



Transverse momentum distribution of charmonium production in lepton-hadron scattering at the EIC

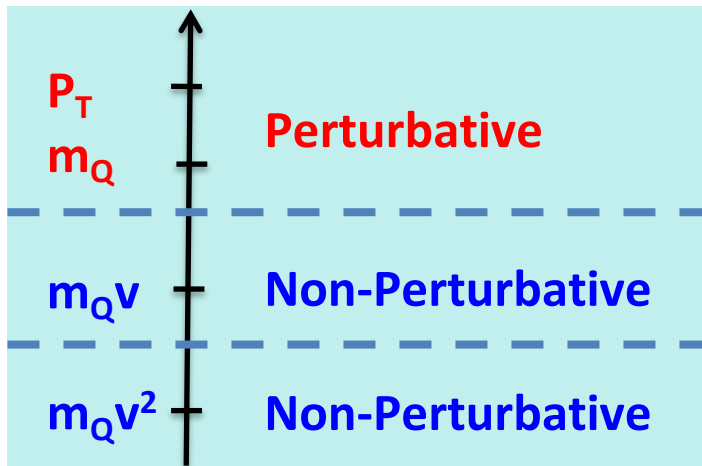
- Single inclusive heavy quarkonium production in hadronic collisions
- Single inclusive heavy quarkonium production in lepton-hadron collisions at the EIC
- Nuclear modification to quarkonium production in e-A collisions
- Summary and outlook

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Scales for heavy quarkonium production at high P_T

Well-separated momentum scales – effective theory:



Hard — Production of $Q\bar{Q}$ [pQCD]

To make this part as reliable as we can!

Soft — Relative Momentum [NRQCD]

$\leftarrow \Lambda_{\text{QCD}}$

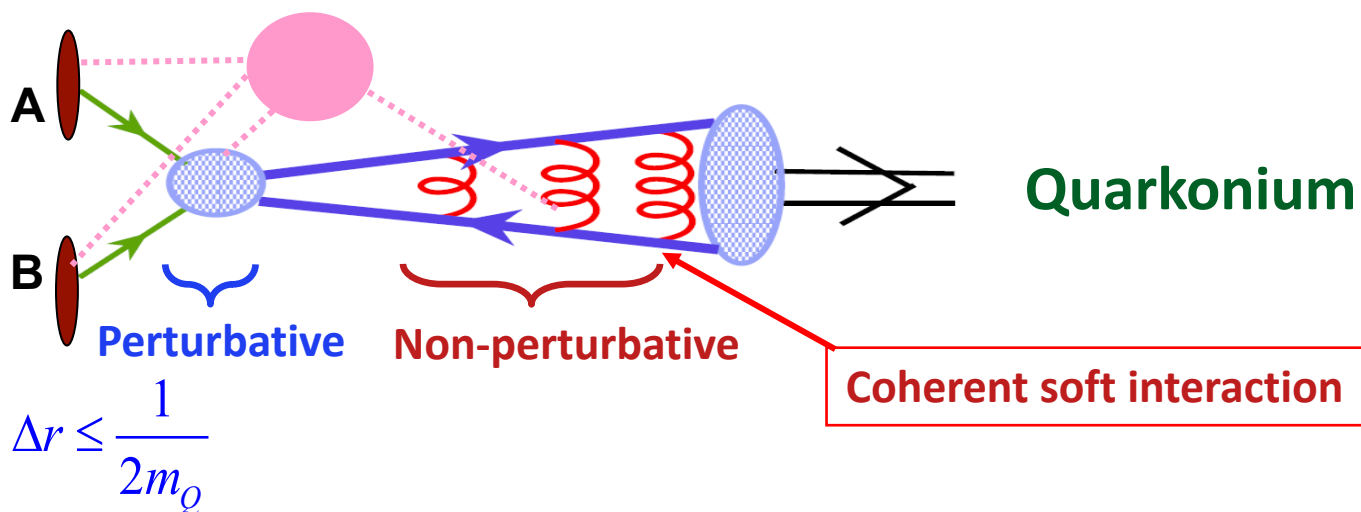
$\Lambda_{\text{QCD}} \rightarrow$

Ultrasoft — Binding Energy [pNRQCD]

Known quarks

Flavor	Mass
u	1.5 – 4.5 MeV
d	5.0 – 8.5 MeV
s	80 – 155 MeV
c	1.0 – 1.4 GeV
b	4.0 – 4.5 GeV
t	174.3 ± 5.1 GeV

Basic production mechanism:



- QCD Factorization is “expected” to work for the production of heavy quark pair
- Difficulty: how the heavy quark pair becomes a quarkonium?
- Medium: filter/diagnose the emergence

QCD factorization for heavy quarkonium production at high P_T

Lee, Qiu, Sterman, Watanabe, 2022

□ PQCD factorization:

$$E \frac{d\sigma_{hh' \rightarrow J/\psi(P)X}}{d^3P} = \sum_{c\bar{c}[n]} F_{c\bar{c}[n] \rightarrow J/\psi} \otimes \sum_{a,b} \int dx_a f_{a/h}(x_a, \mu_f^2) \int dx_b f_{b/h'}(x_b, \mu_f^2) \\ \times \left[E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Resum}}}{d^3P} + E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{NRQCD}}}{d^3P} - E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Asym}}}{d^3P} \right]$$

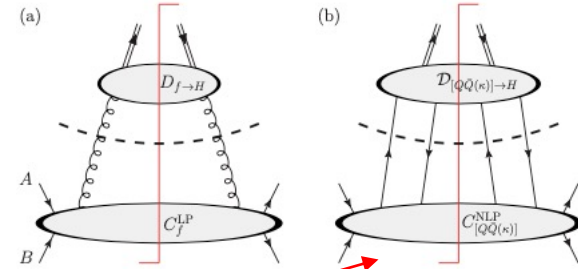
NRQCD:

$$F_{c\bar{c}[n] \rightarrow J/\psi} = \langle O_{c\bar{c}[n]}^{J/\psi}(0) \rangle \\ c\bar{c}[n] = c\bar{c} [^{2S+1}L_J^{[1,8]}]$$

■ PQCD factorization + FFs:

$$\kappa = (v, a, t)^{[1,8]} = (\gamma^+, \gamma^+ \gamma_5, \gamma^+ \gamma_\perp^i)^{[1,8]}$$

$$E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Resum}}}{d^3P} \approx \sum_f \int \frac{dz}{z^2} D_{f \rightarrow c\bar{c}[n]}(z, \mu_f^2) E_f \frac{d\hat{\sigma}_{ab \rightarrow f(p_f)X}}{d^3p_f}(z, p_f = P/z, \mu_f^2) \\ + \sum_{[c\bar{c}(\kappa)]} \int \frac{dz}{z^2} D_{[c\bar{c}(\kappa)] \rightarrow c\bar{c}[n]}(z, \mu_f^2) E_c \frac{d\hat{\sigma}_{ab \rightarrow [c\bar{c}(\kappa)](p_c)X}}{d^3p_c}(z, p_c = P/z, \mu_f^2)$$



Kang, Ma, Qiu, Sterman, 2014

■ PQCD fixed-order:

$$E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{NRQCD}}}{d^3P} \quad \text{Known to NLO}$$

■ PQCD Asymptotic contribution:

$$E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Asym}}}{d^3P} = E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Resum}}}{d^3P} \Bigg|_{\text{fixed order}}$$

QCD factorization for heavy quarkonium production at high P_T

Lee, Qiu, Sterman, Watanabe, 2022

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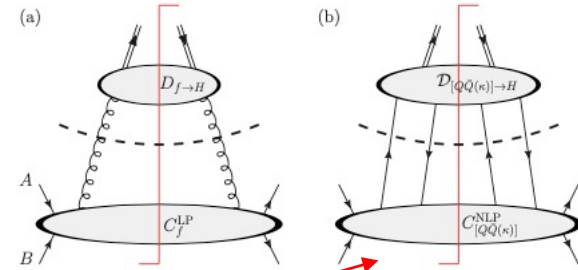
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Kang, Ma, Qiu, Sterman, 2014

■ PQCD fixed-order:

$$E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{NRQCD}}}{d^3P} \quad \text{Known to NLO}$$

When $P_T \gg m_c$, $E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Asym}}}{d^3P}$ **cancels** $E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{NRQCD}}}{d^3P}$

■ PQCD Asymptotic contribution:

$$E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Asym}}}{d^3P} = E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Resum}}}{d^3P} \Big|_{\text{fixed order}}$$

When $P_T \gtrsim m_c$, $E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Asym}}}{d^3P}$ **cancels** $E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Resum}}}{d^3P}$

Renormalization group improvement

Kang, Ma, Qiu, Sterman, PRD 90, 034006 (2014)

Renormalization group:

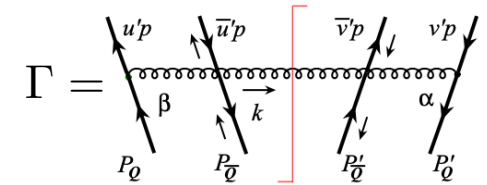
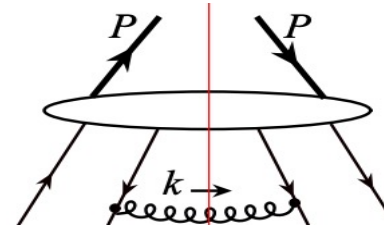
$$\frac{d}{d \ln \mu_f^2} \left[E \frac{d\tilde{\sigma}_{ab \rightarrow c\bar{c}[n](P)X}^{\text{Resum}}}{d^3 P} \right] = 0$$

