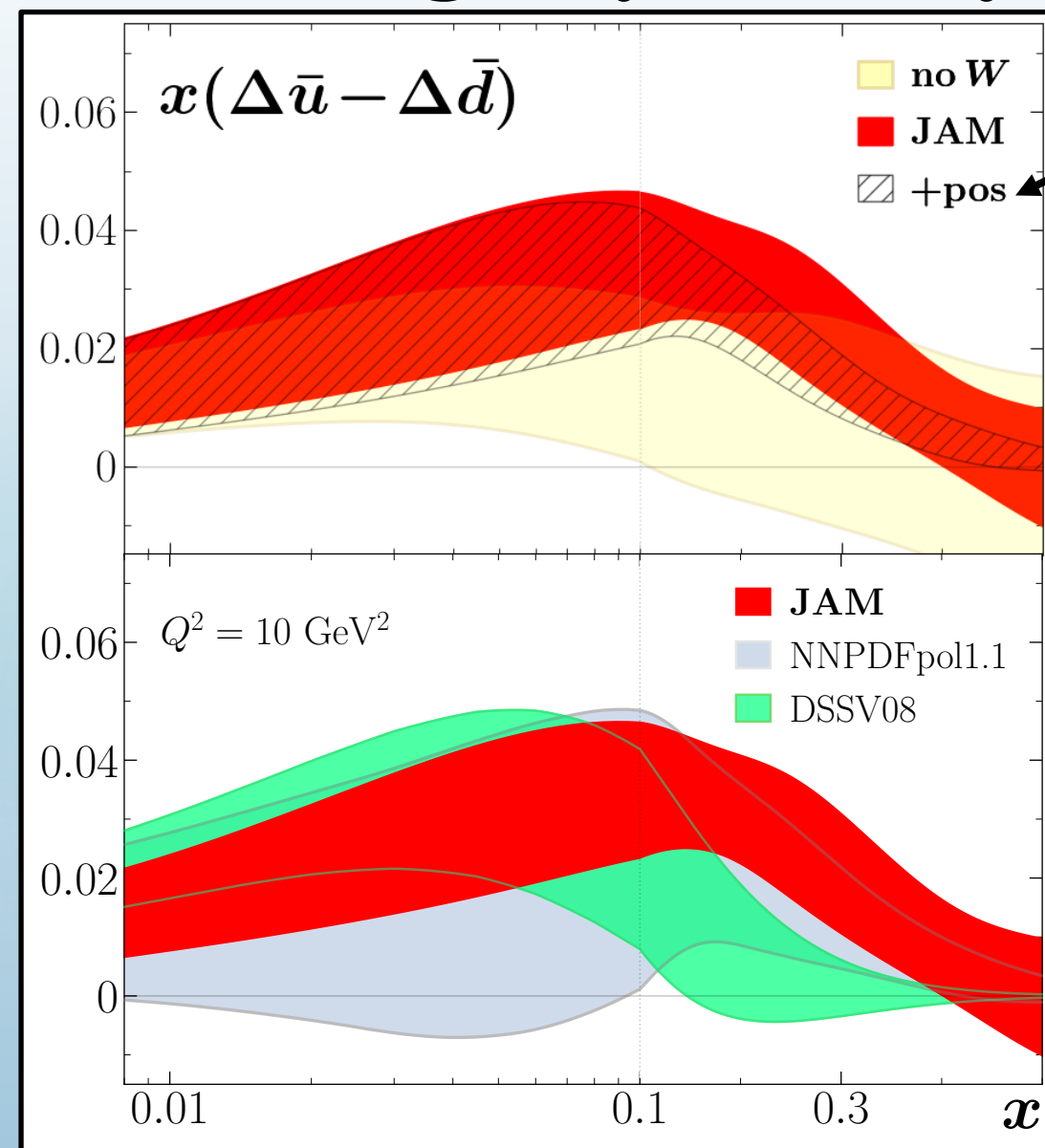
$$A_L^{W^+}(y_W) \propto \frac{\Delta\bar{d}(x_1)u(x_2) - \Delta u(x_1)\bar{d}(x_2)}{\bar{d}(x_1)u(x_2) + u(x_1)\bar{d}(x_2)}$$

$$A_L^{W^-}(y_W) \propto \frac{\Delta\bar{u}(x_1)d(x_2) - \Delta d(x_1)\bar{u}(x_2)}{\bar{u}(x_1)d(x_2) + d(x_1)\bar{u}(x_2)}$$





# Resulting Asymmetry



Positivity Constraints:  
 $|\Delta f(x, Q^2)| < f(x, Q^2)$

Can  $\overline{\text{MS}}$  parton distributions be negative?

Alessandro Candido, Stefano Forte and Felix Hekhorn

Positivity and renormalization of parton densities

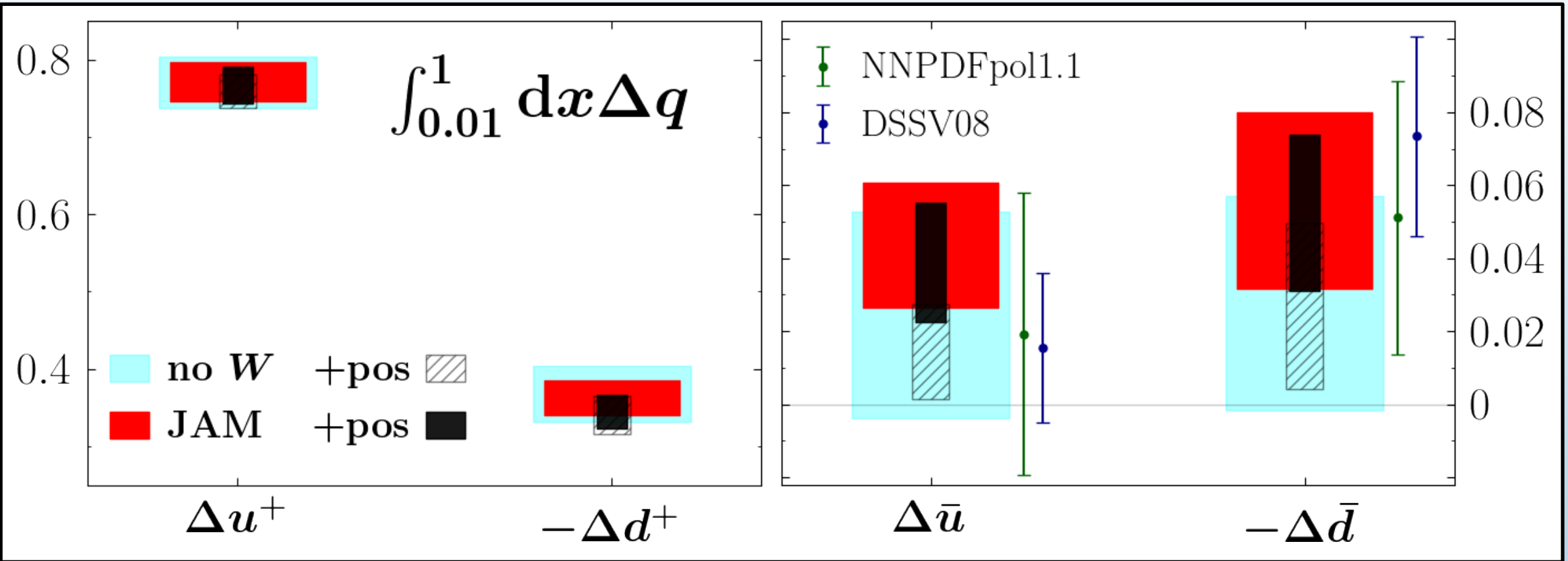
John Collins, Ted C. Rogers, Nobuo Sato

DSSV08 shows positive asymmetry at low  $x < 0.1$

NNPDF shows hint of positive asymmetry at intermediate  $x$

Our result is strongly positive in both regions of  $x$

# Proton Spin Contributions



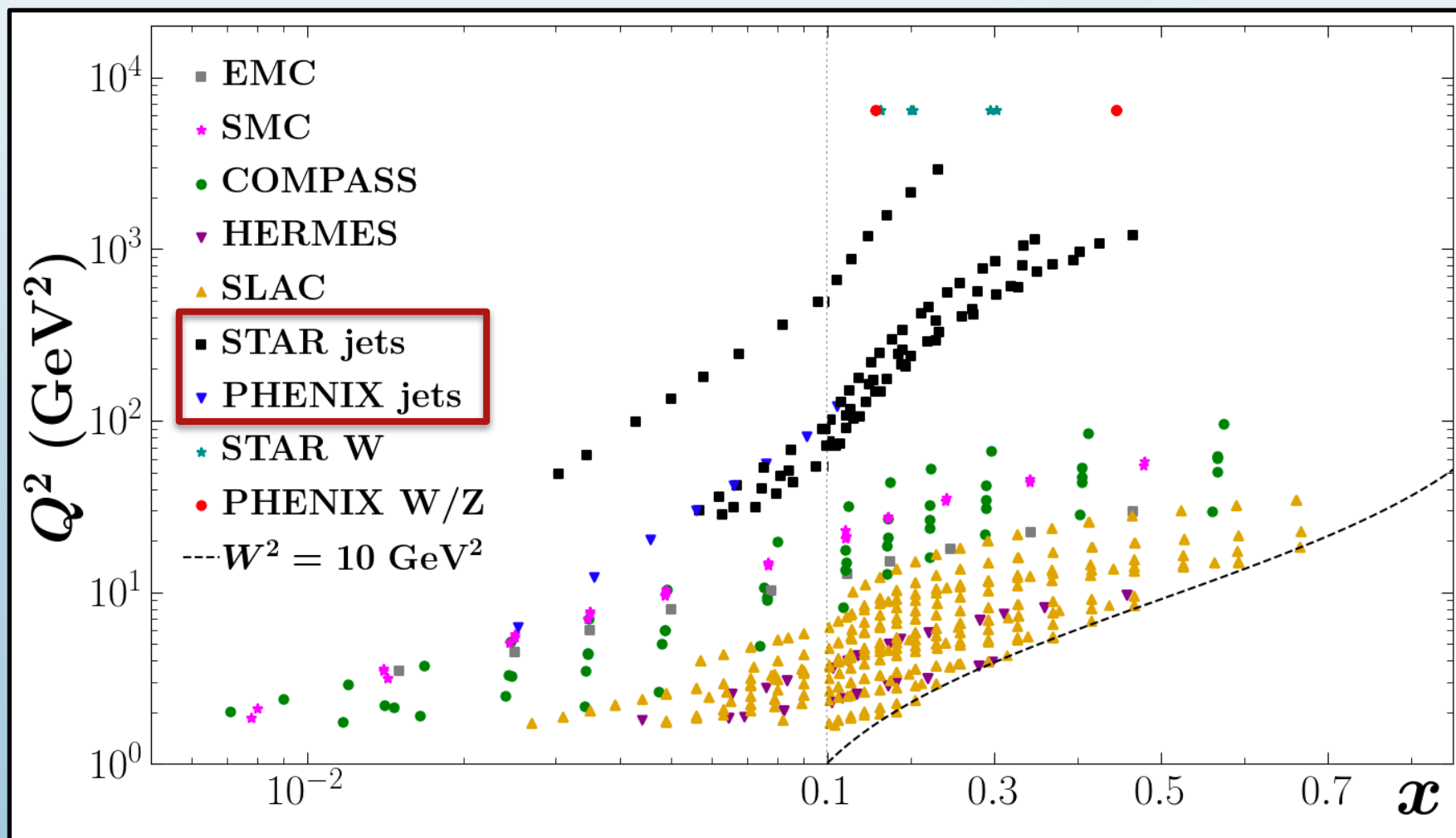
Inclusion of RHIC  $W/Z$  data shows that  $\Delta \bar{u}$  ( $\Delta \bar{d}$ ) contribution is small and positive (negative)

Flavor	JAM moment (truncated)	Lattice Moment (full)	Difference
$\Delta u^+$	0.779(34)	0.864(16)	10%
$\Delta d^+$	-0.370(40)	-0.426(16)	13%



<b>Deep Inelastic Scattering</b>	COMPASS, EMC, HERMES, SLAC, SMC	365 points
<b>Semi-Inclusive DIS</b>	COMPASS, HERMES, SMC	231 points
<b>W/Z Boson Production</b>	STAR, PHENIX	18 points
<b>Jets</b>	STAR, PHENIX	61 points

