

Current Results from the PRad Experiment

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for the PRad Collaboration

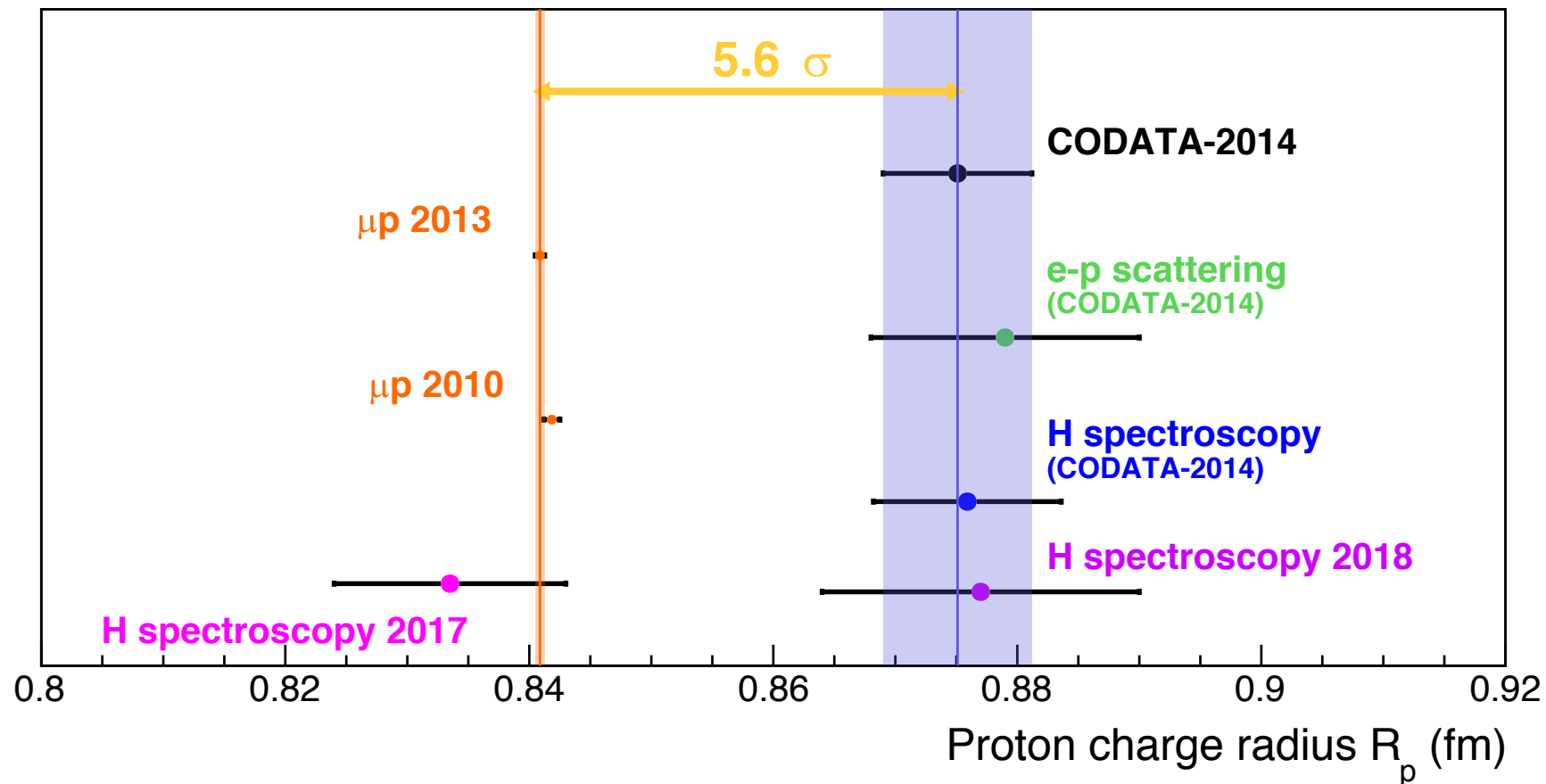
JLab Users Group Meeting 2019
June 25th 2019

Outline

- Introduction and the proton charge radius puzzle
- PRad experiment and apparatus
- Analysis and current results
- Summary



Proton Charge Radius Puzzle: Current Status



Electron scattering: 0.879 ± 0.011 fm (CODATA 2014)

Muon spectroscopy: 0.8409 ± 0.0004 fm (CREMA 2010, 2013)

H spectroscopy (2017): 0.8335 ± 0.0095 fm (A. Beyer et al. Science 358 6359 (2017))

H spectroscopy (2018): 0.877 ± 0.013 fm (H. Fleurbaey et al. PRL 120 183001 (2018))

ep Elastic Scattering

- Elastic ep scattering, in the limit of Born approximation (one photon exchange):

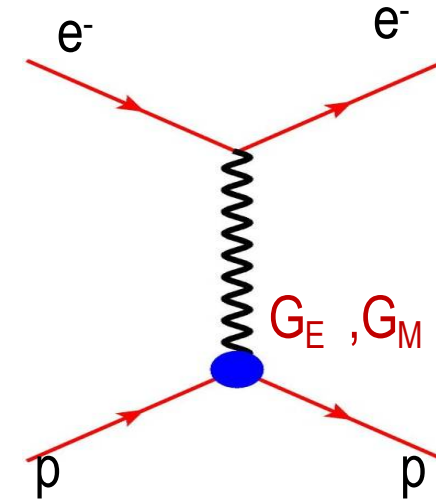
$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega} \right)_{\text{Mott}} \left(\frac{E'}{E} \right) \frac{1}{1 + \tau} \left(G_E^p{}^2(Q^2) + \frac{\tau}{\varepsilon} G_M^p{}^2(Q^2) \right)$$

$$Q^2 = 4EE' \sin^2 \frac{\theta}{2} \quad \tau = \frac{Q^2}{4M_p^2} \quad \varepsilon = \left[1 + 2(1 + \tau) \tan^2 \frac{\theta}{2} \right]^{-1}$$

- Structure-less proton:

$$\left(\frac{d\sigma}{d\Omega} \right)_{\text{Mott}} = \frac{\alpha^2 [1 - \beta^2 \sin^2 \frac{\theta}{2}]}{4k^2 \sin^4 \frac{\theta}{2}}$$

- G_E and G_M can be extracted using Rosenbluth separation
- For PRad, cross section dominated by G_E



Taylor expansion of G_E at low Q^2

$$G_E^p(Q^2) = 1 - \frac{Q^2}{6} \langle r^2 \rangle + \frac{Q^4}{120} \langle r^4 \rangle + \dots$$

Derivative at low Q^2 limit

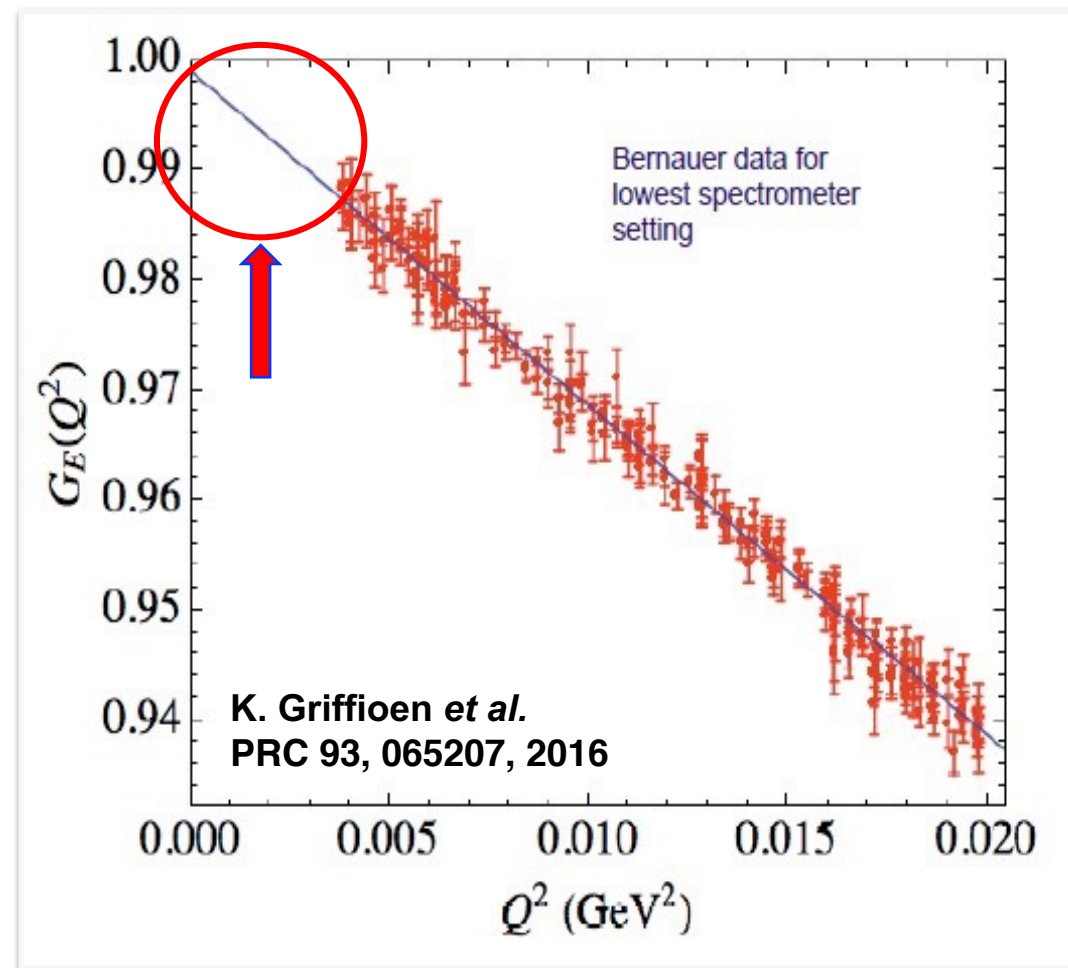
$$\langle r^2 \rangle = -6 \left. \frac{dG_E^p(Q^2)}{dQ^2} \right|_{Q^2=0}$$