To be accurate up to the 1st power correction

Modified evolution equations: NRQCD: $H = c\bar{c}^{[2S+1} L_J^{[1,8]}$

$$\frac{\partial \mathcal{D}_{[Q\bar{Q}(n)] \rightarrow H}}{\partial \ln \mu_f^2} = \Gamma_{[Q\bar{Q}(n)] \rightarrow [Q\bar{Q}(\kappa)]} \otimes \mathcal{D}_{[Q\bar{Q}(\kappa)] \rightarrow H}$$

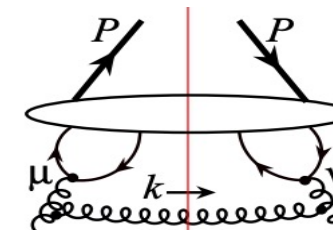
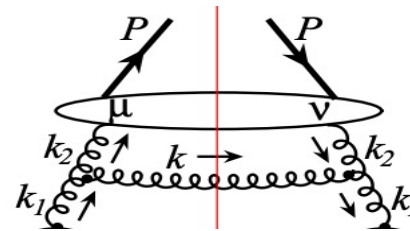
DGLAP-type: Heavy quark pair produced at the hard scale



$$\frac{\partial D_{[f] \rightarrow H}}{\partial \ln \mu_f^2} = \gamma_{[f] \rightarrow [f']} \otimes D_{[f'] \rightarrow H}$$

$$+ \frac{1}{\mu_f^2} \bar{\gamma}_{[f] \rightarrow [Q\bar{Q}(\kappa)]} \otimes \mathcal{D}_{[Q\bar{Q}(\kappa)] \rightarrow H}$$

Heavy quark pair produced at the input scale



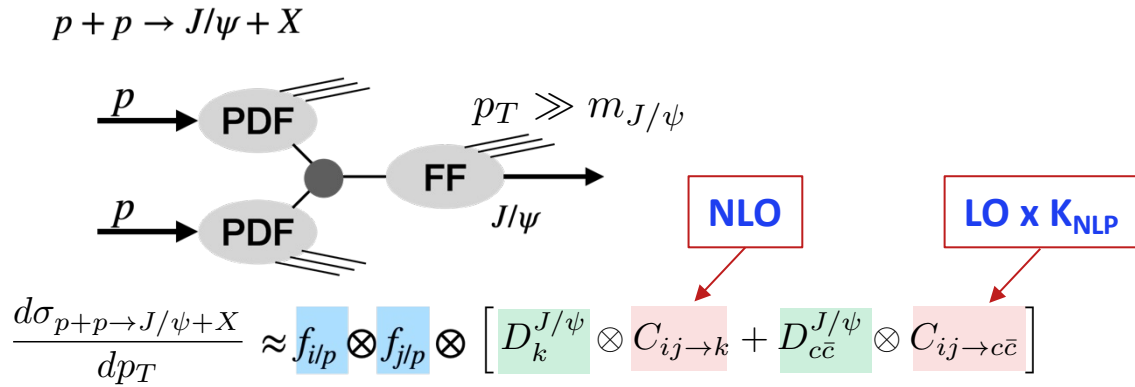
$\leftarrow \bar{\gamma}_{g \rightarrow [Q\bar{Q}]}$

Heavy quark pair produced between the hard scale and the input scale

Modified DGLAP – inhomogeneous evolution

Single inclusive high P_T J/ψ -production in hadronic collisions

Test the consistency:



Input FFs from NRQCD:

Ma, Qiu, Zhang, PRD89 (2014) 094029;
ibid. 94030

$$D_{f \rightarrow H}(z; m, \mu_0) = \sum_{[Q\bar{Q}(n)]} \pi \alpha_s \left\{ \hat{d}_{f \rightarrow [Q\bar{Q}(n)]}^{(1)}(z; m, \mu_0, \mu_\Lambda) + \frac{\alpha_s}{\pi} \hat{d}_{f \rightarrow [Q\bar{Q}(n)]}^{(2)}(z; m, \mu_0, \mu_\Lambda) + \mathcal{O}(\alpha_s^2) \right\} \frac{\langle \mathcal{O}_{[Q\bar{Q}(n)]}^H(\mu_\Lambda) \rangle}{m^{2L+3}}$$

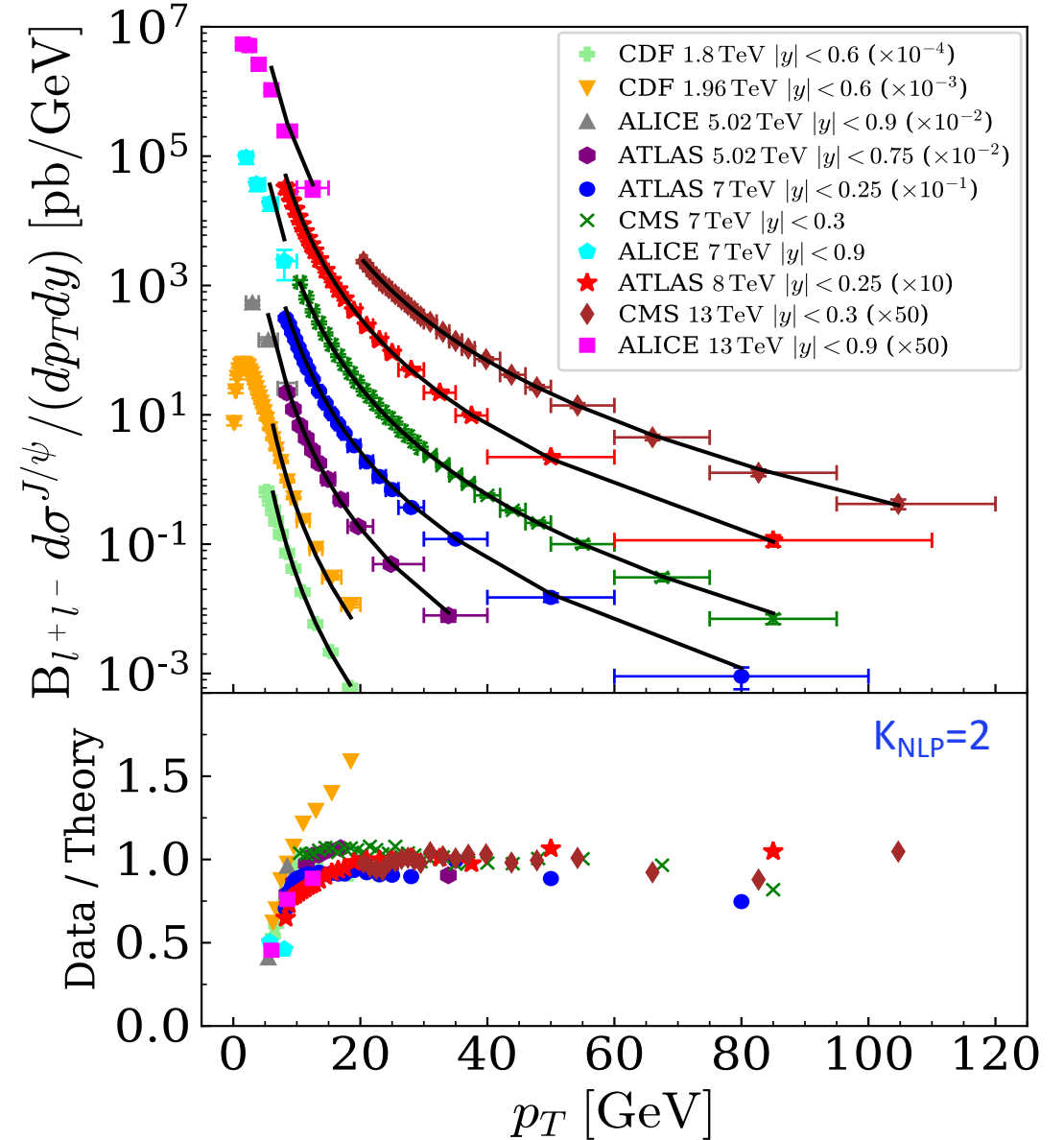
$\kappa = v^{[c]}, a^{[c]}, t^{[c]}, \quad n = 2S+1 L_j^{[c]}$

$$D_{[Q\bar{Q}(\kappa)] \rightarrow H}(z; m, \mu_0) = \sum_{[Q\bar{Q}(n)]} \left\{ \hat{d}_{[Q\bar{Q}(\kappa)] \rightarrow [Q\bar{Q}(n)]}^{(0)}(z; m, \mu_0, \mu_\Lambda) + \frac{\alpha_s}{\pi} \hat{d}_{[Q\bar{Q}(\kappa)] \rightarrow [Q\bar{Q}(n)]}^{(1)}(z; m, \mu_0, \mu_\Lambda) + \mathcal{O}(\alpha_s^2) \right\} \frac{\langle \mathcal{O}_{[Q\bar{Q}(n)]}^H(\mu_\Lambda) \rangle}{m^{2L+1}}$$

