

PION NUCLEUS DRELL-YAN PROCESS

AND

PARTON TRANSVERSE MOMENTUM IN THE PION

JLab Theory Seminar

9/5/18

A. Courtoy

**Instituto de Física
Universidad Nacional Autónoma de México
(IFUNAM)**



Pion DY

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Pion DY

OUTLINE

- Drell-Yan in πN scattering
- Drell-Yan with transverse momentum
 - Pion dynamics
 - Effects on DY cross section
- Outlook

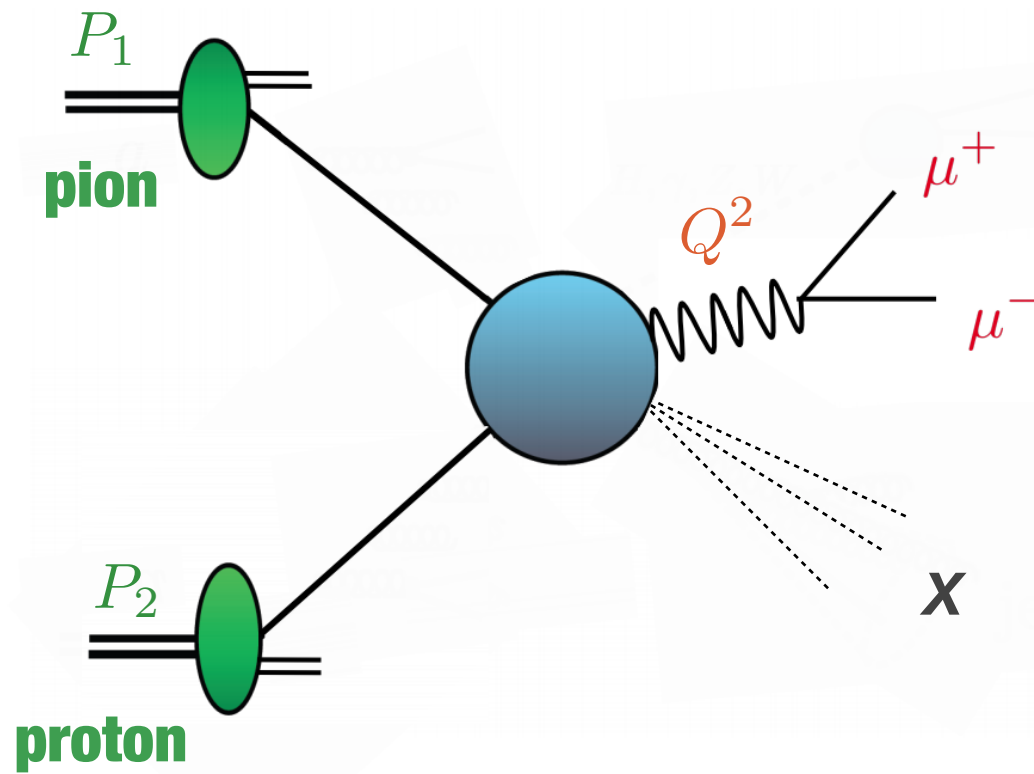
OUTLINE

- Drell-Yan in πN scattering
- Drell-Yan with transverse momentum
 - Pion dynamics
 - Effects on DY cross section
- Outlook

Based on
Eur.Phys.J. C78 (2018) no.8, 644
with F.A. Ceccopieri, S. Noguera & S. Scopetta

FOCUS ON THE PION

Pion DY



$$Q^2 = M^2$$

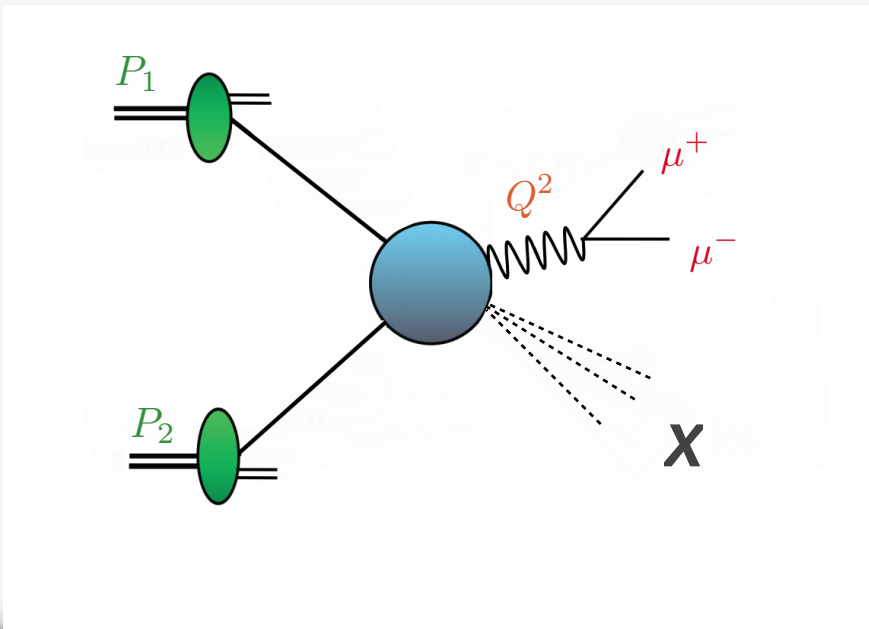
$$s = 2P_1 \cdot P_2$$

$$\tau = \frac{Q^2}{s} \equiv \text{finite as } Q^2, s \rightarrow \infty$$

Pion DY

Pion-proton Drell-Yan differential cross-section

$$d\sigma = \sum_{ab} \int dx_a \int dx_b f_a^\pi(x_a, \mu) f_b(x_b, \mu) d\hat{\sigma}_{ab}(x_a P_a, x_b P_b, Q, \alpha_s(\mu), \mu)$$



$$x_a x_b = \tau \qquad Q^2 = M^2$$
$$s = 2P_1 \cdot P_2$$

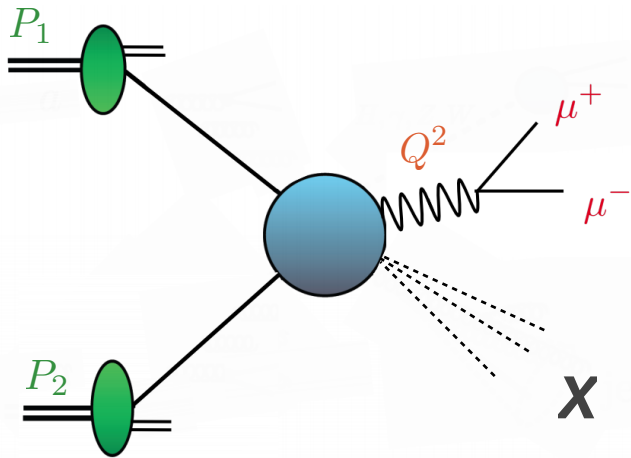
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Pion PDF



$$x_a x_b = \tau \quad \begin{aligned} Q^2 &= M^2 \\ s &= 2P_1 \cdot P_2 \end{aligned}$$

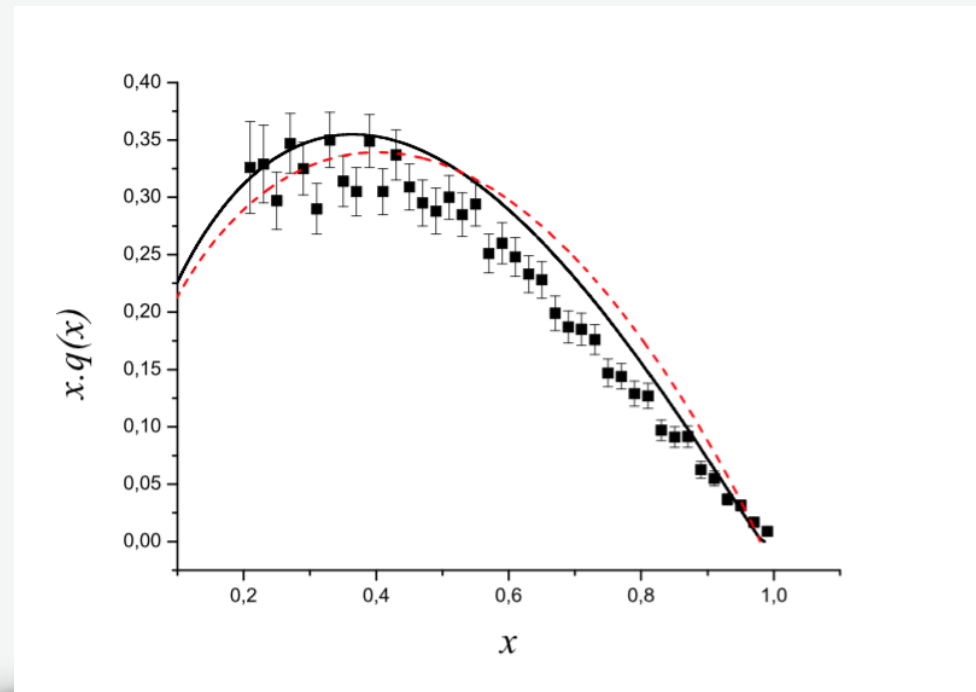
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Pion DY

Pion-proton Drell-Yan: main source of information on pion structure

E615 extraction
(joint proton and pion PDF)

Momentum fraction carried by valence quarks
→ allows Q_0 fixing



Nambu - Jona-Lasinio (NJL)

$Q_0 = 0.29\text{GeV}$, for the LO evolution ;
 $Q_0 = 0.43\text{GeV}$, for the NLO evolution .

$\Lambda_{\text{LO}} = 0.174\text{ GeV}$
 $\Lambda_{\text{NLO}} = 0.246\text{ GeV}$

Pion DY

THE PION IN NJL

Distribution Functions as Functions of x

Calculation in QCD not possible \rightarrow Nonperturbative Objects

Approaching QCD by Models, Effective theories,... \rightarrow not an exact calculation

Pion \rightarrow Chiral Low-Energy Models

Why NJL?

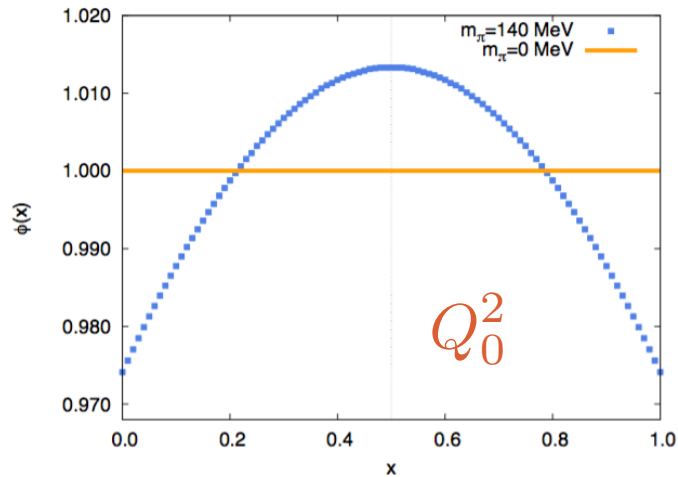
- Quarks degrees of freedom
- Relation **current** \leftrightarrow **constituent** quarks
- Pion as a **Goldstone** mode
- Pion as a **Bound-State** in the sense of **Bethe-Salpeter**
- Choice of a **covariant** regularization scheme

Why are we confident about the use of NJL?

- Calculations of PDFs in NJL \rightarrow **OK**
- Non perturbative QCD \rightarrow **Evolution of initial PDF**
- Comparison with data \rightarrow **OK**

Long story of successful results and predictions

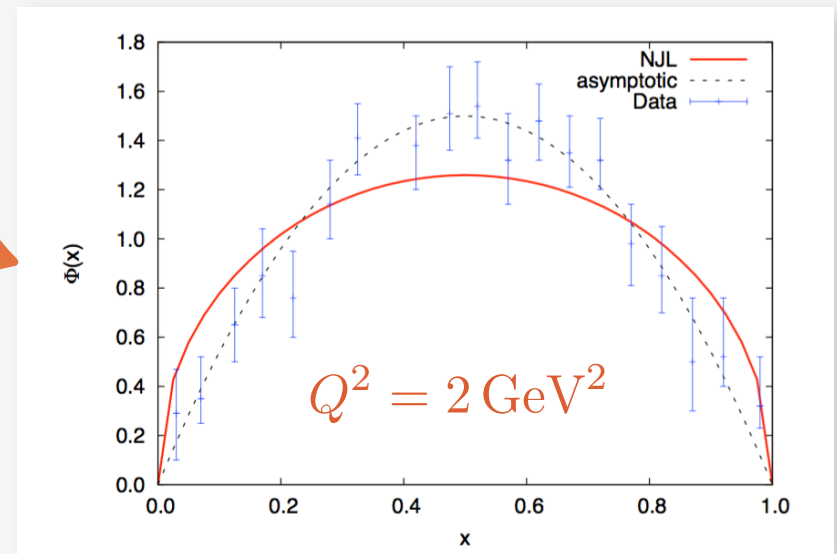
THE PION IN NJL: DISTRIBUTION AMPLITUDE



Mind the scale of y-axis!

