

Meson structure at JLab 22 GeV

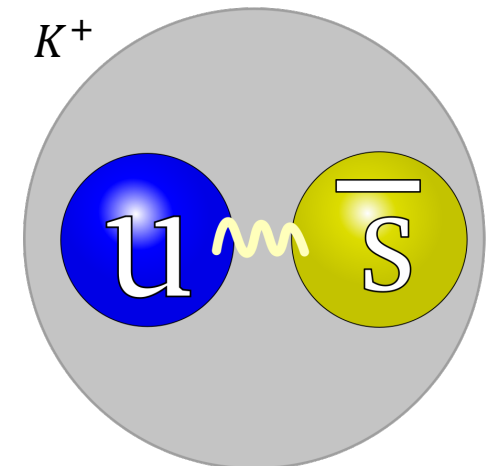
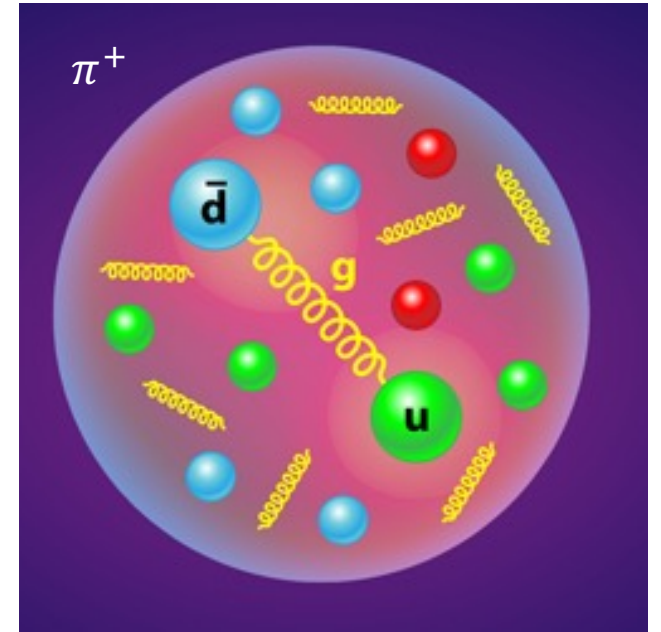
Patrick Barry, JLab

Science at the Luminosity Frontier: Jefferson Lab at 22 GeV Workshop

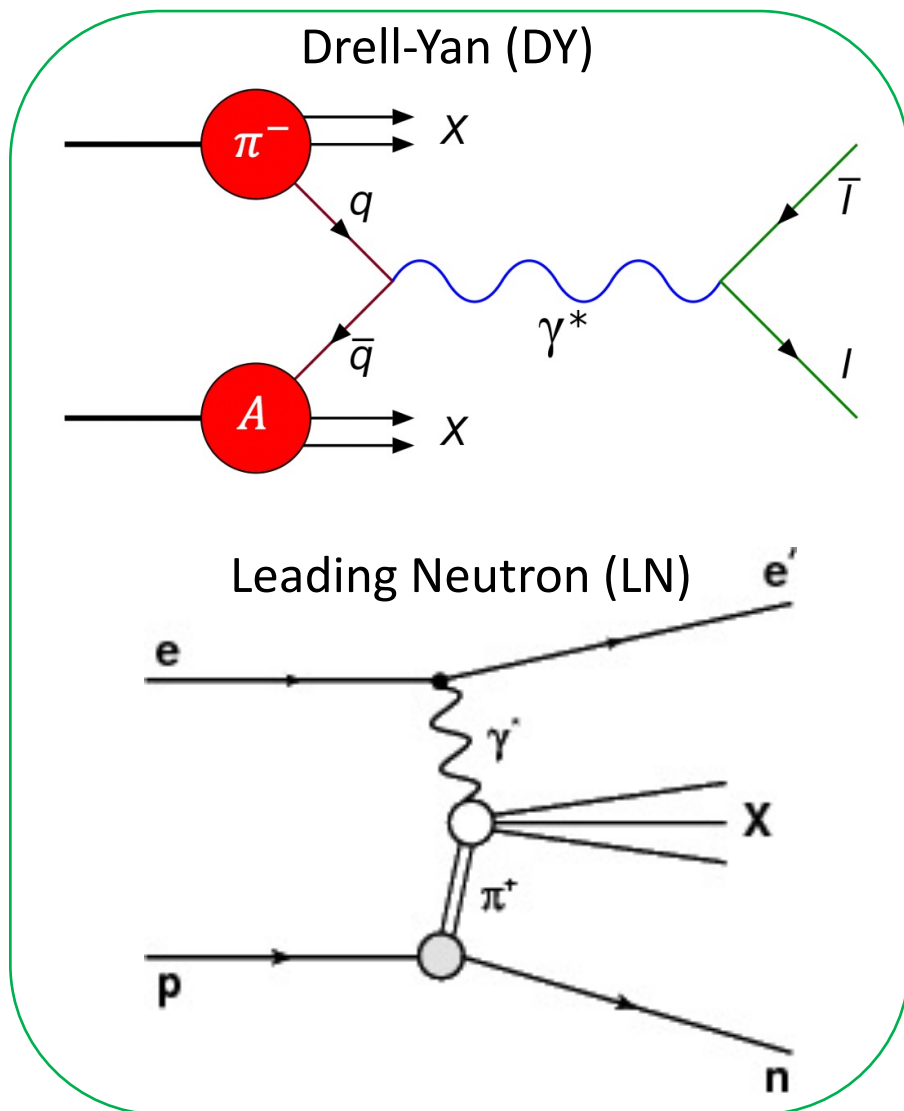
January 23th, 2023

Mesons

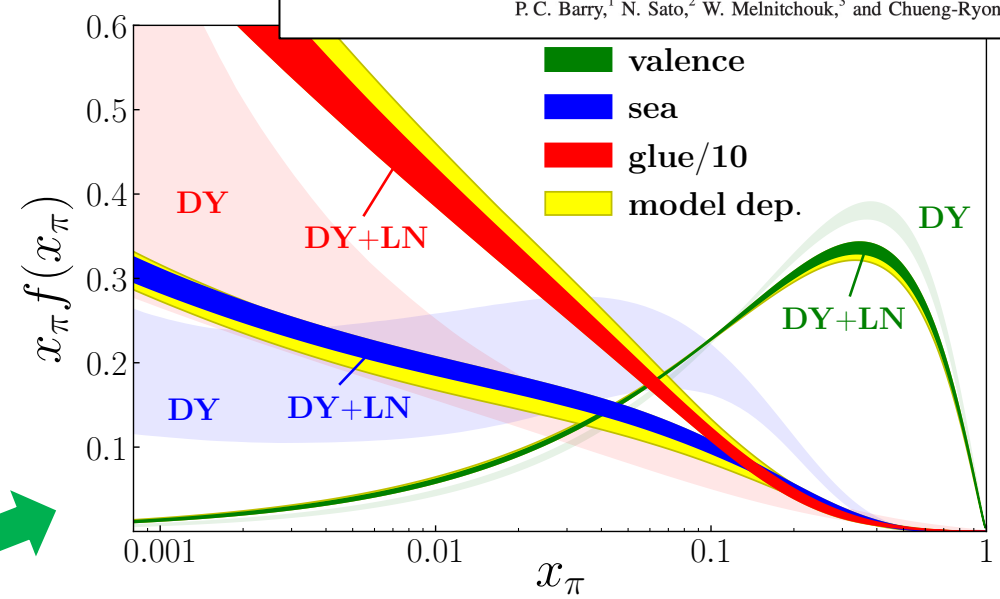
- Pion is the **Goldstone boson** associated with SU(2) chiral symmetry breaking
- Kaon – SU(3)
- Simultaneously a $q\bar{q}$ bound state
- Studying these structures provides another angle to **probe QCD** and effective confinement scales
- More available data is desperately needed



Pion PDFs in JAM



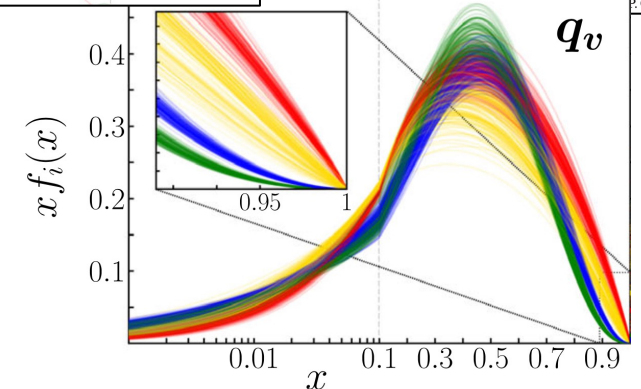
PHYSICAL REVIEW LETTERS 121, 152001 (2018)
 Featured in Physics
First Monte Carlo Global QCD Analysis of Pion Parton Distributions
 P. C. Barry,¹ N. Sato,² W. Melnitchouk,³ and Chueng-Ryong Ji¹



Threshold resummation in DY

Legend for zoomed plot:
 NLO (red)
 NLO+NLL cosine (green)
 NLO+NLL expansion (blue)
 NLO+NLL double Mellin (yellow)

PHYSICAL REVIEW LETTERS 127, 232001 (2021)
Global QCD Analysis of Pion Parton Distributions with Threshold Resummation
 P. C. Barry,¹ Chueng-Ryong Ji,² N. Sato,¹ and W. Melnitchouk¹