$\mu_0 = \mathcal{O}(2m)$: input scale, $\mu_\Lambda = \mathcal{O}(m)$: NRQCD factorization scale

➔

$$D_{f \rightarrow H}(z) = N_f \frac{z^{\alpha_f} (1-z)^{\beta_f}}{B(1+\alpha_f, 1+\beta_f)}$$



Matching to fixed-order PQCD calculation

- Leading power logarithmically enhanced contributions start to dominate when

$$P_T \gtrsim 5(2m_c) \sim 15 \text{ GeV}$$

- Next-to-leading power is important for

$$5(2m_c) \gtrsim P_T \gtrsim (2m_c)$$

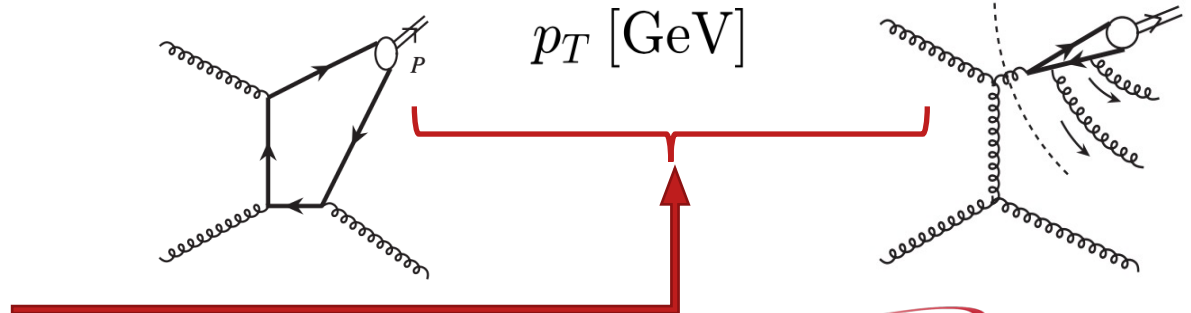
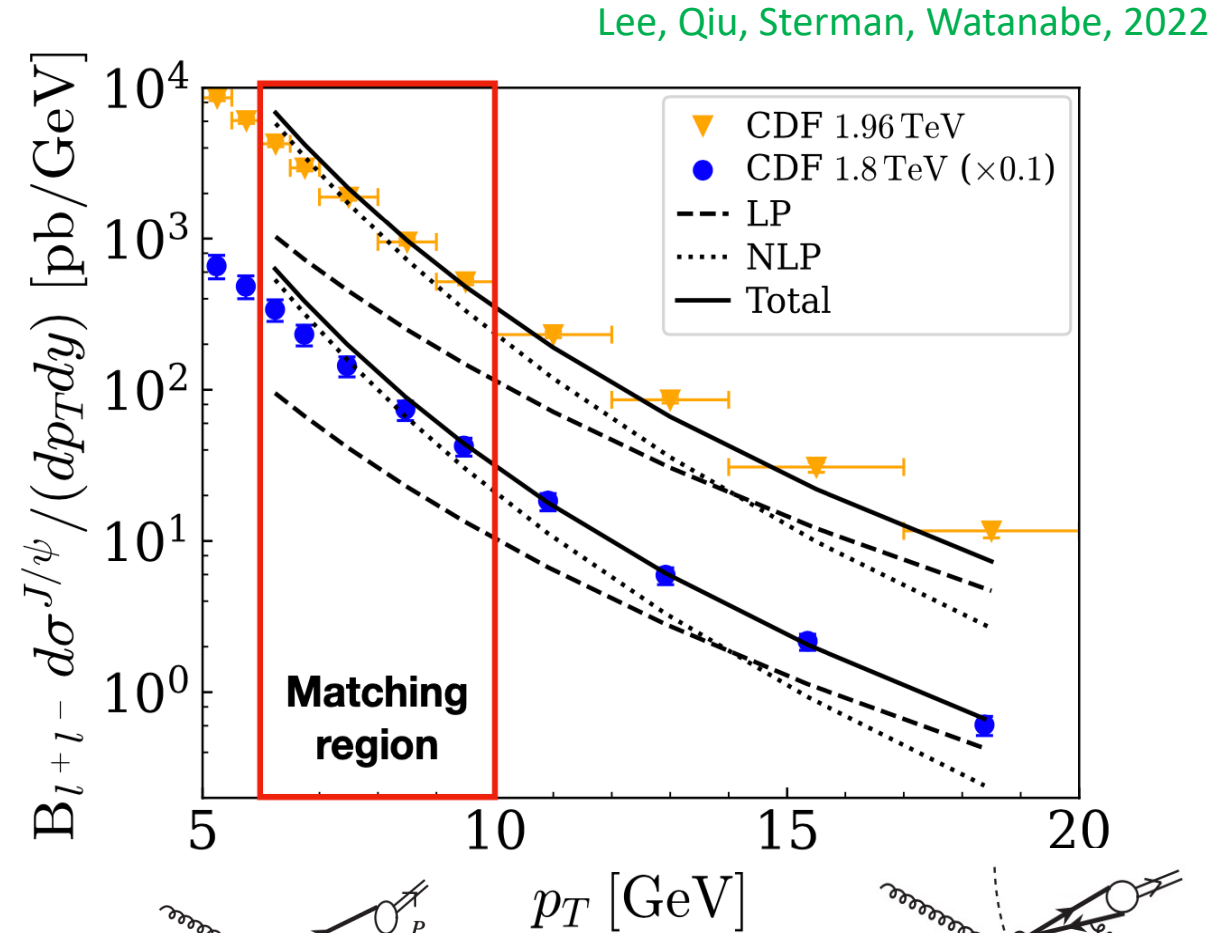
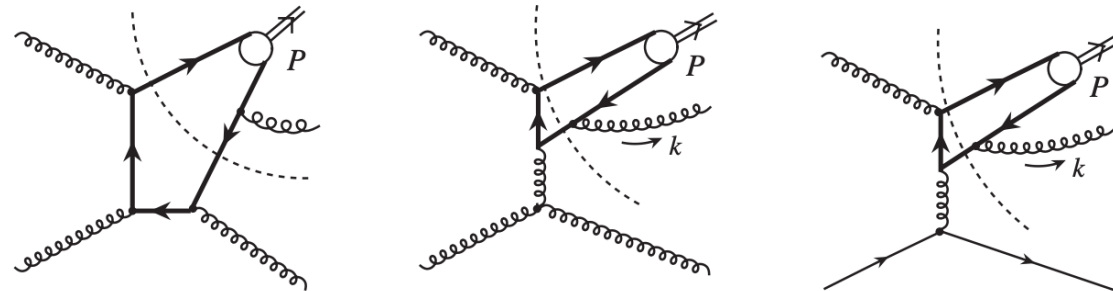
- Matching to fixed-order NRQCD calculation

$$P_T \sim (2m_c)$$

NLP term is necessary for the matching

- Further improvement by exploring the FFs

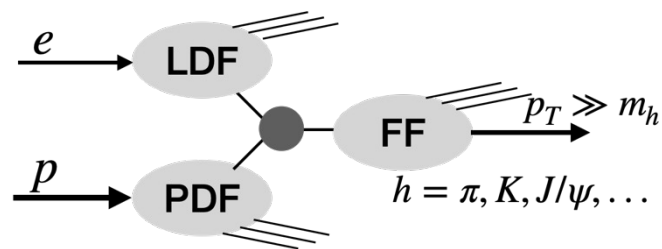
Use the medium as a filter?



Single inclusive high P_T J/ψ -production in lepton-hadron collisions

□ PQCD factorization:

$$e + p \rightarrow h(p_T) + X$$



PDFs, FFs are common blocks in and collisions.

$$\frac{d\sigma_{e+p \rightarrow J/\psi+X}}{dp_T} \approx \underbrace{f_{i/e}}_{\text{LDFs}} \otimes \underbrace{f_{j/p}}_{\text{PDFs}} \otimes \underbrace{\left[D_k^{J/\psi} \otimes C_{ij \rightarrow k} + D_{c\bar{c}}^{J/\psi} \otimes C_{ij \rightarrow c\bar{c}} \right]}_{\text{Perturbatively calculable coefficients}}$$

Universal functions: LDFs, PDFs, FFs

NLO LO x K_{NLP}

Kang, Metz, Qiu and Zhou, PRD84, 034046 (2011)
 Hinderer, Schlegel, Vogelsang, PRD92, 014001 (2015)
 Abelo, Boughezal, Liu, Petriello, PLB763, 52-59 (2016)

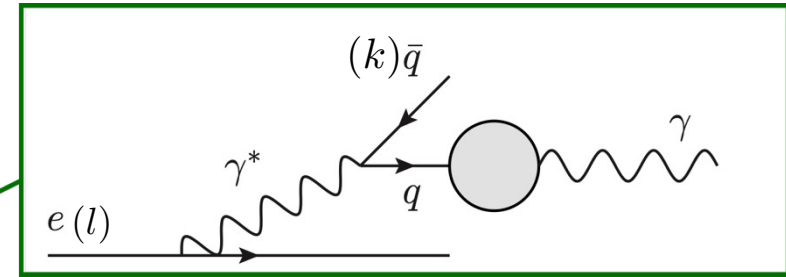
- The scattered lepton is **not observed** (cf. semi-inclusive DIS: $e + p \rightarrow e' + h + X$)
- Collision-induced QED and QCD radiations are consistently treated in terms of collinear factorization formalism [Liu, Melnitchouk, Qiu, Sato, PRD104, no.9, 094033 (2021), JHEP11, 157 (2021)]
- Leptons, photons, and partons in the beam lepton: Universal Lepton Distribution Functions (LDFs)

Remark: DESY-HERA introduced a cut on the transverse momentum of the scattered lepton to separate (electro-production) from (photo-production), leading to the “direct” vs “resolved” photon production

In our approach: we have a choice of the factorization scale, but, no need for such a cut!