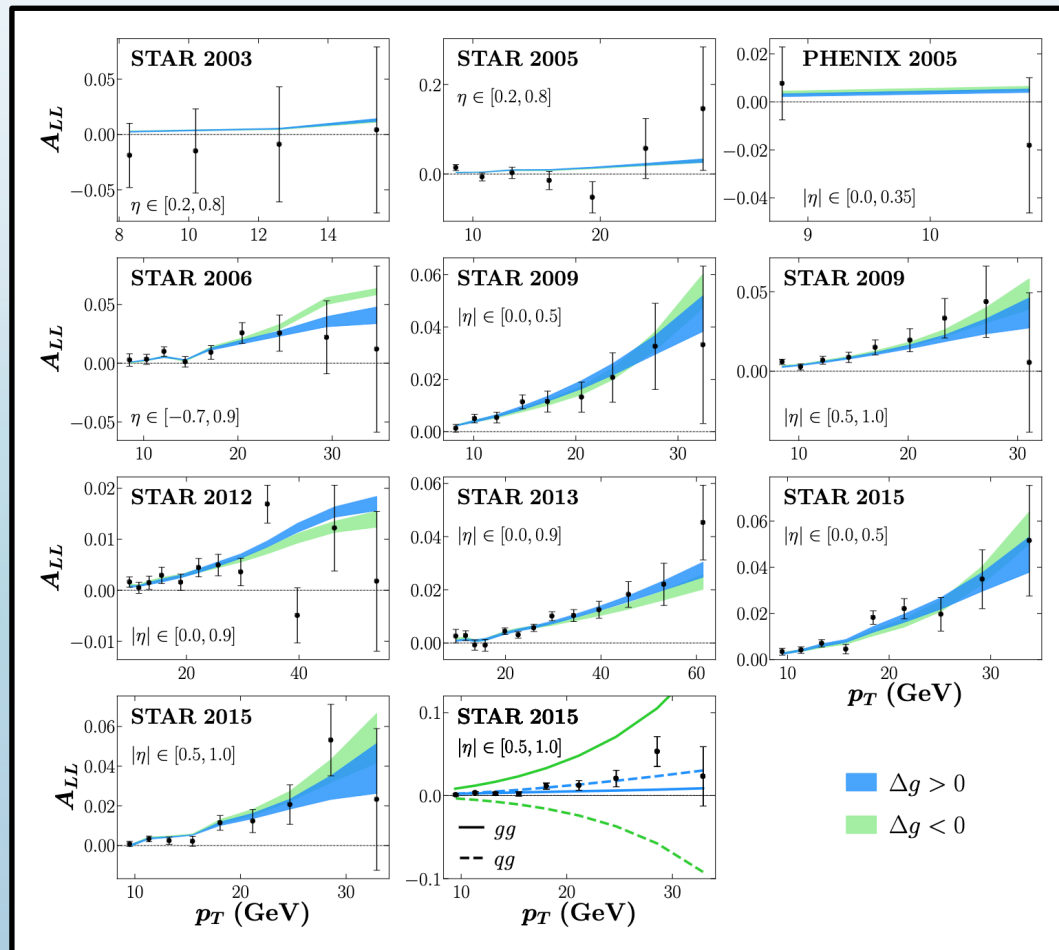
Jets provide most direct constraints on gluon distribution



How well do we know the gluon polarization in the proton? #1

Jefferson Lab Angular Momentum (JAM) Collaboration • Y. Zhou (South China Normal U. and UCLA and William-Mary Coll. and Jefferson Lab) et al. (Jan 6, 2022)

Published in: *Phys.Rev.D* 105 (2022) 7, 074022 • e-Print: [2201.02075](#) [hep-ph]



Positivity constraints rule out negative solution

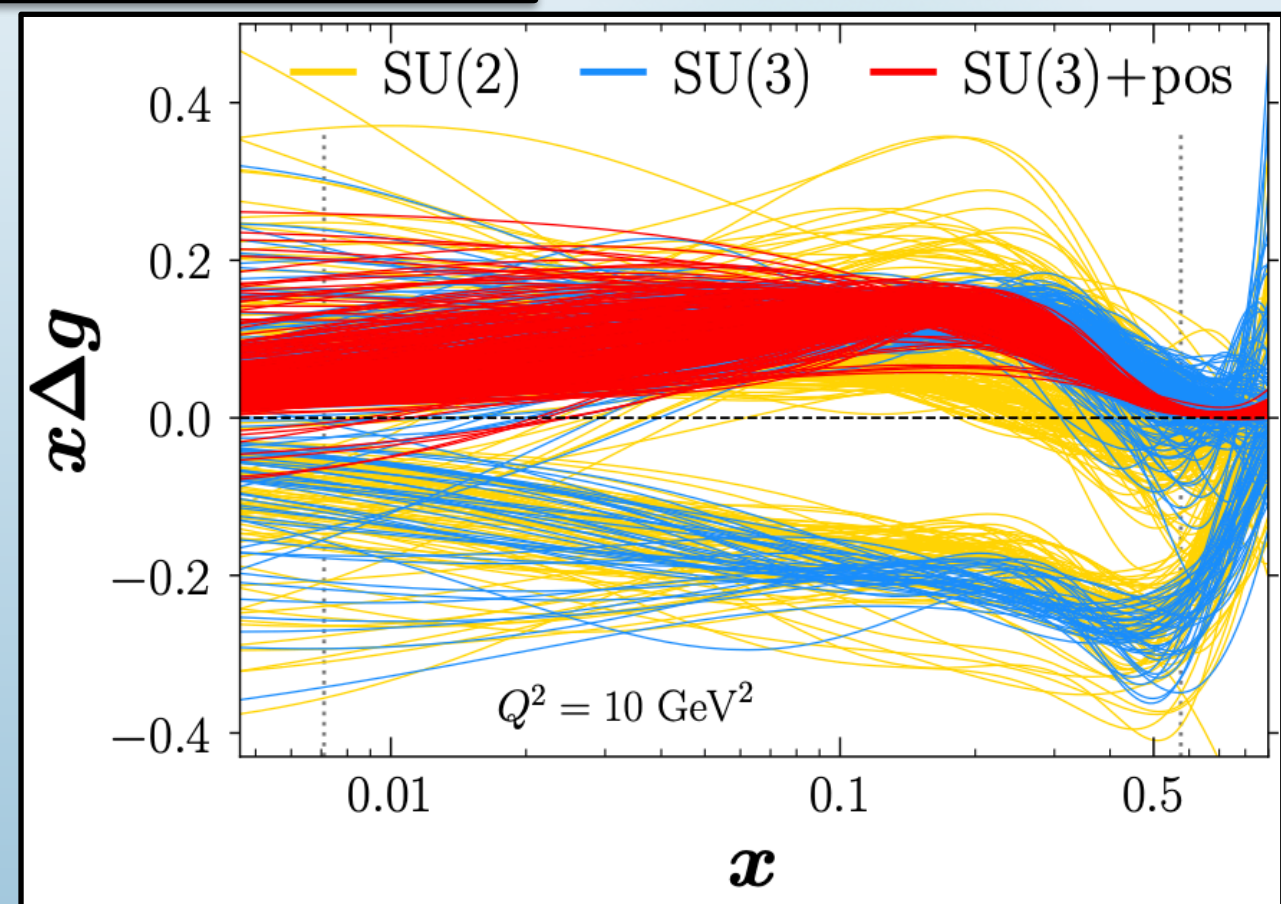
Can  $\overline{\text{MS}}$  parton distributions be negative?

Alessandro Candido, Stefano Forte and Felix Hekhorn

Positivity and renormalization of parton densities

John Collins, Ted C. Rogers, Nobuo Sato

$$|\Delta f(x, Q^2)| < f(x, Q^2)$$



$$A_{LL}^{\text{jet}} \sim (\Delta g)^2 + \Delta q \Delta g + \dots$$

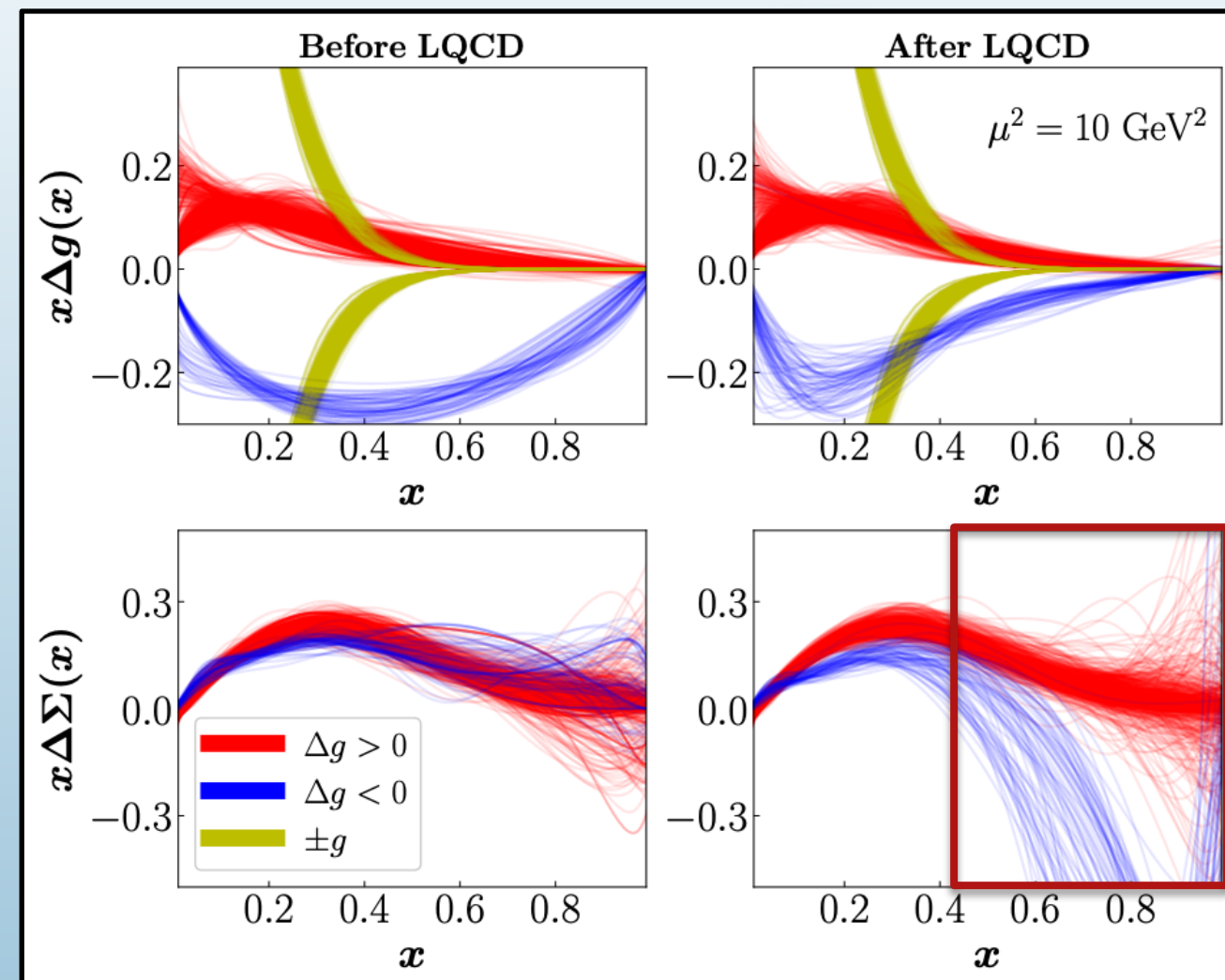
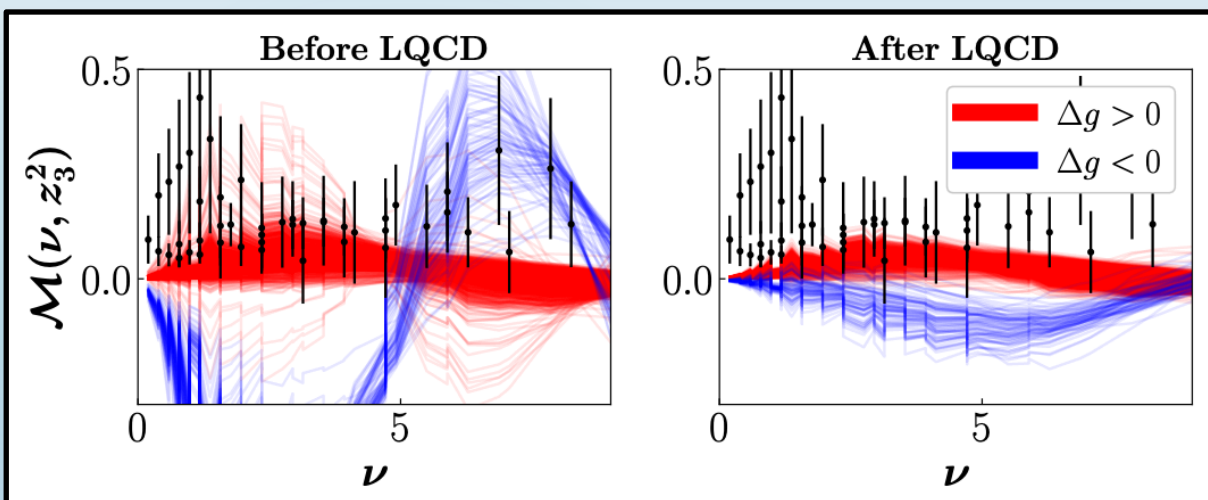