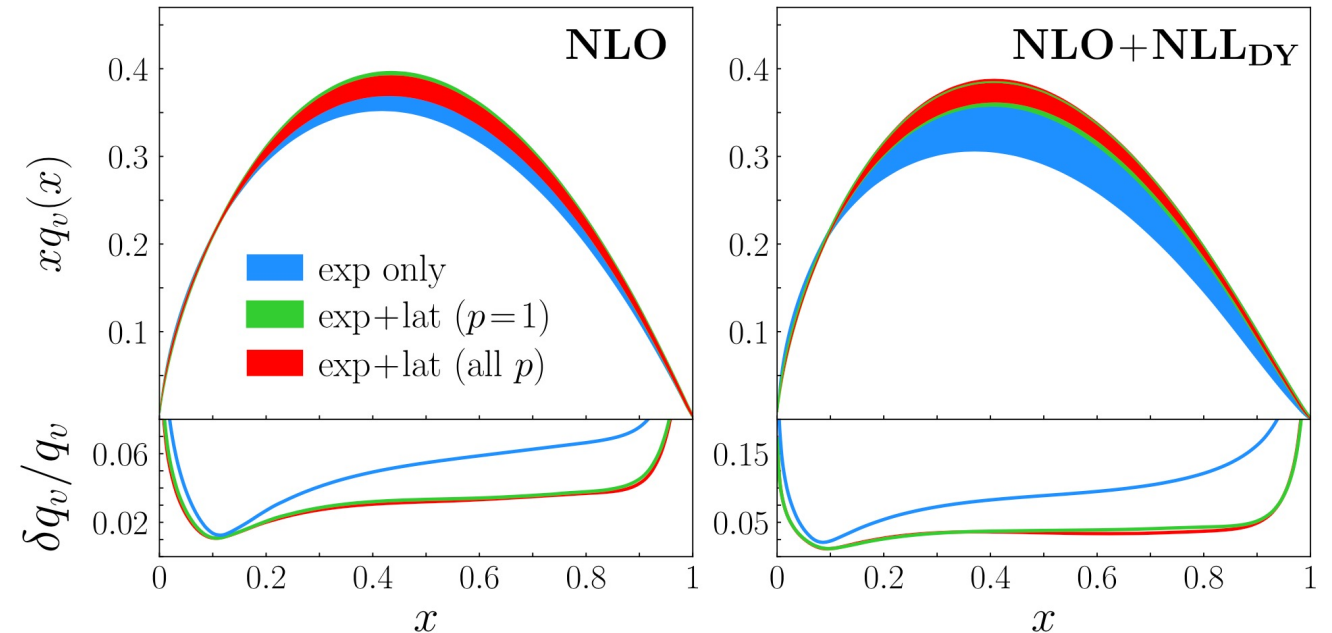
Pion PDFs from lattice + experimental data

PHYSICAL REVIEW D **105**, 114051 (2022)

Complementarity of experimental and lattice QCD data on pion parton distributions

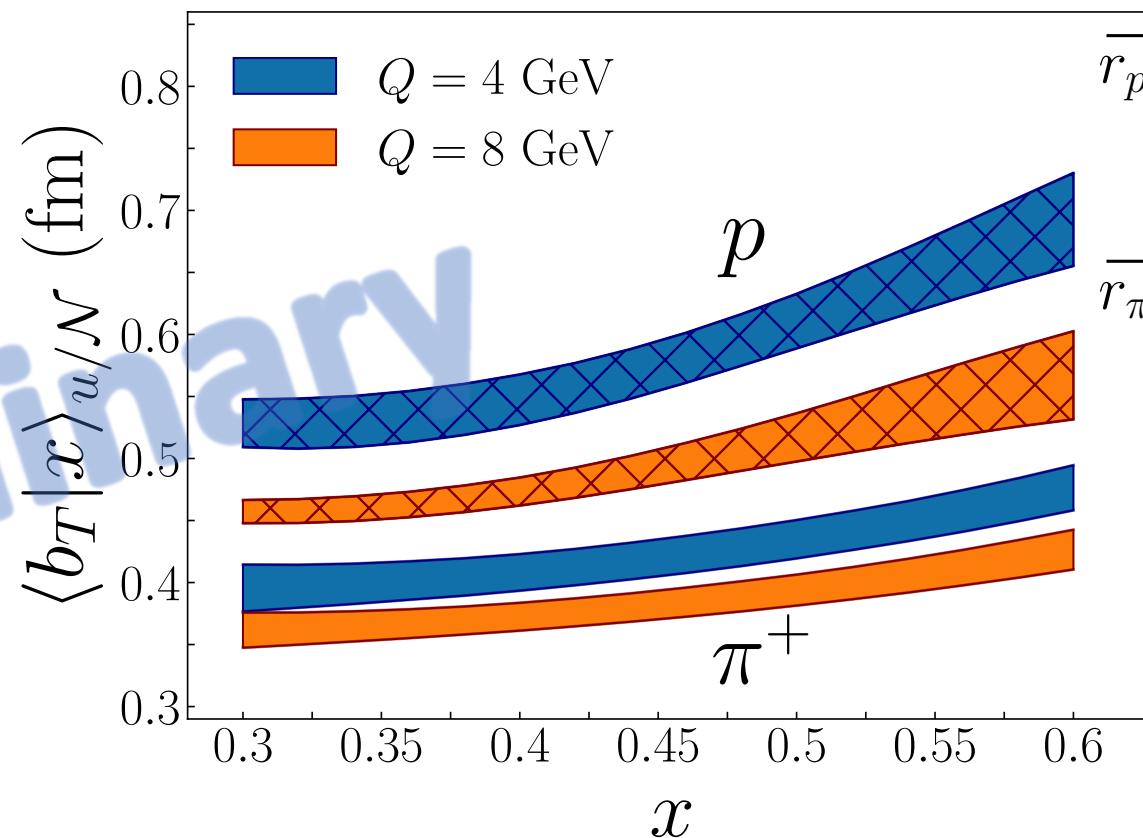
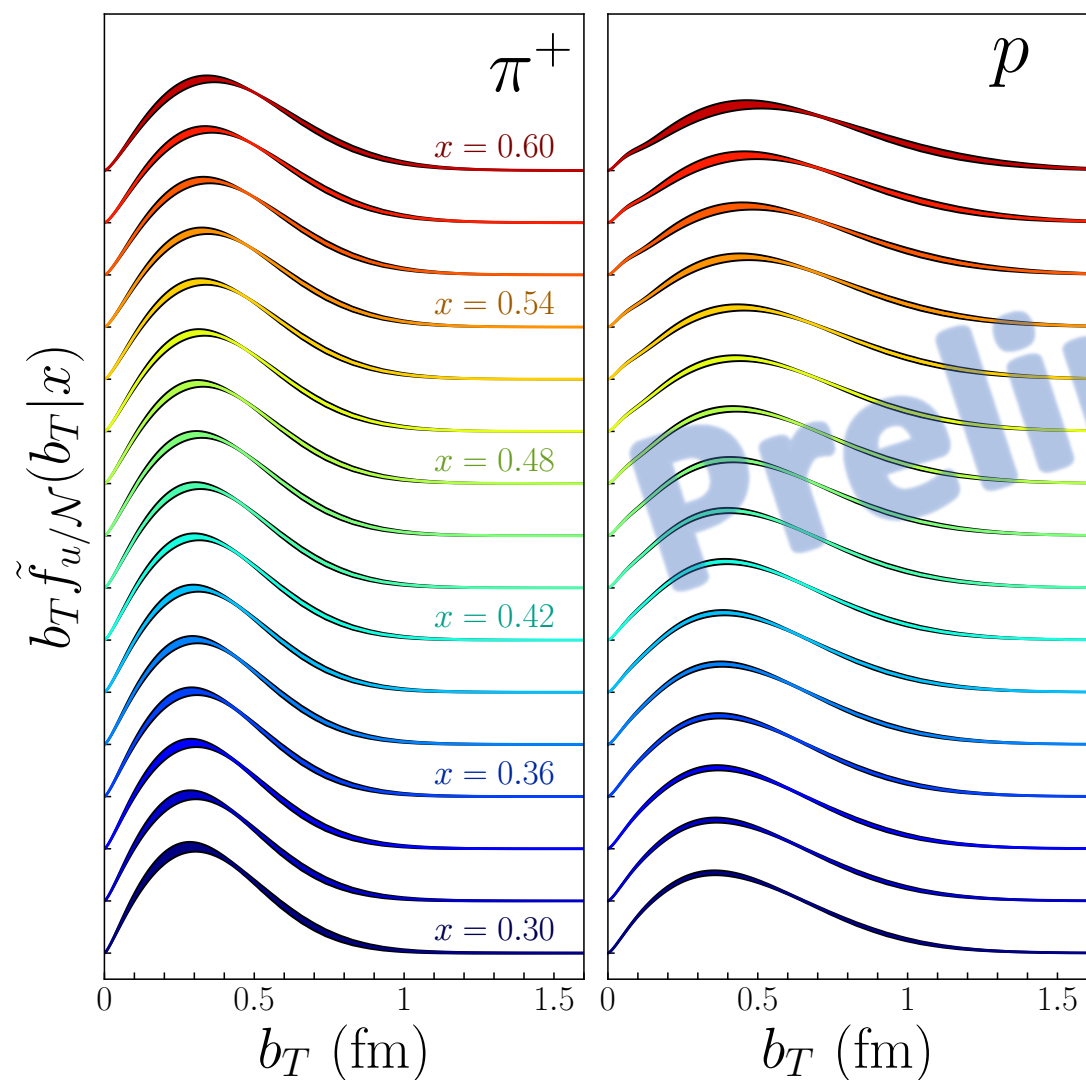
P. C. Barry¹, C. Egerer¹, J. Karpie², W. Melnitchouk¹, C. Monahan^{1,3}, K. Orginos^{1,3},
Jian-Wei Qiu^{1,3}, D. Richards¹, N. Sato¹, R. S. Sufian^{1,3} and S. Zafeiropoulos⁴

(Jefferson Lab Angular Momentum (JAM) and HadStruc Collaborations)



- The inclusion of lattice QCD data along with experimental data can also help us to reveal pion structure

