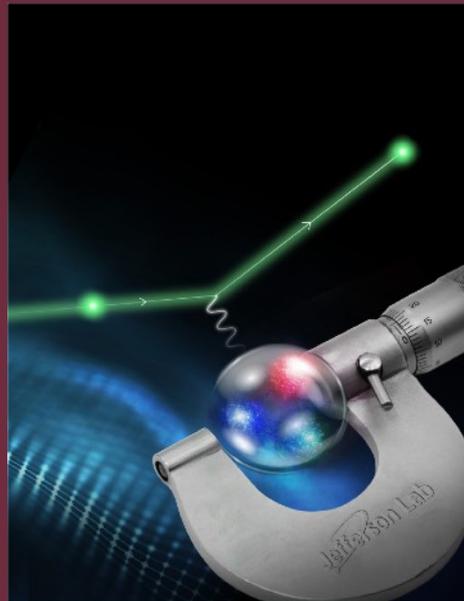


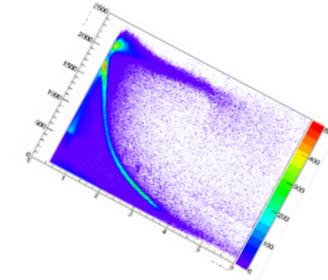
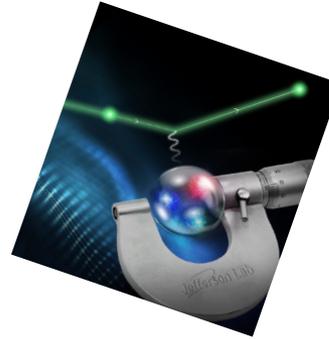
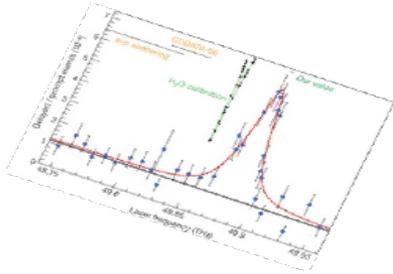
The Incredible Shrinking Proton and the PRad Experiment

Dipangkar Dutta



JLUO Meeting, June 22, 2020

Outline



- Introduction
- The Proton Charge Radius Puzzle
- A Novel Experiment (**PRad**) & Results
- Other Experiments & Future Prospects



The study of the proton has revolutionized physics

The proton is the primary, stable building block of all visible matter in the Universe.

The proton played a leading role in the development of Quantum Chromo Dynamics (QCD): theoretical framework for strong interaction between quarks mediated by gluons.

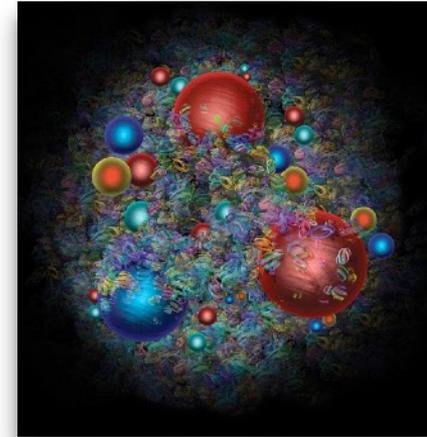
In the last 100 yrs. since its discovery, the proton has evolved from



to



**Positively charged
structure-less point particle**



Bag of quarks and gluons, with 99% of its mass due to the quark gluon interaction (and hence 99% of the visible mass in the Universe).

The story of the proton has been in lock-step with many of the key advances in physics over the last 100 years.

It continues to surprise us time and again.

Proton's basic properties such as its RMS charge radius is interesting on its own right, but also needed for determining fundamental constants such as the Rydberg constant.

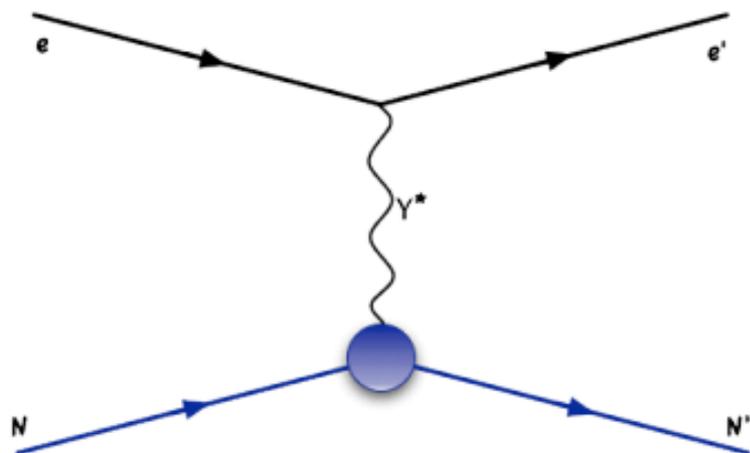
H - spectroscopy and elastic e-p scattering are the two traditional methods for determining proton charge radius

The forces defining the surface of a proton do not come to an abrupt end, its boundary is somewhat fuzzy.

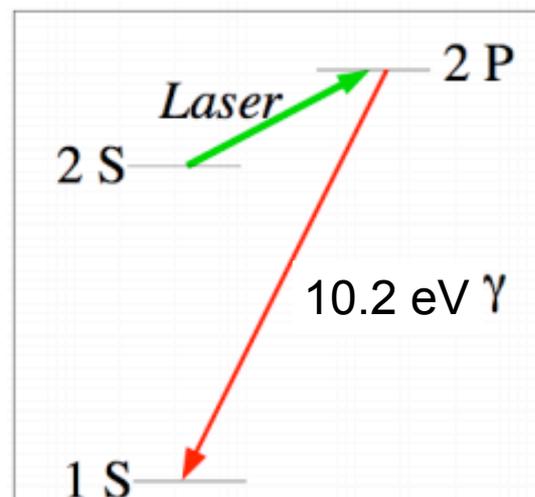
**If the proton has no definite boundaries
how do you define its radius?**

RMS charge radius (r_p) is obtained from a consistent interpretation of hydrogen spectroscopy and electron-proton scattering experiments

e-p Scattering



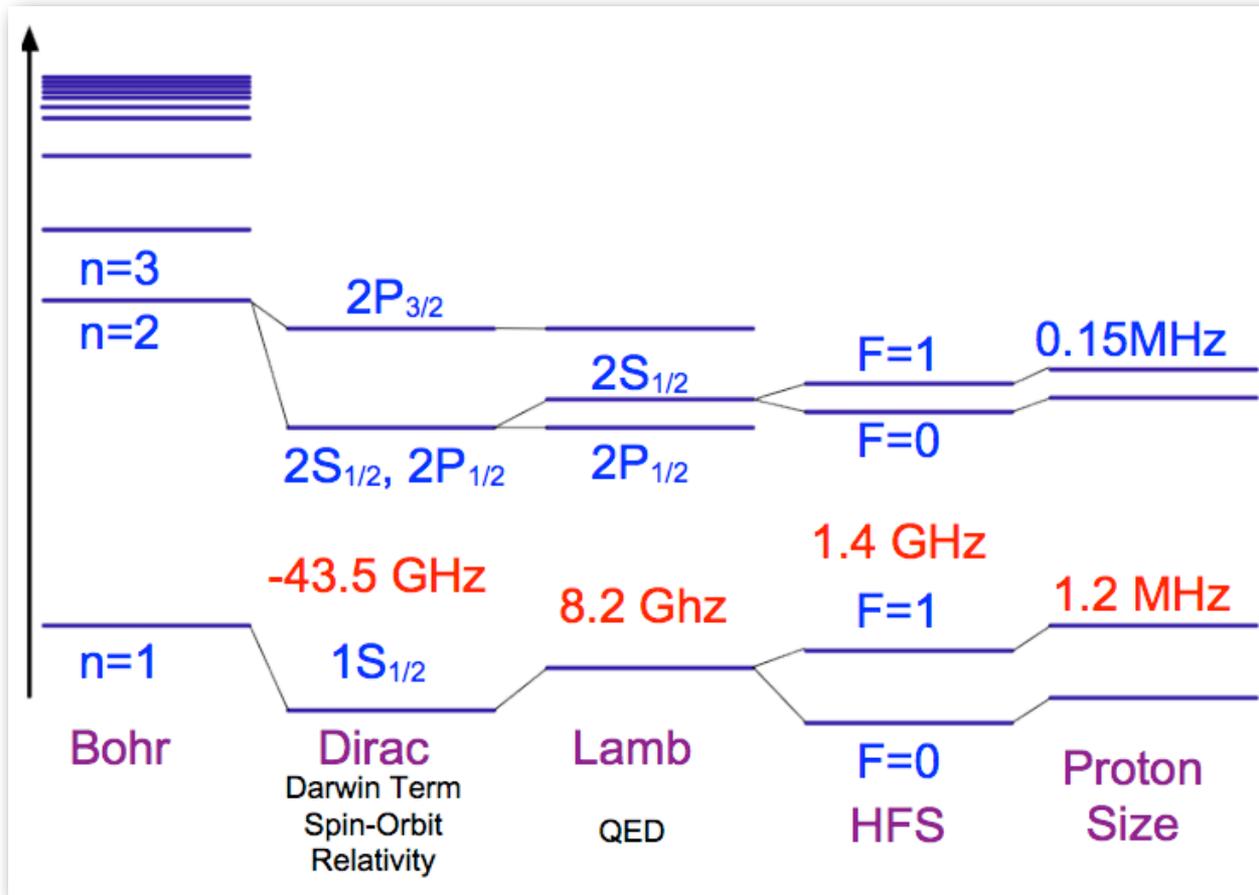
H-spectroscopy



This definition has been rigorously shown to be consistent for all types of experimental measurements.

G. Miller, Phys. Rev., C 99, 035202 (2019)

Corrections to H - spectroscopy due to the extended charge distribution of the proton used to extract r_p

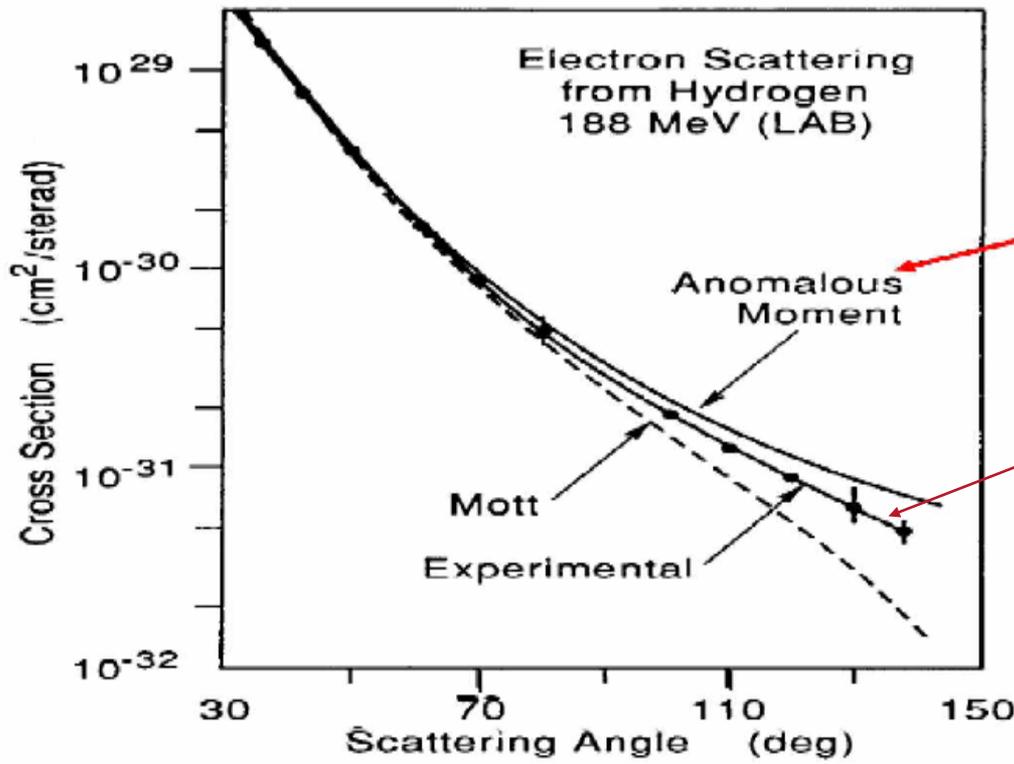


The absolute frequency of H energy levels has been measured with an accuracy of **1.4 part in 10^{14}** via comparison with an atomic Cs fountain clock as a primary frequency standard.

Comparing measurements to QED calculations that include corrections for the finite size of the proton provide a precise value of the **rms proton charge radius**.

Also, yields R_∞ (the most precisely known constant in Physics)

The slope of the electric form factor down to zero Q^2 used to extract r_p from elastic e-p scattering.



Point like proton with $G_E = 1$ and $G_M = \mu_p = 2.79$

Data show proton Has finite size

R. Hofstadter and R. W. McAllister, Phys. Rev., 98 (1955)

At very low Q^2 , cross section dominated by G_E :

Charge radius given by the slope at $Q^2 = 0$:

$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{\text{Mott}} \left(\frac{E'}{E}\right) \frac{1}{1+\tau} G_E^2(Q^2)$$

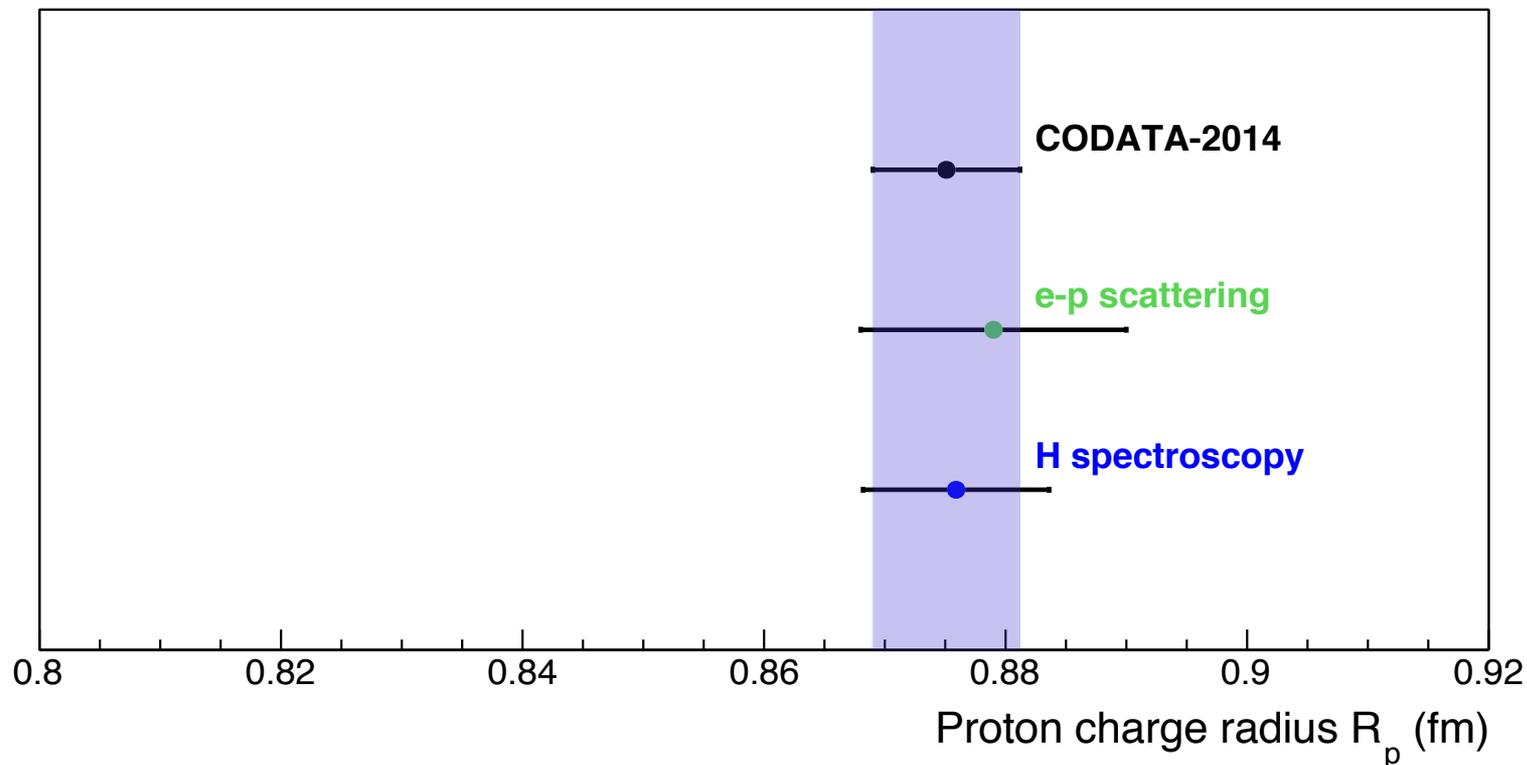
$$G_E(Q^2) = 1 - \frac{Q^2}{6} \langle r^2 \rangle + \frac{Q^4}{120} \langle r^4 \rangle + \dots$$

$$\langle r^2 \rangle = -6 \left. \frac{dG_E^2}{dQ^2} \right|_{Q^2=0}$$

This definition has been rigorously shown to be consistent with all experimental measurements.

G. Miller, Phys. Rev., C 99, 035202 (2019)

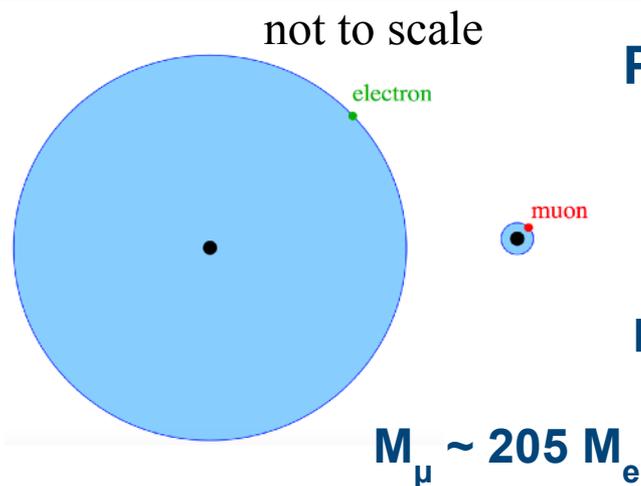
Prior to 2010 the r_p extracted from H - spectroscopy and elastic e-p scattering were consistent with each other.



CODATA average: 0.8751 ± 0.0061 fm
ep-scattering average (CODATA): 0.879 ± 0.011 fm
Regular H-spectroscopy average (CODATA): 0.859 ± 0.0077 fm

The charge radius of the proton was considered a settled question.

A new method based on muonic hydrogen spectroscopy was used to extract r_p for the first time in 2010.