Gluon helicity from global analysis of experimental data and lattice QCD loffe time distributions

J. Karpie (Jefferson Lab), R.M. Whitehill (Old Dominion U.), W. Melnitchouk (Jefferson Lab), C. Monahan (Jefferson Lab and William-Mary Coll.), K. Orginos (Jefferson Lab and William-Mary Coll.) [Show All\(9\)](#)

Oct 27, 2023

$$\mathcal{M}(\nu, z_3^2) = \int_0^1 dx \, x \sin(x\nu) \Delta g(x) \quad (\text{LO})$$



LQCD data does not rule out negative gluon, but leads to wild behavior for  $\Delta\Sigma$  at large  $x$

Measurement of charged pion double spin asymmetries at midrapidity in longitudinally polarized  $p + p$  collisions at  $\sqrt{s} = 510$  GeV

PHENIX Collaboration • U.A. Acharya (Georgia State U.) et al. (Apr 6, 2020)

Published in: *Phys.Rev.D* 102 (2020) 3, 032001 • e-Print: [2004.02681](#) [hep-ex]

$$\vec{p} + \vec{p} \rightarrow \pi^{\pm} + X$$

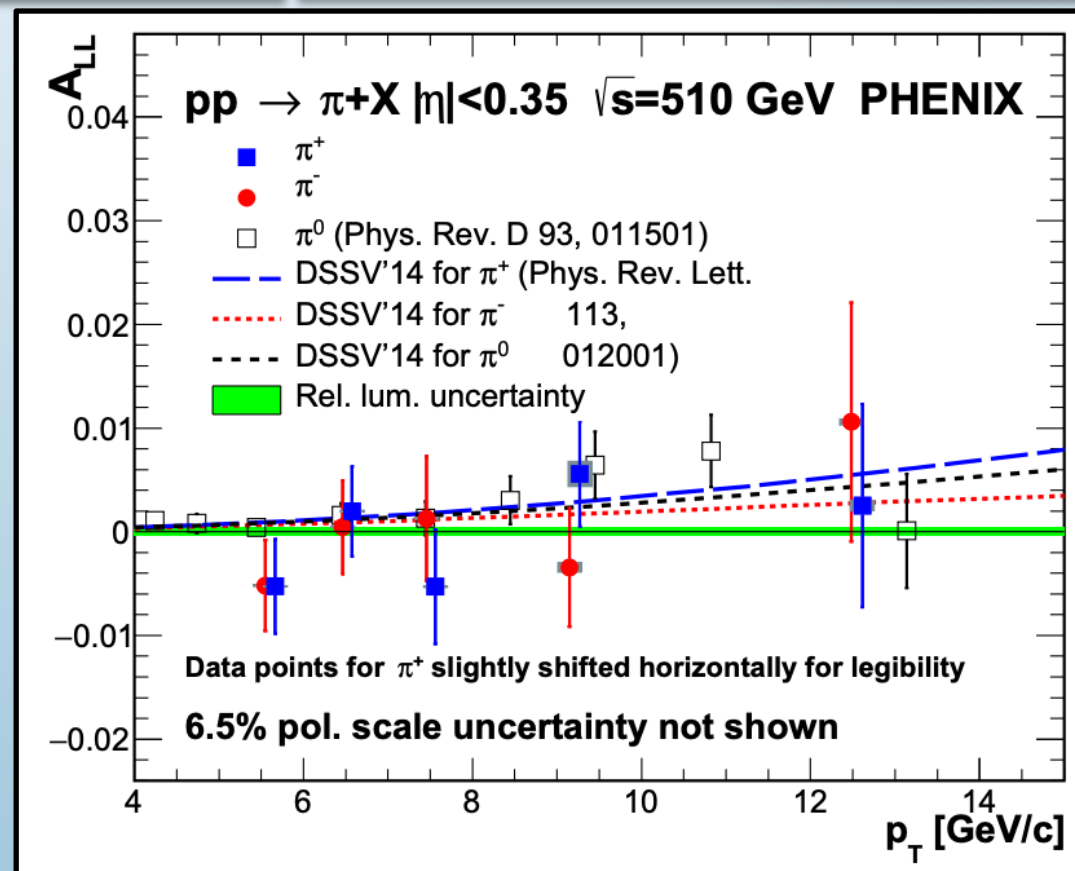
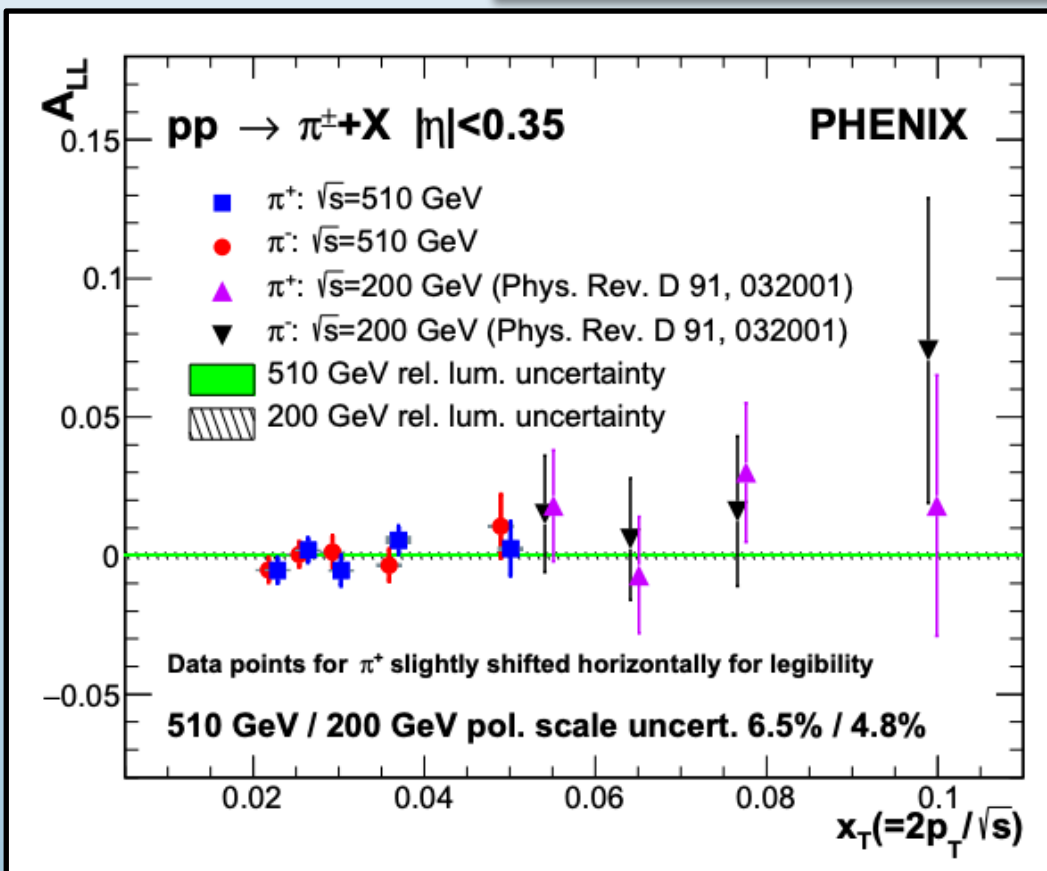
Charge ordering:  
If  $\Delta g > 0$  :  $A_{LL}^{\pi^+} > A_{LL}^{\pi^0} > A_{LL}^{\pi^-}$

Charged-pion cross sections and double-helicity asymmetries in polarized  $p+p$  collisions at  $\sqrt{s}=200$  GeV

PHENIX Collaboration • A. Adare (Colorado U.) et al. (Sep 5, 2014)

Published in: *Phys.Rev.D* 91 (2015) 3, 032001 • e-Print: [1409.1907](#) [hep-ex]

Consistent with DSSV14 analysis (which included 210 GeV data) with  $\Delta g > 0$



*Phys.Rev.Lett.* 113 (2014) 1, 012001

Measurement of charged pion double spin asymmetries at midrapidity in longitudinally polarized  $p + p$  collisions at  $\sqrt{s} = 510$  GeV

PHENIX Collaboration • U.A. Acharya (Georgia State U.) et al. (Apr 6, 2020)

Published in: *Phys.Rev.D* 102 (2020) 3, 032001 • e-Print: [2004.02681](#) [hep-ex]

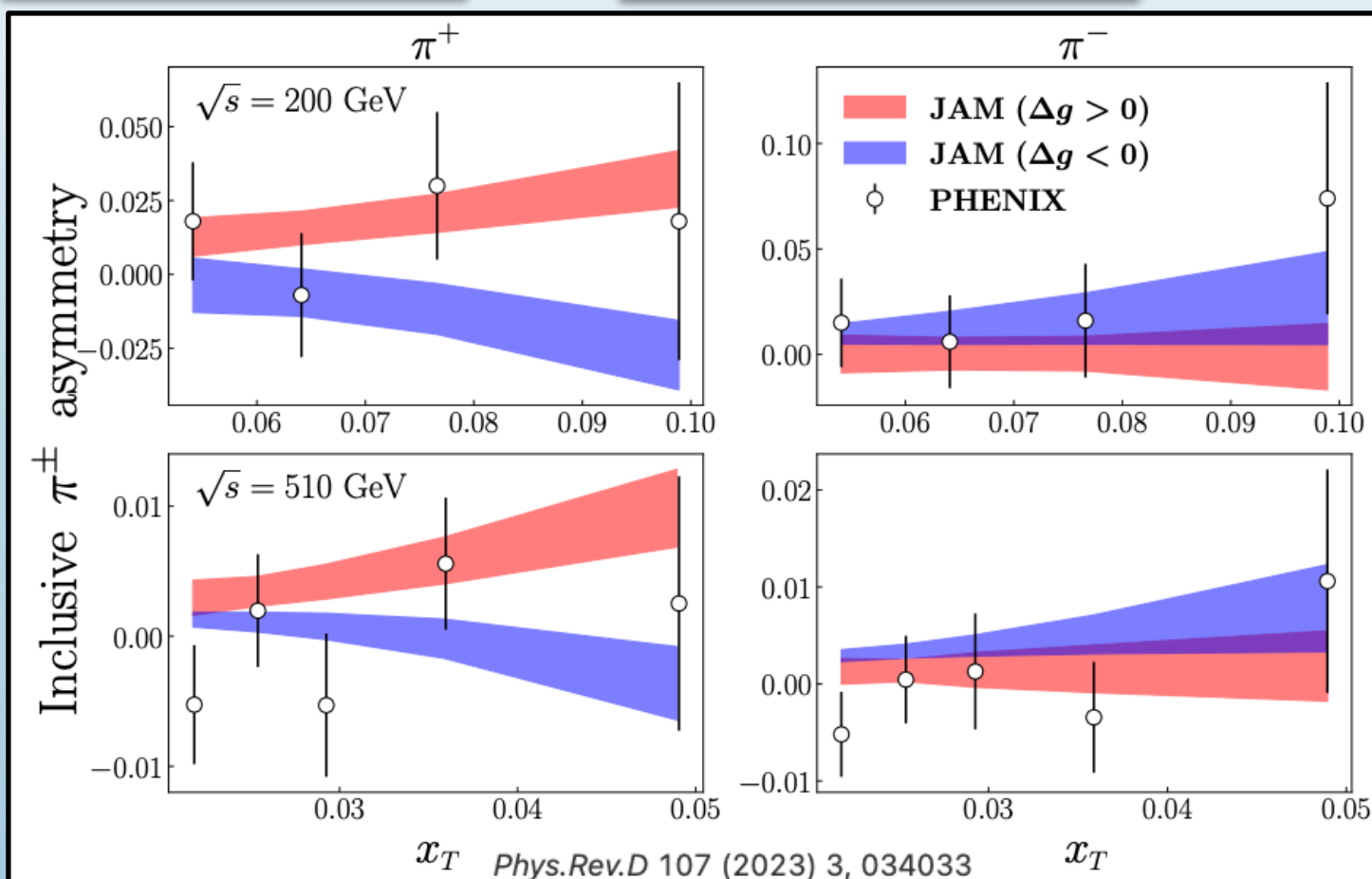
Charged-pion cross sections and double-helicity asymmetries in polarized p+p collisions at  $\sqrt{s}=200$  GeV