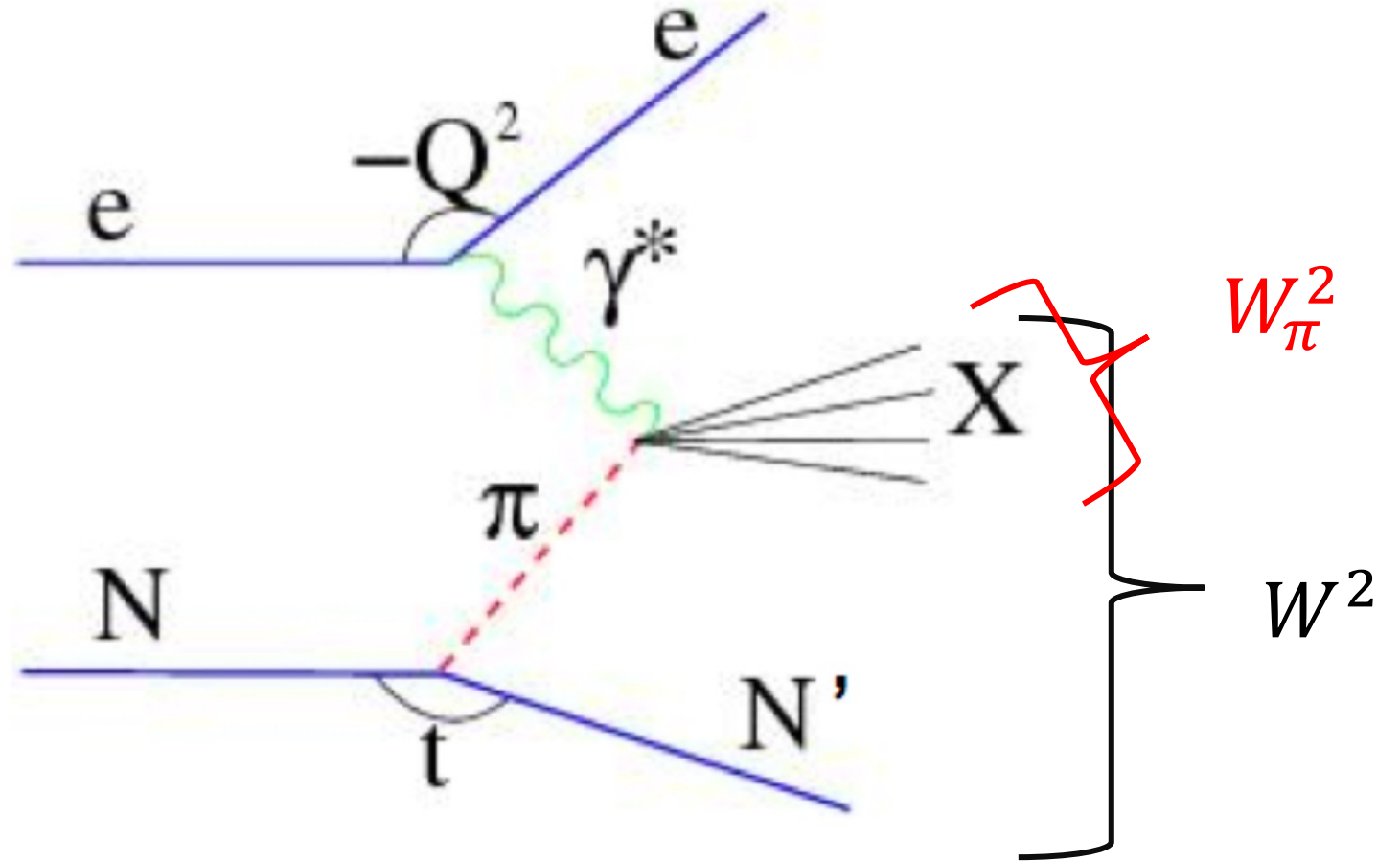
Pion vs proton TMDs



- Differences are purely non-perturbative TMDs
- Important to compare different hadronic systems

TDIS program: Sullivan process and W_{π}^2

- Impose kinematic cuts on experimental data
- What about the W_{π}^2 ?



Check the resonance regions

π^\pm

$$I^G(J^P) = 1^-(0^-)$$

Mass $m = 139.57039 \pm 0.00018$ MeV (S = 1.8)
Mean life $\tau = (2.6033 \pm 0.0005) \times 10^{-8}$ s (S = 1.2)
 $c\tau = 7.8045$ m

γ (photon)

$$I(J^{PC}) = 0,1(1^{--})$$

Mass $m < 1 \times 10^{-18}$ eV
Charge $q < 1 \times 10^{-46}$ e (mixed charge)
Charge $q < 1 \times 10^{-35}$ e (single charge)
Mean life $\tau =$ Stable

$\rho(770)$

$$I^G(J^{PC}) = 1^+(1^{--})$$

See the note in $\rho(770)$ Particle Listings.
Mass $m = 775.26 \pm 0.25$ MeV
Full width $\Gamma = 149.1 \pm 0.8$ MeV
 $\Gamma_{ee} = 7.04 \pm 0.06$ keV

$b_1(1235)$

$$I^G(J^{PC}) = 1^+(1^{+-})$$

Mass $m = 1229.5 \pm 3.2$ MeV (S = 1.6)
Full width $\Gamma = 142 \pm 9$ MeV (S = 1.2)

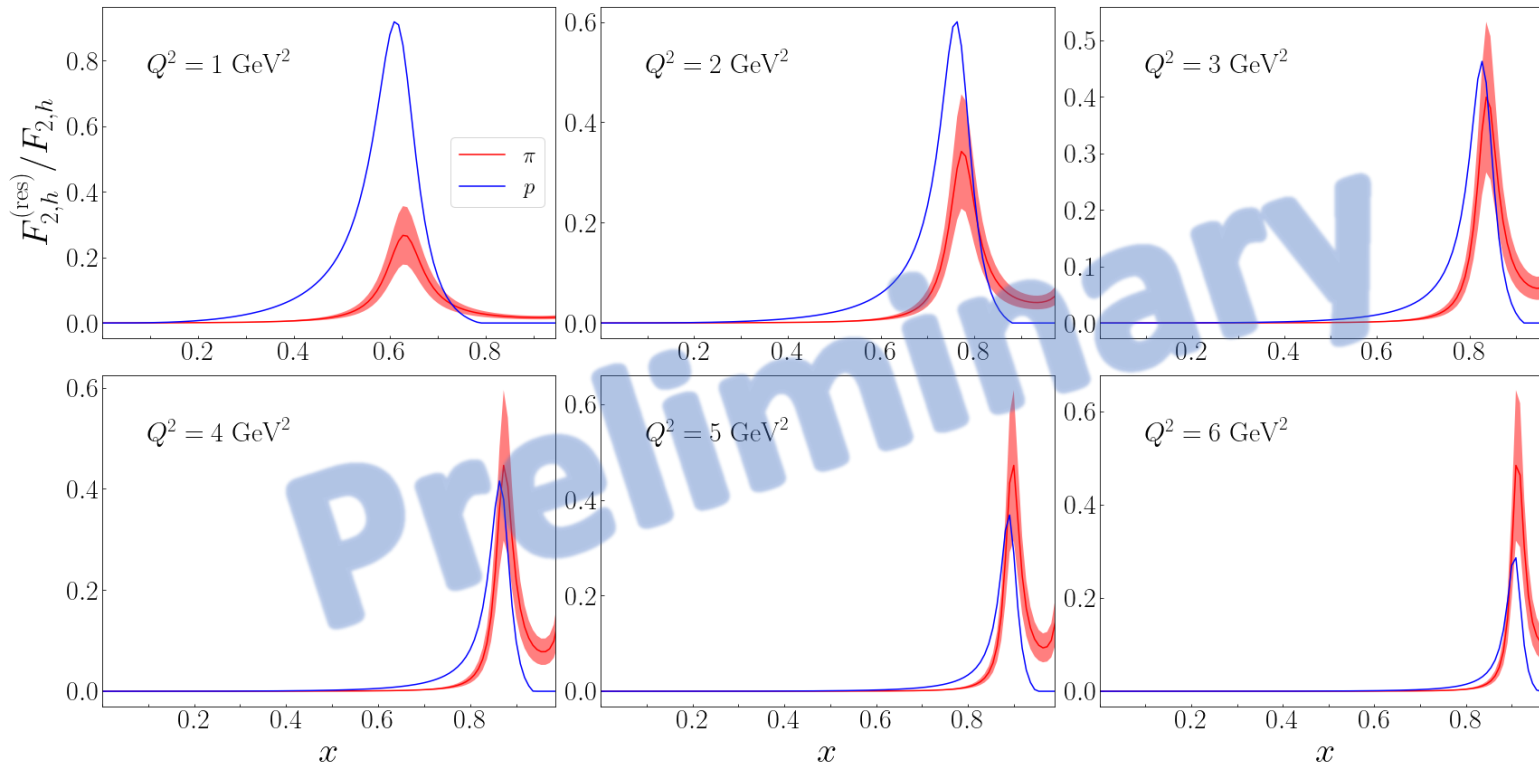
$a_2(1320)$

$$I^G(J^{PC}) = 1^-(2^{++})$$

Mass $m = 1316.9 \pm 0.9$ MeV (S = 1.9)
Full width $\Gamma = 107 \pm 5$ MeV [1]

The quantum numbers of a charged π and photon result in specific outgoing mesons, here considered the ρ -meson

Contribution from ρ to F_2^π

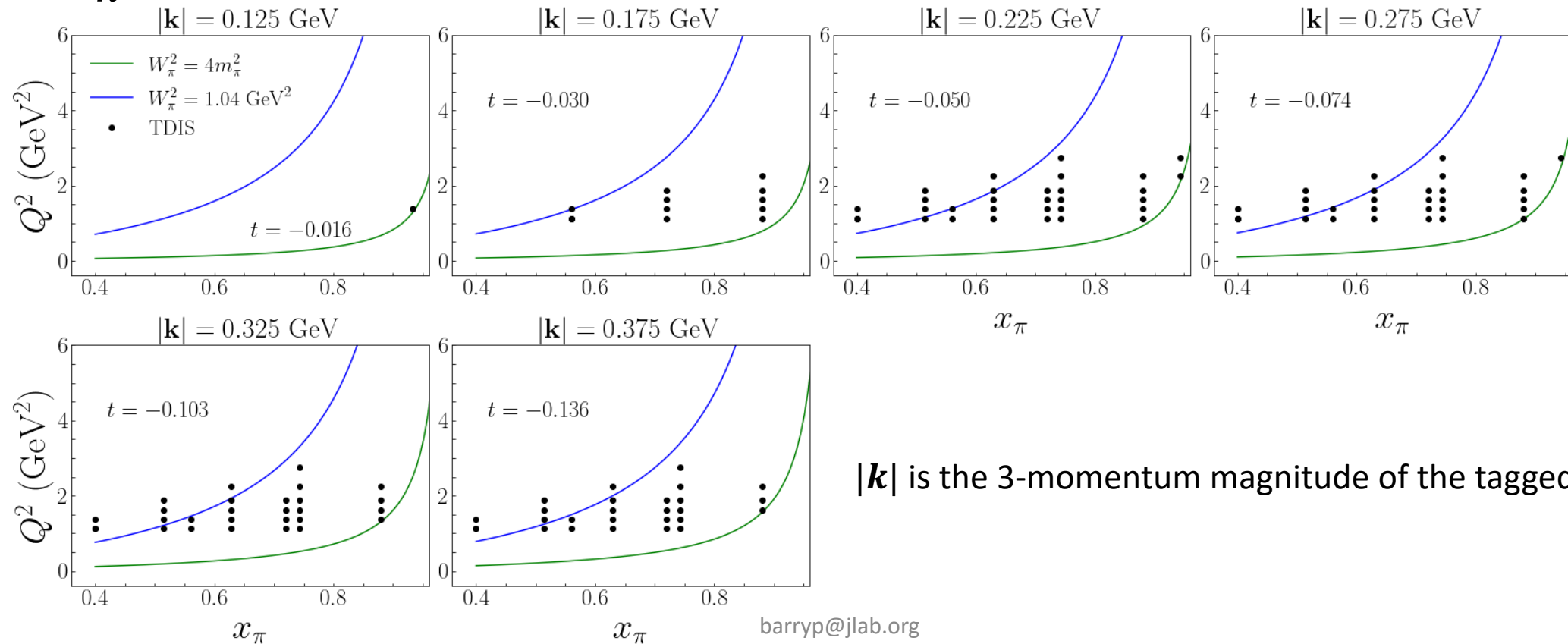


Δ resonance courtesy of
Astrid Hiller Blin

- Comparing the Δ resonance in the nucleon to the ρ resonance in the pion
- Appreciable certainly at larger Q^2 – challenging to describe with partonic degrees of freedom – introduce a cut in W_π^2