Probability of lepton to be inside proton

$$\sim \left(\frac{r_p}{a_B} \right)^3 = (r_p \alpha)^3 m^3$$

m = reduced mass
 $\sim 186 M_e$

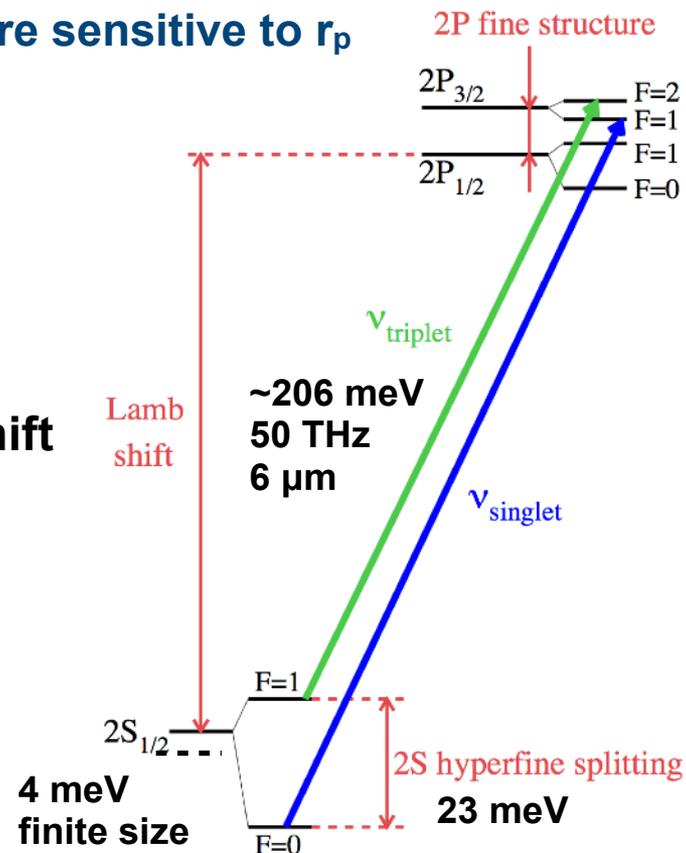
μH is $\sim 6 \times 10^6$ times more sensitive to r_p

Lamb shift in μH :

$$\Delta E = 206.0668(25) - 5.2275(10) r_p^2 \text{ [meV]}$$

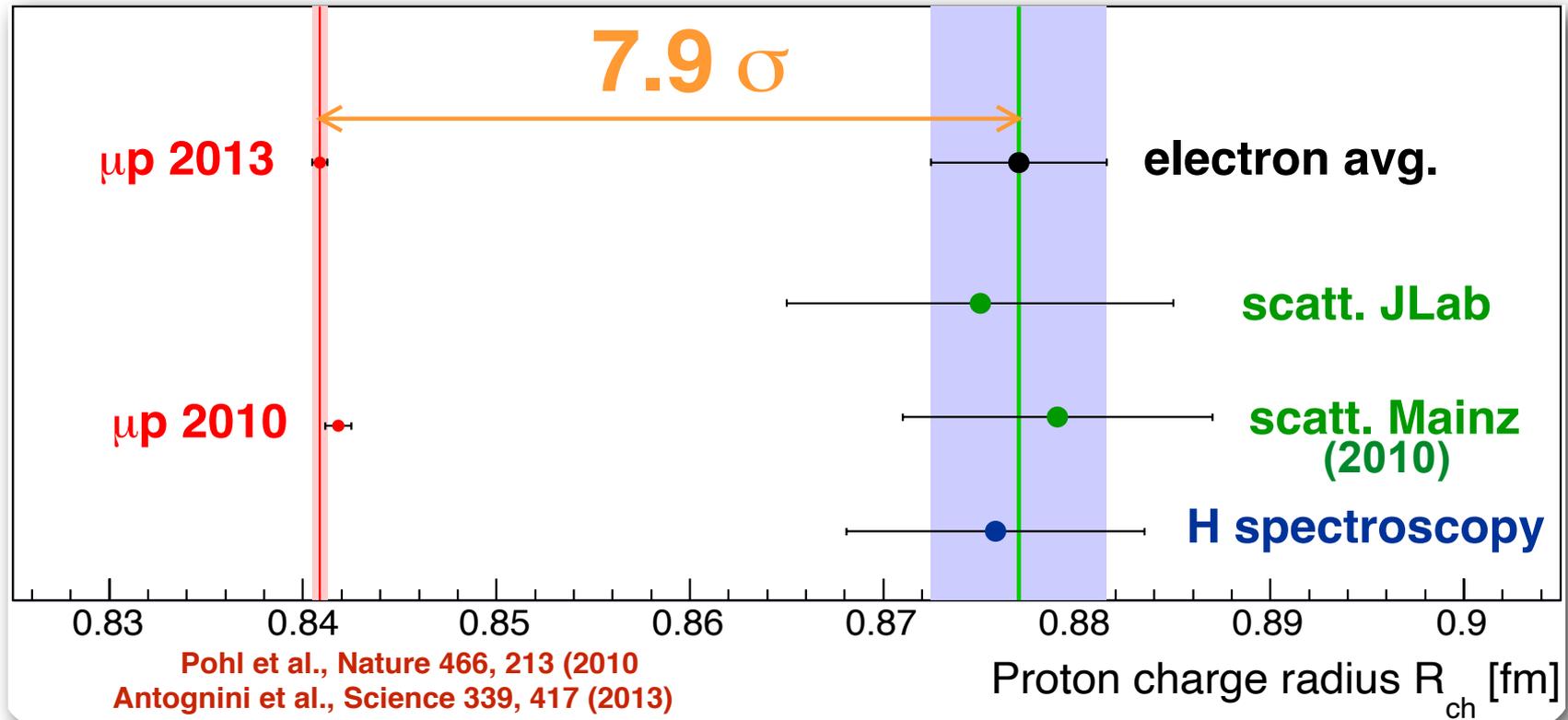
finite proton size is $\sim 2\%$ correction to μH Lamb shift

r_p was extracted with
 10 times higher precision ($\sim 0.1\%$)
 compared to all previous measurements



The results from the muonic hydrogen spectroscopy led to the so called “proton radius puzzle.”

~8 σ discrepancy between muon and electron based measurements



Proton rms charge radius measured using

- **unprecedented precision ~0.08%**
- **$Q^2 \sim 10^{-6} \text{ GeV}^2$**

electrons: **0.8770 ± 0.0045** (CODATA2010 + Zhan et al.)

muons: **0.8409 ± 0.0004**

There was a world wide effort to explore numerous possible resolutions to the “proton radius puzzle.”

★ Are the state of the art QED calculations incomplete?

- E. Borie, Phys. Rev. A 71, 032508 (2005)
- U. D. Jentschura, Ann. of Phys. 326, 500 (2011)
- F. Hagelstein, V. Pascalutsa, Phys. Rev. A 91, 040502 (2015)

★ Are there additional corrections to the muonic Lamb shift due to proton structure (such as proton polarizability of $\mathcal{O}(\alpha^5)$)?

- C. E. Carlson, V. Nazaryan and K. Griffioen, Phys. Rev. A 83, 042509 (2011)
-  R. J. Hill and G. Paz, Phys. Rev. Lett. 107, 160402 (2011)

★ Are higher moments of the charge distribution accounted for in the extraction of rms charge radius?

- M. O. Distler, J. C. Bernauer and T. Walcher, Phys. Lett. B 696, 343 (2011)
- A. de Rujula, Phys. Lett. B 693, 555 (2010), and 697, 264 (2011)
- I. Cloet, and G. A. Miller, Phys. Rev. C. 83, 012201(R) (2011)

★ Is there an extrapolation problem in electron scattering data?

- D. W. Higinbotham et al., Phys. Rev. C 93, 055207 (2016)
- K. Griffioen, C. Carlson, S. Maddox, Phys. Rev. C 93, 065207 (2016)

★ Has new physics been discovered (violation of Lepton Universality)?

- V. Barger, et al., Phys. Rev. Lett. 106, 153001 (2011)
- B. Batell, D. McKeen, M. Pospelov, Phys. Rev. Lett. 107, 011803 (2011)
- D. Tucker-Smith, I. Yavin, Phys. Rev. D 83, 101702 (2011).

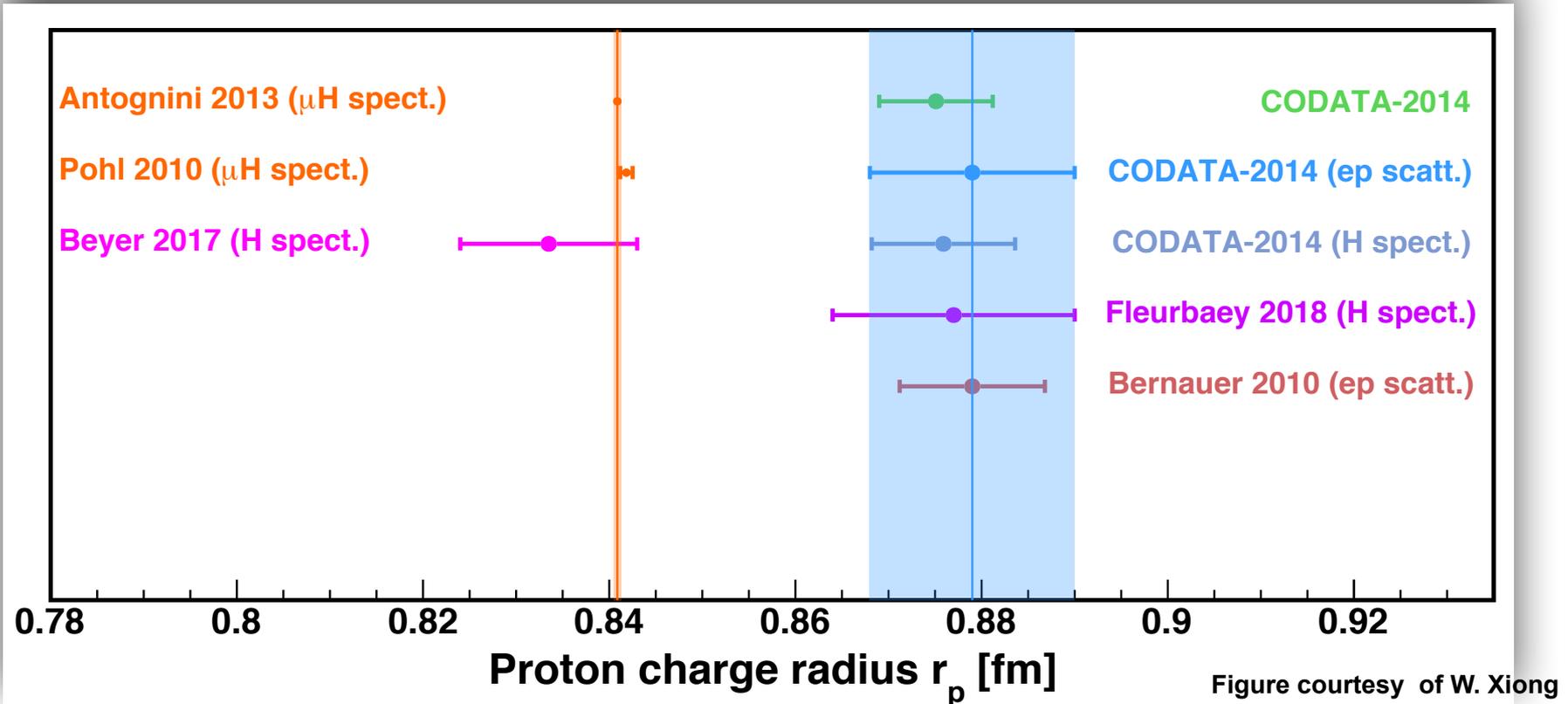
★ New force carriers?

- C. E. Carlson, Prog. Part. Nucl. Phys. 82, 59–77 (2015).
- Y. S. Liu and G. A. Miller, Phys. Rev. D 96, 016004 (2017).

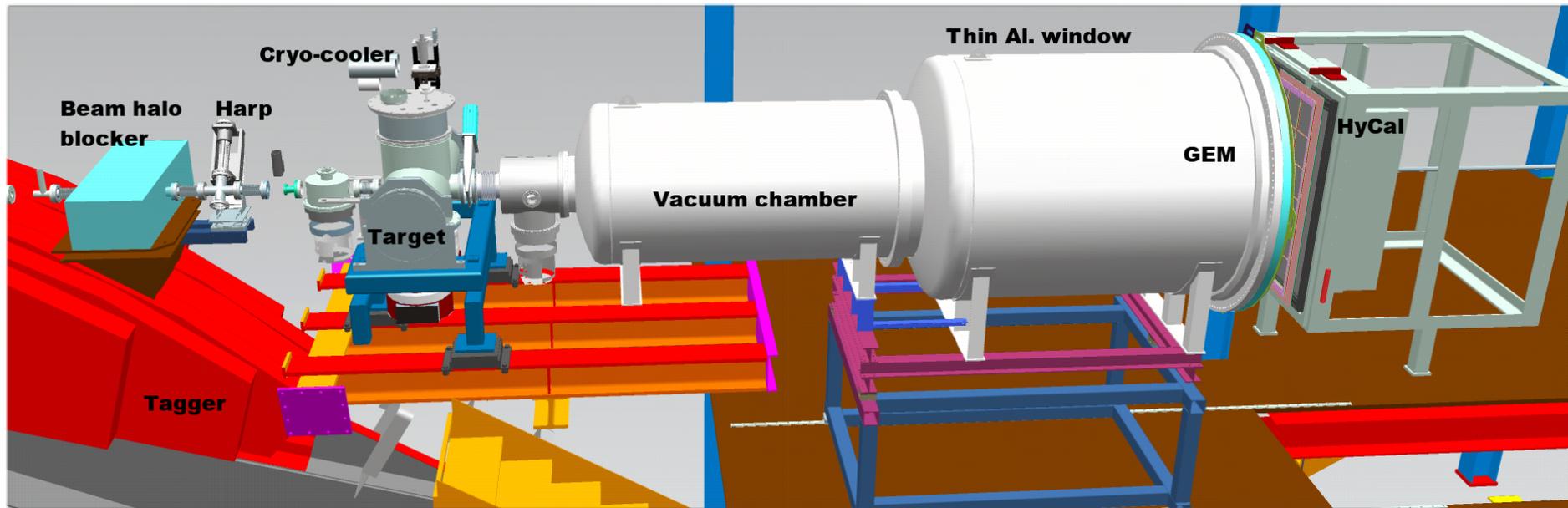
Clearly more experiments were needed !

- ◆ Redo atomic hydrogen spectroscopy (3 different groups)
- ◆ Muon-proton scattering (MUSE experiment-2020)
- ◆ **Electron scattering experiments (PRad-2016, ISR, ProRad, ULQ²...)**

The status of “proton radius puzzle” in 2018



PRad: a novel electron scattering experiment



*Spokesperson: A. Gasparian,
Co-spokespersons: D. Dutta, H. Gao, M. Khandaker*

- High resolution, Hybrid calorimeter (magnetic spectrometer free)
- Windowless, high density H₂ gas flow target (reduced backgrounds)
- Simultaneous detection of elastic and Møller electrons (control of systematics)
- Vacuum chamber, one thin window, large area GEM chambers (better resolution)
- Q² range of 10⁻⁴ – 6x10⁻² GeV² (lower than all previous electron scattering expts.)

Ran in Hall-B at JLab in 2016, using 1.1 GeV and 2.2 GeV electron beam

The first experiment to use a magnetic spectrometer free method to measure r_p

Reused PrimEx Hybrid Calorimeter

- PbWO_4 and Pb-glass calorimeter (118x118 cm²)
- 34x34 matrix of 2.05 x 2.05 cm² x 18 cm PbWO_4
- 576 Pb-glass detectors (3.82x3.82 cm² x 45 cm)
- 5.5 m from the target,
- 0.5 sr acceptance

Allows coverage of extreme forward angle (0.7° - 7.5°) in a **single setting** and complete azimuthal angle coverage

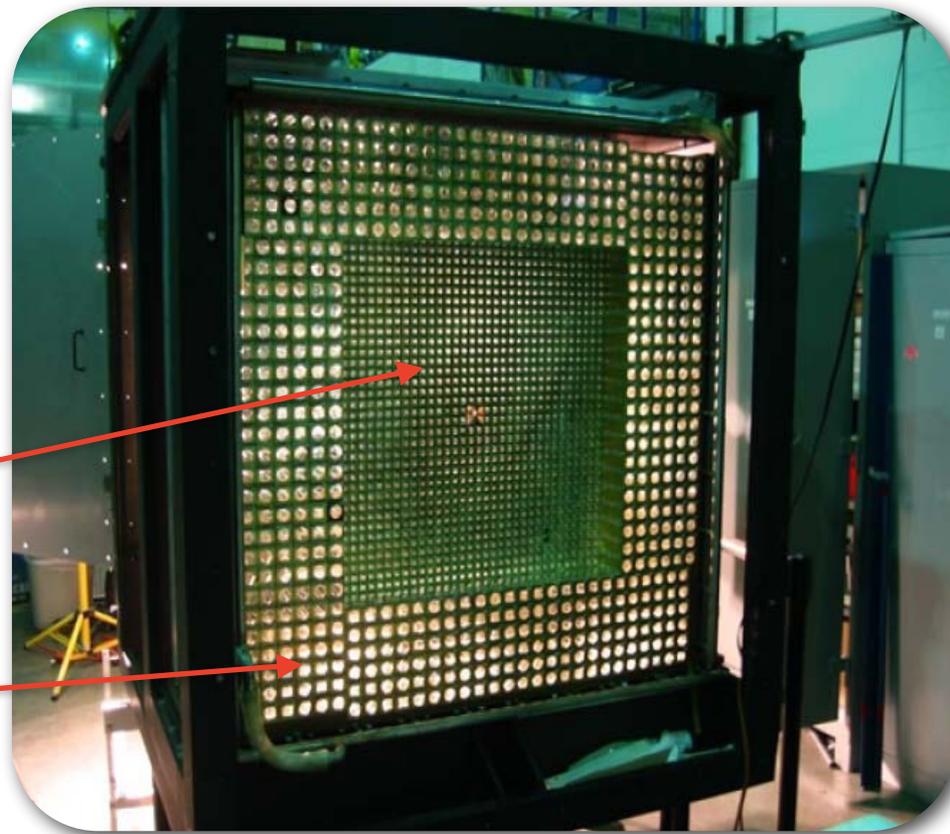
PbWO_4 resolution:

$$\sigma_E/E = 2.6\%/\sqrt{E}$$

$$\sigma_{xy} = 2.5 \text{ mm}/\sqrt{E}$$

Pb-glass:

2.5 times worse



The first experiment to use a windowless target to measure r_p

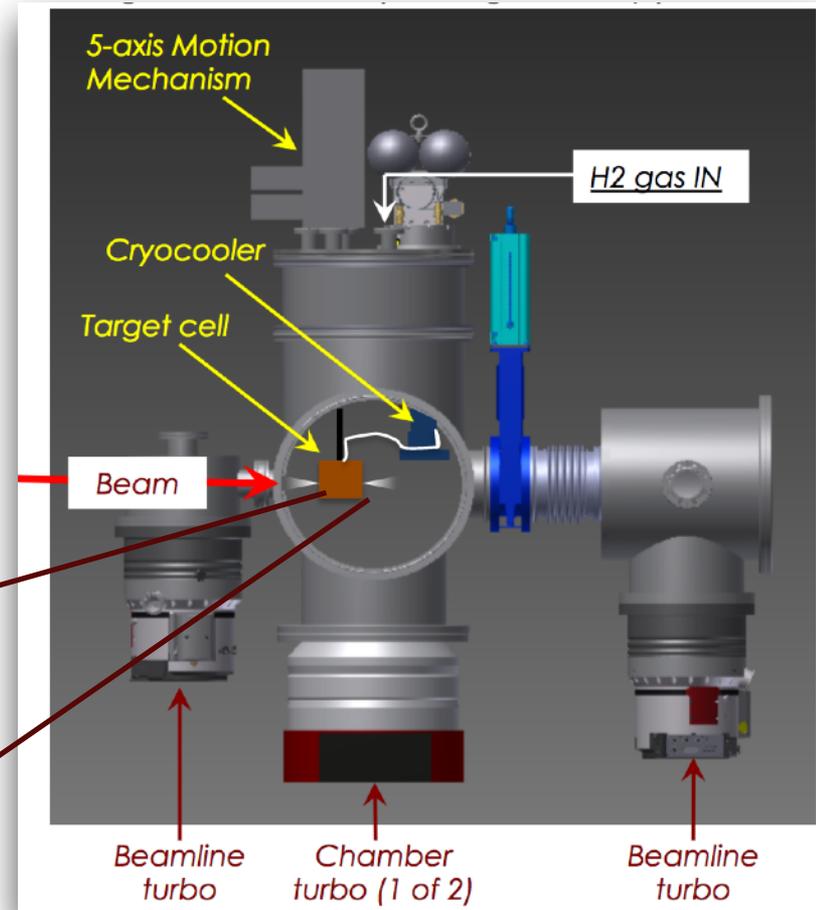
Used a cryo-cooled windowless gas flow hydrogen target.

density:

$\sim 2 \times 10^{18}$ atoms/cm²

cell / chamber/ tank pressure:

470 / 2.3 / 0.3 mtorr



Target cell
(8 cm dia x 4 cm long
copper)

Gas IN, 25 K

Gas OUT

Gas OUT

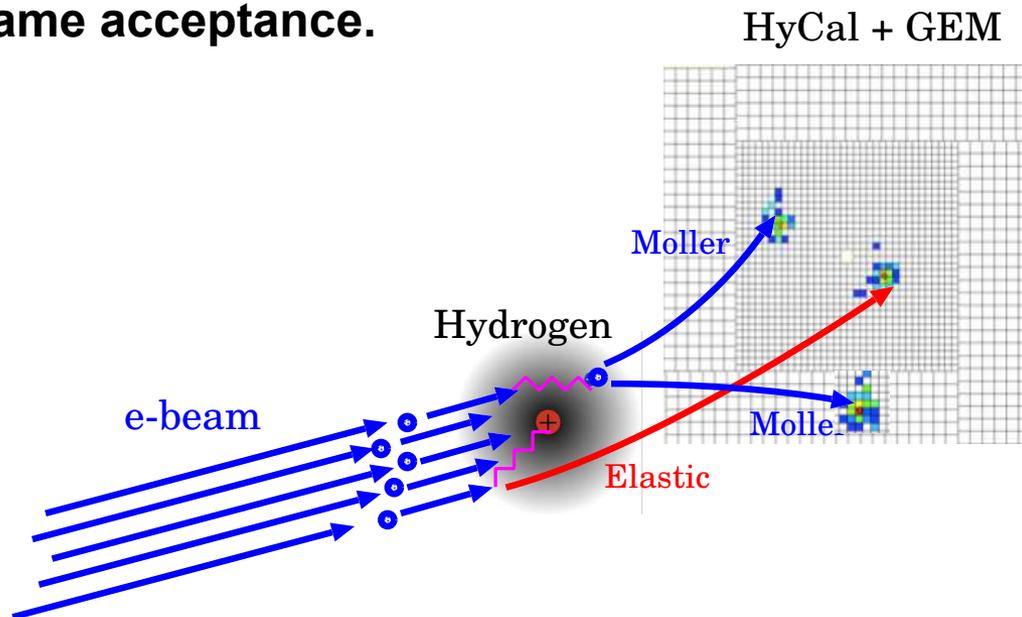
7.5 μ m kapton foil
with 2mm hole

40 mm

Empty target runs used to subtract background

Key innovations in the design allowed a unique high precision measurement.

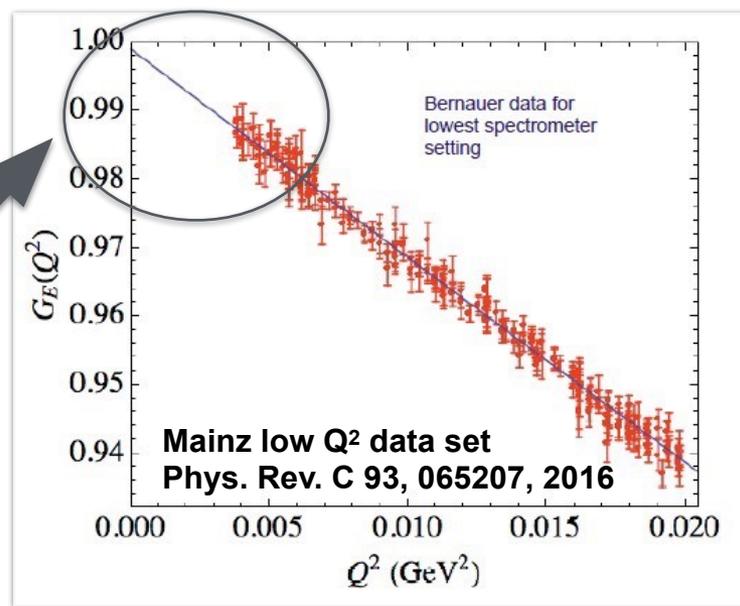
Simultaneous detection of the Møller ($e-e$) and $e-p$ elastic events within the same acceptance.



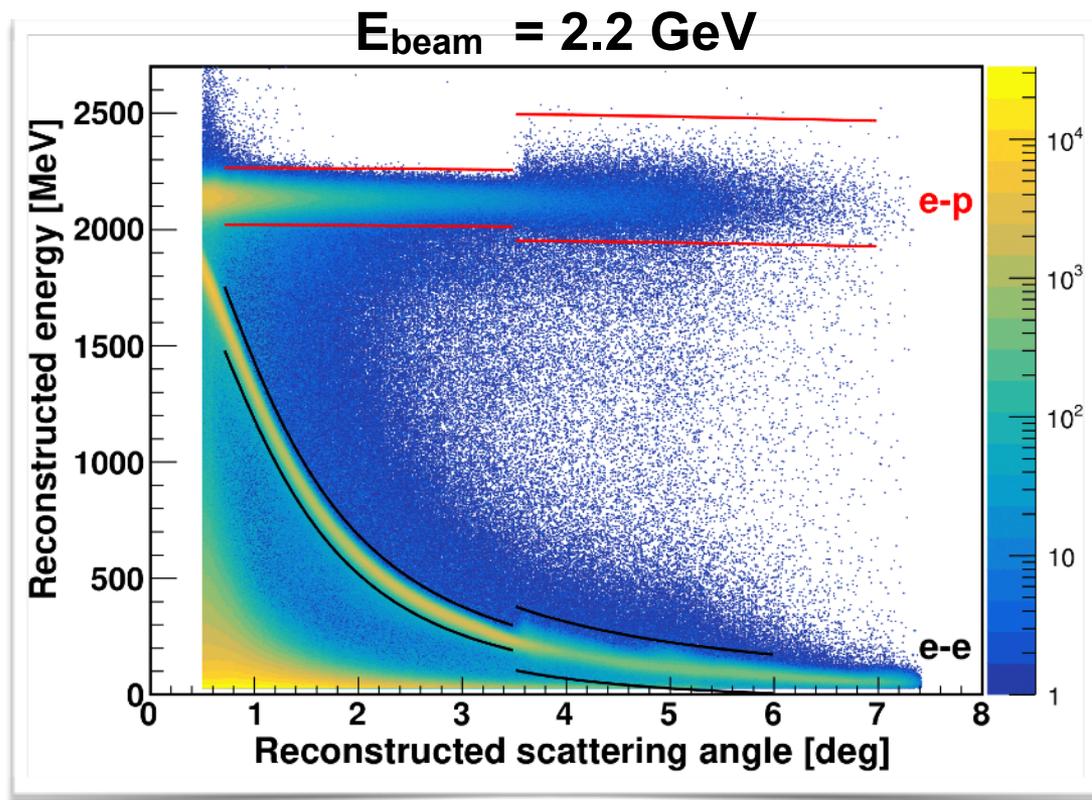
Large forward angle acceptance with high energy resolution (HyCal) and $72 \mu\text{m}$ position resolution (GEM).

- Experimental design allows:
 - fill in the very low Q^2 range
 - large Q^2 range in a single setting ($\sim 2 \times 10^{-4} - 6 \times 10^{-2} \text{ GeV}^2$)

- Experimental design allows:
 - control of systematics
 - eliminates need to monitor luminosity



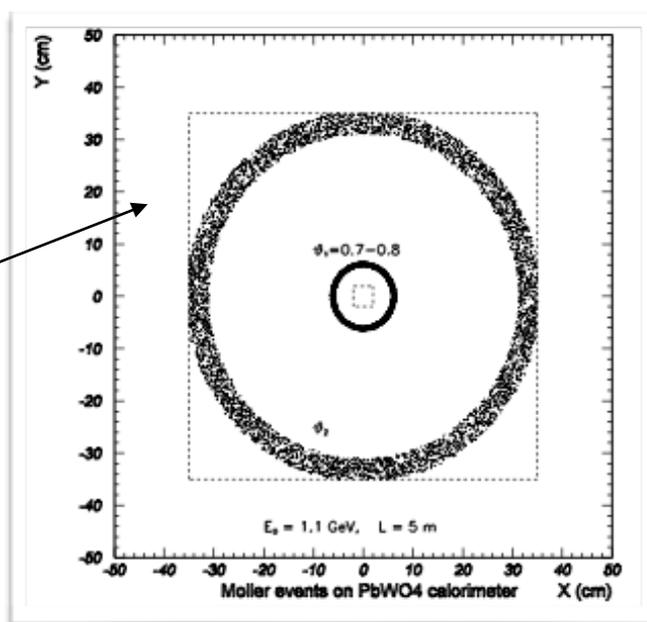
Angle dependent energy cuts are used to select the Møller (e-e) and e-p elastic events.



GEM and HyCal detector hits must match for all (e-p) and (e-e) events

Angle dependent energy cuts for (e-p) and (e-e) events based on kinematics with the cut size based on local resolution.

Additional constraints for double arm Møller events on: **co-planarity, elasticity, z-vertex**



e - p elastic cross section extracted by normalizing to Møller cross section.

bin-by-bin normalization (double arm Møller)

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^- \rightarrow e^-e^-)} \cdot \frac{\varepsilon_{\text{geom}}^{e^-e^-}}{\varepsilon_{\text{geom}}^{ep}} \cdot \frac{\varepsilon_{\text{det}}^{e^-e^-}}{\varepsilon_{\text{det}}^{ep}} \right] \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$

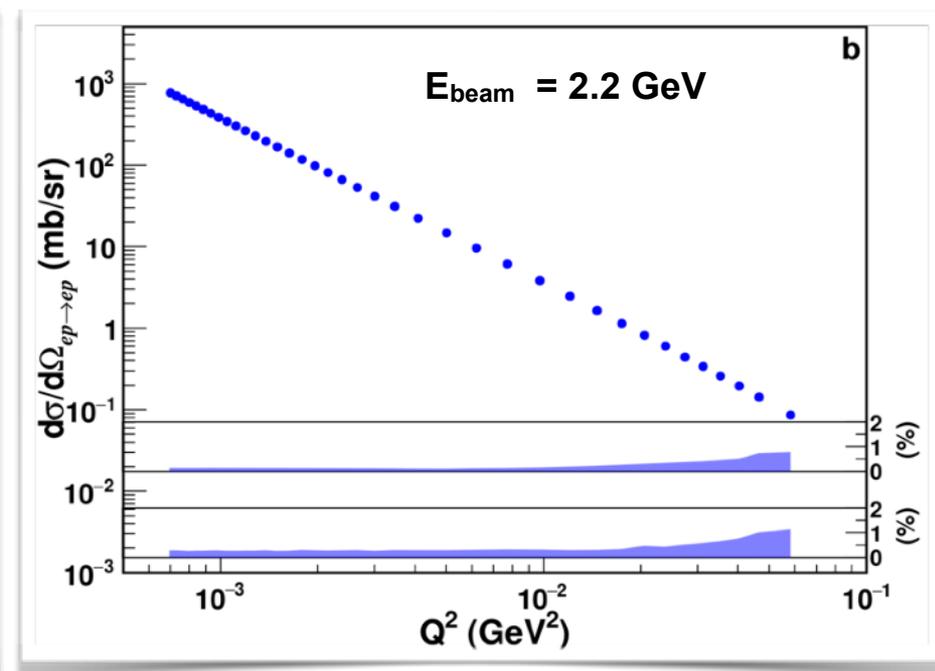
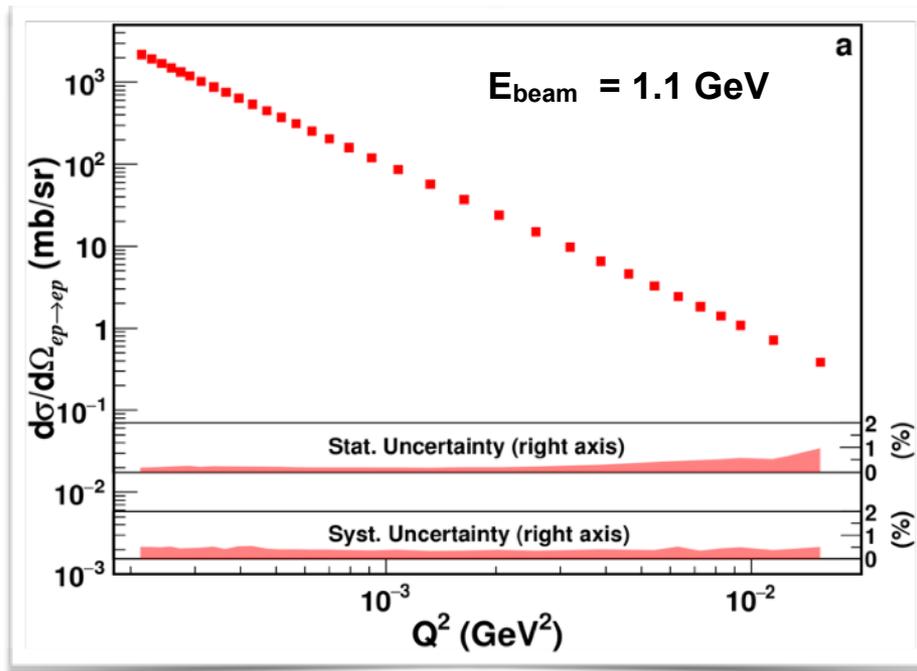
or

integrated over HyCal acceptance

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep, \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^-, \text{on PWO})} \cdot \frac{\varepsilon_{\text{geom}}^{e^-e^-}(\text{all PWO})}{\varepsilon_{\text{geom}}^{ep}(\theta_i \pm \Delta\theta)} \cdot \frac{\varepsilon_{\text{det}}^{e^-e^-}(\text{all PWO})}{\varepsilon_{\text{det}}^{ep}(\theta_i \pm \Delta\theta)} \right] \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$

Event generator for e - p elastic and Møller include radiative corrections beyond the ultra-relativistic approximation & two photon exchange (used iteratively within a Geant4 simulation)

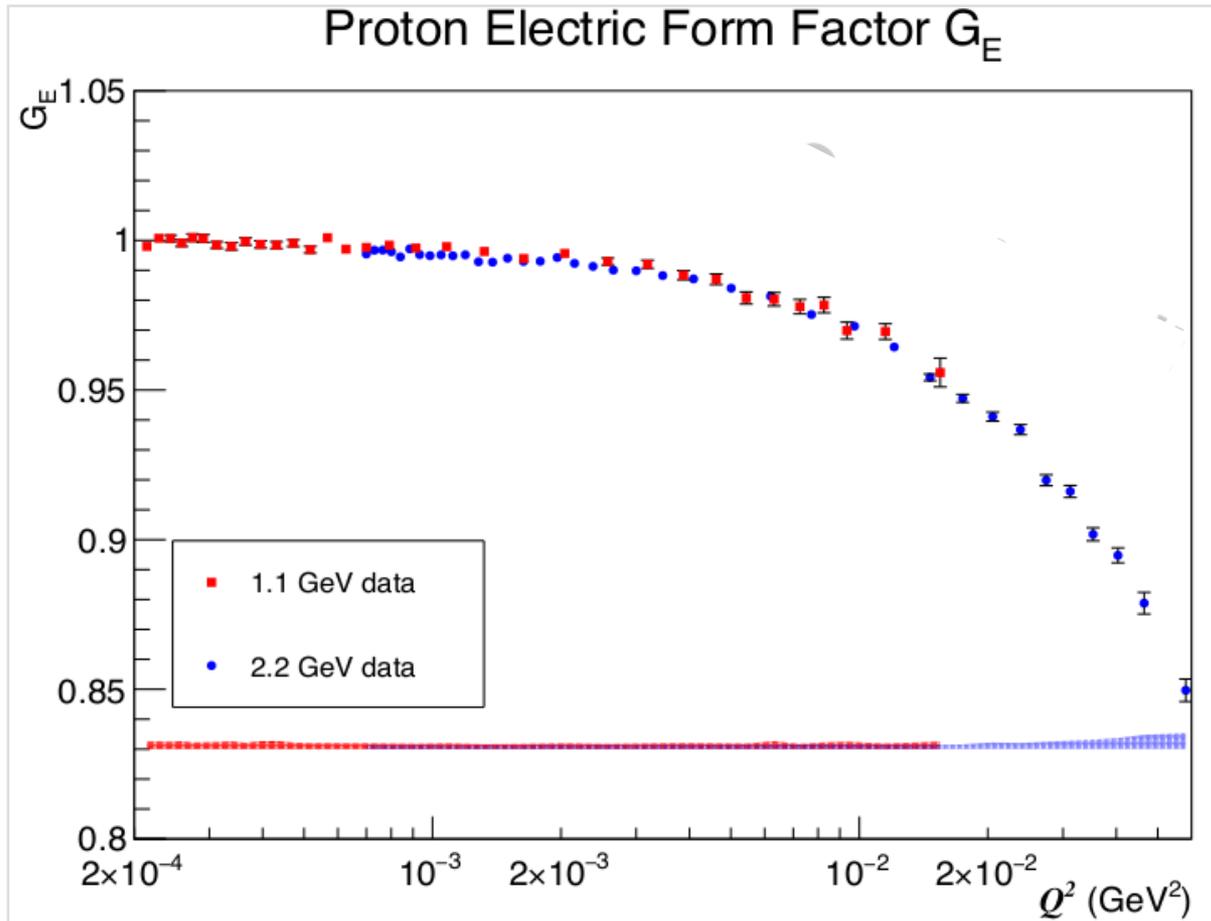
1. A. V. Gramolin et al., J. Phys. G Nucl. Part. Phys. 41, 115001 (2014).
2. I. Akushevich et al., Eur. Phys. J. A 51, 1 (2015).
3. O. Tomalak, Few Body Syst. 59, 87 (2018). (two photon exchange formalism)



Systematic uncertainties: 0.3% - 0.5% at 1.1 GeV and 0.3% - 1.1% at 2.2 GeV

Figures courtesy of W. Xiong

The proton electric form factor was extracted at the lowest Q^2 ever achieved in electron scattering.