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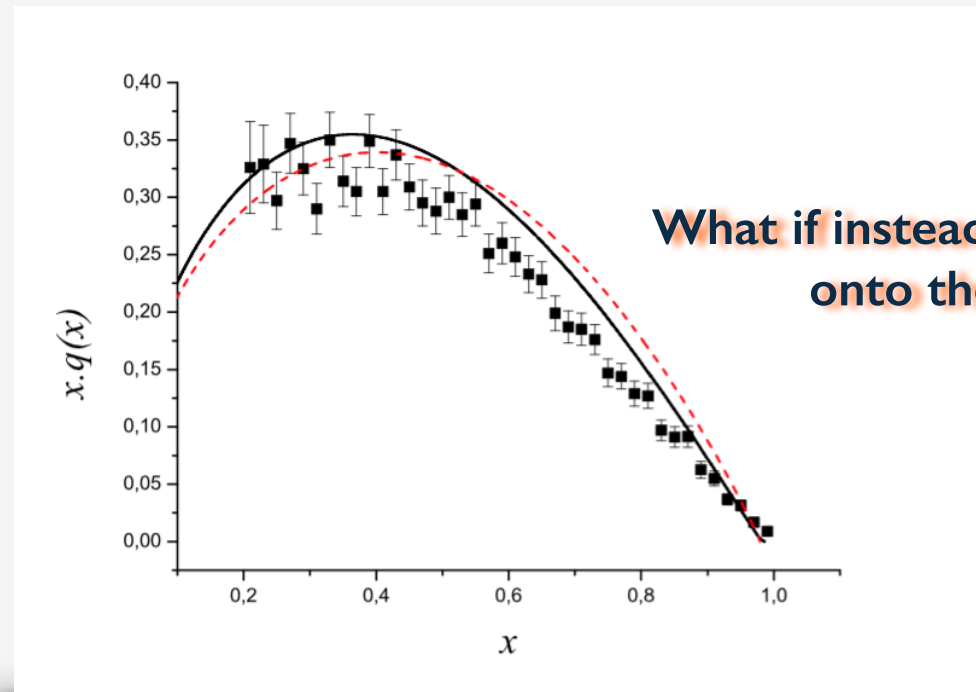


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Pion DY

Determination of NJL's scale

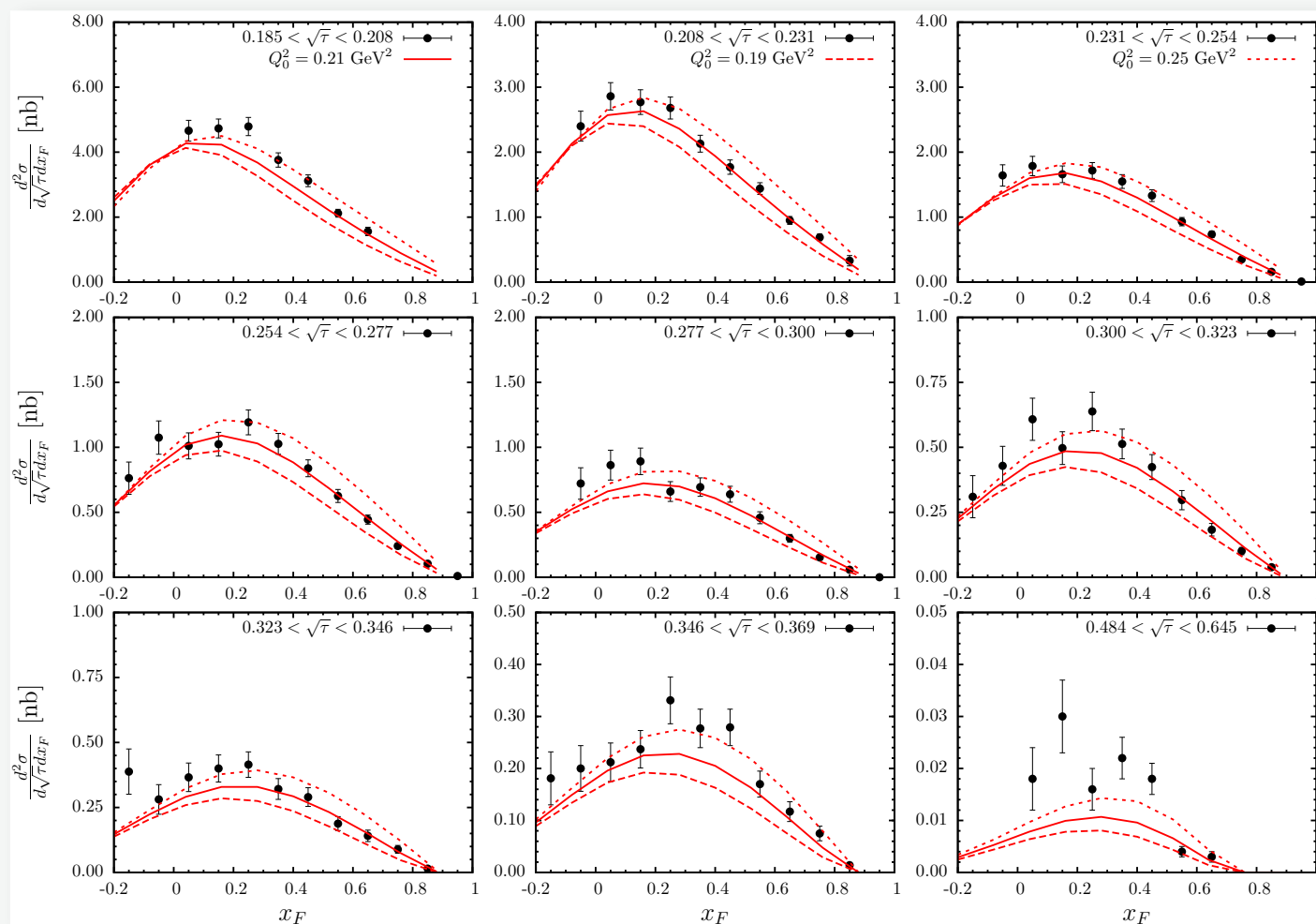
Comparison of integrated X-section
with theory at NLO:

- pion from NJL
- proton from CTEQ6M

We find

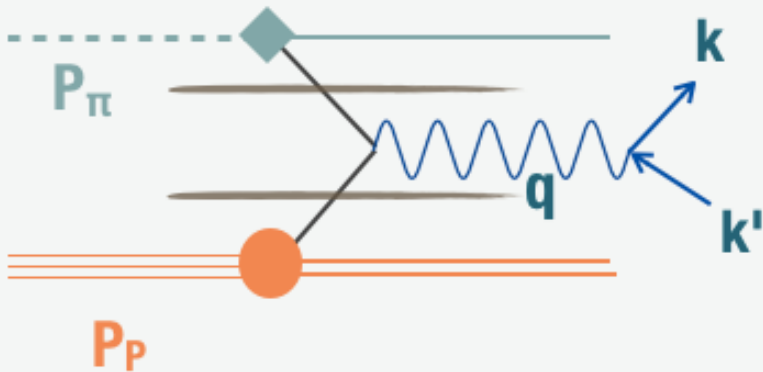
$$Q_0^2=0.21 \text{ GeV}^2 / Q_0=0.46 \text{ GeV}$$

with $\chi^2/\text{dof}=2$



Pion DY

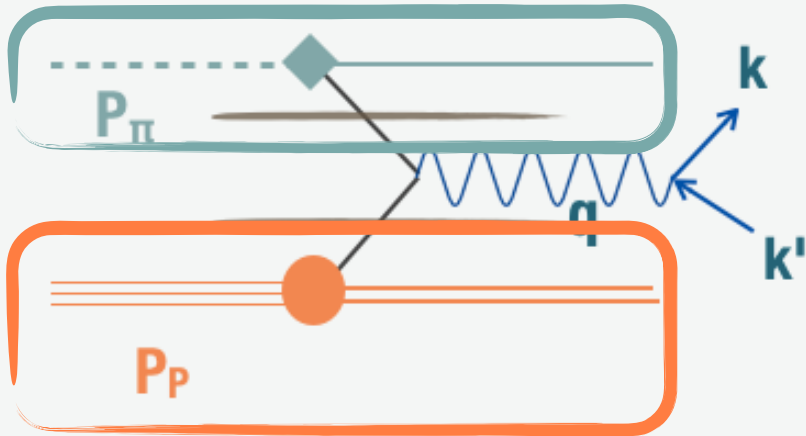
DRELL-YAN WITH TRANSVERSE MOMENTUM



With measured Q_T of order Q

$$\frac{d\sigma}{dQ^2 dy dQ_T^2} = \frac{4\pi^2\alpha^2}{9Q^2 s} \sum_{a,b} \int_{x_\pi}^1 \frac{d\xi_\pi}{\xi_\pi} \int_{x_P}^1 \frac{d\xi_P}{\xi_P} T_{ab}(\cdots) f_{a/\pi}(\xi_\pi, \mu) f_{b/P}(\xi_P, \mu)$$

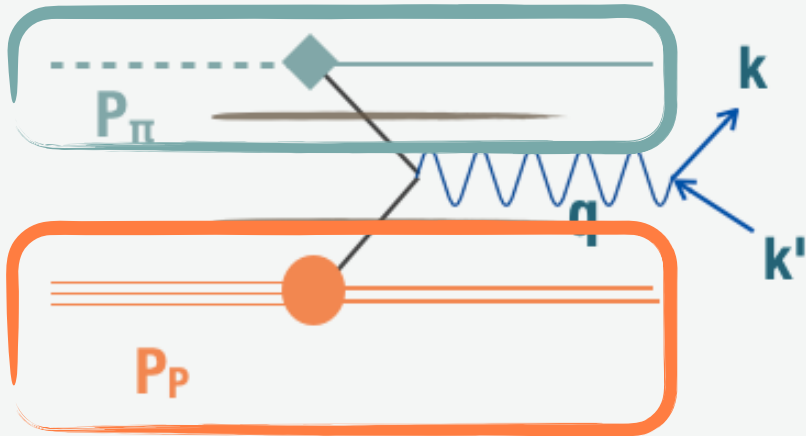
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$$q^2 = (k + k')^2$$

$$x_\pi = \frac{Q^2}{2P_\pi \cdot q}, \quad x_P = \frac{Q^2}{2P_P \cdot q}$$

$$\tau = \frac{Q^2}{s} \text{ fixed and finite as } Q^2, s \rightarrow \infty$$

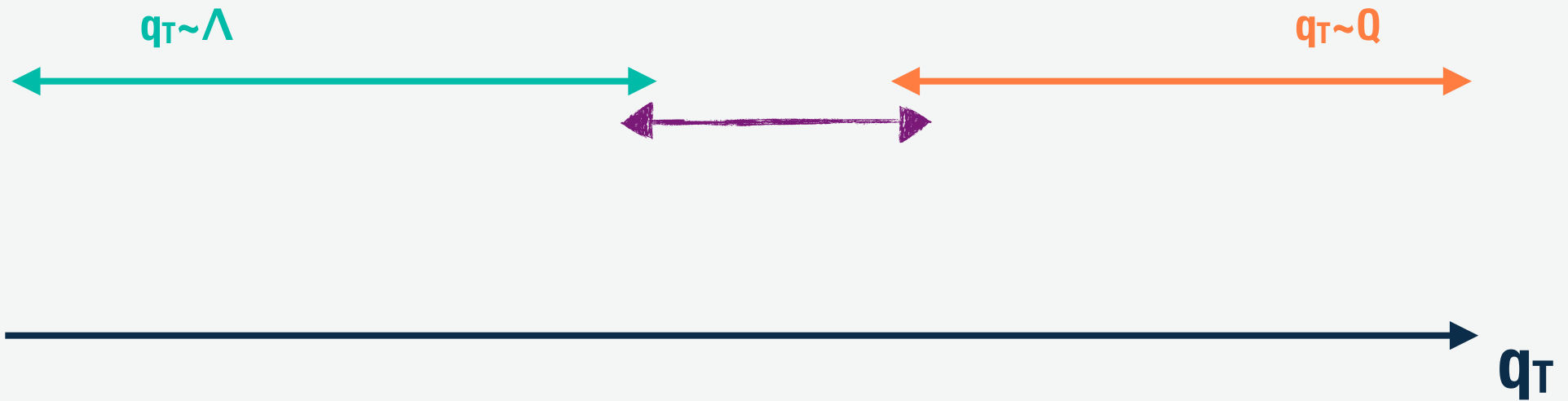
$$q^\mu = (x_\pi P_\pi^+, x_P P_P^-, \vec{q}_T)$$

$$y = \frac{1}{2} \ln \frac{x_\pi}{x_P}$$

Pion DY

REGION OF TRANSVERSE MOMENTUM

$$Q^2 \gg \Lambda^2$$

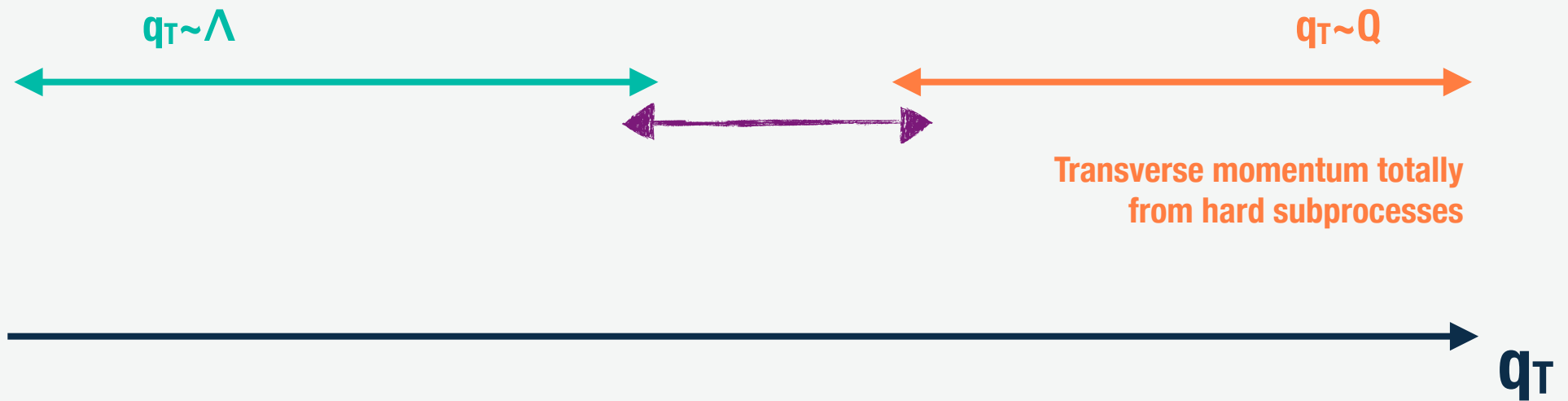


[Collins, Soper & Sterman, Nucl.Phys.B250]