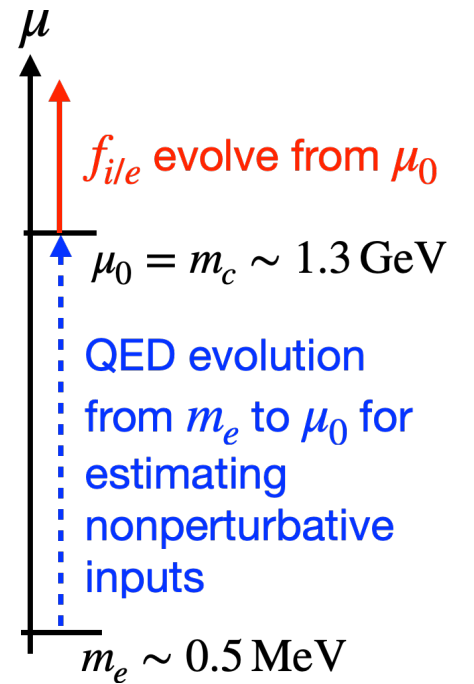
Quantum evolution of LDFs

□ **DGLAP evolution:** $\xi = \frac{k^+_{\text{active lepton (quark)}}}{l^+_{\text{lepton}}}$



$$\frac{\partial}{\partial \ln \mu^2} \begin{pmatrix} f_{ele}(\xi, \mu^2) \\ f_{\bar{e}le}(\xi, \mu^2) \\ f_{\gamma le}(\xi, \mu^2) \\ f_{qle}(\xi, \mu^2) \\ f_{\bar{q}le}(\xi, \mu^2) \\ f_{g le}(\xi, \mu^2) \end{pmatrix} = \begin{pmatrix} \text{QED part} & \text{Mixing part} \\ P_{ee}^{(1,0)} P_{e\bar{e}}^{(2,0)} P_{e\gamma}^{(1,0)} & P_{eq}^{(2,0)} P_{e\bar{q}}^{(2,0)} P_{eg}^{(2,1)} \\ P_{\bar{e}e}^{(2,0)} P_{\bar{e}\bar{e}}^{(1,0)} P_{\bar{e}\gamma}^{(1,0)} & P_{\bar{e}q}^{(2,0)} P_{\bar{e}\bar{q}}^{(2,0)} P_{\bar{e}g}^{(2,1)} \\ P_{\gamma e}^{(1,0)} P_{\gamma\bar{e}}^{(1,0)} P_{\gamma\gamma}^{(1,0)} & P_{\gamma q}^{(1,0)} P_{\gamma\bar{q}}^{(1,0)} P_{\gamma g}^{(1,1)} \\ P_{qe}^{(2,0)} P_{q\bar{e}}^{(2,0)} P_{q\gamma}^{(1,0)} & P_{qq}^{(0,1)} P_{q\bar{q}}^{(0,2)} P_{qg}^{(0,1)} \\ P_{\bar{q}e}^{(2,0)} P_{\bar{q}\bar{e}}^{(2,0)} P_{\bar{q}\gamma}^{(1,0)} & P_{\bar{q}q}^{(0,2)} P_{\bar{q}\bar{q}}^{(0,1)} P_{\bar{q}g}^{(0,1)} \\ P_{ge}^{(2,1)} P_{g\bar{e}}^{(2,1)} P_{g\gamma}^{(1,1)} & P_{gq}^{(0,1)} P_{g\bar{q}}^{(0,1)} P_{gg}^{(0,1)} \end{pmatrix} \otimes \begin{pmatrix} f_{ele}(\xi, \mu^2) \\ f_{\bar{e}le}(\xi, \mu^2) \\ f_{\gamma le}(\xi, \mu^2) \\ f_{qle}(\xi, \mu^2) \\ f_{\bar{q}le}(\xi, \mu^2) \\ f_{g le}(\xi, \mu^2) \end{pmatrix}$$

Mixing part QCD part

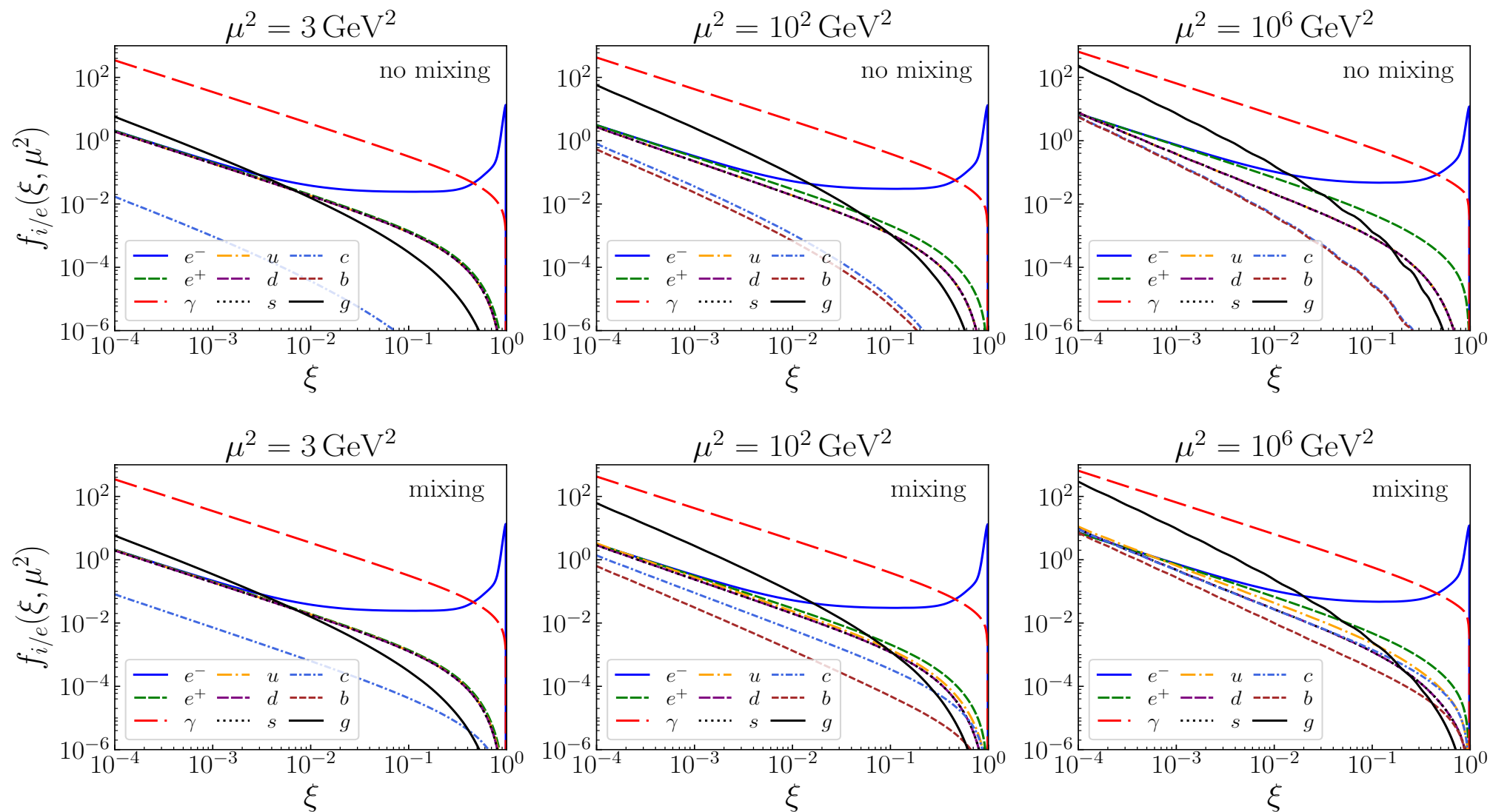


Splitting functions in QED+QCD:

$$P_{ij}(\xi, \mu^2) = \sum_{n,m=0}^{\infty} \left(\frac{\alpha_{em}(\mu^2)}{2\pi} \right)^n \left(\frac{\alpha_s(\mu^2)}{2\pi} \right)^m \hat{P}_{ij}^{(n,m)}(\xi) \equiv \sum_{n,m=0}^{\infty} P_{ij}^{(n,m)}(\xi, \mu^2)$$