PRad Experiment Overview

- PRad goal: Measuring proton charge radius using ep elastic scattering
- Covers **two orders** of magnitude in low Q^2 with the **same detector setting**
 - $\sim 2 \times 10^{-4} - 6 \times 10^{-2} \text{ GeV}^2$
- Unprecedented low Q^2 ($\sim 2 \times 10^{-4} \text{ GeV}^2$)
 - Fill in very low Q^2 region
- Normalize to the simultaneously measured **Møller** scattering process
 - best known control of systematics
- **Windowless** H₂ gas flow target removes major background source
- Extract the radius with precision from **sub-percent** cross section measurement

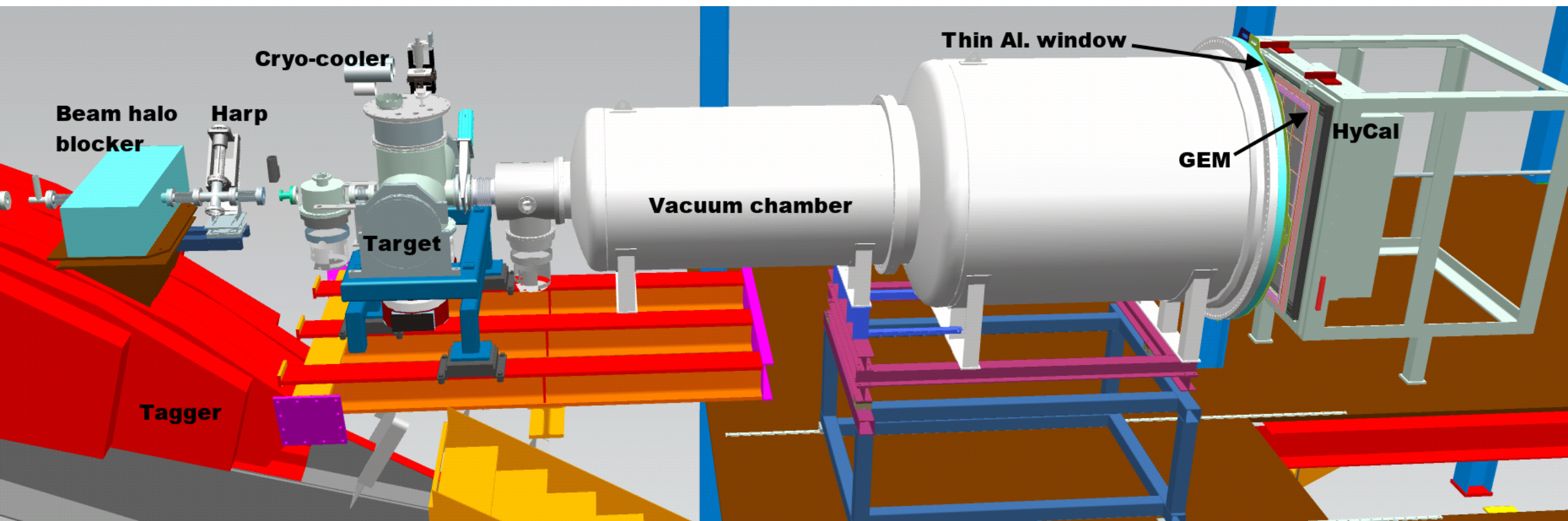
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PRad Experimental Apparatus