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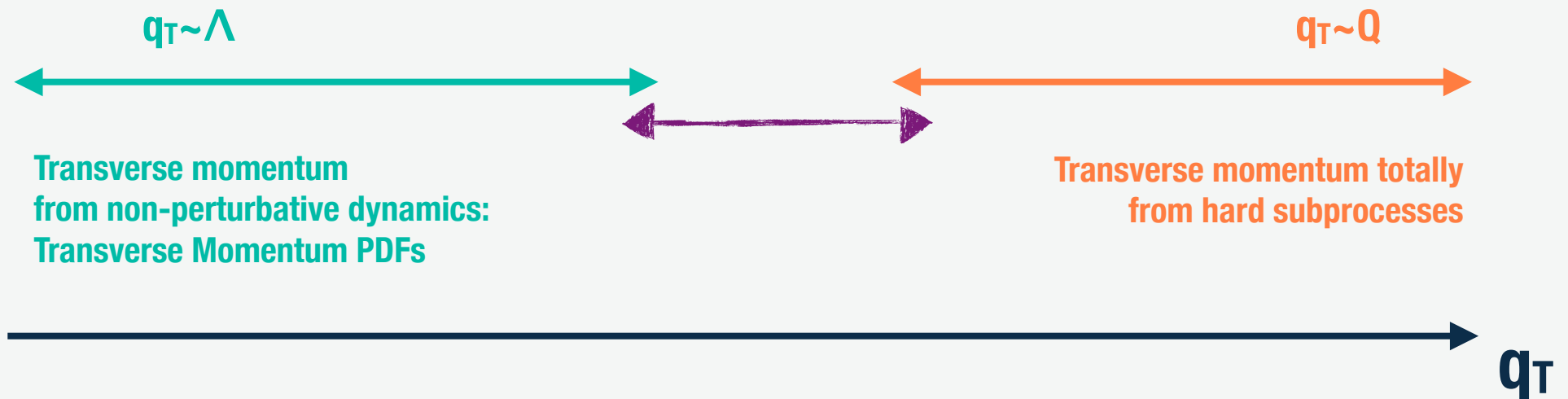


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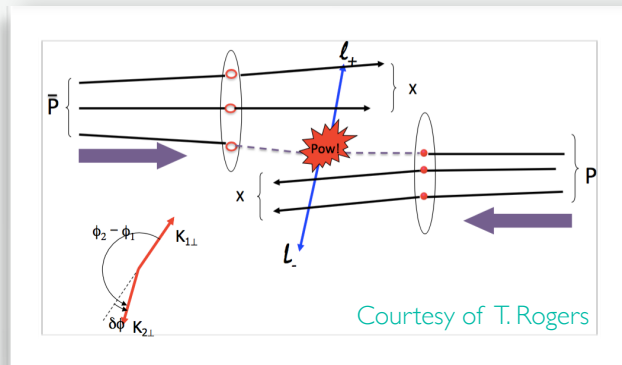


[Collins, Soper & Sterman, Nucl.Phys.B250]

Pion DY

REGION OF TRANSVERSE MOMENTUM

$$Q^2 \gg \Lambda^2$$



$$q_T \sim \Lambda$$

$$q_T \sim Q$$

Transverse momentum
from non-perturbative dynamics:
Transverse Momentum PDFs

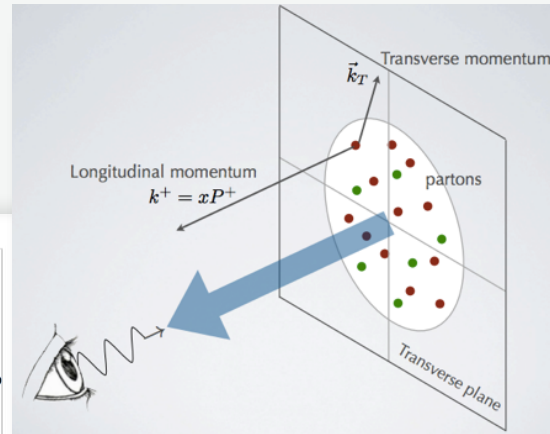
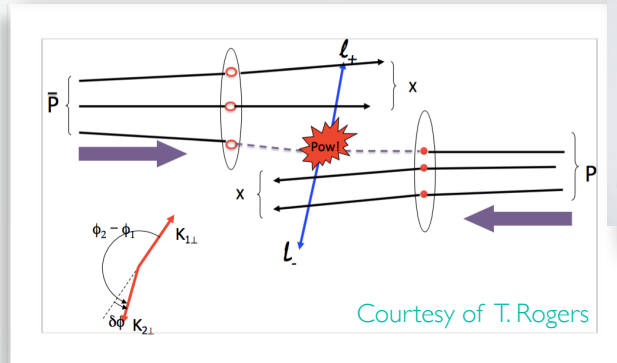
Transverse momentum totally
from hard subprocesses

q_T

[Collins, Soper & Sterman, Nucl.Phys.B250]

Pion DY

REGION OF TRANSVERSE MOMENTUM



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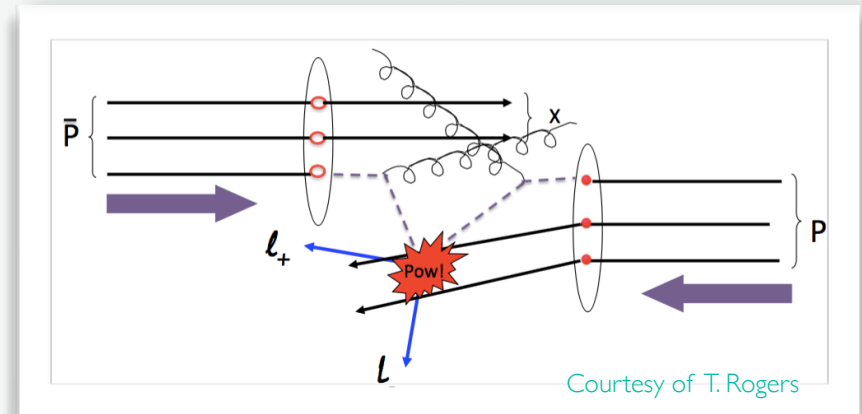
q_T

[Collins, Soper & Sterman, Nucl.Phys.B250]

Pion DY

PERTURBATIVE CORRECTIONS

Q_T appears at NLO



$$\frac{d\sigma}{dQ^2 dy dQ_T^2} = \frac{4\pi^2\alpha^2}{9Q^2 s} \int \frac{d^2b}{2\pi^2} e^{i\vec{Q}_T \cdot \vec{b}} \sum_{a,b} \int_{x_\pi}^1 \frac{d\xi_\pi}{\xi_\pi} \int_{x_P}^1 \frac{d\xi_P}{\xi_P} f_{a/\pi}(\xi_\pi, \mu) f_{b/P}(\xi_P, \mu) \\ \times \sum_j e_j^2 C_{ja}(x_\pi/\xi_\pi, b; Qb; \mu) C_{jb}(x_P/\xi_P, b; Qb; \mu)$$

$$C_{ja}(x_\pi/\xi_\pi, b; Qb; \mu) = \delta_{ja} \delta(x_\pi/\xi_\pi - 1) + \frac{\alpha_s(\mu)}{\pi} C_{ja}^{(1)} + \dots$$

Pion DY

FULL REGION



$$\frac{d\sigma}{dQ^2 dy dQ_T^2} = \frac{4\pi^2 \alpha^2}{9Q^2 s} \int \frac{d^2 b}{2\pi^2} e^{i\vec{Q}_T \cdot \vec{b}} \sum_{a,b} \int_{x_\pi}^1 \frac{d\xi_\pi}{\xi_\pi} \int_{x_P}^1 \frac{d\xi_P}{\xi_P} f_{a/\pi}(\xi_\pi, \mu_b) f_{b/P}(\xi_P, \mu_b) \\ \times \exp \left(-C_F \frac{\alpha_s(q)}{2\pi} \int_{b_0^2/b^2}^{Q^2} \frac{dq^2}{q^2} \left[2 \ln \frac{Q^2}{\mu^2} - 3 \right] + \text{H.O} \right) \\ \times \sum_j e_j^2 C_{ja}(x_\pi/\xi_\pi, b; 2e^{-\gamma}; \mu_b) C_{jb}(x_P/\xi_P, b; 2e^{-\gamma}; \mu_b)$$

Taming $b \sim 1/\Lambda$:

● b-prescription

$$\times e^{S_{\text{NP}}^\pi(b)} e^{S_{\text{NP}}^P(b)}$$

$$\mu_b = 2e^{-\gamma}/b^* \\ b^* = b/\sqrt{1 + b^2/b_{\text{max}}^2}$$

NLL

Pion DY

FULL REGION



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$$\times \sum_j e_j^2 C_{ja}(x_\pi/\xi_\pi, b; 2e^{-\gamma}; \mu_b) C_{jb}(x_P/\xi_P, b; 2e^{-\gamma}; \mu_b)$$

$$\times e^{S_{\text{NP}}^\pi(b)} e^{S_{\text{NP}}^P(b)}$$

Taming $b \sim 1/\Lambda$:

• b-prescription

$$\mu_b = 2e^{-\gamma}/b^*$$

$$b^* = b/\sqrt{1 + b^2/b_{\text{max}}^2}$$

NLL

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FULL REGION



$$\begin{aligned}
 \frac{d\sigma}{dQ^2 dy dq_T^2} &= \frac{4\pi^2 \alpha^2}{9Q^2 s} \int \frac{d^2 b}{2\pi^2} e^{i\vec{q}_T \cdot \vec{b}} \sum_{a,b} \sum_j e_j^2 \\
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 &\times C_{ja} \left(x_\pi / \xi_\pi, \vec{b}; 2e^{-\gamma}; \mu_b \right) C_{jb} \left(x_P / \xi_P, \vec{b}; 2e^{-\gamma}; \mu_b \right)
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 \end{aligned}$$

Ideally, we'd use

- full TMD for both hadrons
- either from pheno. or similar models

But,

- no pheno proton TMD available (when we started this...)
- no model similar to NJL for the proton

NLL

Pion DY

STRATEGY

- use a phenomenologically estimated $f_{b/P}(\xi_P; \mu_b) \times e^{S_{\text{NP}}^P(b)}$
 - PDF from CTEQ6M
 - NP + b-prescription from [Konychev & Nadolsky, Phys. Lett. B 633, 710 (2006)]
- use the pion TMD from the NJL model $f_{a/\pi}(\xi_\pi, \vec{b}; \zeta_\pi, \mu_b)$
 - [Noguera, S. Scopetta, JHEP 1511, 102 (2015)]
 - redefine the hadronic scale of PDF from DY integrated data
 - interpret the k_T -dependence of the model onto the (unintegrated) DY data

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from now on: $e^{S_{\text{NP}}^P(b)} \rightarrow S_{\text{NP}}^P(b)$

THE NON-PERTURBATIVE PART

$$\frac{d\sigma}{dQ^2 dy dQ_T^2} \sim \frac{4\pi^2 \alpha^2}{9Q^2 s} \left\{ (2\pi)^{-2} \int d^2b e^{iQ_T \cdot b} \sum_j e_j^2 \tilde{W}_j(b_*; Q, x_A, x_B)_{\text{pert}} \right. \\ \left. \times \exp \left[-\ln(Q^2/Q_0^2) g_1(b) - g_{j/\Lambda}(x_A, b) - g_{j/B}(x_B, b) \right] \right\}$$