Lepton distribution functions (LDFs) after evolution

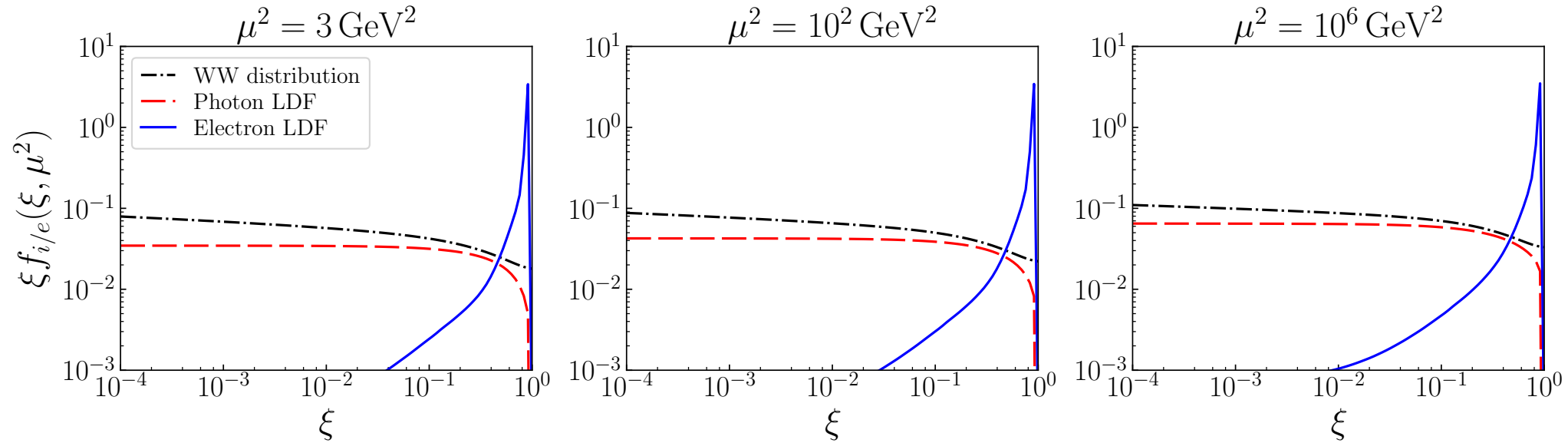
Qiu, Watanabe
in preparation



QED (QCD) evolution is slow (fast) due to the weak (strong) μ -dependence of $\alpha_{em}(\alpha_s)$

Photon LDF vs. Weizsäcker-Williams distribution

Qiu, Watanabe
in preparation



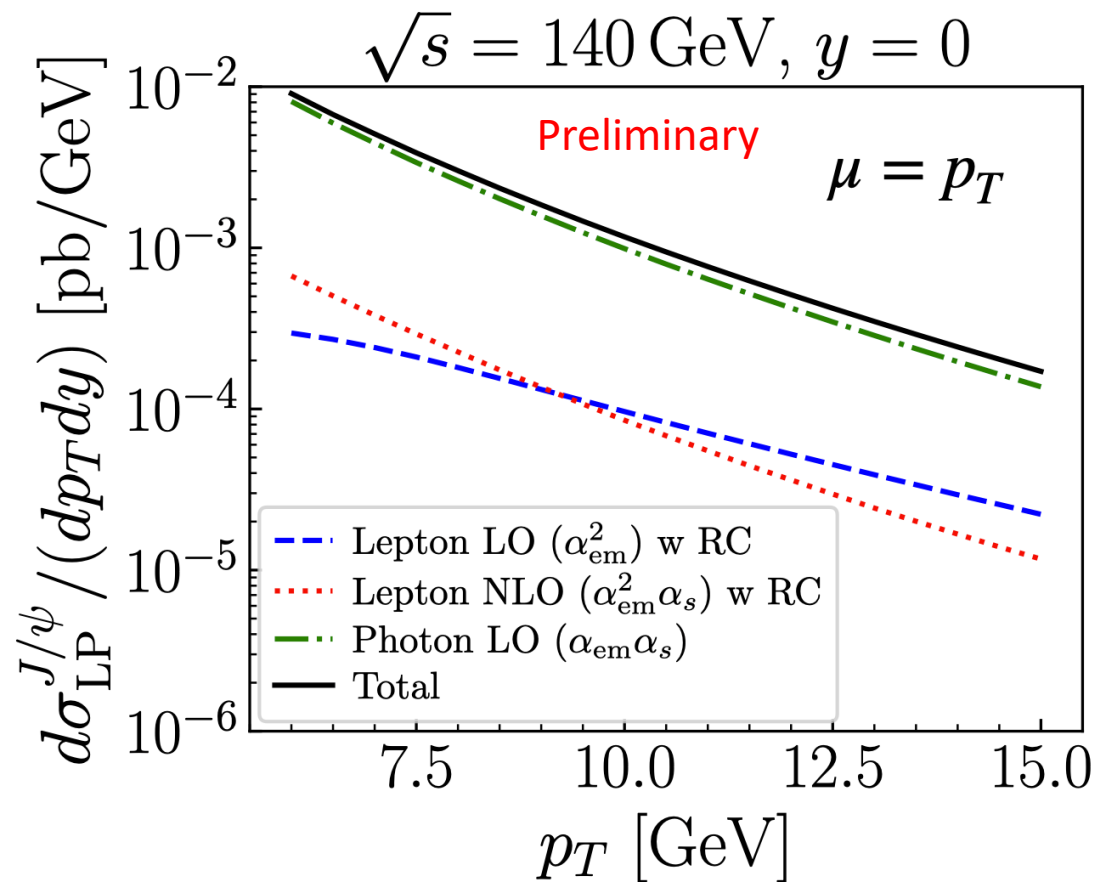
Weizsäcker-Williams (WW) distribution at LO with $\overline{\text{MS}}$ -scheme: [Hinderer, Schlegel, Vogelsang, PRD92, no.1, 014001 \(2015\)](#)

$$f_{\gamma/l}^{WW}(\xi, \mu^2) = \frac{\alpha_{\text{em}}}{2\pi} P_{\gamma l}(\xi) \left[\ln \left(\frac{\mu^2}{\xi^2 m_l^2} \right) - 1 \right] + \mathcal{O}(\alpha_{\text{em}}^2)$$

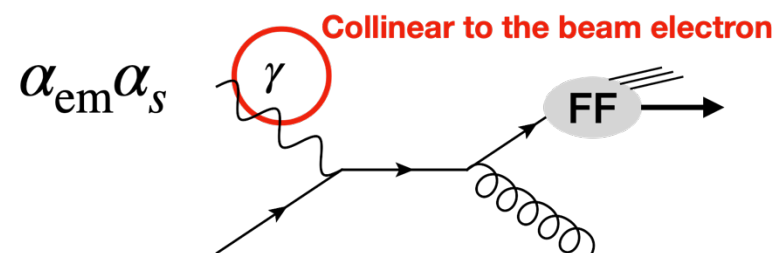
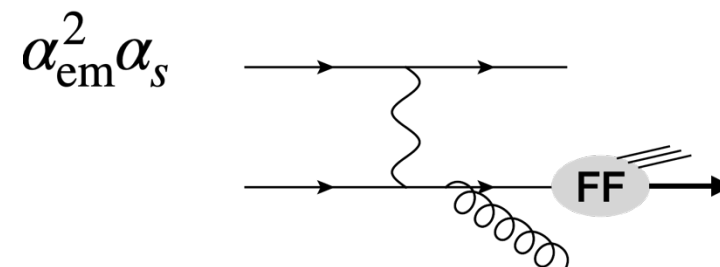
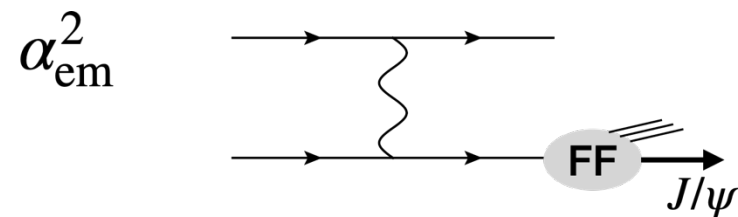
- Photon LDF is smaller to WW distribution, but different because of the resummation of large logs, and higher-order corrections, such as $\gamma \rightarrow e^+ e^-, q^+ \bar{q}, \dots$.
- Photon LDF depends on our purely QED evolution from m_e to μ_0 ; a global fitting could systematically improve the "red" dashed line.

Lepto- and photo-production of J/ψ at leading power (LP)

Qiu, Watanabe
in preparation



Leading-power in P_T :