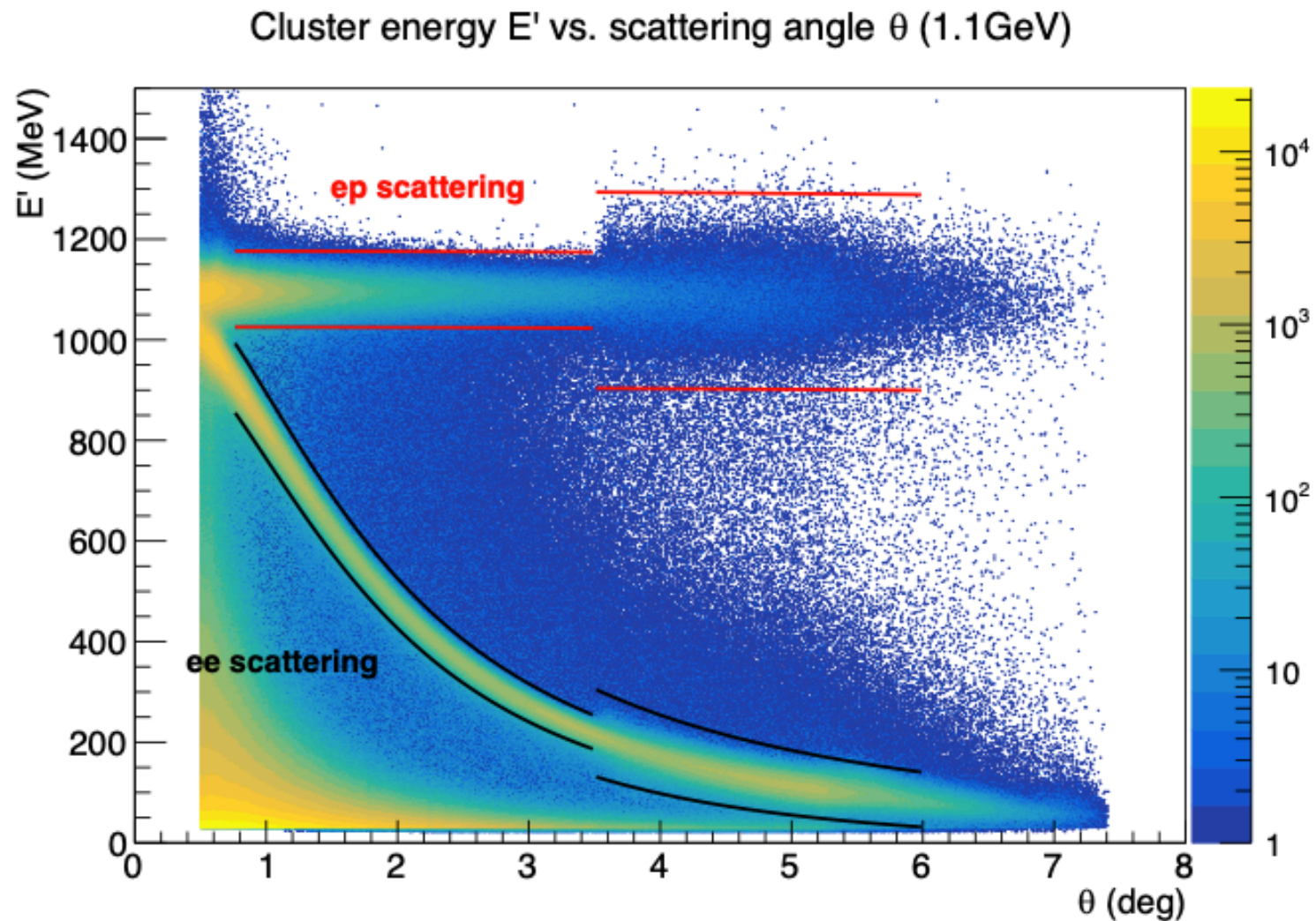
Hall B



Analysis – Event Selection

Event selection method

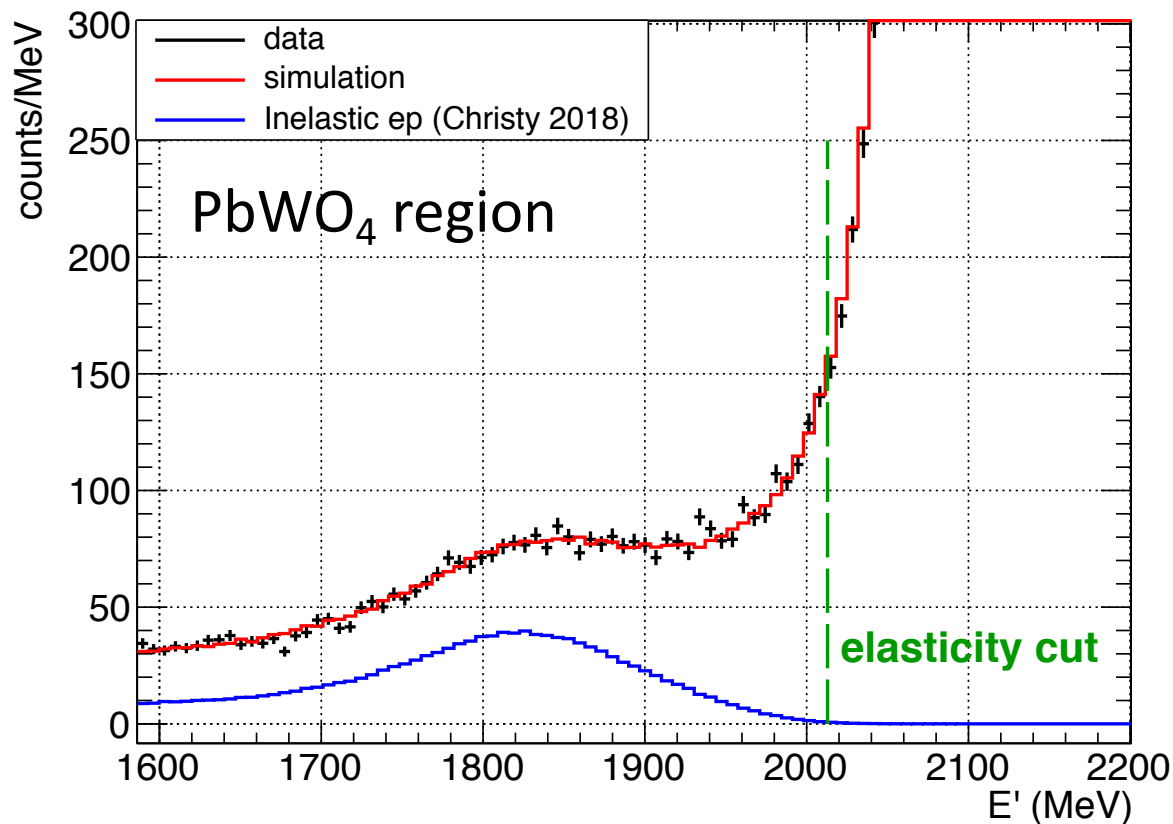
1. For all events, require hit matching between GEMs and HyCal
2. For *ep* and *ee* events, apply angle dependent energy cut based on kinematics
 1. Cut size depend on local detector resolution
3. For *ee*, requiring double-arm events, apply additional cuts
 1. Elasticity
 2. Co-planarity
 3. Vertex z



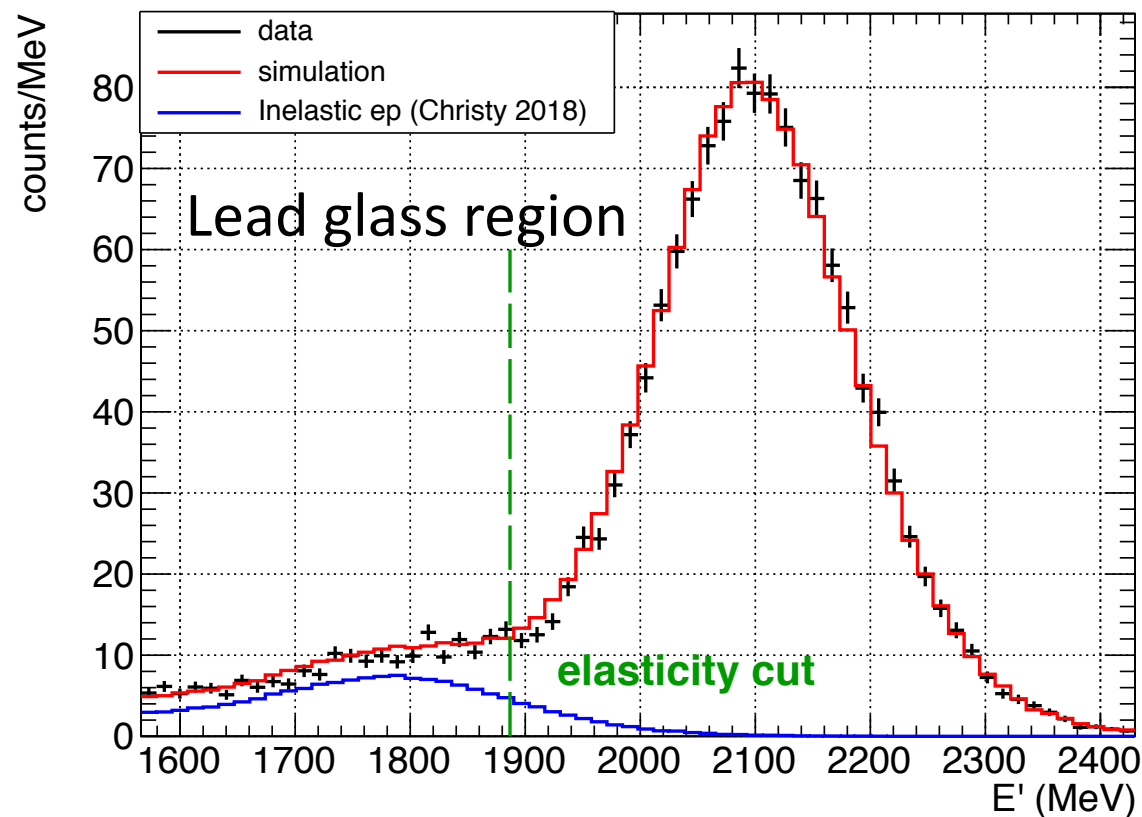
Analysis – Inelastic ep Contribution

- Using Christy 2018 empirical fit to study inelastic ep contribution
- Good agreement between data and simulation
- Negligible for the PbWO_4 region ($<3.5^\circ$), less than 0.2%(2.0%) for 1.1GeV(2.2GeV) in the Lead glass region

spectrum for $3.0^\circ < \theta < 3.3^\circ$ ($Q^2 \sim 0.014 \text{ GeV}^2$)



spectrum for $6.0^\circ < \theta < 7.0^\circ$ ($Q^2 \sim 0.059 \text{ GeV}^2$)



Extraction of ep Elastic Scattering Cross Section

- To reduce the systematic uncertainty, the ep cross section is normalized to the Møller cross section:

$$\left(\frac{d\sigma}{d\Omega}\right)_{ep} = \left[\frac{N_{\text{exp}}(ep \rightarrow ep \text{ in } \theta_i \pm \Delta\theta_i)}{N_{\text{exp}}(ee \rightarrow ee)} \cdot \frac{\varepsilon_{\text{geom}}^{ee}}{\varepsilon_{\text{geom}}^{ep}} \cdot \frac{\varepsilon_{\text{det}}^{ee}}{\varepsilon_{\text{det}}^{ep}} \right] \left(\frac{d\sigma}{d\Omega}\right)_{ee}$$

- Method 1: bin by bin method – taking ep/ee counts from the same angle bin
 - Cancellation of energy independent part of the efficiency and acceptance
 - Limited converge due to double arm Møller acceptance
- Method 2: integrated Moller method – integrate Møller in a fixed angle range and use it as common normalization for all angle bins
- Luminosity cancelled from both methods

Radiative Correction

- Radiative effects corrected by Monte-Carlo method:
 1. Geant4 simulation package with full geometry setup
 2. event generators with complete calculations of radiative corrections^{1,2}, include emission of radiative photons
 3. Consistent results between generators
 4. Include TPE effect³, less than 0.2% for ep in PRad kinematic range
 5. Iterative procedure applied for radiative correction

$$\sigma_{ep}^{Born(exp)} = \left(\frac{\sigma_{ep}}{\sigma_{ee}} \right)^{exp} / \left(\frac{\sigma_{ep}}{\sigma_{ee}} \right)^{sim} \cdot \left(\frac{\sigma_{ep}}{\sigma_{ee}} \right)^{Born(model)} \cdot \sigma_{ee}^{Born(model)}$$