One parameterization of the non-perturbative contribution

Here: $S_{NP}^{\pi W}(b) = S_{NP}^{\pi}(b) \sqrt{S_{NP}^{pp}(b)}$

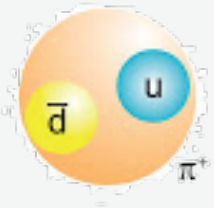
$\bullet S_{NP}^{pp}(b) = \exp\{-[a_1 + a_2 \ln(M/(3.2 \text{ GeV})) + a_3 \ln(100x_1x_2)]b^2\}.$

purely comes from
the dynamics of the model

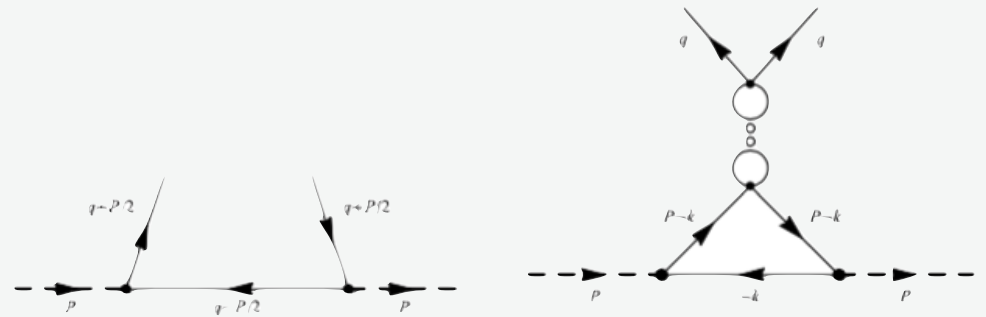
$\bullet b_*(b, b_{\max}) = \frac{b}{\sqrt{1 + \left(\frac{b}{b_{\max}}\right)^2}} \quad \text{with} \quad b_{\max} = 1.5 \text{ GeV}^{-1}$

FULL TRANSVERSE MOMENTUM DEPENDENCE FOR THE PION

$$f(x; \mu) \times \exp(g_{j/P}(b)) = f(x, b; \mu)$$



TMD PDFs



$$f_{1,\pi}(x, k_T^2) = \frac{3}{4\pi^3} g_{\pi qq}^2 \theta(x) \theta(1-x) \sum_{i=0}^2 c_i \times \left\{ \frac{1}{k_T^2 + M_i^2 - m_\pi^2 x(1-x)} + \frac{m_\pi^2 x(1-x)}{[k_T^2 + M_i^2 - m_\pi^2 x(1-x)]^2} \right\}$$

Pion DY

THE PION IN A CHIRAL MODEL

$$f_{\pi}(x, b; \mu) \xrightarrow{\text{chiral lim}} f'_{\pi}(x; \mu) f''_{\pi}(b)$$

Our interpretation: $\exp(g_{j/\pi}(b)) = f''_{\pi}(b)$

→ no “ $g_1(b)$ ” is this model picture

$$\begin{aligned} f''_{\pi}(b) &= \frac{3}{2\pi^2} \left(\frac{m}{f_{\pi}} \right)^2 \sum_{i=0,2} \int dk_T k_T J_0(bk_T) \frac{a_i}{k_T^2 + m_i^2} \\ &= \frac{3}{2\pi^2} \left(\frac{m}{f_{\pi}} \right)^2 \sum_{i=0,2} a_i K_0(m_i b) \end{aligned}$$

THE PION IN A CHIRAL MODEL

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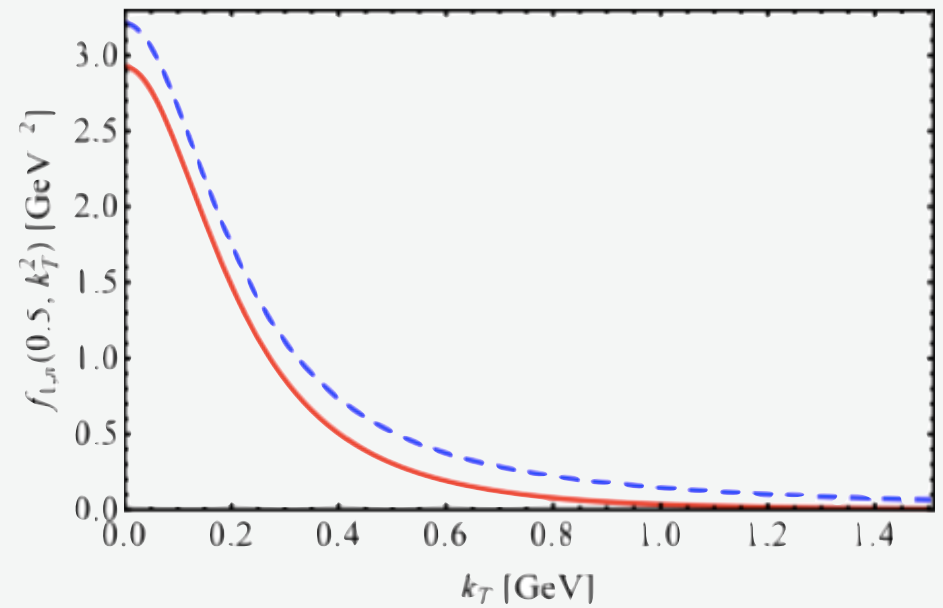
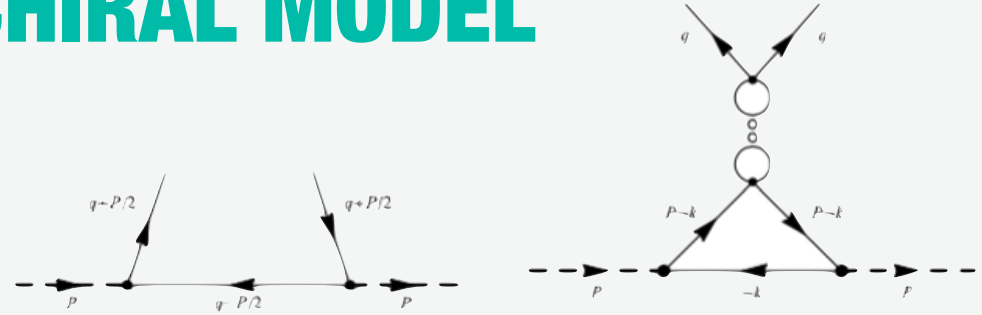
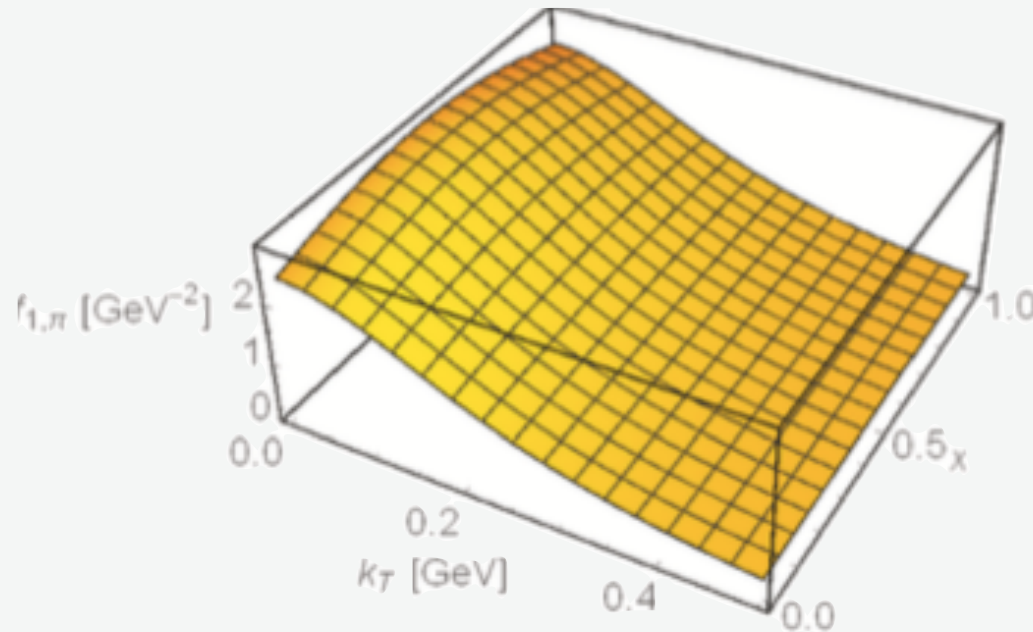
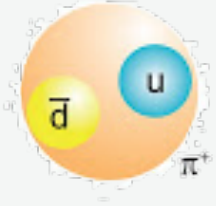
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$$\begin{aligned} f''_{\pi}(b) &= \frac{3}{2\pi^2} \left(\frac{m}{f_{\pi}} \right)^2 \sum_{i=0,2} \int dk_T k_T J_0(bk_T) \frac{a_i}{k_T^2 + m_i^2} \\ &= \frac{3}{2\pi^2} \left(\frac{m}{f_{\pi}} \right)^2 \sum_{i=0,2} a_i K_0(m_i b) \end{aligned}$$

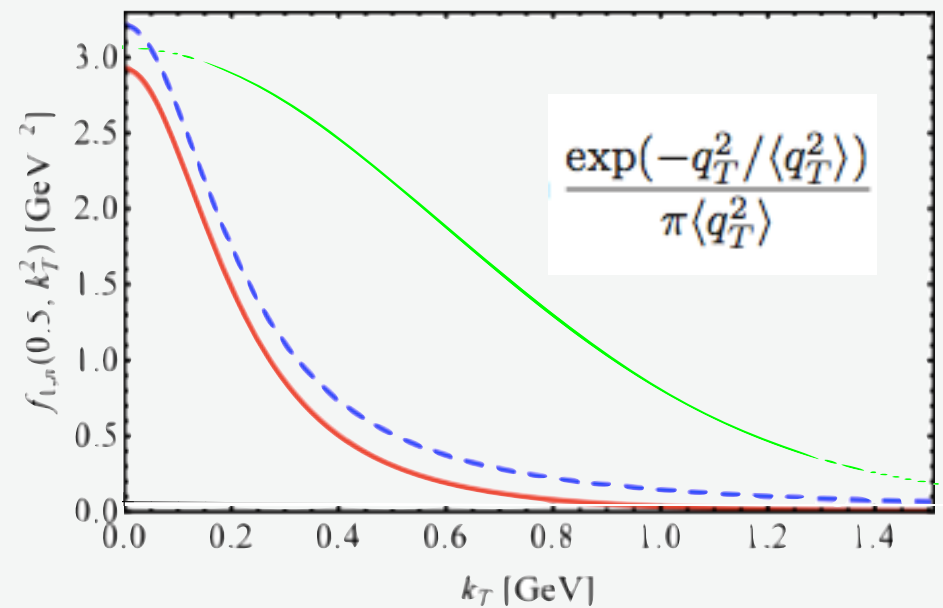
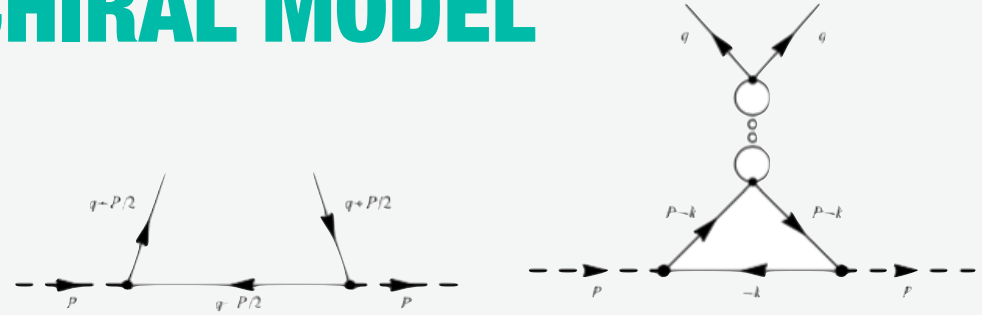
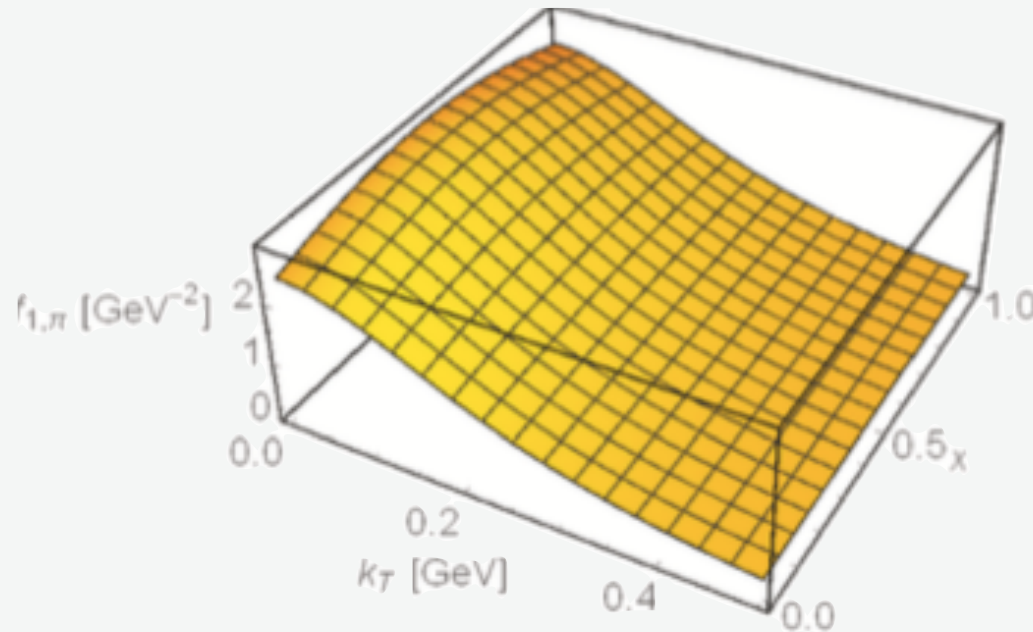
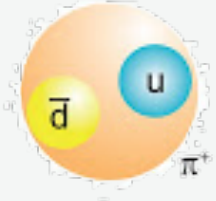
We assumed that factorization of the transverse momentum occurs at Q_0 only.