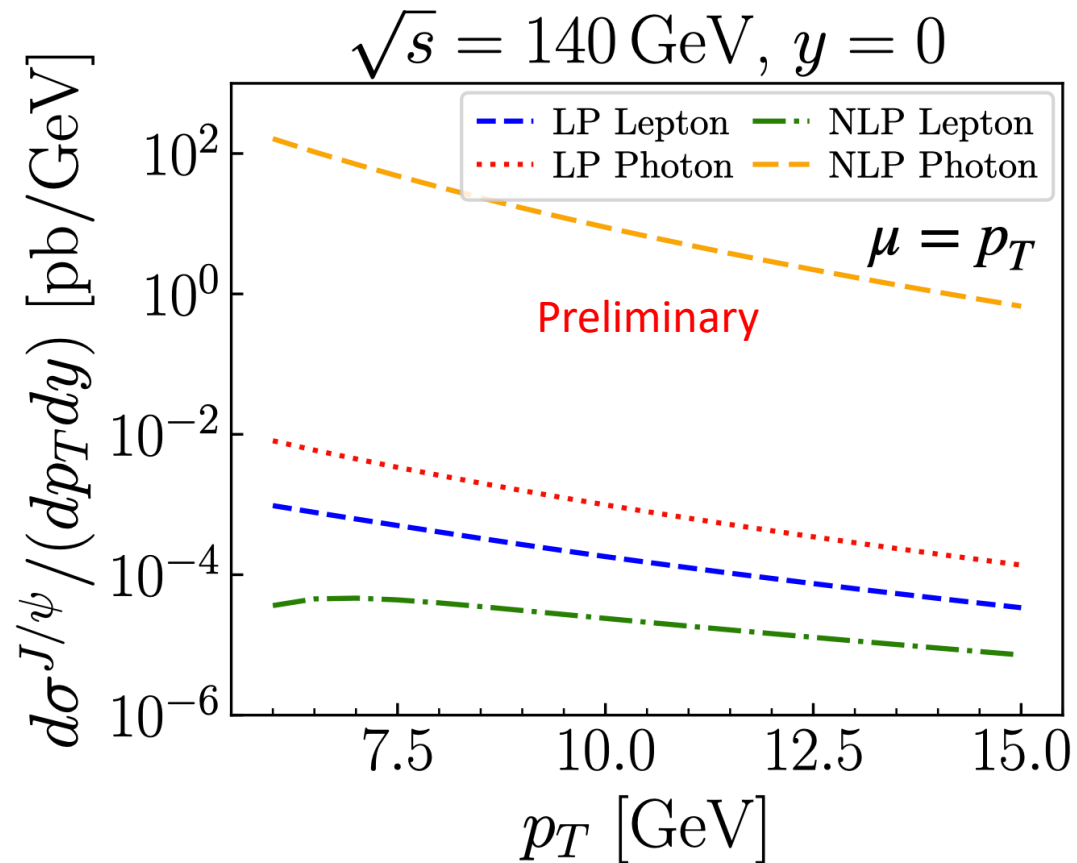


- No Q^2 -cut in calculations.
- Input scale for the evolution of quarkonium FFs: $\mu_0 = 2m_{J/\psi} \sim 6 \text{ GeV}$.
- The photoproduction overwhelms the leptonproduction at lower P_T .

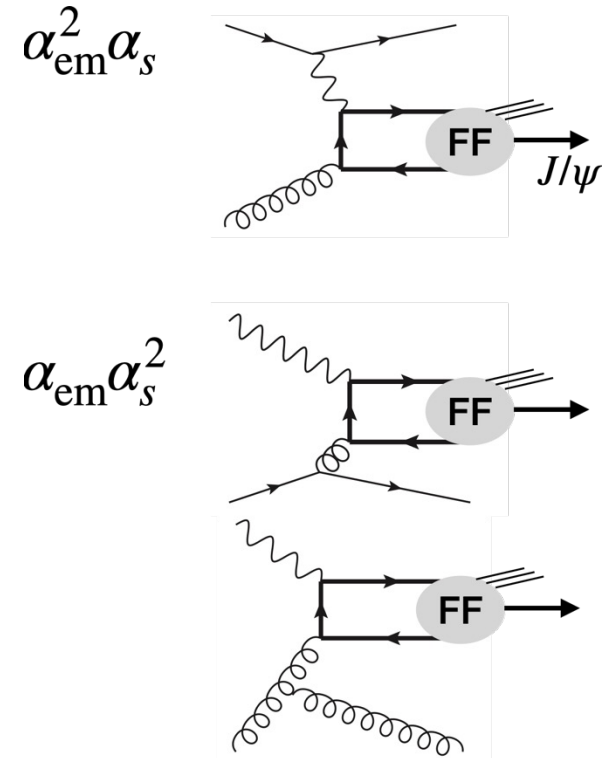
PDFs: CT18ANLO central set
FFs: LQSW set [Lee, Qiu, Sterman, KW, 2108.00305, 2211.12648, and 2023.xxxx]

Next-to-leading power (NLP) contributions

Qiu, Watanabe
in preparation



Next-to-Leading-power in P_T :

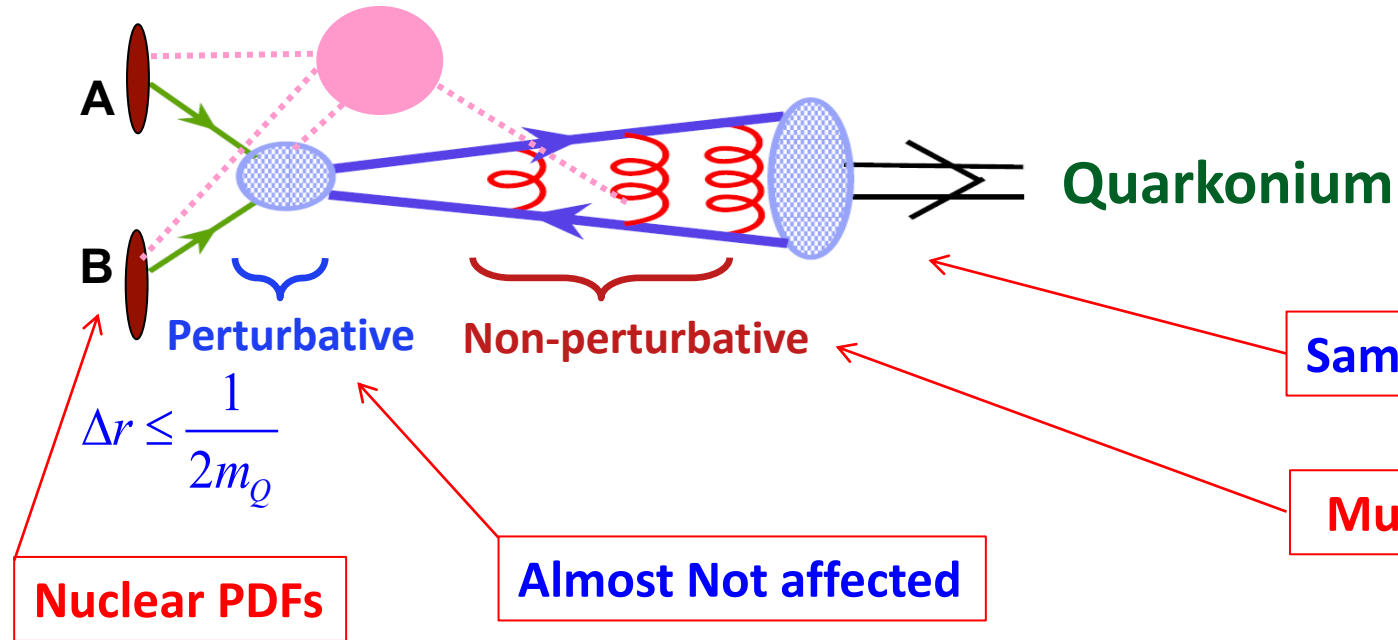


- The photoproduction of J/ψ at NLP is predominant over the LP contribution.
- A pair produced at short-distance can easily form a bound state compared to a single parton that fragments into it.

Heavy quarkonium production in a cold medium

Qiu, Watanabe, 2022

From ep to eA collision:



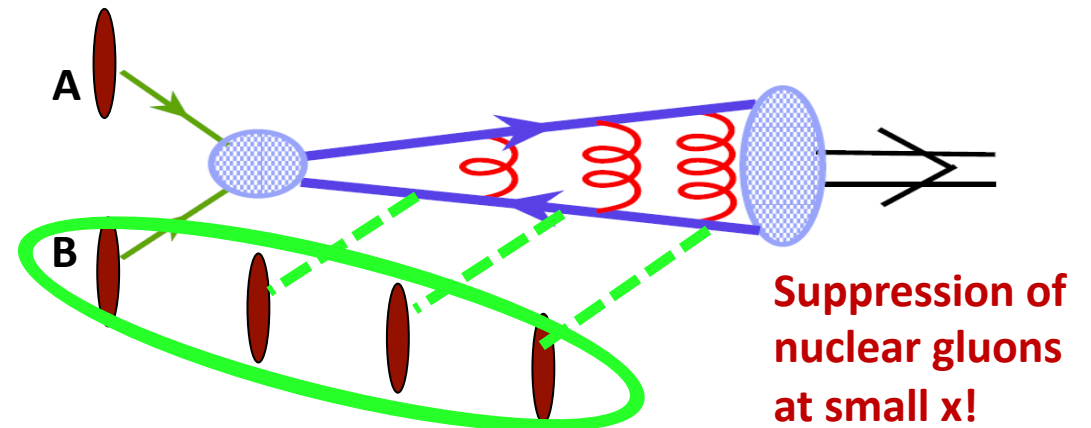
- QCD Factorization is “expected” to work for the production of heavy quark pair
- Hadronization can break the factorization
- Large y – time dilation – delay hadronization

Multiple scattering of heavy quarks can change:

- Distribution of total momentum of the pair
 - Cronin effect
- Invariant mass of the pair (broadening)