Current 11 GeV TDIS kinematics

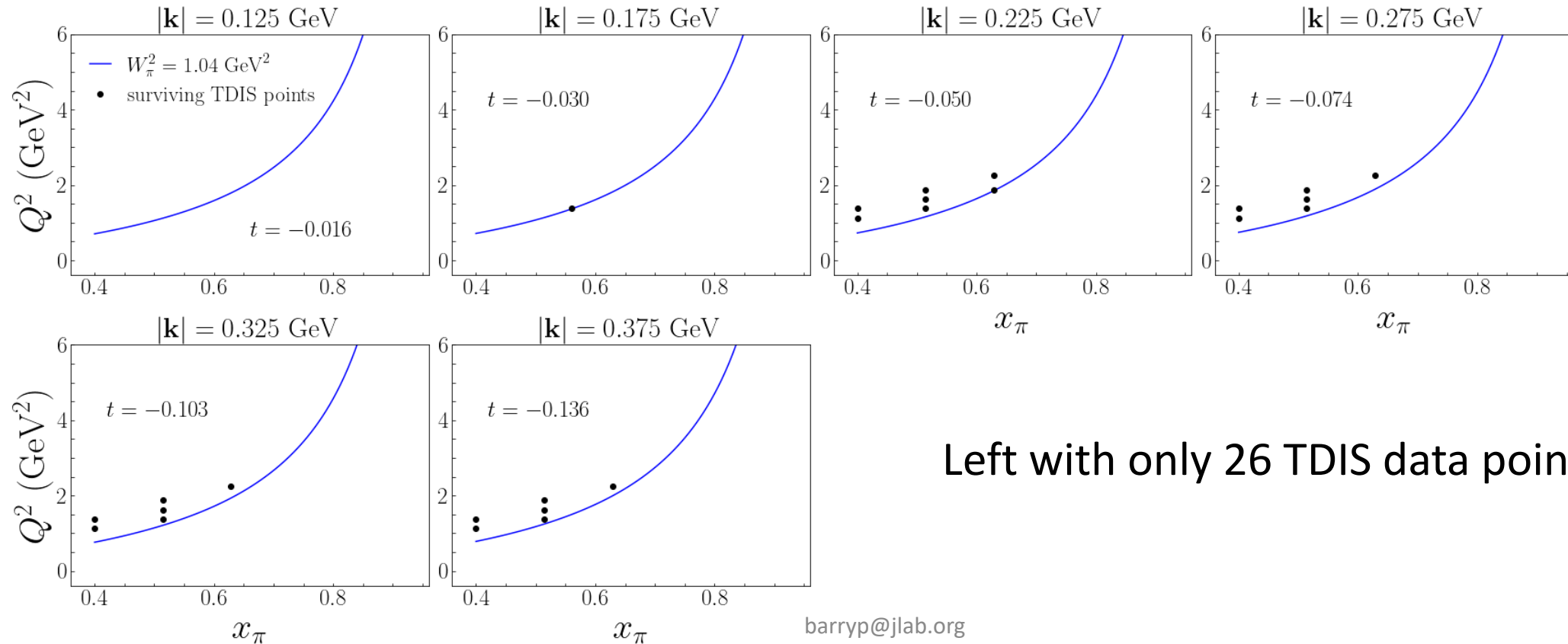
- Plotting available 11 GeV TDIS kinematics with a few representative W_π^2 curves



$|\mathbf{k}|$ is the 3-momentum magnitude of the tagged nucleon

Choosing $W_{\pi,\max}^2 = 1.04 \text{ GeV}^2$

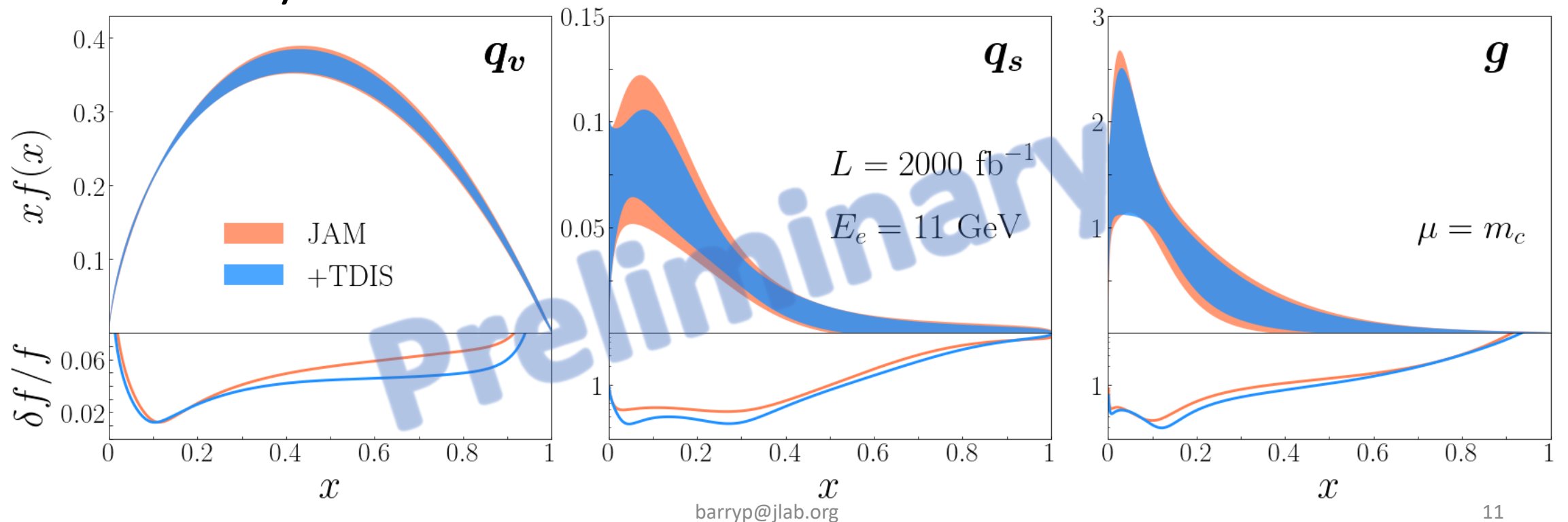
- Removing all data points that could be contaminated by ρ -resonance regions



Left with only 26 TDIS data points

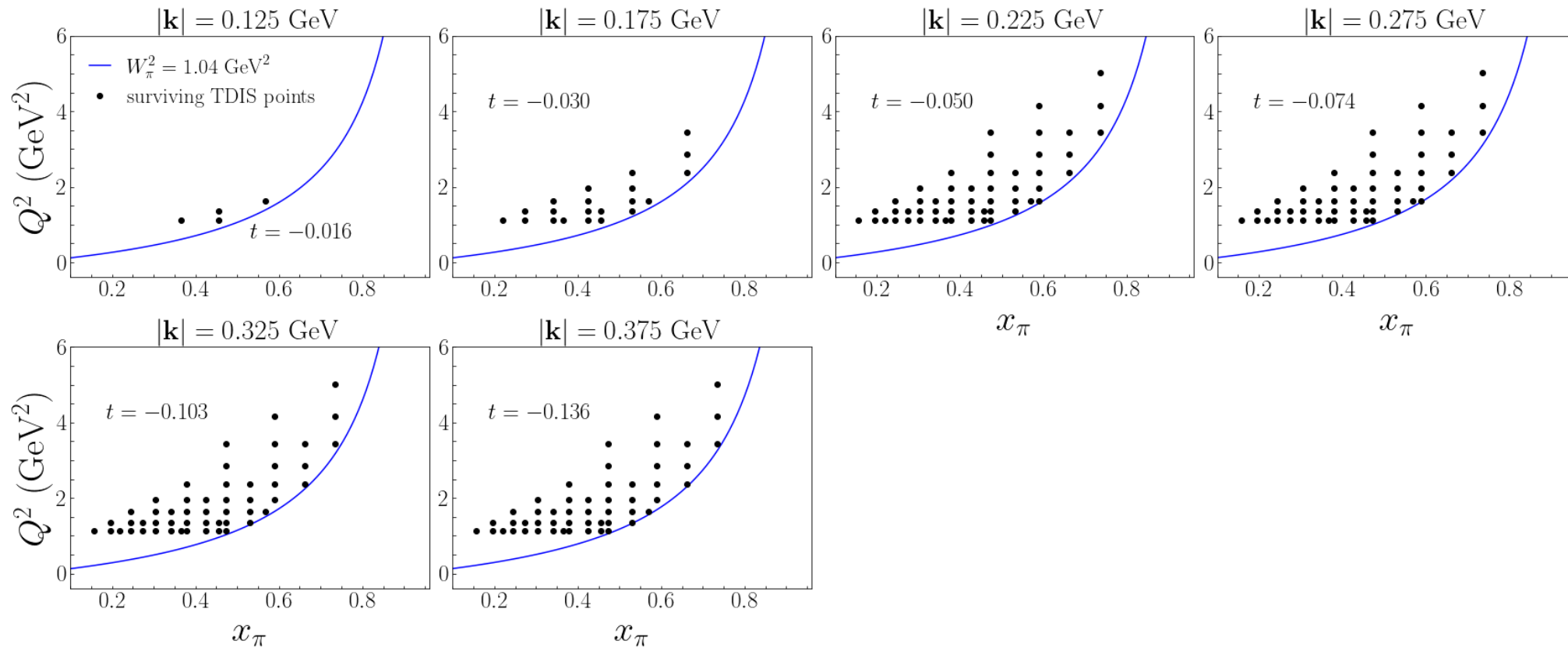
Performing impact study with 11 GeV

- Create pseudodata from these points and perform global analysis with available experimental data assuming 6.5% systematic uncertainty