THE PION IN A CHIRAL MODEL



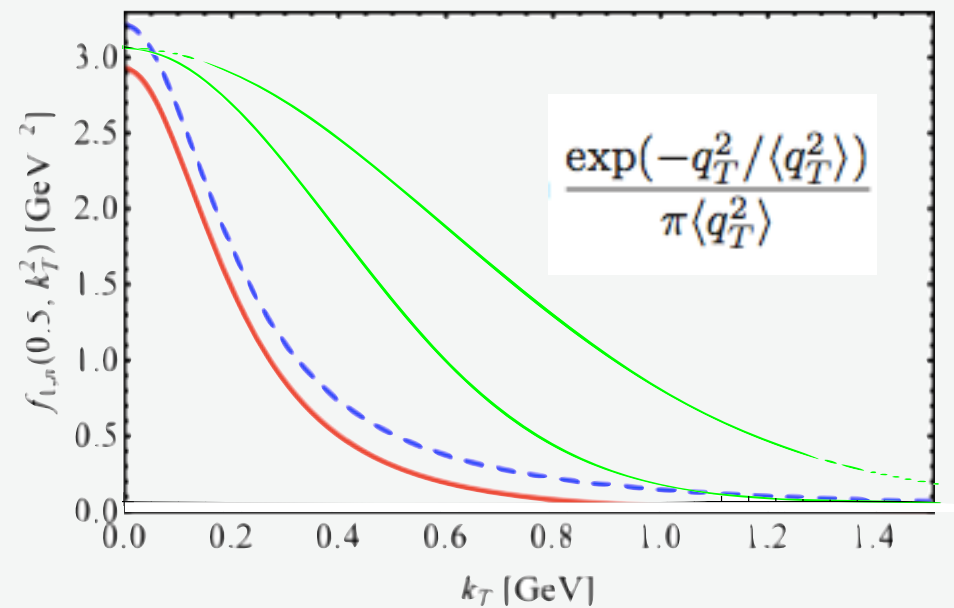
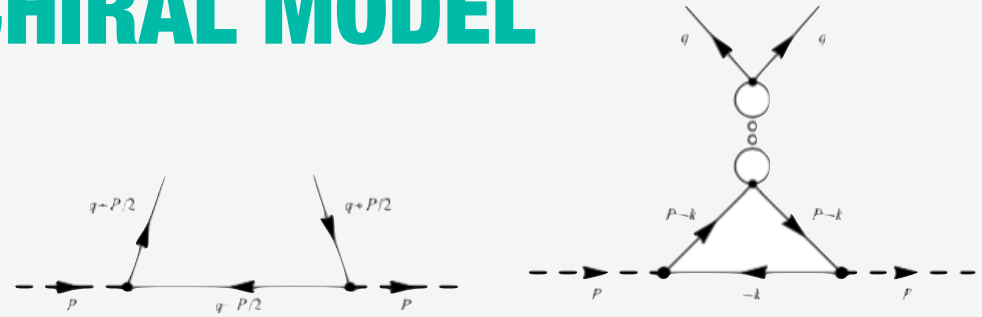
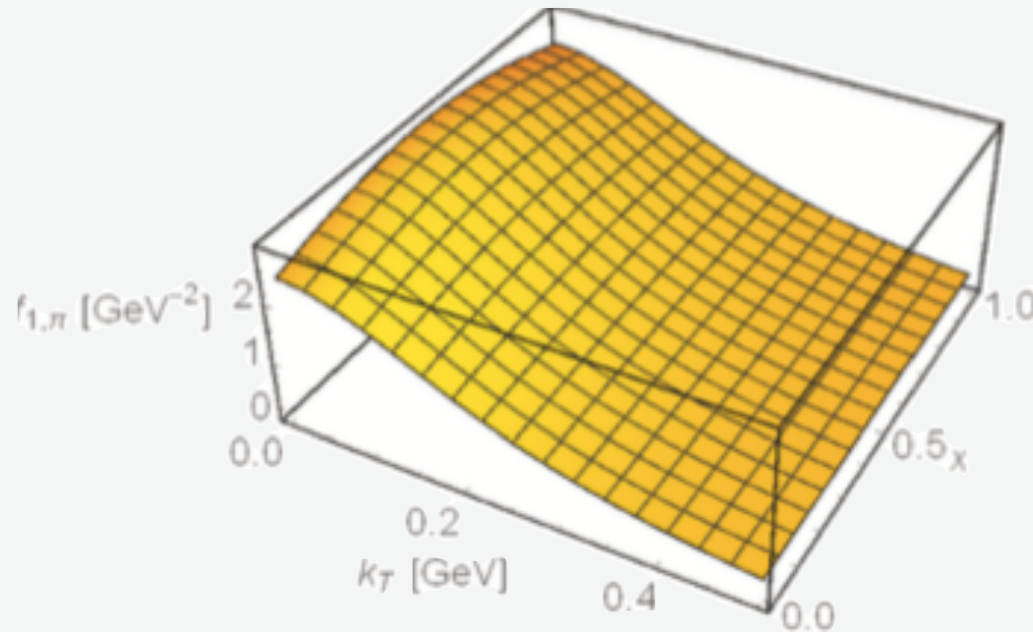
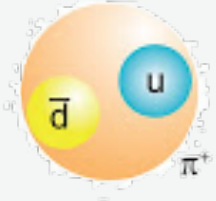
Pion DY

THE PION IN A CHIRAL MODEL



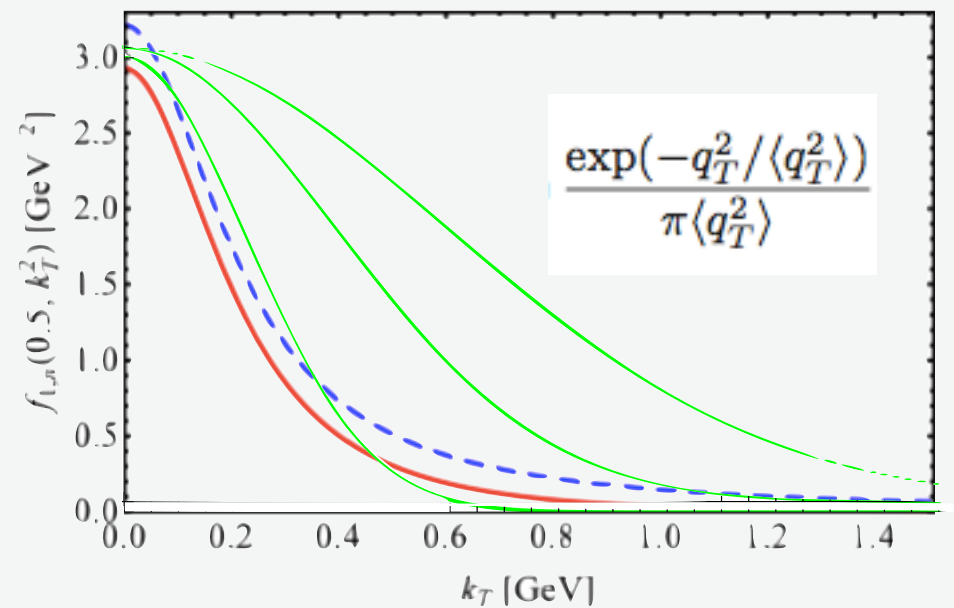
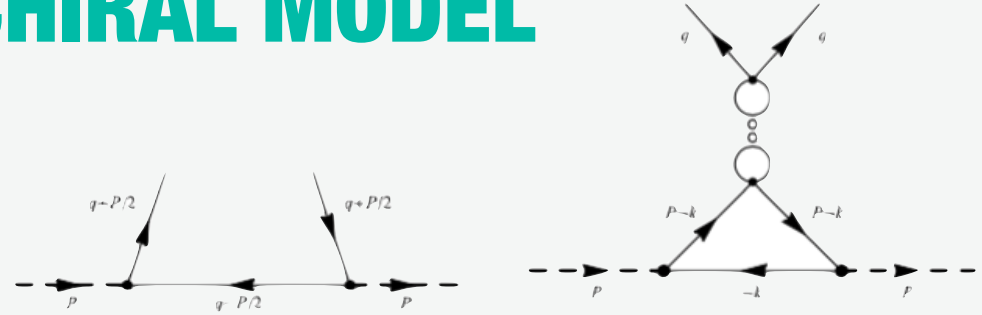
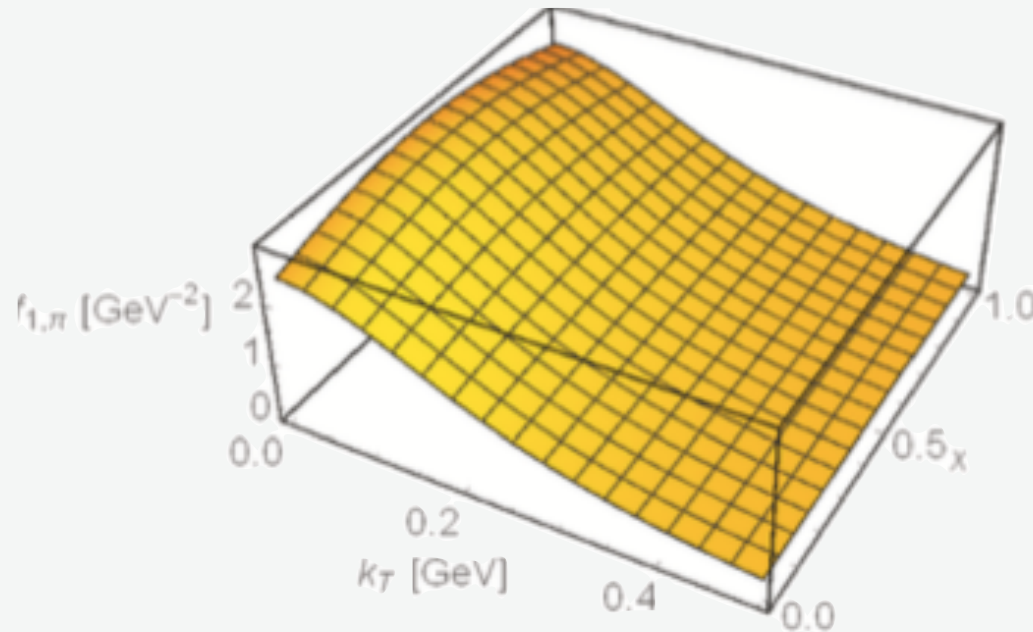
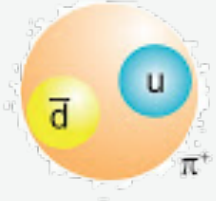
Pion DY

THE PION IN A CHIRAL MODEL



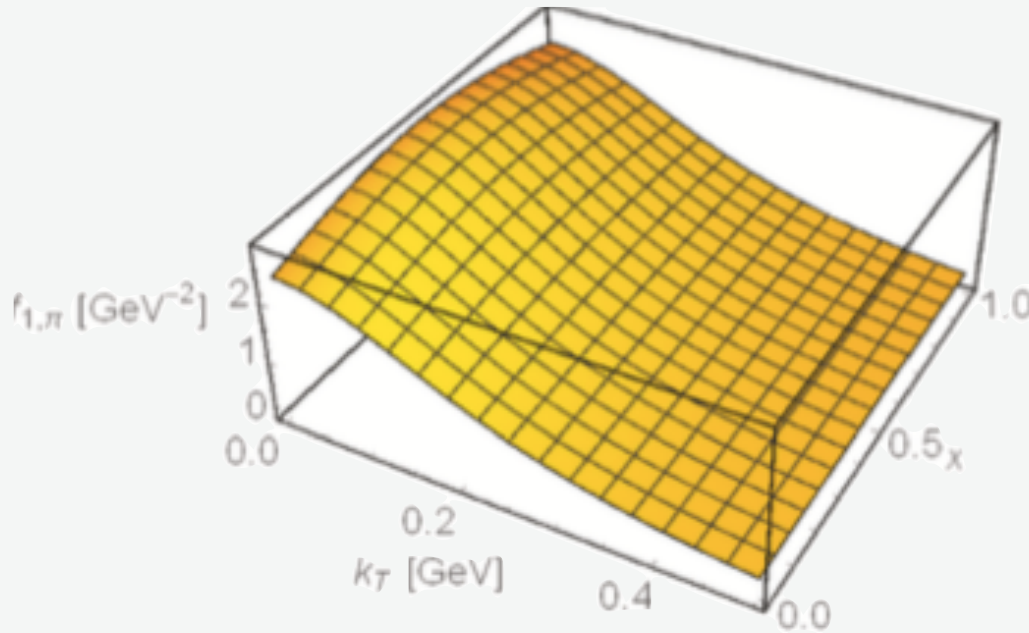
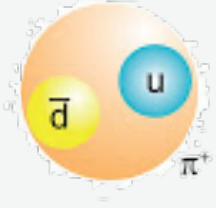
Pion DY