1. I. Akushevich et al., Eur. Phys. J. A 51(2015)1 (fully beyond ultra relativistic approximation)

2. A. V. Gramolin et al., J. Phys. G Nucl. Part. Phys. 41(2014)115001

3. O. Tomalak, Few Body Syst. **59**, no. 5, 87 (2018)

Systematic Uncertainties

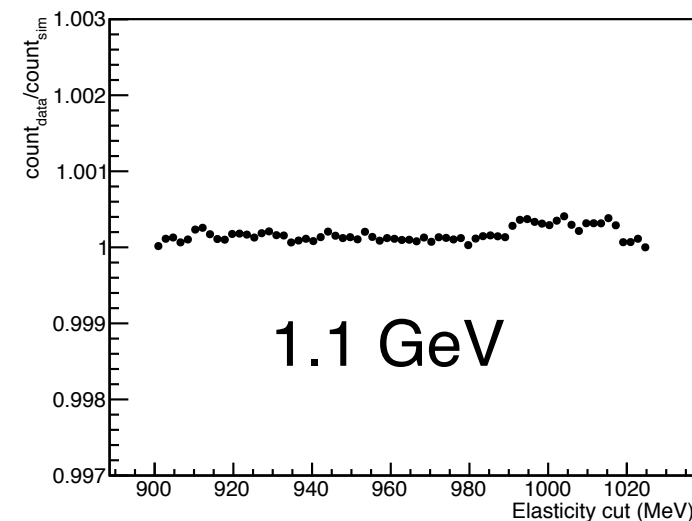
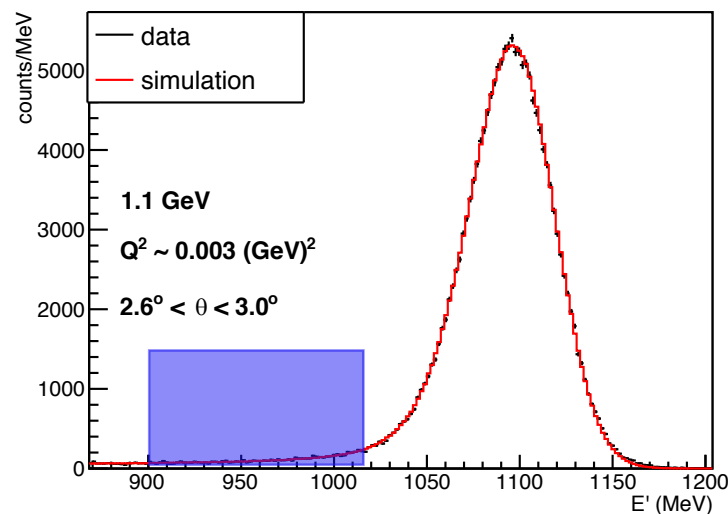
- For PRad, systematic uncertainties may come from:
 1. Event selection (elasticity cuts, co-planarity cuts...)
 2. Radiative correction
 3. Detector efficiencies (GEM and HyCal)
 4. Beam-line background (Halo hitting collimator, residual gas...)
 5. HyCal energy calibration
 6. Detector position
 7. Beam energy
 8. Inelastic ep contribution
 9. Assumed magnetic form factors during the G_E extraction
 10. ...

Systematic Uncertainties

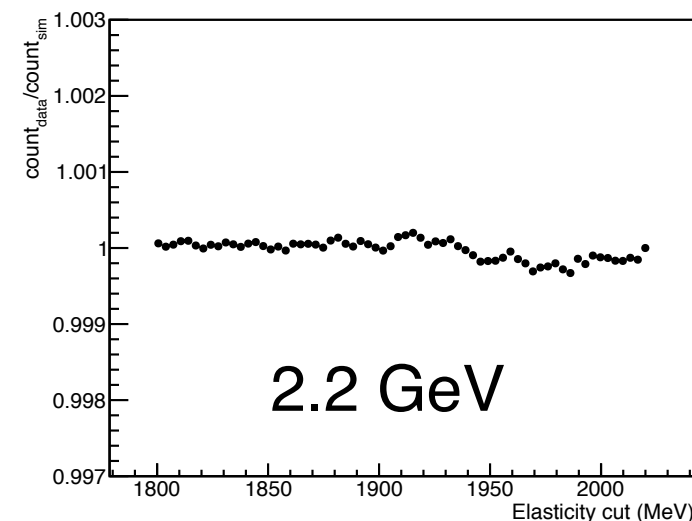
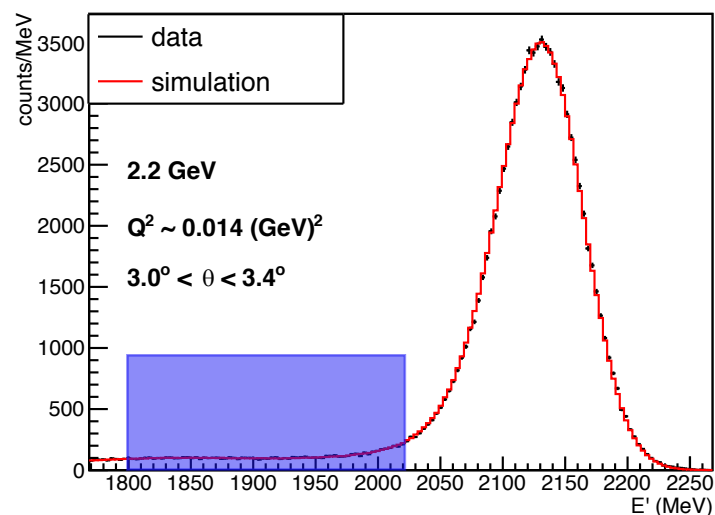
(Example of Event Selection)

- Changing elasticity cut at the radiative tail and obtain different sets of cross section results
- Sensitivity on cross section: typically bounded by $\pm 0.15\%$
- Mostly due to non-uniformity of HyCal modules