PHENIX Collaboration • A. Adare (Colorado U.) et al. (Sep 5, 2014)

Published in: *Phys.Rev.D* 91 (2015) 3, 032001 • e-Print: [1409.1907](#) [hep-ex]

$$\vec{p} + \vec{p} \rightarrow \pi^{\pm} + X$$

JAM Prediction



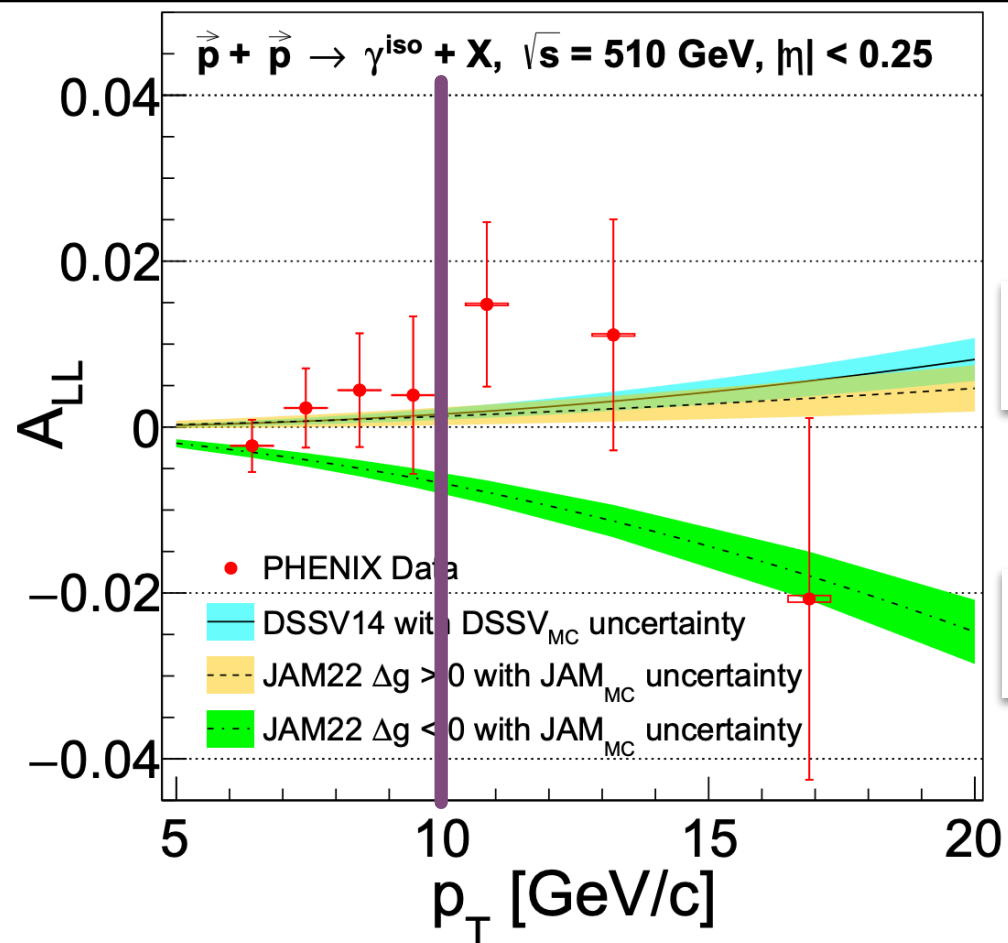
It is inconclusive whether data can distinguish between two solutions



## Measurement of Direct-Photon Cross Section and Double-Helicity Asymmetry at $\sqrt{s} = 510$ GeV in $\vec{p} + \vec{p}$ Collisions

PHENIX Collaboration • U. Acharya (Georgia State U., Atlanta) et al. (Feb 16, 2022)

e-Print: [2202.08158](https://arxiv.org/abs/2202.08158) [hep-ex]



$$\chi^2 = 4.7$$

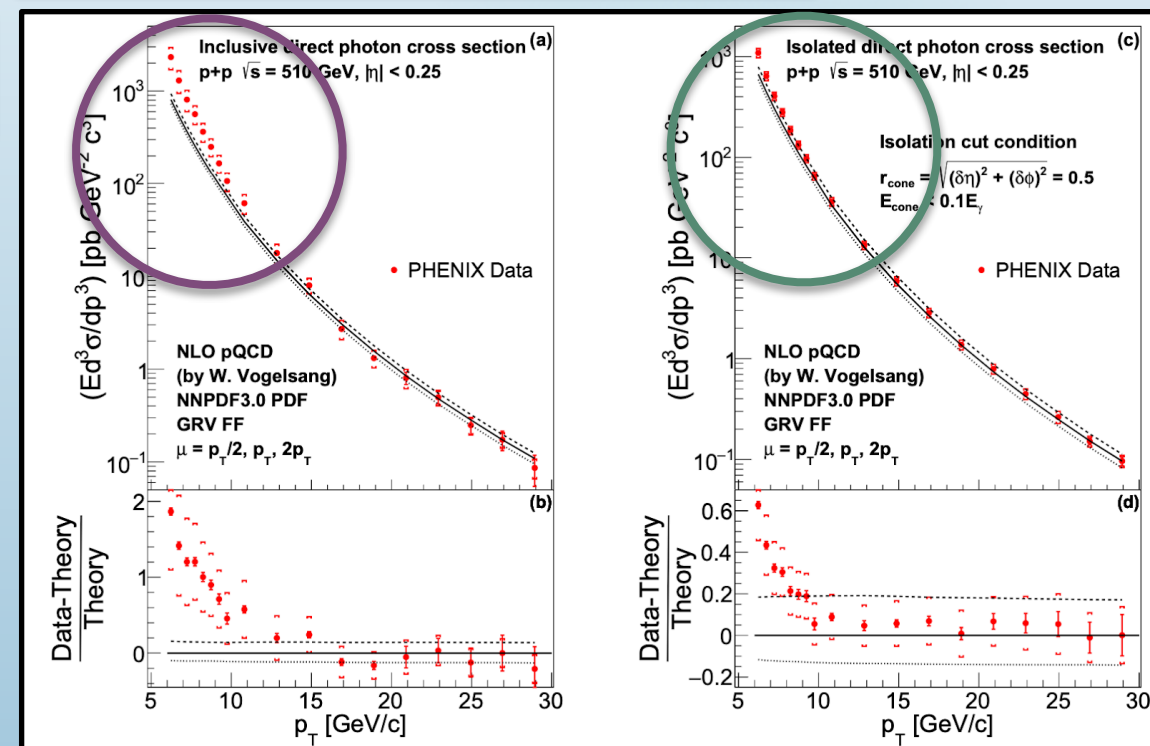
$$2.8\sigma$$

$$\chi^2 = 12.6$$

Direct sensitivity to the sign of  $\Delta g$ !