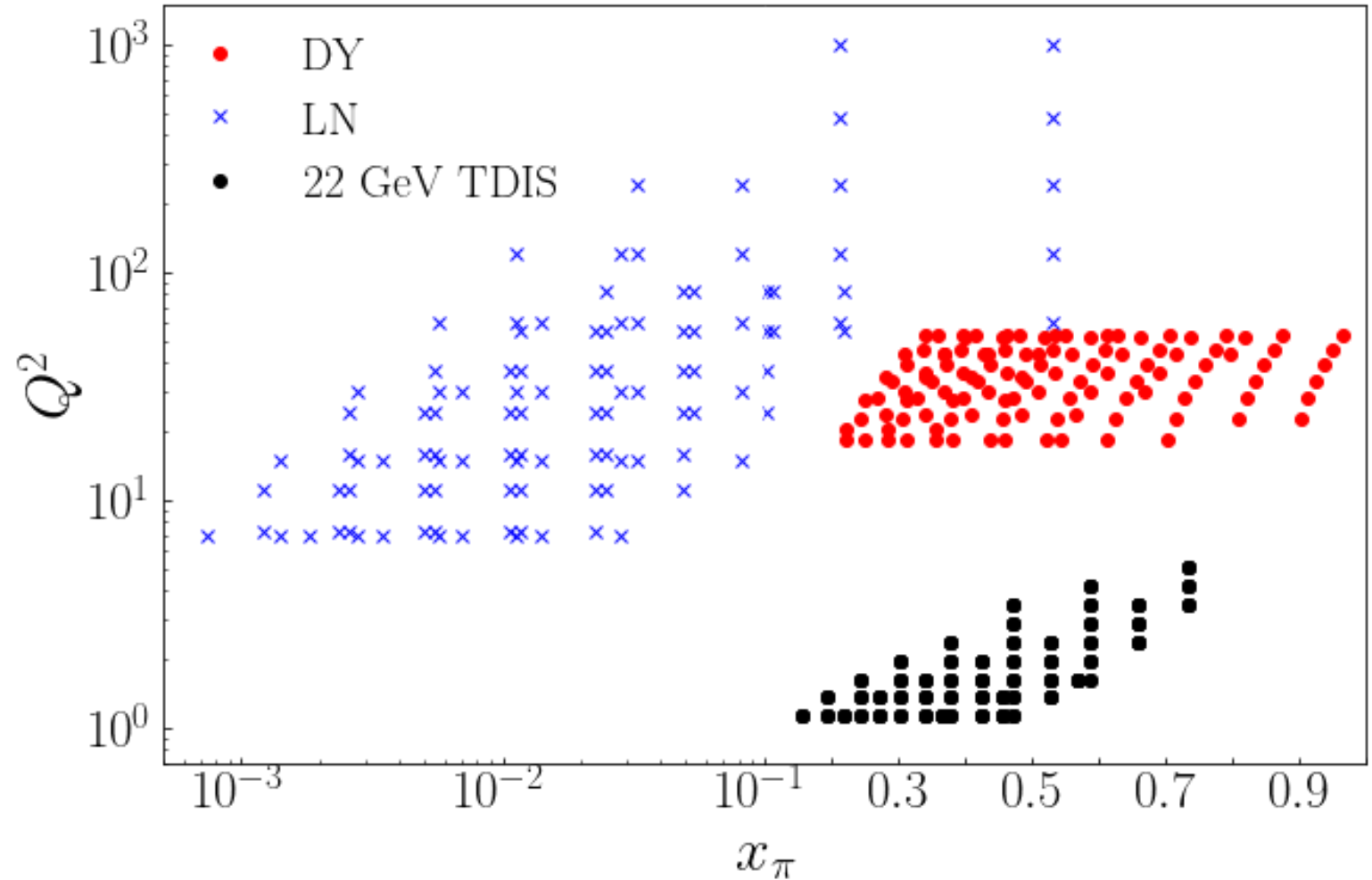
Kinematics with 22 GeV

- MASSIVE increase in available data points



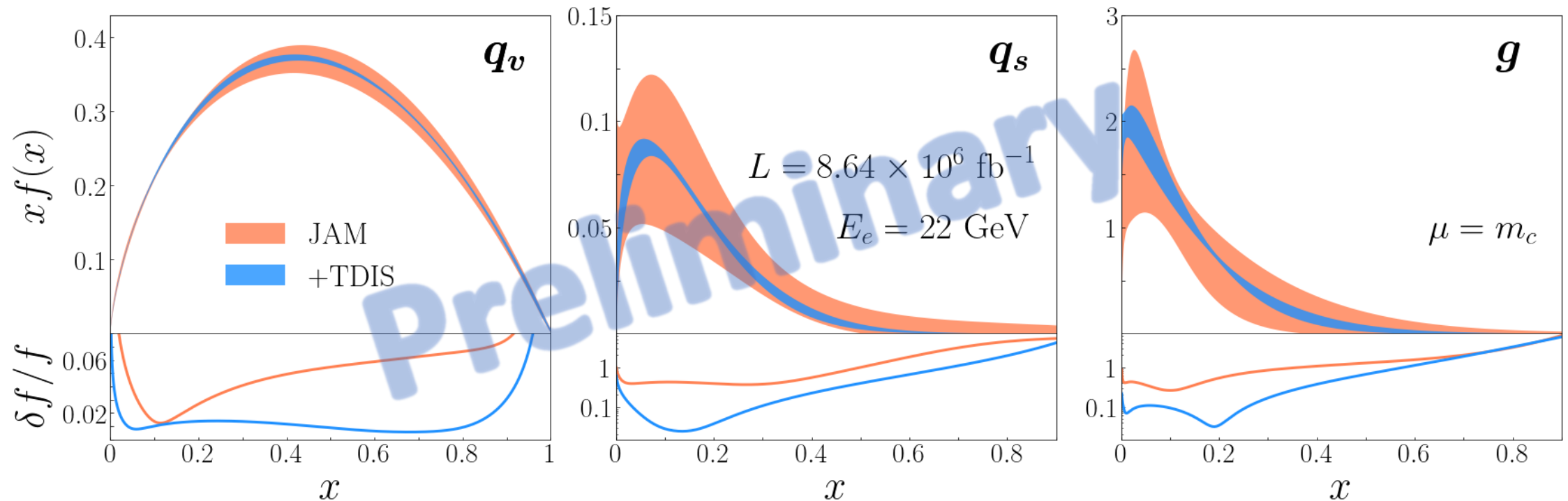
Total kinematics

- Much larger range in x_π and Q^2



Impact on pion PDFs with 22 GeV

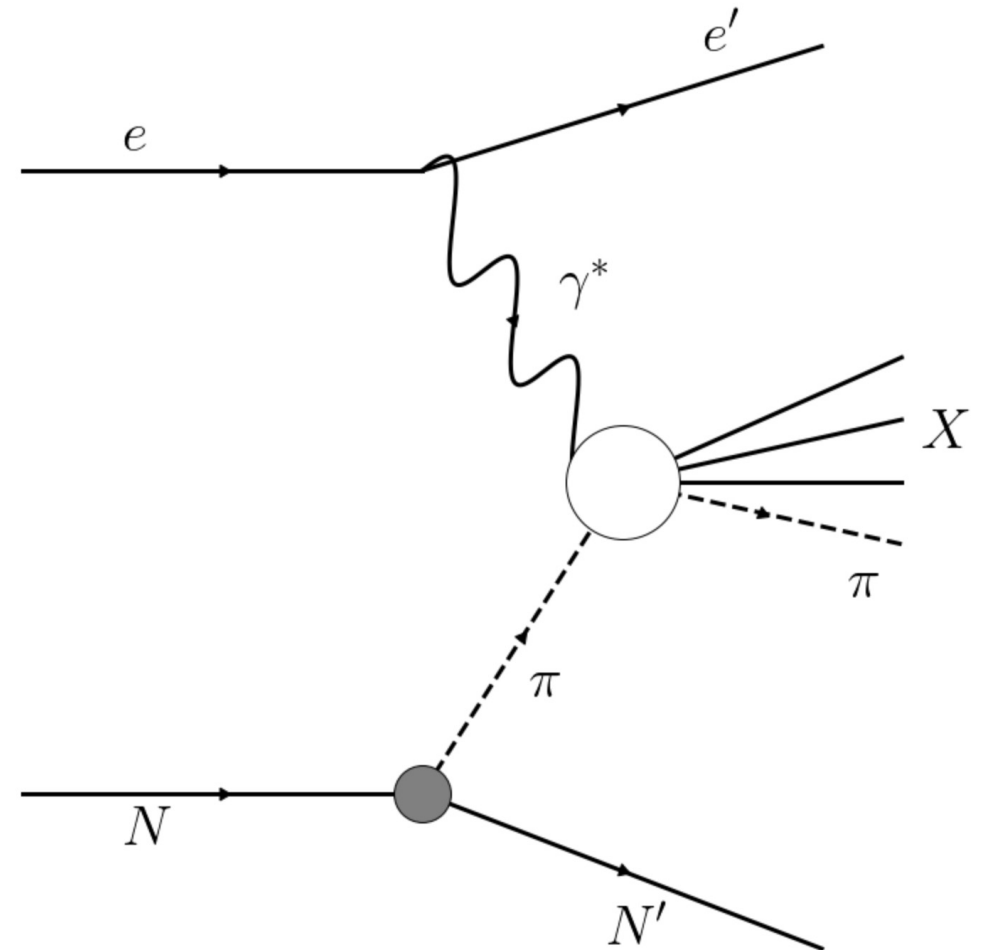
- Knowledge of pion PDFs increases dramatically with 22 GeV beam
- Assuming 1.2% systematic uncertainty