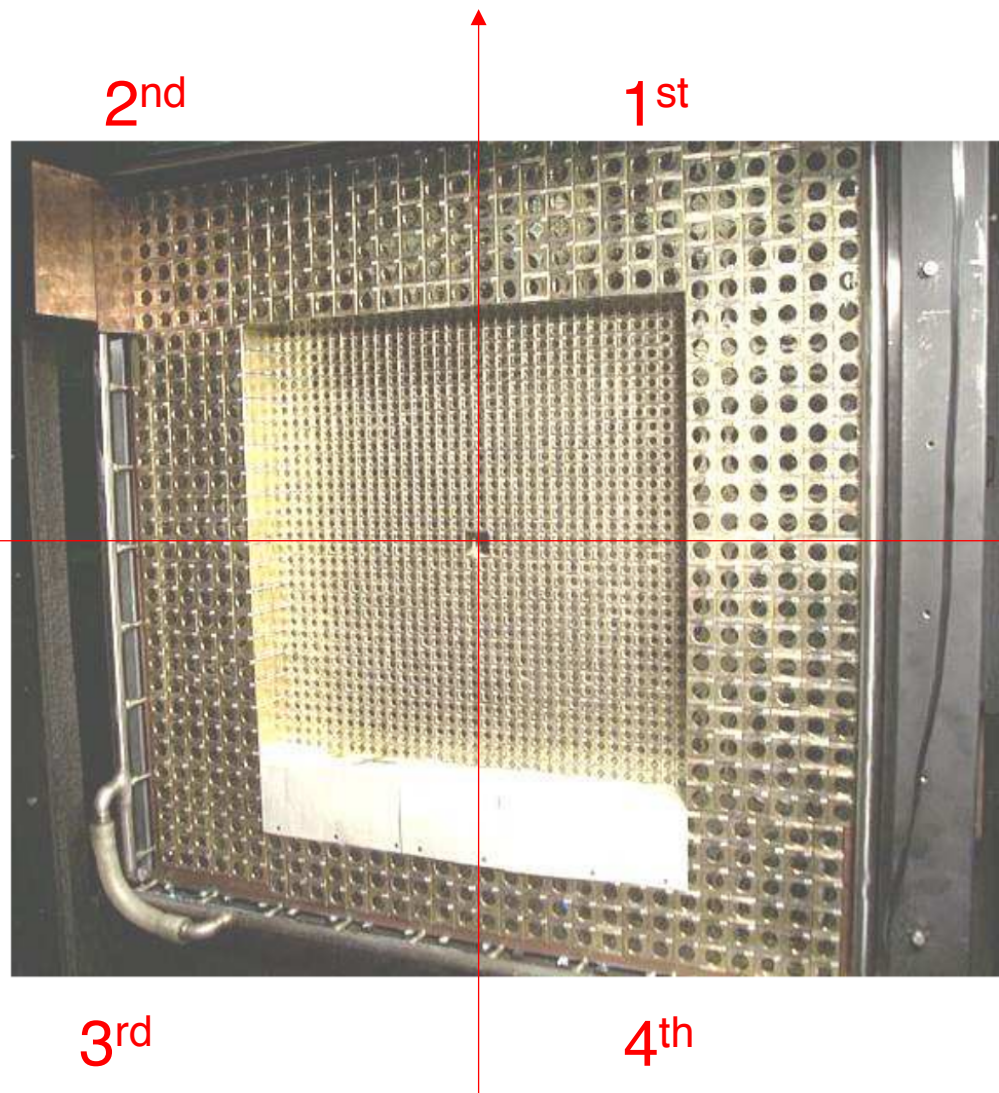
Data vs. simulation



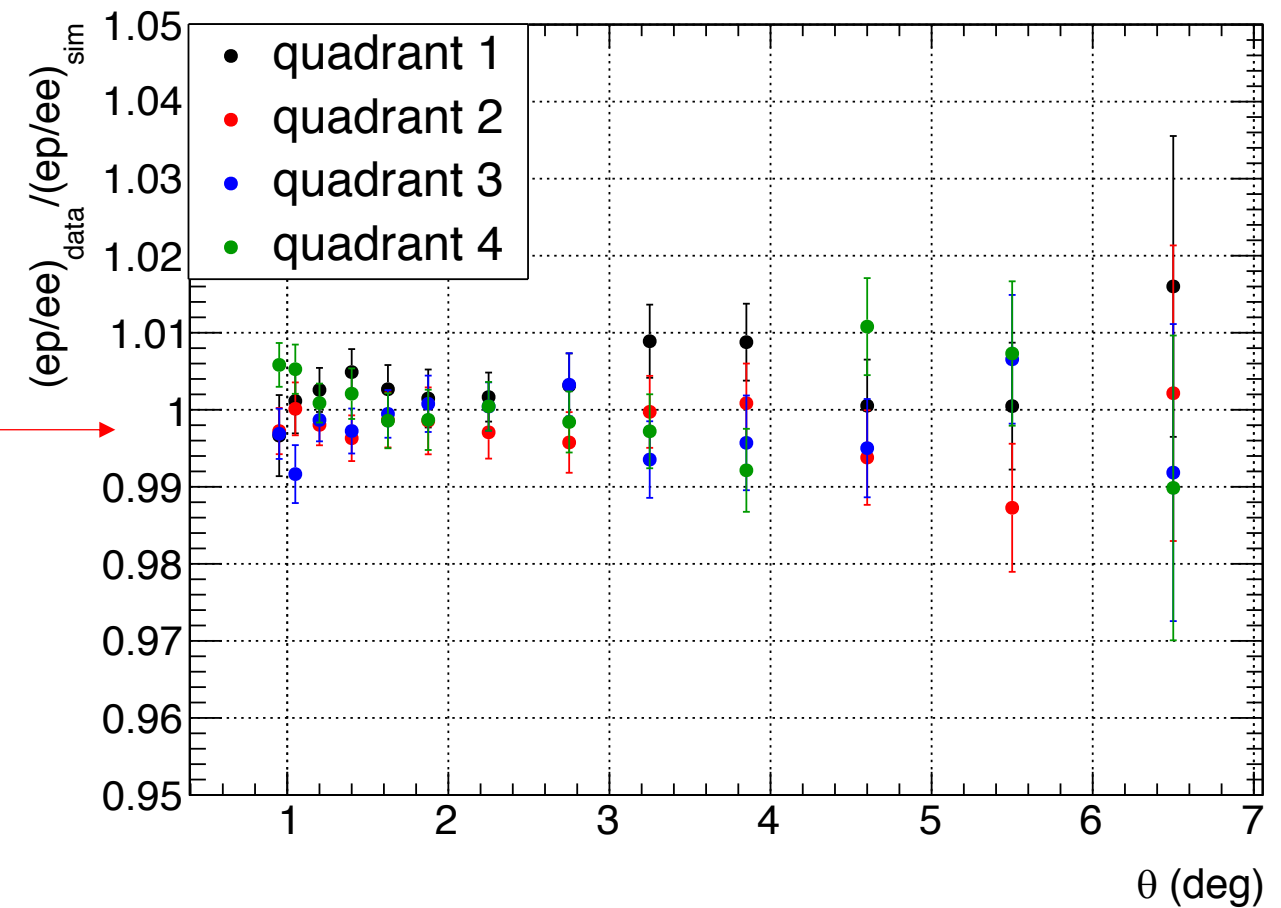
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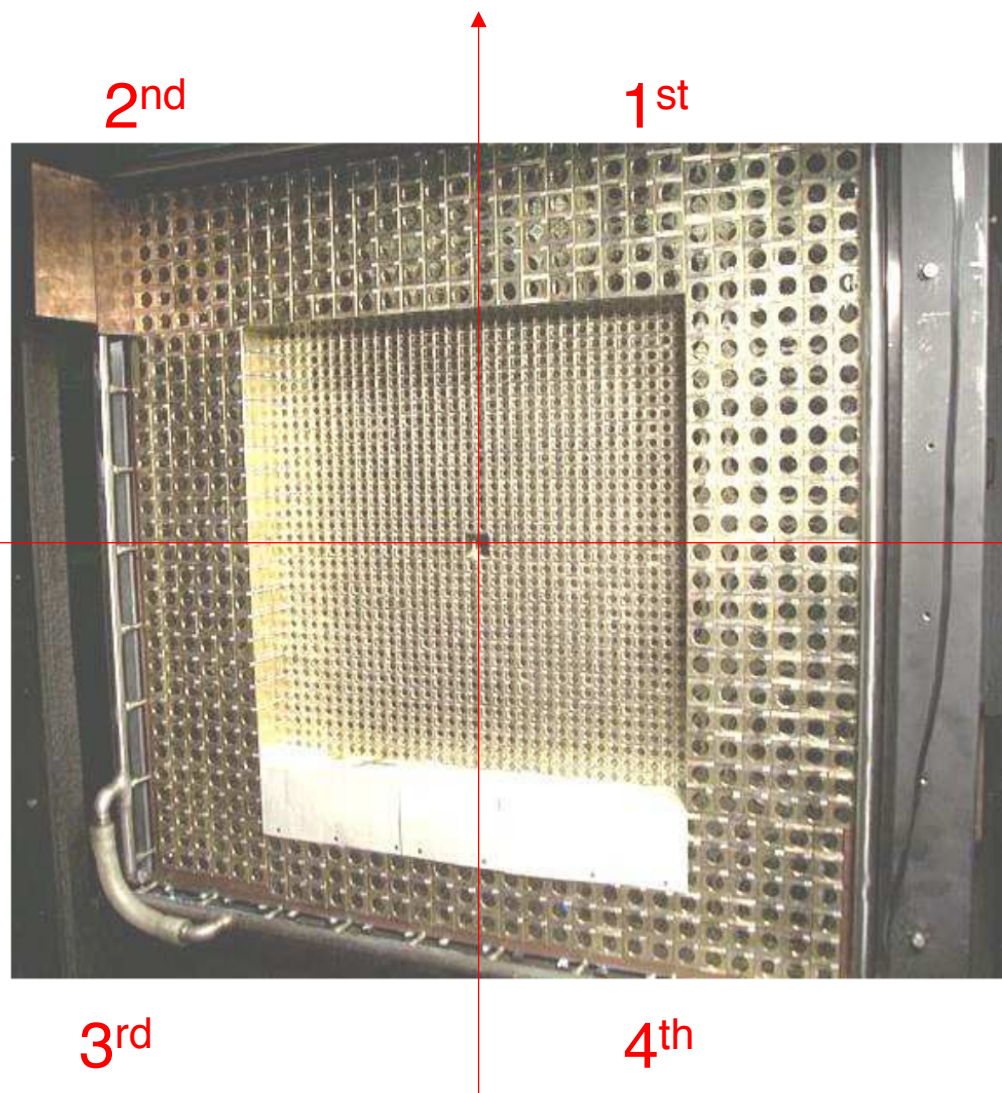
Checking Systematics – Sector Dependence