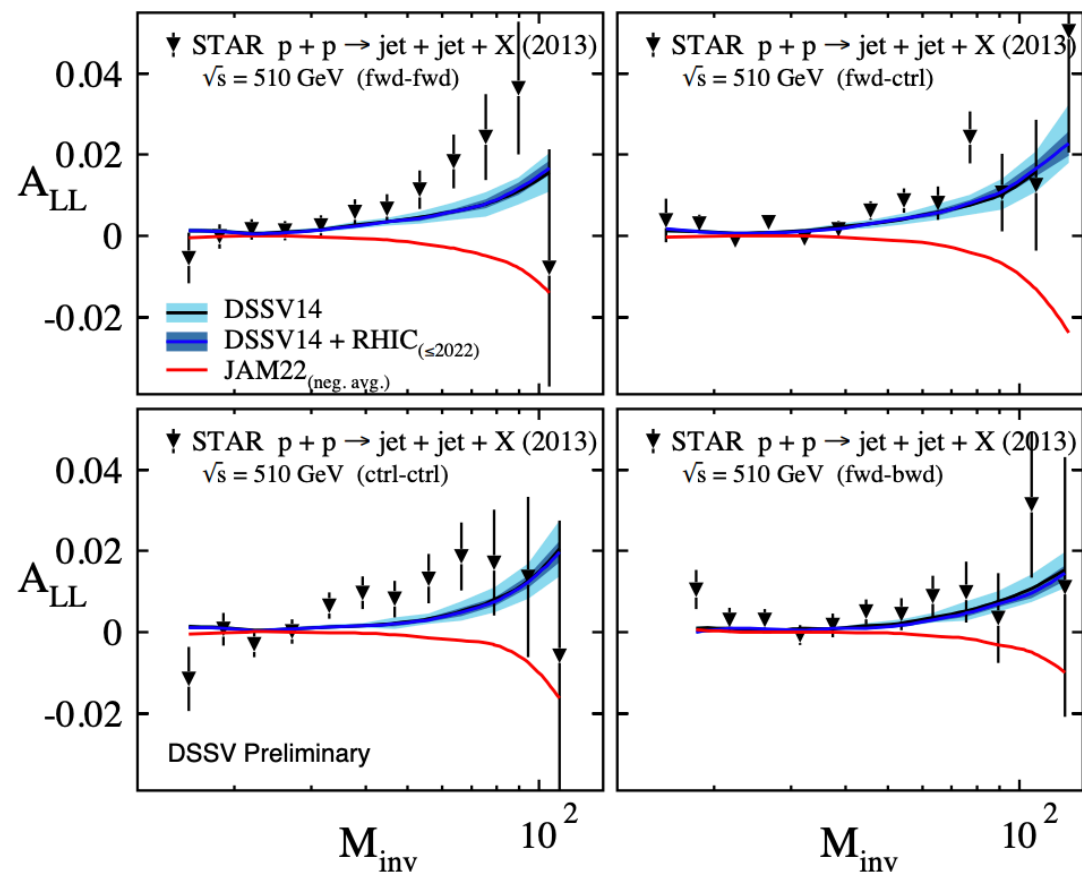
May be aided by isolation cut

Potential issues at  $P_T < 10$



# The RHIC Cold QCD Program

## White Paper

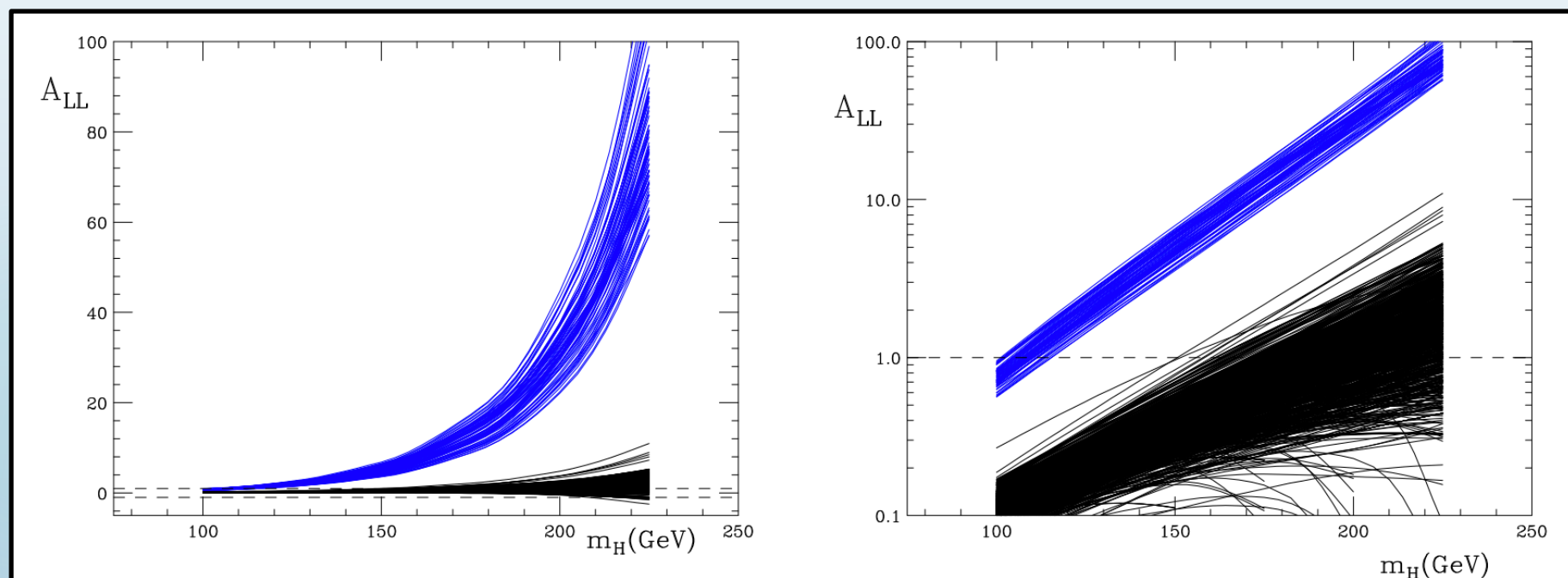


**Figure 8:** STAR double-helicity asymmetries  $A_{LL}$  for dijet production vs dijet invariant mass  $M_{inv}$  in polarized  $pp$  collisions at  $\sqrt{s}=510$  GeV at midrapidity from 2013 data set [21]. DSSV14 evaluation [17] is plotted as the black curve with the  $1\sigma$  uncertainty band marked in light blue. The blue curve with  $1\sigma$  uncertainty band in dark blue shows the impact of all the data sets included in the new preliminary DSSV fit [2] as in Fig. 6. The red curves show the JAM  $\Delta g < 0$  solution [41] calculated by the DSSV group.

## Higgs production at RHIC and the positivity of the gluon helicity distribution

Daniel de Florian, Stefano Forte, Werner Vogelsang

Jan 19, 2024



Negative solution  
(blue) strongly violates  
physical limit.  
Positive solution  
(black) far less so.

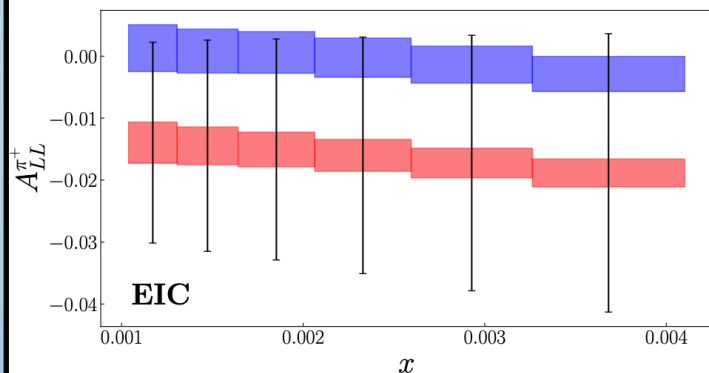
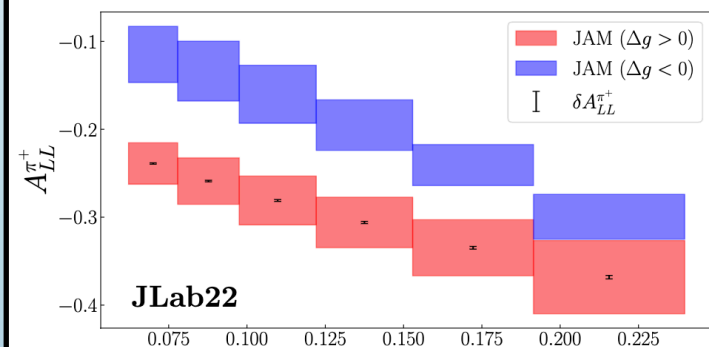
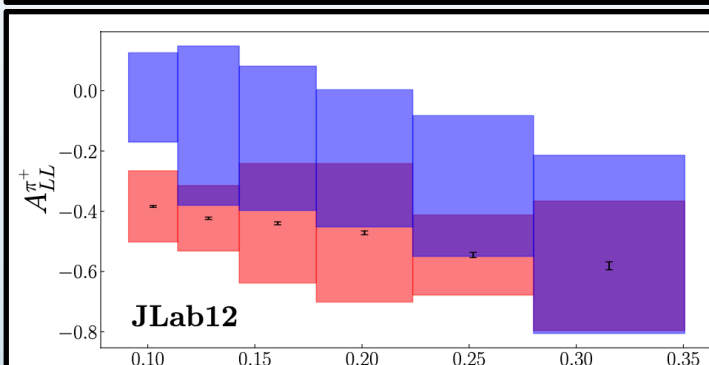
Figure 2: Double-helicity asymmetry for Higgs production at RHIC as a function of the Higgs mass, with a linear (left) or logarithmic (right) scale on the vertical axis. The upper bands show  $A_{LL}$  as obtained for the gluon distribution shown in Fig. 1, while the lower bands provide the corresponding result for the sets of  $[\gamma]$  with  $\Delta g \geq 0$ . In both plots, the dashed lines show the physical limit given by  $|A_{LL}| = 1$ .

## Accessing gluon polarization with high- $P_T$ hadrons in SIDIS

Jefferson Lab Angular Momentum (JAM) Collaboration • R.M. Whitehill (Wichita State U.) et al. (Oct 21, 2022)

Published in: *Phys.Rev.D* 107 (2023) 3, 034033 • e-Print: [2210.12295](https://arxiv.org/abs/2210.12295) [hep-ph]

$$\vec{l} + \vec{N} \rightarrow l' + h + X$$



$\mathcal{L} = 86 \text{ fb}^{-1}$  for JLab  
 $\mathcal{L} = 10 \text{ fb}^{-1}$  for EIC

JLab22 has stronger  
distinguishing power due  
to more evolution and  
access to smaller  $x$

EIC asymmetry is small due to  
scaling behavior of unpolarized  
cross section

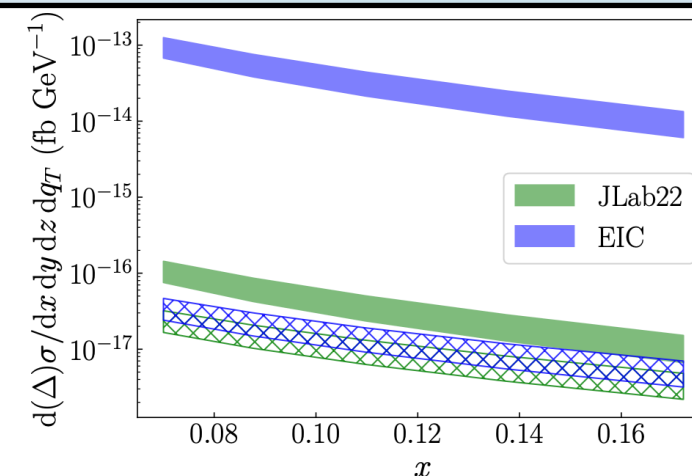


FIG. 7. Unpolarized (solid bands) and polarized (hatched bands) differential cross sections calculated for semi-inclusive  $\pi^+$  production at the  $(x, Q^2, z, q_T)$  kinematics displayed in Fig. 5 for Jefferson Lab with a 22 GeV beam energy (green bands) and EIC center of mass energy  $\sqrt{s} = 140$  GeV (blue bands).

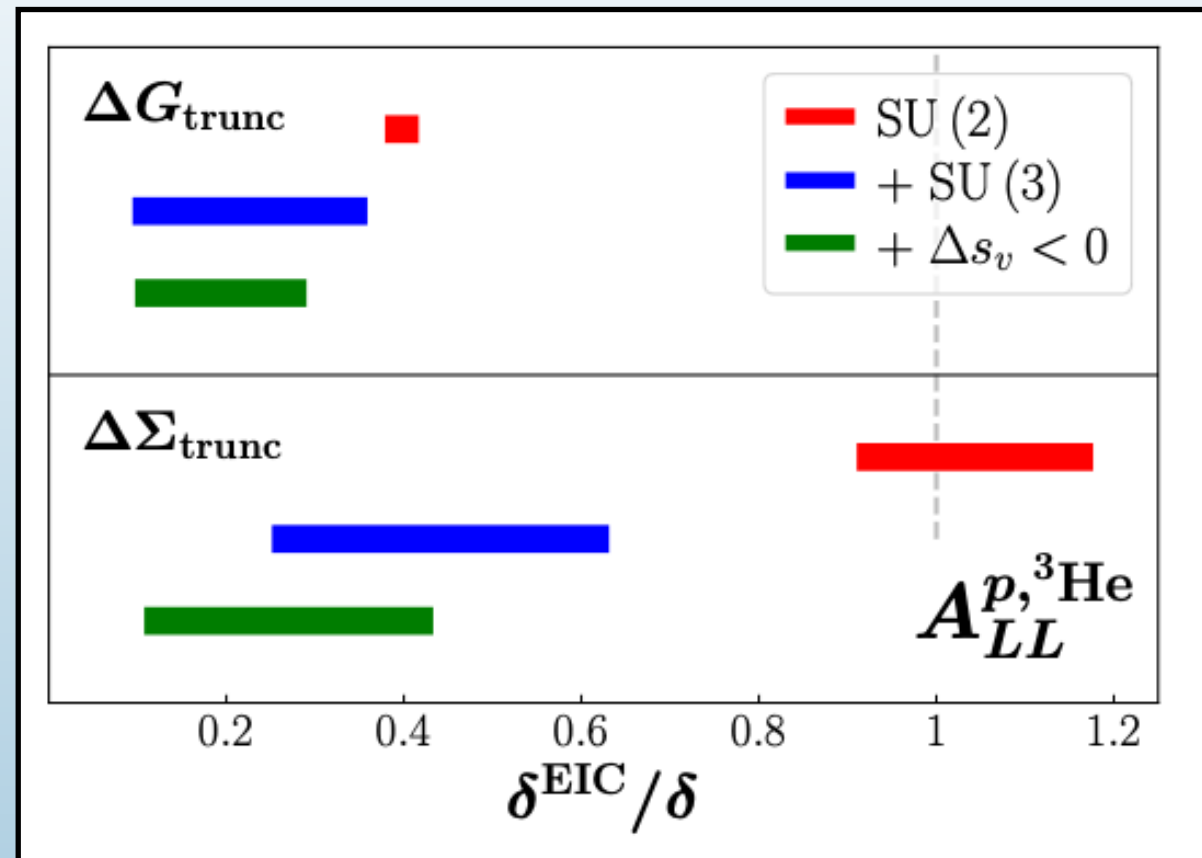
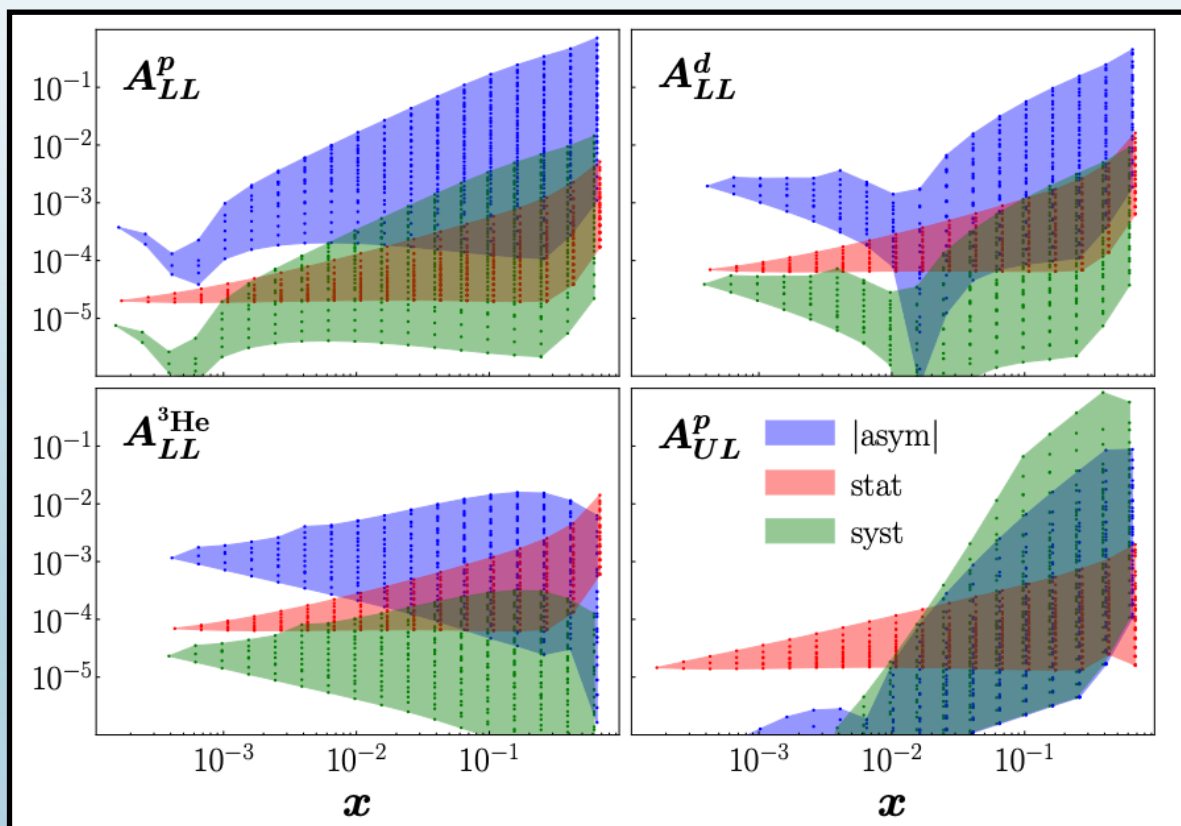