THE PION IN A CHIRAL MODEL

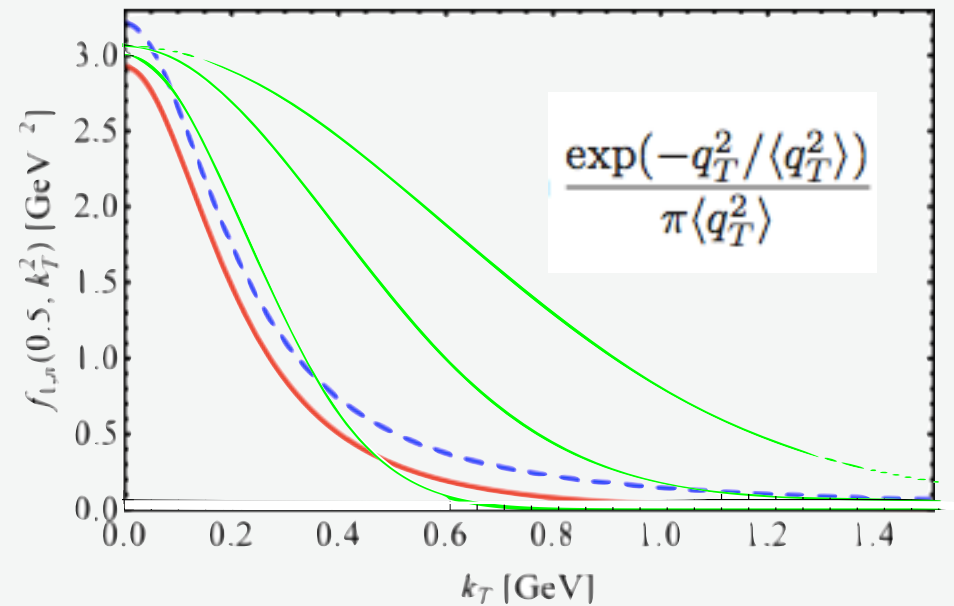
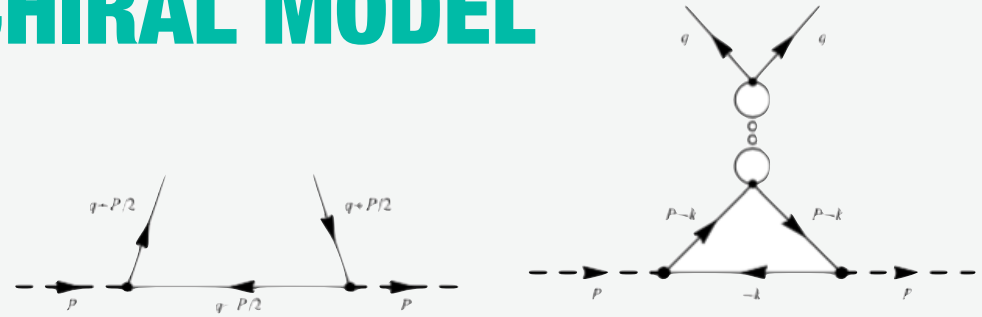


Pion DY

THE PION IN A CHIRAL MODEL

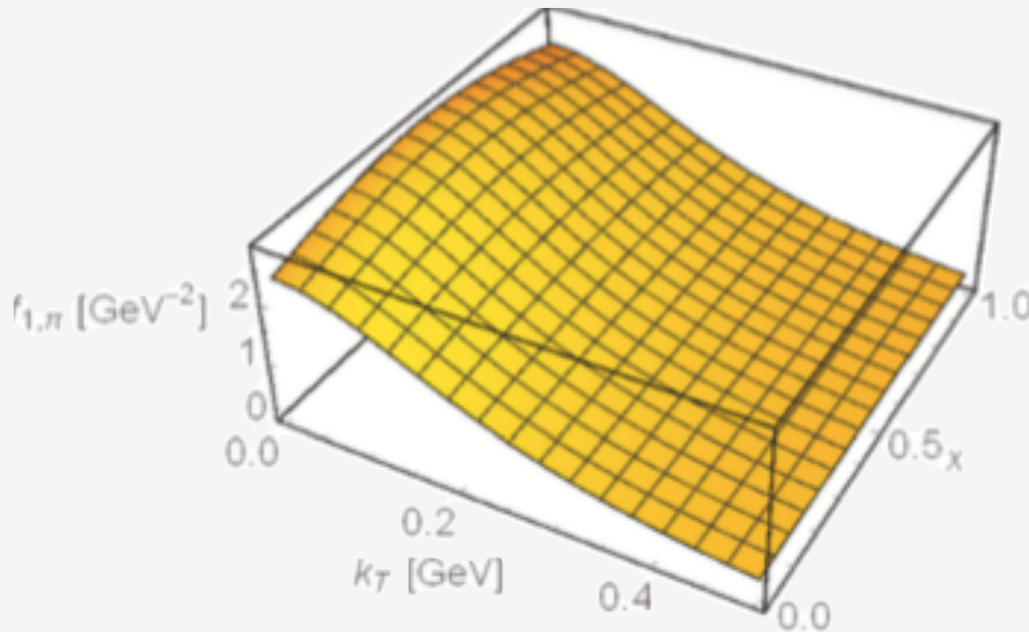
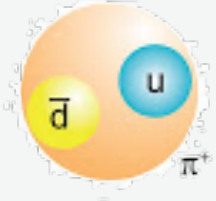


Pion dynamics → differs from a gaussian



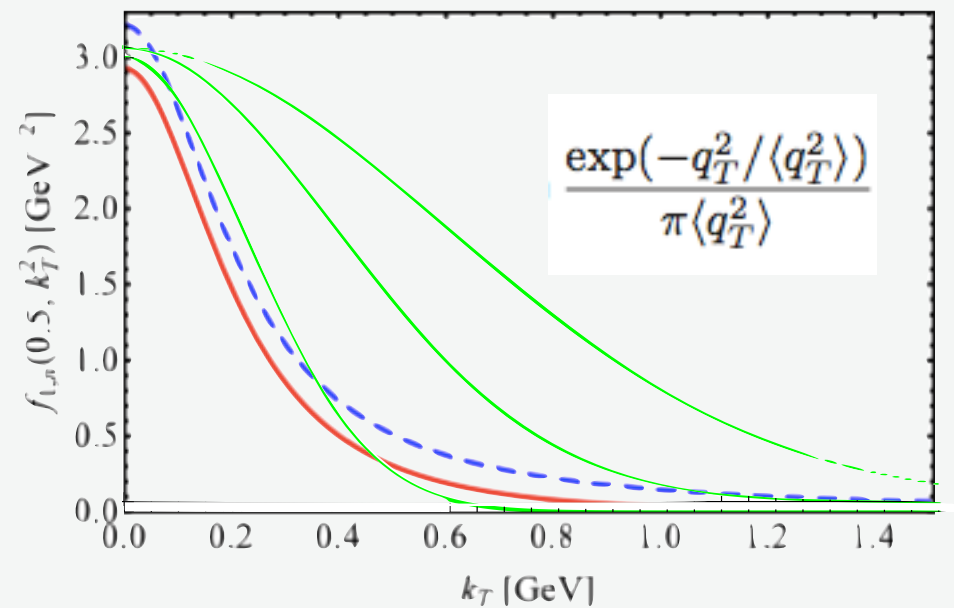
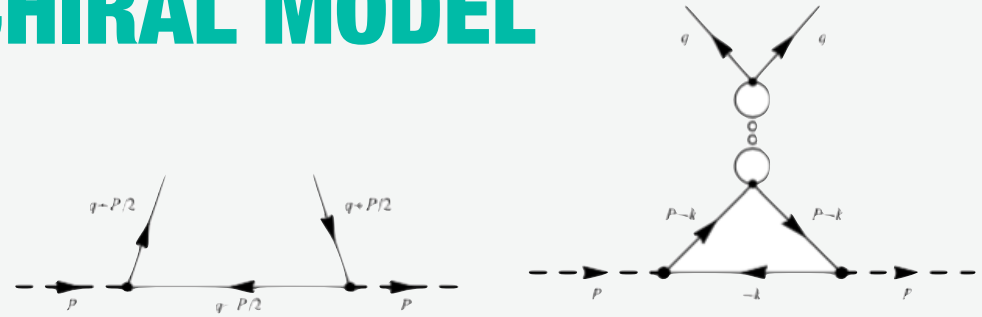
Pion DY

THE PION IN A CHIRAL MODEL



Pion dynamics → differs from a gaussian

Transverse profile → no dpdce on x or M



Pion DY

DRELL-YAN WITH PION DYNAMICS

Next-to-Leading Log

$$\sigma_{DY\pi N} \equiv \frac{d\sigma}{d\tau dy dp_T^2} = \sum_q \frac{\sigma_{q\bar{q}}^0}{2} \int_0^\infty db b J_0(bp_T) e^{S(b, b_{\max}, Q, C_1)} e^{S_{NP}^\pi(b)} e^{S_{NP}^N(b)} \cdot \left[\left(f_{q_a}^\pi(x_a, \mu_b) \otimes C_{aa'} \right) \left(F_{\bar{q}_b}^N(x_b, \mu_b) \otimes C_{bb'} \right) + q \leftrightarrow \bar{q} \right],$$

Wilson coeff. at order α_s
CTEQ6M PDFs evolved at NLO

Proton $b_{\max}=0.86 \text{ GeV}^{-1}$

Pion $b_{\max}=\text{educated guess/adjusted to data}$

$= b_0/Q_0=2.44 \text{ GeV}^{-1}$

☑ stability upon variation of regulator

Pion DY

[Ceccopieri & Trentadue, Phys.Lett.B741]
[Ceccopiero, A.C, Noguera & Scopetta, in preparation]

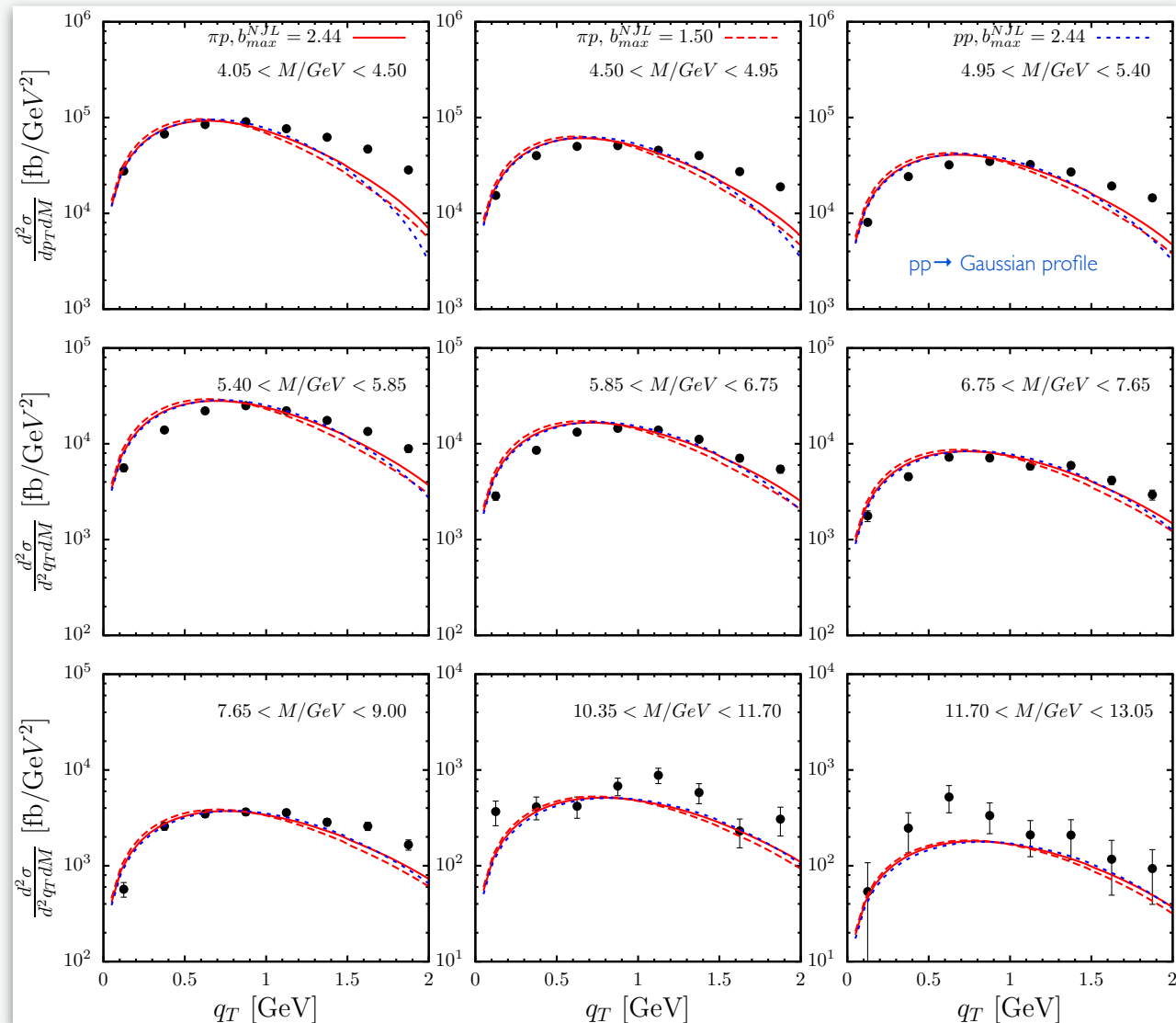
$\pi^- W$ DRELL-YAN

Cross section in Q-bins

- ☒ overall magnitude
- ☒ small q_T
- ☒ stability upon b-prescription
- ☐ higher q_T
- ☐ Gaussian profile ~indistinguishable

No free parameters
Only Q_0 is fixed beforehand

with KN param.