The slope of $G_E(Q^2)$ as $Q^2 \rightarrow 0$ is proportional to r_p^2 .

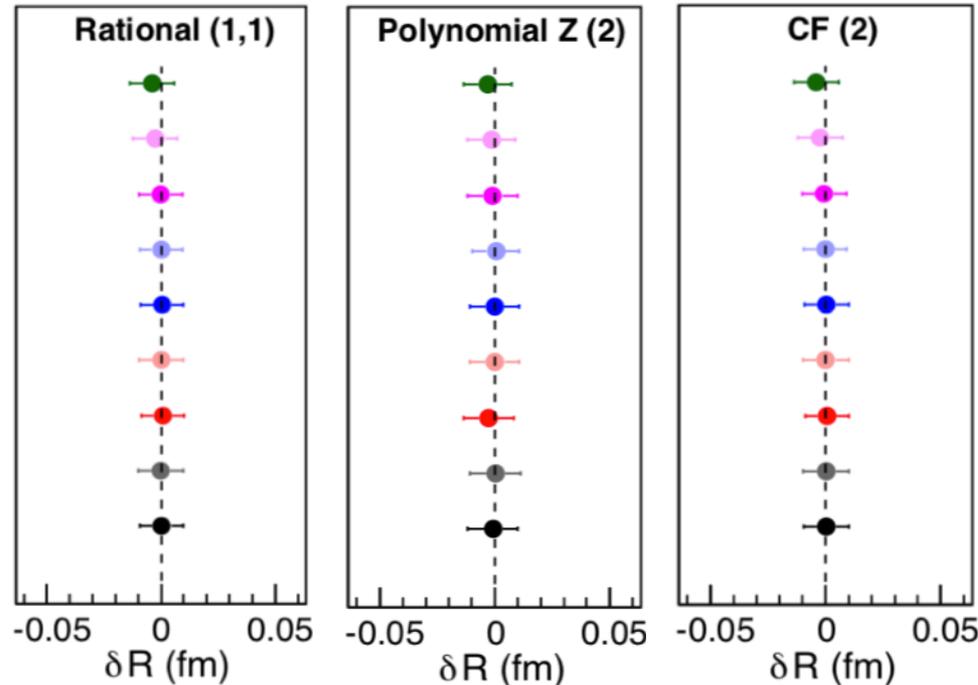
Typically r_p is obtained by fitting $G_E(Q^2)$ to a functional form and extrapolating to $Q^2 = 0$.

The truncation of the higher-order moments of $G_E(Q^2)$ introduces a model dependence which can bias the determination of r_p .

Figure courtesy of W. Xiong

A wide range of functional forms were systematically tested for their robustness in extracting r_p .

- Numerous functional forms were tested with a wide range of G_E parameterizations, using PRad kinematic range and uncertainties: X. Yan *et al.* Phys. Rev. C98, 025204 (2018)
- Rational (1,1), 2nd order z transformation and 2nd order continuous fraction are identified as robust fitters with also reasonable uncertainties



- Ye-2018
- Bernauer-2014
- Alarcón-2017
- Arrington-2007
- Arrington-2004
- Kelly-2004
- Gaussian
- Monopole
- Dipole

$$\begin{aligned}
 &\text{Rational (1,1)} \\
 & p_0 \frac{1 + p_1 Q^2}{1 + p_2 Q^2} \\
 \hline
 &\text{2nd order z transformation} \\
 & p_0(1 + p_1 z + p_2 z^2) \\
 & z = \frac{\sqrt{T_c + Q^2} - \sqrt{T_c - T_0}}{\sqrt{T_c + Q^2} + \sqrt{T_c - T_0}} \\
 \hline
 &\text{2nd order continuous fraction} \\
 & p_0 \frac{1}{1 + \frac{p_1 Q^2}{1 + p_2 Q^2}}
 \end{aligned}$$

The robustness = root mean square error (RMSE)

$$\text{RMSE} = \sqrt{(\delta R)^2 + \sigma^2},$$

δR = difference between the input and extracted radius
 σ = statistical variation of the fit to the mock data

Figure courtesy of W. Xiong

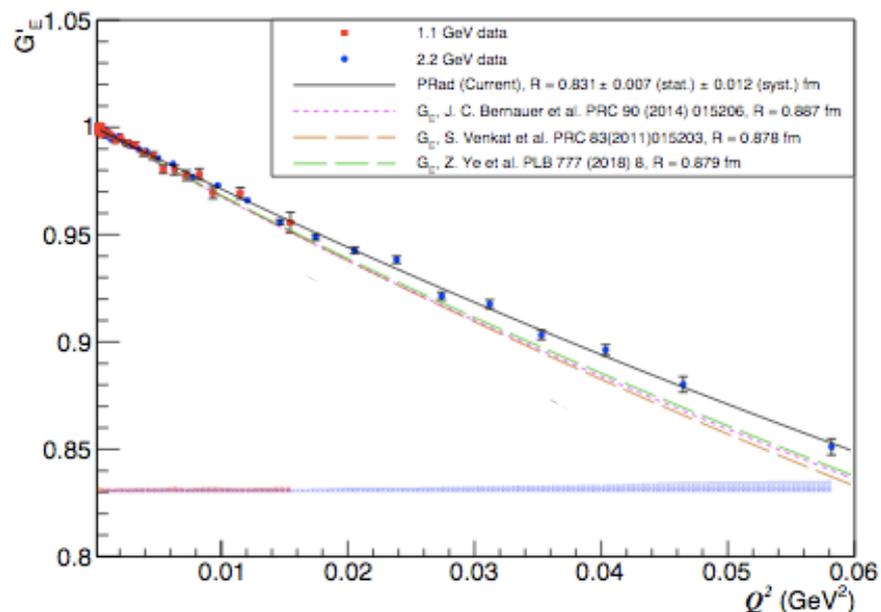
The rational (1,1) functional forms provides the most robust extraction of r_p from the PRad data.

- n_1 and n_2 obtained by fitting PRad G_E to $\begin{cases} n_1 f(Q^2), & \text{for 1GeV data} \\ n_2 f(Q^2), & \text{for 2GeV data} \end{cases}$
- G'_E as normalized electric Form factor: $\begin{cases} G_E/n_1, & \text{for 1GeV data} \\ G_E/n_2, & \text{for 2GeV data} \end{cases}$
- PRad fit shown as $f(Q^2)$ $r_p = 0.831 \pm 0.007$ (stat.) ± 0.012 (syst.) fm

Using rational (1,1)

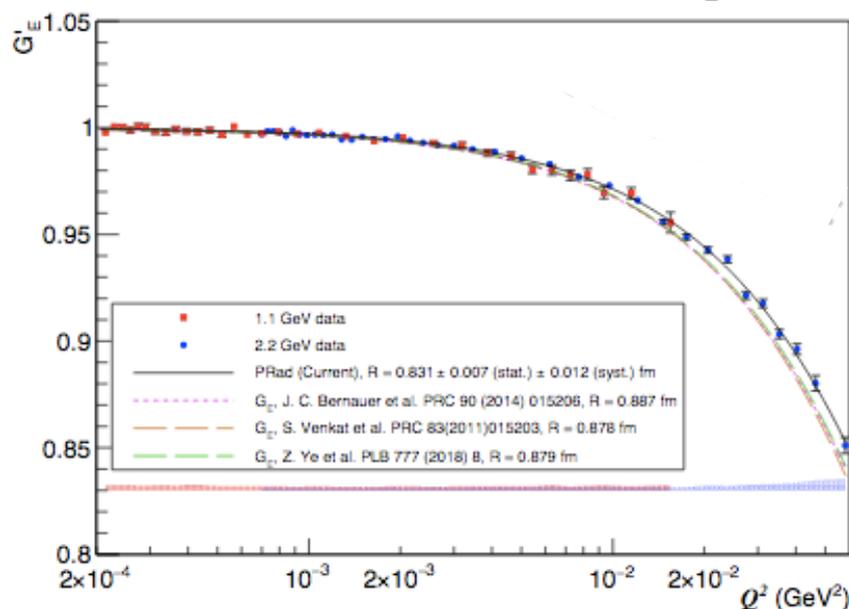
$$f(Q^2) = \frac{1 + p_1 Q^2}{1 + p_2 Q^2}$$

Proton Electric Form Factor G'_E



$$n_1 = 1.0002 \pm 0.0002(\text{stat.}) \pm 0.0020(\text{syst.}),$$

Proton Electric Form Factor G'_E

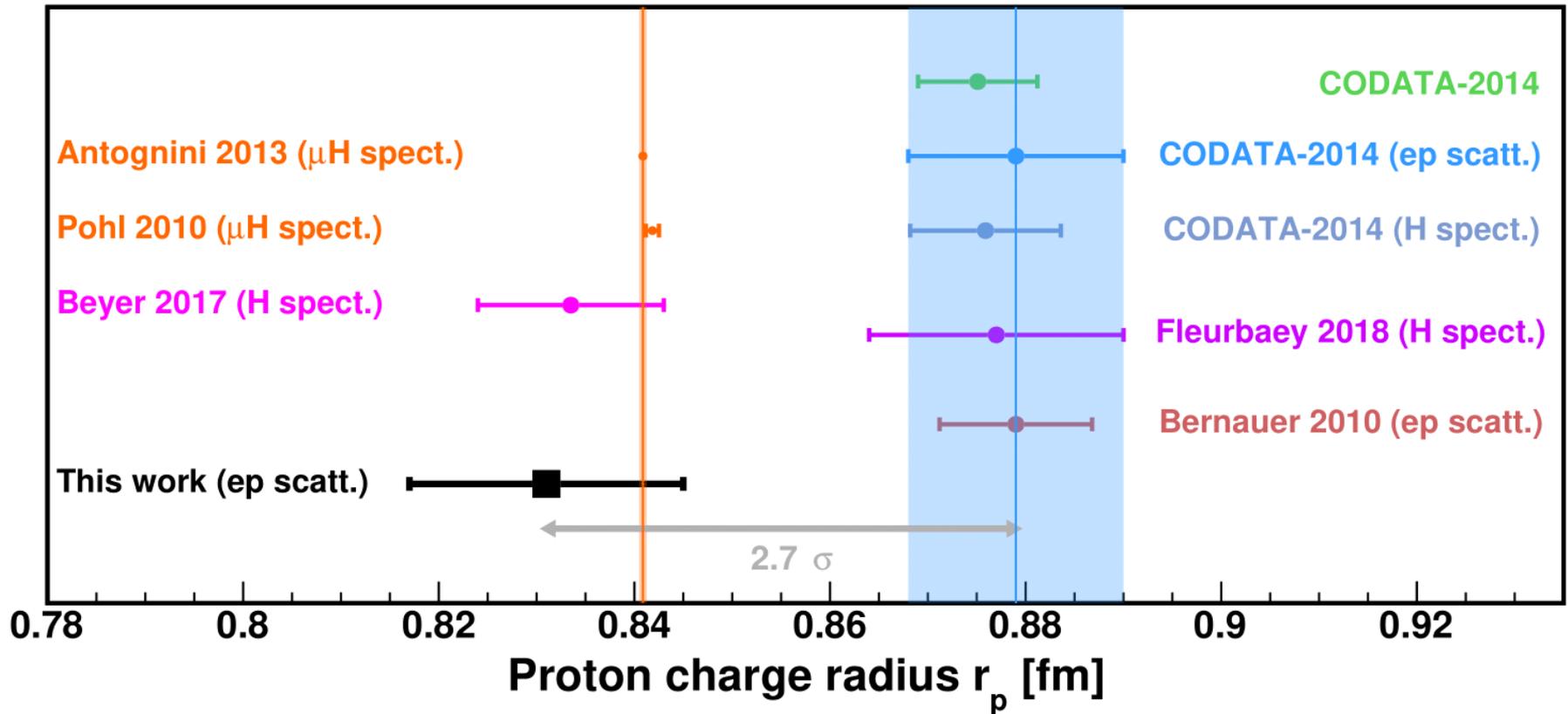


$$n_2 = 0.9983 \pm 0.0002(\text{stat.}) \pm 0.0013(\text{syst.})$$

Figures courtesy of W. Xiong

The PRad result for the proton charge radius.

PRad result: 0.831 ± 0.007 (stat.) ± 0.012 (syst.) fm



W. Xiong et al., Nature, 575, 147 (2019)

There has been some rapid and dramatic development over the last few months.

A new H-spectroscopy results was reported in Science Magazine in November.

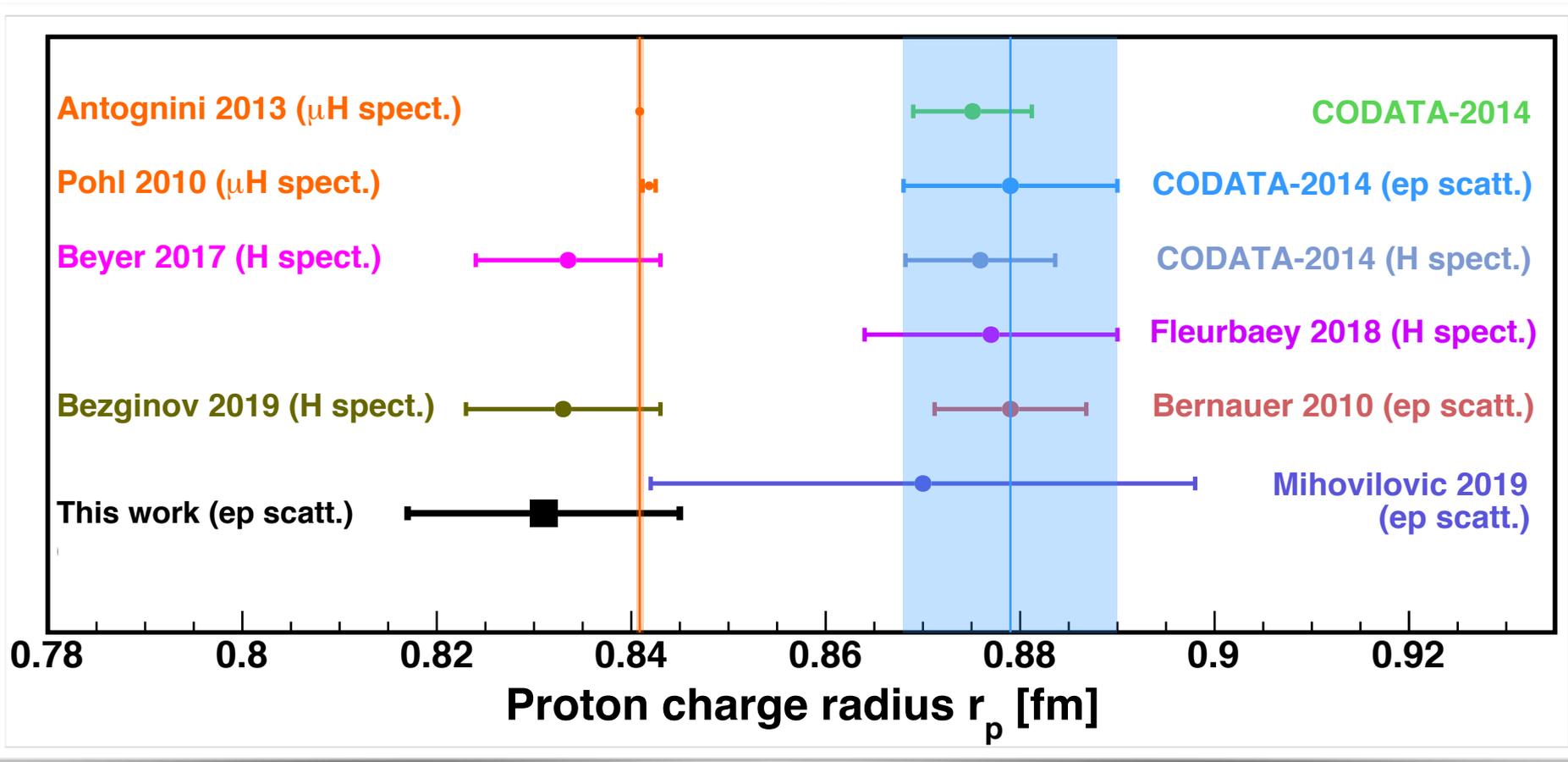
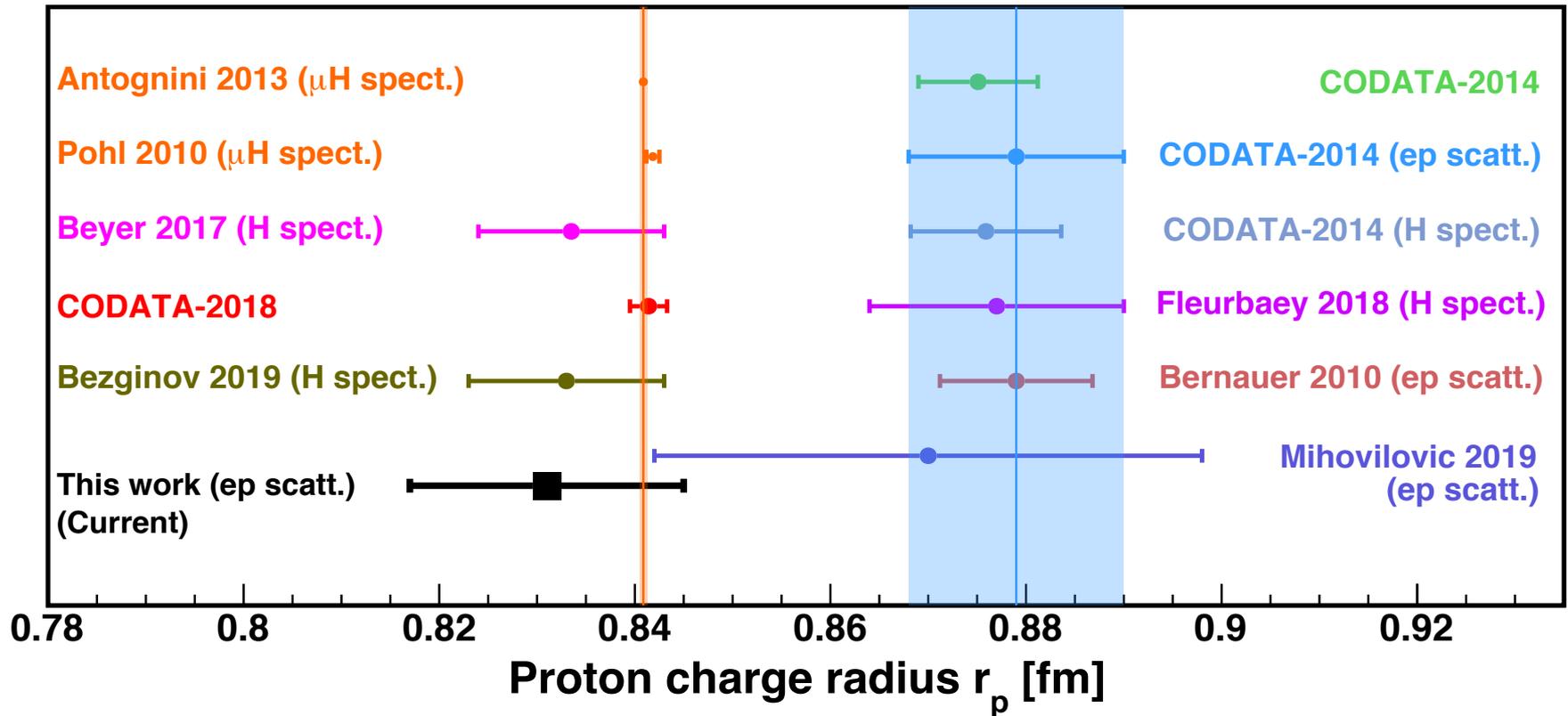


Figure courtesy of W. Xiong

There has been some rapid and dramatic development over the last few months.