## Revisiting quark and gluon polarization in the proton at the EIC

Jefferson Lab Angular Momentum (JAM) Collaboration • Y. Zhou (William-Mary Coll.) et al. (May 10, 2021)

Published in: *Phys.Rev.D* 104 (2021) 3, 034028 • e-Print: [2105.04434](https://arxiv.org/abs/2105.04434) [hep-ph]

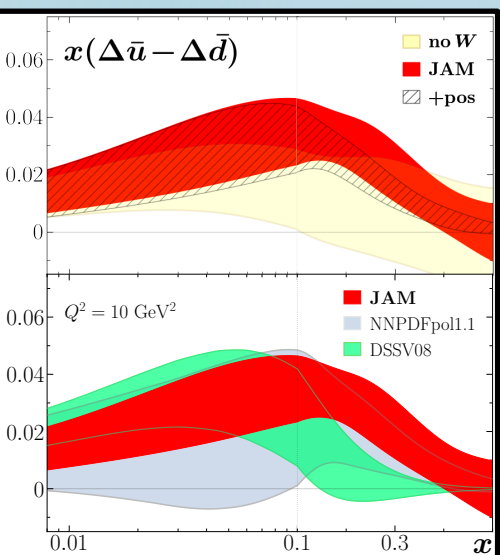
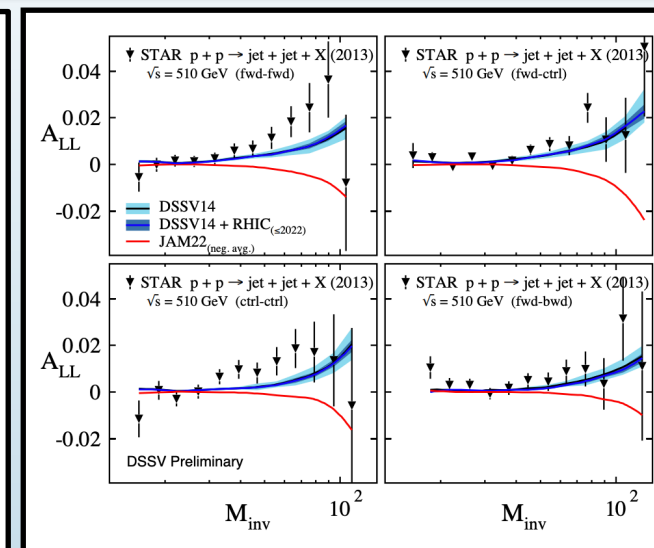
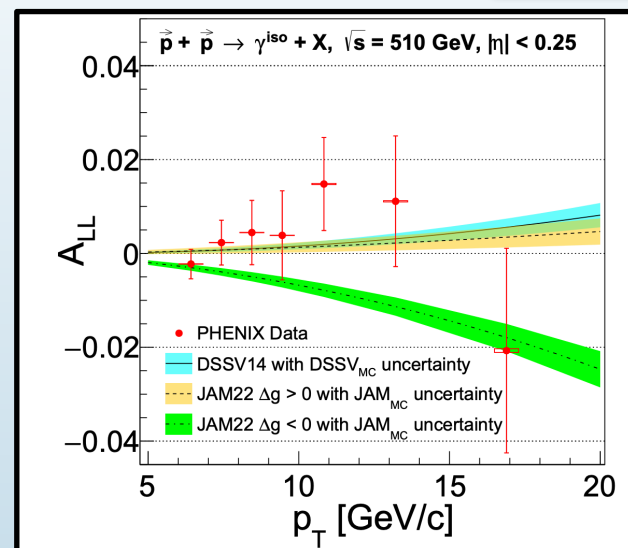
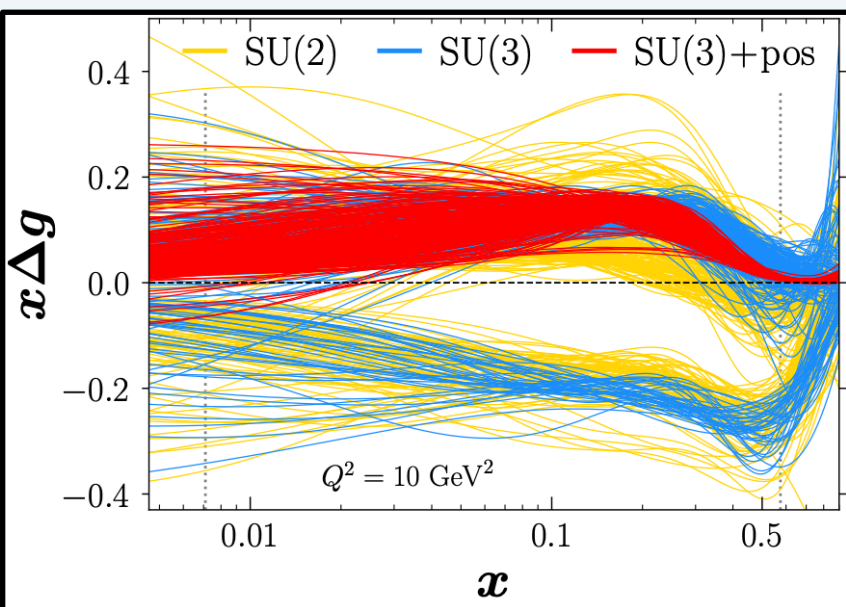
$$\vec{l} + \vec{N} \rightarrow l' + X$$



$$\Delta G_{\text{trunc}} = \int_{10^{-4}}^1 dx \Delta g(x)$$

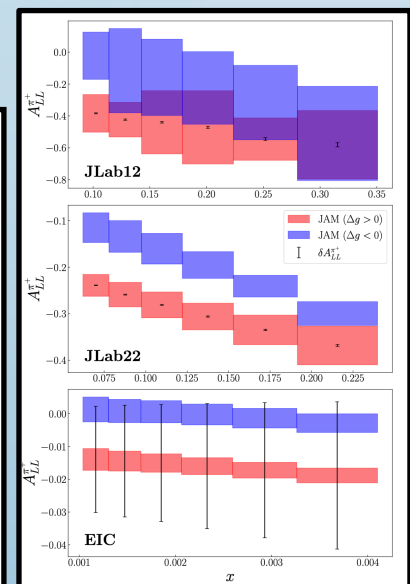
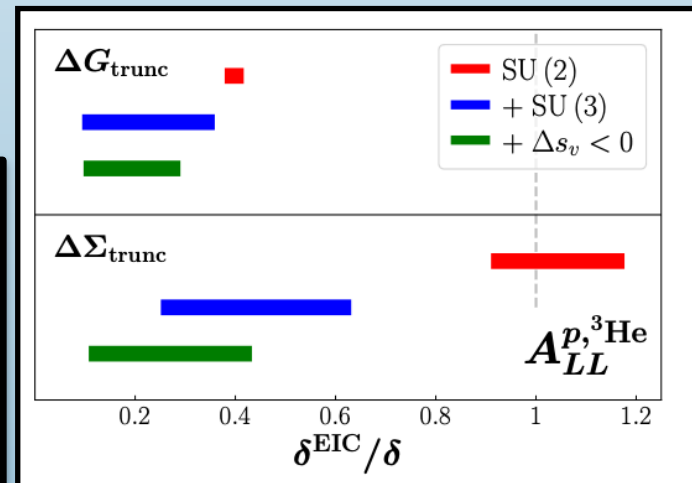
Current JAM analyses have two gluon solutions

New data from RHIC may help distinguish them



Nonzero sea asymmetry

Future data from the EIC and JLab should provide new information



# Extra Slides

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Parameterize PDFs at input scale  $Q_0^2 = m_c^2$

$$f_i(x) = Nx^\alpha(1-x)^\beta(1+\gamma\sqrt{x}+\eta x)$$

Evolve PDFs using DGLAP

$$\frac{d}{d \ln(\mu^2)} f_i(x, \mu) = \sum_j \int_x^1 \frac{dz}{z} P_{ij}(z, \mu) f_j\left(\frac{x}{z}, \mu\right)$$

Calculate Observables

$$d\sigma^{pp} = \sum_{ij} H_{ij}^{pp} \otimes f_i \otimes f_j$$

Mellin Space Techniques

$$d\sigma^{pp} = \sum_{ijkl} \frac{1}{(2\pi i)^2} \int dN \int dM \tilde{f}_j(N, \mu_0) \tilde{f}_l(M, \mu_0) \\ \otimes \left[ x_1^{-N} x_2^{-M} \tilde{\mathcal{H}}_{ik}^{pp}(N, M, \mu) U_{ij}^S(N, \mu, \mu_0) U_{kl}^S(M, \mu, \mu_0) \right]$$



Experimentally measured  
cross-section

**“Soft part” (process independent)**  
Describes internal structure

$$\sigma = \sum_{ij} H_{ij} \otimes f_i \otimes f_j + \mathcal{O}(1/Q)$$

**“Hard part” (process dependent)**  
Cross-section at parton level  
Calculated in perturbative QCD

Now that the observables have been calculated...

$$\chi^2(\mathbf{a}) = \sum_{i,e} \left( \frac{d_{i,e} - \sum_k r_e^k \beta_{i,e}^k - T_{i,e}(\mathbf{a})/N_e}{\alpha_{i,e}} \right)^2 + \sum_k (r_e^k)^2 + \left( \frac{1 - N_e}{\delta N_e} \right)^2$$

Diagram illustrating the components of the chi-squared function  $\chi^2(\mathbf{a})$ :

- Data** points to the first term:  $\sum_{i,e} \left( \frac{d_{i,e} - \sum_k r_e^k \beta_{i,e}^k - T_{i,e}(\mathbf{a})/N_e}{\alpha_{i,e}} \right)^2$
- Theory** points to the second term:  $\sum_k (r_e^k)^2$
- Normalization** points to the third term:  $\left( \frac{1 - N_e}{\delta N_e} \right)^2$
- Uncorrelated Uncertainties** points to the denominator  $\alpha_{i,e}$  in the first term.
- Correlated Uncertainties** points to the coefficient  $\alpha_{i,e}$  in the first term.
- Normalization Uncertainty** points to the third term.