Pion SIDIS: access to TMDs

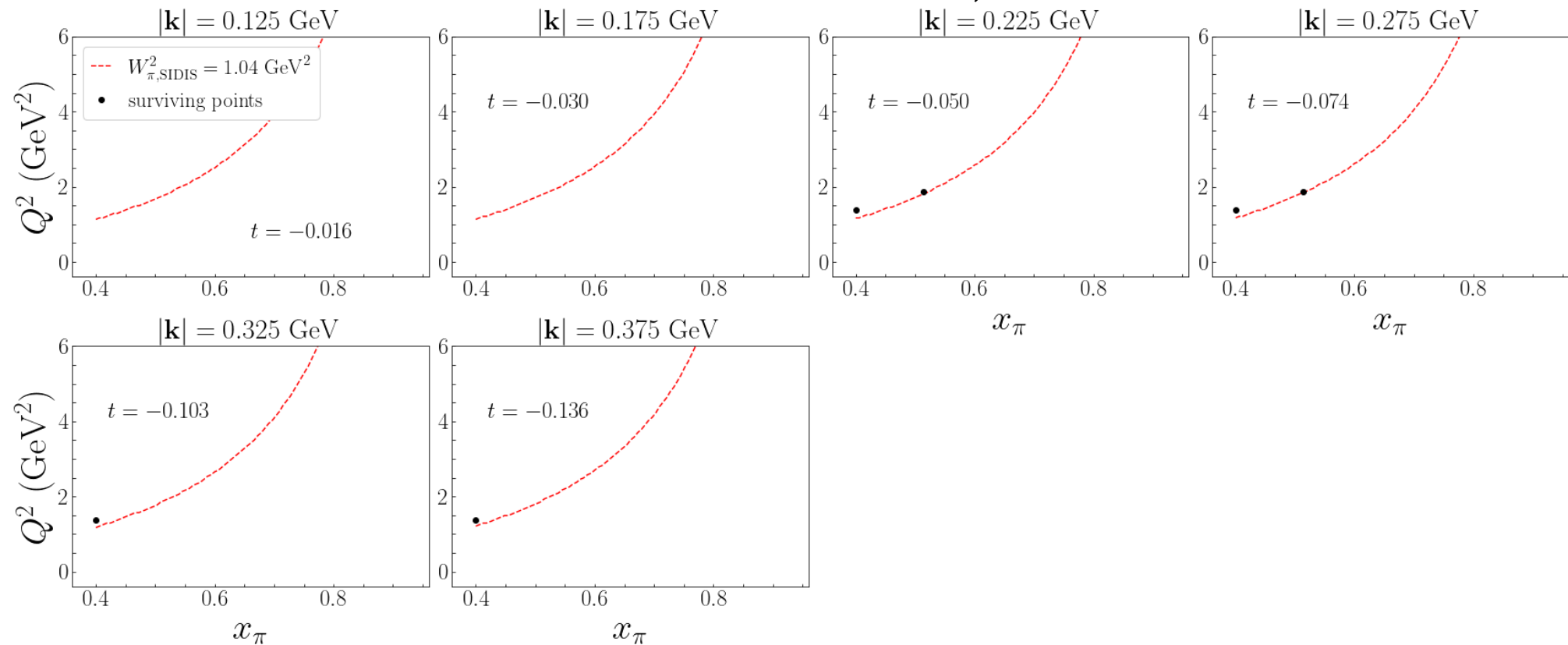
$$eN \rightarrow e'N'\pi X$$

- Measure an outgoing pion in the TDIS experiment
- Gives us another observable sensitive to pion TMDs
 - Needed for tests of universality



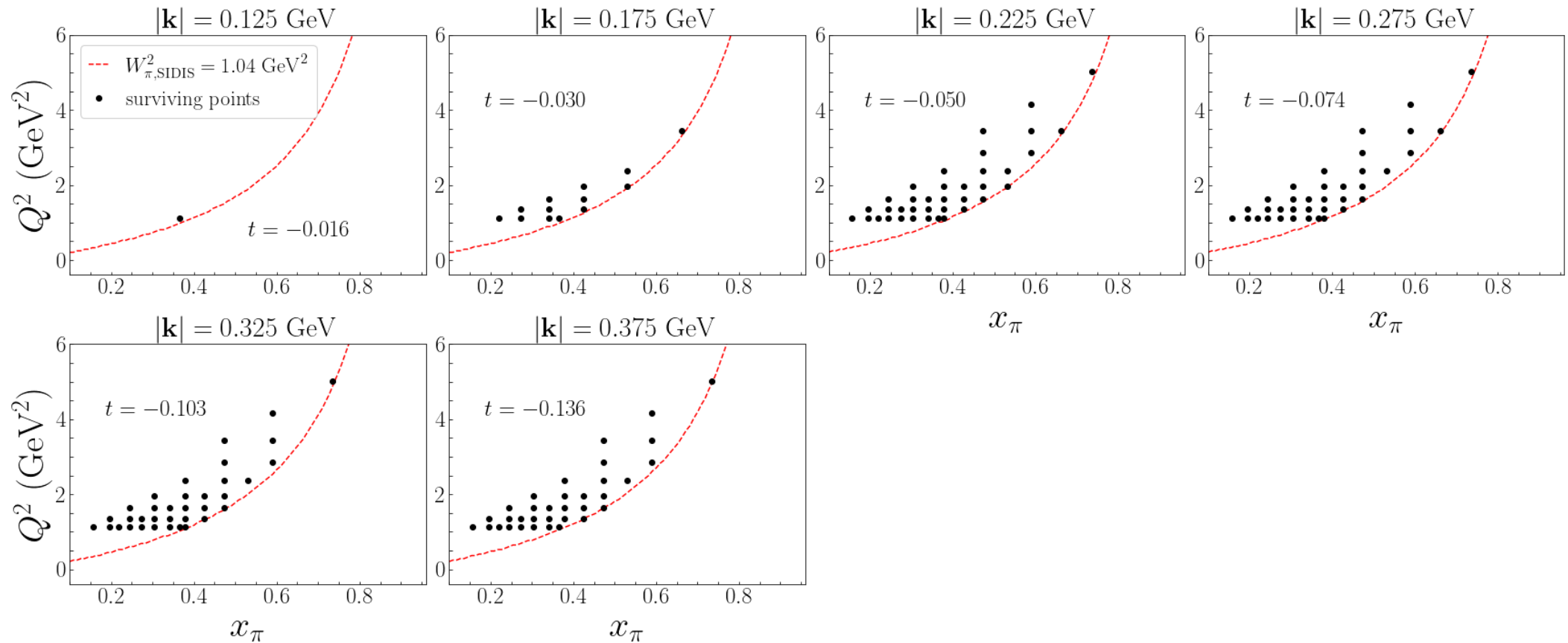
Kinematics with 11 GeV

- Still a cut on $W_\pi^2 = 1.04 \text{ GeV}^2$, but SIDIS requires more phase space
- Hardly anything available with $z = 0.2, P_{h,T} = 0.2 \text{ GeV}$



Kinematics with 22 GeV

- Huge increase – TMD studies becomes possible!



Conclusion

- Impacts from the 11 GeV TDIS experiment on pion PDFs will be limited, but can test the large- x_π behavior inferred from the Drell-Yan data
- The 11 GeV TDIS can measure the low- W_π pion structure function
- **Much** more constraints will come from larger 22 GeV upgrade
- Compared with EIC, JLab can provide more precise data
- Kaon PDF analysis may be more realistic with energy upgrade

Backup Slides

Conditional density

- We define a quantity in which describes the ratio of the 2-dimensional density to the integrated, b_T -independent number density

$$\tilde{f}_{q/\mathcal{N}}(b_T|x; Q, Q^2) \equiv \frac{\tilde{f}_{q/\mathcal{N}}(x, b_T; Q, Q^2)}{\int d^2\mathbf{b}_T \tilde{f}_{q/\mathcal{N}}(x, b_T; Q, Q^2)} .$$

Average b_T

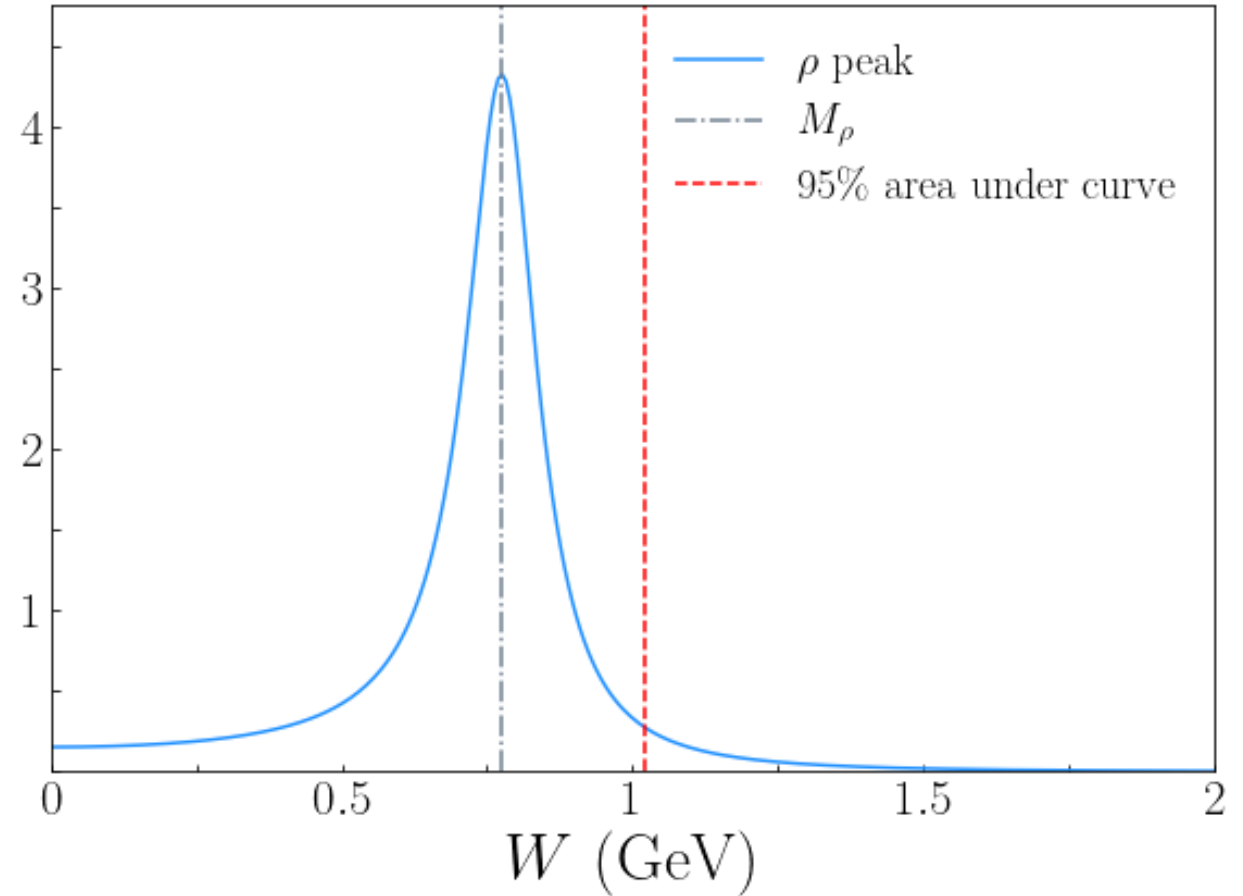
- The conditional expectation value of b_T for a given x

$$\langle b_T | x \rangle_{q/\mathcal{N}} = \int d^2 \mathbf{b}_T b_T \tilde{f}_{q/\mathcal{N}}(b_T | x; Q, Q^2)$$