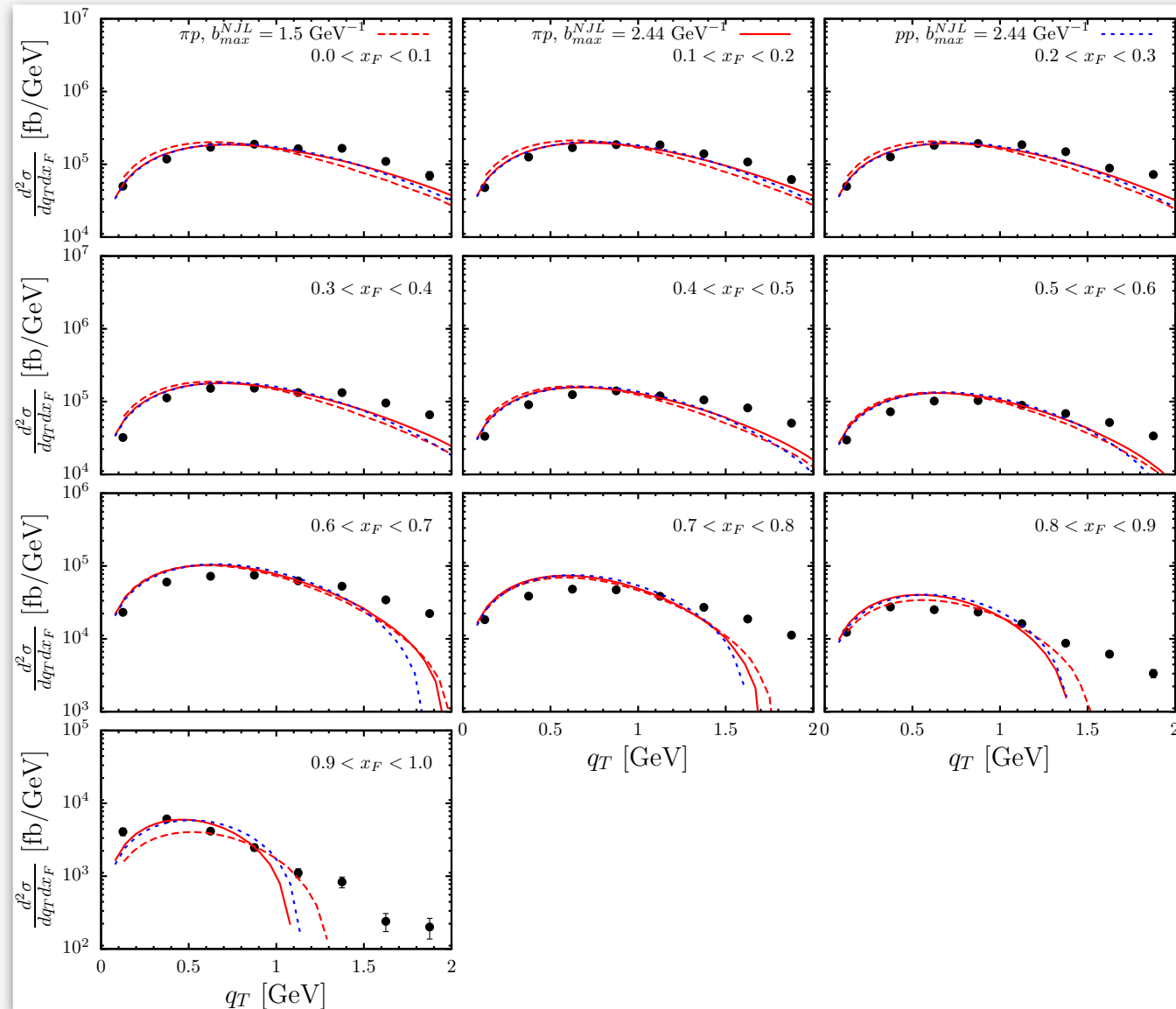
Pion DY

$\pi^- W$ DRELL-YAN

Cross section in x-bins

- ☒ overall magnitude
- ☒ small q_T
- ☒ stability upon b-prescription
- ☐ higher q_T
- ☐ Gaussian profile ~indistinguishable

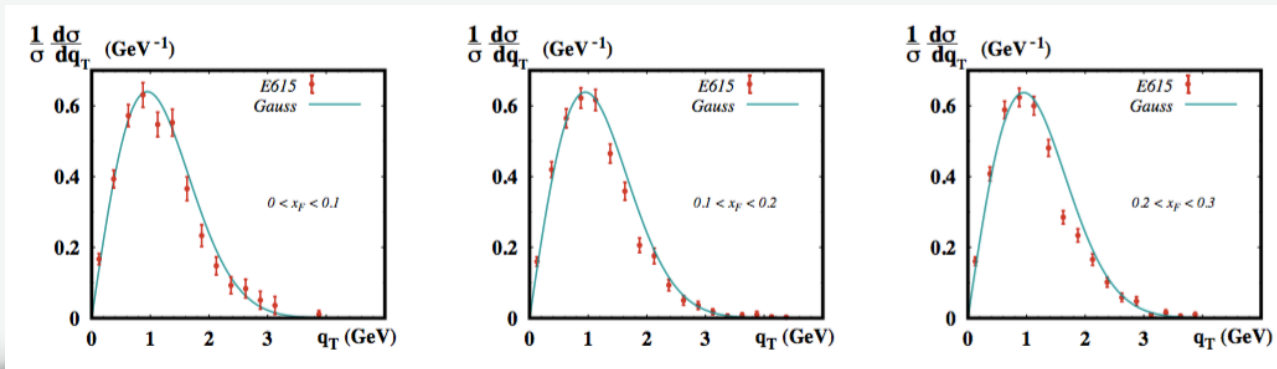
No free parameters
Only Q_0 is fixed beforehand



with KN param.

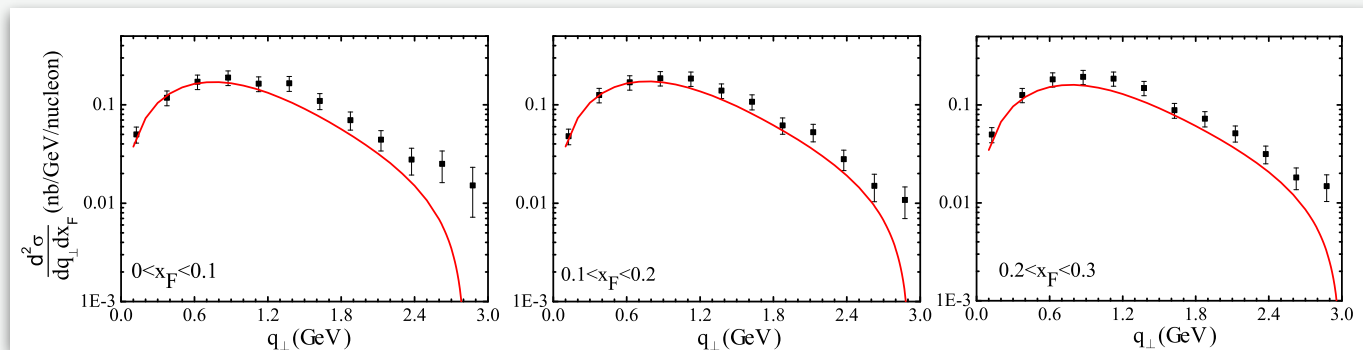
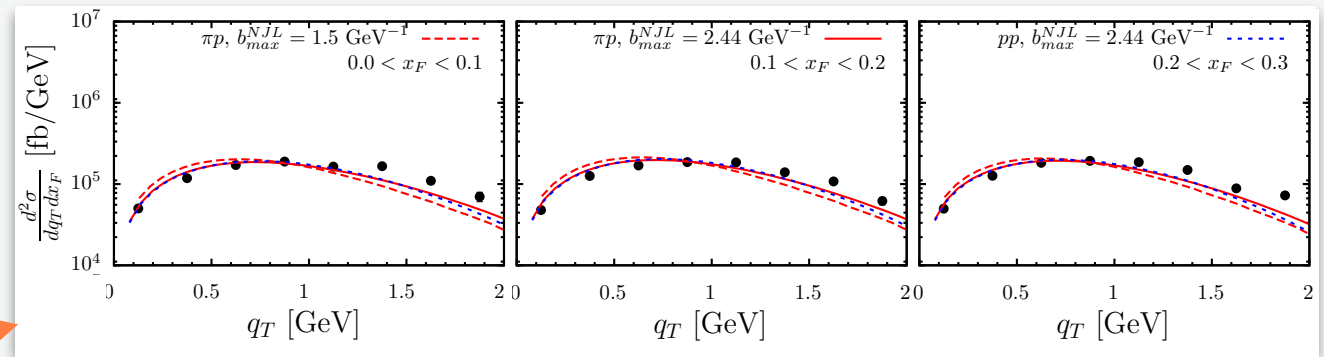
Pion DY

$\pi^- W$ DRELL-YAN



Only gaussian

[Pasquini & et al, Phys.Rev.D90]

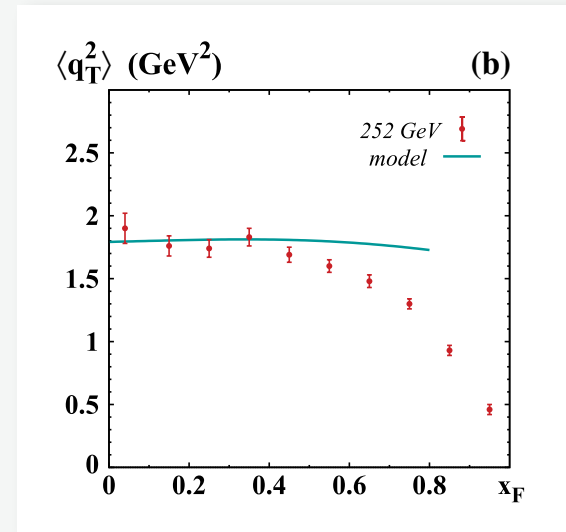
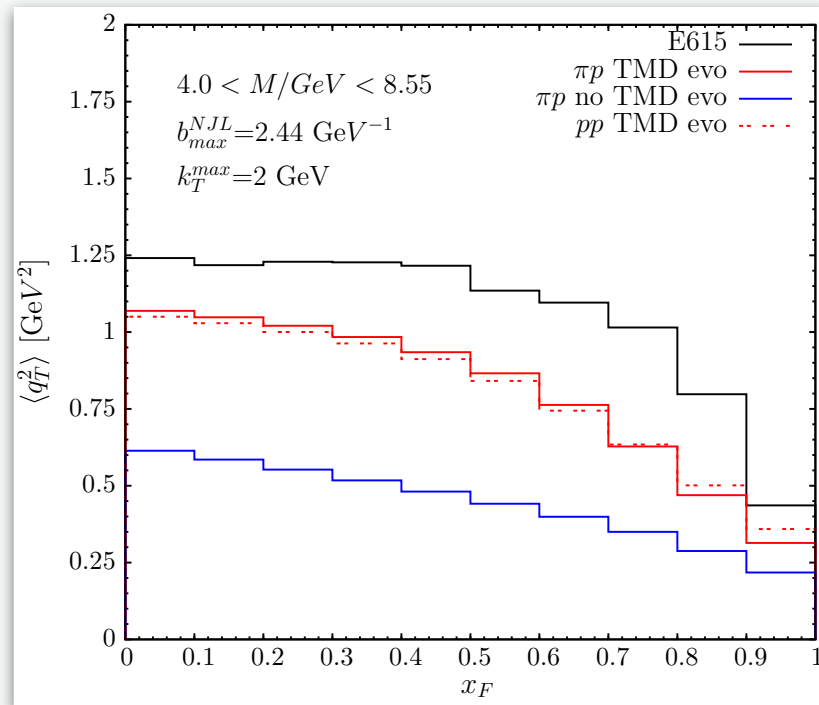


Fit

[Wang & et al, JHEP08-137]

Pion DY

$\pi^- W$ DRELL-YAN

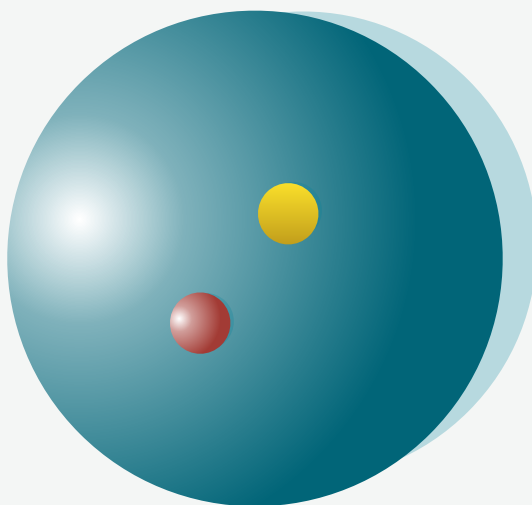
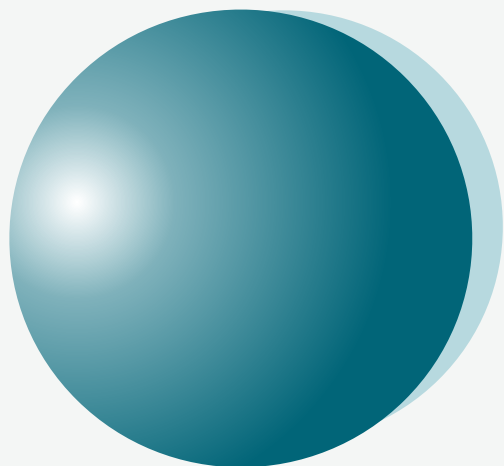


[Pasquini & et al, Phys.Rev.D90]

CSS evolution affects the transverse mmt distribution.