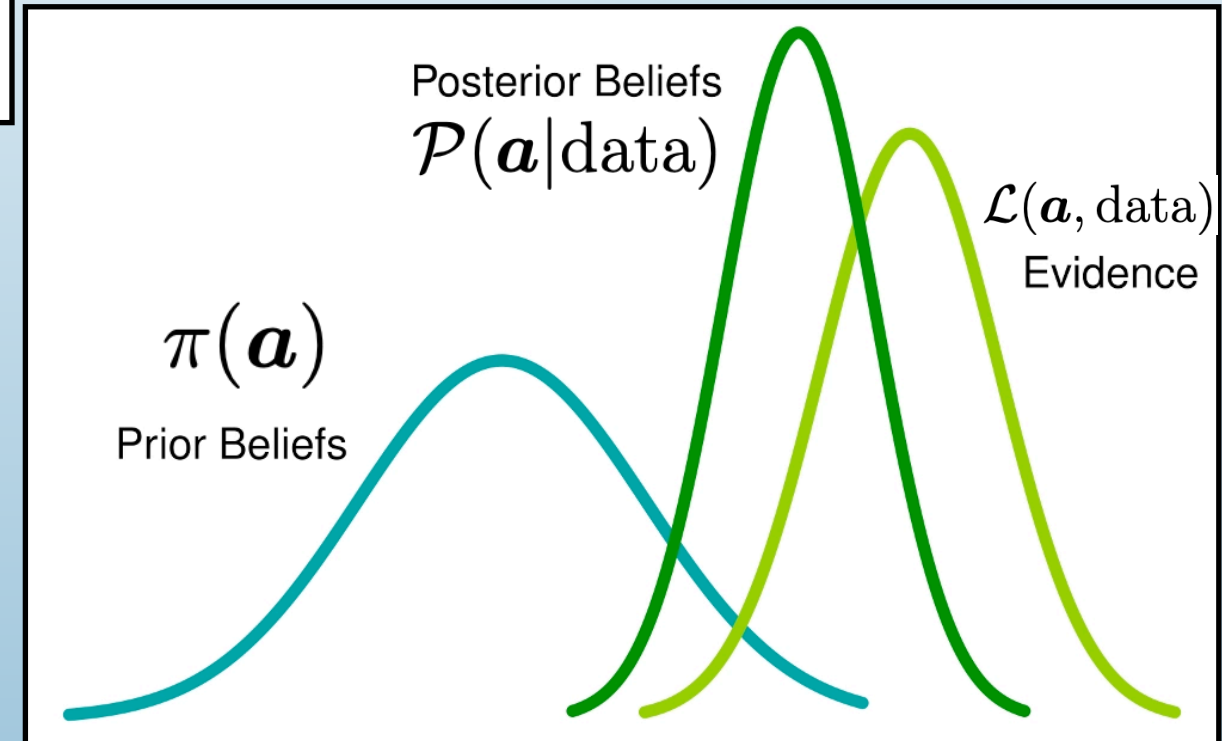
Now that we have calculated  $\chi^2(\mathbf{a}, \text{data}) \dots$

Likelihood Function

$$\mathcal{L}(\mathbf{a}, \text{data}) = \exp \left( -\frac{1}{2} \chi^2(\mathbf{a}, \text{data}) \right)$$

Bayes' Theorem

$$\mathcal{P}(\mathbf{a}|\text{data}) \sim \mathcal{L}(\mathbf{a}, \text{data}) \pi(\mathbf{a})$$



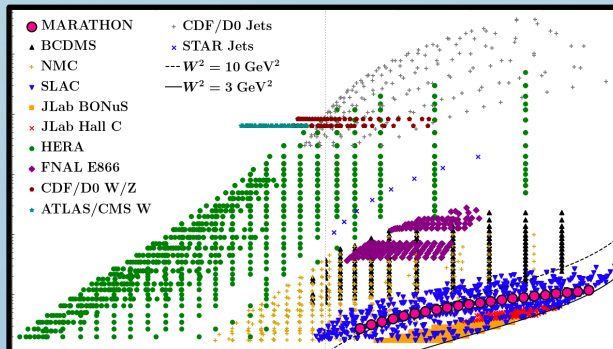
Pseudo-Data

$$\tilde{\sigma} = \sigma + N(0,1) \alpha$$

Uncorrelated  
Uncertainties

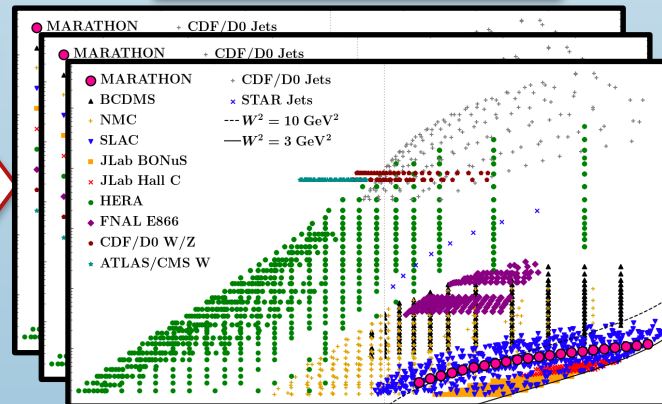
Data

Original Data

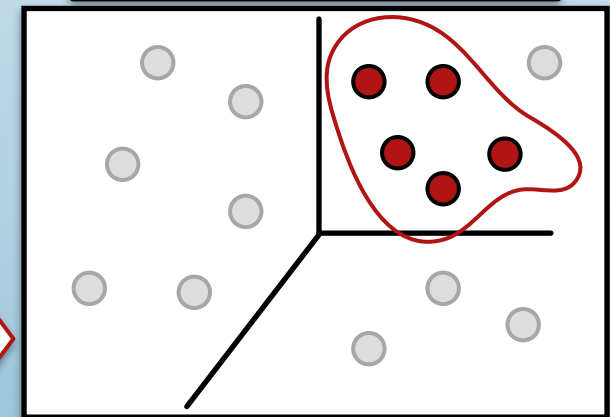


DR

Replica Data

Maximum  
LikelihoodMaximum  
LikelihoodMaximum  
Likelihood

Parameter Space





For a quantity  $O(\mathbf{a})$ : (for example, a PDF at a given value of  $(x, Q^2)$ )

$$E[O] = \int d^n a \, \rho(\mathbf{a} | \text{data}) \, O(\mathbf{a})$$

$$V[O] = \int d^n a \, \rho(\mathbf{a} | \text{data}) \, [O(\mathbf{a}) - E[O]]^2$$

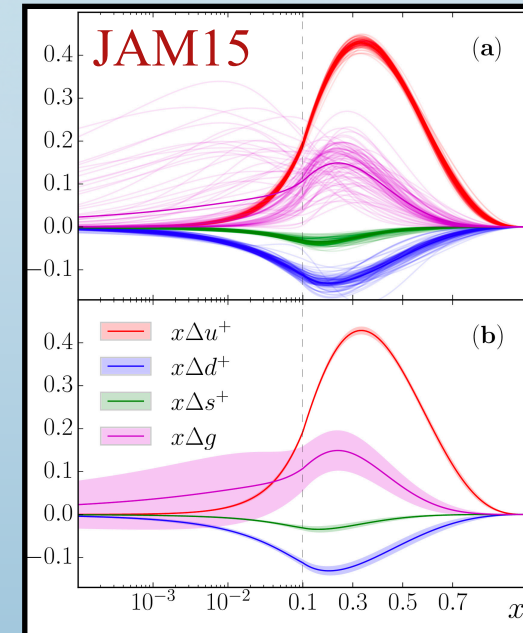
Build an MC ensemble

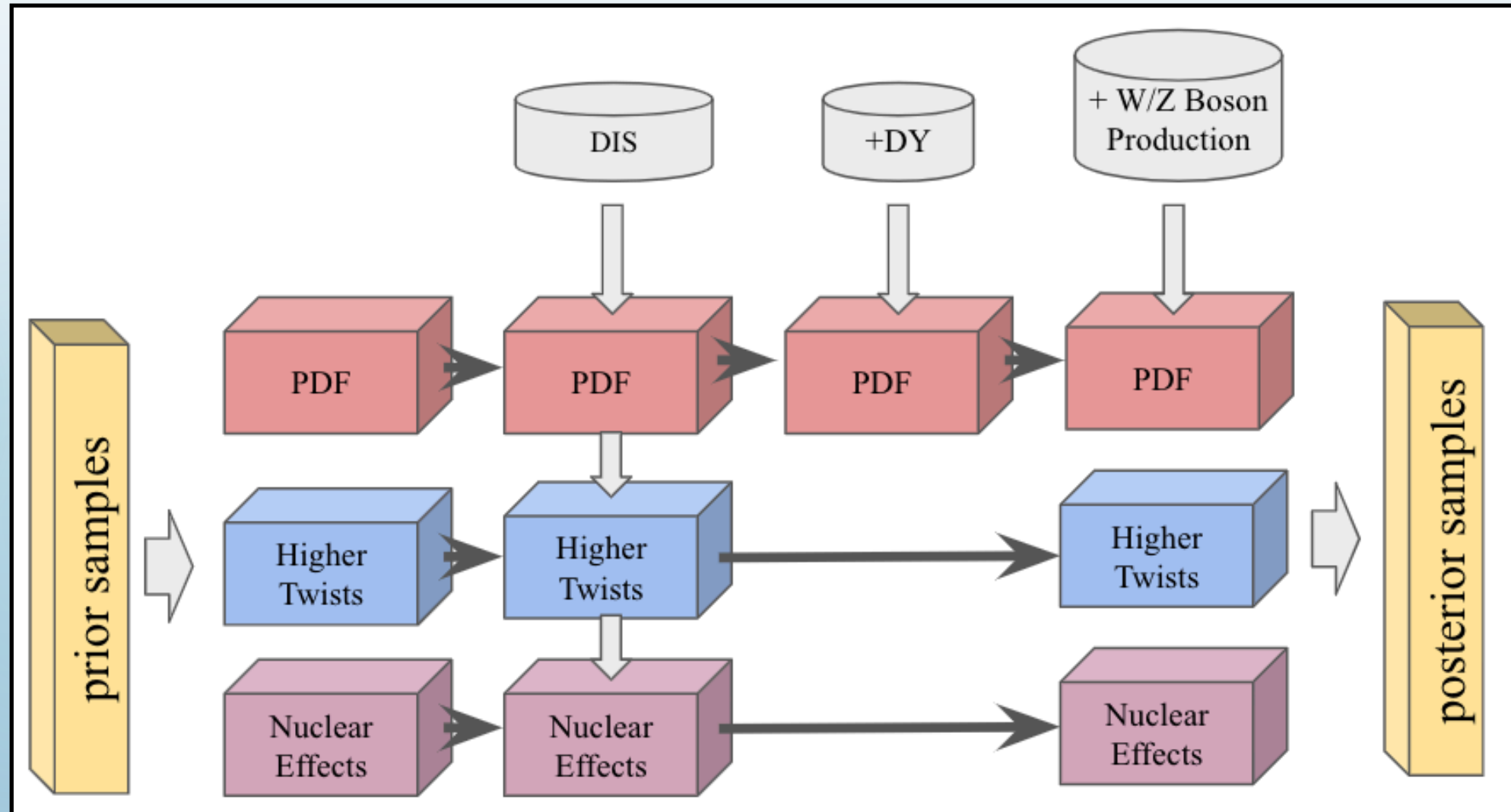
$$E[O] \approx \frac{1}{N} \sum_k O(\mathbf{a}_k)$$