Recently, CODATA released, online, their revised value of r_p



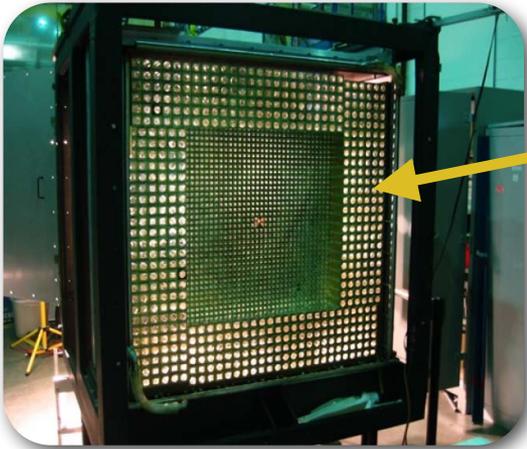
CODATA has also revised the value of the Rydberg constant.

2020 Review of Particle Physics claims - "...the puzzle appears to be resolved"

[P.A. Zyla et al.](#) (Particle Data Group), to be published in Prog. Theor. Exp. Phys. **2020**, 083C01 (2020)

Figure courtesy of W. Xiong

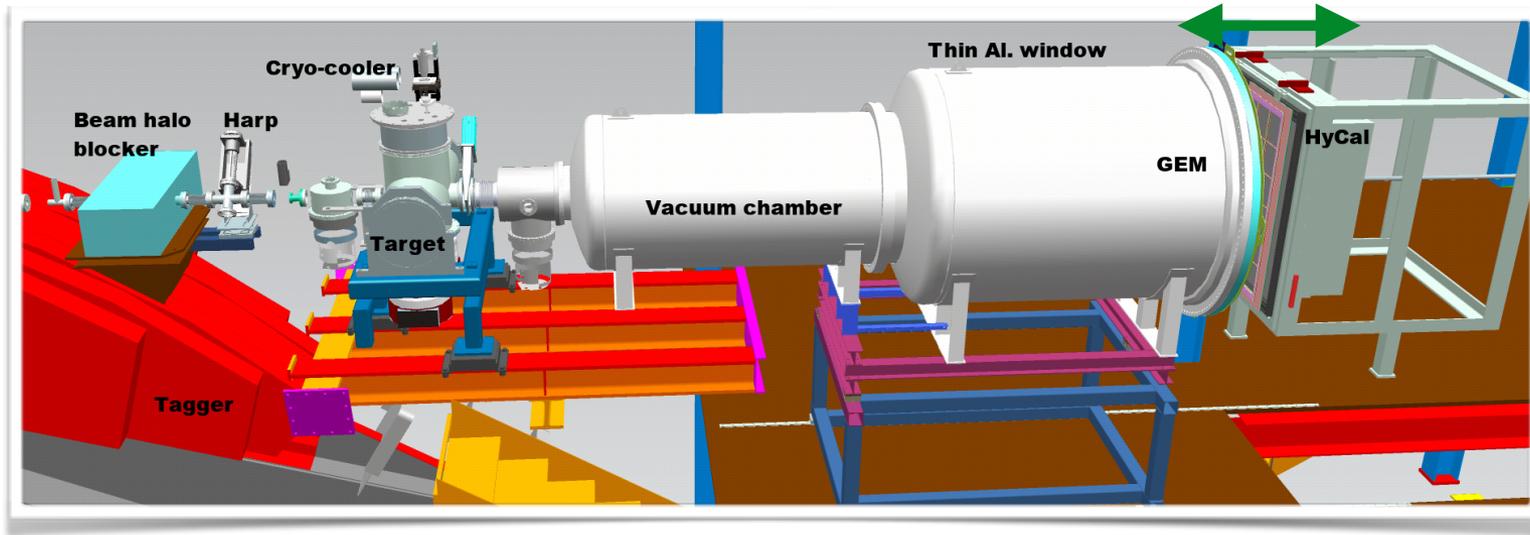
A new proposal - PRad-II was submitted to push the precision frontier of electron scattering.



Upgrade HyCal to be replace all lead-glass modules with PbWO_4 modules to have uniform high resolution.

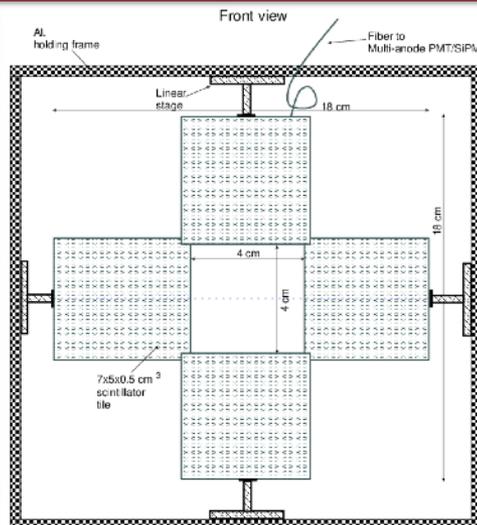
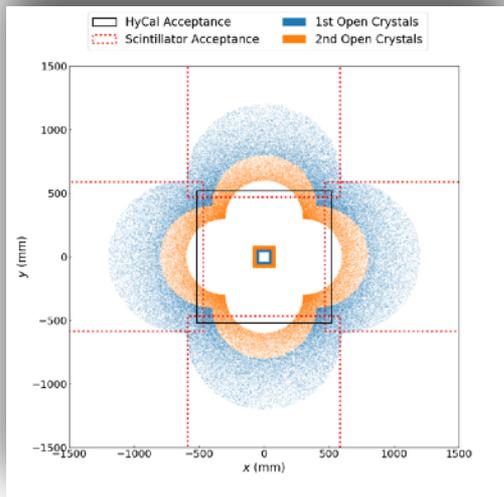
Convert to FADC based readout of HyCal

Add a second GEM plane between HyCal and vacuum chamber to further reduce the backgrounds and improve vertex resolution.

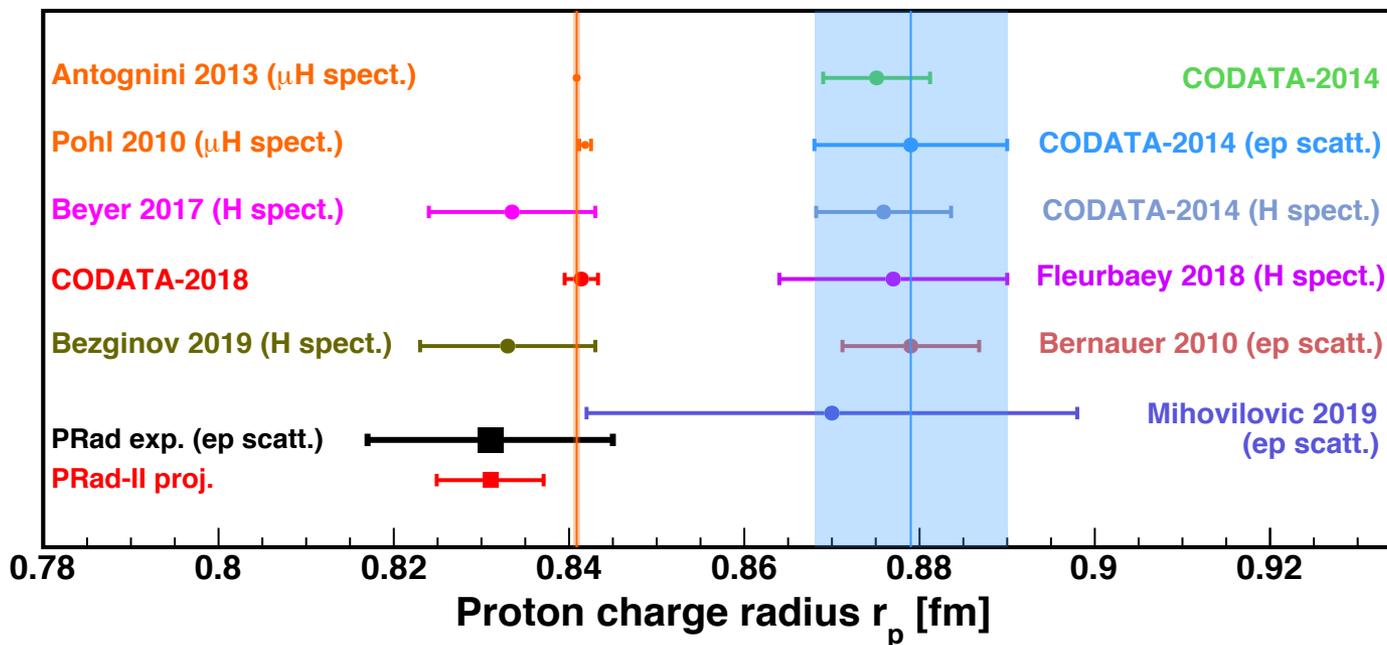


Will improve the precision of r_p measurements and start a new program of high precision measurements using the PRad method

PRad-II is projected to be 2.5 times more precise than PRad



A new scintillator detector will help reach the smallest scattering angles and the lowest Q^2 range (10^{-5} GeV²) in lepton scattering.



The PRad Collaboration



Duke University, NC A&T State University,
Mississippi State University, Idaho State University,
University of Virginia, Jefferson Lab,
Argonne National Lab,
University of North Carolina at Wilmington,
Kharkov Institute of Physics and Technology,
MIT, Old Dominion University, ITEP,
University of Massachusetts, Amherst
Hampton University, College of William & Mary,
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Post-docs

Chao Gu (Duke)
Xuefei Yan (Duke)
Mehdi Meziane (Duke)
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Maxime Lavillain (NC A&T)
Latif-ul Kabir (MSU)

Summary

- **The proton charge radius is a fundamental quantity in Physics**
 - ✓ Important for precision atomic spectroscopy
 - ✓ Precision tests of future lattice QCD calculations
 - ✓ “New Physics”
- **The “proton radius puzzle” arose in 2010 with the first μH spectroscopy measurement of r_p .**
- **A novel electron scattering experiment (PRad) was completed at JLab Hall-B in 2016**
 - ✓ lowest Q^2 ($\sim 2 \times 10^{-4} \text{ GeV}^2$) in ep-scattering experiments was achieved;
 - ✓ simultaneous measurement of the **Møller and elastic** scattering processes was demonstrated to control systematic uncertainties;
 - ✓ data in a large Q^2 range ($2 \times 10^{-4} - 6 \times 10^{-2} \text{ GeV}^2$) was recorded in the same experimental setting, for the first time in ep-scattering experiments.
- **The PRad result found a small proton charge radius.**
- **Several other recent results seem to confirm the small proton radius.**
- **Several new experiments are being prepared to help further establish these results.**

This work was supported by NSF-MRI grant PHY-1229153 and US DOE grant DE-FG02-07ER41528

The PRad results received some press coverage.



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- 5 Facebook pages
- 2 Wikipedia pages

SUMMARY

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Misc.

? So far, Altmetric has seen **27** news stories from **27** outlets.

bild der wissenschaft

Bild der wissenschaft 01-2020 - wissenschaft.de

wissenschaft.de, 16 Dec 2019

Zu den Nachrichten in der Rubrik „Magazin“ in der bild der wissenschaft-Ausgabe 01/2020, finden Sie hier die Quellen und weiterfü...

Daily Press

Jefferson Lab helping to resolve the “proton radius puzzle”

Daily Press, 15 Nov 2019

How do you measure the width of a proton? A ruler won't help and neither will a microscope. Instead, it involves smashing...

madriod

Científicos confirman que el protón ha menguado

Madrid, 13 Nov 2019

La medida más precisa hasta la fecha le otorga un radio de 0,8331 fentómetros, menos que lo asignado por mediciones anteriores...

physicsworld

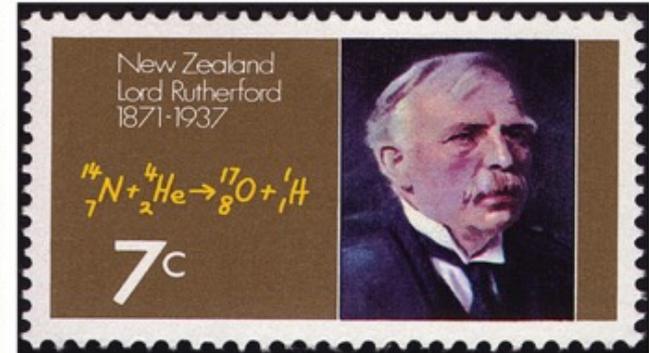
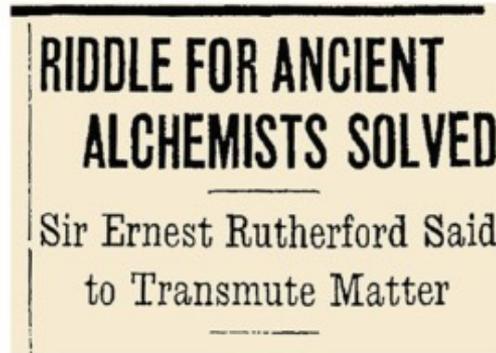
Electron scattering experiment is first to point to a small proton radius Physics

Rutherford discovers the hydrogen nucleus is produced in α -scattering from air.



when α -particles were shot into air, hydrogen nuclei were detected as a product.

α -scattering on other atoms produced hydrogen nuclei in every case.



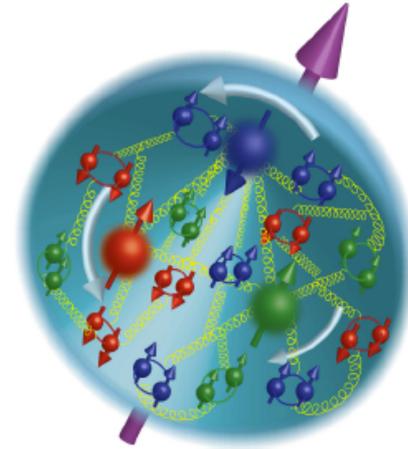
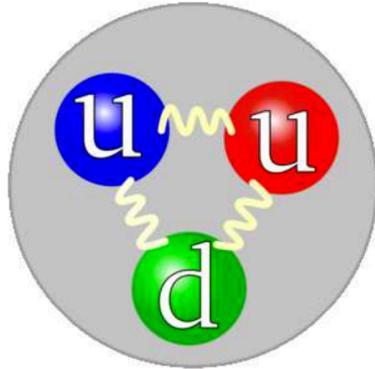
Rutherford concluded that hydrogen nucleus played a fundamental role in atomic structure, and called it a proton (**proton appears in literature for the first time in 1920**).

In 1933 Stern measured the anomalous magnetic moment of the proton $\mu_p = 2.79$

Showing that the proton is **NOT** an elementary point like particle.



The proton proved to be an ideal laboratory to study the strong interaction.



Many questions still left to answer:

- How does proton acquire its mass: only 1% of proton mass comes from Higgs.
- What are the different contributions to nucleon spin (especially the gluons)?
- How does the confinement come about and does the proton decay?

But we thought we at least understood the ground state bulk properties of the proton, such as the charge radius....

The proton electric form factor was extracted at the lowest Q^2 ever achieved in electron scattering.