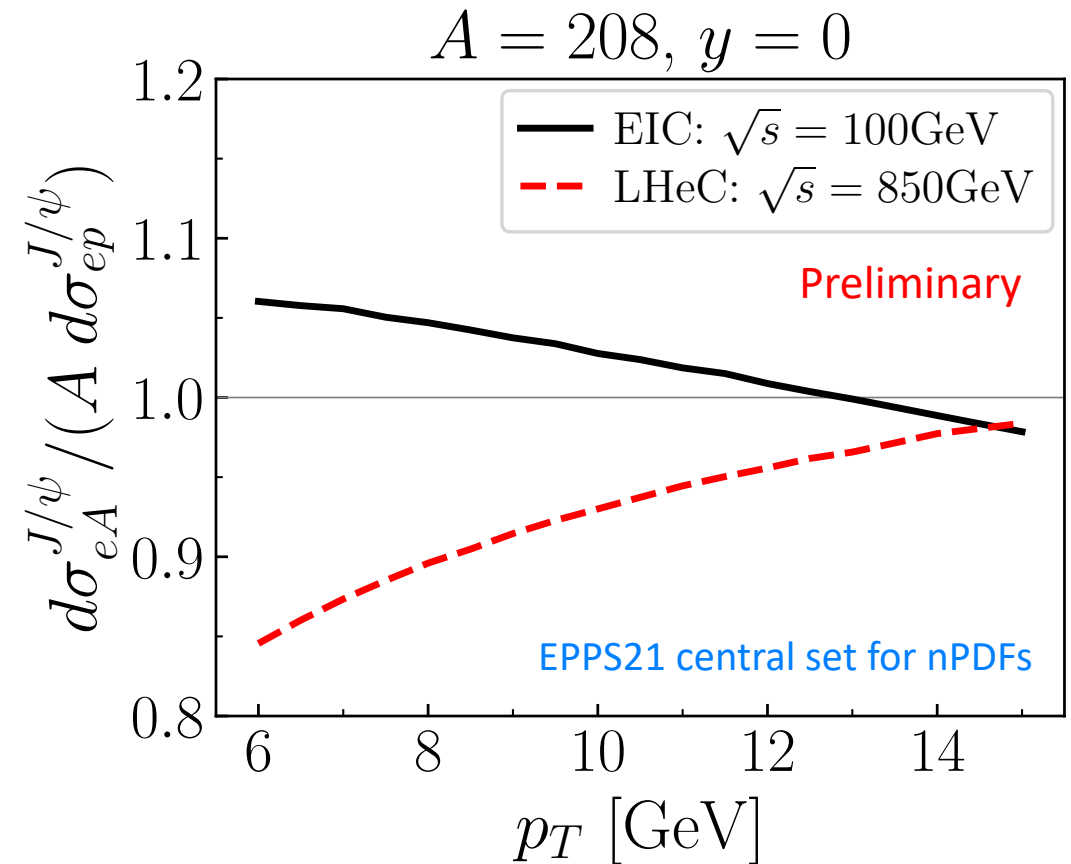
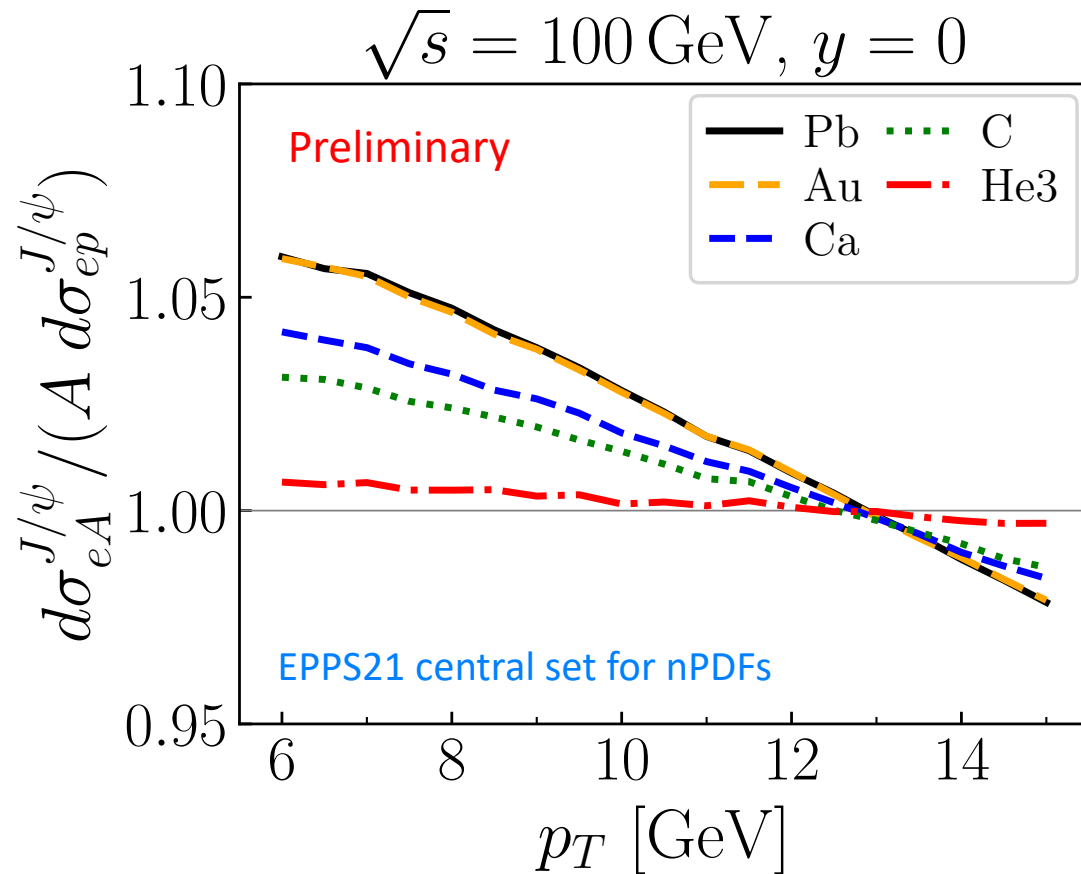
Guo, Qiu, Zhang, PRL 2000

– **Suppression of quarkonium** $R_{pA}(3\Upsilon) < R_{pA}(2\Upsilon) < R_{pA}(1\Upsilon)$



Qiu, Vary, Zhang, PRL 2002

Nuclear modification from nuclear PDFs



- The onset of nuclear anti-shadowing or EMC effects can be seen in J/ψ production at high P_T in eA collisions at the U.S.-EIC.
- LHeC experiments could allow us to explore nuclear shadowing effect.

Summary and Outlook

- We studied the QCD factorization for single inclusive J/ψ production at high P_T
 - Our approach can consistently describe the full P_T distribution of J/ψ production at Tevatron and the LHC
 - The LP contribution dominates the high P_T regime while NLP contribution is necessary for the low P_T shape
 - Theory predictions could be further improved with better determined FFs
 - The FFs at the input scale μ_0 can be extracted for testing NRQCD factorization
- We calculated single inclusive J/ψ production at high P_T in lepton-hadron collisions at the EIC
 - We do not need to introduce artificial cut to separate the lepto- and photo-production of J/ψ
 - Both are very naturally included in our factorization formalism with universal LDFs
 - We found NLP contribution from the production of charm-anticharm pair dominates the production rate
 - We introduced a systematic matching between the fixed-order NRQCD calculation and our factorized contributions
- We calculated nuclear dependence of J/ψ production in eA collisions
 - Soft interaction between colliding nuclei and the hadronization to J/ψ can potentially break the factorization
 - Nuclear dependence from nuclear PDFs, multiple scattering, and de-coherence of the charm-anticharm pair
- Heavy quarkonium production offers more opportunities and challenges

Thanks!

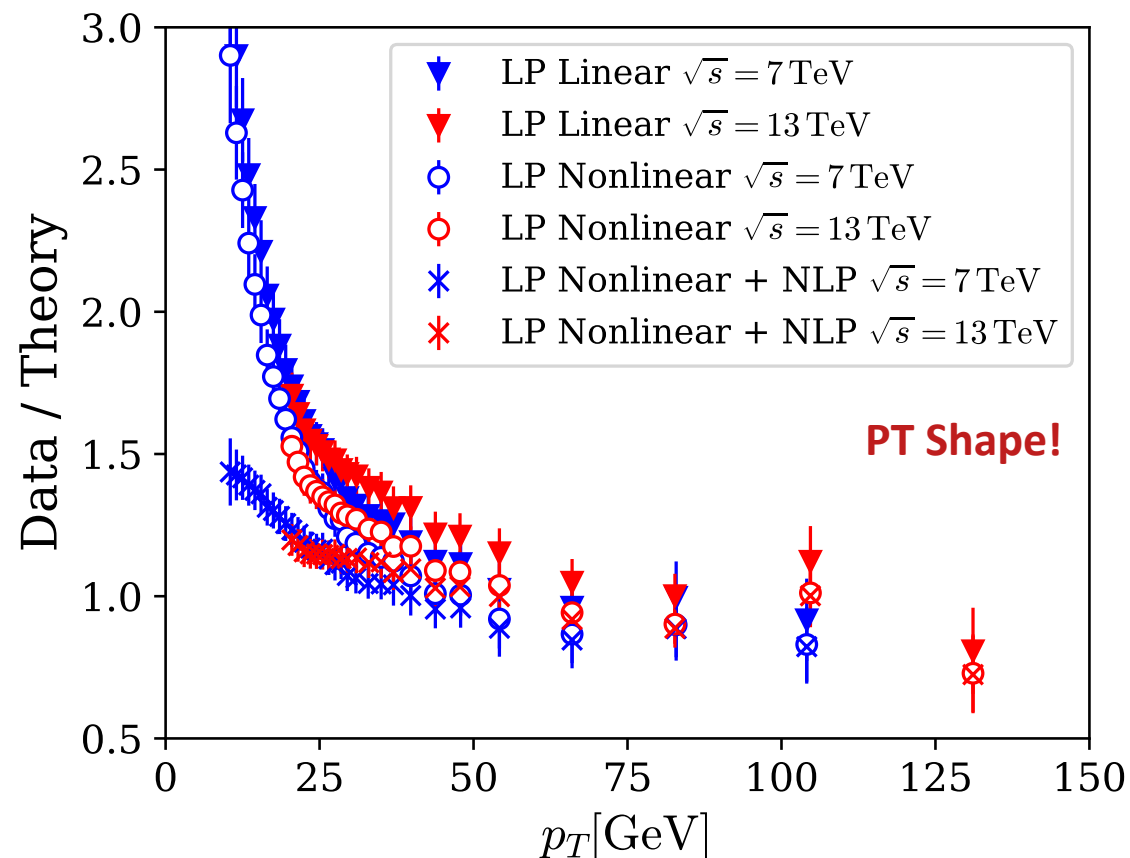
Backup slides

Single inclusive J/ψ -production in hadronic collisions

Lee, Qiu, Sterman, Watanabe, 2022

Leading power contribution:

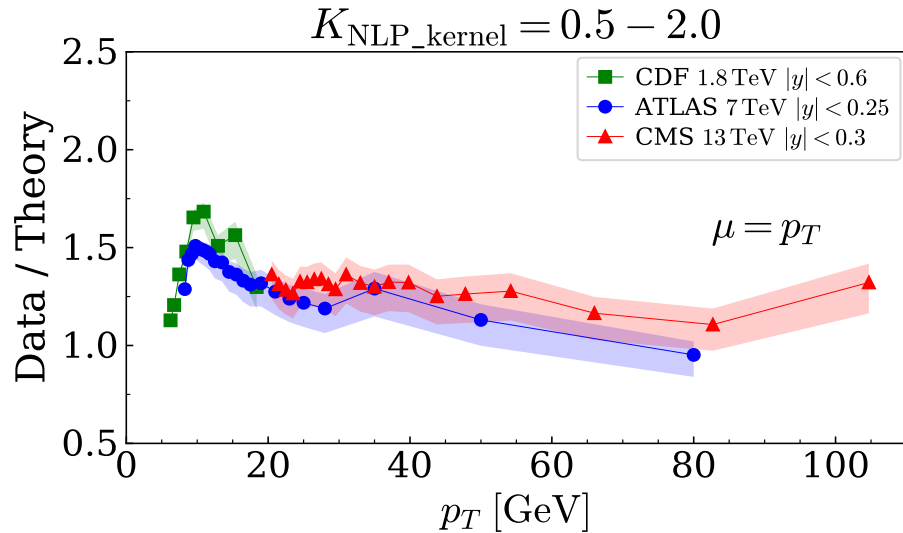
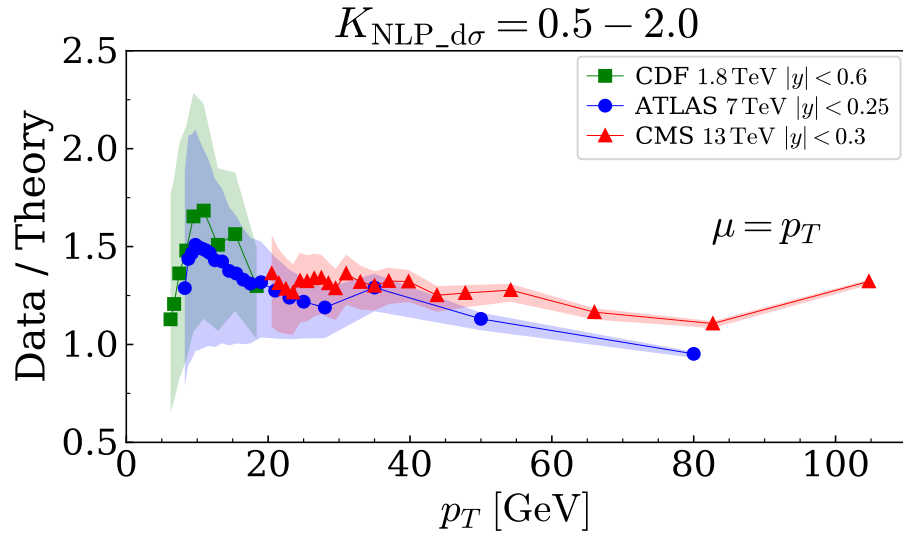
- Fitting the LP formalism with the linear evolution eq. to CMS data on high p_T prompt J/ψ at $\sqrt{s} = 7, 13$ TeV in the bin, $|y| < 1.2$.
- # of data points in a fit: $3@7\text{TeV} + 4@13\text{TeV} = 7$ for $p_T \geq 60$ GeV.
- Only the $^1S_0^{[8]}$ channel is considered, yielding unpolarized J/ψ . The other two color octet channels could overshoot data by combining LP and NLP.
- $\langle \mathcal{O}(^1S_0^{[8]}) \rangle / \text{GeV}^3 = 0.1286 \pm 5.179 \cdot 10^{-3}$ fitted by high p_T data is similar to the one extracted using fixed order NRQCD at NLO. [Chao, Ma, Shao, Wang, Zhang, PRL108, 242004 \(2012\)](#)
- Global data fitting is useful to pin down LDMEs and the shape of input FFs.



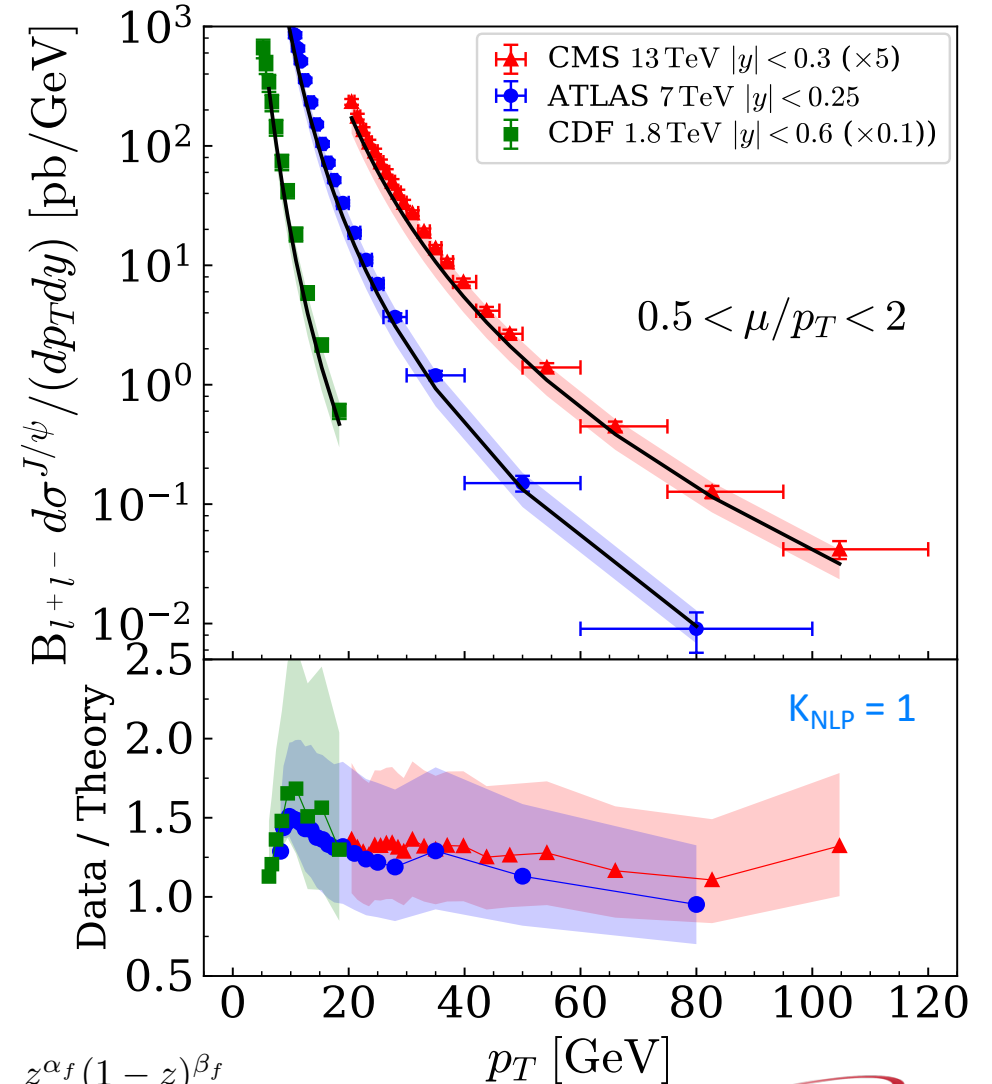
The “power corrections” do not vanish even at the highest p_T , giving 10-30% corrections.
At $p_T = 30$ GeV and below, the NLP corrections become significant.

Uncertainty of theoretical calculations for hadronic collisions

□ K-factor for NLP:



□ Choice of factorization/renormalization scale:



Model III FFs:

$$D_{f \rightarrow H}(z) = N_f \frac{z^{\alpha_f} (1-z)^{\beta_f}}{B(1+\alpha_f, 1+\beta_f)}$$