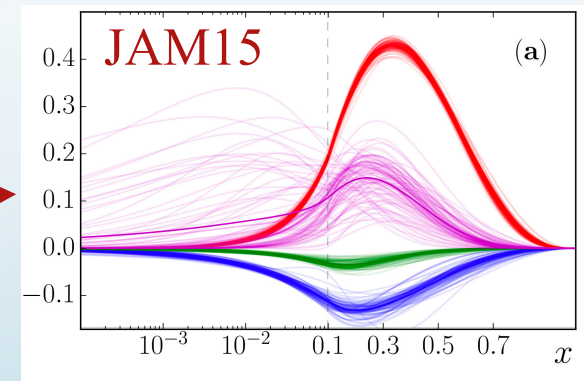
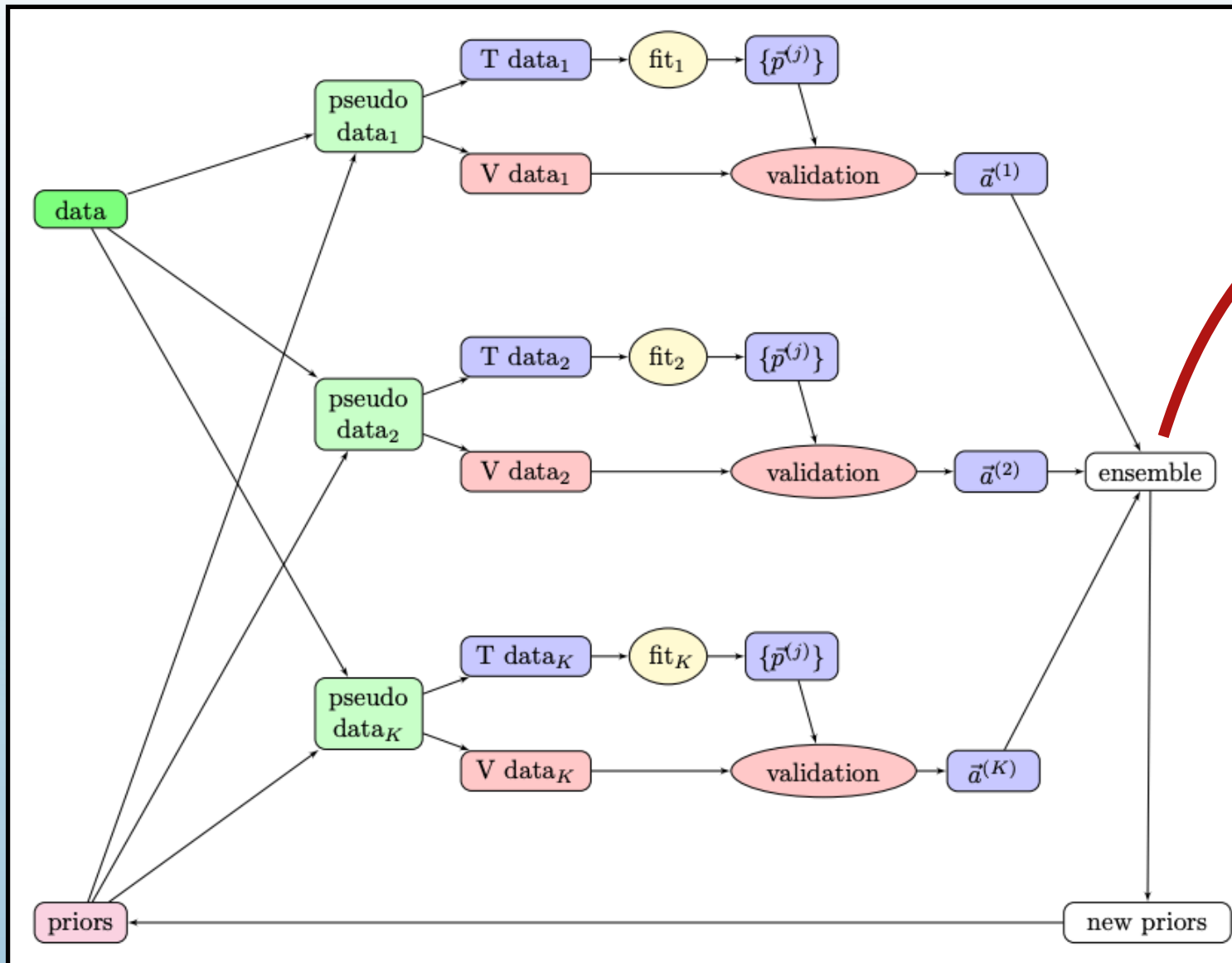
$$V[O] \approx \frac{1}{N} \sum_k [O(\mathbf{a}_k) - E[O]]^2$$


Exact, but  
 $n = \mathcal{O}(100)$ !

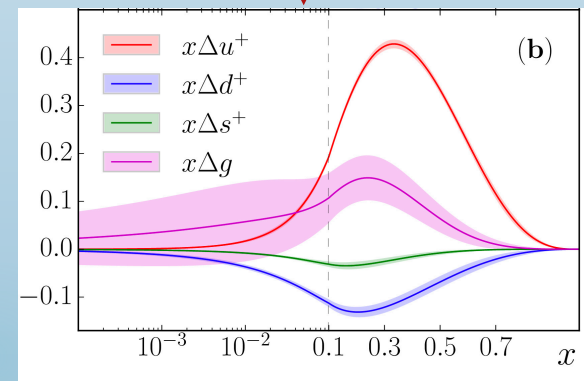
Average over  $k$  sets  
of the parameters  
(replicas)








$$E[O] \approx \frac{1}{N} \sum_k O(a_k)$$
$$V[O] \approx \frac{1}{N} \sum_k [O(a_k) - E[O]]^2$$



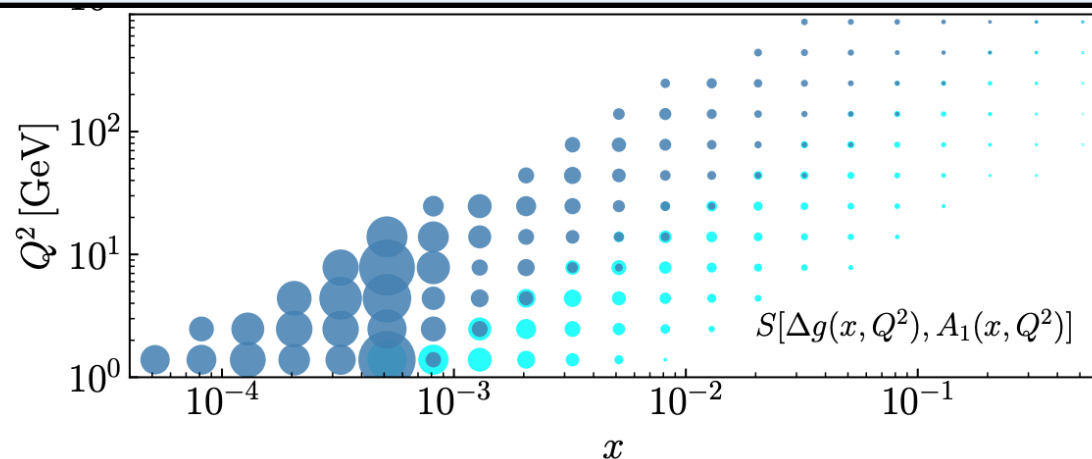
## Revisiting helicity parton distributions at a future electron-ion collider

#2

Ignacio Borsa (U. Buenos Aires), Gonzalo Lucero (U. Buenos Aires), Rodolfo Sassot (U. Buenos Aires), Elke C. Aschenauer (Brookhaven Natl. Lab.), Ana S. Nunes (Brookhaven Natl. Lab.) (Jul 16, 2020)

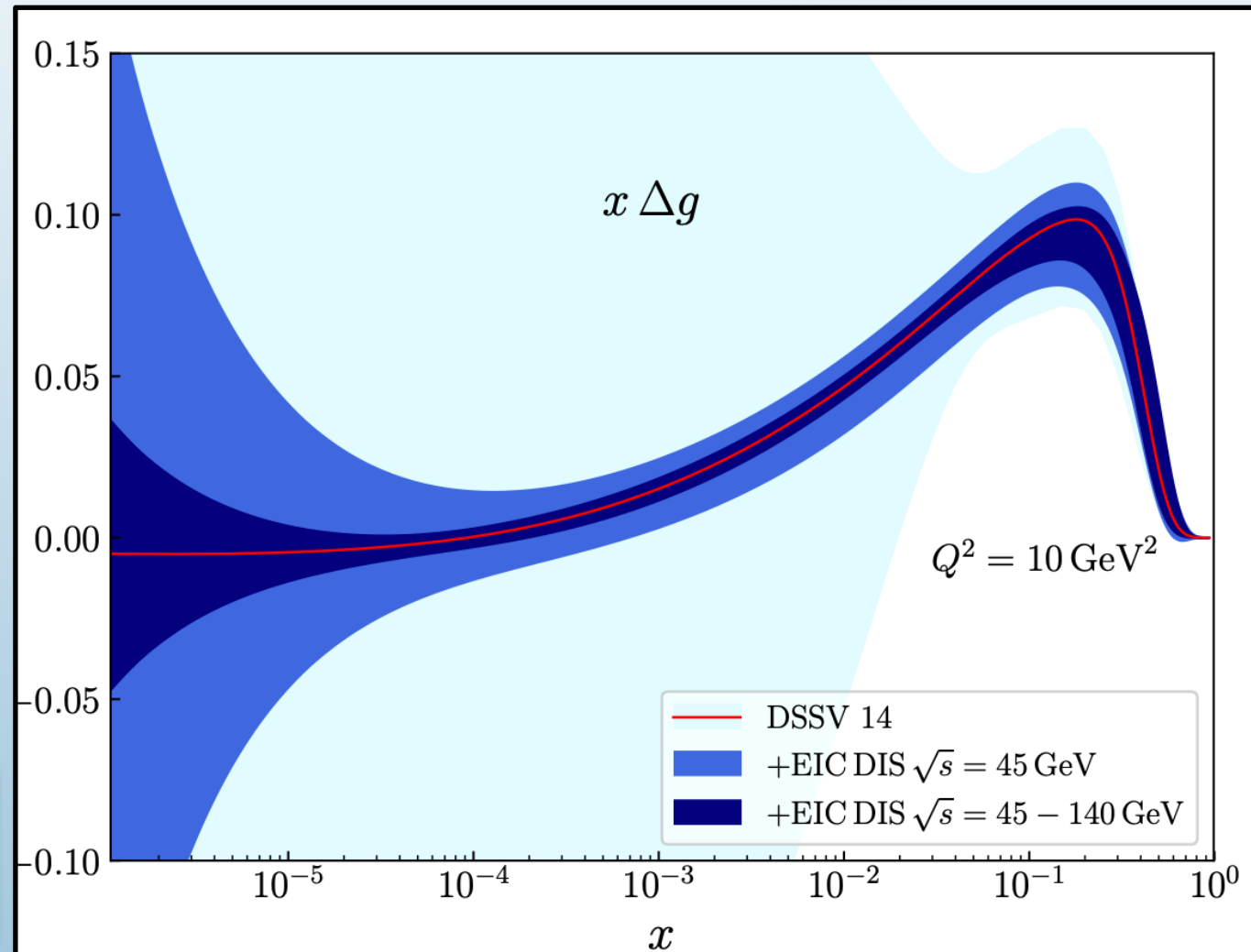
Published in: *Phys.Rev.D* 102 (2020) 9, 094018 • e-Print: [2007.08300](#) [hep-ph]

$$\vec{l} + \vec{N} \rightarrow l' + X$$



Sensitivity of  $A_1$  to  $\Delta g$

Large impact on  $\Delta g$  predicted, especially below  $x \approx 0.01$





## Positivity and renormalization of parton densities

#1

John Collins ([Penn State U.](#)), Ted C. Rogers ([Old Dominion U.](#) and [Jefferson Lab](#)), Nobuo Sato ([Jefferson Lab](#)) (Nov 1, 2021)

Published in: *Phys.Rev.D* 105 (2022) 7, 076010 • e-Print: [2111.01170](#) [hep-ph]

As regards the positivity issue itself, there are several points to make. First, we emphasize that we have not argued that  $\overline{\text{MS}}$  pdfs *must* be negative for any particular choice of scales or  $\mu_{\overline{\text{MS}}}$ . Rather we proved that nothing in the definition of pdfs or in the factorization theorems themselves excludes negativity as a possibility, especially at low or moderate input scales. But we did show arguments that indicate that certain generic situations do tend to lead to negative pdfs of partons with small pdfs, notably for non-valence quarks. Giving a full theoretical answer to the question of whether a particular pdf turns negative depends on its large distance/low energy non-perturbative properties, as the sensitivity to mass scales in the example of Sec. VIII illustrates. Also, the failure of