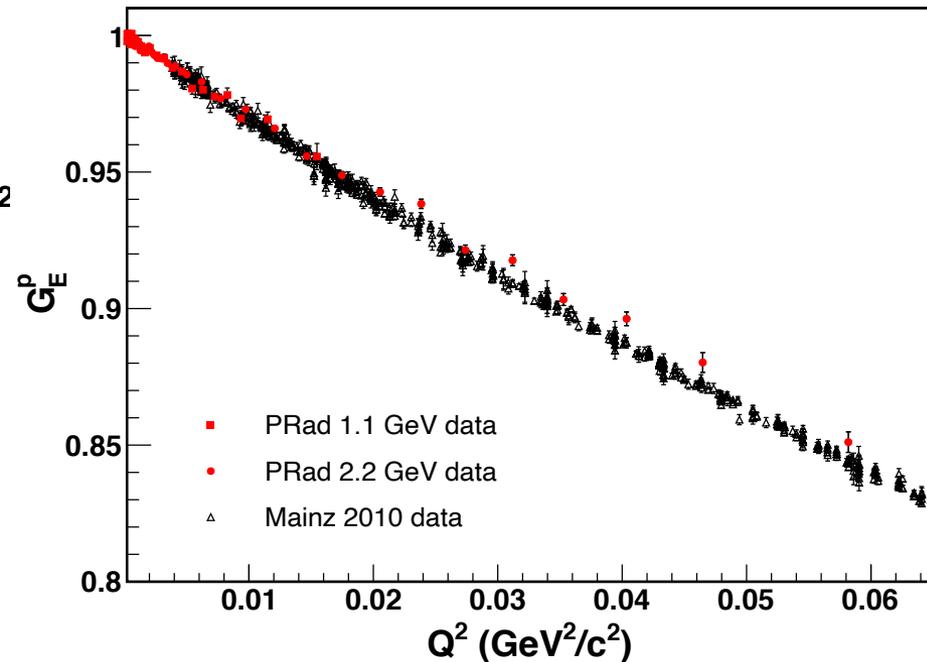
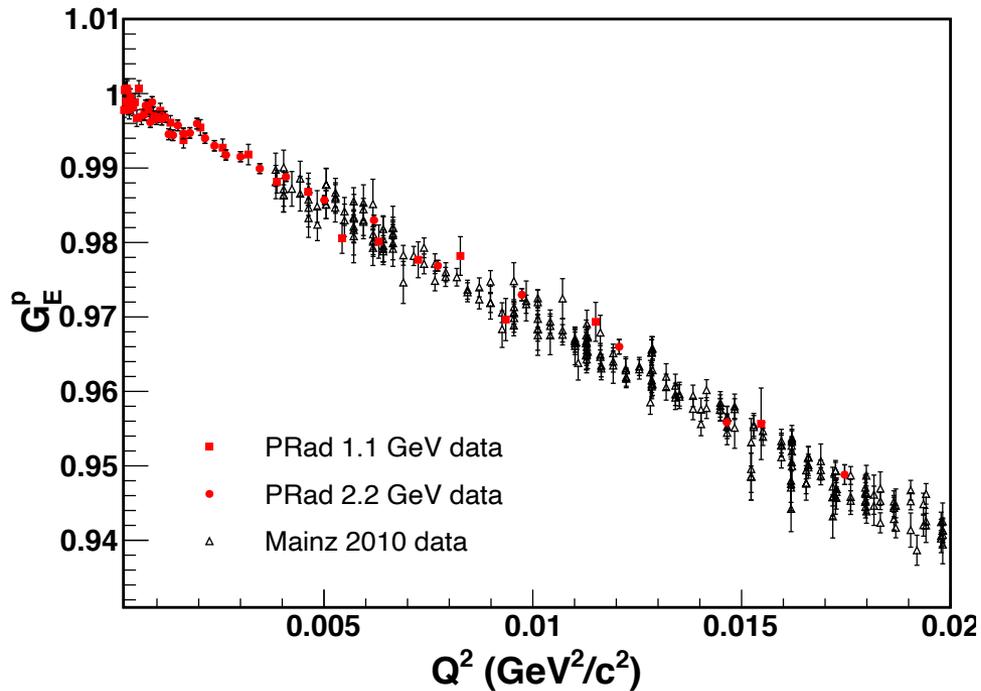
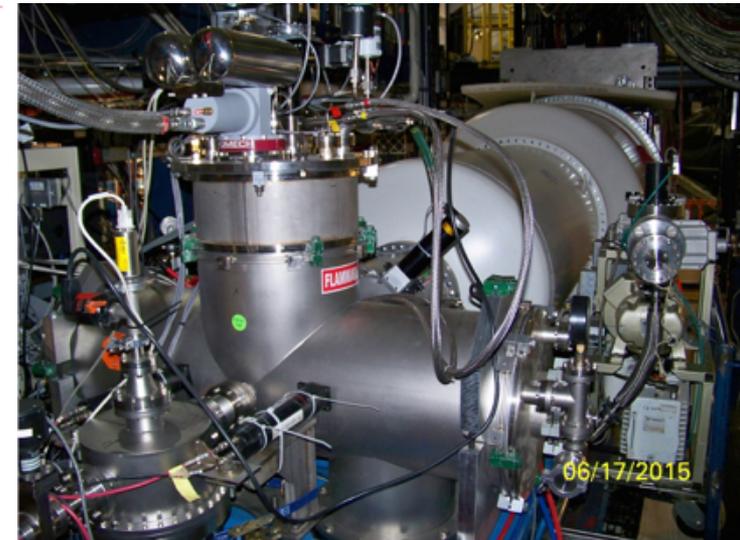
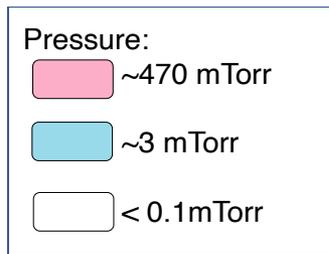
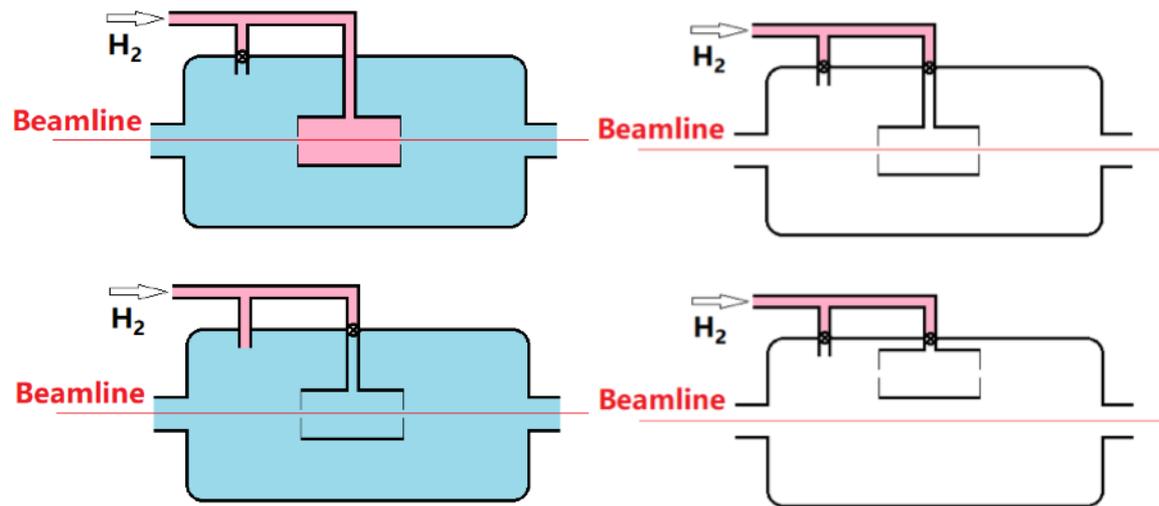


Figure courtesy of W. Xiong

Empty target runs were taken for background subtraction.

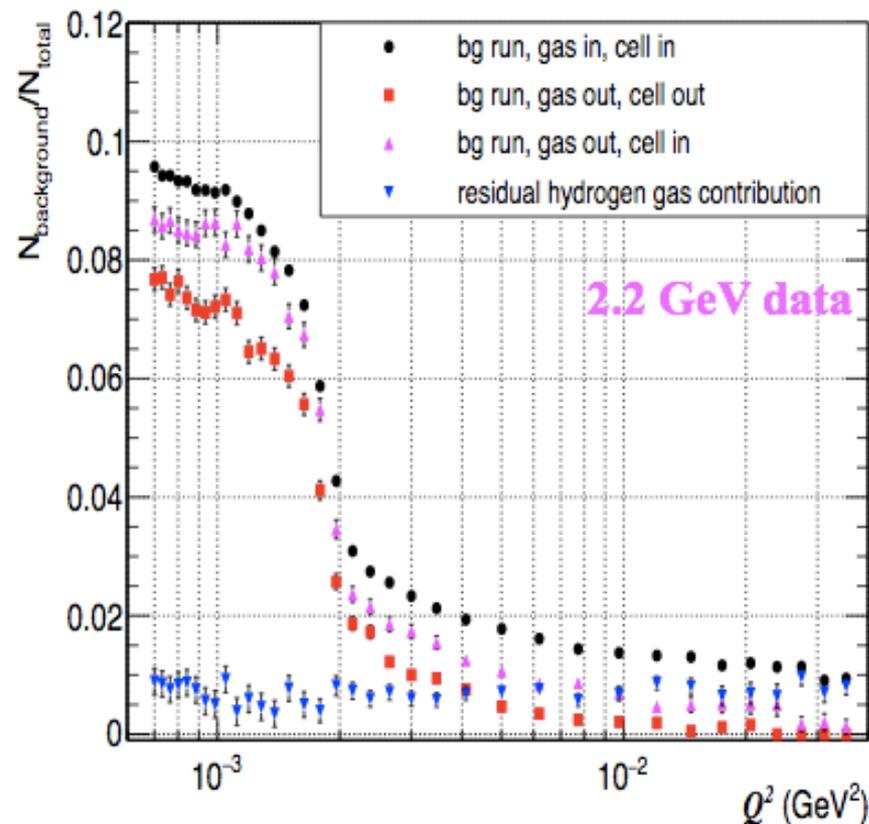
- Runs with different target condition taken for background subtraction and studies for the systematic uncertainty
- Developed simulation program for target density (COMSOL finite element analysis)



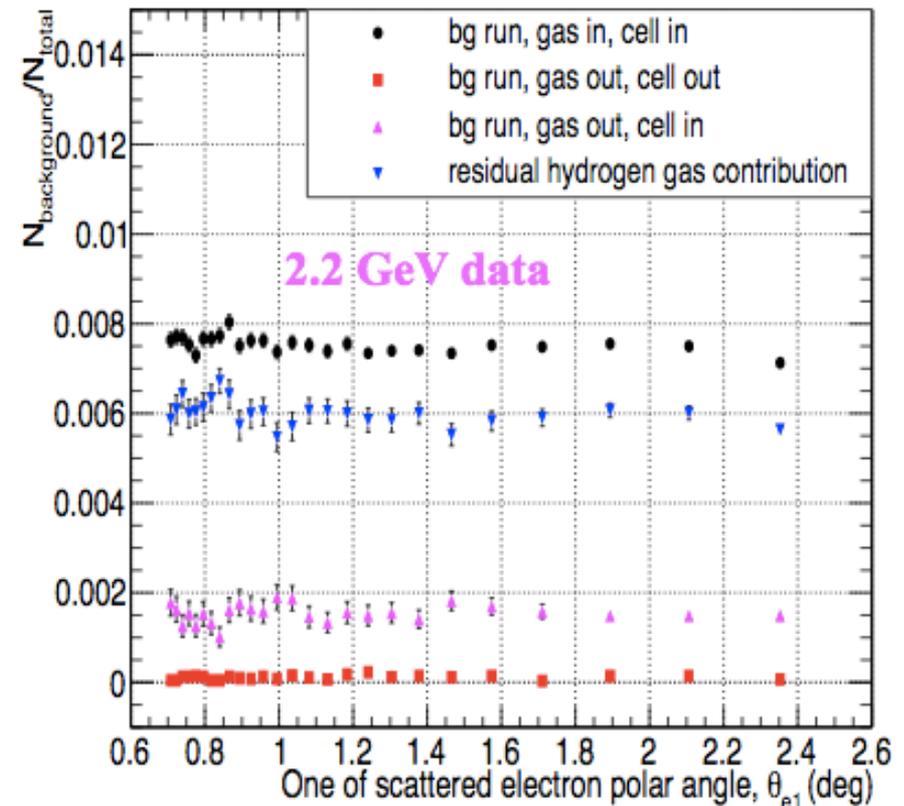
Empty target runs were used for background subtraction.

- ep background rate $\sim 10\%$ at forward angle (<1.3 deg, dominated by upstream collimator), less than 2% otherwise
- ee background rate $\sim 0.8\%$ at all angles

ep Background Contribution



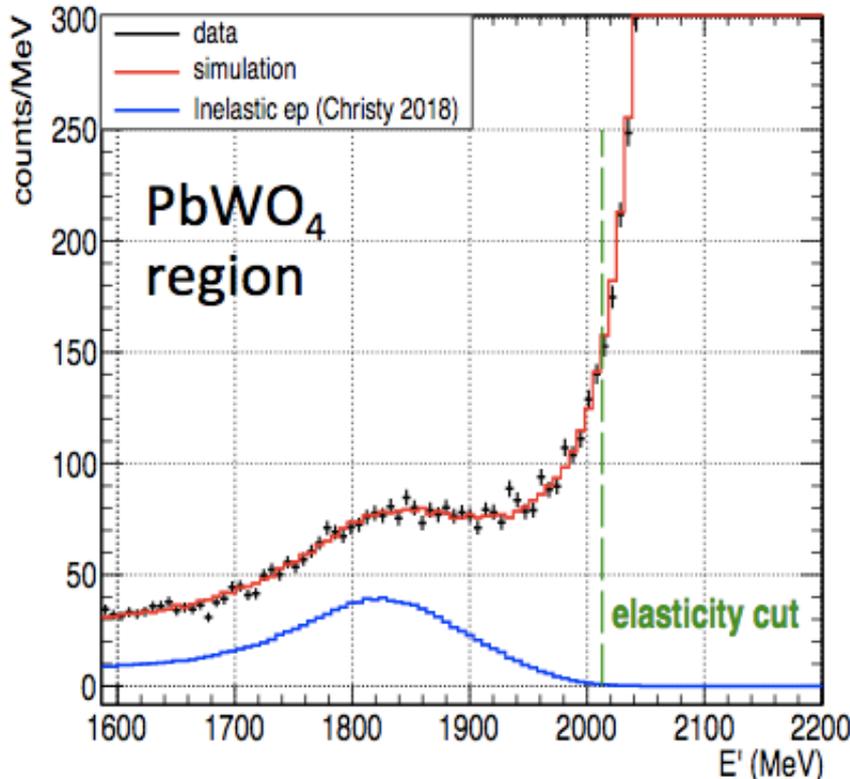
ee Background Contribution



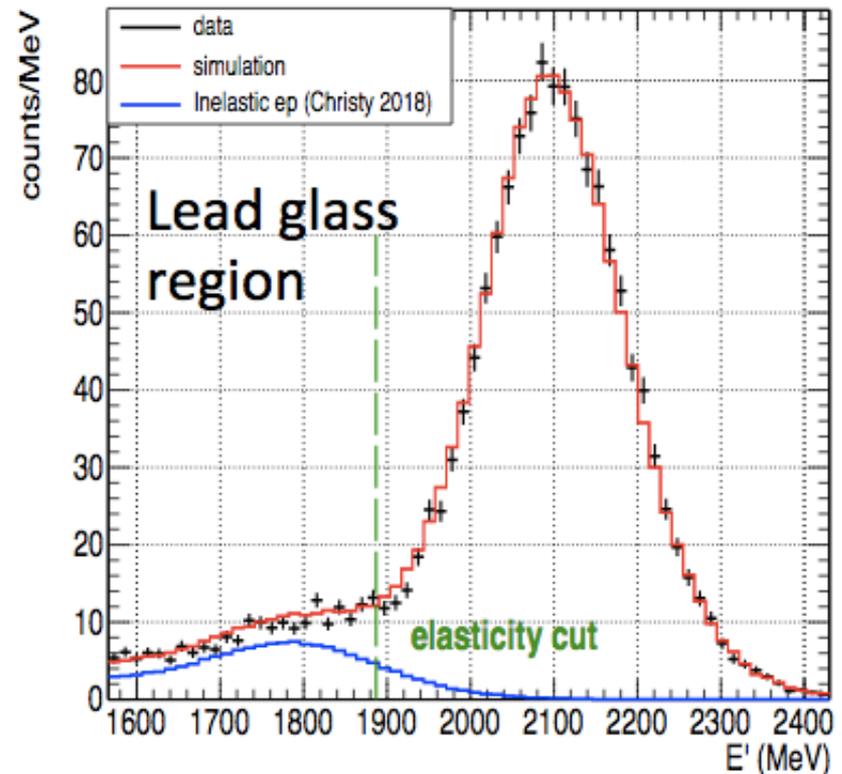
Contribution from inelastic scattering was simulated and compared to data.

- Using Christy 2018 empirical fit to study inelastic ep contribution
- Good agreement between data and simulation
- Negligible for the PbWO_4 region ($<3.5^\circ$), less than 0.2%(2.0%) for 1.1GeV(2.2GeV) in the Lead glass region

spectrum for $3.0^\circ < \theta < 3.3^\circ$ ($Q^2 \sim 0.014 \text{ GeV}^2$)

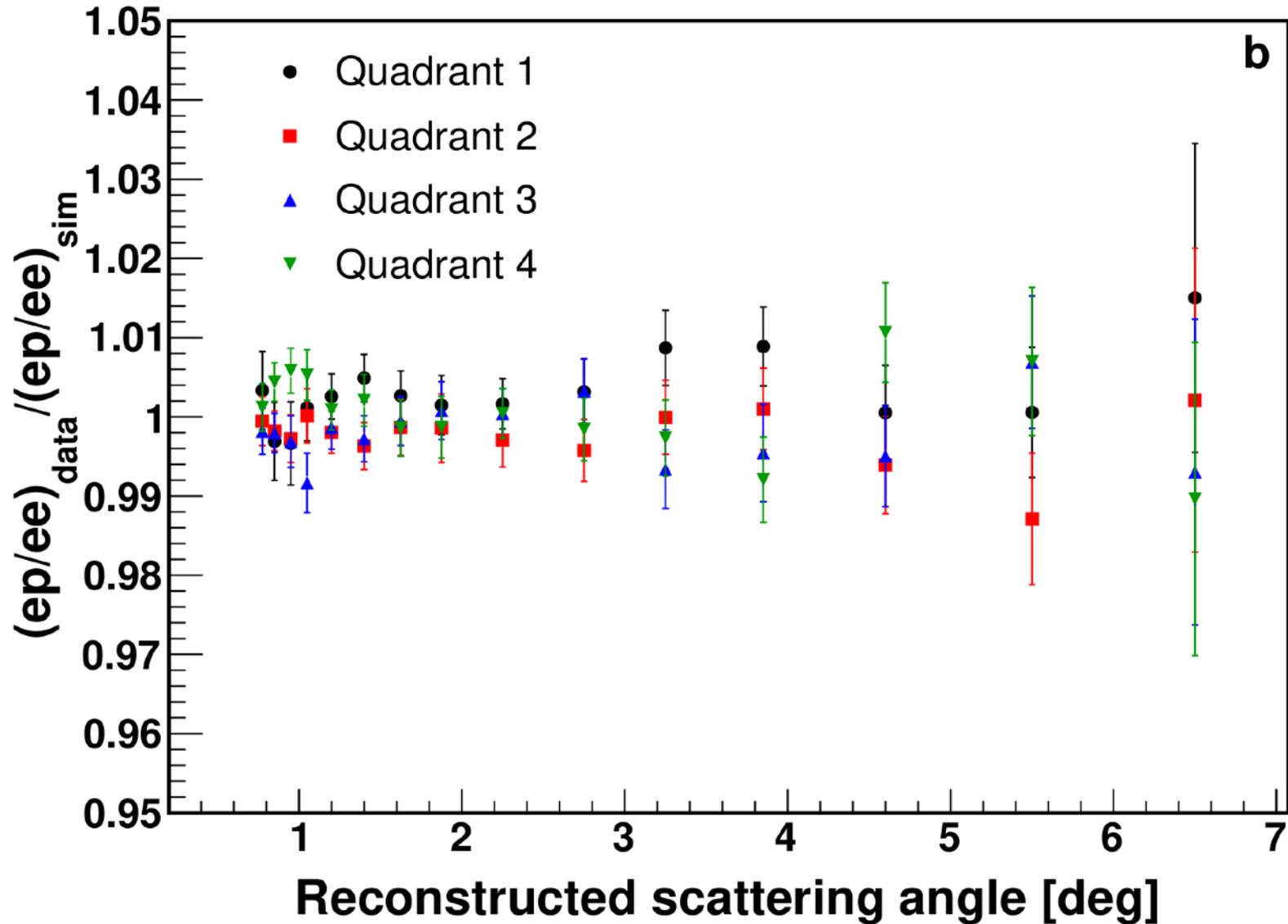


spectrum for $6.0^\circ < \theta < 7.0^\circ$ ($Q^2 \sim 0.059 \text{ GeV}^2$)