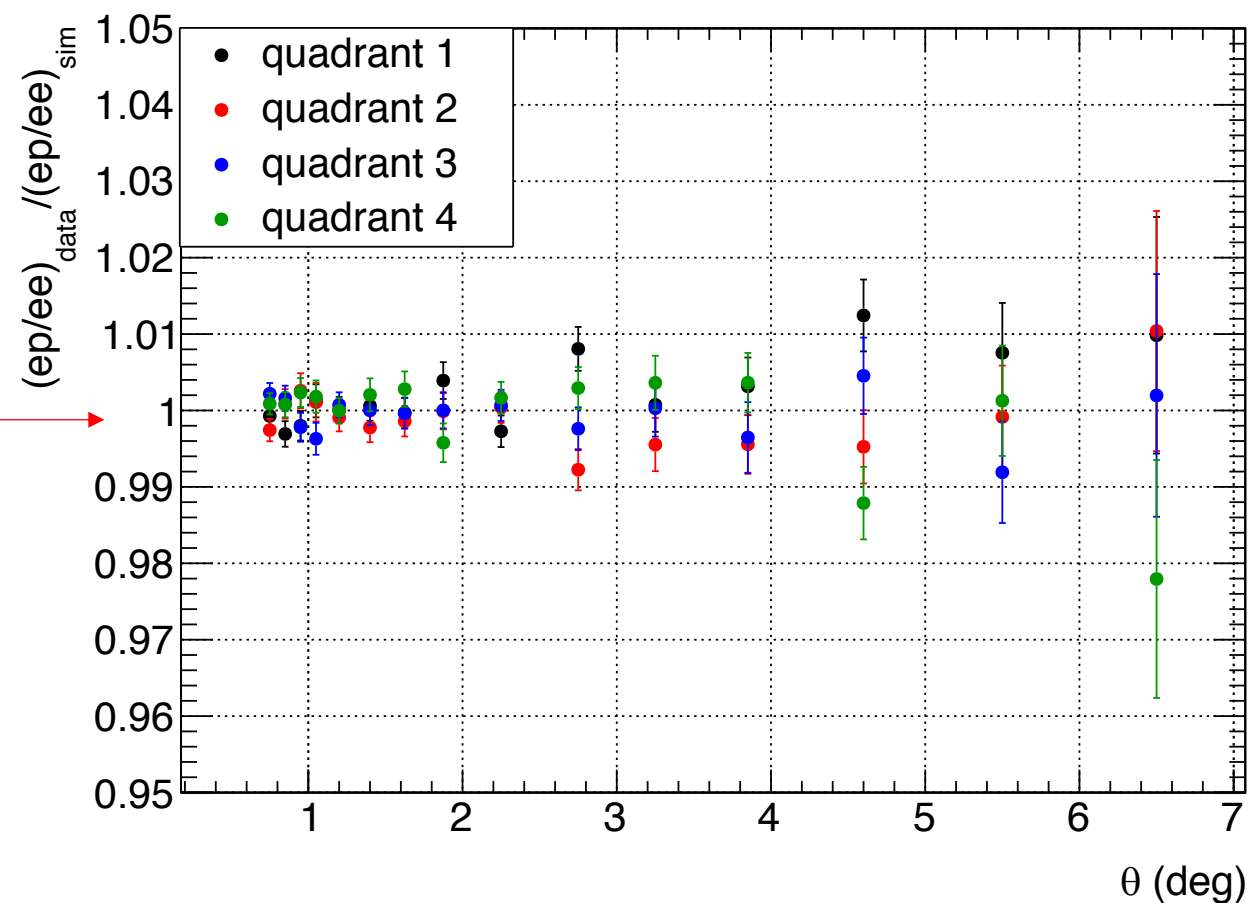
1.1 GeV data



Checking Systematics – Sector Dependence

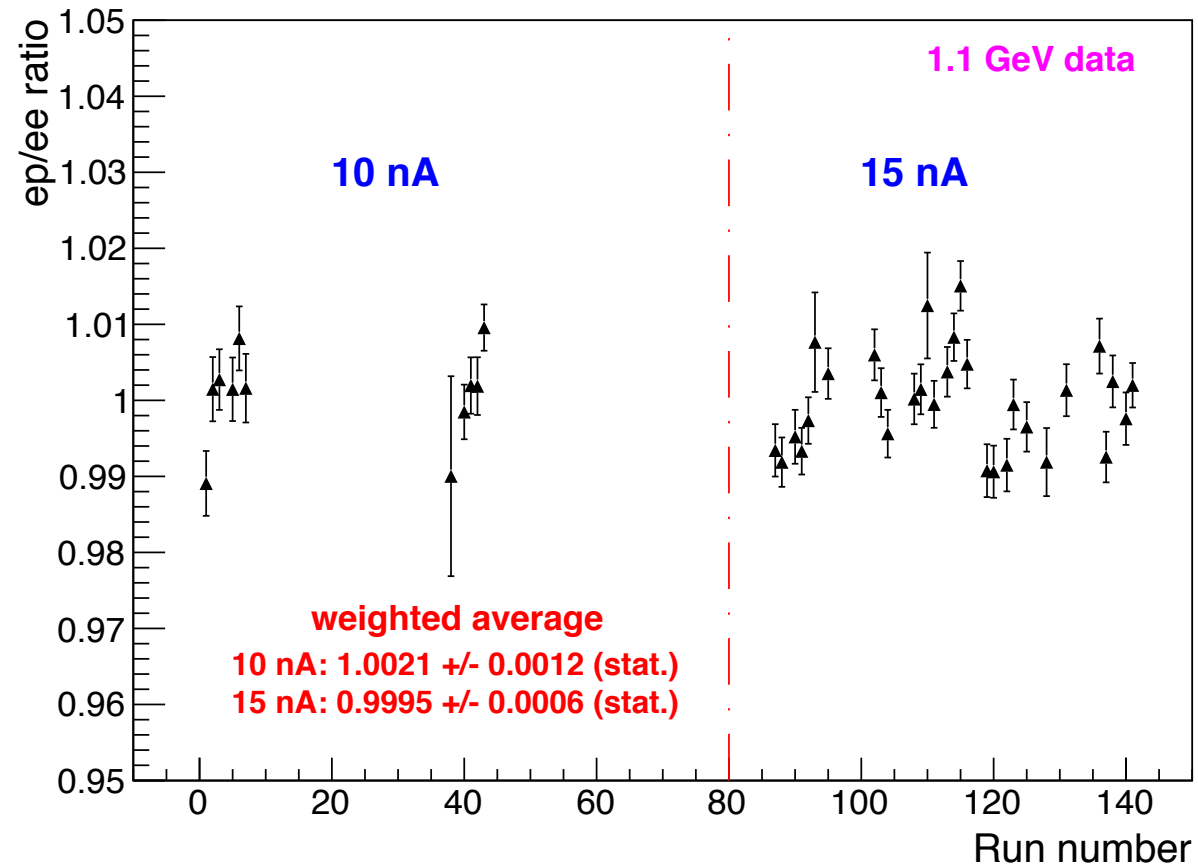


2.2 GeV data

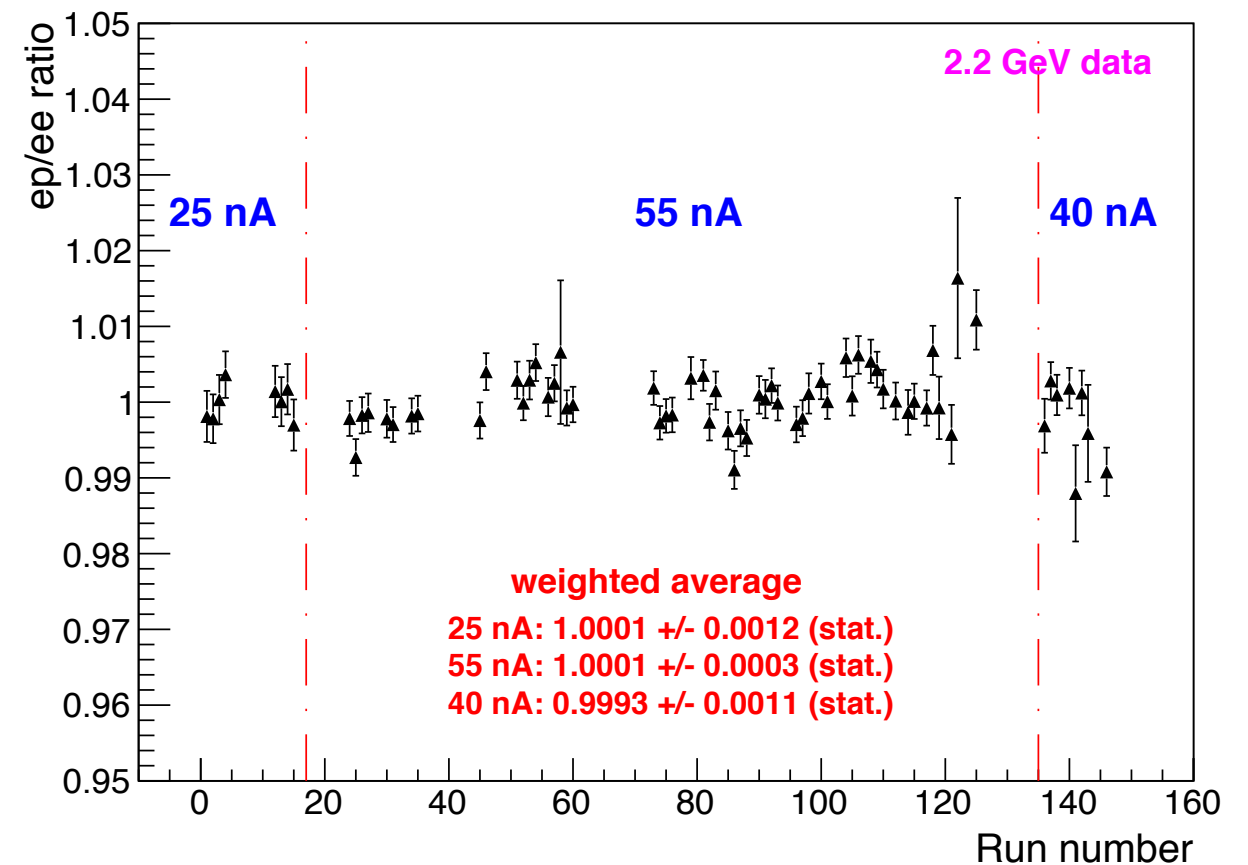


Checking Systematics – Stability vs. Run

Normalized ep/ee ratio ($6.2 \times 10^{-4} < Q^2 < 4.5 \times 10^{-3} \text{ GeV}^2$)