Pion DY

PION STRUCTURE FROM DY?



Degrees of freedom change governed
by the chiral symmetry.

Resolution

Pion DY

CONCLUSIONS

- Pion-proton collision to $\mu^+\mu^-$
- We have included pion nonperturbative dynamics in DY cross section
- Slight change in shape w.r.t. pure gaussians
- Need to understand another function: $g_K(b)$

Importance of nonperturbative inserts in perturbative evolution!

Exciting physics ahead!

OUTLOOK

- Predictions for COMPASS-II
- Go to polarized case
 - T-odd TMDs and universality
- Go to the modern TMD description of the factorized form

$$\begin{aligned} \frac{d\sigma}{d^4q d\Omega} = & \frac{2}{s} \sum_j \frac{d\hat{\sigma}_{j\bar{j}}(Q, \mu_Q, \alpha_s(\mu_Q))}{d\Omega} \int d^2\mathbf{b}_T e^{iq_T \cdot \mathbf{b}_T} \tilde{f}_{j/A}(x_A, \mathbf{b}_T; Q_0^2, \mu_{Q_0}) \tilde{f}_{\bar{j}/B}(x_B, \mathbf{b}_T; Q_0^2, \mu_{Q_0}) \\ & \times \exp \left\{ \left[-g_K(b_T; b_{\max}) + \tilde{K}(b_*; \mu_{b_*}) - \int_{\mu_{b_*}}^{\mu_{Q_0}} \frac{d\mu'}{\mu'} \gamma_K(\alpha_s(\mu')) \right] \ln \frac{Q^2}{Q_0^2} \right\} \\ & \times \exp \left\{ \int_{\mu_{Q_0}}^{\mu_Q} \frac{d\mu'}{\mu'} \left[2\gamma_j(\alpha_s(\mu'); 1) - \ln \frac{Q^2}{(\mu')^2} \gamma_K(\alpha_s(\mu')) \right] \right\} \end{aligned}$$

[Collins & Rogers, PRD91]

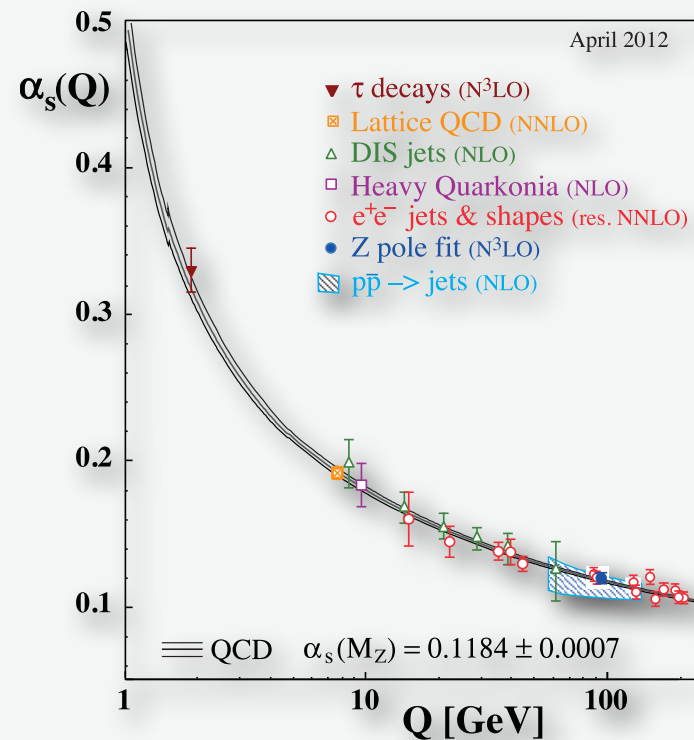
- Use knowledge on pion to fix NP parameters
- Redefine/evaluate the hadronic scale from TMD pheno.

BACKUP SLIDES

THE THEORY OF THE STRONG INTERACTIONS

$$\text{QM: } \hat{H} = \hat{H}_0 + \lambda \hat{H}_1 + \dots, \quad \lambda \ll 1$$

$$\text{QCD: } A = A_0 + \frac{\alpha_s(Q)}{4\pi} A_1 + \left(\frac{\alpha_s(Q)}{4\pi} \right)^2 A_2 + \dots$$



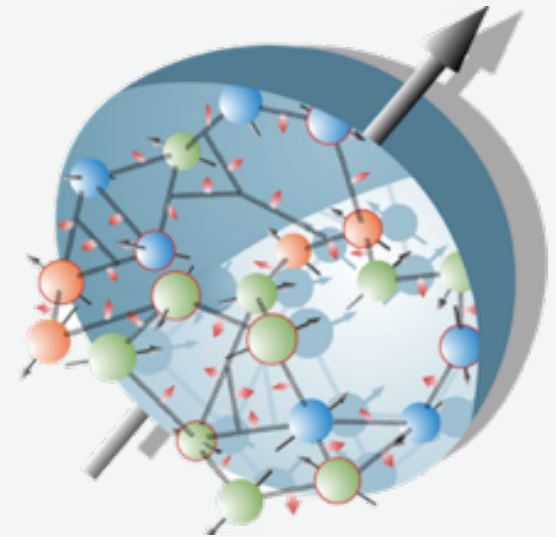
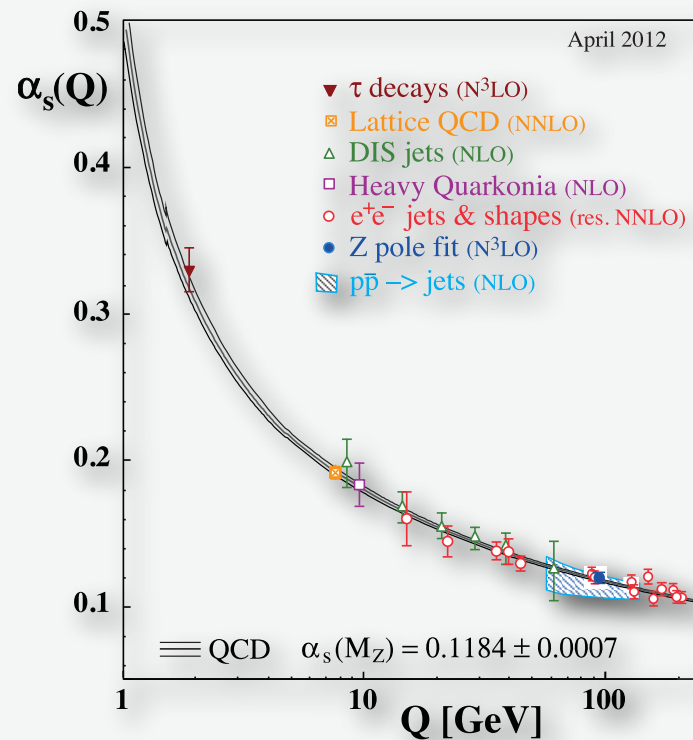
Confinement

Asymptotic freedom

Pion DY
Resolution

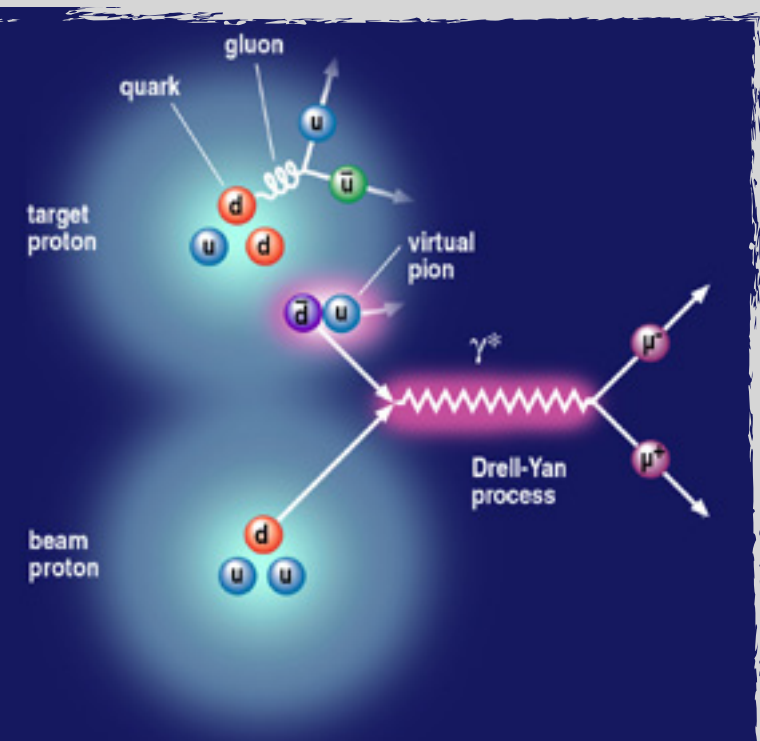
HADRON STRUCTURE

$$A = A_0 + \frac{\alpha_s(Q)}{4\pi} A_1 + \left(\frac{\alpha_s(Q)}{4\pi} \right)^2 A_2 + \dots$$



Pion DY
Resolution

DRELL-YAN PROCESSES





That's a pion

Photon

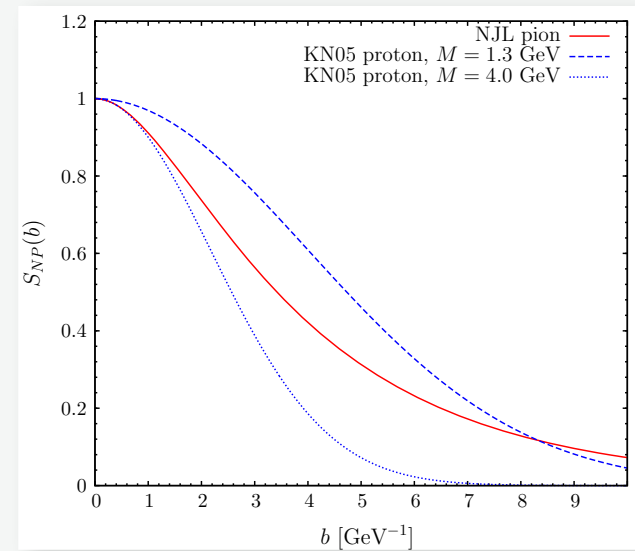
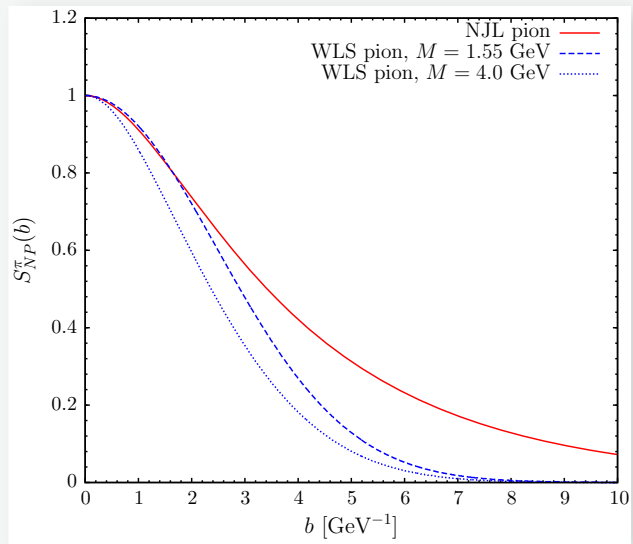
**Pion-proton collision
to a lepton pair**

Process called Drell-Yan

Pion DY

That's a proton

TRANSVERSE PROFILE



Pion DY