- Shows a measure of the transverse correlation in coordinate space of the quark in a hadron for a given x

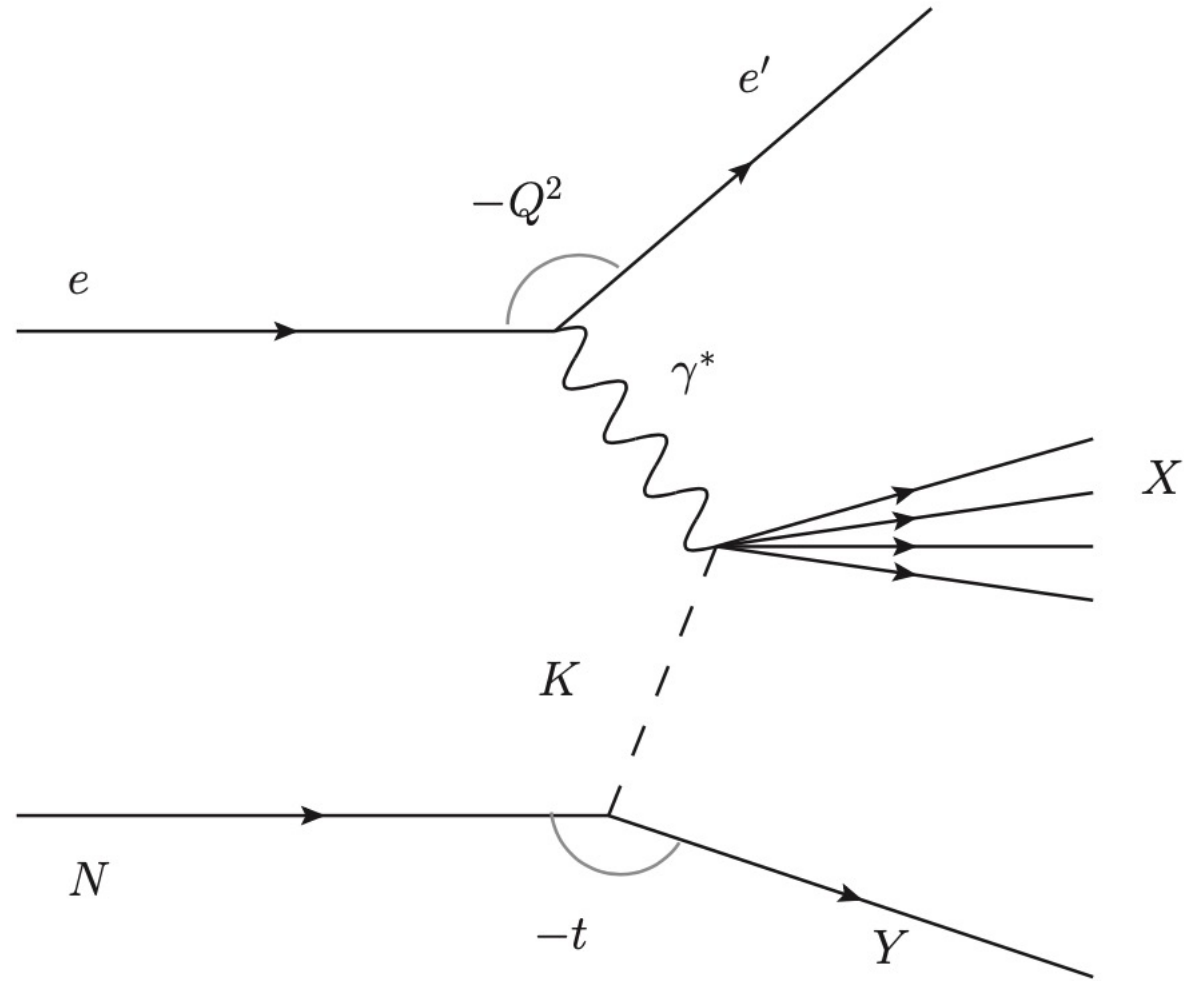
What to choose for W_π^2

- HERA did not measure the low- W_π^2 region
- Potentially largest resonance comes from the ρ -meson
- Must be well above the peak of the resonance
- Estimating the safe region to be an energy above 95% of the area under the curve



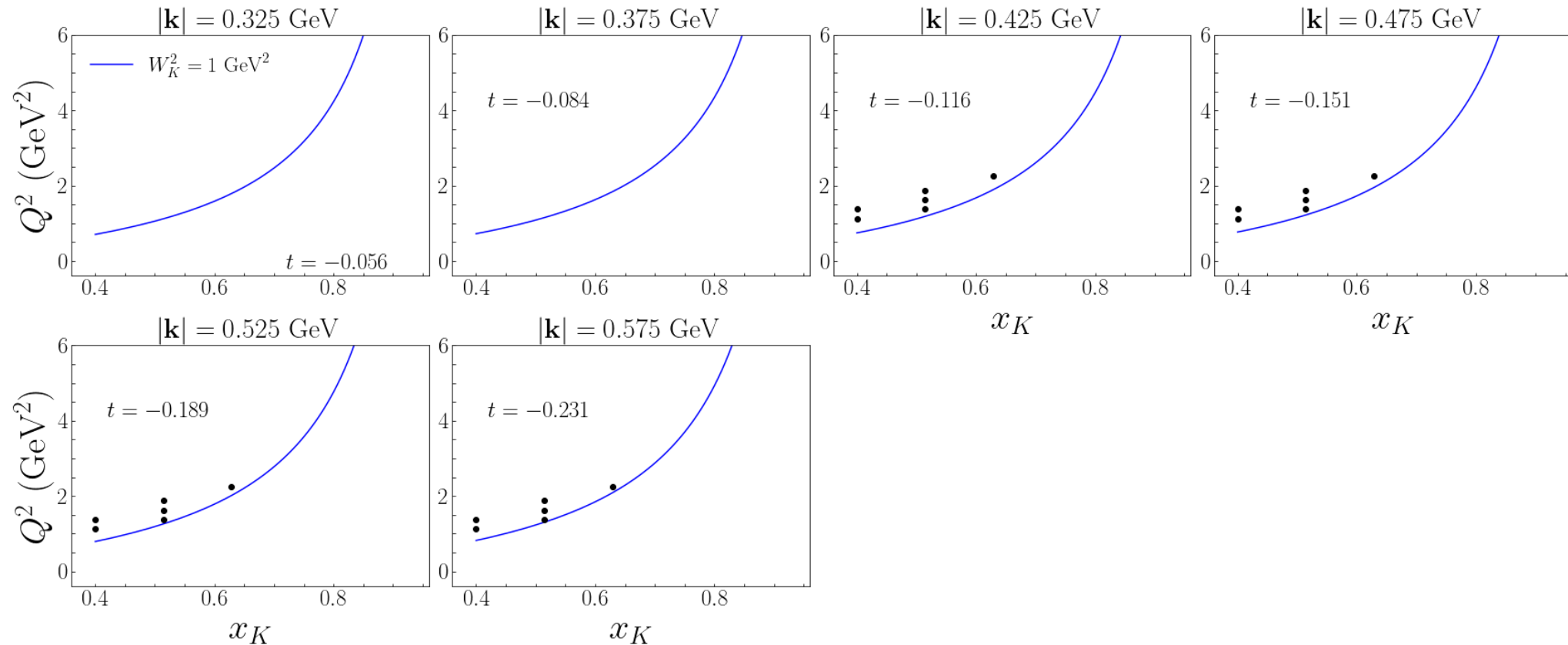
Brief words on kaon TDIS

- Sullivan process applies, but a *hyperon* must be tagged
- Consider again, not only inclusive W^2 but W_K^2