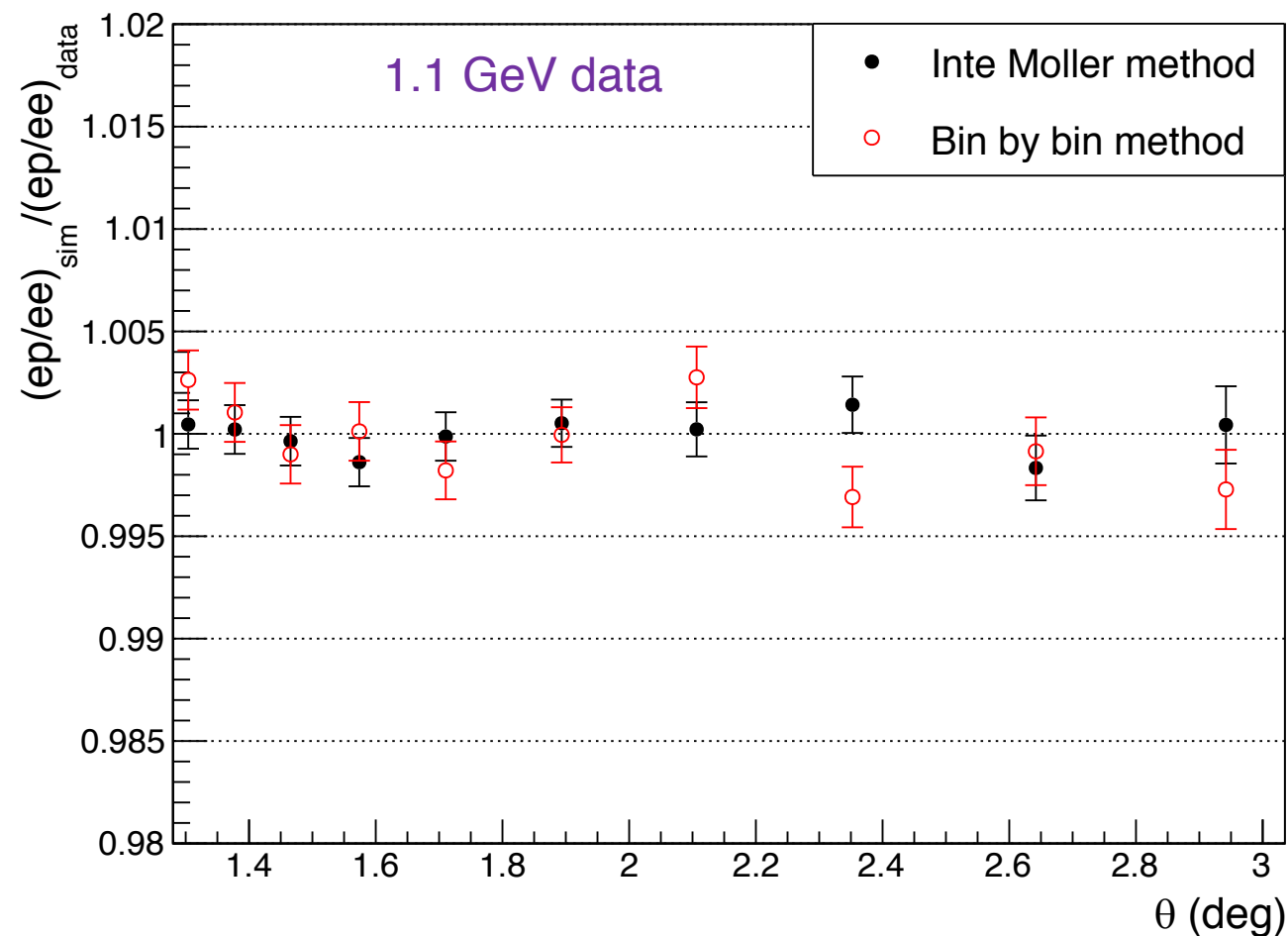


Normalized ep/ee ratio ($1.1 \times 10^{-3} < Q^2 < 5.6 \times 10^{-3} \text{ GeV}^2$)



Checking Systematics – Different methods of Forming ep/ee ratio

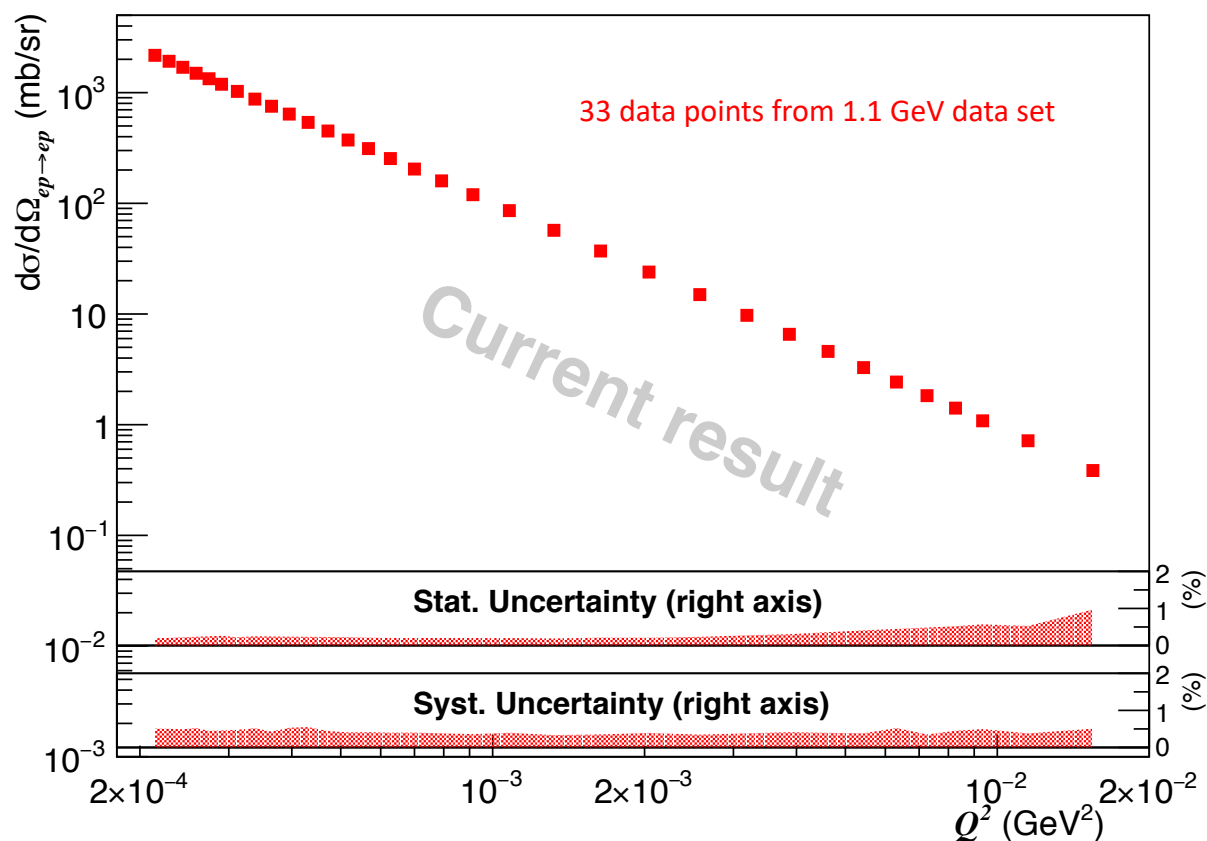
- **Method 1: bin by bin method** – taking ep/ee counts from the same angle bin
 - Cancellation of GEM efficiency
 - May introduce Q^2 dependent uncertainty from Moller
 - Limited converge due to double arm Moller acceptance
- **Method 2: integrated Moller method** – integrate Moller in a fixed angle range and use it as common normalization for all angle bins
 - Moller uncertainty only affects normalization
 - Need to correct for GEM efficiency
- Luminosity cancelled in both methods