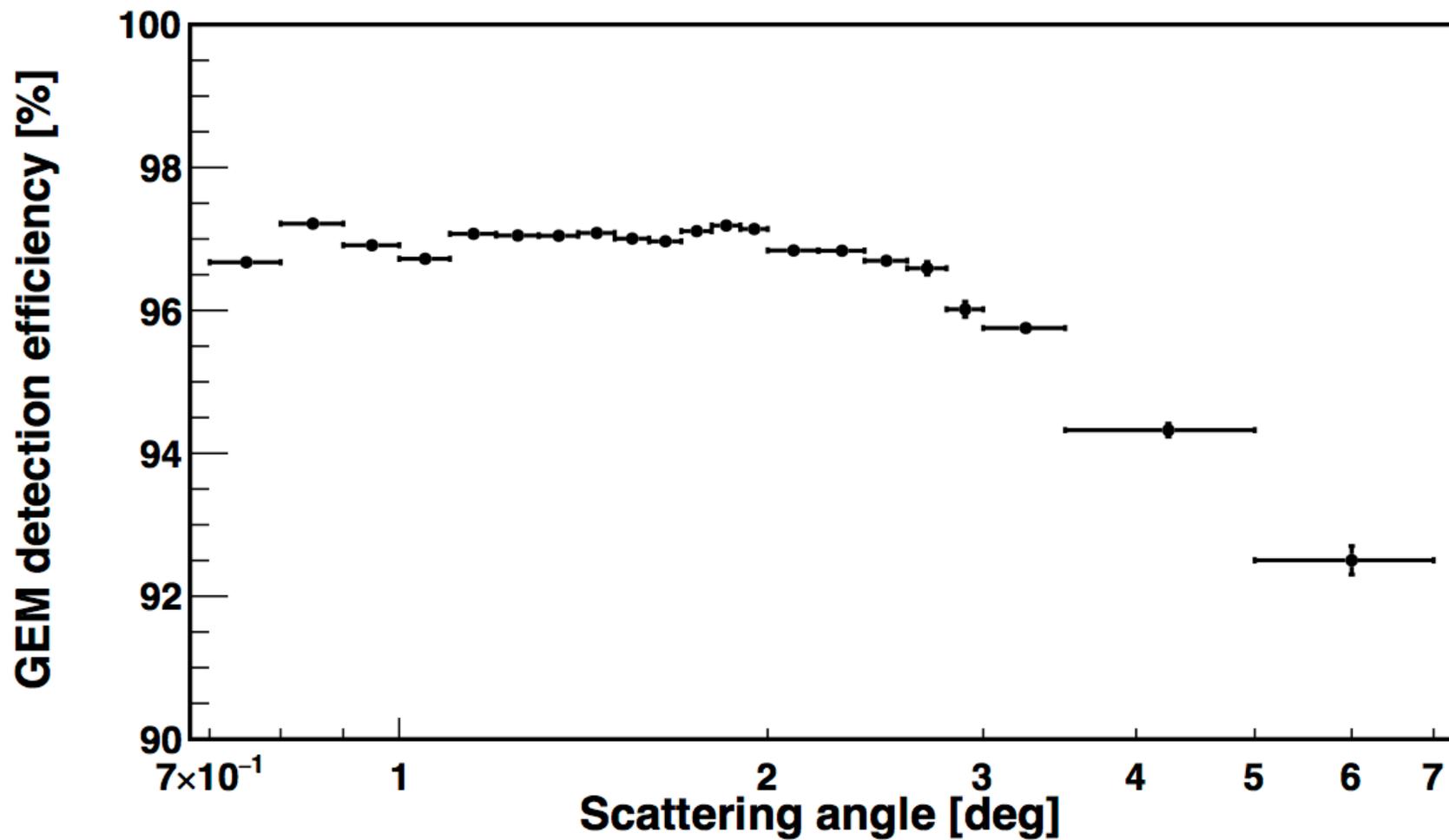


M.E. Christy and P.E. Bosted. PRC 81, 055213 (2010)

4-quadrant test demonstrated azimuthal symmetry



GEM efficiency



Simultaneous detection of ep elastic and ee Moller events

- ep cross section measured related to Moller:

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^- \rightarrow e^-e^-)} \cdot \frac{\epsilon_{\text{geom}}^{e^-e^-}}{\epsilon_{\text{geom}}^{ep}} \cdot \frac{\epsilon_{\text{det}}^{e^-e^-}}{\epsilon_{\text{det}}^{ep}} \right] \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$

Two major sources of systematic errors, N_e and N_{tgt} , cancel

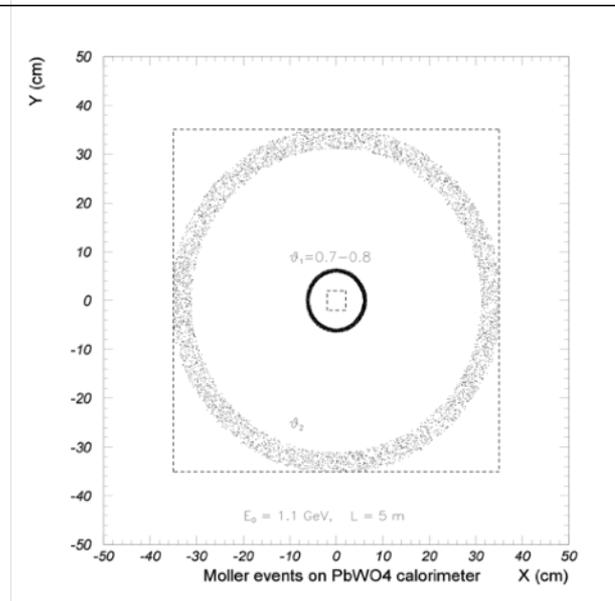
ϵ_{det} will be measured for [0.5 – 2.0] GeV range

Relative ϵ_{det} are needed for this experiment

Alternative Moller analysis methods possible

Detect both Moller electrons in coincidence

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^- \rightarrow e^-e^-)} \cdot \frac{\epsilon_{\text{geom}}^{e^-e^-}}{\epsilon_{\text{geom}}^{ep}} \cdot \frac{\epsilon_{\text{det}}^{e^-e^-}}{\epsilon_{\text{det}}^{ep}} \right] \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$



Integrated over HyCal acceptance

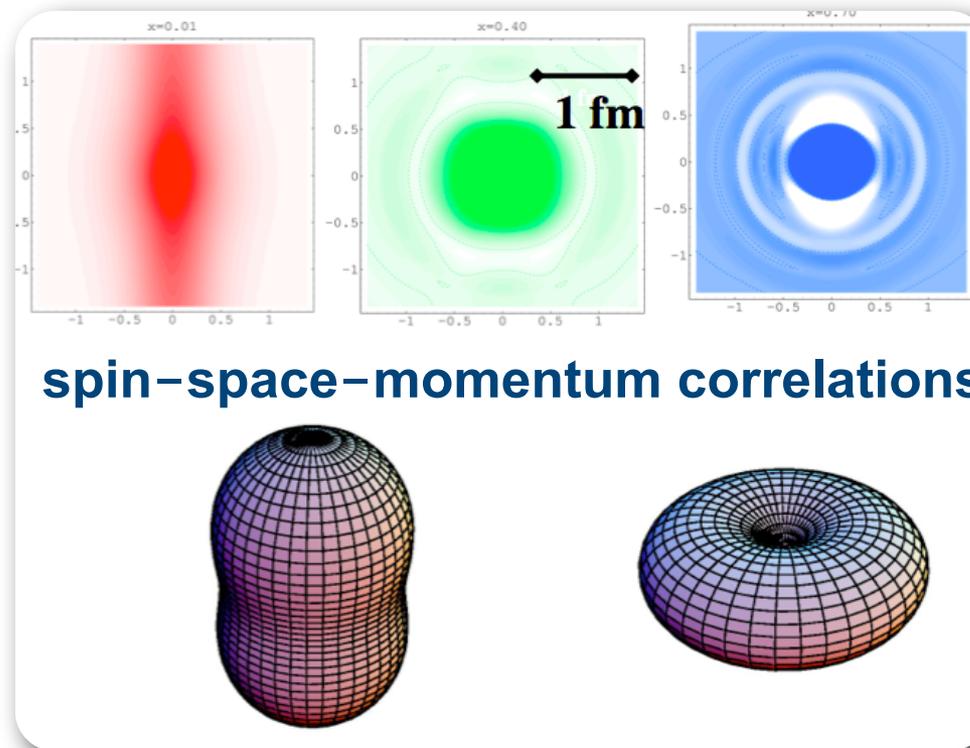
$$\left(\frac{d\sigma}{d\Omega}\right)_{ep}(Q_i^2) = \left[\frac{N_{\text{exp}}^{\text{yield}}(ep, \theta_i \pm \Delta\theta)}{N_{\text{exp}}^{\text{yield}}(e^-e^-, \text{ on PWO})} \right] \frac{\epsilon_{\text{geom}}^{e^-e^-}(\text{all PWO})}{\epsilon_{\text{geom}}^{ep}(\theta_i \pm \Delta\theta)} \frac{\epsilon_{\text{det}}^{e^-e^-}(\text{all PWO})}{\epsilon_{\text{det}}^{ep}(\theta_i \pm \Delta\theta)} \left(\frac{d\sigma}{d\Omega}\right)_{e^-e^-}$$

Over the last decade a new framework has been developed to map the 3D structure of the proton.

Generalized Parton Distributions (GPDs): a 3D map of the proton

GPDs provide connection between the formfactors and the parton distributions

the shape of the proton in the GPD framework



M. Burkardt ; A.Belitsky, X.Ji, F.Yuan PRD69, 074014 (2004) ; G.Miller, PRC68, 022201 (2003)

The PRad Collaboration

nature

Article | Published: 06 November 2019

A small proton charge radius from an electron–proton scattering experiment

13 of the **58** authors from **MSU**
3 faculty, **3** post-docs (former)
6 graduate students (**1** thesis student) & **1** undergraduate

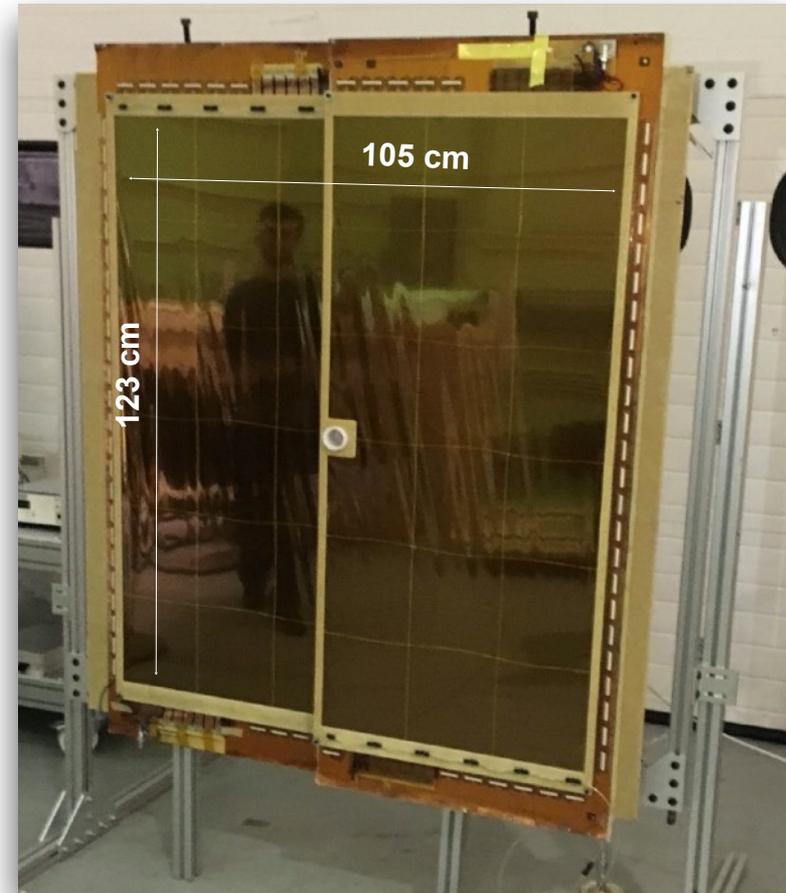
W. Xiong, A. Gasparian , H. Gao, D. Dutta , M. Khandaker, N. Liyanage, E. Pasyuk, C. Peng, X. Bai, L. Ye, K. Gnanvo, C. Gu, M. Levillain, X. Yan, D. W. Higinbotham, M. Meziane, Z. Ye, K. Adhikari, B. Aljawrneh, H. Bhatt, D. Bhetuwal, J. Brock, V. Burkert, C. Carlin, A. Deur, D. Di, J. Dunne, P. Ekanayaka, L. El-Fassi, B. Emmich, L. Gan, O. Glamazdin, M. L. Kabir, A. Karki, C. Keith, S. Kowalski, V. Lagerquist, I. Larin, T. Liu, A. Liyanage, J. Maxwell, D. Meekins, S. J. Nazeer, V. Nelyubin, H. Nguyen, R. Pedroni, C. Perdrisat, J. Pierce, V. Punjabi, M. Shabestari, A. Shahinyan, R. Silwal, S. Stepanyan, A. Subedi, V. V. Tarasov, N. Ton, Y. Zhang & Z. W. Zhao - Show fewer authors

Nature **575**, 147–150(2019) | Cite this article

Large area GEM coordinate detectors

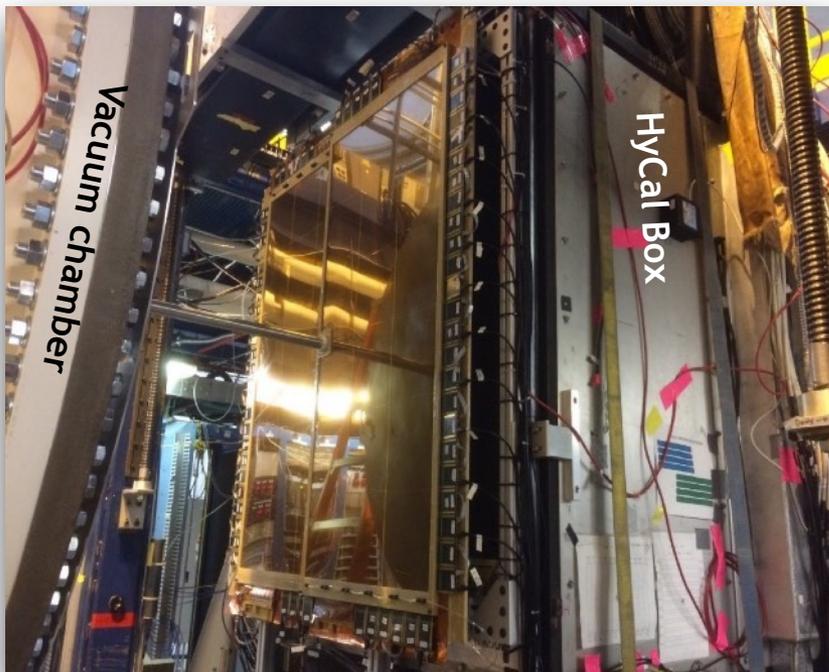
- Two large GEM based X and Y- coordinate detectors with 100 μm position resolution
- The GEM detectors provided:
 - factor of **>20 improvements in coordinate resolutions**
 - similar improvements in Q^2 resolution
 - unbiased coordinate reconstruction (including HyCal transition region)
 - increase Q^2 range by enabling use of Pb-glass part of calorimeter

- Designed and built at University of Virginia (UVa)