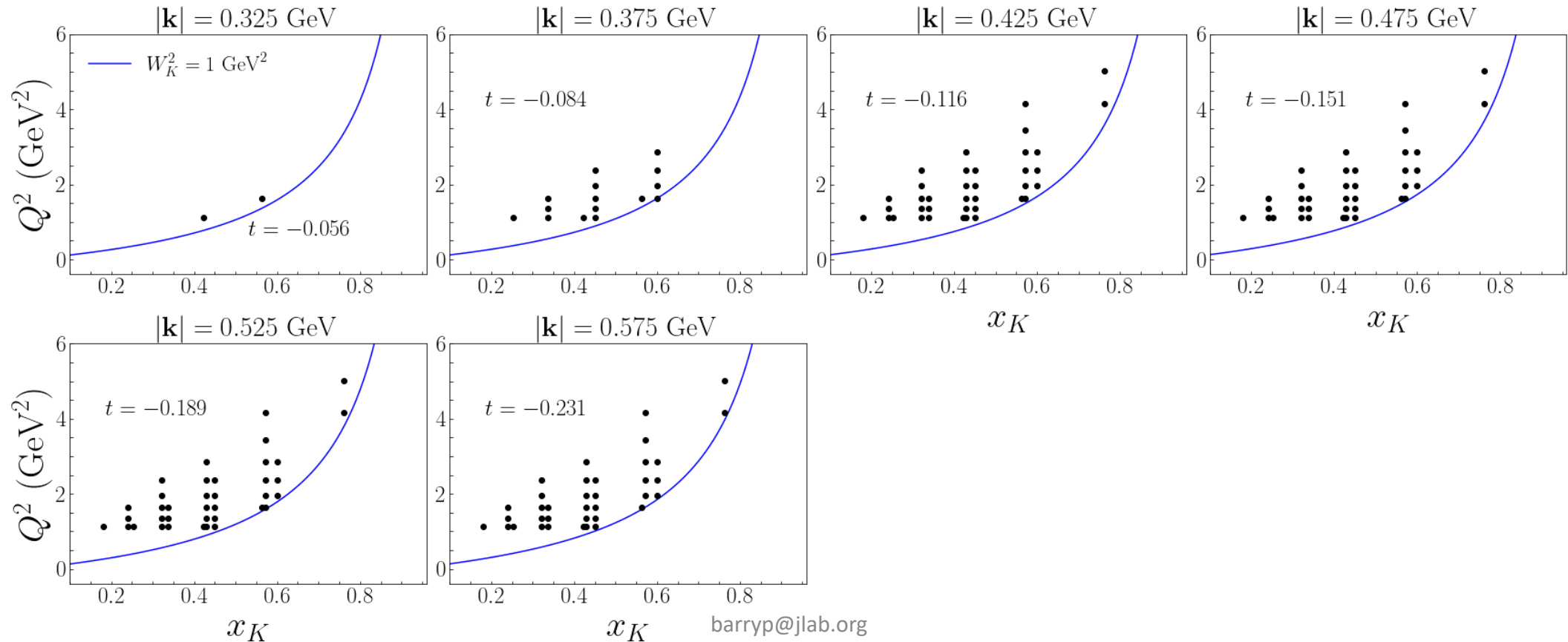
Kinematics for 11 GeV Kaon TDIS

- Beware of such large $|t|$ further away from kaon pole



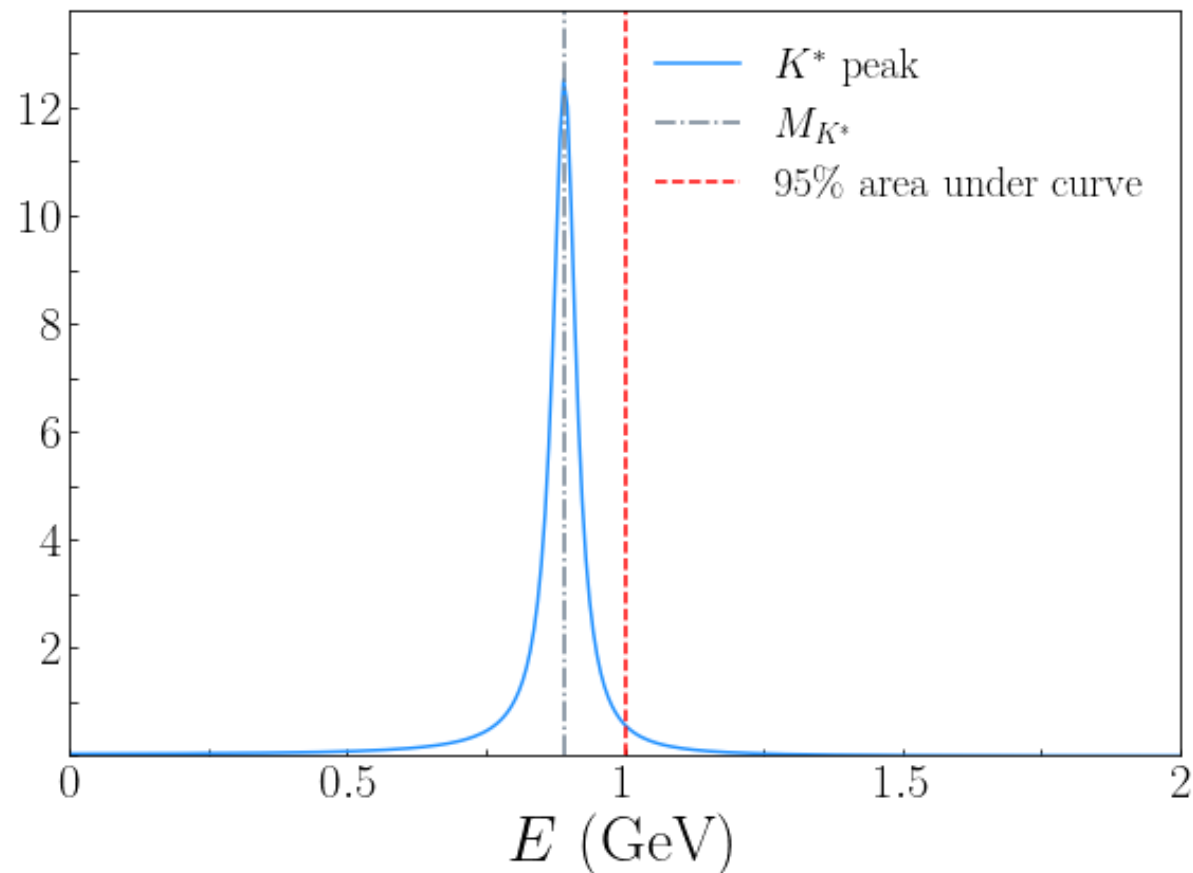
Kinematics for 22 GeV Kaon TDIS

- Accepting of more points at smaller $|\mathbf{k}|$



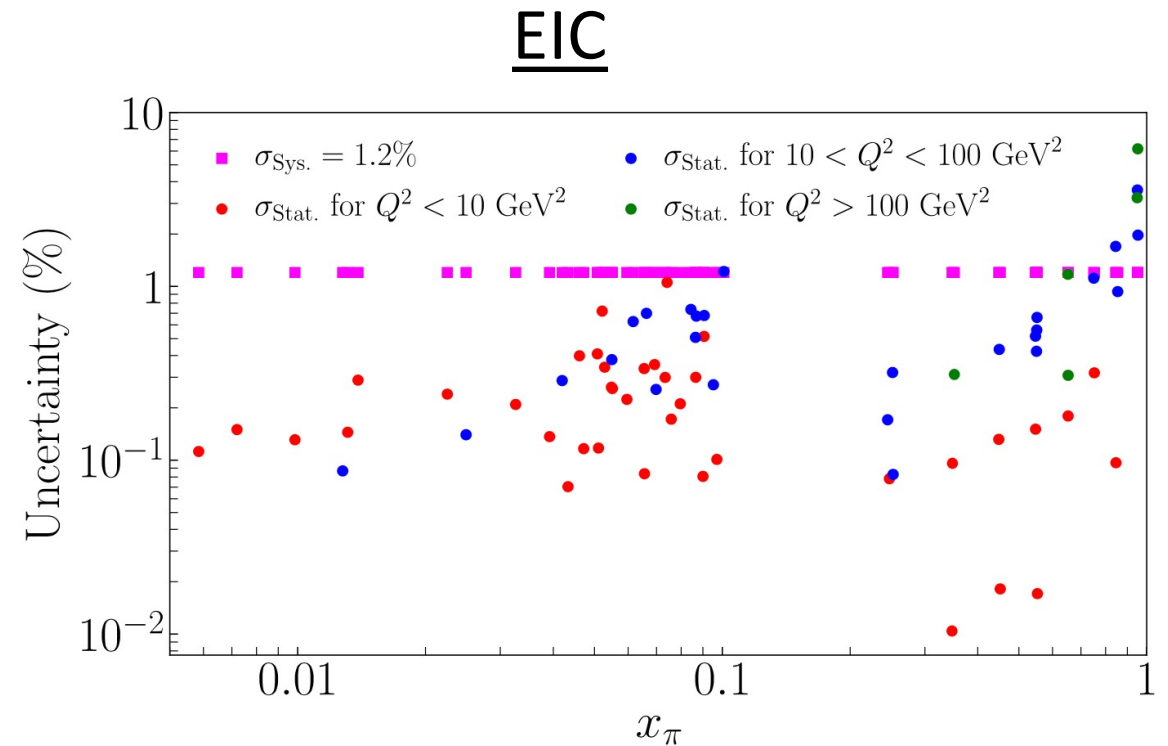
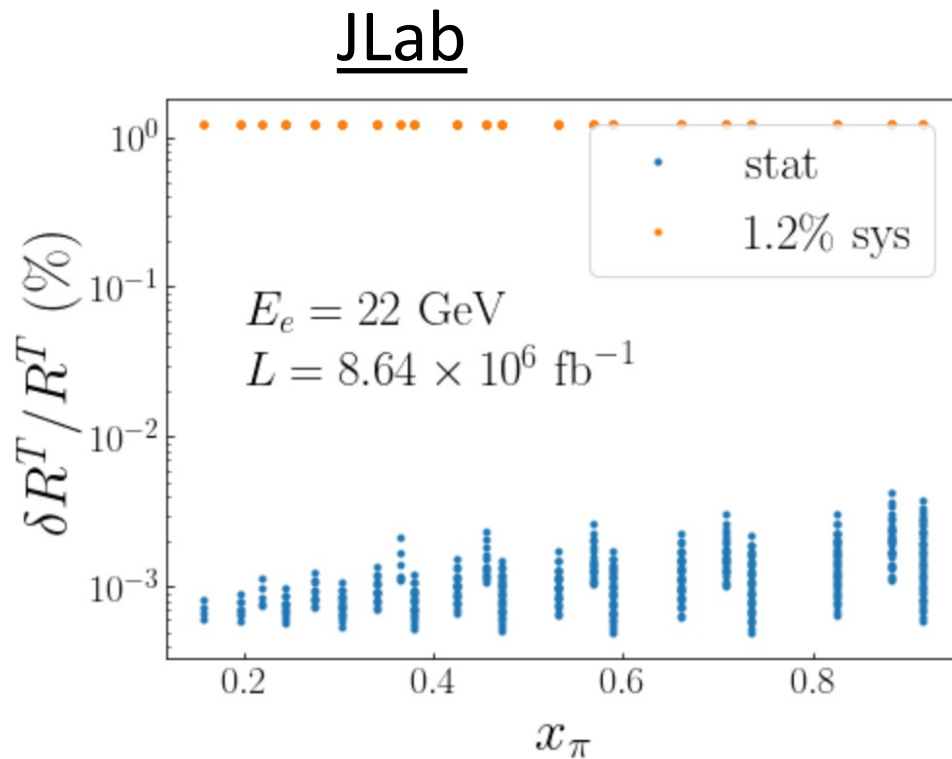
Resonance from K^*

- The K^* resonance is much more narrow than for ρ meson
- $W_{K,\max}^2 = 1 \text{ GeV}^2$



EIC vs JLab 22 GeV

- JLab measurements will be much more precise with a 200 day beam run – luminosity plays a big role



Use of W^2 for SIDIS

The unobserved invariant mass-squared in inclusive DIS is

$$W_{\text{tot}}^2 = M^2 + \frac{Q^2(1 - x_{\text{Bj}})}{x_{\text{Bj}}}. \quad (6.26)$$

In SIDIS it is

$$W_{\text{SIDIS}}^2 = M^2 + M_{\text{B}}^2 + \frac{Q^2(1 - x_{\text{Bj}} - z_{\text{h}})}{x_{\text{Bj}}} + \frac{Q^4 z_{\text{h}} \left(\sqrt{1 + \frac{4M^2 x_{\text{Bj}}^2}{Q^2}} \sqrt{1 - \frac{4M^2 x_{\text{Bj}}^2 M_{\text{B},\text{T}}^2}{z_{\text{h}}^2 Q^4}} - 1 \right)}{2M^2 x_{\text{Bj}}^2}$$
$$\stackrel{M, M_{\text{B}} \rightarrow 0}{\approx} \frac{Q^2(1 - x_{\text{Bj}})(1 - z_{\text{h}})}{x_{\text{Bj}}} - \frac{\mathbf{P}_{\text{B},\text{T}}^2}{z_{\text{h}}}. \quad (6.27)$$

- Replace M^2 with t