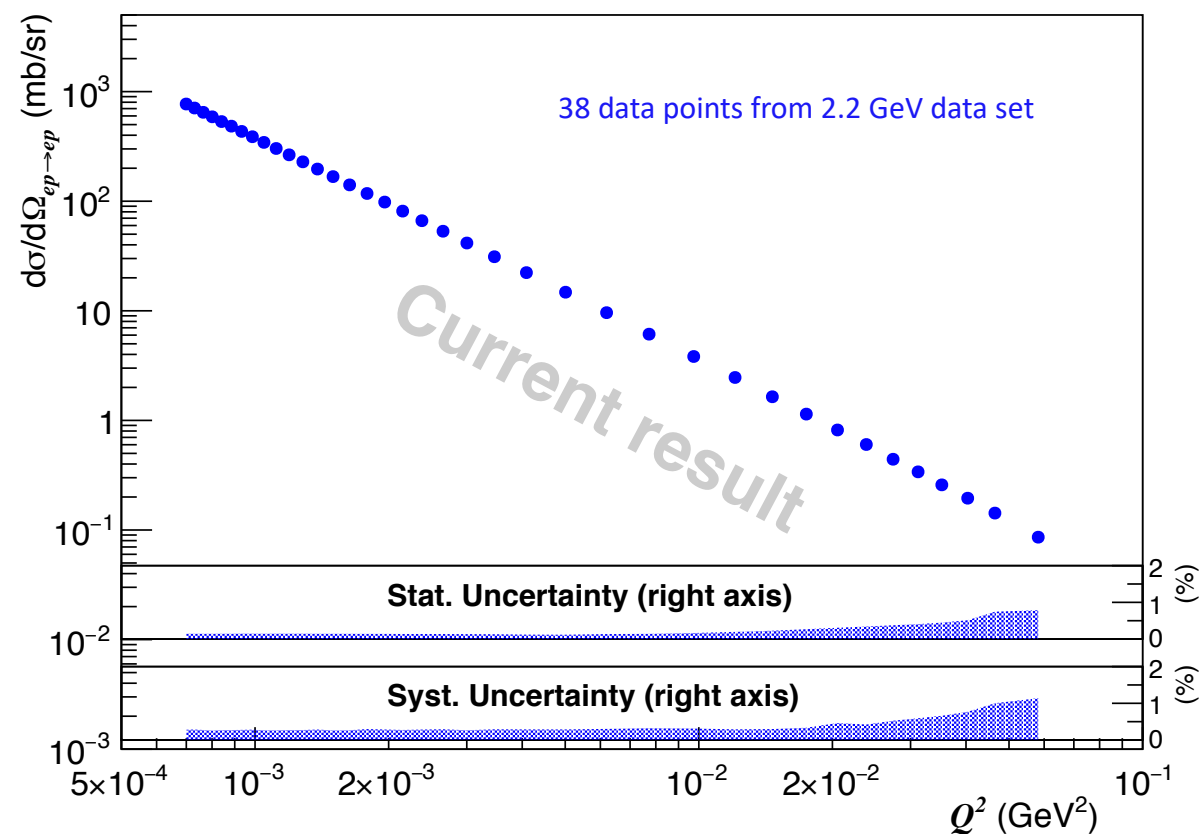
Extracted Differential Cross Sections (Current)

- Extracted differential cross section v.s. Q^2 , with 2.2 and 1.1 GeV data (current)
- Statistical uncertainties at current stage: $\sim 0.15\%$ for 2GeV, $\sim 0.2\%$ for 1GeV per point
- Systematic uncertainties at current stage: $0.3\% \sim 1.1\%$ for 2GeV, $0.3\% \sim 0.5\%$ for 1GeV

ep elastic scattering cross section (1.1 GeV)

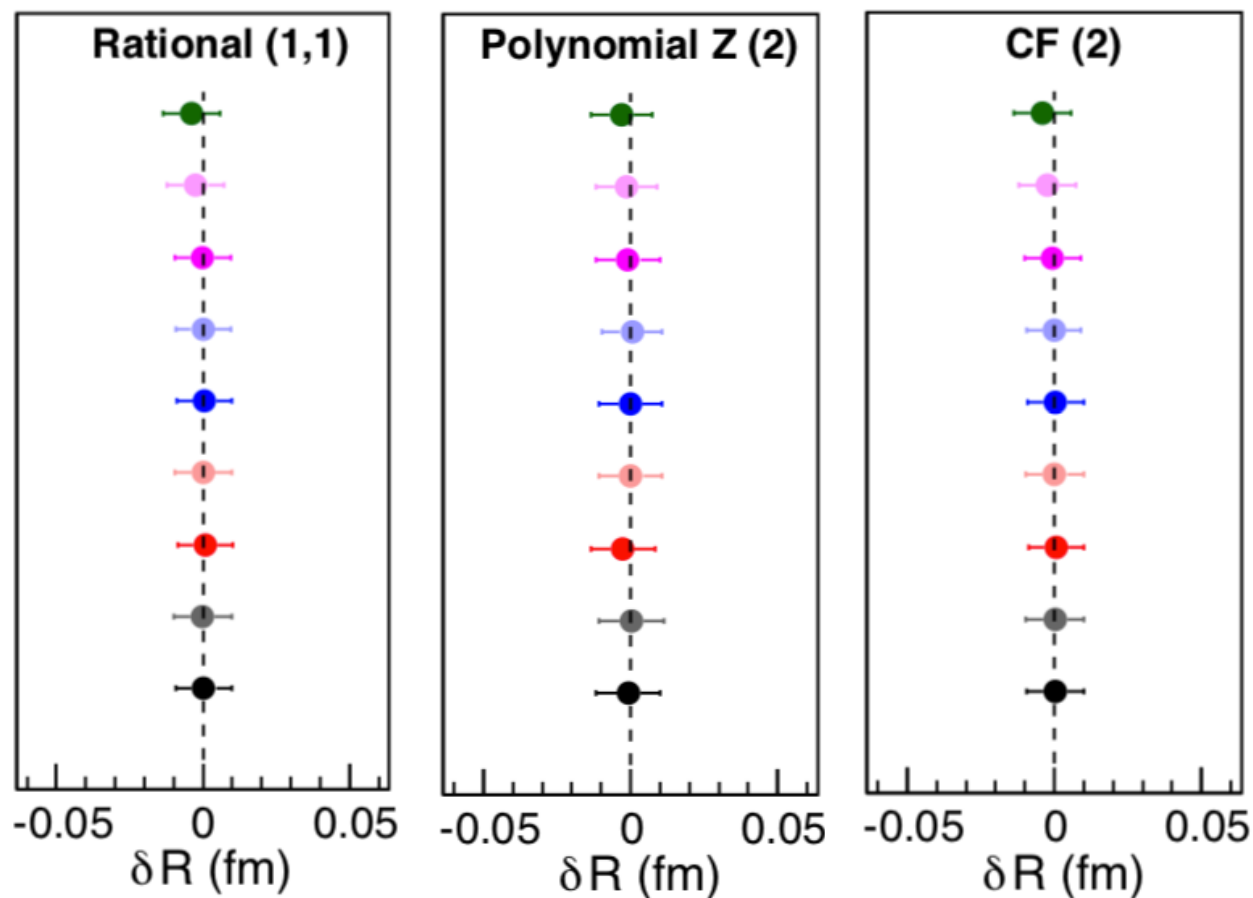


ep elastic scattering cross section (2.2 GeV)



Searching the Robust fitters

- Various fitters tested with a wide range of G_E parameterizations, using PRad kinematic range and uncertainties:
 - X. Yan *et al.* Phys. Rev. C98, 025204 (2018)
- Rational (1,1), 2nd order z transformation and 2nd order continuous fraction are identified as robust fitters with also reasonable uncertainties



Ye-2018

Bernauer-2014

Alarcón-2017

Arrington-2007

Arrington-2004

Kelly-2004

Gaussian

Monopole

Dipole

Rational (1,1)

$$p_0 \frac{1 + p_1 Q^2}{1 + p_2 Q^2}$$

2nd order z transformation

$$p_0 (1 + p_1 z + p_2 z^2)$$

$$z = \frac{\sqrt{T_c + Q^2} - \sqrt{T_c - T_0}}{\sqrt{T_c + Q^2} + \sqrt{T_c - T_0}}$$

2nd order continuous fraction

$$p_0 \frac{1}{1 + \frac{p_1 Q^2}{1 + p_2 Q^2}}$$

PRad Collaboration Institutional List

- Currently 17 collaborating universities and institutions:

Jefferson Laboratory
NC A&T State University
Duke University
Idaho State University
Mississippi State University
Norfolk State University
University of Virginia
Argonne National Laboratory
University of North Carolina at Wilmington
University of Kentucky
Hampton University
College of William & Mary
Tsinghua University, China
Old Dominion University
ITEP, Moscow, Russia
Budker Institute of Nuclear Physics , Russia
MIT

- Graduate students:

Chao Peng (Duke)
Weizhi Xiong (Duke)
Li Ye (MSU)
Xinzhan Bai (UVa)
Abhisek Karki (MSU)

- Postdocs:

Chao Gu (Duke)
Xuefei Yan (Duke)
Mehdi Meziane (Duke)
Zhihong Ye (Duke)
Maxime Lavidain (NC A&T)
Krishna Adhikari (MSU)
Rupesh Silwal (MIT)

Summary

- After almost 10 years, the proton radius puzzle still unresolved
- The PRad collaboration carried out a first electron scattering experiment using a non-magnetic spectrometer approach – calorimeter and GEMs
 1. Covers **two orders** of magnitude in low Q^2 with the **same detector setting**
 2. Unprecedented low Q^2 data set (**$\sim 2 \times 10^{-4} \text{ GeV}^2$**) has been collected in e - p elastic scattering experiment
 3. Simultaneous measurements of ep and ee scattering to reduce systematics
 4. Novel use of a window-less cryogenically cooled hydrogen gas target

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