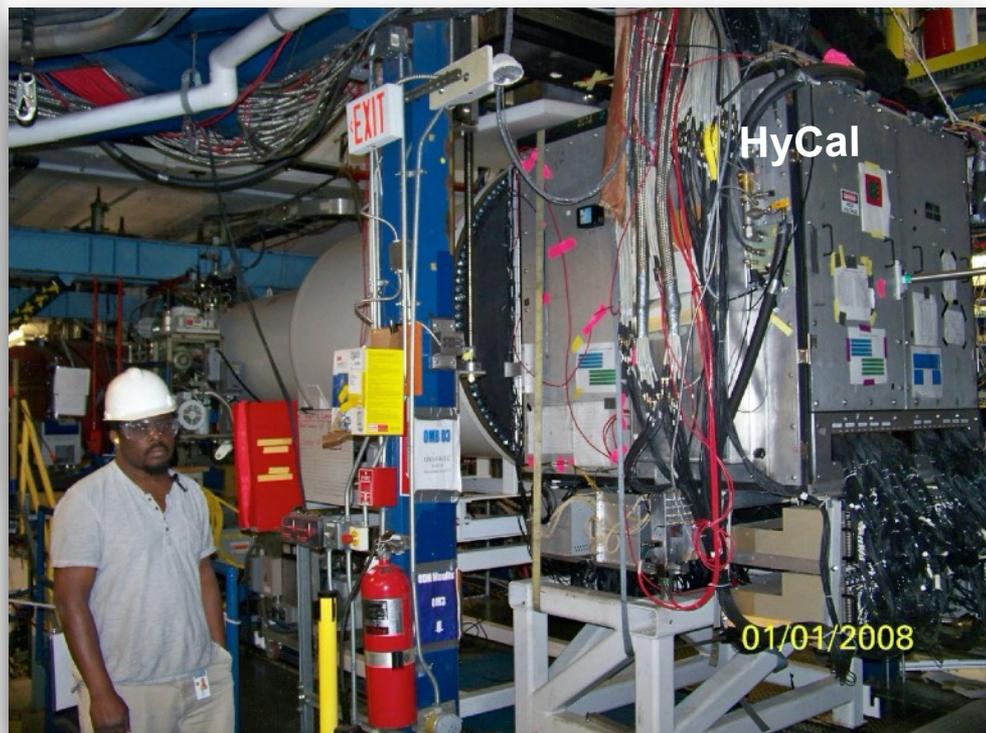


HyCal and GEMs on the beamline

beam view



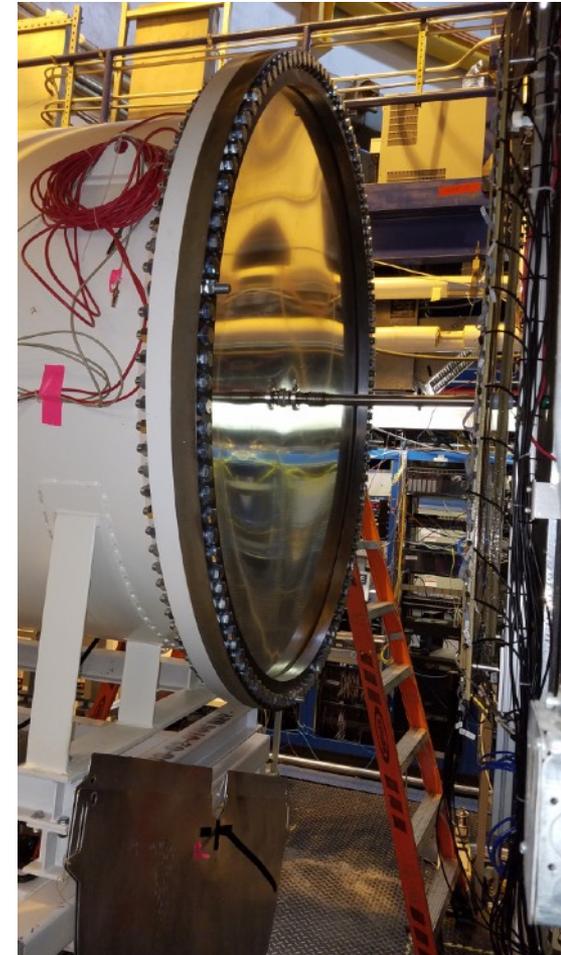
downstream view



Vacuum chamber with one thin window



two stage, 5 m long vacuum chamber



1.7 m dia, 2 mm thick
Al window

High quality, stable CEBAF electron beam

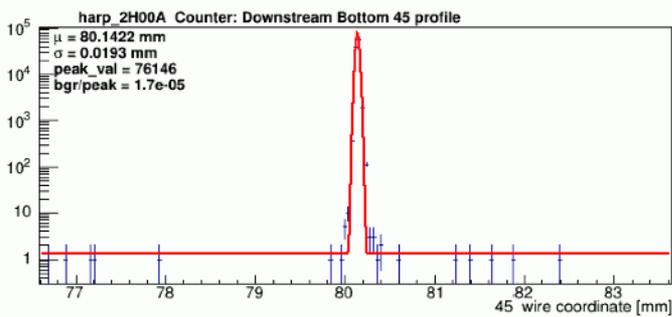
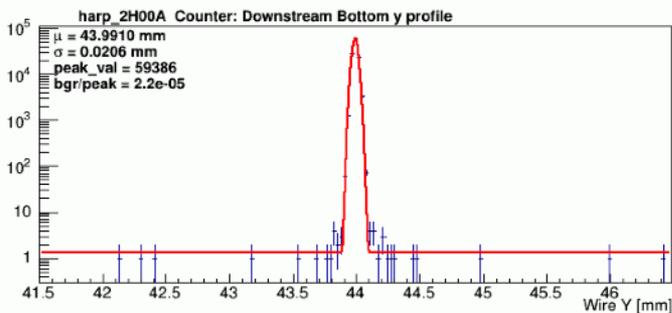
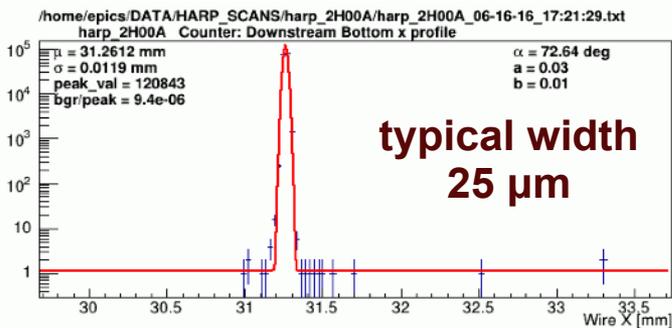
electron beam profile at target
(measured with harp scan)

position stability : $\pm 250 \mu\text{m}$

Experiment ran during May/June 2016

With $E_e = 1.1 \text{ GeV}$ beam
collected **4.2 mC** on target (2×10^{18} H atoms/cm²)
604 M events with H and
53 M events without H in target
25 M events on $1 \mu\text{m}$ Carbon foil target

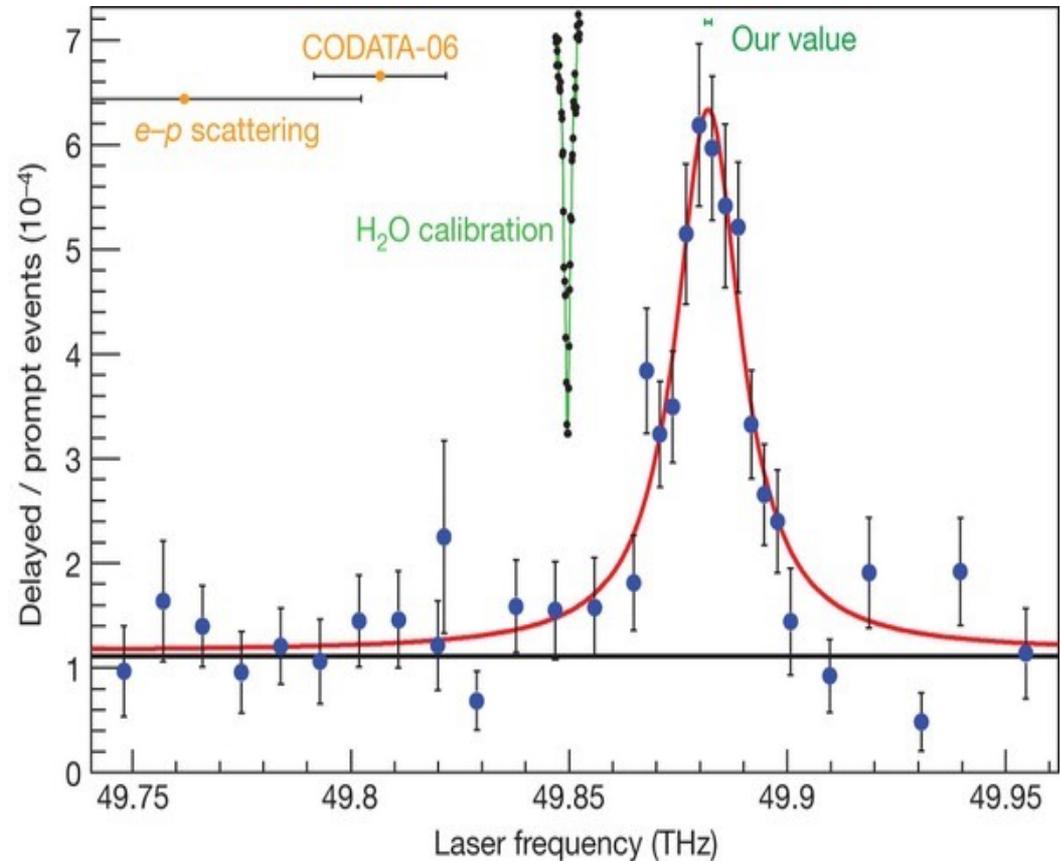
With $E_e = 2.2 \text{ GeV}$ beam
collected **14.3 mC** on target (2×10^{18} H atoms/cm²)
756 M events with H and
38 M events without H in target
10.5 M events on $1 \mu\text{m}$ Carbon foil target



The muonic hydrogen spectroscopy results had unprecedented precision and were very surprising.



R. Pohl et al, Nature, 466, 213 (2010).

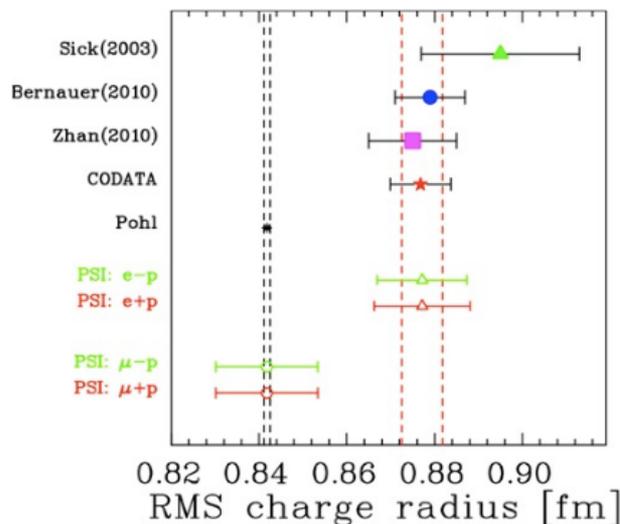
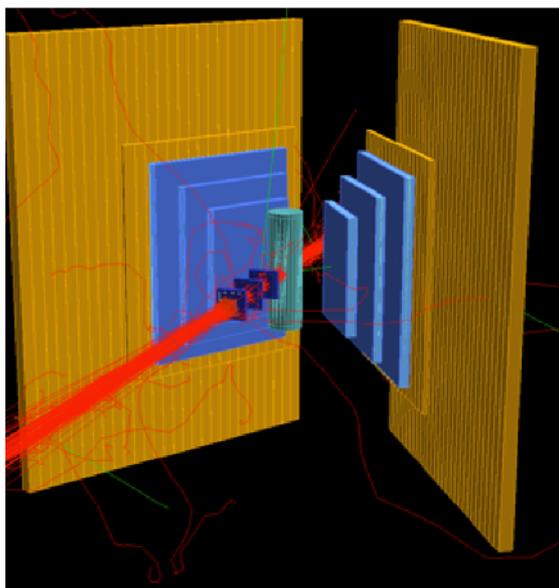


- Muonic hydrogen Lamb shift experiment at PSI: $Q^2 \sim 10^{-6} \text{ GeV}^2$
- $r_p = 0.84184(67) \text{ fm} \rightarrow$ unprecedented precision $\sim 0.08\%$
- Different from most previous experimental results and analysis.

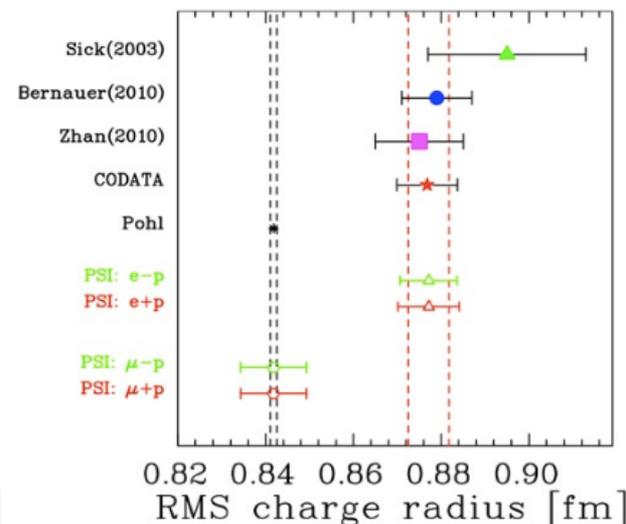
Several new experiments are currently being prepared and some are expected to run as soon as Fall 2019.

The MUon proton Scattering *Experiment (MUSE)* at the PSI will simultaneously measure elastic μ^\pm -p and elastic e^\pm -p scattering to determine r_p .

Spokespersons: R. Gilman, E. Downie, & G. Ron



Absolute errors



Relative errors

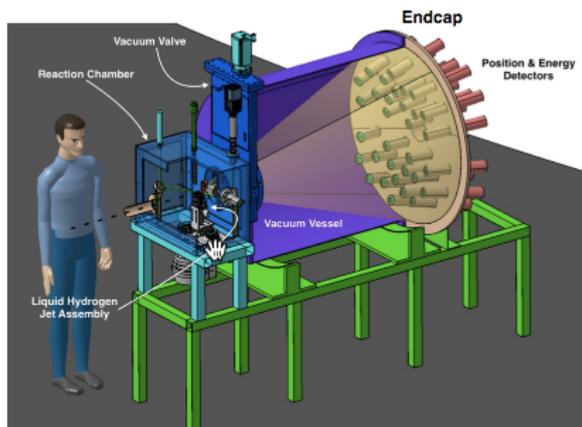
Individual radius extractions from e^\pm , μ^\pm each to 0.01 fm

- Test of lepton universality
- determination contribution of two-photon exchange in μ -p scattering.

$\theta \approx 20^\circ - 100^\circ$
 $Q^2 \approx 0.002 - 0.07 \text{ GeV}^2$
 3.3 MHz total beam flux
 $\approx 2\text{-}15\% \mu$'s
 $\approx 10\text{-}98\% e$'s
 $\approx 0\text{-}80\% \pi$'s

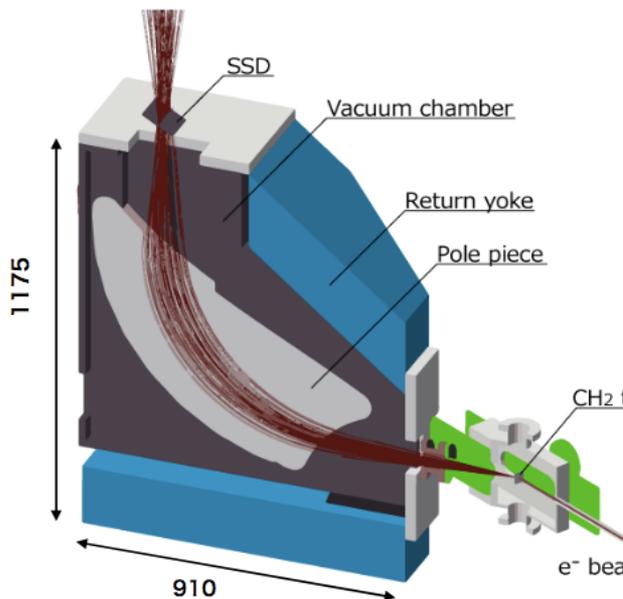
Figures courtesy of J. Arrington and PSI

The ProRad and ULQ² experiments will use very low energy electron beams to reach ultra low Q².



ProRad at IPNO will use a **30-70 MeV** electron beam on a laminar liquid hydrogen jet target to measure the cross section in the **6° - 15°** angular range with a 32 cell detector where each cell consists of a sci-fi coordinate detector and a BGO crystal. ProRad plans to cover a Q² range of **10⁻⁶ - 10⁻⁴ (GeV/c)²**.

Spokesperson: **E. Voutier**

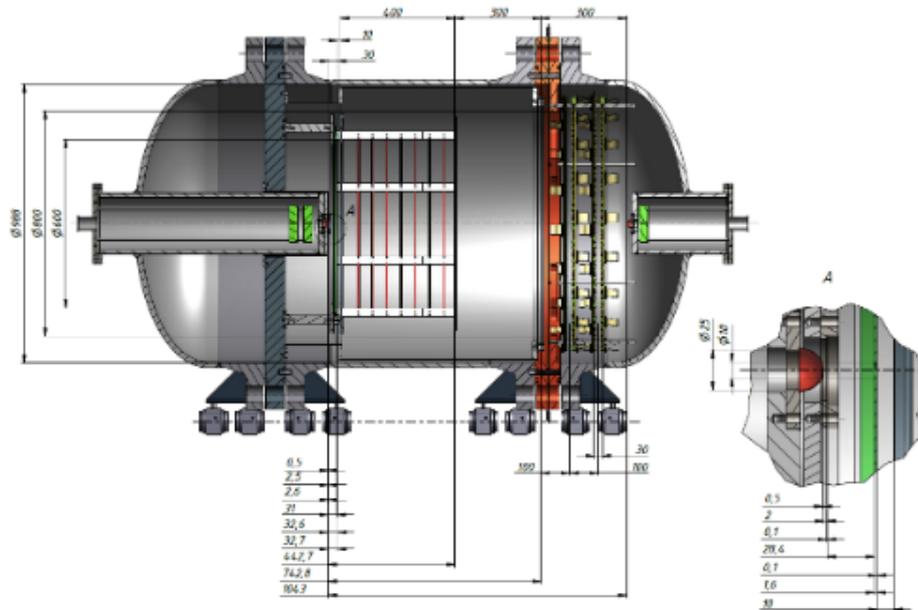


ULQ² collaboration at Tohoku U, will use a **20-60 MeV** electron beam on a CH₂ target to measure the cross section in the **30° - 150°** angular range with double arm high resolution spectrometers. ULQ² plans to cover a Q² range of **3x10⁻⁴ - 8x10⁻³ (GeV/c)²**.

Spokesperson: **T. Suda**

Proton charge radius will be measured at COMPASS and at Mainz using a hydrogen gas TPC.

μ - p scattering will be used to measure r_p at COMPASS using a high pressure hydrogen gas TPC as an active target and recoil proton detector. COMPASS plans to cover a Q^2 range of $10^{-4} - 1$ (GeV/c) 2 .

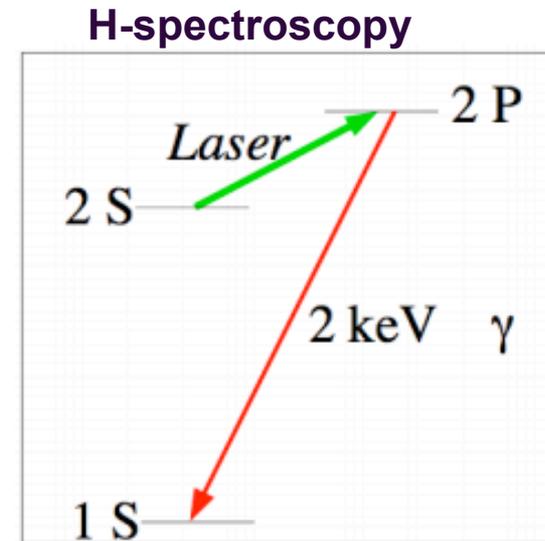
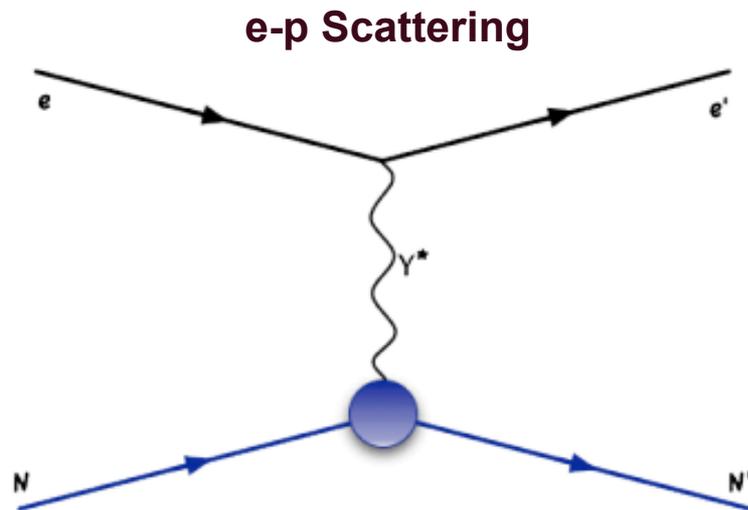


The same high pressure hydrogen gas TPC will be used as an active target and recoil proton detector for an e - p scattering experiment at Mainz to determine r_p

H - spectroscopy and elastic e-p scattering are the two traditional methods for determining proton charge radius

The forces defining the surface of a proton do not come to an abrupt end, its boundary is somewhat fuzzy.

RMS charge radius (r_p) is obtained from a consistent interpretation of hydrogen spectroscopy and electron-proton scattering experiments



For all types of experiments:

r.m.s. charge radius given by the slope at $Q^2 = 0$:

$$\langle r^2 \rangle = -6 \left. \frac{dG_E^p(Q^2)}{dQ^2} \right|_{Q^2=0}$$

This definition has been rigorously shown to be consistent with all experimental measurements. *G. Miller, Phys. Rev., C 99, 035202 (2019)*